# **CS726 Programming Assignment – 2 Report**

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### **Denoising Diffusion Probabilistic Models**

Here are the results of unconditional DDPMs on various datasets (with respect to the number of time steps). We had fixed all other parameters (the best settings observed):

- lbeta=0.0001
- ubeta=0.02
- lr=0.0001 (so that training loss decreases across epochs)
- n\_samples=10000
- $n_dim=2$  (for helix it is 3)
- batch\_size=128 (to avoid CUDA memory errors and produce optimal results)
- epochs=40

### **Moons**

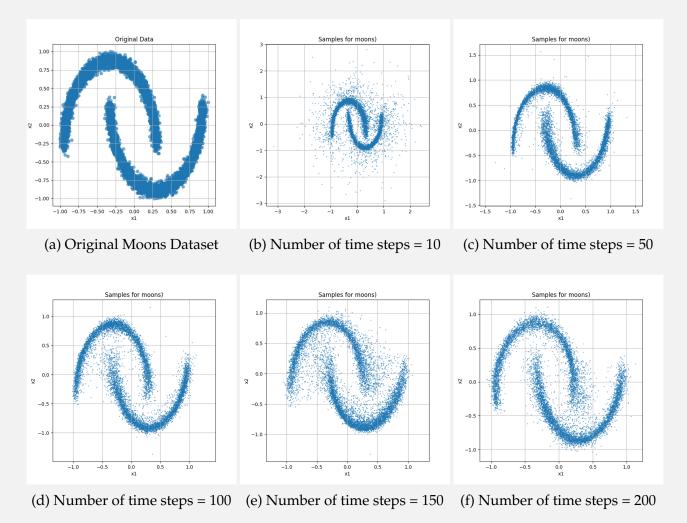


Figure 1: Moons Dataset

#### Here are the NLL values:

- *T* = 10: 1.048
- *T* = 50: 0.9599
- T = 100: 0.9519
- *T* = 150: 0.9218
- T = 200: 0.9321

As, we can see from both NLL values and the images, T = 150 performed the best.

#### **Blobs**

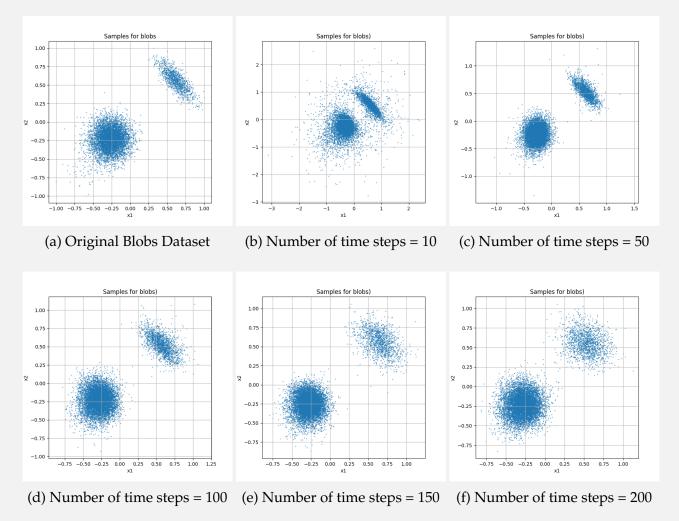


Figure 2: Blobs Dataset

Here are the NLL values:

