

BM

## Determinants:-

$$\begin{vmatrix} 2 & 4 \\ 3 & 1 \end{vmatrix} = 2 \times 1 - 3 \times 4 = 2 - 12 = -10$$

$$\begin{vmatrix} 3 & 2 & 1 \\ 3 & 2 & 2 \\ 2 & 1 & 2 \end{vmatrix} = 3(2 \times 2) - 3(2 \times 2) + 2(1 \times 2) = 12 - 12 + 4 = 4$$

## Properties of determinants:-

- (i) In a determinant if row or a column is interchanged then the value of determinant does not change.

ex:-

$$\begin{vmatrix} 2 & 3 & 6 & 8 \\ 0 & 1 & 5 & 7 \\ 4 & 5 & 10 & 12 \end{vmatrix} = 10 - 12 = -2$$

$$\begin{vmatrix} 2 & 4 & 6 & 8 \\ 0 & 1 & 5 & 7 \\ 3 & 5 & 10 & 12 \end{vmatrix} = 10 - 12 = -2$$

(iii)

If two rows or two columns are interchanged, the sign is changed.

Ex :-

$$\begin{vmatrix} 2 & 7 \\ 6 & 3 \end{vmatrix} = 6 - 42 = -3$$

$$\begin{vmatrix} 7 & 2 \\ 3 & 6 \end{vmatrix}$$

$$= 42 - 6 = 36$$

(iii) If all the diagonal elements are same

If two rows or two columns of a determinant are same, the value of a determinant is zero.

$$\begin{vmatrix} 2 & 2 & 2 \\ 2 & 2 & 2 \end{vmatrix} = 0$$

(iv)

If all elements of any rows or any column is zero, the value of determinant is zero.

$$\begin{vmatrix} 2 & 0 & 2 \\ 3 & 0 & 1 \\ 4 & 0 & 2 \end{vmatrix} = 0$$

(V)

Ex:-

$2 \times 2$

$3$

$2 \times 3$

$4$

$= 8 - 6 = 2$

$4$

$3$

$= 2 \times 2$

$4 \quad 4$

$= 16 - 12 = 4$

(vi)

Minor of a determinant :-

$2 \quad 3$

$4 \quad 1 \quad 3$

$5$

$M_{11} = 3$

$8 \quad 5 \quad 3$

$M_{12} = 4$

$M_{21} = 3$

$M_{22} = 2$

$2 \quad 3 \quad 4$

$= M_{11} =$

$2 \quad 8$

$(8 \quad 6)$

$6 \quad 2 \quad 8$

$-1 \quad 16$

$6 \quad 5 \quad -8$

$M_{11} = 20 + 8 = 28$

$M_{12} = 4$

$M_{13} = -20$

$M_{21} = 34$

$M_{22} = -8$

→ The minor of a determinant is defined as a determinant obtained by deleting the row and column containing the element.

Co-factor :-

$$(-1)^{i+j} \times \text{minor } (m_{ij})$$

→  $i+j = \text{even}$ ,  $= (+)$  sign

$i+j = \text{odd}$ ,  $= (-)$  sign

	2	3	4	
	6	2	8	$\Rightarrow$
	7	-1	10	

$$C_{11} = (28)$$

$$C_{12} = -4$$

$$C_{13} = -20$$

$$C_{21} = -34$$

Q.1 The minors and Co-factor of -4 and 9 in determinant

$$\begin{vmatrix} -1 & 2 & 3 \\ -4 & 5 & -6 \\ -7 & -8 & 9 \end{vmatrix}$$

$$M_{21} = \begin{vmatrix} 2 & 3 \\ -8 & 9 \end{vmatrix} = 18 + 24 = 42$$

$$C_{21} = -42$$

$$M_{33} = \begin{vmatrix} -1 & 2 \\ -4 & 5 \end{vmatrix} = -5 + 8 = 3$$

$$C_{33} = 3$$

$$q_1x + b_1y + c_1z = d_1$$

$$q_2x + b_2y + c_2z = d_2$$

$$q_3x + b_3y + c_3z = d_3$$

$$D = \begin{vmatrix} q_1 & b_1 & c_1 \\ q_2 & b_2 & c_2 \\ q_3 & b_3 & c_3 \end{vmatrix}$$

$$D_1 = \begin{vmatrix} d_1 & b_1 & c_1 \\ d_2 & b_2 & c_2 \\ d_3 & b_3 & c_3 \end{vmatrix}$$

$$D_2 = \begin{vmatrix} q_1 & d_1 & c_1 \\ q_2 & d_2 & c_2 \\ q_3 & d_3 & c_3 \end{vmatrix}$$

$$D_3 = \begin{vmatrix} q_1 & b_1 & c_1 \\ q_2 & b_2 & c_2 \\ q_3 & b_3 & c_3 \end{vmatrix}$$

$$D_4 = \begin{vmatrix} q_1 & b_1 & d_1 \\ q_2 & b_2 & d_2 \\ q_3 & b_3 & d_3 \end{vmatrix}$$

$$D_5 = \begin{vmatrix} q_1 & d_1 & c_1 \\ q_2 & d_2 & c_2 \\ q_3 & d_3 & c_3 \end{vmatrix}$$

$$x = \frac{D_1}{D}, \quad y = \frac{D_2}{D}, \quad z = \frac{D_3}{D}$$

Solve the following equation by using  
cramer's rule:-

$$2x - 3y + 4z = -9$$

$$-3x + 4y + 2z = -12$$

$$4x - 2y - 3z = -3$$

$$D = \begin{vmatrix} 2 & -3 & 4 \\ -3 & 4 & 2 \\ 4 & -2 & -3 \end{vmatrix}$$

$$= 2 \begin{vmatrix} -12+4 & +3 \end{vmatrix}$$

$$= -16 + 3 - 40 = \underline{-53} \quad \begin{matrix} 9-8 \\ +4 \\ +6-16 \end{matrix}$$

$$D_1 = \begin{vmatrix} -9 & -3 & 4 \\ -12 & -4 & 2 \\ -3 & -2 & -3 \end{vmatrix}$$

$$D_1 = -9 \begin{vmatrix} 4 & 2 & +3 \\ -8 & -3 & -6 \end{vmatrix} - 3 \begin{vmatrix} -12 & 4 \\ -3 & -2 \end{vmatrix}$$

$$= 4 \begin{vmatrix} -12 & 4 \\ -3 & -2 \end{vmatrix}$$

$$D_1 = -9 [-12 + 4] + 3 [+36 + 6] + 4 [+24 + 12]$$

$$D_1 = -9 [-8] + 3 [-18] + 4 [+34]$$

$$D_1 = 72 + (-18) + 4 \times 34$$

$$D_1 = 72 - 138 \\ D_1 = -66$$

$$D_1 = 348$$

$$x = \frac{D_1}{D} = \frac{342}{-53}$$

$$D_2 = \begin{vmatrix} 2 & -9 & 4 \\ -3 & -12 & 2 \\ 4 & -3 & -3 \end{vmatrix}$$

$$D_2 = 2[36+6] + 9[-9+8] + 4[9+48]$$

$$D_2 = 84 + 9 + (57 \times 4)$$

$$D_2 = 84 + 9 + 228$$

$$D_2 = 321$$

$$y = \frac{D_2}{D} = \frac{321}{-53}$$

$$D_3 = \begin{vmatrix} 2 & -3 & -9 \\ -3 & 4 & -12 \\ 4 & -2 & -3 \end{vmatrix}$$

$$D_3 = 2 \begin{vmatrix} -12+24 \end{vmatrix} + 3 \begin{vmatrix} 9+48 \end{vmatrix} + (-9) \begin{vmatrix} -6-16 \end{vmatrix}$$

$$D_3 = 2(12) + 3(57) - 9(-22)$$

$$D_3 = \cancel{24} + \cancel{186} + \cancel{188} \quad 189 \quad z = \frac{189}{-53}$$

