

# CS & IT ENGINEERING

## Theory of Computation

Regular Languages

Lecture No.- 17

A man with a beard and mustache, wearing a black polo shirt, stands with his arms crossed in front of a blurred bookshelf. He is wearing a black watch on his left wrist.

Malleham Devasane Sir

# Recap of Previous Lecture



**Topic**

**Model-I (Easy:  $\Phi$ ,  $\Sigma^*$ , only epsilon,  $\Sigma^+$ )**

**Topic**

**Important concepts of DFA**



# Topics to be Covered



**Topic**

**Construction of DFA Model II (Length)**

**Topic**

**Construction of DFA Model III (No. of symbols)**

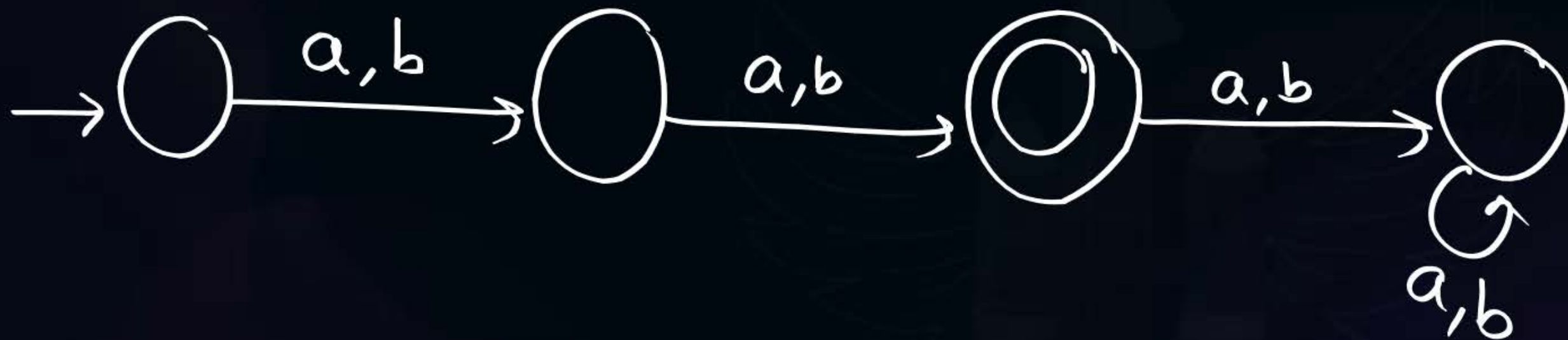
**Topic**

**Construction of DFA Model IV (Over 1 symbol)**

(17) Set of all strings having exactly 2 length over  $\Sigma = \{a, b\}$ .

