

# CS663 Assignment-3

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## Question 1

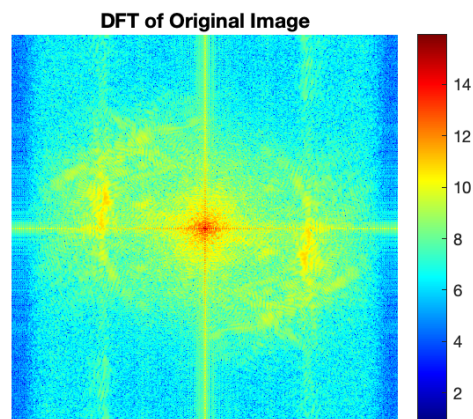
### Solution

**Note:** All the Fourier Transform and Frequency Response figures are shown in logarithm absolute format.

### Original Image



(a) Original Image



(b) Fourier Transform of Original Image

## Ideal Low Pass Filter

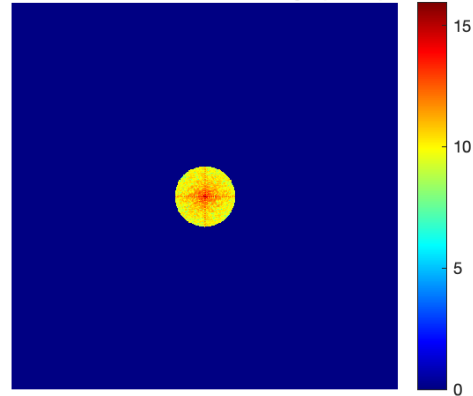
Cutoff Frequency = 40

**Ideal LP Filtered Image (f = 40)**



(a) Filtered Image

**DFT of Ideal LP Filtered Image (f = 40)**



(b) Fourier Transform of Filtered Image

**Ideal Low Pass Filter (f = 40)**

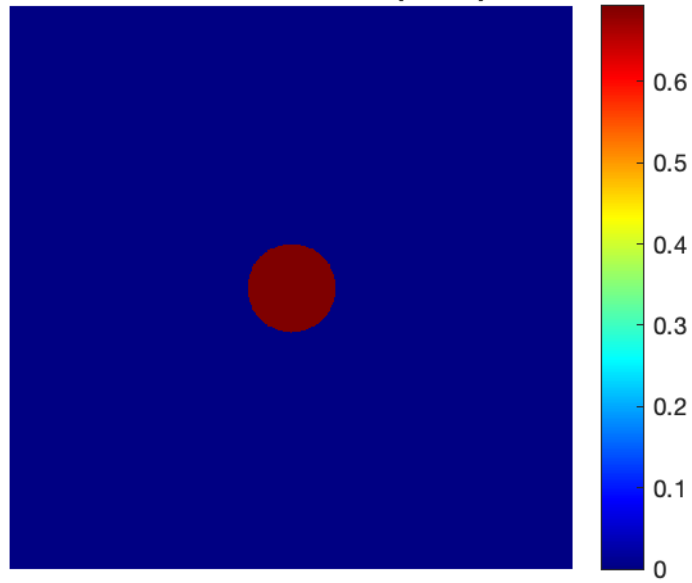


Figure 3: Frequency Response of Filter

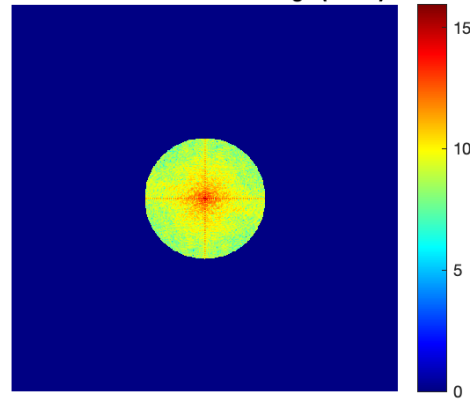
Cutoff Frequency = 80

**Ideal LP Filtered Image ( $f = 80$ )**



(a) Filtered Image

**DFT of Ideal LP Filtered Image ( $f = 80$ )**



(b) Fourier Transform of Filtered Image

**Ideal Low Pass Filter ( $f = 80$ )**

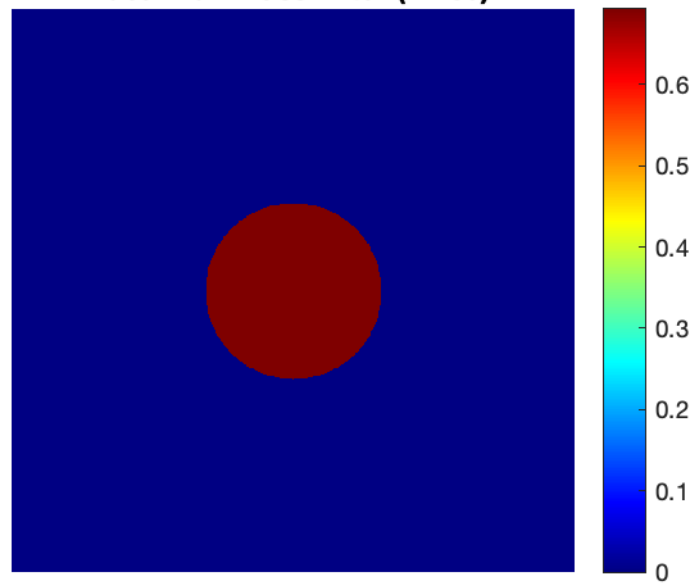


Figure 5: Frequency Response of Filter

## Gaussian Low Pass Filter

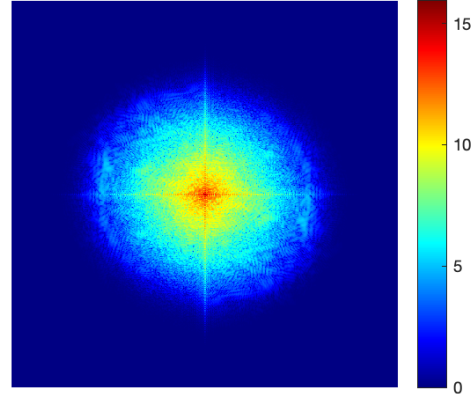
Sigma = 40

**Gaussian LP Filtered Image (sigma = 40)**



(a) Filtered Image

**DFT of Gaussian LP Filtered Image (sigma = 40)**



(b) Fourier Transform of Filtered Image

