

PRACTICAL NO 1

Topic: Basics of R software

- (i) R is a software for data analysis and statistical computation
- (ii) This software is used for effective data handling and output storage is possible.
- (iii) It is capable of graphical display
- (iv) It is a free software

Q. 1

$$\begin{aligned}
 & (i) 2^2 + \sqrt{25} + 35 \\
 & > (2^{**} 2) + \text{sqrt}(25) + 35 \\
 & [1] 44
 \end{aligned}$$

$$\begin{aligned}
 & (ii) 2 \times 5 \times 3 + 62 \div 5 + \sqrt{49} \\
 & > (2 * 5 * 3) + (62 / 5) + \text{sqrt}(49) \\
 & [1] 49.4
 \end{aligned}$$

$$\begin{aligned}
 & (iii) \sqrt{76 + 4 \times 2 + 9 \div 5} \\
 & > \text{sqrt}(76 + (4 * 2) + (9 / 5)) \\
 & [1] 9.262829
 \end{aligned}$$

$$\begin{aligned}
 & (iv) 42 + |-10| + 7^2 + 3 \times 9 \\
 & > 42 + \text{abs}(-10) + (7^{**} 2) + (3 * 9) \\
 & [1] 128
 \end{aligned}$$

Q.2]

$$x = 20$$

$$y = 30$$

find $x+y$, x^2+y^2 , $\sqrt{y^3-x^3}$, $|x-y|$

$$> x+y$$

$$[1] \quad 50$$

$$> (x^{**} 2) + (y^{**} 2)$$

$$[1] \quad 1300$$

$$> \text{sqrt}((y^{**} 3) - (x^{**} 3))$$

$$[1] \quad 137.8405$$

$$> \text{abs}(x-y)$$

$$[1] \quad 10$$

Q.3]

$$> c(2, 3, 4, 5)^1 2$$

$$[1] \quad 4 \ 9 \ 16 \ 25$$

$$> c(4, 5, 6, 8)^* 3$$

$$[1] \quad 12 \ 15 \ 18 \ 24$$

$$> c(2, 3, 5, 7)^* c(-2, -3, -5, -4)$$

$$[1] \quad -4 \ -9 \ -25 \ -28$$

$$> c(2, 3, 5, 7)^* c(8, 9)$$

$$[1] \quad 16 \ 27 \ 40 \ 63$$

$$> c(1, 2, 3, 4, 5, 6)^* (2, 3)$$

$$[1] \quad 1 \ 8 \ 9 \ 64 \ 25 \ 216$$

Q.4] find the sum, product, maximum, minimum of the values
 $5, 8, 6, 7, 9, 10, 15, 5$

```
> x = c(5, 8, 6, 7, 9, 10, 15, 5)
> length(x)
[1] 8
> sum(x)
[1] 65
> prod(x)
[1] 11340000
> max(x)
[1] 15
> min(x)
[1] 5
```

Q.5] > x <- matrix(nrow=4, ncol=2, data=c(1, 2, 3, 4, 5, 6, 7, 8))

```
> x
[1] [,1] [,2]
[1,] 1 5
[2,] 2 6
[3,] 3 7
[4,] 4 8
```

Q8

B.6) $x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$

$y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$

> $x <- \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(1, 2, 3, 4, 6, 9))$

> $y <- \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(10, -11, 12))$

> $x + y$

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \begin{bmatrix} 2 \\ 0 \\ 13 \end{bmatrix} \begin{bmatrix} 3 \\ 8 \\ 12 \end{bmatrix} \begin{bmatrix} 17 \\ -3 \\ 21 \end{bmatrix}$$

> $x^* y$

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \begin{bmatrix} 2 \\ -4 \\ 30 \end{bmatrix} \begin{bmatrix} 16 \\ 40 \\ 36 \end{bmatrix} \begin{bmatrix} 70 \\ -88 \\ 108 \end{bmatrix}$$

> $x^* 2 + y^* 3$

$[1]$	$[2]$	$[3]$	
$[1]$	8	20	44
$[2]$	-2	34	-17
$[3]$	36	30	54

> $x = c(2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 3, 2, 5, 0, 15, 9, 14, 18, 10, 12)$

> length(x)

[1] 23

> a = table(x)

► a

X

0	1	2	3	4	5	6	7	9	10	12	14	15	16	17	18	19
1	1	2	3	1	2	1	1	1	1	1	2	1	1	1	2	1

> transform(a)

	x	freq
0		1
1		1
2		2
3		3
4		1
5		2
6		1
7		1
9		1
10		1

PE

12	1
14	2
15	1
16	1
17	1
18	2
19	1

```
> breaks = seq(0, 20, 5)
> s = cut(x, breaks, right = FALSE)
> c = table(s)
> transform(c)
```

[1]	S	Freq
1	[0, 5)	8
2	[5, 10)	5
3	[10, 15)	4
4	[15, 20)	6

Q.1] Can the following be p.d.f?

$$(i) f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow \int_1^2 (2-x) dx$$

$$= \int_1^2 2 dx - \int_1^2 x dx$$

$$= 2x \Big|_1^2 - \frac{x^2}{2} \Big|_1^2$$

$$= (4-2) - (2-0.5)$$

$$\neq 1$$

\Rightarrow Not a p.d.f

$$(ii) f(x) = \begin{cases} 3x^2 & ; 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow \int_0^1 (3x^2) dx$$

$$= \int_0^1 3x^3 dx$$

$$= x^3 \Big|_0^1$$

$$= 1$$

\Rightarrow It is a p.d.f

(iii) $f(x) = \begin{cases} \frac{3x}{2} \left(1 - \frac{x}{2}\right) & ; 0 \leq x \leq 2 \\ 0 & , \text{ otherwise} \end{cases}$