$$L = \{w \mid w \in (a+b)^*, |w| = 2\} = (a+b)^2 \\ = aa + ab + ba + bb$$

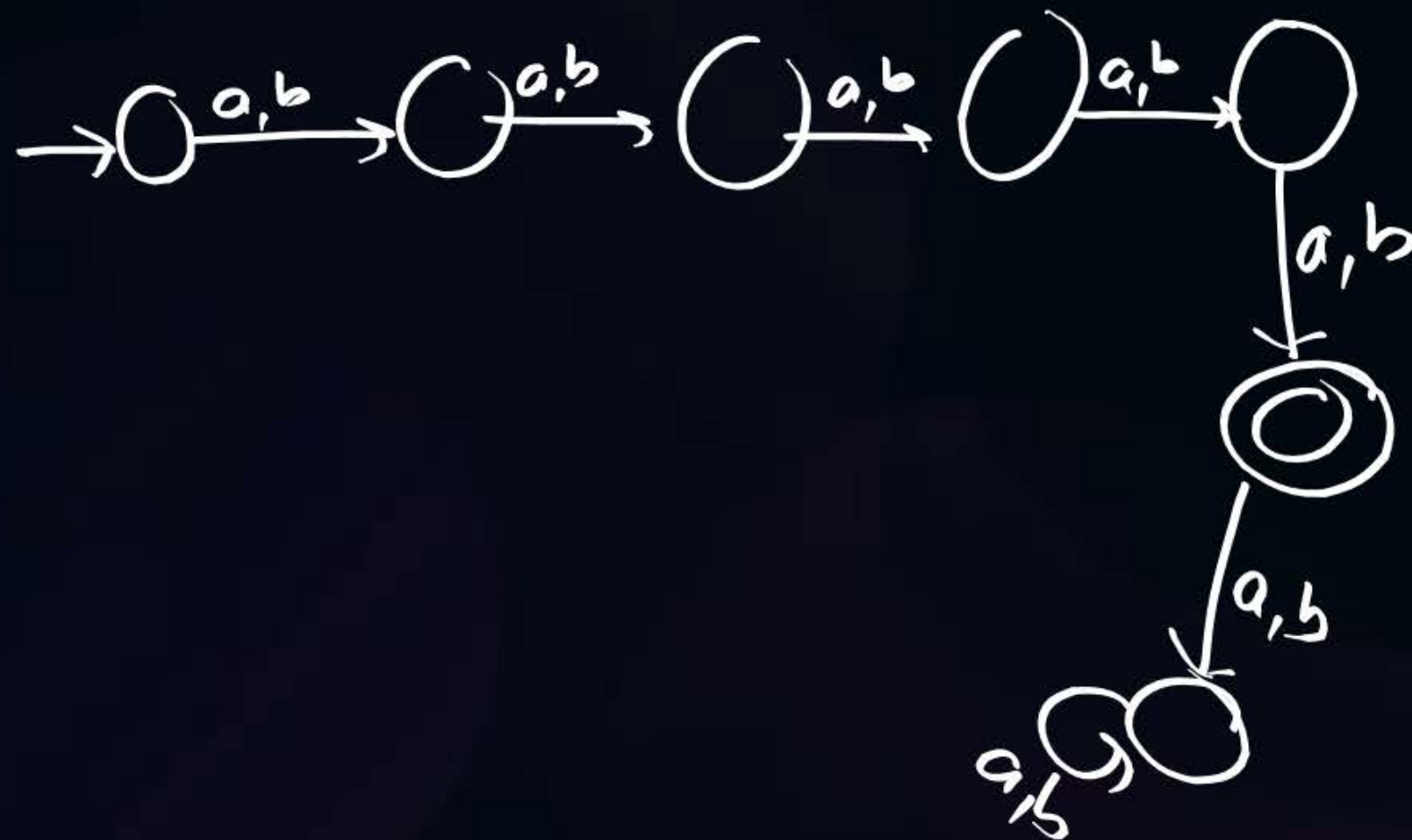
= 4 states  
in min DFA





