# Portfolio Theory w/ Settlement Frictions

by Javier Bianchi (FRB-Min) Saki Bigio (UCLA & NBER) on UCLA Workshop – July 2025

## Big Picture & Agenda

- Recent macro-finance: convenience yields
  - Treasuries, Repo, FX markets
- Convenience yields: premia unexplained by cash flow (risk)
- Agenda: links convenience yields to
  - Supply of settlement instruments (e.g., reserves, debt)
  - OTC market frictions
- Why Microfoundations?
  - 1. Testable micro predictions: volumes, rates, dispersion
  - 2. Policy-relevance: non-invariant to policy
  - 3. Interaction with risk-aversion

#### Preview of Mechanism

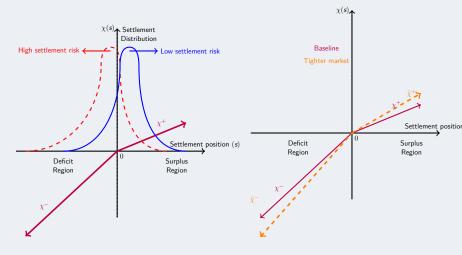
- Investors with portfolios
- Cash-flows: **settlement shocks** (e.g., deposits, margin calls)
- Cash deficit: borrow in OTC market or face penalty rate
- Kinked convenience-yield function of cash position s:

$$\chi(\mathbf{s}) = \begin{cases} \chi^- \mathbf{s} & \text{if } \mathbf{s} < 0 \\ \chi^+ \mathbf{s} & \text{if } \mathbf{s} \ge 0 \end{cases}$$

- $\chi^-$  and  $\chi^+$  depend on:
  - market tightness  $\theta = S^-/S^+$  matching technology  $G, \bar{\lambda}$

  - bargaining power  $\eta$

#### Preview of Mechanism



(a) Convenience yields

(b) Tightness and convenience yields

#### What we do here

- Afonso-Lagos ECMA '15
  - OTC market for Fed Funds
- Bianchi-Bigio ECMA '22
  - analytic OTC model (Leontief matching)
  - embedded in GE
  - study monetary policy
- Novelty here:
  - arbitrary assets (not only deposits)
  - generalize matching function
  - comparative statics convenience-yields
- Input in Recent work:
  - applications to exchange rates
  - optimal size of central-bank balance sheets

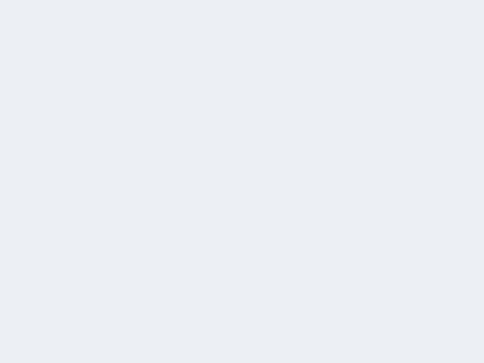
#### Contributions here

#### 1. Portfolio Theory:

integrate OTC friction into rich asset choice/asset pricing framework

#### 2. OTC Market:

- formulas for trading rates & volumes for various cases
- focus identification w/ micro data
- 3. **Asset Pricing:** theory of convenience yields
  - details how convenience yields vary with market structure/quantities
- 4. Normative: Identifies inefficient portfolio choices: guide regulation



#### Model Environment

- Infinite-horizon, unit mass of investors
- Asset return risk and settlement risk
- Trade in settlement instrument frictional OTC market
- Failure to borrow: penalty rate

### Timeline: Two-Stages

#### 1. Portfolio Stage

• Choose holdings in assets  $\{a^i\}$ ,  $i \in \mathcal{I}$ , and cash m

#### 2. Balancing Stage

- Idiosyncratic cash-flow shocks  $\omega^i$
- Settlement in cash m
- OTC trade: Borrow (or lend) from other investors f and or amount w at penalty (lender of last resort)

#### Asset Structure

- Assets  $\{a^i\}_{i\in\mathbb{I}}$  differ in payoffs and liquidity properties
- Special asset *m*: riskless
- Constraint: must end each period  $m \ge 0$

## Cash-Flow Shocks and Surplus Definition

• At balancing stage, shocks  $\omega^i$  perturb asset positions:

$$a_{t+1}^i = \tilde{a}_{t+1}^i (1 + \omega_t^i)$$

• Settlement surplus:

$$s = \tilde{m}_{t+1} + \sum_{i} \frac{R'_{t+1}}{R^{m}_{t+1}} \omega^{i}_{t} \tilde{a}^{i}_{t+1}$$

- s < 0: deficit  $\rightarrow$  needs funding
- s > 0: surplus  $\rightarrow$  can lend or hold
- Examples: deposits, credit lines, margin calls, insurance claims, refinancing options, etc.