$$\Rightarrow \int_0^2 \left(\frac{3x}{2} - \frac{3x^2}{4} \right) dx$$

$$= \frac{3}{2} \int_0^2 x dx - \frac{3}{4} \int_0^2 x^2 dx$$

$$= \frac{3}{2} \left[\frac{x^2}{2} \right]_0^2 - \frac{3}{4} \left[\frac{x^3}{3} \right]_0^2$$

$$= \frac{3}{4} [x^2]_0^2 - \frac{1}{4} [x^3]_0^2$$

$$= \frac{3}{4} [4] - \frac{1}{4} [8]$$

$$= 1$$

\Rightarrow It is a p.d.f

Q.2] Can the following be p.m.f

(i)	x	1	2	3	4	5
	$p(x)$	0.2	0.3	-0.1	0.5	0.1

Since, 1 of the probability is negative, it is not a p.m.f

(ii)	x	0	1	2	3	4	5
	$p(x)$	0.1	0.3	0.2	0.2	0.1	0.1

Since $p(x) \geq 0 \quad \forall x$
and $\sum p(x) = 1$
 \therefore It is a p.m.f

(iii)	x	10	20	30	40	50
	$p(x)$	0.2	0.3	0.3	0.6	0.2

Since $p(x) \geq 0 \quad \forall x$
and $\sum p(x) \neq 1$
 \therefore It is not a p.m.f

Q.3] Find $P(X \leq 2)$, $P(2 \leq x < 4)$, $P(\text{atleast } 4)$, $P(3 < x < 6)$

x	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\Rightarrow P(x \leq 2)$$
$$= P(0) + P(1) + P(2)$$
$$= 0.1 + 0.1 + 0.2$$
$$= 0.4$$

$$P(2 \leq x < 4)$$
$$= P(2) + P(3)$$
$$= 0.2 + 0.2$$
$$= 0.4$$

$$P(\text{atleast } 4)$$
$$= P(4) + P(5) + P(6)$$
$$= 0.1 + 0.2 + 0.1$$
$$= 0.4$$

$$P(3 < x < 6)$$
$$= P(4) + P(5)$$
$$= 0.1 + 0.2$$
$$= 0.3$$

P

Probability Distribution

b] find c.d.s of the following p.m.f and draw the graph.

X	10	20	30	40	50
$p(x)$	0.15	0.25	0.3	0.2	0.1

$$f(x) = 0 \quad \text{if } x < 10$$

$$= 0.15 \quad 10 \leq x \leq 20$$

$$= 0.40 \quad 20 \leq x < 30$$

$$= 0.70 \quad 30 \leq x < 40$$

$$= 0.90 \quad 40 \leq x < 50$$

$$= 1.0 \quad x \geq 50$$

$$> x = c(10, 20, 30, 40, 50)$$

$$> prob = c(0.15, 0.25, 0.3, 0.2, 0.1)$$

$$> cumsum(prob)$$

$$[1] 0.15 \quad 0.40 \quad 0.70 \quad 0.90 \quad 1.0$$

> plot(x, cumsum(prob), xlab = "values", ylab = "probability", main = "graph of c.d.f", "s")

Binomial Distribution

Q) Suppose there are 12 mcq's in a test each question has 3 option and only one of them is correct. Find the probability of having in 5 correct answer (2) Atm, 4 correct answers.

→ Given that

$$n = 12, p = 1/5, q = 4/5$$

x = Total no of correct answers

$$x \sim B(n, p)$$

$$n = 12, p = 1/5, q = 4/5, x = 5$$

$$> n = 12; p = 1/5; q = 4/5; x = 5$$

$$> sum(n, p, q, x)$$

[1] 18

$$> dbinom(5, 2, 1/5)$$

[1] 0.05315022

$$> pbinom(4, 12, 1/5)$$

[1] 0.9274445

3] There are 10 members in a committee, the probability of any member attending a meeting is 0.9. Find the probability

- (i) 7 members attended (ii) Atleast 3 members attended
(iii) Atmost 6 members attended

→ Given that

$$n = 10, p = 0.9, q = 0.1$$

x = Total no of member attended

$$x \sim B(n, p)$$

$$n = 10, p = 0.9, q = 0.1$$

$$> n = 10; p = 0.9; q = 0.1$$

$$> dbinom(7, 10, 0.9)$$

$$[1] 0.05739563$$

$$> 1 - pbinom(5, 10, 0.9)$$

$$[1] 0.9983651$$

$$> pbinom(6, 10, 0.9)$$

$$[1] 0.0127952$$

4] Find the c.d.f and draw the graph

x	0	1	2	3	4	5	6
---	---	---	---	---	---	---	---

p(x)	0.1	0.1	0.2	0.2	(0.1	0.2	0.1
------	-----	-----	-----	-----	------	-----	-----

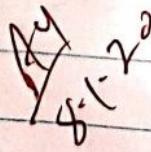
$\rightarrow x = c(1, 2, 3, 4, 5, 6)$

$\rightarrow \text{prob} = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$

$\rightarrow \text{cumsum}(\text{prob})$

[1] 0.1 0.2 0.4 0.6 0.7 0.9 1.0

$\rightarrow \text{plot}(x, \text{cumsum}(\text{prob}), \text{xlab} = \text{"Values"}, \text{ylab} = \text{"probability"} \text{, main} = \text{"graph of c.d.f", "s"})$



(P=0, 0.1, 0.2)
1.0

(P=0, 0.1, 0.2)
1.0

Binomial Distribution

- 1] Find the complete binomial distribution where $n=5$ and $p=0.1$
- 2] find the probability of exactly 10 success in 100 trials where $p=0.1$
- 3] X follows binomial distribution with $n=12$, $p=0.25$.
 Find (i) $P(X=5)$
 (ii) $P(X \leq 5)$
 (iii) $P(X > 7)$
 (iv) $P(5 < X < 7)$
- 4] The probability of a salesman makes a sale to a customer is 0.15. Find the probability
 (i) No sale for 10 customers
 (ii) More than 3 sale in 20 customers
- 5] A student writes 5 mcq's. Each question has 4 options out of which one is correct. Calculate the probability for atleast 3 correct answers.
- 6] X follows binomial distribution with $n=10$, $p=0.4$
 Plot the graph of p.m.f and c.d.f