(20) Set of all strings having exactly 5 length over  $\Sigma = \{a, b\}$ .

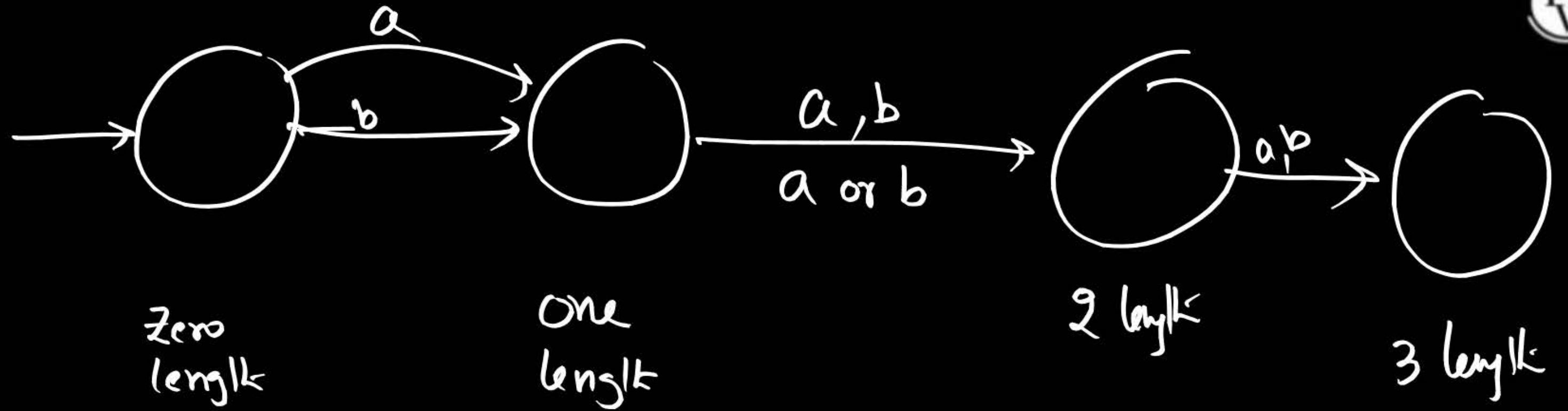
$$L = \{w \mid w \in (a+b)^*, \underbrace{|w|=5}\} = (a+b)^5$$



