

# Computer Science

## Theory of Computation

Undecidability

Lecture No.- 1

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# Recap of Previous Lecture



**Topic**

**Turing Machine**





# Topics to be Covered



Topic

Decidable (Recursive)

Topic

SDUD (RE but not recursive)

Topic

RE

Topic

Not RE

Topic

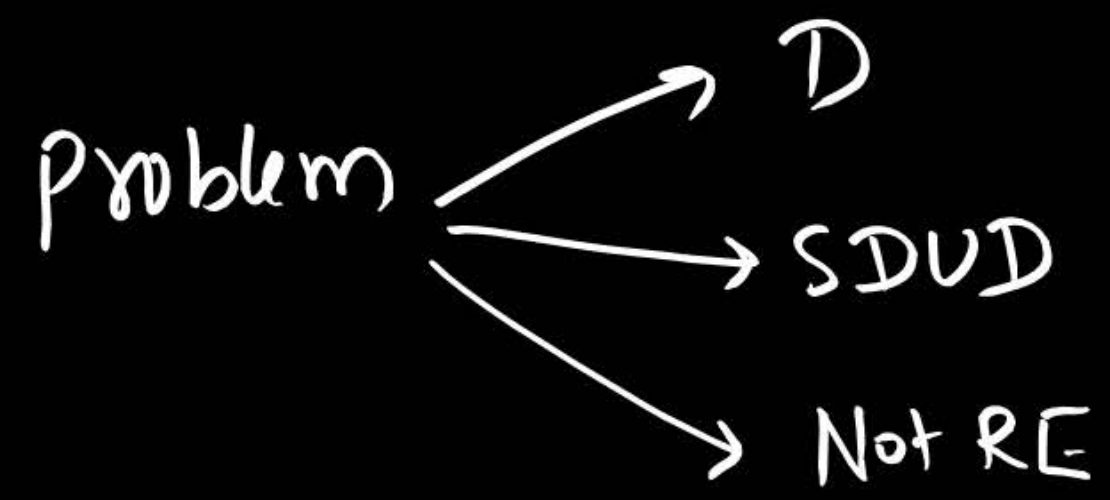
Undecidable

[either SDUD or Not RE]

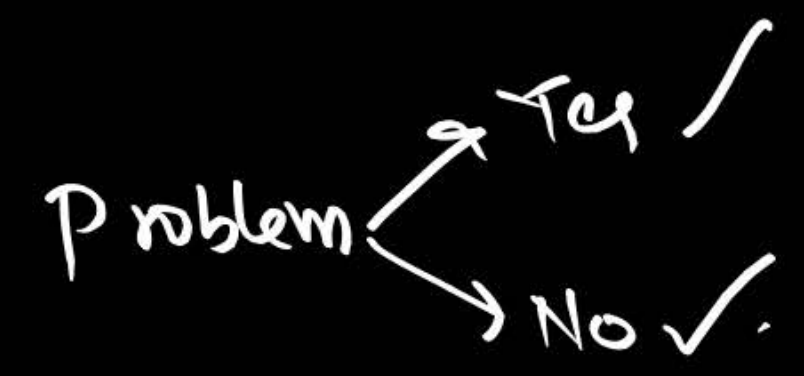
} SD (RE)

	Problem	FA	DPDA	PDA	LBA or NTM	TM
1)	Halting	✓	✓	✓	✓	✗
2)	Membership	✓	✓	✓	✓	✗
3)	Emptiness	✓	✓	✓	✗	✗
4)	Finiteness	✓	✓	✓	✗	✗
5)	Totality	✓	✓	✗	✗	✗
6)	Equivalence	✓	✓	✗	✗	✗
7)	Disjoint	✓	✗	✗	✗	✗
8)	Set containment	✓	✗	✗	✗	✗

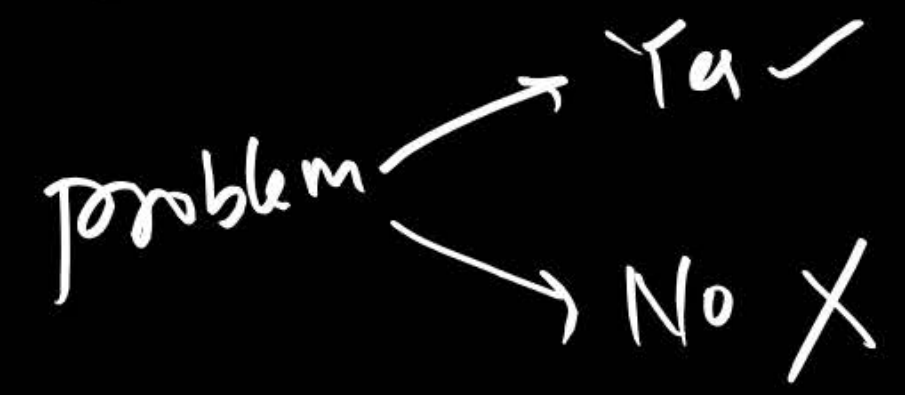
✓ : Decidable  
✗ : Undecidable



D:



SDUD:



Not RE





## Halting problem:

IS FA halts on  $w$ ?

IS DPDA halts on  $w$ ?

IS PDA halts on  $w$ ?

IS Htm halts on  $w$ ?

IS Tm halts on  $w$ ?

Decidable

Yes: Halts at final ✓

No: Halts or never halts

UNDECIDABLE

Membership problem

( IS M accepts  $w$  ? )  
 IS  $w \in L$  ?  
 IS  $w \in L(G)$  ?



TM : valid  $\Rightarrow$  Halt ✓  
 Invalid  $\Rightarrow$  ? X

SCUD



Emptiness problem:

Is  $M$  accepts nothing?

Is  $L = \emptyset$ ?

Is  $L(G) = \emptyset$ ?



Finiteness:

Is  $M$  accepts finite language?

Is  $L(M) = \text{finite}$ ?

Is  $L(G) = \text{finite}$ ?

Totality:

IS  $L = \Sigma^*$ ?

IS  $M$  accepts everything?



Equivalence:

IS  $M_1 \cong M_2$ ?

IS  $L(M_1) = L(M_2)$ ?

Disjoint : (Intersection empty)

$$\text{IS } L_1 \cap L_2 = \emptyset ?$$

$$\text{IS } L(M_1) \cap L(M_2) = \emptyset ?$$



Set Containment [subset check]:

IS  $L_1 \subseteq L_2$ ?

IS  $L(M_1) \subseteq L(M_2)$ ?



## 2 mins Summary



Topic

→ Decision properties



**THANK - YOU**