Q.1 Solve using cramer's rule:-

$$\begin{aligned} 5x - 7y + z &= 11 \\ 6x - 8y - z &= 15 \\ 3x + 2y - 6z &= 7 \end{aligned}$$

$$\begin{array}{|ccc|} \hline & x & x \\ \text{D} = & \left( \begin{array}{ccc} 5 & -7 & 1 \\ 6 & -8 & -1 \\ 3 & 2 & -6 \end{array} \right) & \left( \begin{array}{ccc} 48 & -1 \\ -36 & 3 \\ 12 & 24 \end{array} \right) \\ \hline & 48 & -1 \\ & -36 & 3 \\ & 12 & 24 \\ \hline & 8 & 1 \\ & 12 & 18 \\ & 12 & 18 \\ \hline & 0 & 0 \end{array} = 55$$

$$|D| = 5 [48 + 2] + 7 [-36 + 3] + 1 [12 + 24]$$

$$D = 250 + (-231) + 36$$

$$\begin{array}{r} D = \\ \cancel{+} \begin{array}{r} 286 \\ 231 \\ \hline 517 \end{array} \end{array} \quad \begin{array}{l} 286 \\ 231 \\ \hline 55 \end{array}$$

$$D = 55$$

$$(L) \quad 81 - 10 \quad 8 + 1 + 61 \quad 6 = 55$$

$$(L) \quad 10 - 10 = 10 \quad 1 + 61 = 61$$

$$10 - 10 = 10 \quad 1 + 61 = 61$$

$$D_1 = \begin{vmatrix} 11 & -7 & 1 \\ 15 & -8 & -1 \\ 7 & 2 & -6 \end{vmatrix}$$

$$D_1 = 11 [48 + 2] + 7 [-90 + 7] + 1 [30 + 56]$$

$$D_1 = 555 + (-63 \times 7) + 86$$

$$D_1 = +55$$

$$x = \frac{D_1}{D} = \frac{55}{55} = 1$$

$$D_2 = \begin{vmatrix} 5 & 11 & 1 \\ 15 & -1 & -55 \\ 7 & -6 & 6 \end{vmatrix}$$

$$y = -1$$

$$D_3 = \begin{vmatrix} 5 & -7 & 11 \\ 6 & -8 & 15 \\ 3 & 2 & 7 \end{vmatrix} = -55$$

$$z = -1 = \frac{D_3}{D}$$

matrices:-

let us consider a set of  
simultaneous equations

$$3x + 2y + 4z = 0$$

$$2x + 3y + 8z = 0$$

$$5x + 4y + 7z = 0$$

→ coefficient of variables close in square bracket, we call them bracket, the above system of numbers arranged in a rectangular array in rows and columns and bounded by bracket is called a matrix:

$$A = \begin{bmatrix} 3 & 1 & 4 \\ 2 & 3 & 8 \\ 5 & 4 & 7 \end{bmatrix}$$

## Types of matrices:-

(i)

### Row matrix:-

If a matrix has only one row and any numbers of columns is called row matrix.

Ex:-

$$\begin{bmatrix} 2 \\ 3 \\ 3 \\ 2 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 3 & 4 & 7 \end{bmatrix}_{1 \times 4}$$

(ii)

### Column:-

one column, and any number of rows is known as column matrix

Ex:

$$\begin{bmatrix} 2 \\ 4 \\ 8 \\ 7 \end{bmatrix}_{4 \times 1}$$

$m \times n$   
↓  
row column

(iii)

### Null matrix [zero]:-

In which all the elements are zero called null or zero matrix.

(iv)

Square matrix:-

A matrix in which the number of columns is equal to = no. of rows is called square matrix

(v)

Diagonal matrix:-

A square matrix is called diagonal matrix, if all non diagonal are zero.

Ex:-

$$\begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \end{bmatrix}$$

(vii) unit or identity matrix:-

A square matrix is called unit or identity matrix if all diagonal elements are one and all non-diagonal are zero.  $[I]$ .

$$I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad 3 \times 3$$

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad 2 \times 2$$

$\therefore$  Basic formula:-

$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$(a-b)^2 = a^2 + b^2 - 2ab$$

$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$a^2 - b^2 = (a+b)(a-b)$$

$$a^3 + b^3 = (a+b)(a^2 + b^2 - ab)$$

$$a^3 - b^3 = (a-b)(a^2 + b^2 + ab)$$

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$3x^2 + 9x - 4 = 0$$

$$x^2 - 5x + 6 = 0$$

$$x^2 - 3x - 2x + 6 = 0$$

$$x(x-3) - 2(x-3) = 0$$

$$(x-2) = 0 \quad (x-3) = 0$$

$$x = 2, \quad x = 3$$

~~$$x^2 - 2x - 15 = 0$$~~

~~$$x^2 + 5x - 3x - 15 = 0$$~~

~~$$x(x+5) - 3(x+5) = 0$$~~

~~$$x = -5, \quad x = 3$$~~

$$x^2 - 5x + 3x - 15$$

$$x(x-5) + 3(x-5)$$

$$x = 5, \quad x = -3$$

$$x^2 + 10x + 25 = 0$$

$$x^2 + 5x + 5x + 25 = 0$$

$$x(x+5) + 5(x+5) =$$

$$x = -5, -5$$

$$\begin{cases} (x+5)^2 = 0 \\ (x+5) = 0 \end{cases}$$

$$x^2 - 48x + 576 = 0$$

$$x = 48 + \sqrt{(48)^2 - 4 \times 1 \times 576} \\ 2 \times 1$$

$$x = 48 + \sqrt{1404} \\ = 48 + 37.5 \\ = 85.5$$

$$x^2 - 24x - 240 + 576 = 0 \\ x(x - 24) - 24(x - 24) = 0$$

$$(2x - 24)^2 = 0$$

$$2x^2 - 12x + 144 = 0 \\ x^2 - 6x + 72 = 0$$

$\rightarrow$  remainder theorem

$$2x = 2$$

$$8 - 36 + 72 - 32 = 0 \\ 80 - 80 = 0$$

$$x = 1 - 36 + 72$$

$$(2x - 2) = 0$$

$$2 - 2 \\ \int 2x^3 - 12x^2 + 36x - 32 (2x^2 - 10x + 16 \\ 2x^3 - 2x^2$$

$$+ \quad \quad \quad - 11 \\ - 10x^2 + 36x - 32$$

$$- 10x^2 + 20x \\ + \quad - \quad \quad 2x^2 - 10x + 16$$

$$\frac{16}{6} (x - 3)(x - 8) \\ m - 3 \\ m - 8 \\ m_1 m_2 - 8(m_1 - 2)$$

27 + 9 - 63

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$$x^3 + 2x^2 - 21x - 45 = 0$$