Exactly 5 length

$$\Downarrow \\ = (5+1) + 1 \text{ trap}$$

$$= 7 \text{ states}$$

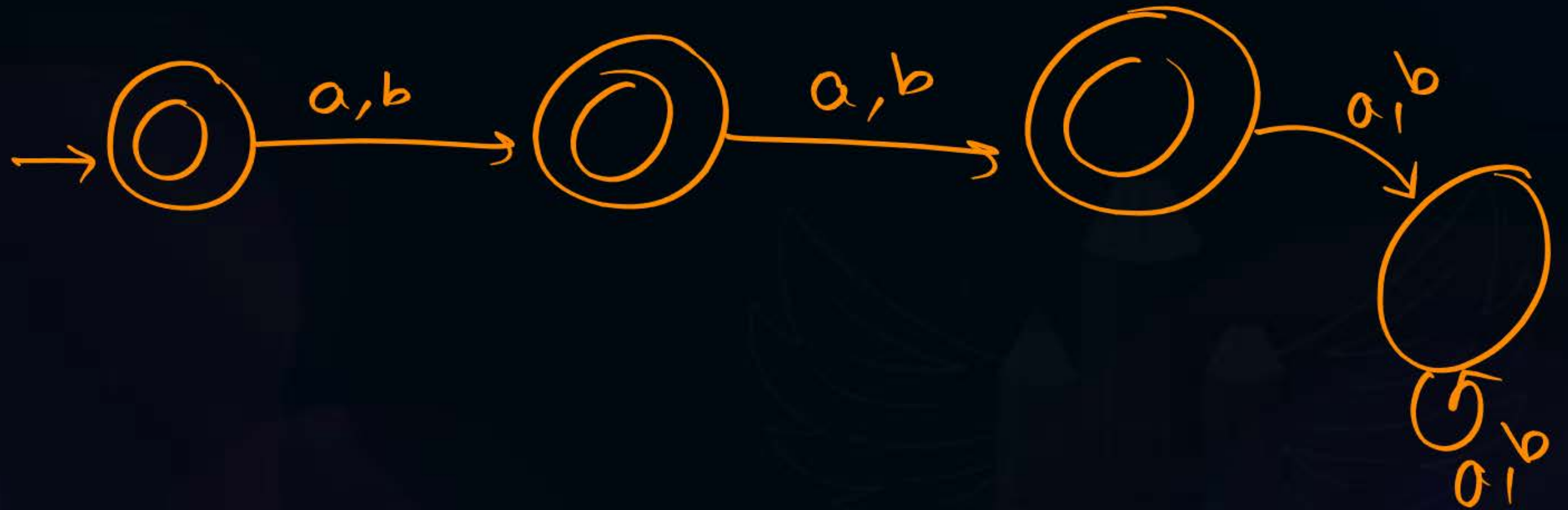


$$|a| = 1$$

$$|b| = 1$$

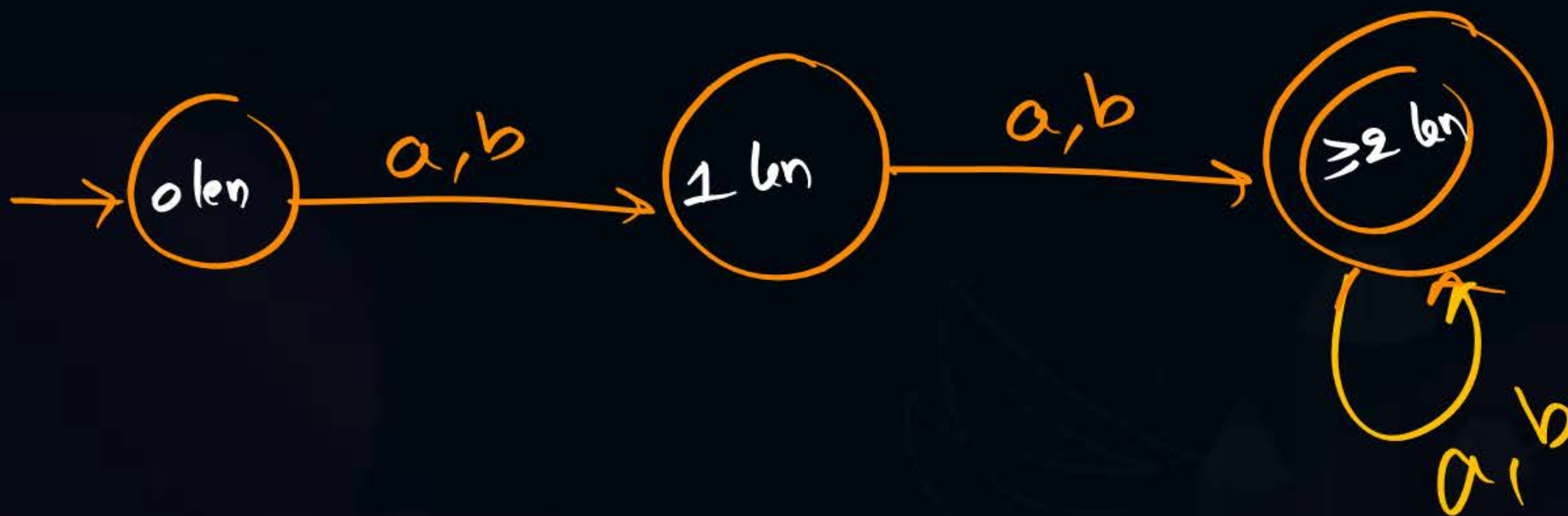
Concept  
for length

(18)  $\{w \mid w \in \{a,b\}^*, \underbrace{|w| \leq 2}_{\text{Atmost 2 length}}\} = (\epsilon + a + b)^2$





(19)  $\{w \mid w \in \{a, b\}^*, |w| \geq 2\} = (a+b)^2 (a+b)^*$   
 $= 2, 3, 4, \dots$





Note :

