

4) Random Variables

Random variable is a process of mapping the output of a random process or experiment to a number.

→ Example:

1) Tossing a coin

$$X = \begin{cases} 0, & \text{if Head} \\ 1, & \text{if Tail} \end{cases}$$

2) Rolling a dice 6 times

$$Y = \{2, 1, 4, 2, 3, 5\}$$

Someone may ask question like if $Y = \{\text{sum of rolling a dice 7 times}\}$ then, what is,

$$P(Y \geq 15), \quad P(Y < 10).$$

5) Sets

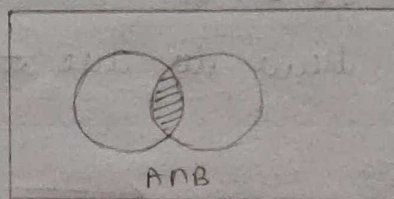
$$A = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

$$B = \{3, 4, 5, 6, 7\}$$

1. Intersection

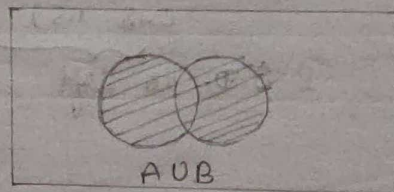
$$(A \cap B)' = \{1, 2, 8\} \text{ (by mistake :)} \}$$

$$A \cap B = \{3, 4, 5, 6, 7\}$$



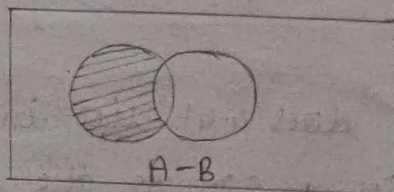
2. Union

$$A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8\}$$



3. Difference

$$A - B = \{1, 2, 8\}$$



4. Subset

$$A \subseteq B \Rightarrow \text{False}$$

$$B \subseteq A \Rightarrow \text{True}$$

5. Superset

$$A \supset B \Rightarrow \text{True}$$

$$B \supset A \Rightarrow \text{False}$$