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#### B.E. (Information Technology) Fourth Semester (C.B.S.)

#### **Theory of Computation**

P. Pages: 3 NRT/KS/19/3385

Time: Three Hours

\* 0 7 8 3 \*

Max. Marks: 80

Notes: 1. All questions carry marks as indicated.

- 2. Solve Question 1 OR Questions No. 2.
- 3. Solve Question 3 OR Questions No. 4.
- 4. Solve Question 5 OR Questions No. 6.
- 5. Solve Question 7 OR Questions No. 8.
- 6. Solve Question 9 OR Questions No. 10.
- 7. Solve Question 11 OR Questions No. 12.
- 8. Due credit will be given to neatness and adequate dimensions.
- 9. Assume suitable data whenever necessary.
- 10. Illustrate your answers whenever necessary with the help of neat sketches.
- 1. a) Construct DFA equivalent to NFA  $(\{p, q, r, s\}, \{0, 1\}, p, \{s\}, \delta)$  where  $\delta$  is given by.

| δ | 0    | 1 |
|---|------|---|
| p | p, q | p |
| q | r    | r |
| r | S    | 1 |
| S | S    | S |

- b) Differentiate between:
  - i) NFA and DFA

- ii) Grammar and Language
- iii) Mealy and Moore machine

OR

- 2. a) Construct Moore machine and transition table for count number of a's % 3 (a mod 3) over  $\Sigma = \{a, b\}$ . Also construct its equivalent Melay machine.
  - 5

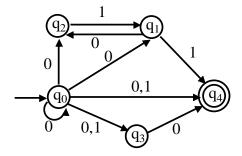
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b) Construct DFA which is equivalent to following NFA over  $\Sigma = \{0, 1\}$ .



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**3.** a) Construct equivalent LLG for the RLG given below.

 $S \rightarrow 0A \mid 1B$ 

 $A \rightarrow 0C | 1A | 0$ 

 $B \rightarrow 1B \mid 1A \mid 1$ 

 $C \rightarrow 0 \mid 0A$ 

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b) Prove that  $L = \{a^n b^{n+m} c^m \mid n, m \ge 1\}$  is not regular.

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c) Prove that regular language is closed under union operation.

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OR

**4.** a) Convert the grammar with the following productions to CNF.

 $S \rightarrow ABa$ 

 $A \rightarrow aab$ 

 $B \rightarrow Ac$ 

b) Convert the grammar with the following productions to GNF.

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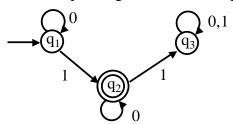
 $E \rightarrow E + T \mid T$ 

 $T \rightarrow T * F | F$ 

 $F \rightarrow (E) | id$ 

c) Construct a regular expression corresponding to the automata given below.

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**5.** a) Convert following regular expression and language to its equivalent grammar.

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- i)  $((a+b)(a+b))^*$
- ii)  $L = \{a^n b^m c^m d^n | n, m >= 1\}.$
- b) Differentiate between Non-Deterministic pushdown Automata & deterministic pushdown Automata.

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OR

**6.** a) Explain closure properties of CFL.

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b) Construct DPDA that accepts the language of strings with the same number of zeros & ones over  $\Sigma = \{0, 1\}$ .

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**7.** a) Explain how TM work as a comparator. Consider & strings to show all the cases of comparison.

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b) Explain in detail different types of TM.

6

OR

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**8.** a) Design a TM to find 2's complement of n digit binary number.

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b) Write short note on any two.

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- i) Counter machine
- ii) Multitape TM
- iii) Offline TM
- iv) Multidimensional TM
- **9.** a) Consider PC

Consider PCP system that described by the following test.

$$A = \{10, 01, 0, 100, 1\}$$

$$\mathbf{B} = \{101, 100, 10, 0, 010\}$$

Does this PCP have solution?

b) Define Ackermann's function Compute

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OR

- **10.** a) State which of the following PCP's have a solution.
  - i)  $\{(01, 011), (1, 10), (1, 11)\}$
  - ii)  $\left\{ \left(b^3, ab^2\right), \left(b^3, bab^3\right) \right\}$ .
  - b) What do you mean by recursion? Explain the properties of Recursive and Recursively enumerable languages.
    - 6
- 11. a) What is primitive recursive function? Explain the category of basic function.
- 6

b) Explain Mod and Div functions with example.

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OR

12. a) Show that the function  $g(x, y) = x^y$  is primitive recursive.

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b) Write short note on **any two.** 

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- i)  $\mu$  recursive function.
- ii) Bounded minimization.
- iii) Unbounded minimization

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# The secret of getting ahead is getting started. ~ Mark Twain

