

## CS8501 THEORY OF COMPUTATION

### MULTIPLE CHOICE QUESTIONS (MCQ)

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### MULTIPLE CHOICE QUESTIONS (MCQ)

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#### UNIT I AUTOMATA FUNDAMENTALS

##### TOPIC 1 : Introduction to formal proof

1. Assume the  $R$  is a relation on a set  $A$ ,  $aRb$  is partially ordered such that  $a$  and  $b$  are

- a) reflexive
- b) transitive
- c) symmetric
- d) reflexive and transitive

**Answer:** d

**Explanation:** A partially ordered relation refers to one which is Reflexive, Transitive and Antisymmetric.

2. The non- Kleene Star operation accepts the following string of finite length over set  $A = \{0,1\}$  | where string  $s$  contains even number of 0 and 1

- a) 01,0011,010101
- b) 0011,11001100
- c)  $\epsilon$ , 0011,11001100
- d)  $\epsilon$ , 0011,11001100

**Answer:** b

**Explanation:** The Kleene star of  $A$ , denoted by  $A^*$ , is the set of all strings obtained by concatenating zero or more strings from  $A$ .

3. A regular language over an alphabet  $\Sigma$  is one that cannot be obtained from the basic languages using the operation

- a) Union
- b) Concatenation
- c) Kleene\*
- d) All of the mentioned

**Answer:** d

**Explanation:** Union, Intersection, Concatenation, Kleene\*, Reverse are all the closure properties of Regular Language.

**4. Statement 1: A Finite automata can be represented graphically;**

**Statement 2: The nodes can be its states;**

**Statement 3: The edges or arcs can be used for transitions**

**Hint: Nodes and Edges are for trees and forests too.**

**Which of the following make the correct combination?**

- a) Statement 1 is false but Statement 2 and 3 are correct
- b) Statement 1 and 2 are correct while 3 is wrong
- c) None of the mentioned statements are correct
- d) All of the mentioned

**Answer: d**

**Explanation:** It is possible to represent a finite automaton graphically, with nodes for states, and arcs for transitions.

**5. The minimum number of states required to recognize an octal number divisible by 3 are/is**

- a) 1
- b) 3
- c) 5
- d) 7

**Answer: b**

**Explanation:** According to the question, minimum of 3 states are required to recognize an octal number divisible by 3.

**6. Which of the following is a not a part of 5-tuple finite automata?**

- a) Input alphabet
- b) Transition function
- c) Initial State
- d) Output Alphabet

**Answer: d**

**Explanation:** A FA can be represented as  $FA = (Q, \Sigma, \delta, q_0, F)$  where  $Q$ =Finite Set of States,  $\Sigma$ =Finite Input Alphabet,  $\delta$ =Transition Function,  $q_0$ =Initial State,  $F$ =Final/Acceptance State).

**7. If an Infinite language is passed to Machine M, the subsidiary which gives a finite solution to the infinite input tape is \_\_\_\_\_**

- a) Compiler
- b) Interpreter
- c) Loader and Linkers
- d) None of the mentioned

**Answer:** a

**Explanation:** A Compiler is used to give a finite solution to an infinite phenomenon. Example of an infinite phenomenon is Language C, etc.

**8. The number of elements in the set for the Language  $L = \{x \in (\Sigma)^* \mid \text{length of } x \text{ is at most } 2\}$  and  $\Sigma = \{0,1\}$  is \_\_\_\_\_**

- a) 7
- b) 6
- c) 8
- d) 5

**Answer:** a

**Explanation:**  $\Sigma^* = \{\epsilon, 0, 1, 00, 11, 01, 10\}$  = 7.

**9. For the following change of state in FA, which of the following codes is an incorrect option?**

- a)  $\delta(m, 1) = n$
- b)  $\delta(0, n) = m$
- c)  $\delta(m, 0) = \epsilon$
- d) s: accept = false; cin >> char;  
if char = "0" goto n;

**Answer:** b

**Explanation:**  $\delta(QX\Sigma) = Q1$  is the correct representation of change of state. Here,  $\delta$  is called the Transition function.