8A

Binomial Distribution

Note:

$$P(X = n) = \text{dbinom}(n, n, p)$$

$$P(X \leq n) = \text{pbinom}(n, n, p)$$

$$P(X > n) = 1 - \text{pbinom}(n, n, p)$$

To find the value of X for which the probability given as p_1 , command is qbinom .

$$\Rightarrow \text{qbinom}(p_1, n, p)$$

Answers:

[1] $n = 5, p = 0.1$

$$> \text{dbinom}(0.5, 5, 0.1)$$

[1] 0.59049 0.32805 0.07290 0.00810 0.00045 0.00001

[2] $x = 10, n = 100, p = 0.1$

$$> \text{dbinom}(10, 100, 0.1)$$

[1] 0.1318658

★

Note:

$$P(X = n) = \text{dbinom}(x, n, p)$$

$$P(X \leq x) = \text{pbinom}(x, n, p)$$

$$P(X > n) = 1 - \text{pbinom}(n, n, p)$$

To find the value of X for which the probability is given as p_1 , command is qbinom .

$$\Rightarrow \text{qbinom}(p_1, n, p)$$

Answers:

1] $n = 5, p = 0.1$

$$> \text{dbinom}(0:5, 5, 0.1)$$

[1] 0.59049 0.32805 0.07290 0.00810 0.00045 0.00001

2] $x = 10, n = 100, p = 0.1$

$$> \text{dbinom}(10, 100, 0.1)$$

[1] 0.1318653

8] $n = 12, p = 0.25$

(i) $P(X=5) = dbinom(n, n, p)$

> $dbinom(5, 12, 0.25)$

[1] 0.1032414

(ii) $P(X \leq 5) = pbinom(n, n, p)$

> $pbinom(5, 12, 0.25)$

[1] 0.9455978

(iv) $P(5 < X < 7) = dbinom(x, n, p)$

> $dbinom(6, 12, 0.25)$

[1] 0.04014945

(iii) $P(X \geq 7)$

= $1 - P(X \leq 7)$

> $1 - pbinom(7, 12, 0.25)$

[1] 0.00278151

9] $p = 0.15$

(i) $n = 10, p = 0.15, x = 0$

> $dbinom(0, 10, 0.15)$

[1] 0.1968744

(ii) $p = 0.15, n = 20$

$$P(X > 3) = 1 - P(X \leq 3)$$

```
> 1 - pbinom(3, 20, 0.15)  
[1] 0.8522748
```

5] $n = 5, p = 1/4$

$$\begin{aligned} P(X \geq 3) \\ = 1 - P(X \leq 2) \end{aligned}$$

```
> 1 - pbinom(3, 5, 1/4)  
[1] 0.015625
```

6] $n = 10, p = 0.4$
 $x = 0:n$

prob = dbinom(n, n, p)

cumprob = pbinom(x, n, p)

d = data.frame("x values" = x, "probability" = prob)

print(d)

```
> prob = dbinom(0:10, 10, 0.4)
```

```
> prob
```

```
> cumprob = pbinom(0:10, 10, 0.4)
```