#### OTC trade

- Deficits funded via:
  - OTC market borrowing (probability  $\Psi_t^-$ )
  - At penalty (probability  $1-\Psi_t^-$ )
- ullet Surplus lent in OTC market (probability  $\Psi_t^+$ )
- Final cash holdings:

$$m_{t+1} = s + f_{t+1} + w_{t+1} \ge 0$$

#### Convenience Yields from Settlement Risk

• Total return includes direct asset return + settlement yield:

$$e_{t+1} = \sum_{i} R_{t+1}^{i} \tilde{a}_{t+1}^{i} + R_{t+1}^{m} \tilde{m}_{t+1} + \chi_{t+1}(s)$$

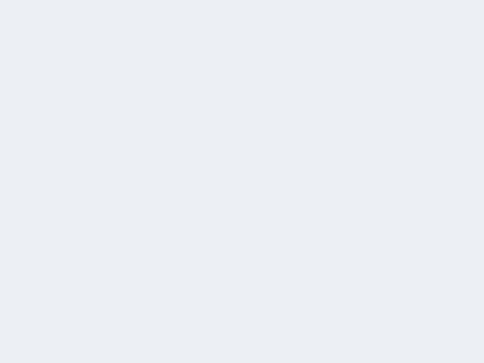
• Kinked convenience-yield function:

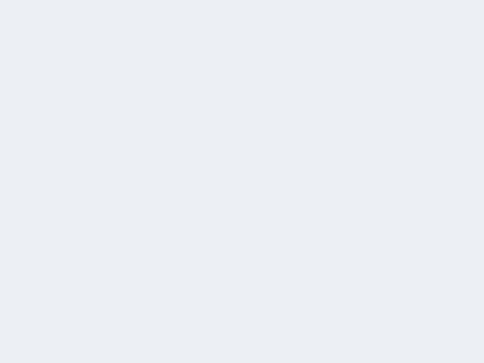
$$\chi_t(s) = \begin{cases} \chi_t^- s & \text{if } s < 0\\ \chi_t^+ s & \text{if } s \ge 0 \end{cases}$$

Slopes depend on equilibrium OTC outcomes:

$$\chi_{t}^{-} = (\bar{R}_{t}^{f} - R_{t}^{m})\Psi_{t}^{-} + (R_{t}^{w} - R_{t}^{m})(1 - \Psi_{t}^{-})$$
 
$$\chi_{t}^{+} = (\bar{R}_{t}^{f} - R_{t}^{m})\Psi_{t}^{+}$$

- $\bar{R}_{t}^{f}$ : average OTC rate,  $R_{t}^{w}$ : penalty rate
- Notation: r<sup>x</sup> lower case for net rate





## OTC Market Equilibrium: Matching Dynamics

- Afonso-Lagos block
- Define initial aggregate surplus and deficit:

$$S_0^+ = S^+, \quad S_0^- = S^-$$

- $n \in \mathcal{N} \equiv \{1, 2, ..., N\}$  rounds
- Round *n*, number of matches:

$$m_n = \lambda_N G(S_n^+, S_n^-)$$

• Surplus and deficit evolve as:

$$S_{n+1}^+ = S_n^+ - m_n, \quad S_{n+1}^- = S_n^- - m_n$$

## Assumptions on Matching Function

#### Assume:

- No disposal: G(0,1) = G(1,0) = 0
- Constant returns to scale: Homogeneous degree one
- **Symmetry:** G(a, b) = G(b, a)
- Weak exhaustion:  $\lambda_N G(S_n^+, S_n^-) \leq \min\{S_n^+, S_n^-\}$
- Monotonicity:  $G_a$ ,  $G_b \ge 0$
- Weak concavity:  $G_{aa}$ ,  $G_{bb} \leq 0$

Note: different in other models that assume IRS.

