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(1)

(7)

AI1110: Probability and Random Variable Assignment-1

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Question: 12.13.2.18

Problem Statement:

Two events A and B will be independent, if

- (A) A and B are mutually exclusive
- (B) Pr(A'B') = [1 Pr(A)][1 Pr(B)]
- (C) Pr(A) = Pr(B)
- (D) Pr(A) + Pr(B) = 1

Solution:

(B) Pr(A'B') = [1 - Pr(A)][1 - Pr(B)]

$$\Rightarrow \Pr(A'B') = 1 - \Pr(A) - \Pr(B) + \Pr(A)\Pr(B)$$

$$\Rightarrow 1 - \Pr(A + B) = 1 - \Pr(A) - \Pr(B) + \Pr(A)\Pr(B)$$

$$\Rightarrow -[\Pr(A) + \Pr(B) - \Pr(AB)] = -\Pr(A) - \Pr(B) + \Pr(A)\Pr(B)$$

$$\Rightarrow -\Pr(A) - \Pr(B) + \Pr(AB) = -\Pr(A) - \Pr(B) + \Pr(A)\Pr(B)$$

$$\Rightarrow \Pr(AB) = \Pr(A) \cdot \Pr(B)$$

$$(5)$$

Pr(A'B') = [1 - Pr(A)][1 - Pr(B)]

Hence it shows A and B are Independent events