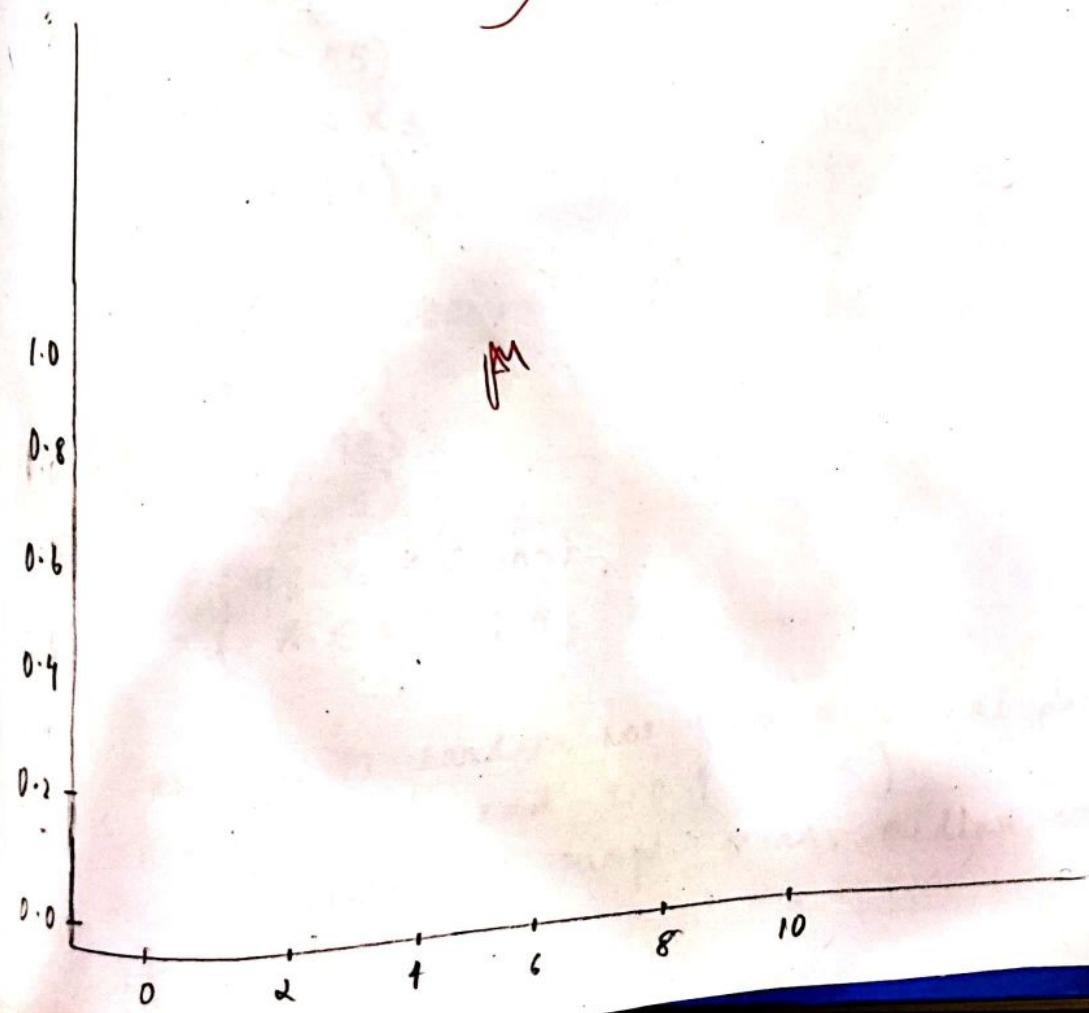
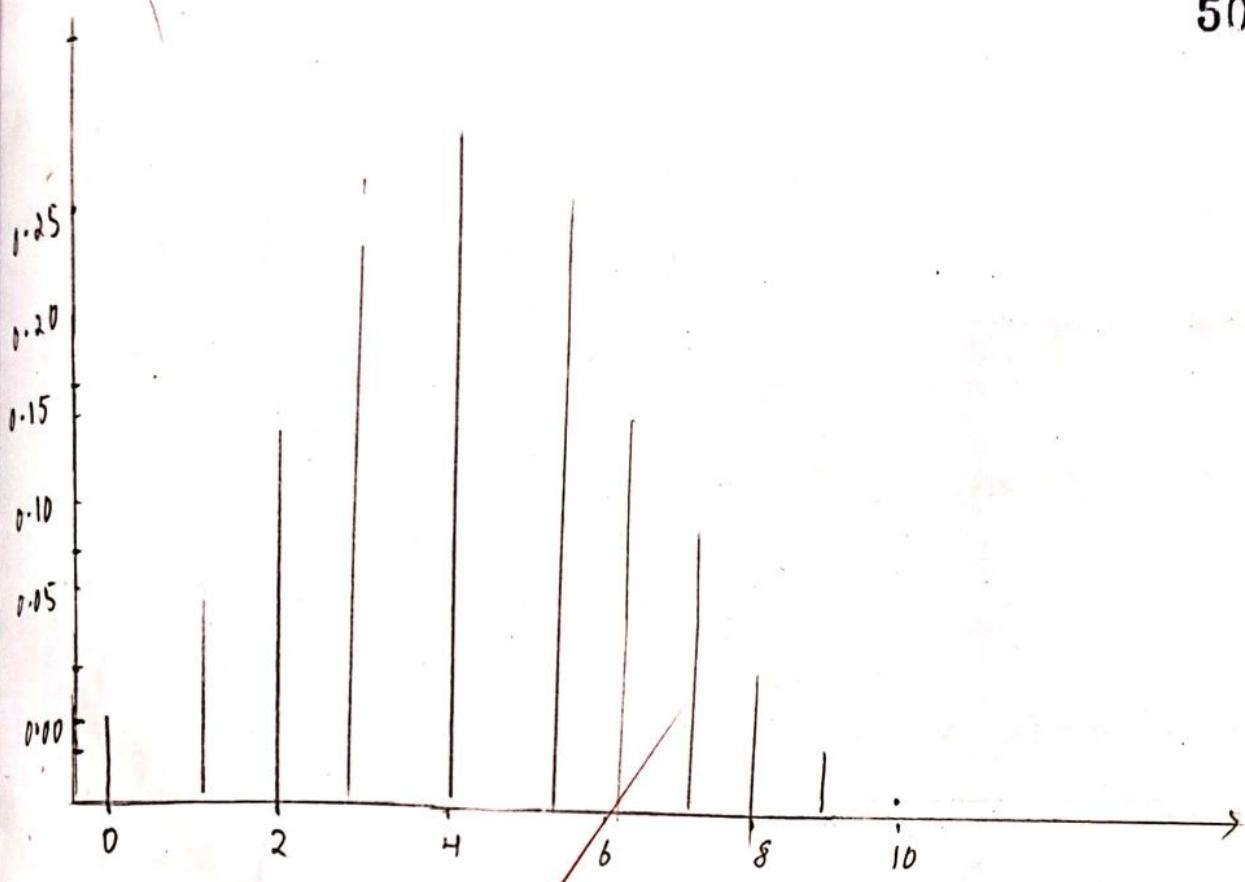
```
> cumprob
```

```
> d = data.frame("x values" = 0:10, "probability" = 0.4)
```

```
> print(d)
```

```
> plot(0:10, prob, "h")
```

```
> plot(0:10, cumprob, "s")
```



PRACTICAL NO 5

51

* NOTE :

$$P(X = x) = \text{dnorm}(x, \mu, \sigma)$$

$$P(X \leq x) = \text{pnorm}(x, \mu, \sigma)$$

$$P(X > x) = 1 - \text{pnorm}(x, \mu, \sigma)$$

$$P(x_1 < X < x_2) = \text{pnorm}(x_2, \mu, \sigma) - \text{pnorm}(x_1, \mu, \sigma)$$

To find the value of k so that

$$P(X \leq k) = p_1 ; \text{ qnorm}(p_1, \mu, \sigma)$$

To generate random no the command is $\text{rnorm}(n, \mu, \sigma)$

1] $X \sim N(\mu = 50, \sigma^2 = 100)$

find (i) $P(X \leq 40)$

(ii) $P(X > 55)$

(iii) $P(42 \leq X \leq 60)$

(iv) $P(X \leq k) = 0.7 ; k = ?$

2] $X \sim N(\mu = 100, \sigma^2 = 36)$

(i) $P(X \leq 110)$

(ii) $P(X \leq 95)$

(iii) $P(X > 115)$

(iv) $P(95 \leq X \leq 105)$

(v) $P(X \leq k) = 0.4 ; k = ?$

3] Generate 10 random nos from a normal distribution with mean ($\mu = 60$) and s.d ($\sigma = 5$).
Also calculate the sample mean, median, variance and standard deviation.