**10. Given:  $\Sigma = \{a, b\}$**

**$L = \{x \in \Sigma^* \mid x \text{ is a string combination}\}$**

**$\Sigma^4$  represents which among the following?**

- a)  $\{aa, ab, ba, bb\}$
- b)  $\{aaaa, abab, \epsilon, abaa, aabb\}$
- c)  $\{aaa, aab, aba, bbb\}$
- d) All of the mentioned

**Answer:** b

**Explanation:**  $\Sigma^*$  represents any combination of the given set while  $\Sigma^x$  represents the set of combinations with length x where  $x \in \mathbb{N}$ .

## TOPIC 2: Finite Automata

1. There are \_\_\_\_\_ tuples in finite state machine.

- a) 4
- b) 5
- c) 6
- d) unlimited

### SOLUTION

**Answer: b**

**Explanation:** States, input symbols, initial state, accepting state and transition function.

2. Transition function maps.

- a)  $\Sigma * Q \rightarrow \Sigma$
- b)  $Q * Q \rightarrow \Sigma$
- c)  $\Sigma * \Sigma \rightarrow Q$
- d)  $Q * \Sigma \rightarrow Q$

### SOLUTION

**Answer: d**

**Explanation:** Inputs are state and input string output is states.

3. Number of states require to accept string ends with 10.

- a) 3
- b) 2
- c) 1
- d) can't be represented.

### SOLUTION

**Answer: a**

**Explanation:** This is minimal finite automata.

4. Extended transition function is .

- a)  $Q * \Sigma^* \rightarrow Q$
- b)  $Q * \Sigma \rightarrow Q$
- c)  $Q^* * \Sigma^* \rightarrow \Sigma$
- d)  $Q * \Sigma \rightarrow \Sigma$

### SOLUTION

**Answer: a**

**Explanation:** This takes single state and string of input to produce a state.

5.  $\delta^*(q, ya)$  is equivalent to .

- a)  $\delta((q, y), a)$
- b)  $\delta(\delta^*(q, y), a)$
- c)  $\delta(q, ya)$
- d) independent from  $\delta$  notation

### SOLUTION

**Answer: b**

**Explanation:** First it parse y string after that it parse a.

6. String X is accepted by finite automata if .

- a)  $\delta^*(q, x) \in A$
- b)  $\delta(q, x) \in A$
- c)  $\delta^*(Q_0, x) \in A$
- d)  $\delta(Q_0, x) \in A$

### SOLUTION

**Answer: c**

**Explanation:** If automata starts with starting state and after finite moves if reaches to final step then it called accepted.

7. Languages of a automata is

- a) If it is accepted by automata
- b) If it halts
- c) If automata touch final state in its life time
- d) All language are language of automata

**SOLUTION**

**Answer: a**

**Explanation:** If a string accepted by automata it is called language of automata.

8. Language of finite automata is.

- a) Type 0
- b) Type 1
- c) Type 2
- d) Type 3

**SOLUTION**

**Answer: d**

**Explanation:** According to Chomsky classification.

9. Finite automata requires minimum \_\_\_\_\_ number of stacks.

- a) 1
- b) 0
- c) 2
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Finite automata doesn't require any stack operation .

10. Number of final state require to accept  $\Phi$  in minimal finite automata.

- a) 1
- b) 2
- c) 3
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** No final state requires.

11. Regular expression for all strings starts with ab and ends with bba is.

- a)  $aba^*b^*bba$
- b)  $ab(ab)^*bba$
- c)  $ab(a+b)^*bba$
- d) All of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Starts with ab then any number of a or b and ends with bba.

12. How many DFA's exists with two states over input alphabet {0,1} ?

- a) 16
- b) 26
- c) 32
- d) 64

**SOLUTION**

**Answer:** d

**Explanation:** Number of DFA's =  $2n * n(2^n)$ .

13. The basic limitation of finite automata is that

- a) It can't remember arbitrary large amount of information.
- b) It sometimes recognize grammar that are not regular.
- c) It sometimes fails to recognize regular grammar.
- d) All of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** Because there is no memory associated with automata.

