



Approximate
Nearest Neighbor
Search via Group
Testing

Authors

Introduction

APPROXIMATE NEAREST NEIGHBOR SEARCH VIA GROUP TESTING

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Nearest Neighbor Search



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Introduction

- Nearest neighbor search is a fundamental problem with many applications in machine learning systems.
- **Task:** Given a dataset $D = \{x_1, x_2, \dots, x_N\}$, the goal is to build a data structure that can be queried with any point q to obtain a small set of points $x_i \in D$ that have high similarity (low distance) to the query. This structure is called an index.
- Such tasks frequently arise in genomics, web-scale data mining, machine learning, and other large-scale applications.

Locality Sensitive Hashing



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- **Locality Sensitive Hashing (LSH)** algorithms use an LSH function to partition the dataset into buckets.
- The hash function is selected so that the distance between points in the same bucket is likely to be small.
- To find the near neighbors of a query, we hash the query and compute the distance to every point in the corresponding bucket.
- **Count-Based LSH** identifies neighbors by simply counting how many times two points land in the same hash bucket across multiple hash functions.

Formal Problem Statement



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- **(R, c)-Approximate Near Neighbor:** Given a dataset D , if there exists a point within distance R of a query y , return some point within distance $c \cdot R$, with high probability.
 - R is the distance threshold (radius).
 - $c > 1$ is the approximation factor.
- Any algorithm that solves the randomized nearest neighbor problem also solves the approximate near neighbor problem with $c = 1$ and any $R \geq$ distance to the nearest neighbor.
- (Definition) **Randomized Nearest neighbor:** Given a dataset D and a distance metric $d(\cdot, \cdot)$ and a failure probability $\delta \in [0, 1]$, construct a data structure which, given a query point y reports the point $x \in D$ with the smallest distance $d(x, y)$ with probability greater than $1 - \delta$.