2. Draw the graph of standard normal distribution.

($\mu = 0, \sigma = 1$) mean

($\mu = 0, \sigma = 1$) showing

($\mu = 0, \sigma = 1$) showing -1 standard deviation

($\mu = 0, \sigma = 1$) showing - ($\mu = 0, \sigma = 1$) missing - ($x > 0$)

Answers:

[i] $a = \text{pnorm}(40, 50, 10)$
cat("P(X ≤ 40) is =", a)

[i] 0.1586553

P(X < 40) is 0.1586553 >

[ii] $b = 1 - \text{pnorm}(55, 50, 10)$
cat("P(X > 55) is =", b)
P(X > 55) is 0.03085375 >

[i] 0.3085375

[iii] $c = \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10)$

[i] 0.6294893

P(X < k) = 0.7, k is 55.24401 >

[iv] $d = \text{qnorm}(0.7, 50, 10)$

[i] 55.24401

2] (i) > $a = \text{pnorm}(110, 100, 6)$

[1] 0.9522096

(ii) > $b = \text{pnorm}(95, 100, 6)$

[1] 0.2023284

(iii) > $c = 1 - \text{pnorm}(115, 100, 6)$

[1] 0.006209665

(iv) > $d = \text{pnorm}(105, 100, 6) - \text{pnorm}(95, 100, 6)$

[1] 0.5953432

(v) > $e = \text{qnorm}(0.4, 100, 6)$

[1] 98.47992

3] $n = 10, \mu = 60, \sigma = 5$
> $x = \text{rnorm}(10, 60, 5)$

[1] 64.30801 56.28556 51.12444 62.66236 51.07212 52.90556 63.04319
59.37558 59.78091 56.45464

> $am = \text{mean}(x)$

> am

[1] 58.30124

> $me = \text{median}(x)$

> me

[1] 58.22385

> $n = 10$

> variance = $(n-1)^* \text{var}(x) / n$

> variance

[1] 17.05339

> $sd = \sqrt{\text{variance}}$

> sd

[1] 4.129575

4.] > $x = \text{seq}(-3, 3, by = 0.1)$

> x

[1] -3.0 -2.9 -2.8 -2.7 -2.6 -2.5 -2.4 -2.3 -2.2 -2.1 -2.0
 -1.9 -1.8 -1.7 -1.6 -1.5 -1.4 -1.3 -1.2 -1.1 -1.0 -0.9
 -0.8 -0.7 -0.6 -0.5 -0.4 -0.3 -0.2 -0.1 0 0.1 0.2 0.3
 0.4 0.5 0.6 0.7 0.8 0.9 1.0 1.1 1.2 1.3 1.4 1.5 1.6 1.7
 1.8 1.9 2.0 2.1 2.2 2.3 2.4 2.5 2.6 2.7 2.8 2.9 3.0

> $y = \text{dnorm}(x)$

> $\text{plot}(n, y, xlab = "x values", ylab = "probability", main = "standard normal graph")$