14. Number of states require to simulate a computer with memory capable of storing '3' words each of length '8'.

- a)  $3 * 28$
- b)  $2(3*8)$
- c)  $2(3+8)$
- d) None of the mentioned

**SOLUTION**

**Answer:** b

**Explanation:**  $2(m*n)$  states requires .

15. FSM with output capability can be used to add two given integer in binary representation. This is

- a) True
- b) False
- c) May be true
- d) None of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** Use them as a flip flop output .

### TOPIC 3: Deterministic Finite Automata

1. Which of the following not an example Bounded Information?

- a) fan switch outputs {on, off}
- b) electricity meter reading
- c) colour of the traffic light at the moment
- d) none of the mentioned

### SOLUTION

**Answer: b**

**Explanation:** Bounded information refers to one whose output is limited and it cannot be said what were the recorded outputs previously until memorized.

2. A Language for which no DFA exist is a \_\_\_\_\_

- a) Regular Language
- b) Non-Regular Language
- c) May be Regular
- d) Cannot be said

### SOLUTION

**Answer: b**

**Explanation:** A language for which there is no existence of a deterministic finite automata is always Non Regular and methods like Pumping Lemma can be used to prove the same.

3. A DFA cannot be represented in the following format

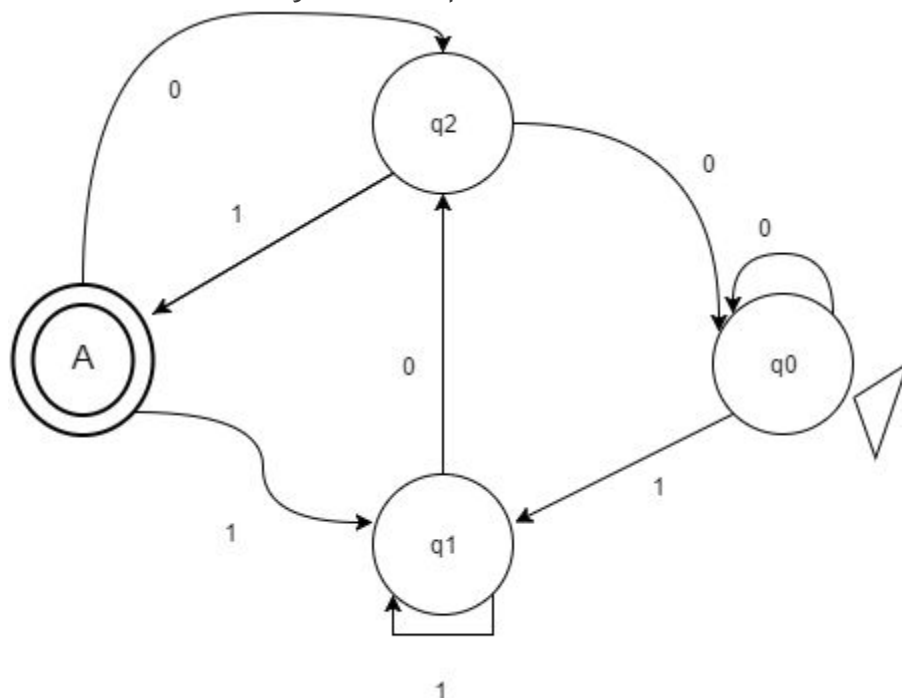
- a) Transition graph
- b) Transition Table
- c) C code
- d) None of the mentioned

### SOLUTION

**Answer: d**

**Explanation:** A DFA can be represented in the following formats: Transition Graph, Transition Table, Transition tree/forest/Any programming Language.