$$x = 1$$

$$1 + 1 - 21 - 45$$

$$x = -2$$

$$x = 3$$

$$8 + 4 + 42 - 45 = 5$$

$$x + 3 = 0$$

$$x^3 + 2x^2 - 21x - 45$$

$$x^2 - 2x -$$

$$0 = 05 - 2x^2 - 21x - 45$$

$$-9x^2 - 6x$$

$$-15x - 45$$

$$-18x$$

6

$$x^2 - 2x - 15 = 0$$

$$x^2 + 3x - 5 = 0$$

$$x = -3, m = 5$$

$$1 + 1 - 21 - 45$$

$$x + 3 = 0$$

$$1 + 1 - 21 - 45$$

$$2x^3 - 6x^2 + 9x - 4 = 0$$

$$x = 1 \quad 1 - 6 + 9 - 4 \\ 1 - 6 + 9 - 4 = 0$$

$$x = -1 \quad -1 - 6 + 9 - 4 \\ -1 - 6 + 9 - 4 = 0 \quad (x - 1) = 0$$

$$x = 2 \quad 2 - 6 + 9 - 4 \\ 2 - 6 + 9 - 4 = 0 \quad (x - 2) = 0$$

$$x = -2 \quad -2 - 6 + 9 - 4 \\ -2 - 6 + 9 - 4 = 0 \quad (x + 2) = 0$$

-15

$$8 - 2x^4 + 18x^4 x^5 - 1 + 4x$$

$$= 8 - 2x^4 + 18x^4$$

$$(x^3 - 2x^2 + 5x + 1)^2 + (x^2 - 5x + 4)$$

$$(x - 1) 2x^3 - 6x^2 + 9x - 4 (x^2 - 5x + 4)$$

$$\cancel{2x^3} + \cancel{2x^2}$$

$$-5x^2 + 9x - 4$$

$$+ \cancel{-10x^2 + 18x}$$

$$4x^2 - 4$$

$$\cancel{4x^2} + \cancel{4} \\ 0 \quad 2x^2 - 5x + 4$$

$$2x^2 - 5x^2 + 5x + 4 \\ 2x^2 - 5x^2 + 5x + 4$$

$$2x^2 - 2x^2 + 5x + 4 \\ 2x^2 - 2x^2 + 5x + 4$$

$$x = 1 \quad x = 4$$

$$2x^3 + 2x^2 - 81x - 45 = 0$$

$$2x = 1$$

$$1 + 1 - 21 - 45 \leftarrow 0$$

$$2x = -1$$

$$2x = -45$$

$$2x = 2$$

$$2x = 45 \cancel{+} 0$$

$$8 + 4 - 42 = -2$$

$$2x = -2$$

$$-8 + 4 + 42 = 45$$

$$46 = 45$$

$$2x = 3$$

$$27 + 9 - 63 = 45 \cancel{+} 0$$

$$-50 = 45$$

$$27 + 9 - 63 = 45 \cancel{-} 0$$

$$-50 = 45$$

$$2x = -3$$

$$2x = -45$$

$$(2x + 3)(2x^2 + 2x - 21) = 45$$

$$2x^3 + 3x^2 -$$

$$-$$

$$2x^3 + 3x^2 -$$

$$x^2 - 2x - 15 = 0$$

$$x^2 - 5x + 3x - 15 = 0$$

$$x(x - 5) + 3(x - 5) = 0$$

$$(x - 5) = 0, (x + 3) = 0$$

$$x = +3, x = 5, x = -3$$

Natural numbers :-

Counting numbers

1, 2, 3, 4, ... are called natural numbers.

Whole numbers :-

All counting numbers put together together within 0 from the set of all whole numbers.

Even numbers:- A number divisible by 2 is called Even number

Ex:- 2, 4,

odd numbers:- Not divisible by 2 is called odd numbers

Ex:- 1, 3, 5, 7

prime numbers:-

A number greater than 1 which is called a prime number. If it has exactly two factors namely 1 and number itself

composite numbers:-

A number greater than one which are not prime are known as composite number

~~2 is the only even number which is prime~~

There are 25 prime numbers b/w 1 - 100

Types of divisibility:

(i) divisibility by 2.

A number is divisible by 2 if its unit digit is any of 0, 2, 4, 6, 8

(ii) divisibility by 3 →

<u>2</u>	<u>64, 128, 412, 624</u>
<u>2</u>	<u>32, 64, 206, 312</u>
<u>2</u>	<u>16, 32, 153, 156</u>
<u>2</u>	<u>8, 16, 153, 78</u>
<u>2</u>	<u>4, 8, 153, 39</u>
<u>2</u>	<u>2, 4, 153, 39</u>
<u>2</u>	<u>1, 2, 153, 39</u>
<u>3</u>	<u>1, 1, 153, 39</u>
<u>3</u>	<u>1, 1, 51, 13</u>
<u>12</u>	<u>1, 1, 17, 13</u>
<u>12</u>	<u>1, 1, 17, 13</u>

$$\text{HCP} \quad 2 \times 2 \times 2 \times 3 = 24$$

$$\text{LCM} = 2x -$$

Q1.

$$896 \times 896 - 204 \times 204$$

$$A^2 - B^2$$

$$(A+B)(A-B)$$

$$(896+204) (896-204)$$

$$1090$$

$$1100 - 692 = 410$$

$$\begin{array}{r} 1100 \times 692 \\ \hline 660600 \\ 660600 \\ \hline 761200 \end{array}$$

$$387 + 114 = 501 \quad (387 + 114) \times 114 = 114 \times 114 + 2 \times 387 \times 114$$

$$= 114$$

$$(387 + 114)^2 = [501]^2$$

$$387 + 114 = 501$$

$$\begin{array}{r} 387 \\ + 114 \\ \hline 501 \end{array}$$

Inverse of a matrix :-

$$(A - I)(A^{-1}) = \frac{\text{adj } A}{|A|}$$

$$A = \begin{bmatrix} 2 & 3 & 4 \\ 0 & 2 & 8 \\ 4 & -1 & 10 \end{bmatrix}$$

$$|A| = 2(20 + 8) - 3(60 - 56) + 4(-6 - 16)$$

$$|A| = 56 - 12 - 80$$

$$(16 \times 2) - (16 \times 4) + (-4 \times 8)$$

$$|A| = 9 - 36 \neq 0$$

$$\text{adj } A = \begin{bmatrix} 28 & -4 & 9 - 20 \\ -34 & -8 & 23 \\ 16 & 8 & -4 \end{bmatrix}$$

→ matrix obtained by the co-factors of A

$$\text{adj} \cdot A = \begin{bmatrix} 28 & -34 & 16 \\ -4 & -8 & 8 \\ -20 & 23 & -14 \end{bmatrix}$$

$$A^{-1} = \frac{\text{adj} \cdot A}{|A|}$$

$$\begin{bmatrix} \frac{28}{36} & \frac{-34}{36} & \frac{16}{36} \\ \frac{-4}{36} & \frac{-8}{36} & \frac{8}{36} \\ \frac{-20}{36} & \frac{23}{36} & \frac{-14}{36} \end{bmatrix}$$

$$c_1(c_1-n) + 81 = PD$$

$$c_1 - n c_1 + 81 = PD$$

$$A^{-1} = \frac{1}{36} \begin{bmatrix} 28 & -34 & 16 \\ -4 & -8 & 8 \\ -20 & 23 & -14 \end{bmatrix}$$

A.P.

$$3, 4, 6, 8 \dots n$$

$$a_n = a + (n-1)d = 1 + 6(n-1)$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

How many numbers between  
11 and 90 are divisible by 9

$$18, 27, \dots 81$$

$$a = 18, d = 9$$

Ans

$$81 = 18 + (n-1)9$$

$$81 = 18 + 9n - 9$$

odd - numbers sum 100.