$$\text{I) } |w| = K \Rightarrow$$

$\downarrow$  string       $\nearrow$  constant

No. of States in min DFA

$$K+2$$

$$\text{II) } |w| \leq K \Rightarrow$$

$$K+2$$

$$\text{III) } |w| \geq K \Rightarrow$$

$$K+1$$

$$\text{IV) } |w| < K \Rightarrow |w| \leq (K-1) \Rightarrow (K-1)+2 = K+1$$

$$\text{V) } |w| > K \Rightarrow |w| \geq (K+1) \Rightarrow (K+1)+1 = K+2$$

(21)  $\{w \mid w \in \{a, b\}^*, n_a(w) = 2\}$

$b^* a b^* a b^*$



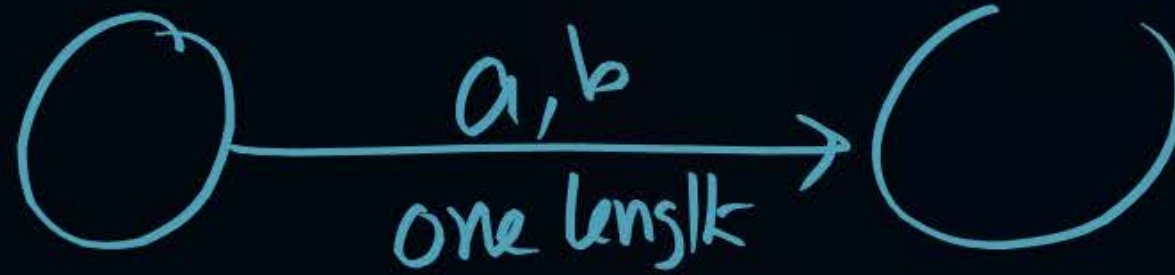
$$n_a(w) = 2$$

$$\#_a(w) = 2$$

$$\text{no. of } a\text{'s}(w) = 2$$



Length:

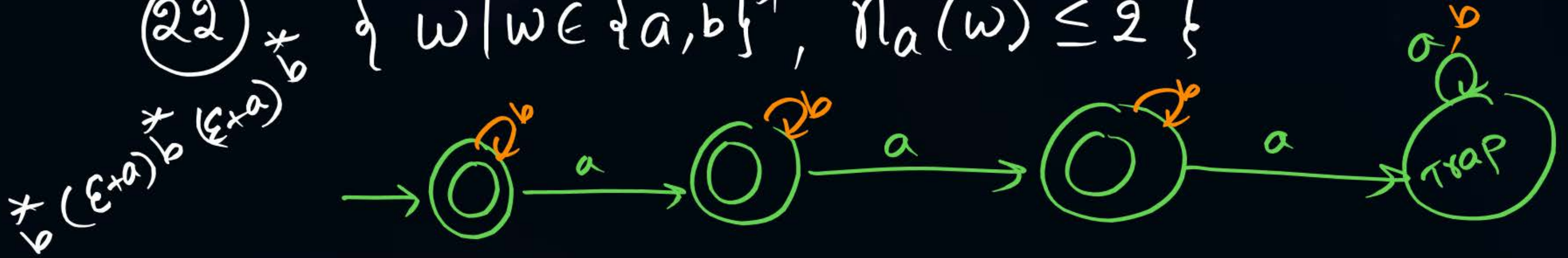


If we want to remember symbol 'a' then change state only for 'a'.