4. What the following DFA accepts?





- a) x is a string such that it ends with '101'
- b) x is a string such that it ends with '01'
- c) x is a string such that it has odd 1's and even 0's
- d) x is a strings such that it has starting and ending character as 1

**SOLUTION**

**Answer: a**

**Explanation:** Strings such as {1101,101,10101} are being accepted while {1001,11001} are not. Thus, this conclusion leads to option a.

5. When are 2 finite states equivalent?

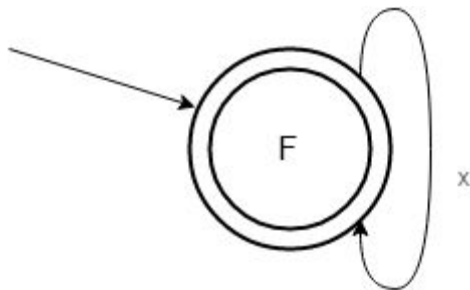
- a) Same number of transitions
- b) Same number of states
- c) Same number of states as well as transitions
- d) Both are final states

**SOLUTION**

**Answer: c**

**Explanation:** Two states are said to be equivalent if and only if they have same number of states as well as transitions.

6. What does the following figure most correctly represents?



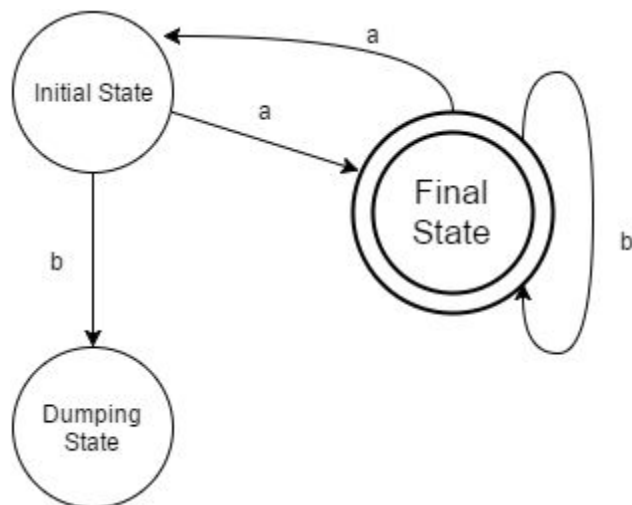
- a) Final state with loop x
- b) Transitional state with loop x
- c) Initial state as well as final state with loop x
- d) Insufficient Data

**SOLUTION**

**Answer: c**

**Explanation:** The figure represents the initial as well as the final state with an iteration of x.

7. Which of the following will not be accepted by the following DFA?



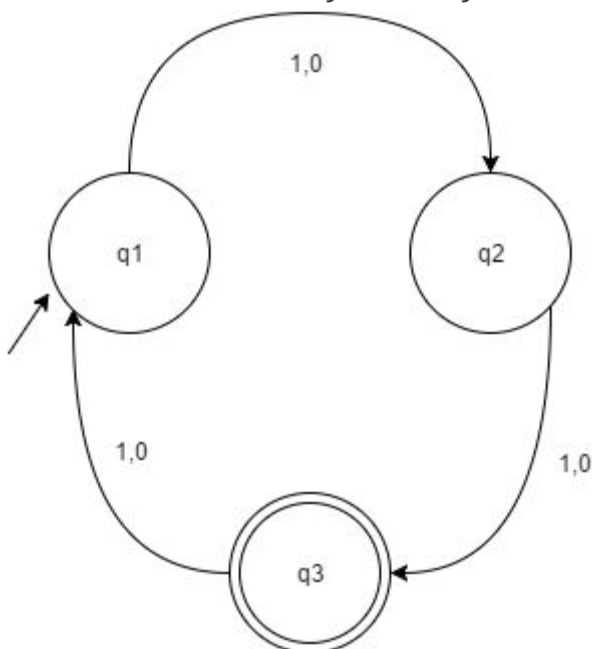
- a) ababaabaa
- b) abbbaa
- c) abbbaabb
- d) abbaabbaa

**SOLUTION**

**Answer: a**

**Explanation:** All the Strings are getting accepted except 'ababaabaa' as it is directed to dumping state. Dumping state also refers to the reject state of the automata.