1, 3, 5, 7, ... 99

$$\text{Sum} = 1 + (n-1)2$$

$$99 = 1 + 2n - 2$$

$$99 = -1 + 2n$$

$$98 = 2n$$

$$(1 - 99) + 51 n = 50$$

$$-98 + 51 = -47$$

$$n = 24$$

$$S_n = \frac{0 + 49}{2} [2 \times 1 + (49-1)2]$$

$$S_n = \frac{49}{2} [2 + 96]$$

$$S_n = \frac{49}{2} \times 98$$

~~$$S_n = \frac{49 \times 46}{2 \times 4}$$~~

~~$$\frac{15 \times 46}{180}$$~~

$$S_n = \frac{50}{2} [2 \times 1 + 49 \times 2]$$

$$S_n = 25 (100 = 2500)$$

Find the sum of 911  $\dots$  2 digit number which 98 divides by 3

12, 15, 18  $\dots$  99

$$a = 12, d = 3$$

$$n = 15 - 1 = 14$$

$$q_n = 12 + (14-1)3$$

$$q_n = 12 + 3(14-1)$$

$$(12 + 5) \times 14 = 50$$

$$S_n = \frac{1}{2} \times 14$$

$$S_n = \frac{1}{2} (2 \times 12 + (14-1) \times 3)$$

$$S_n = 15 [24 + 29 \times 3]$$

$$\frac{29 \times 3}{6}$$

$$S_n = 15 [24 + 67]$$

$$[24 + 67] \times \frac{1}{2} = n$$

$$S_n = \frac{1}{2} (24 + 67)$$

$$15 \times 91 = 1665$$

$$\frac{67}{91}$$

$$135 \times$$

$$540 = 240 + (n-1)60$$

$$540 = 240 + 60n - 60$$

$$540 = 180 + 60n$$

$$360 = 60n$$

$$n = 6$$

$$a, ar, ar^2, ar^3, ar^n$$

$$\frac{ar}{a} = \frac{ar}{a}$$

$$\frac{r}{r} = 1$$

$$a_n = q(r^n - 1)$$

$$a_n = q r^{n-1}$$

$$S_n = \frac{q(1-r^n)}{(1-r)}$$

in 2, 4, 8, 16, ...  $\rightarrow$  1024

$$q = 2, \quad r = \frac{q}{2} = \frac{1}{2} \quad r =$$

$$a_n = q(r^{n-1})$$

~~$$1024 = q(r^n - 1)$$~~

~~$$1024 = q^{n+1} - 1$$~~

~~$$1024 = q^{n+1}$$~~

~~$$a_n = q(r^{n-1})$$~~

~~$$1024 = q \left( \left(\frac{1}{2}\right)^n - 1 \right)$$~~

~~$$1024 = 2 \cdot \left(\frac{1}{2}\right)^{n-1}$$~~

~~$$512 = \left(\frac{1}{2}\right)^{n-1}$$~~

$$T_n = q r^{n-1}$$

$$1024 = 12 (2)^{n-1}$$

$$512 = 2^{n-1}$$

$$2^9 = 2^{n-1}$$

$$n-1 = 9$$

$$n = 10$$

$$\sim \frac{1}{N} \sim$$

$$\frac{4}{2} -$$

2.2

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Find the sum of series:-

$$2 + 2^2 + 2^3 + \dots - 2^8$$

$$q_n = 2^{n-1}$$

$$2^8 = 2^{n-1}$$

$$2^8 = 2^n$$

$$n = 8$$

$$S_n = \frac{2(1 - 2^8)}{1 - 2} = \frac{2 - 2^9}{-1}$$

$$S_n = \frac{2 - 2^9}{-1} = \frac{2 - 512}{-1}$$

$$S_n = \frac{-510}{-1} = 510$$

FIND Inverse of this matrix:

$$A = \begin{vmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{vmatrix}$$

$$|A| =$$

$$M_{11} = \begin{vmatrix} -3 & 4 \\ -1 & 1 \end{vmatrix} = -(-3+4) = 1$$

$$M_{12} = \begin{vmatrix} 2 & 4 \\ 0 & 1 \end{vmatrix} = 2 \cdot 1 - 0 = 2$$

$$M_{13} = \begin{vmatrix} 2 & -3 \\ 0 & -1 \end{vmatrix} = 2 \cdot (-1) - 0 = -2$$

$$M_{21} = \begin{vmatrix} -3 & 4 \\ -1 & 1 \end{vmatrix} = -(-3+4) = 1$$

$$M_{22} = \begin{vmatrix} 3 & 4 \\ 0 & 1 \end{vmatrix} = 3 \cdot 1 - 0 = 3$$

$$M_{23} = \begin{vmatrix} 3 & -3 \\ 0 & -1 \end{vmatrix} = -3 + 0 = -3$$

$$M_{31} = \begin{vmatrix} -3 & 4 \\ -3 & 4 \end{vmatrix} = -12 + 12 = 0$$

$$M_{32} = \begin{vmatrix} 3 & 4 \\ 2 & 4 \end{vmatrix} = 12 - 8 = 4$$

$$M_{33} = \begin{vmatrix} 3 & -3 \\ 2 & -3 \end{vmatrix} = -9 + 6 = -3$$

$$M_{11} = 1, \quad M_{12} = -2, \quad M_{13} = -2$$

$$M_{21} = -1, \quad M_{22} = +3, \quad M_{23} = +3$$

$$M_{31} = 0, \quad M_{32} = -4, \quad M_{33} = -3$$

$$\text{adj} J \cdot A = \begin{bmatrix} 1 & -2 & 2 \\ -1 & 3 & 3 \\ 0 & -4 & -3 \end{bmatrix}$$

$$\text{adj} J \cdot A = \begin{bmatrix} 1 & -1 & 0 \\ -2 & 3 & -4 \\ 0 & 3 & -3 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \text{adj} J \cdot A$$

$$A^{-1} = \begin{bmatrix} 1 & -1 & 0 \\ -2 & 3 & -4 \\ 0 & 3 & -3 \end{bmatrix}$$

## Permutation and Combination

→ let  $n$  be a positive number  
then factorial  $n$  denote,  
by →  $(n) = n!$

$n$  is define as  $n! = n \times (n-1) \times \dots \times 1$

$$(3) = 3 \times 2 = 6$$

$$(0) = 1$$

$$(4) = 24$$

$$5! = 120$$

$$6! = 720$$

### Permutation:-

The different arrangement of  $n$  given numbers by taking sum of all at a time are called permutation.

Ex:- All permutation made with the letters  $a, b, c$  by taking 2 time at a time are

$a, b, c \Rightarrow$

$(ab, bc, ac, ba, cb, ca)$

→ no. of all permutation of  $n$  things written at a time given by

$\Rightarrow$

$n_P_r$

NOTE:- number of all permutations of  $n$  things taken  $r$  at a time is factorial

$$\text{Q.1} \quad \frac{13!}{28!} = \frac{30!}{28!} - \frac{30 \times 29 \times 28!}{28!}$$

$$\begin{array}{r} 13 \\ \times 12 \\ \hline 156 \end{array} \quad \begin{array}{r} 30 \\ \times 29 \\ \hline 870 \end{array}$$

$$\begin{array}{r} 13 \\ + 29 \\ \hline 42 \\ \times 29 \\ \hline 120 \\ + 870 \\ \hline 1000 \end{array}$$

→ FIND the value of

$$P_{28} =$$

$$60! \\ 32!$$

:combinations:-

Each of different groups or selection which can be formed by taking some or all of a number of objects is called a combination.

Ex:- Suppose we want to select 2 out of 3 boys A, B, C then possible selection are

AB, BC, CA

→ Note that AB and BA represent same selection

→ The number of combinations of  $n$  things taken at a time is

$nC_2$

Estimate the number of ways in which we can select a team of 10 players from 15.

$$\text{Required number of ways} = \frac{15!}{(15-10)!} = \frac{15!}{5!}$$

$\rightarrow$  Note than  $n^c_n = 1$ ,  $n^c_0 = 1$

$\rightarrow$  Find the value of

$$10^c_3 = \frac{10!}{3!7!}$$

$$\begin{aligned} & 10 \times 9 \times 8 \times \frac{3!}{3!} \\ & 10 \times 8 \times \frac{9 \times 8 \times 7 \times 6 \times 5 \times 4}{3 \times 2} = \frac{(10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4)}{3 \times 2} \\ & 120 \end{aligned}$$

$\rightarrow$  In how many ways can a cricket team of 10 be selected out of 15 players?