Symbol  
a



(22)  $\{w \mid w \in \{a,b\}^*, n_a(w) \leq 2\}$



(23)  $\{w \mid w \in \{a,b\}^*, n_a(w) \geq 2\}$

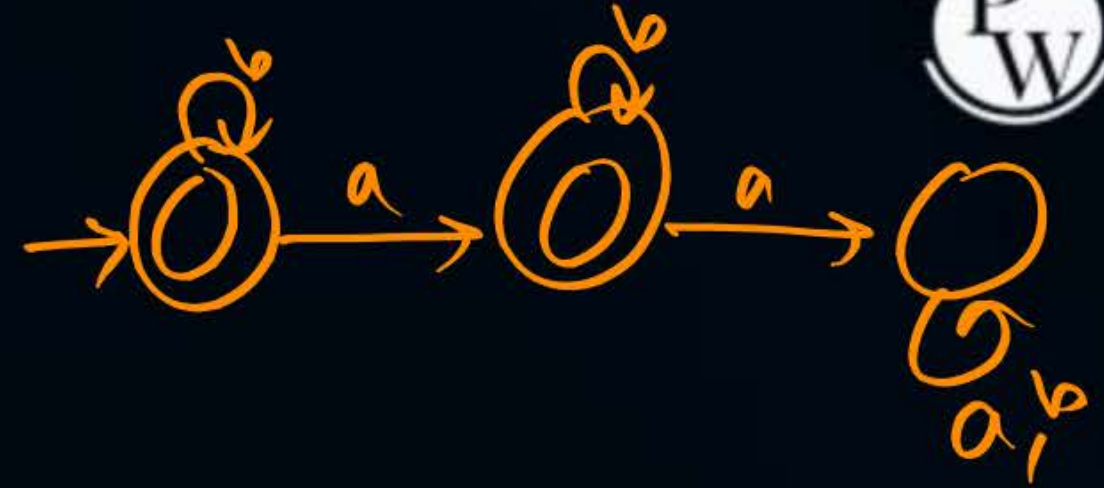




## Construction of DFA

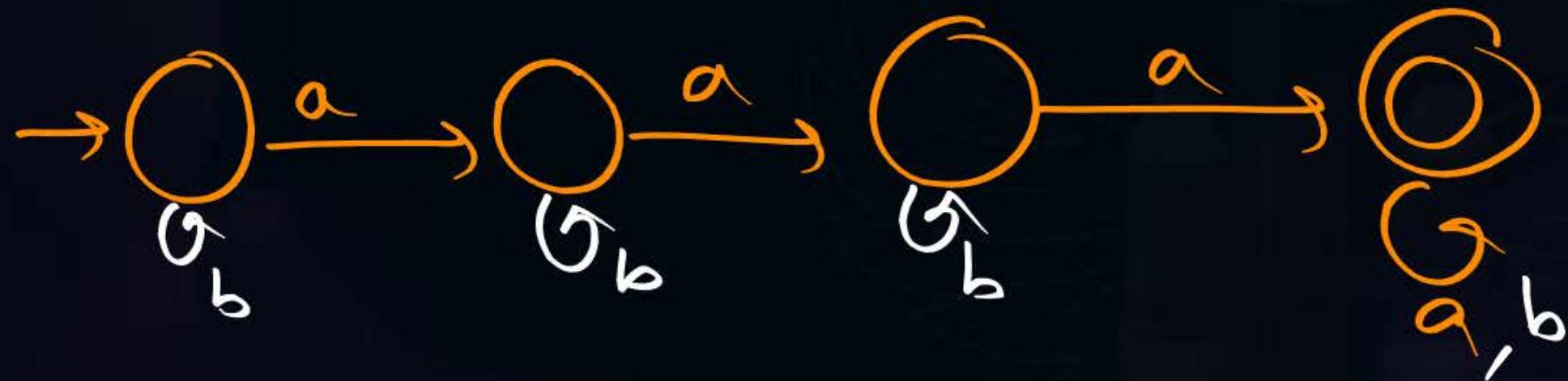


(24)  $\{w \mid w \in \{a, b\}^*, n_a(w) < 2\}$   
= 3 states  
 $n_a(w) \leq 1$



(25)  $\{w \mid w \in \{a, b\}^*, n_a(w) > 2\}$   
= 4 states  
 $n_a(w) \geq 3$

= 4 states



Note:  $\rightarrow$  No. of 'a's in string  $w$

$$\text{I) } n_a(w) = K \Rightarrow$$

$\rightarrow$  constant

No. of states in min DFA

$$K+2$$

$$\text{II) } n_a(w) \leq K \Rightarrow K+2$$

$$\text{III) } n_a(w) \geq K \Rightarrow K+1$$

$$\text{IV) } n_a(w) < K \Rightarrow K+1$$

$$\text{V) } n_a(w) > K \Rightarrow K+2$$



Σ={a}

(26)

$$L = \{a^n \mid n \geq 0\} = a^* = \Sigma^* \rightarrow$$



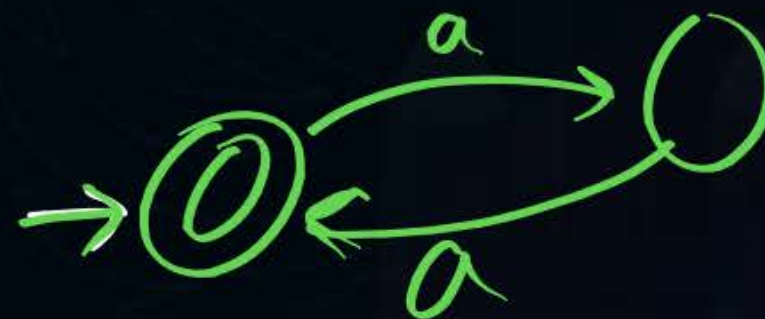
(27)