## Tightness and Matching Probabilities

• Define market tightness:

$$\theta_n = \frac{S_n^-}{S_n^+}$$

Matching probabilities for round n:

$$\psi_n^+ = \lambda_N G(1, \theta_{n-1}), \quad \psi_n^- = \lambda_N G(\theta_{n-1}^{-1}, 1)$$

- Convention:  $\psi_{N+1}^{\pm} = 0$
- Equilibrium:  $\psi_n^+ = \theta_{n-1}\psi_n^-$

## Nash Bargaining in OTC Market

- Trick: investor delegates  $\Delta$  trade sizes to traders
- In round *n*, traders bargain over  $r_n^f = R_n^f 1$ :

$$r_n^f(\Delta) = \arg\max_{r_n} \left[\mathcal{S}_n^-(\Delta)\right]^{\eta} \left[\mathcal{S}_n^+(\Delta)\right]^{1-\eta}$$

Surplus from trade (for deficit and surplus traders):

$$\mathcal{S}_n^- = V(\mathcal{E}^j(\Delta) - (r_n^f - r^m)\Delta) - J_U^-(n; \Delta)$$

$$\mathcal{S}_n^+ = V(\mathcal{E}^j(\Delta) + (r_n^f - r^m)\Delta) - J_U^+(n;\Delta)$$

•  $\mathcal{E}^{j}(\Delta)$ : "estimate" of investor equity, ex own trade

#### Limit Result: $\Delta \to 0$

- Infinitesimal trade: Shi '97 or Atkeson, Eisfeldt, Weill '15
- As trade size  $\Delta \to 0$ , trader's effect on equity becomes marginal:

$$V(e + \Delta x) \approx V(e) + V'(e) \cdot \Delta x$$

Nash becomes:

$$\lim_{\Delta \downarrow 0} \left\{ \max_{r_n^f} \left[ \mathcal{S}_n^-(\Delta) / \Delta \right]^{\eta} \left[ \mathcal{S}_n^+(\Delta) / \Delta \right]^{1-\eta} \right\} = V \left( \mathcal{E}^j \right)^{\eta} V \left( \mathcal{E}^k \right)^{1-\eta} \max_{r_n^f} \left[ \chi_{n+1}^- - (r_n - r^m) \right]^{\eta} \left[ (r_n - r^m) - \chi_{n+1}^+ \right]^{1-\eta}.$$

ullet Result: marginal utility V' factors out: outcome depends only on round n

## Result: Infinitesimal Trade Bargaining

#### Dynamic Bargaining Problem

$$\max_{r_n^f \in \{r^m + \chi_n^+, r^m + \chi_n^-\}} \left( \chi_n^- - (r_n^f - r^m) \right)^{\eta} \left( (r_n^f - r^m) - \chi_n^+ \right)^{1-\eta}$$

Solution:

$$r_n^f = r^m + (1 - \eta)\chi_n^- + \eta\chi_n^+$$

### Difference Equation: $\chi_n^+$ and $\chi_n^-$

$$\chi_n^+ = (r_{n+1}^f - r^m)\psi_{n+1}^+ + \chi_{n+1}^+ (1 - \psi_{n+1}^+)$$

$$\chi_n^- = (r_{n+1}^f - r^m)\psi_{n+1}^- + \chi_{n+1}^- (1 - \psi_{n+1}^-)$$

given 
$$\chi_{\mathit{N}+1}^+,\chi_{\mathit{N}+1}^-=0,=\mathit{r^w}-\mathit{r^m}$$
 ,  $\{\psi_\mathit{n}^+,\psi_\mathit{n}^-\}$ 

## Consistency

#### Proposition

Matching probabilities:

$$\Psi^{-} = 1 - \prod_{n=1}^{N} (1 - \psi_{n}^{-}), \quad \Psi^{+} = 1 - \prod_{n=1}^{N} (1 - \psi_{n}^{+})$$

Convenience yield slopes:

$$\chi^{-} = \Psi^{-}(\bar{r}^{f} - r^{m}) + (1 - \Psi^{-})(r^{w} - r^{m}) = \chi_{0}^{-}$$
  
$$\chi^{+} = \Psi^{+}(\bar{r}^{f} - r^{m}) = \chi_{0}^{+}$$

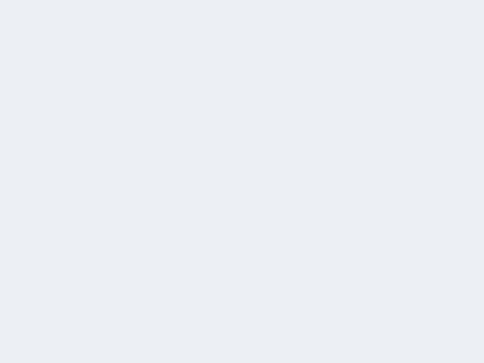
Rates:  $\bar{r}^f$  is average rate across rounds weighted by volume

## Algorithm: Convenience Yields

- 1. Forward iteration: compute  $\{\psi_n^+,\psi_n^-\}$  using  $\theta_0$
- 2. Backward iteration: compute  $\{\chi_n^+, \chi_n^-\}$  using terminal values
- 3. Then:  $r_n^f = r^m + (1 \eta)\chi_n^- + \eta\chi_n^+$

#### Arrive at:

•  $\chi_t^- = \chi_0^-$ ,  $\chi_t^+ = \chi_0^+$  (slopes of liquidity yield)



#### Continuous-Time Limit

Limit  $N \to \infty$ ,  $\lambda_N \to 0$  with  $N\lambda_N \to \bar{\lambda}$ 

• Trading rounds indexed by  $\tau \in [0, 1]$ .