$$\text{Required number of ways} = \frac{15!}{(15-10)!} = 15!$$

$$14! 4!$$

$$\begin{array}{r} 2 \\ 15 \times 14 \times 13 \times 12 \\ 4 \times 3 \times 2 \end{array}$$

$$15 \times 14 \times 13 \times 12$$

$$180 \times 13$$

$$\begin{array}{r} 2 \\ 180 \times 13 \\ 540 \end{array}$$

$$\begin{array}{r} 3 \\ 360 \end{array}$$

in how many ways a committee  
of 5 men and 5 ladies  
constituting of 3 men  
and 2 ladies

$$6c_3 \times 5c_2$$

$$3! \times 3! \quad 2! \times 3!$$

$$2$$

$$6 \times 4 \times 3! \quad * \quad 5 \times 4 \times 3!$$

$$3 \times 2 \times 1$$

$$90 \times 10 = 900$$

→ How many words can be  
form by using all the  
letters of word Bihar.

$$5! = 120$$

Evaluate

$$28\% \text{ of } 450 + 45\% \text{ of } 100$$

0.82

$$450 \times 28 + 280 \times 45$$

100  
100

$$\{ 450 \times 28 + 280 \times 45 \}$$

12

$$12600$$

R

100

12600

2 is what % of 50

$$\frac{2}{50} \times 50$$

$$2 = \frac{2 \times 2}{100}$$

difference of two numbers  
is 1660. If 7.5%  
of one number is 12.  
of the other number  
Find the 2 numbers

$$x - y$$

$$x - y = 1660$$

$$\frac{7.5}{100} x = \frac{12.5}{100} y$$

$$75x = 125y$$

$$x = \frac{125y}{75}$$

$$x = \frac{5y}{3}$$

$$\frac{5y}{3} - y = 1660$$

$$5y - 3y = 1660 \times 3$$

$$2y = \frac{1660 \times 3}{4} - 280$$

$$2y = 4980$$

$$y = \frac{4980}{2} = 2490$$

$$2490$$

$$2x = 1660 + 2490$$

$$2x = 2900$$

$$1660$$

$$4150$$

a)

If the G.S.T. be reduced from  $\frac{7}{2} \text{ of } 10\%$  to  $\frac{1}{3} \text{ of } 10\%$ , what difference does it make to a person who purchases an artificial lamp at a marked price of ₹ 84.00

$$\left( \frac{84.00 \times \frac{7}{2}}{100} \right) - \left( \frac{84.00 \times 10}{300} \right)$$

$$\left( \frac{84 \times 7}{200} \right) - \left( \frac{84 \times 10}{300} \right)$$

$$(42 \times 7) - (284 - 280) = 14$$

$$S.I. = \frac{T \times R \times P}{100}$$

Find the simple I

$$P = 68000$$

$$R = \frac{50}{3} \text{ %}$$

T = 1 year for

g.m.c.

$$S.I. = 68000 \times \frac{50}{3} \times \frac{1}{12} = 34000$$

100

Ques. 1. A sum of money at simple interest amounts to Rs. 201 in 2 years and to Rs. 205 in 4 years. Find the sum and the rate percent.

$$S.I. = 680 \times \frac{50}{3} \times \frac{1}{12} = 34000$$

$$S.I. = 680 \times \frac{50}{3} \times \frac{1}{12} = 34000$$

$$100 = 17000$$

→ Find the S.I. on rupees = 3000

at the rate =  $\frac{24}{4}$  per year  
for the period of 3 years

4th feb 2005

18th Mar 2005

on 3000 at 6% per annum for 3 years

on 3000 at 6% per annum for 3 years

S.I. =  $\frac{P \times R \times T}{100}$

$$S.I. = \frac{3000 \times 6 \times 3}{100} = 540$$

$$S.I. = 3000 \times 6 \times \frac{3}{100} = 540$$

$$S.I. = 3000 \times 6 \times \frac{3}{100} = 540$$

$$S.I. = 3000 \times 6 \times \frac{3}{100} = 540$$

on 3000

on 3000

on 3000

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- compound interest -

$$A = P \left(1 + \frac{r}{100}\right)^n$$

$$C.I. = A - P$$

→ First we find A.

Find compound Interest on  
Rs. = 7500, 4% per annum

for 2 years compound annually.

$$P = 7500 \quad C.I. = ?$$

$$r = 4\% \quad C.I. = ?$$

$$n = 2$$

$$A = P \left(1 + \frac{r}{100}\right)^n \quad C.I. = ?$$

$$A = 7500 + 1 + \frac{4}{100} + 4 \times 4$$

$$A = 7500 + 1 + \frac{4}{100} + \frac{4}{100}$$

$$5000 + \frac{4}{100}$$

$$A = 7500 + 1 + \frac{4}{25} + \frac{2}{25}$$

$$A = 7500 + 1 + 1 + \frac{1}{25} + \frac{2}{25}$$

$$A = 300 \times 26 \times \frac{26}{25}$$

$$\cancel{\frac{600}{600}} \times \cancel{\frac{600}{600}}$$

$$A = 8112$$

$A = 10000$ ,  $T = 2$  years,  $r = 4\%$ ,  
compounded half yearly :-

$$A = 10000 \left(1 + \frac{2}{100}\right)^4$$

$$A = 10000 \left(1 + \frac{1}{50}\right)^4$$

$$A = 10000 \left(\frac{51}{50}\right)^4$$

$$A = 10000 \times \frac{51 \times 51 \times 51 \times 51}{50 \times 50 \times 50 \times 50}$$

$$A = \left(\frac{51^4}{50^4}\right) 10000$$

$$A = \underline{\underline{51 \times 51 \times}}$$

$$\begin{array}{r} 151 \\ \times 255 \\ \hline 2601 \end{array}$$

$$2601 \times 51$$

$$\begin{array}{r} 9601 \\ \times 1305 \\ \hline 139651 \end{array}$$

$$\begin{array}{r} 1132 \\ \times 132651 \\ \hline 1633955 \end{array}$$

$$\begin{array}{r} 6763901 \\ \hline 6763901 \end{array}$$

$$I = 824.32 \quad | \quad 6765281 = \frac{6765281}{625}$$

$$\begin{array}{r} 125 \times 5 \\ \hline 125 \times 5 \end{array} = 10824.3216$$

(iii) when the interest compounds quarterly:

$$A = P \left( 1 + \frac{\gamma}{4 \times 100} \right)$$

$$0.00 = 0$$

Find the compound interest P = 16000

$\gamma = 30^\circ$ . per quantum for

9 months compare quality

$$A = 16000 \left( 1 + \frac{5}{4 \times 100} \right)$$

$$A = 16000 \left( 1 + \frac{1}{20} \right)^3$$

$$A_1 = \left( 6000 \left( \frac{21}{20} \right) \right)$$

$$A = \frac{16000 \times \frac{21}{26} + \frac{21}{26} \times 21}{2 \times 10}$$

$$A = \cancel{1444 \times 21 \times 16} = 18512$$

$$A = 441 \times 21$$

$$\begin{array}{r} 144 \\ \times 882 \\ \hline 930 \end{array}$$

~~80301 X 16.~~  
~~55806~~  
~~930 X 816~~

Ans

→ If the simple interest sum of money at 5% per annum for 3 years is 12000, find the compound interest on the same sum, for the same time.

$$\text{P} = \frac{12000}{(1 + \frac{5}{100})^3}$$

$$12000 = 3 \times m \times 5$$

$$12000 = 15 \times m$$

$$m = \frac{12000}{15}$$

$$m = 8000$$

(Q) 9261

$$A = 60000 \left(1 + \frac{8}{100}\right)^3$$

$$A = 60000$$

$$A = 60000 \times \frac{105 \times 105 \times 105}{100 \times 100 \times 100}$$

$$A = 81000 \times \frac{105 \times 105 \times 105}{100 \times 100 \times 100}$$

Ques C. → Percentage  
S.I., G.I. etc.