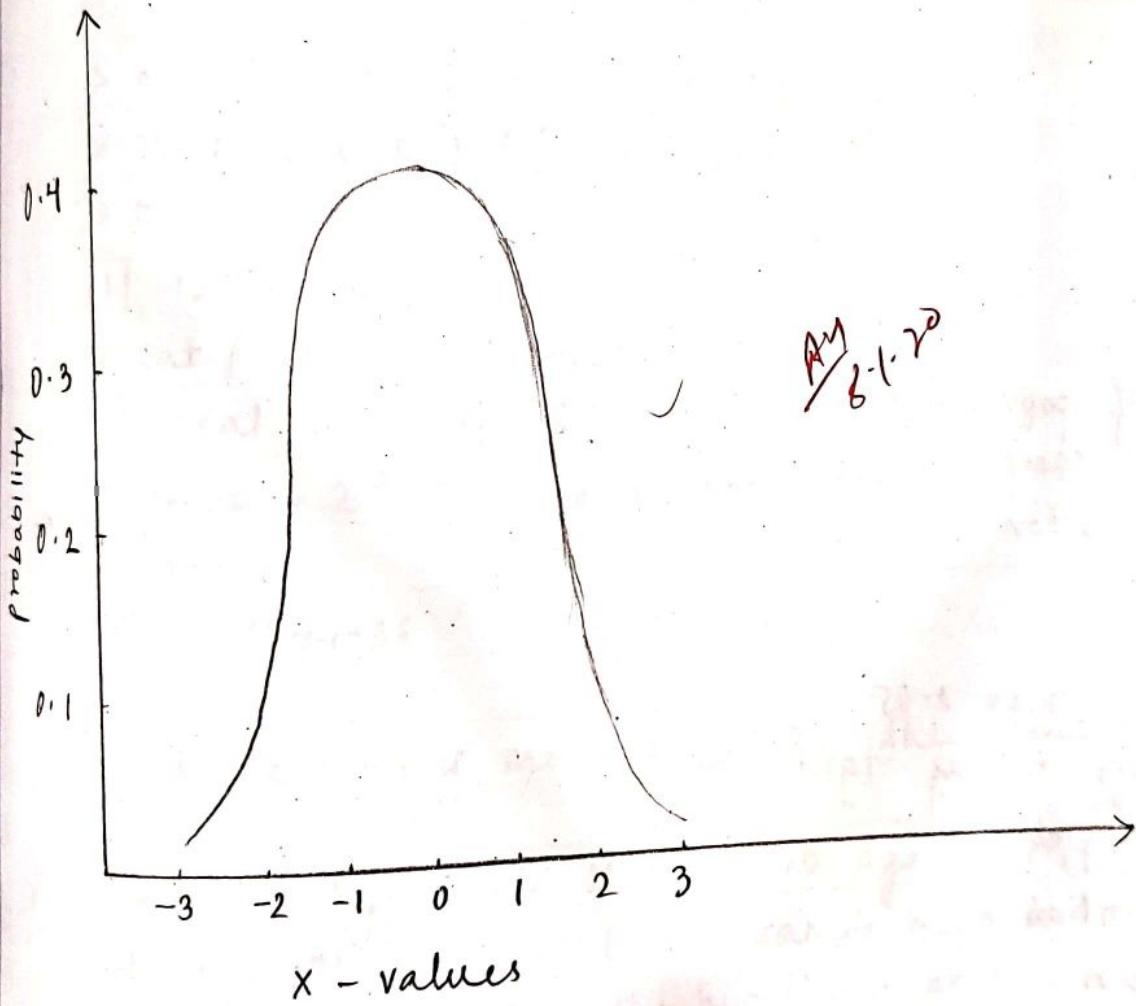
(x) $\text{mean} = 0$

0.608833

(x) $\text{mean} = 0$

0.608833

STANDARD NORMAL GRAPH



μ_0 = mean of population

μ_n = ' ' sample

s_d = std deviation

n = total

if ans is more than 0.05

then accept H_0 as right ans

or else it is false

p = popln proportion

p = sample proportion

PRACTICAL NO 6

55

Topic: Z distribution

i] Test the hypothesis (H_0) $H_0: \mu = 10$ against $H_1: \mu \neq 10$. A sample of size 400 is selected which gives the mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance

> $m_0 = 10; m_x = 10.2; s_d = 2.25; n = 400$

> $z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$

> z_{cal}

[1] 1.777778

> cat ("zcal is =", zcal)

[1] zcal is = 1.777778

> pvalue = 2 * (1 - pnorm (abs (zcal)))

> pvalue

[1] 0.07544036

\because The answer is more than 0.05, the value of H_0 is correct.
 H_0 is accepted.

ii] Test the hypothesis $H_0: \mu = 75$ against $H_1: \mu \neq 75$. A sample of size 100 is selected and sample mean is 80 with standard deviation of 3. Test the hypothesis at 5% level of significance.

> $m_0 = 75; m_x = 80; s_d = 3; n = 100$

> $z_{cal} = (m_x - m_0) / (s_d / (\sqrt{n}))$

> z_{cal}

[1] 16.66667

> cat ("zcal is =", zcal)

[1] zcal is = 16.6667

Q2

> pvalue = 2 * (1 - pnorm (abs(zcal)))

> pvalue

[1] 0

Since, the value of p is less than 0.05, the value H_0 is incorrect.

Q3) Test the hypothesis $H_0: \mu = 25$ against $H_1: \mu \neq 25$ at 5% of significance. Following sample of 30 is selected.

S: 20, 24, 27, 35, 30, 46, 26, 27, 10, 20, 30, 37, 35, 21, 22, 24, 25, 26, 27, 28, 29, 30, 39, 27, 15, 19, 22, 20, 18

> n = c()

> mn = mean(n)

> mn

[1] 26.06667

> n = length(n)

[1] 30

> Variance = (n-1) * var(n)/n

> variance

[1] 52.99556

> sd = sqrt(variance)

> sd

[1] 7.279805

> m0 = 25; mn = 26.07; sd = 7.3; n = 30

> zcal = $(\bar{x} - \mu_0) / (\text{sd} / \sqrt{n})$

> zcal

[1] 0.8050318

> cat ("zcal is = ", zcal)

[1] zcal is = 0.8050318

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.408013

∴ The value is ~~less~~^{more} than 0.05, the value of H_0 is correct

- 4) Experience has shown that 20% students of a college smoke. A sample of 400 students reveal that out of 400 only 50 smoke. Test the hypothesis that the experience gives the correct proportion or not.

> P = 0.2

> Q = 1 - P

> Q

[1] 0.8

> p = 50 / 400

> p

[1] 0.125

> n = 400

> zcal = $(p - P) / (\sqrt{P \cdot Q / n})$

> zcal

[1] -3.75

∴ The value is less than 0.05, the value of H_0 is incorrect

5] Test the hypothesis $H_0: P = 0.5$ against $H_1: P \neq 0.5$. A sample of 200 is selected and the sample proportion is calculated $p = 0.56$. Test the hypothesis at 2% level of significance.

> $P = 0.5$

> $Q = 1 - P$

> $Q = 0.5$

> $p = 0.56$

> $n = 200$

> $z_{\text{cal}} = (p - P) / (\sqrt{P \cdot Q / n})$

[1] 1.697056

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

[1] 0.089688

"The value is more than 0.05, the value of H_0 is correct"

AM
32.320

PRACTICAL NO 7

59

Topic: Large Sample Tests

- Q] A study of noise level in two hospital is calculated below. Test the hypothesis that the noise level into hospital. Test the hypothesis in 2 hospitals are same or not

HosA	Hos A	Hos B
No of		
Sample obs	84	34
Mean	61	59
S. D	7	8

H_0 : The noise levels are same

> $n1 = 84$

> $n2 = 34$

> $m1 = 61$

> $m2 = 59$

> $sdx = 7$

> $sdy = 8$

> $z = (m1 - m2) / \sqrt{((sdx^2/n1) + (sdy^2/n2))}$

z

[1] 1.273682

> cat ("z calculated is = ", 2)

[1] z calculated is = 2

> pvalue = 2 * (1 - pnorm (abs (z)))

[1] 0.84582 0.1211

since pvalue is 0.1211, we reject H_0 at 5% level of significance

Q.2

Two random samples of size 1000 & 2000 are drawn from populations with a mean 67.5 and 68 respectively and with the same S.D of 2.5. Test the hypothesis that the means of 2 populations are equal.