#### ODE for market tightness

$$\dot{\theta}_{\tau} = \bar{\lambda}\theta_{\tau} \left[ \gamma(1/\theta_{\tau}) - \gamma(\theta_{\tau}) \right], \quad \gamma(\theta) = G(1,\theta)$$

Matching intensities:

$$\psi_{\tau}^{+} = \bar{\lambda}\gamma(\theta_{\tau}), \quad \psi_{\tau}^{-} = \bar{\lambda}\gamma(1/\theta_{\tau})$$

### Convenience Yields - Cont. Time Solution

#### Proposition

Given path of:  $\{\psi^+, \psi^-\}$ ,

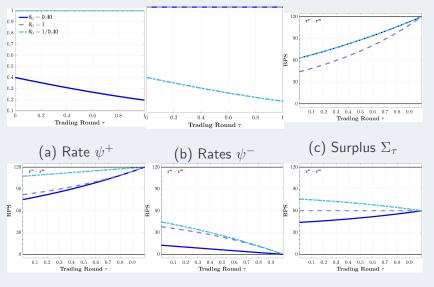
$$\chi_{\tau}^{+} = (r^{w} - r^{m}) \int_{\tau}^{1} (1 - \eta) \psi_{y}^{+} e^{-\int_{y}^{1} ((1 - \eta) \psi_{x}^{+} + \eta \psi_{x}^{-}) dx} dy$$

$$\chi_{\tau}^{-} = (r^{w} - r^{m}) \left[ 1 - \int_{\tau}^{1} \eta \psi_{y}^{-} e^{-\int_{y}^{1} ((1 - \eta) \psi_{x}^{+} + \eta \psi_{x}^{-}) dx} dy \right]$$

Bargaining Outcome still:

$$r_{\tau}^{f} = r^{m} + (1 - \eta)\chi_{\tau}^{-} + \eta\chi_{\tau}^{+}$$

## Example: Leontief Matching $G(a, b) = \min\{a, b\}$



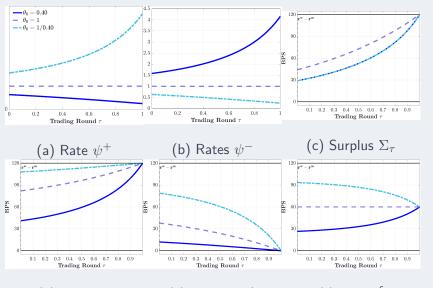
(d) Cost  $\chi^-$ 

(e) Benefit  $\chi^+$ 

(f) Rate  $r_{\tau}^f$ 

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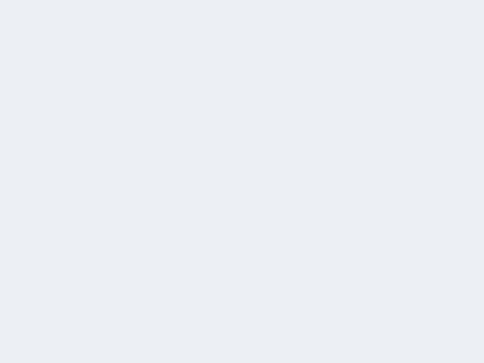
## Example: Cobb-Douglas $G(a, b) = \sqrt{a \cdot b}$



(d) Cost  $\chi^-$ 

(e) Benefit  $\chi^+$ 

(f) Rate  $r_{\tau}^f$ 



## Four Properties

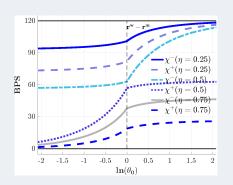
- Balanced market balanced market  $(\theta_0 = 1)$ , stays balanced.
  - Exogenous trading probs.
- Time Dilation Dynamics from any point in session
  - Reset to full session, scale matching efficiency  $\bar{\lambda}$  remaining time
- **Symmetry** Swapping deficit and surplus sides  $(\theta \leftrightarrow \theta^{-1}, \eta \leftrightarrow 1 \eta)$ 
  - mirrors yields around  $r^w r^m$
- Bargaining Power Borrower power  $(\eta \uparrow)$  lowers rates and yield coefficients
  - full borrower power  $\Rightarrow \bar{r}^f = r^m$ , viceversa