PTA  
→ A certain sum amounts to Rs. 8.575  
in 2 years and Rs. 10.910  
in 3 years find the sum  
and rate of interest.

$$7380 \times r \times 2 = 8575 \times 100$$

$$7380 \times 2 \times r = 8575 \times 100$$

$$\frac{7380}{100} = P_r \times 2$$

$$8575 = P_r \times \frac{100}{100}$$

$$7380 = 2P_r \quad \text{or} \quad 8575 = 3P_r$$

1200

2 + 18.20

Let the sum be  $\alpha$  rs.

$$8575 - 7380 = 1195$$

S.I. at 1 year

$$S.I. = \frac{P \times R \times T}{100}$$

$$1195 = \frac{7380 \times R \times 1}{100}$$

$$R = \frac{162}{23}$$

$$A = P \left(1 + \frac{R}{100}\right)^n$$

$$A =$$

$$7380 = x \left(1 + \frac{5}{3 \times 10}\right)$$

$$7380 = x \left(1 + \frac{5}{30}\right)$$

$$7380 = x \left(\frac{35}{30}\right) \quad 7380 = \frac{7}{6}x + x$$

$$x = \frac{7380 \times 6 \times 6}{7 \times 8 \times 5}$$

$$= 54$$

a. A sum of money to RS. 6690 after 3 years and to 10035 after 6 years on compound interest. Find the sum.

Let the sum be P

$$P \left(1 + \frac{R}{100}\right)^3 = 6690 \quad \text{--- (1)}$$

$$P \left(1 + \frac{R}{100}\right)^6 = 10035 \quad \text{--- (2)}$$

$$\frac{P \left(1 + \frac{R}{100}\right)^6}{P \left(1 + \frac{R}{100}\right)^3} = \frac{10035}{6690} = \frac{3}{2}$$

$$\left(1 + \frac{R}{100}\right)^3 = \frac{3}{2}$$

$$\left(1 + \frac{R}{100}\right) = \sqrt[3]{\frac{3}{2}}$$

$$P \times \frac{3}{2} = 6690$$

$$P = \frac{2230}{6690 \times 2} = \frac{2230}{3} = 4460$$

probability  $P(A) \rightarrow m/n$

→ where  $m$  is the number of favorable cases  
~~favorable~~  $n$  is the total no. of cases.

(Q.) Two unbiased dice are thrown  
 find the probability:-

(i) Both the dice show the same number

$\therefore P(\text{both same}) = \frac{6}{36} = \frac{1}{6}$

(ii) The first die showed 6,

$P(\text{first die } 6) = \frac{1}{6}$

(iii) The total of numbers on the dice greater than 8

(iv) The total of the numbers on the dice is 13. (6)

Sol:  $(1,1), (1,2), (1,3), (1,4), (1,5)$   
 $m(1,6)$  for 6s  $(2,1), (2,2), (2,3), (2,4), (2,5)$

$(2,6)$

$(3,1), (3,2), (3,3), (3,4), (3,5)$

$(3,6)$

$(4,1), (4,2), (4,3), (4,4), (4,5)$

$(4,6)$

$(5,1), (5,2), (5,3), (5,4), (5,5)$

→ Impossible event  $P(A) \rightarrow 0$

Q. what is prob. of getting at most two heads in tossing of three coins

$$(\{H, T\} \times \{H, T\}) \times \{H, T\}$$

$$= \{H.H, HT, TH, TT\} \times \{H, T\}$$

$$\Rightarrow \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$$

$$\Rightarrow \frac{1}{8}$$

Q. what is the chance that a leap year selected at random will contain 53 sundays.

→ in a leap year consists of 366 days, in 52 complete weeks and 2 more days

$$\begin{aligned}
 & \text{S M} \\
 & \text{M T} \\
 & \text{T W} \\
 & \text{W TH} \\
 & \text{TH fo} \\
 & \text{fo sat} \\
 & \text{sat syn} = \frac{2}{7}
 \end{aligned}$$

A B C → Are three events associated

with a random experiment

with a random experiment find  $P(A)$  given that

$$P(B) \text{ is } \frac{3}{2} \quad P(C) = \frac{1}{2} \cdot (pp)$$

$$P = P(A) + P(B) + P(C)$$

$$1 = P(A) + \frac{3}{2} + \frac{1}{2} \cdot P(B)$$

$$1 = P(A) + \frac{3}{2} + \frac{1}{2}P(P)$$

$$2 = 2P(A) + 3 + P(B) \quad | -2$$

$$\cancel{2} + 4 = 4P(A) + 6 \quad | -\frac{3}{2}$$

→ The probability of an even A is sum of numbers b/w and including 0.

→ Probability of a certain event is always 1.  
therefore

$$P(A) + P(\bar{A}) = 1$$

$$P(A) = P$$

$$P(B) = \frac{3}{2} P$$

$$P(A) + P(B) + P(C) = 1$$

$$P + \frac{3}{2} + \frac{3}{4} = 1$$

$$2i = 1$$

$$2i = 1 \Rightarrow i = \frac{1}{2}$$

$$(A_1) + (A_2) + (A_3) = 1$$

$$X_1 + X_2 + X_3 = 1$$

$$X_1 + X_2 + X_3 = 1$$

6) 198 (131)

0) 193 6) 196 (21)

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Theorem:- If A and B are any two events then

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \cap B)$$

$$(A \cap B) = P(A) + P(B) - P(A \cup B)$$

- Q. An integer is taken at random from the first 200(+) integers what is the probability that the integer is divisible by 6 and 8.

$$P(\text{Both}) =$$

$$P(A) = 6, 12, 18, \dots = 198$$

$$a_n = 33$$

$$a_n = 6 + (n-1)6$$

$$198 = 6 + (n-1)6$$

$$198 = 6 + 6n - 6 \\ = 33$$

$$A = 33$$

$$24,48$$

$$P(B) = 25$$

$$A$$

$$A \cap B = 8$$

$\Rightarrow$

$$P(A) = \frac{33}{200}$$

$$P(B) = \frac{25}{200}$$

$$P(A \cap B) = \frac{8}{200}$$

$$P(A \cup B) = \frac{33}{200} + \frac{25}{200} - \frac{8}{200}$$

$$P(A \cup B) = \frac{33}{200} + \frac{25}{200} + \frac{8}{200}$$

$$P(A \cup B) = \frac{66}{200}$$

Q.

$$P(A \cap B) = P(A) \cdot P(B)$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$n(A) = n(A \cap B) + n(A \cap B^c)$$

88

- profit and loss:-

$$\text{Graín} = \frac{S.P. - C.P.}{S.P.} = \frac{C.P.}{S.P.} = \frac{S.P. - \text{Graín}}{S.P.} = \frac{\text{Graín}}{S.P.} + \frac{C.P.}{S.P.}$$

$$\text{Gain \%} = \frac{\text{S.R. - C.P}}{\text{T.O.C}} \times 100$$

$$\text{Loss \%} = \frac{\text{Loss} \times 100}{\text{C.P.}}$$

$$SP = \frac{100 + \text{gain} \cdot c}{c}$$

$$SP = \frac{100 - loss\%}{100} \times CP$$

→ If an article is sold at gain of say 135%, then  $SP = 135\% \text{ of } CP$ ,  ~~$\frac{135}{100} CP$~~

→ If an article is loss at gain of 35%, then  $SP = 65\% \text{ of } CP$ .