H_0 = 2 populations are equal

> $n_1 = 1000$

BETH AETH AETH

> $n_2 = 2000$

> $m_x = 67.5$

68 68

> $m_y = 68$

PC 10

> $sdx = 2.5$

8 7

> $sdy = 2.5$

> $z = (m_x - m_y) / \sqrt{((sdx^2/n_1) + (sdy^2/n_2))}$

> $z =$

[1] -5.163978

> cat ("z calculated is = ", z)

[1] z calculated is = 2

> pvalue = 2 * (1 - pnorm (abs(z)))

> pvalue

[1] 2.417564e-07

Since pvalue is $2.417564e-07$, we reject H_0 at 5% level of significance.

3) In a first year class (F.Y.B.Sc), 20% of a random sample of 400 students had defective eyesight. In S.Y class, 15.5% of 500 sample had same defect. Is the difference of proportion is same?

H_0 = The proportion of the population are equal

> $n_1 = 400$

> $n_2 = 500$

> $p_1 = 0.2$

> $p_2 = 0.155$

> $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> p

[1] 0.175

> $q = 1 - p$

> q

[1] 0.825

> $z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

> z

[1] 1.76547

> cat ("z calculated is ", z)

[1] z calculated is 1.76547

> pvalue = 2 * (1 - pnorm (abs(z)))

> pvalue

[1] 0.07748487

Since pvalue is 0.077, we accept H_0 at 5% level of significance.

4.] From each of the box of the apples, a sample size of 200 is collected. It is found that, there are 44 bad apples in the 1st sample and 30 bad apples in the 2nd sample. Test the hypothesis that 2 boxes are equivalent in terms of bad apples.

H_0 = The proportion of boxes is same.

> n1 = 200

> n2 = 200

> p1 = 44/200

> p2 = 30/200

> p = (n1*p1 + n2*p2)/(n1+n2)

> p

[1] 0.185

> q = 1-p

> q

[1] 0.815

> z = (p1-p2)/sqrt(p*q*(1/n1 + 1/n2))

> z

[1] 1.8027

> cat("z calculated is = ", z)

> calculated is 1.8027

> pValue = 2 * (1 - pnorm(abs(z)))

> pvalue

[1] 0.0714

Since pvalue is 0.0714, we accept the null hypothesis at 5% level of significance.

Q] In a MA class, out of a sample of 60, mean height is 63.5 inch with a S.D 2.5. In a MCom class, out of 50 students, mean height 69.5 inches with a S.D of 2.5. Test the hypothesis that the mean of MA and MCom class are same.

H_0 = Mean height of MA and MCom students are equal.

> n1 = 60

> n2 = 50

> m1 = 63.5

> m2 = 69.5

> sd1 = 2.5

> sd2 = 2.5

> z = ($m_1 - m_2$) / $\sqrt{(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2})}$

> z
[1] -12.5335

> cat ("z calculated is = ", z)

z calculated is = -12.5335

> pvalue = 2 * (1 - pnorm (abs (z)))

> pvalue

[1] 0.04550

Since pvalue is 0.04550, we reject at 5% level of significance

8.8

PRACTICAL NO 8

Topic: Small Sample Test

Q.1] The tens are selected and height are found to be 68, 69, 71, 64, 70, 72 cms. Test hypothesis that mean height 66 cm or not at 1%.

$$H_0 \neq \text{Mean} = 66 \text{ cms}$$

$$> \text{mean} = 66$$

$$> x = c(68, 63, 68, 69, 71, 71, 72)$$

> t.test(x)

One Sample t-test

data : x

$$t = 47.94, df = 6, pvalue = 5.22e-09$$

Alternative hypothesis: True mean is not equal to 0

95 percent confidence interval:

$$64.66479 \quad 71.62092$$

Sample estimates:

Mean of x

$$68.14286$$

\therefore pvalue < 0.01 is rejected on H_0 in 1% level of significance

Q.2] Two random sample was drawn from two different populations

Sample 1: 7, 8, 10, 12, 14, 16, 15, 18, 7

Sample 2: 20, 15, 18, 9, 8, 10, 11, 12

Test the hypothesis that there is no difference between the population mean at 5% loss.

H_0 there is no difference in the population mean

> $x = c(8, 10, 12, 11, 16, 15, 18, 7)$
 > $y = c(20, 15, 18, 9, 8, 10, 11, 12)$
 > t.test(x, y)

Welch Two Sample t-test

data: x & y

t = -0.36247, df = 13.837, p-value = 0.7225
 Alternative hypothesis: True difference in mean is not equal to 5.192719

Sample estimates

Mean of x

12.125

Mean of y

12.875

p-value < 0.01 is accepted in H₀ on 1% level of significance

3] following are the weights of 10 people

Before = (100, 125, 95, 96, 98, 102, 115, 104, 109, 110)

After = (95, 80, 75, 98, 90, 100, 110, 85, 100, 101)

H₀: The diet program is not effective

> $x = c(100, 125, 95, 96, 98, 102, 115, 104, 109, 110)$

> $y = c(95, 80, 75, 98, 90, 100, 110, 85, 100, 101)$

> t.test(x, y, paired = T, alternative = "less")

Paired t-test

data: x and y

t = 2.3215, df = 9, p-value = 0.9773

Alternative hypothesis: True difference in means is less than 0

95% confidence interval

Q. 3

-Inf 17.89635

Sample estimates:

Mean of the differences 10

4] Marks before and after a training program is given below:

Before = 20, 25, 32, 28, 27, 36, 35, 25

After = 30, 35, 32, 37, 37, 40, 40, 23

Test the hypothesis that training program is effective or not.
 H_0 = The training program is not effective

> $x = c(20, 25, 32, 28, 27, 36, 35, 25)$

> $y = c(30, 35, 32, 37, 37, 40, 40, 23)$

> t.test(x, y, paired = T, alternative = "greater")

Paired t-test

Data: x and y

t = -3.3859, df = 7, p-value = 0.9942

Alternative hypothesis: True difference in means is greater than
percent confidence interval.