### **Efficiency Limits**

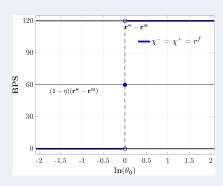
The OTC market equilibrium satisfies:

- Walrasian Limit  $(\bar{\lambda} \to \infty)$ 
  - $\theta > 1$ :  $\Psi^+ = 1$ ,  $\Psi^- = 1/\theta$ ,  $\chi^+ = \chi^- = r^w r^m$
  - $\theta < 1$ :  $\Psi^+ = \theta$ ,  $\Psi^- = 1$ ,  $\chi^+ = \chi^- = 0$
  - $\theta = 1$ :  $\Psi^+ = \Psi^- = 1$ ,  $\chi^+ = \chi^- = (1 \eta)(r^w r^m)$
- Static Limit ( $\bar{\lambda} \to 0$ )
  - $\Psi^+ = \Psi^- = 0$ ,  $\chi^+ = 0$ ,  $\chi^- = r^w r^m$
  - $\bar{r}^f = r^m + (1 \eta)(r^w r^m)$
- High efficiency leads to Walrasian outcomes
- · Low efficiency: bargaining as in one round

## Symmetry and Walrasian Limit



(a) Symmetry Property



(b) Walrasian Limit

## Market Tightness

- $\chi^+,\chi^-,\bar{r}^f$  increasing in tightness  $\theta$
- What about extrema?

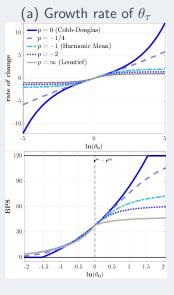
#### Proposition (Extrema of Market Tightness)

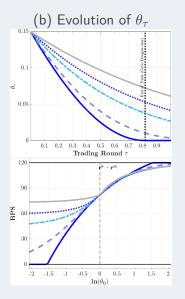
- $\theta \to 0$ :  $\chi^+ \to 0$ ,  $\chi^- \to (r^w r^m)e^{-\bar{\lambda}\bar{\gamma}\eta}$
- $\theta \rightarrow \infty$ :  $\chi^- \rightarrow r^w r^m$ ,  $\chi^+ \rightarrow (r^w r^m)(1 e^{-(1-\eta)\bar{\lambda}\bar{\gamma}})$
- Key: boundedness  $\bar{\gamma} = \lim_{\theta \to 0} \gamma(\theta^{-1})$
- $\bar{\gamma}$  finite: yields/rates stay positive even as  $\theta \to 0$

## The CES Matching Class

- CES:  $G(a,b) = (a^p + b^p)^{1/p}, p \le 0$
- Within CES: Cobb-Douglas (p = 0) is knife-edge
  - Only matching function  $\theta_{\tau}$  can reach 0 in finite time
  - We care because Cobb-Douglas allows zero convenience yields