→ A men buy an article for ₹ 27.50 and sells it for ₹ 28.0 find gain percent.

$$\text{gain} = 0.50$$

$$\text{gain (\%)} = \frac{0.50 \times 100}{27.50}$$

$$\text{gain (\%)} = \frac{500}{275} = \frac{100}{55}$$

$$55) \overline{100} \\ \underline{55} \\ 45$$

→ If a pen is purchase for ₹ 490 and sold for ₹ 465.50 finding the loss %.

$$\text{loss} = 490 - 465.50 = 24.50$$

$$\text{loss \%} = \frac{24.50 \times 100}{490.00}$$

$$= 2450 = 5\%$$

$$490 - 2450 = 2450$$

Find CP when S.P. = ~~56.25~~ 56.25  
Graint = 16%

$$\text{C.P.} =$$

$$SP = \frac{100 + \text{Graint}\% \times CP}{100}$$

$$56.25 = \frac{100 + 16 \times CP}{100}$$

$$562.5 = 116 \times CP$$

$$CP = \frac{562.5}{116}$$

$$CP = 48.49$$

~~Sold~~  
→ A book was sold for = 27.50  
with a profit of 10%. If  
it were sold for RS. 25.75  
find what is percentage  
of profit or loss

~~$CP = 27.50$~~

~~$S.P. = 27.50$~~

~~$S.P. = 25.75$~~

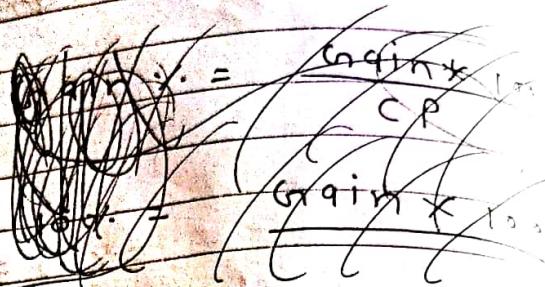
~~25.75% Profit.~~

$$CP - S.P. = \frac{27.50 - 25.75}{25.75}$$

$$S.P. = 27.50$$

$$\text{Profit} = 10\%$$

$$\text{After S.P.} = 25.75$$



$$\text{Gain} = 27.50 \times \frac{100}{110}$$

$$= 25.00$$

$$C.P. = \frac{110}{100} \times C.P. = 27.5$$

$$C.P. = \frac{27.5 \times 110}{100 \times 110}$$

$$C.P. = \frac{27.5 \times 11}{100}$$

$$C.P. = 2.75 \times 11$$

$$C.P. = 25$$

$$S.P. = 25.75$$

$$\text{Gain} = 0.75$$

$$\text{Gain \%} = \frac{0.75 \times 100}{25} = 3\%$$

→ The CP of 21 artical = SP of 18 artical  
find gain or loss.

Let the CP of 1 artical = 1

$$\cancel{10 \times \text{gain} \times 10} = 18 \times \cancel{\text{gain} \times 10}$$

$$\text{Gain \%}$$

$$\cancel{10 \times (gain + CP)} = 18 \times (gain + CP)$$

therefore SP of 18 artical = 21  
RS.

and CP of 18 artical  
RS. 18

$$21 - 18 = 3$$

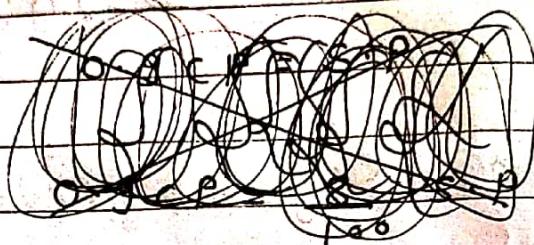
$$\text{Profit \%} = \frac{3 \times 100}{18} = \frac{300}{18}$$

$$= \frac{150}{9} . 50$$

$$\begin{array}{r}
 9) \overline{)150} \\
 9 \\
 \hline
 60 \\
 54 \\
 \hline
 6 \\
 6 \\
 \hline
 0
 \end{array}
 \quad
 \begin{array}{r}
 3) \overline{)150} \\
 3 \\
 \hline
 15 \\
 15 \\
 \hline
 0
 \end{array}$$

$$16.66 \%$$

→ monica purchased a pressure cooker  
at  $\frac{9}{10}$  th of its S.P.  
and sold it at 8% more  
than its S.P. find the  
gain %.



Let

$$S.P. = 100$$

$$C.P. = \frac{9}{10} \times 100 = 90$$

$$S.P. = 108 \times 100 - 100$$

→ A dealer sold  $\frac{3}{4}$  th of its  
artical at  $\frac{1}{4}$  gain  
of 2 days and the  
remaining artical at the cost  
price + time the gain  
by the dealer

In the end all progress

Island at bay around

3700 2002 9.17.2006

~~Pt. 4.1. (b) (i) (c) (d) (e) (f) of word~~

~~Left~~ 600000 400000

all tons C.P. = x

461-80082 201-80082

~~✓~~ 26 ✓

$$\cancel{SP} = \cancel{2e \times 100}$$

$$CP$$

$$SP = 0.1 = 0.9$$

$$SP^0 =$$

Let CP = 100

$$100 \times \frac{3}{4} = 75$$

$$\text{Chain} = \frac{75 \times 200}{100} = 15.$$

$$SP = 100 + 15 = 115$$

$$\text{gain } \gamma = 15$$

## Time and distance:

→ If  $n$  men do a piece of work in  $n$  days, then one day work of  $A = \frac{1}{n}$

Q. → worker A and B takes 8 hours and 10 hours to do the same work how long should it take both A and B working together but independently to do the same job.

$$A = 8$$

$$B = 10$$

(~~A + B~~)

$$1 \text{ hour} = \text{work of } A = \frac{1}{8}$$

$$B = \frac{1}{10}$$

Qn2 One work of A and B total =  $\frac{1}{8} + \frac{1}{10}$

$$\frac{10 + 8}{80} = \frac{18}{80}$$

$$= \frac{9}{40}$$

→ therefore A and B finish  
the work

40 Am.  
9

- Q. A and B together can complete a piece of work in 4 days. If A alone can complete the same work in 12 days, how many days can B complete this work.

~~$$A + B = \frac{1}{n}$$~~

~~$$A = \frac{1}{4}$$~~

~~$$\frac{x}{4} + \frac{1}{n} = \frac{1}{12}$$~~
~~$$x + 4n = 12$$~~

~~$$B = \left( \frac{1}{A+B} \right) - \frac{1}{A} = \frac{1}{\frac{12}{n}} - \frac{1}{4}$$~~

~~$$1 = (3 + n)$$~~

~~$$\text{one day of work} = \frac{1}{4}$$~~

~~$$6 \text{ days} A + \frac{1}{4} + \frac{1}{n} = \frac{1}{12} - \frac{1}{4}$$~~

~~$$\frac{1}{B} = \frac{1}{\frac{1}{12} - \frac{1}{4}}$$~~

do it, working ~~to~~  
 $8\frac{2}{3}$  hours per day.

$$\boxed{\frac{26}{3}}$$

$$A - = 63 \text{ hours}$$

$$B - = 42 \text{ hours}$$

$$A - \cancel{days} = \frac{1}{63}$$

$$B - \cancel{days} = \frac{1}{42}$$

therefore

$$A \rightarrow 63 \text{ hr, work} = 1$$

(a) A can complete +

$$\frac{126}{5} * \frac{8}{42} = \frac{126}{42}$$

Q. A and B can do piece of work  
in 18 days,  $B+C = 24$  days  
 $A+C = 36$  days      In how  
many days  $A, B, C = ?$

$$\frac{1}{A} + \frac{1}{B} = \frac{1}{18}$$

$$\frac{1}{B} + \frac{1}{C} = \frac{1}{24} \quad \Rightarrow \left( \frac{1}{24} - \frac{1}{C} \right)$$

$$\frac{1}{A} + \frac{1}{C} = \frac{1}{36} \quad +$$

$$A \cdot \frac{1}{C} = \frac{1}{36} - \frac{1}{A}$$

$$\frac{1}{A} + \frac{1}{24} - \frac{1}{C} = \frac{1}{18}$$

$$\frac{1}{A} + \frac{1}{24} + \frac{1}{36} + \frac{1}{A} = \frac{1}{18}$$

$$\frac{1}{A} + \frac{1}{B} = \frac{1}{18} \quad (1)$$

$$\frac{1}{B} + \frac{1}{C} = \frac{1}{24} \quad (2)$$

$$\frac{1}{A} + \frac{1}{C} = \frac{1}{36} \quad (3)$$

$$(1) + (2) + (3)$$

$$\frac{1}{A} + \frac{1}{B} + \frac{1}{B} + \frac{1}{C} + \frac{1}{A} + \frac{1}{C} = \frac{1}{18}$$