-8.967399

Sample estimates:

Mean of the difference -5.75

5] Two random sample were drawn from two normal populations
the values are:

A = 66, 67, 75, 76, 82, 84, 88, 90, 92

B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

Test Whether the population have same variance at 5% level

H_0 : Variance of the population are equal

> $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

> $y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

> var.test(x, y)

F test to compare two variances

Data: x and y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359

Alternative hypothesis: True ratio of variances is not equal to 1

95 percent confidence interval:

6.1833662 3.0360393

Sample estimates:

Ratio of variances 0.7068567

- 6] The A.P. of sample 100 observations is 52 if S.D is 7 test the hypothesis that the population mean 55 or not at 5% of level of significance.

H_0 : Population mean = 55

> n = 100

> mx = 52

> mo = 55

> sd = 7

> zcal = $(mx - mo) / (sd / \sqrt{n})$

> pvalue = $2 * (1 - pnorm(\text{abs}(zcal)))$

> pvalue

[1] 1.82153e-05

13

PRACTICAL NO 9

Chi Square and ANOVA

Use the following data to test whether the condition of the name depends upon the child condition or not.

		Condition of home	
		Clean	dirty
Condition of name	Child	clean	dirty
name	fairly	70	50
name	dirty	80	20
name	dirty	35	45

→ H₀: Condition of the name and child are independent

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = Matrix(x, nrow = m, ncol = n)

[1,]	70	50
[2,]	80	20
[3,]	35	45

> pvalue = chisq.test(y)

> pvalue

Pearson's chi-squared test
data = 4

χ^2 squared = 25.646, df = 2, pvalue = 2.698e-0.6

pvalue is less than 0.05. we reject H_0 at 5% LOS

Q] Table below shows the relation between the performances of mathematics and computer of CS students.

		Maths		
		HG	MG	LG
Comp	HG	56	71	12
	MG	47	163	38
	LG	14	42	85

H_0 : performance between maths and computer are independence

$$X = C(56, 47, 14, 71, 163, 42, 12, 38, 85)$$

$$m = 3$$

$$n = 3$$

$$Y = \text{matrix}(x, \text{ncol} = n)$$

[,1] [,2] [,3]

[1,]	56	71	12
[2,]	47	163	38
[3,]	14	42	85

117

pvalue.chisq.test(y)
pvalue

data y

x-squared = 145.78, df = 4, p-value < 2.2e-16

3) Varieties

Observation

A	50, 52
B.	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

Mean A, B, C, D

> x1 = c(50, 52)

> x2 = c(53, 55, 53)

> x3 = c(60, 58, 57, 56)

> x4 = c(52, 54, 54, 55)

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> oneway.test(values ~ ind, data = d, var.equal = TRUE)

anova = aov(values ~ ind, data = d)

F = 11.735, num df = 3, denom df = 9, p-value = 0.00183

summary(anova)

Non-Parametric Test

following are the amounts of sulphur oxide in mg/m³ in different areas of the city.

Data:

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26

Apply sign test to test the hypothesis that population median is 21.5 against the alternative it is less than 21.5

$$H_0: \text{population median} = 21.5$$

$$H_1: \text{It is less than } 21.5$$

$$\gt x = c(17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$$

$$\gt x$$

$$\gt x$$

$$\gt m = 21.5$$

$$\gt sp = \text{length}(x[x > m])$$

$$\gt sn = \text{length}(x[x < m])$$

$$\gt n = sp + sn$$

$$\gt n$$

$$[1] 20$$

$$\gt pr = \text{pbisom}(sp, n, 0.5)$$

$$\gt pr$$

$$[1] 0.411$$

NOTE: If the alternative is greater than median,
 $pr = \text{pbisom}(sn, n, 0.5)$

2] For the observations

12, 19, 31, 28, 43, 40, 55, 49, 70, 63

Apply sign test to test population median is 25 against the alternative is more than 25.

> $x = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$

> $m = 25$

> $sp = \text{length}(x[x > m])$

> $sn = \text{length}(x[x < m])$

> $n = sp + sn$

> $pv = \text{pbinom}\left(\frac{sp}{n}, n, 0.5\right)$

> pv

[1] 0.054

3] 80, 65, 63, 89, 61, 71, 58, 51, 48, 66

Test the hypothesis using wilcoxon sign test.

for testing the hypothesis that the median is 60, against alternative it is greater than 60.

H_0 : Median is 60

H_1 : Median is greater than 60.

> $x = c(80, 65, 63, 89, 61, 71, 58, 51, 48, 66)$

> $m = 60$

> $sp = \text{length}(x[x > m])$

> $sn = \text{length}(x[x < m])$

> $n = sp + sn$

> $pv = \text{pbisom}(m, n, 0.5)$

[1] 0.253

> wilcox.test(x, alter = "greater", mu = 60)
 $v=29$, p-value = 0.2386

Alternative hypothesis: true location is greater than 60

+ If the alternative is less,

wilcox.test(x, alter = "less", mu = -)

If the alternative is not equal to

wilcox.test(x, alter = "2.sided", mu = 6)

| Using wilcoxon test, test the hypothesis where the median is 12 against the alternative is less than 12.

Data:

12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20

> x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)

> m = 12

> sp = length(x[x > m])

> sn = length(x[x < m])

> n = sn + sp

> pv = pbisom(sn, n, 0.5)

> pv

[1]

> wilcox.test(x, alter = "less", mu = 12)

$v=25$, p-value = 0.775

Alternative hypothesis: true location is greater than 12