• T = 10: 0.37

• *T* = 50: 0.0152

• T = 100: 0.0232

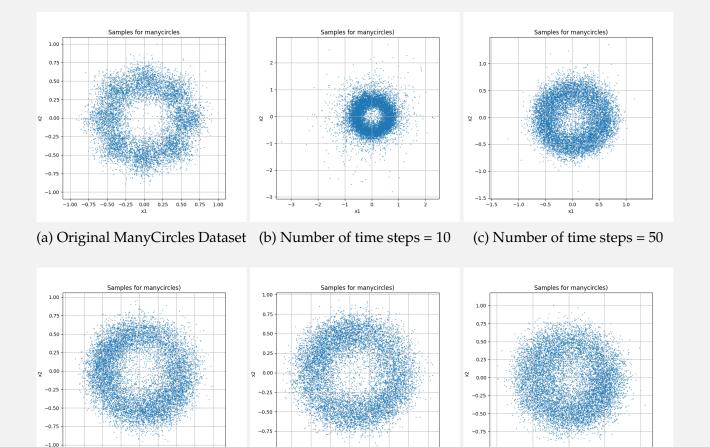
• T = 150: -0.0223

• T = 200: 0.0045

As, we can see from both NLL values and the images, T=150 performed the best. Moreover, there is a sudden decrease in NLL from 10 to 50, which shows the significant impact of increasing the number of time steps.

(f) Number of time steps = 200

### **Many-Circles**



(e) Number of time steps = 150

Figure 3: Many Circles Dataset

Here are the NLL values:

(d) Number of time steps = 100

• T = 10: 0.75

• T = 50: 0.548

• T = 100: 0.545

• T = 150: 0.558

• *T* = 200: 0.522

As, we can see from both NLL values and the images, T = 200 performed the best.

### **Circles**

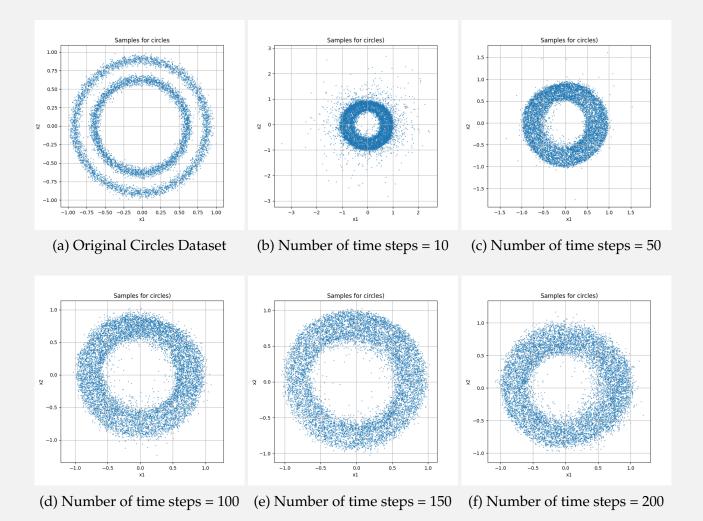


Figure 4: Circles Dataset

#### Here are the NLL values:

- *T* = 10: 1.081
- T = 50: 0.991
- *T* = 100: 0.9869
- *T* = 150: 1.004
- *T* = 200: 0.992

#### Helix

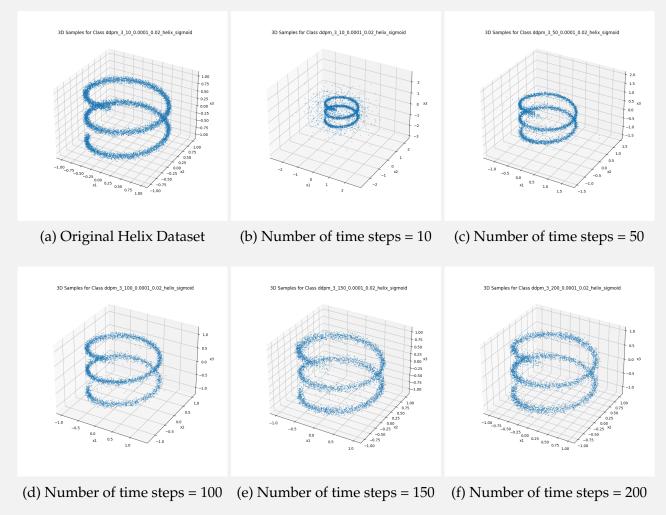


Figure 5: Helix Dataset

Here are the NLL values:

• T = 10: 1.6179

• T = 50: 1.514

• *T* = 100: 1.5198

• *T* = 150: 1.528

• *T* = 200: 1.528

As we can see from the images (and the NLL values), 50 performs the best.