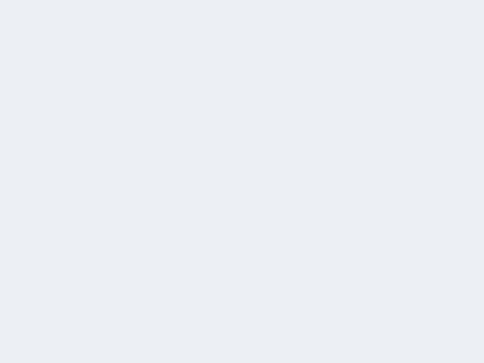
## The CES Matching Class





(c)  $\chi^+$ 

(d)  $\chi^-$ 



# Tightness Formula: Cobb-Douglas vs. Leontief

Market Tightness $\theta( au)$		
Feature	Cobb-Douglas $(p = 0)$	Leontief $(p = -\infty)$
$\theta( au)$	$\left(\frac{(1+\sqrt{\theta_0})e^{-\bar{\lambda}\tau}-(1-\sqrt{\theta_0})}{(1+\sqrt{\theta_0})e^{-\bar{\lambda}\tau}+(1-\sqrt{\theta_0})}\right)^2$	$\begin{cases} 1 + (\theta_0 - 1)e^{\bar{\lambda}\tau}, & \theta_0 > 1\\ \theta_0/(\theta_0 + (1 - \theta_0)e^{\bar{\lambda}\tau}), & \theta_0 < 1 \end{cases}$
Stop T	$\min \left\{ \frac{1}{\lambda} \log \left( \left  \frac{1+\sqrt{ heta_0}}{1-\sqrt{ heta_0}} \right  \right), 1 \right\}$	∞
Ψ+	$1 - e^{-\bar{\lambda}T} \left( \frac{(1+\sqrt{\theta_0}) + (1-\sqrt{\theta_0})e^{\bar{\lambda}T}}{(1+\sqrt{\theta_0}) + (1-\sqrt{\theta_0})} \right)^2$	$\begin{cases} 1 - e^{-\bar{\lambda}}, & \theta_0 \ge 1\\ \theta_0 (1 - e^{-\bar{\lambda}}), & \theta_0 < 1 \end{cases}$
Ψ-	$1 - e^{-\bar{\lambda}T} \left( \frac{(1 + \sqrt{\theta_0}) - (1 - \sqrt{\theta_0})e^{\bar{\lambda}T}}{(1 + \sqrt{\theta_0}) - (1 - \sqrt{\theta_0})} \right)^2$	$\begin{cases} (1 - e^{-\bar{\lambda}})\theta_0^{-1}, & \theta_0 > 1\\ 1 - e^{-\bar{\lambda}}, & \theta_0 \le 1 \end{cases}$

### Closed-Form: Yields and OTC Rate

Set 
$$\bar{\theta}=\theta_1$$
 and  $\theta=\theta_0$ 

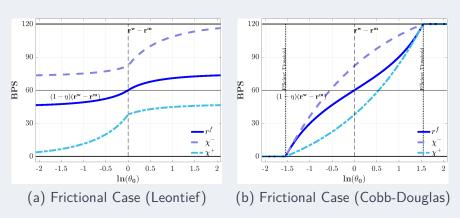
#### Yield Coefficients and OTC Rate

For both Cobb-Douglas and Leontief:

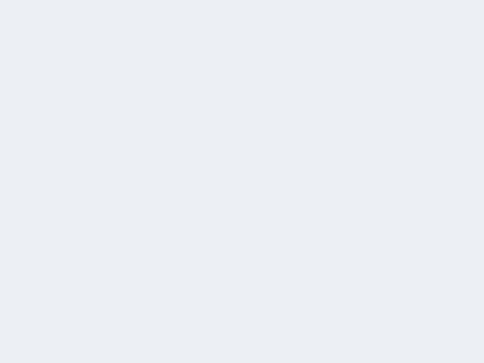
$$\chi^{+} = (r^{w} - r^{m}) \left( \frac{\bar{\theta} - \bar{\theta}^{\eta} \theta^{1-\eta}}{\bar{\theta} - 1} \right), \quad \chi^{-} = (r^{w} - r^{m}) \left( \frac{\bar{\theta} - \bar{\theta}^{\eta} \theta^{-\eta}}{\bar{\theta} - 1} \right)$$
$$\bar{r}^{f} = \phi(\theta) r^{m} + (1 - \phi(\theta)) r^{w}, \quad \phi(\theta) = \frac{(\bar{\theta}/\theta)^{\eta} - \theta}{\bar{\theta}/\theta - 1}$$

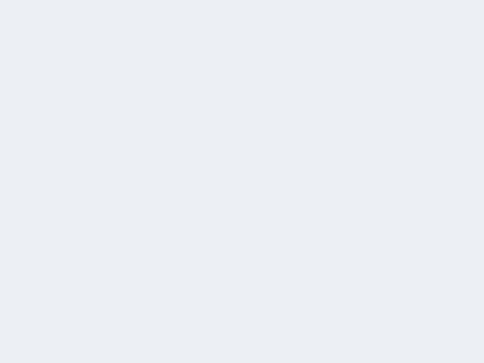
- $\phi(\theta)$  acts as endogenous bargaining index
- Valid in closed-form only for p=0 and  $p=-\infty$ 
  - but not for all p

## Cobb-Douglas vs. Leontief



 $\bullet$  T takes care of making  $\theta=0$  of T<1





### Portfolio Problem with Settlement Risk

#### Investor Preferences and Problem

Investor solves:

$$\max_{\{c, \tilde{a}_{t+1}^{i}, \tilde{m}_{t+1}\}} \mathbb{E}_{0} \sum_{t=0}^{\infty} \beta^{t} \frac{c_{t}^{1-\gamma} - 1}{1 - \gamma}$$

subject to budget and return constraints.