**Gaussian Low Pass Filter (sigma = 40)**

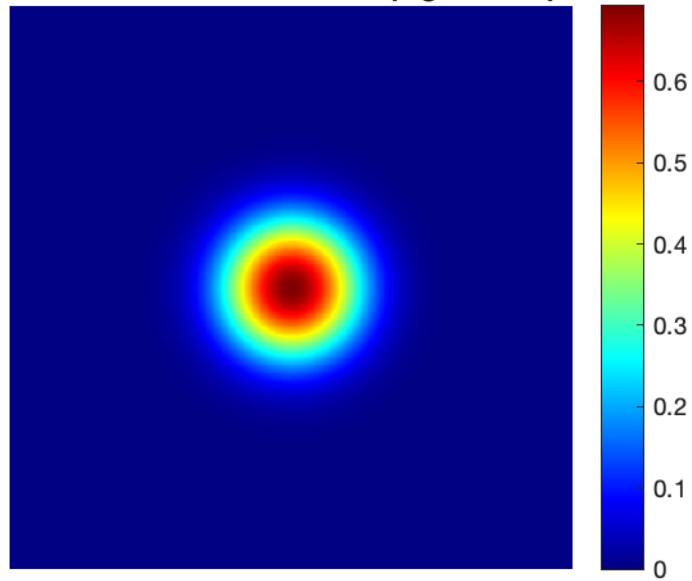


Figure 7: Frequency Response of Filter

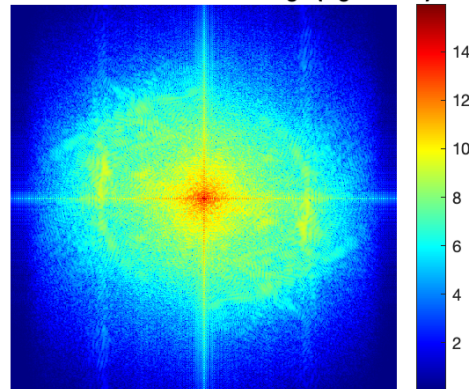
Sigma = 80

Gaussian LP Filtered Image (sigma = 80)



(a) Filtered Image

DFT of Gaussian LP Filtered Image (sigma = 80)



(b) Fourier Transform of Filtered Image

Gaussian Low Pass Filter (sigma = 80)

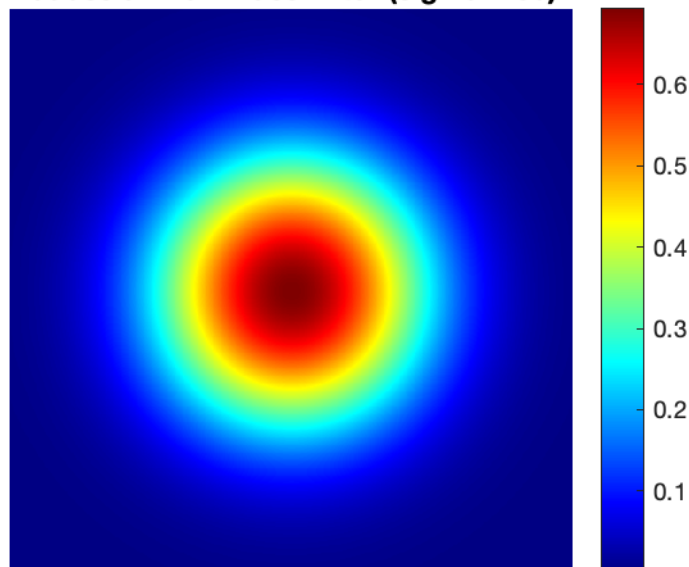


Figure 9: Frequency Response of Filter

## Observations

- From the obtained results we can easily see that as the cut-off frequency (for ideal low pass filter) / sigma (for Gaussian low pass filter) is increased, the higher frequency components which correspond to finer details in the image start becoming clearly visible.
- Also we can see that for ideal low pass filter there is a presence of **ringing artifacts** that appear as spurious signals near sharp transitions in the images. These ringing artifacts are quite undesirable and are a result of the complete elimination of high frequencies higher than the cut-off frequency by the ideal low pass filter.

- When a Gaussian low pass filter is used these ringing artifacts are absent. This is because the Gaussian low pass filter does not completely eliminate the higher frequencies and rather weakens them.