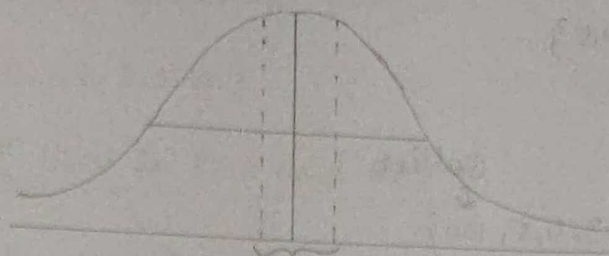


2) Measure of Central Tendency: [EDA]

1. Mean or Average
2. Median
3. Mode



Central Data

If I want to know what is central data information use one of the above measures.

[Measure of Central Tendency are statistical measure used to describe the centre or average of data set. There are 3 measures of central tendency. These measures help to understand the distribution of data. The choice of which measure to use depends on the type of data you are dealing with.]

1. Mean

Population (N)

$$x = \{1, 1, 2, 2, 3, 3, 4, 5, 5, 6\}$$

$$\begin{aligned}\text{Population mean } (\mu) &= \sum_{i=1}^N \frac{x_i}{N} \\ &= \frac{1+1+2+2+\dots+5+6}{10} \\ &= \frac{32}{10} \\ &= 3.2\end{aligned}$$

Sample (n)

$$x = \{2, 3, 1, 4, 8, 9, 5\}$$

$$\begin{aligned}\text{Sample mean } (\bar{x}) &= \sum_{i=1}^n \frac{x_i}{n} \\ &= \frac{32}{7} \\ &= 4.57\end{aligned}$$

2. Median

$$x = \{4, 5, 2, 3, 2, 1\}$$

1] Sort the random variable

2] No. of elements

→ If $n = \text{even} \Rightarrow$ Take avg. of middle 2 elts.
→ If $n = \text{odd} \Rightarrow$ Central element.

$$\therefore x = \{1, 2, \boxed{2, 3}, 4, 5\}$$

$$\frac{2+3}{2} = \underline{\underline{2.5}}$$

Why Median if you have Mean?

Let, consider $\{1, 2, 3, 4, 5\}$

$$\text{Mean} = 3$$

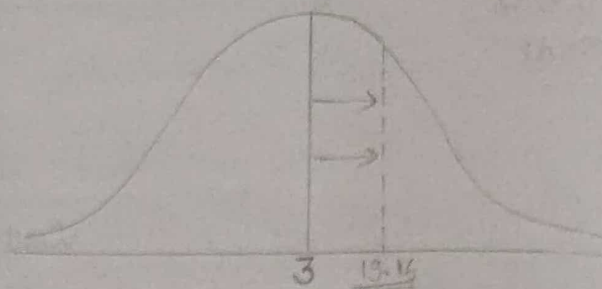
$$\text{Median} = 3$$

Now, Consider $\{1, 2, 3, 4, 5, 100\}$

$$\text{Mean} = 19.16$$

$$\text{Median} = 3.5$$

Outlier



Initially, Mean was 3 and because of the outlier it is shifted to 19.16. So, if we used Median, there is hardly any minor shift from 3 to 3.5.

So, if you have Outlier, the best thing to use is Median.

• Example of Outlier: Transaction fraudulent

• Example:

Let, $X = \{2, 8, 4, 5, 1, 7, 9, 120, 130\}$
Find Mean and Median

$$\therefore \{1, 2, 4, 5, 7, 8, 9, 120, 130\}$$

$$\text{Mean} = \frac{1+2+4+5+\dots+130}{9}$$

$$\therefore \text{Mean} = 31.77$$

$$\text{Median} = 7$$

Here, we can see 2 outliers and that's why Mean is shifted.

Because of outlier entire measure of central tendency is moving in case of Mean & In case of Median only a little movement is there.

By removing outlier we have,
 $\{1, 2, 4, 5, 7, 8, 9\}$

$$\therefore \text{Mean} = 5.1$$

$$\text{Median} = 5$$

[NOTE]: Have Outlier \Rightarrow Use Median \Rightarrow To Calculate Central Tendency

• Example: $X = \{-5, 10, 1, 2, 3, 4, 5\}$ Mean = 0

$$\Rightarrow \{-10, -5, 1, 2, 3, 4, 5\} \quad \text{Median} = 2$$

After removing Outlier $\Rightarrow \{1, 2, 3, 4, 5\}$ Mean = 3

$$\text{Median} = 3$$

3) Mode
Frequency of Maximum occurring element.

ex: $X = \{2, 1, 1, 1, 4, 5, 7, 8, 9, 9, 10\}$

$\therefore \text{Mode} = 1$ [Used in EDA and FE]

Categorical variable

	Age	Weight	Salary	Gender	Degree
	24	70	40K	M	B.E.
	25	80	70K	F	-
	27	95	45K	F	-
	24	-	50K	M	Phd.
	32	-	60K {Mode}	-	B.E.
Mean {	-	60	-	-	MSc.
	-	65	55K	-	BSc.
	40	72	-	M	B.E.
Median	150 (suppose)				

To handle the missing values,

- you can find Mean/Average of all the values.
- you can replace it with mean.

Let's say we have Outlier 150, then use Median.

- In Gender and Degree Columns, use Mode (repeated ones) to replace the missing values.

Mode are use for Categorical Variable replacement.

If M and F are similar, use anyone.

- Based on Outlier, we will use Mean / Median.
- we can also use Mode for Numerical variable but, there are very less chances that values will get repeated.

{ Statistics is all about assumption