- Cash return  $R^m$  and asset returns  $R^i$  are exogenous.
- Only OTC rate  $\bar{R}^f$  and  $\chi(s;\theta)$  endogenous
- Portfolio separation holds

### Return on Portfolio and Risk

### Portfolio Objective

Investor chooses weights to maximize equity return:

$$\max_{m,a^i} \left( \mathbb{E} \left[ R^{\mathbf{e}} \right]^{1-\gamma} \right)^{\frac{1}{1-\gamma}}$$

where:

$$R^{e} = \sum_{i} R^{i} a^{i} + R^{m} m + \chi \left( s(a^{i}, m, \omega); \theta \right)$$

- $\chi(s)$  is kinked: costly to be in deficit, modest benefit in surplus.
- s depends on portfolio weights and liquidity shocks.

### Convenience Yields and Portfolio Premia

### Decomposition of Excess Returns

At optimality:

$$\begin{split} \mathbb{E}[R^i] - R^m &= \underbrace{-\mathbb{E}[\chi_s(\partial_m s - \partial_{a^i} s)]}_{\text{first-order liquidity yield}} \\ &- \underbrace{\frac{\mathsf{Cov}[R_e^{-\gamma}, R^i + \chi_s(\partial_m s - \partial_{a^i} s)]}{\mathbb{E}[R_e^{-\gamma}]}}_{\text{total risk premium}} \end{split}$$

- $\chi_s$  is the marginal convenience yield  $(\chi^+$  or  $\chi^-)$ .
- Lesson: premia reflect both mean liquidity effects and covariance with risk.
  - Risk and liquidity, not decoupled!
  - FX literature: assumes they are

## Lessons for Portfolio Theory

#### Convenience yields:

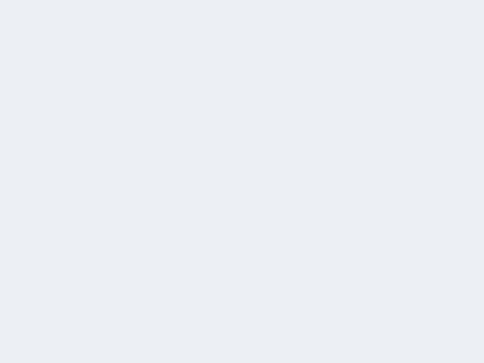
force toward determinate portfolios even under risk neutrality

Risk premia vs. convenience yield decompositions:

not decoupled

Applications: Pricing anomalies

- short-term rate puzzle (Lenel-Piazzesi-Schneider)
- corporate-rate puzzle (Liao)
- CIP deviations (Krishnarmurthy-Jian-Lustig)
- deposit-rate heterogeneity (Dreschler-Savov-Schnabl)

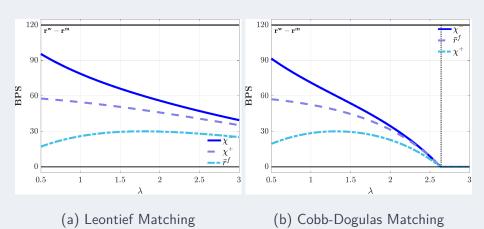


## What Are We Trying to Identify?

### Three Key Parameters

- Market tightness  $\theta$ : imbalance between buyers and sellers
- Matching efficiency  $\bar{\lambda}$ : how quickly matches form
- Bargaining power  $\eta$ : who keeps the surplus
- Why identify them?
  - Decompose sources of convenience yields
  - Run policy or institutional counterfactuals
  - Map observed premia to underlying frictions

## Non-Monotonicity: Identification Challenge



Non monotonic yields in efficiency

# Identification Strategy: Moments and Mapping

#### Observable Moments

- $\bar{r}^f$  and  $\chi^{\pm} \Rightarrow \text{pin down } \theta \text{ (monotonicity)}$
- Portfolios and implied  $\theta \Rightarrow$  shock distribution  $\Phi$
- ullet Intraday dispersion  $Q\Rightarrow$  moment identify  $ar{\lambda}$  or  ${\sf G}$
- Relative volume  $I(\theta) \equiv \frac{\Psi^-}{1-\Psi^-} \Rightarrow$  clean moment for  $\bar{\lambda}$
- Use  $\chi^+/\chi^-$  near  $\theta=1\Rightarrow$  infer  $\eta$

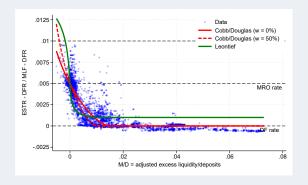
# Identification Strategy: Moments and Mapping

