

Q) $F = \prod_M (0, 1, 3, 6, 7)$ [POS]

	B'C'	B'C	BC	BC'
A'	0	1	3	2
A	4	5	7	6

2 Pairs

Thus Simplified

$$\Rightarrow (A' + B')(B + C)(A + B)$$

Since its POS,

$$0, 1 \Rightarrow (A' + B' + C')(A'B + B' + C) \Rightarrow (A' + B')$$

$$3, 7 \Rightarrow (A' + B + C)(A + B + C) \Rightarrow (B + C)$$

$$7, 6 \Rightarrow (A + B + C)(A + B + C') \Rightarrow (A + B)$$

Q) $F = \sum_m (0, 1, 3, 5, 6, 9, 11, 13, 15)$

	C'D'	C'D	CD	CD'
A'B'	1	1	1	2
A'B		1		1
AB	1	1	1	1
AB'		1	1	

Four variables.
since max number is 15.

(LSB \rightarrow Least significant Bit)
(MSB \rightarrow Most significant Bit)

$$\rightarrow \begin{cases} M \leq 7 & 3 \text{ var} \\ M \leq 15 & 4 \text{ var} \end{cases}$$

16 Box K-Map

3 Quads

$$1, 5, 13, 9 \rightarrow C'D$$

$$13, 15, 9, 11 \rightarrow AD$$

$$9, 11, 1, 3 \rightarrow B'D$$

Essential (largest comb.)
Prime
Implicants

2 Pairs

$$0, 1 \rightarrow A'B'C'$$

$$12, 13 \rightarrow ABC'$$

$$\begin{aligned} 1 \text{ singular} \\ 6 \rightarrow A'BCD' \end{aligned}$$

$$F = A'BCD' + A'B'C' + ABC' + C'D + AD + B'D$$

Prime implicants are the largest combination of units aka quads chosen

Form

\rightarrow AOI Logic
 \rightarrow NAND Logic (Better)
 \rightarrow NOR Logic

\therefore Since SOP

Q) $F = \sum_m (2, 3, 5, 7, 9, 11, 12, 13, 14, 15)$

	$C'D'$	$C'D$	CD	CD'
$A'B'$	0	1	1	1
$A'B$	4	1	1	6
AB	1	1	1	1
AB'	8	1	1	10

4 Quads

5, 7, 13, 15

3 Quads

→ 5, 7, 13, 15

→ 13, 15, 9, 11

→ 12, 13, 15, 14

1 Pair

→ 3, 2

1 Redundant Quad
→ 3, 7, 15, 11

Removing / Not involving
it will keep number of
terms same

$F = AB + AD + BD + A'B'C$

- NAND-NAND logic → 7 gates (Better ∵ SOP form)
- NOR-NOR logic → 13 gates

Q) $F = \sum_m (2, 3, 4, 6, 7, 10, 13, 14)$

	$C'D'$	$C'D$	CD	CD'
$A'B'$	0	1	1	1
$A'B$	1	5	1	1
AB	12	1	13	1
AB'	8	9	11	1

2 Quads

(2, 3, 6, 7) and (2, 6, 14, 10)

1 Pair

(1, 6)

$F = ABD' + ABCD + A'C + CD'$

- NAND-NAND Logic → 10 gates (Better)
- NOR-NOR Logic → 12 gates

Q) $F = \prod_M (0, 2, 4, 7, 11, 14)$

	$C'D'$	$C'D$	CD	CD'
$A'B'$	0	1	3	2
$A'B$	0	5	7	6
AB	12	13	15	14
AB'	8	9	11	10

$F = (B+C+D')(A+B+D')(A'$
 $(A+C+D)(A+B+D)(A+B'+C+D')$
 $(A'+B'+C+D)(A'+B+C+D')$