$$+ \frac{1}{24} + \frac{1}{36}$$

$$2 \left( \frac{1}{A} + \frac{1}{B} + \frac{1}{C} \right) = \frac{9}{72}$$

$$\frac{1}{A} + \frac{1}{B} + \frac{1}{C} = \frac{9}{36} \times 2$$

$$\frac{1}{A} + \frac{1}{B} + \frac{1}{C} = \frac{9}{144}$$

$$\frac{1}{A} + \frac{1}{24} = \frac{9}{144}$$

$$\frac{1}{A} = \frac{9}{144} - \frac{1}{24}$$

$$\frac{1}{A} = \frac{3}{144}$$

18/7

18/144

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$$\frac{1}{A} + \frac{1}{B} + \frac{1}{C} = \frac{1}{16}$$

$$\frac{1}{A} + \frac{1}{B} + \frac{1}{C} = \frac{9}{144}$$

$$\frac{1}{18} + \frac{1}{C} = \frac{9}{144}$$

$$\frac{1}{C} = \frac{9}{144} - \frac{1}{18}$$

$$\frac{9 - 8}{144} = \frac{1}{144}$$

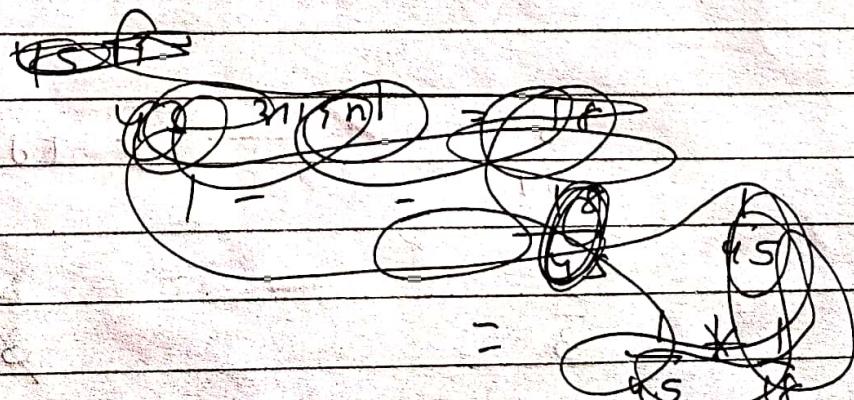
$$C = 144$$

$$+ \frac{1}{24} + \frac{1}{36}$$

$$3 + 2$$

45 men can complete the work in 18 days. 6 days after <sup>they</sup> started working 30 more men join them now will they take to complete the remaining work  $\frac{2}{3}$  of the work

16 days



$$\begin{array}{r}
 45 + 18 = 63 \\
 45 \times 1.66 \\
 \hline
 270 \\
 270 \\
 \hline
 0 \\
 1 \text{ day's work} = \frac{1}{810}
 \end{array}$$

one day work of 1m =  $\frac{1}{810}$

6 day's work of 45 =

$$6 \times 45 = \frac{1}{810}$$

$$\text{Remaining work} = 1 - \frac{1}{3} = \frac{2}{3}$$

$$\text{one day's work of } 75\text{ m} = \frac{75}{810} = \frac{5}{54}$$

$$\frac{5}{54} = 1 \text{ day}$$

$$\begin{array}{r}
 \frac{2}{3} - \frac{2}{5} = \frac{10 - 6}{15} = \frac{4}{15} = \frac{3}{5} \\
 = 7.2 \text{ days}
 \end{array}$$

Time & distance:-

$$D = V \times T$$

$$D = S \times T$$

$$\text{km/h} = \frac{5}{18} \text{ m/sec.}$$

- Q. How many minutes does a person take to cover a distance of 400m if he runs at a speed of 20 km/h

$$20 \times \frac{5}{18} = \frac{50}{9} \text{ m/sec}$$

$$D = S \times T$$

~~$$400 = S \times T \times 2$$~~

$$400 = \frac{50}{9} \times T$$

$$400 \times 9 = T$$

~~180~~

500

$$360m = T$$

$$\overline{5} = T = 5 \sqrt[3]{360}$$

$\overline{35}$   
 $\overline{10}$   
 $\overline{J}$

(72 min)

Q. While covering a distance of 24 km a men notice that a man walking in 40 minutes covers by way of the remaining distance what was his speed?

$$D = 24 \text{ km}$$

$$D = 24000 \text{ m}$$

$$t = 100 \text{ min}$$

$$60 \text{ min}$$

$$24 \times \frac{1}{7}$$

$$17.14 \times 100 =$$

Let remaining distance = ?

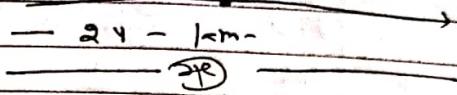
$$\frac{24000}{100} = S \times 60$$

$$S = \frac{240}{60} \text{ m/min}$$

$$S = 4 \text{ m/sec}$$

$$\frac{5}{7} - * = \frac{1}{2}$$

$$* = S \times t$$



Let total distance =  $x$

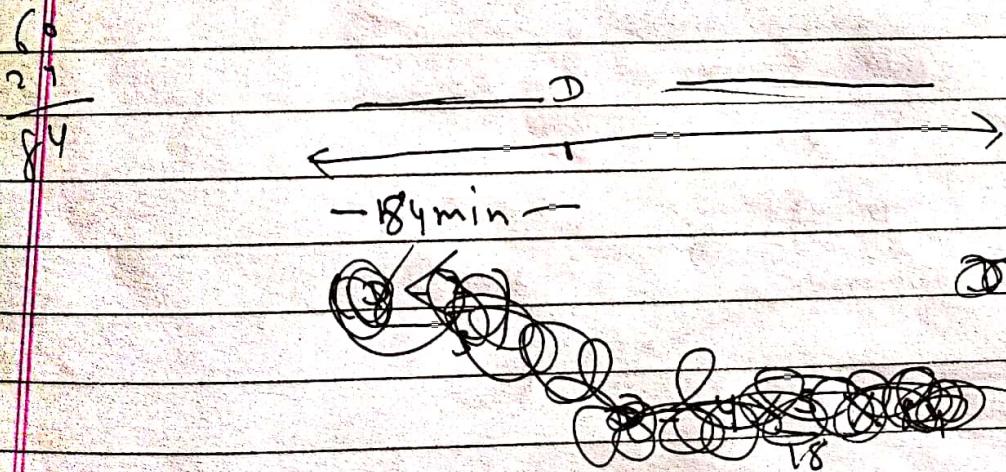
Remaining  $\theta = (24 - \text{circled } 24)$

$$\theta = \frac{s}{t} * (24 - \text{circled } 24)$$

$$\theta = 10 \text{ km}$$

$$(10 * 1000) / (100 * 60) = 1.66 \text{ m/s}$$

- Q. Peter can cover a certain distance in 1 hour 24 minutes by covering  $\frac{2}{3}$  of the distance at  $4 \text{ km/h}$  and the rest  $5 \text{ km/h}$  find the total distance  $\theta$



$$20 = 21 * 0.9$$

$$\frac{2x}{3} + \frac{1}{3} = \frac{7}{5}$$

$$\frac{x}{6} + \frac{x}{15} = \frac{7}{15}$$

$$\frac{(10+4)x}{60} = \frac{7}{5}$$

$$x = \frac{7 \times 60}{5 \times 42} = 6$$