#### Observable Moments

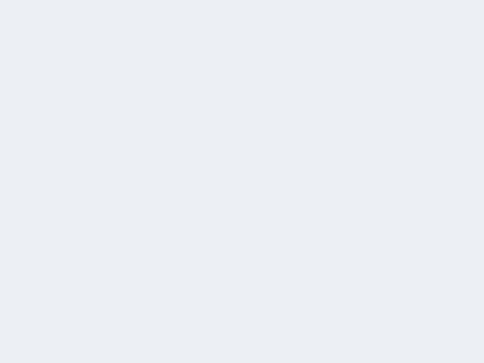
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- Use  $\chi^+/\chi^-$  near  $\theta=1\Rightarrow$  infer  $\eta$

## **Payoff**

- Estimate of  $\frac{R^f R^m}{R^w R^m}$  as function of  $\theta(M/D)$  for Euro Area
- Used in Bigio-Linzert-Mendo-Schumacher-Thaler:



Fit to Euro Area



### **Efficiency**

- Portfolio choice may be constrained inefficient
- Depends on who earns penalties
- Here, assume it's waste

# Banking Example: Withdrawal Risk

### Portfolio Structure in Bianchi-Bigio '22

- Assets: cash m, illiquid bond b.
- Liability: deposit d subject to withdrawal shock  $\omega$ .
- Settlement position:

$$s(b, d, m) = m + \left(\frac{R^d}{R^m}\omega - \rho(1+\omega)\right)d$$

• Budget: b + m = 1 + d.

# Liquidity Premium on Bonds

### Illiquid Asset vs. Cash

$$R^{b}-R^{m}=\chi^{+}+(\chi^{-}-\chi^{+})\tilde{\Phi}(\omega^{*})$$

where:

$$\tilde{\Phi}(\omega^*) = \Phi(\omega^*) \cdot \frac{\mathbb{E}[R^{\mathrm{e}}(\omega)^{-\gamma} | \omega < \omega^*]}{\mathbb{E}[R^{\mathrm{e}}(\omega)^{-\gamma}]}, \quad \omega^* = \frac{\rho - m/d}{R^d/R^m - \rho}$$

- $\Phi(\omega^*)$ : probability of cash deficit.
- $\tilde{\Phi}$ : risk-adjusted deficit probability.

## Efficiency of Portfolio Management

- Investors: not internalize effect on market tightness  $\theta$
- Externality: cash improves reduces external borrowing + but has opportunity cost
- Haider-Ismail and Zuniga
  - flipside, study loan-deposit wedge with rebate

### Planner Problem

### Planner Optimality Condition

$$R^{b} - R^{m} = \chi^{+} + (\chi^{-} - \chi^{+})\tilde{\Phi}(\omega^{*}) + H$$

- H: pecuniary externality from m's effect on  $\theta$  and  $\chi$ .
- Planner internalizes how *m* affects matching and yields.

## Direction of the Externality

• Risk-neutrality ( $\gamma \to 0$ ), planner values cash more iff

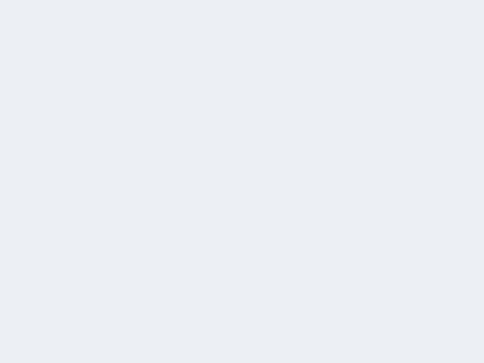
$$\frac{\partial \chi^+}{\partial \theta} S^+ > \frac{\partial \chi^-}{\partial \theta} S^-$$

## Cases: Leontief vs. Cobb-Douglas

- Cobb-Douglas:
  - near balanced market ( $\theta = 1$ ), no inefficiency.
  - risk-aversion: force toward more liquidity  $m \Rightarrow$  precautionary motive
- Leontief:
  - matching probabilities of short-side fixed
  - no inefficiency if planner & market allocation feature aggregate surplus
- Inefficiencies: matching-function specific

## **Policy Implications**

- Inefficiency: liquidity regulation
- Planner: more cash to reduce exposure to costly borrowing (e.g., FX reserve management, Central Bank balance sheet)



### Limitations and Extensions

- Results rely on simplifying assumptions
  - large number of traders, no network, no effort
- Portfolio: one layer. Reality: multi-layered.
- Still, useful to know simplest outcomes

### Thank You!

Questions, comments?