$$L = \{a^n \mid n \geq 1\} = a^+$$



(28)

$$L = \{a^{2n} \mid n \geq 0\} = (aa)^*$$



$$= \{\epsilon, a^2, a^4, a^6, \dots\}$$

# Arithmetic progression Series:

I)  $0, 1, 2, 3, \dots$

II)  $2, 3, 4, 5, \dots$

III)  $0, 2, 4, 6, 8, \dots$

IV)  $0, 3, 6, 9, 12, \dots$

V)  $10, 20, 30, 40, \dots$   


$$\{a^n \mid n \geq 0\}$$

$$\{a^n \mid n \geq 2\}$$

$$\{a^{2n} \mid n \geq 0\}$$

$$\{a^{3n} \mid n \geq 0\}$$

$$\{a^{10n} \mid n \geq 1\}$$



## Not A.P. Series:

$$\text{I) } n! : 0!, 1!, 2!, 3!, \dots \quad a^{n!}$$

$$\text{II) } 2^n : 2^0, 2^1, 2^2, 2^3, \dots \quad a^{2^n}$$

$$\text{III) } n^2 : 0^2, 1^2, 2^2, 3^2, \dots \quad a^{n^2}$$

$$\text{IV) } n^n : 1^1, 2^2, 3^3, 4^4, \dots \quad a^{n^n}$$

$$\text{V) } \text{Prime} : 2, 3, 5, 7, 11, \dots \quad a^{\text{Prime}}$$

## Construction of DFA

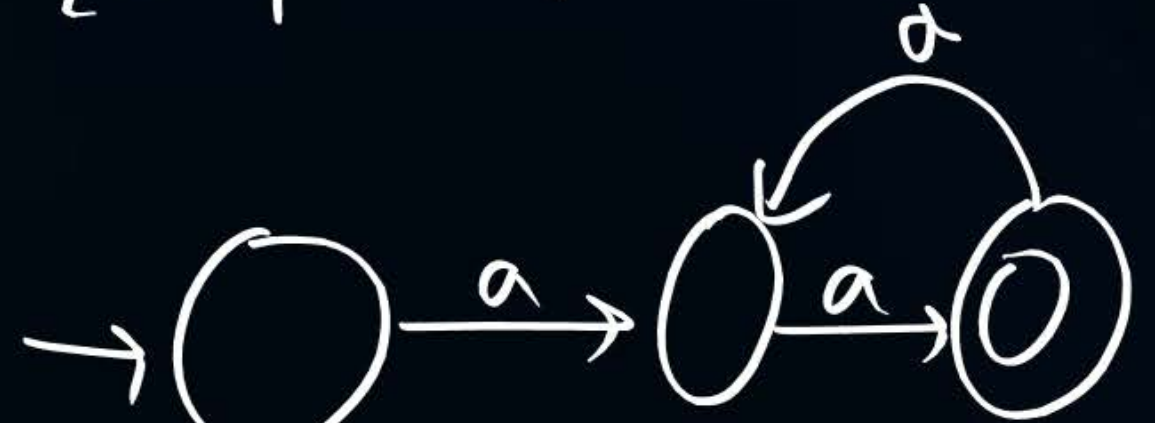


(29)  $\{a^{3n} \mid n \geq 0\}$

(30)  $\{a^{3n+2} \mid n \geq 0\}$

(31)  $\{a^{3n+5} \mid n \geq 0\}$

(32)  $\{a^{2n} \mid n \geq 1\}$







## 2 mins Summary



Topic

Length based problems

Topic

Symbol based problems

Topic

One symbol based problems  $\Rightarrow$  Next



**THANK - YOU**