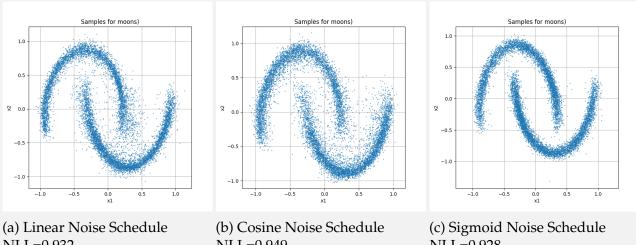
### Comparison of different noise schedules

Along with the linear noise schedule, we have studied the effect of cosine and signmoid noise schedules for the DDP model. The results of the comparison are as shown below. In each of the cases we have set the other hyperparameters as follows:

- Number of time steps = 200
- lbeta=0.0001
- ubeta=0.02

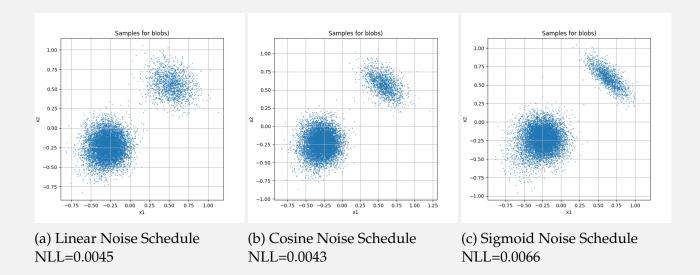
- lr=0.0001
- n\_samples=10000
- n\_dim=2
- batch\_size=128
- epochs=40

#### Moons



- NLL=0.932
- NLL=0.949
- NLL=0.928

#### **Blobs**



In both cases (as well as on the other datasets) we observe that the NLL is least for the sigmoid noise schedule.

### **Classifier-Free Guidance**

### Difference between Guided Sampling and Conditional Sampling

In conditional sampling, we model p(x|y) directly, where y is a conditioning variable (like a class label). During generation, we sample from this conditional distribution to get samples that match the condition.

In guided sampling (specifically classifier-free guidance), we train two models: one conditional p(x|y) and one unconditional p(x). During sampling, we interpolate between them with a guidance scale w:

$$\epsilon_{\theta}(x_t, t, y) = (1 + w) * \epsilon_{\theta}(x_t, t, y) - w * \epsilon_{\theta}(x_t, t)$$

Firstly, guided sampling is more expensive in terms of computation required to train and sample points (almost double, since we are training two models, and using both of them to sample points). However, this guidance increases the impact of the conditioning information and can produce higher quality samples that better match the condition, but with a potential loss of diversity.

### Effect of guidance scale

We sampled points using CFG on a variety of guidance scale values, here are the images from the moon dataset:

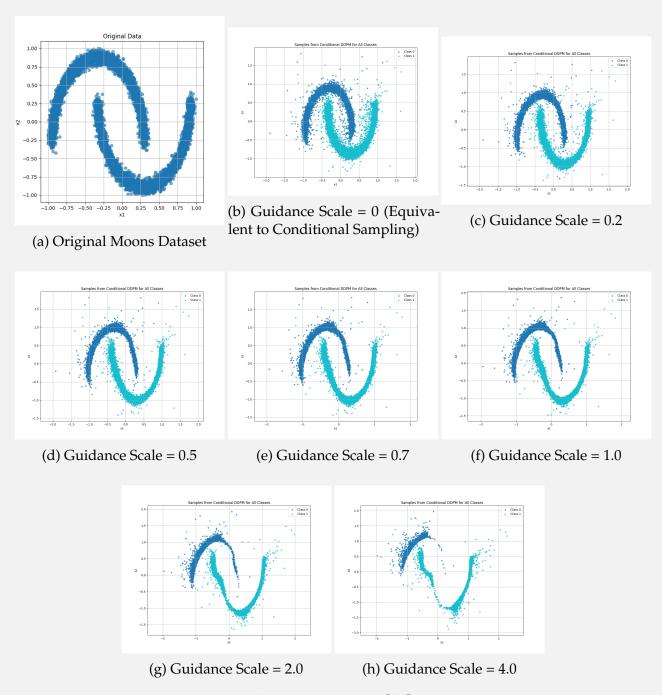


Figure 8: Moons - CFG

Here are the NLL values for the two class labels:

<b>Guidance Scale</b>	NLL for Class Label 0	NLL for Class Label 1
0.0	0.53	0.58
0.2	0.51	0.58
0.5	0.50	0.59
0.7	0.50	0.60
1.0	0.51	0.62
2.0	0.57	0.66
4.0	0.65	0.71

Table 1: NLL Values for the two class labels of the Moons Dataset

As, it is evident from the NLL values and the images shown above, guidance scales 0.2 and 0.5 perform the best. With higher guidance scales, we typically lose focus on randomly generated data, and rely too much on the training labels provided, thus the NLL values are low, when another sample

is chosen from the actual dataset. These observations match with the ones presented in the CFG paper too.

We had also compared the samples generated with a simple classifier model trained, here are the accuracy results across various guidance scale values:

<b>Guidance Scale</b>	Accuracy for Class Label 0	Accuracy for Class Label 1
0.0	0.52	0.49
0.2	0.52	0.50
0.5	0.52	0.51
0.7	0.52	0.52
1.0	0.52	0.52
2.0	0.49	0.55
4.0	0.46	0.61
8.0	0.44	0.67
10.0	0.44	0.68

Table 2: Accuracy Values for the two class labels of the Moons Dataset

As we can see, the accuracy values do not vary much across various guidance scale values. They peak around a scale of 1 (which is as per the results obtained in the paper), similar to NLL results. Higher scale values tend to bias towards one of the class labels as demonstrated in the images too.

#### **Classifier using Conditional DDPM**

The ClassifierDDPM class implements a classification method using a Diffusion Probabilistic Model (DDPM). The classification is performed by computing the likelihood of each class given the input, using a pre-trained conditional DDPM.

Given an input  $x \in \mathbb{R}^d$ , we generate a noisy sample  $x_t$  at a fixed timestep t using the variance-preserving noise schedule:

$$x_t = \sqrt{\bar{\alpha}_t} x + \sqrt{1 - \bar{\alpha}_t} \epsilon, \tag{1}$$

where:

- $\bar{\alpha}_t$  is the cumulative product of noise scheduling parameters,
- $\epsilon \sim \mathcal{N}(0, I)$  is Gaussian noise.

For each class label  $c \in 0, 1, ..., C-1$ , the classifier uses the conditional DDPM model to predict the noise:

$$\hat{\epsilon}_c = \text{model}(x_t, t, c), \tag{2}$$

where  $\hat{\epsilon}_c$  is the predicted noise when conditioning on class *c*.

The classification score for class *c* is computed as the negative mean squared error between the predicted and actual noise:

$$S_c = -\mathbb{E}\left[|\hat{\epsilon}_c - \epsilon|^2\right]. \tag{3}$$

This score measures how well the model's noise prediction aligns with the actual noise for each class. A lower error implies a higher likelihood of the class being correct.

To convert the classification scores into probabilities, a softmax function is applied:

$$P(c \mid x) = \frac{\exp(S_c)}{\sum_{c'} \exp(S_{c'})}.$$
 (4)

The predicted class is then obtained as:

$$\hat{c} = \arg\max_{c} P(c \mid x). \tag{5}$$

## **Reward Guidance**