8. Which of the following will the given DFA won't accept?



- a)  $\epsilon$
- b) 11010
- c) 10001010
- d) String of letter count 11

### SOLUTION

**Answer:** a

**Explanation:** As the initial state is not made an acceptance state, thus  $\epsilon$  will not be accepted by the given DFA. For the automata to accept  $\epsilon$  as an entity, one should make the initial state as also the final state.

9. Can a DFA recognize a palindrome number?

- a) Yes
- b) No
- c) Yes, with input alphabet as  $\Sigma^*$
- d) Can't be determined

### SOLUTION

**Answer:** b

**Explanation:** Language to accept a palindrome number or string will be non-regular and thus, its DFA cannot be obtained. Though, PDA is possible.

10. Which of the following is not an example of finite state machine system?

- a) Control Mechanism of an elevator
- b) Combinational Locks
- c) Traffic Lights
- d) Digital Watches

### SOLUTION

**Answer:** d

**Explanation:** Proper and sequential combination of events leads the machines to work in hand which includes The elevator, Combinational Locks, Traffic Lights, vending machine, etc. Other applications of Finite machine state system are Communication Protocol Design, Artificial Intelligence Research, A Turnstile, etc.

## TOPIC 4: Non-deterministic Finite Automata

1. Which of the following options is correct?

Statement 1: Initial State of NFA is Initial State of DFA.

Statement 2: The final state of DFA will be every combination of final state of NFA.

- a) Statement 1 is true and Statement 2 is true
- b) Statement 1 is true and Statement 2 is false
- c) Statement 1 can be true and Statement 2 is true
- d) Statement 1 is false and Statement 2 is also false

### SOLUTION

**Answer:** a

**Explanation:** Statement 1 and 2 always true for a given Language.

2. Given Language:  $L = \{ab \cup aba\}^*$

If X is the minimum number of states for a DFA and Y is the number of states to construct the NFA,

$$|X - Y| = ?$$

- a) 2
- b) 3
- c) 4
- d) 1

**SOLUTION**

**Answer: a**

**Explanation:** Construct the DFA and NFA individually, and then attain the difference of states.

3. An automaton that presents output based on previous state or current input:

- a) Acceptor
- b) Classifier
- c) Transducer
- d) None of the mentioned.

**SOLUTION**

**Answer: c**

**Explanation:** A transducer is an automaton that produces an output on the basis of what input has been given currently or previous state.

4. If NFA of 6 states excluding the initial state is converted into DFA, maximum possible number of states for the DFA is ?

- a) 64
- b) 32
- c) 128
- d) 127

**SOLUTION**

**Answer: c**

**Explanation:** The maximum number of sets for DFA converted from NFA would be not greater than  $2^n$ .

5. NFA, in its name has 'non-deterministic' because of :

- a) The result is undetermined
- b) The choice of path is non-deterministic
- c) The state to be transited next is non-deterministic
- d) All of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Non deterministic or deterministic depends upon the definite path defined for the transition from one state to another or undefined (multiple paths).

6. Which of the following is correct proposition?

Statement 1: Non determinism is a generalization of Determinism.

Statement 2: Every DFA is automatically an NFA

- a) Statement 1 is correct because Statement 2 is correct
- b) Statement 2 is correct because Statement 2 is correct
- c) Statement 2 is false and Statement 1 is false

d) Statement 1 is false because Statement 2 is false

**SOLUTION**

**Answer: b**

**Explanation:** DFA is a specific case of NFA.

7. Given Language  $L = \{x \in \{a, b\}^* \mid x \text{ contains aba as its substring}\}$

Find the difference of transitions made in constructing a DFA and an equivalent NFA?

a) 2

b) 3

c) 4

d) Cannot be determined.

**SOLUTION**

**Answer: a**

**Explanation:** The individual Transition graphs can be made and the difference of transitions can be determined.

8. The construction time for DFA from an equivalent NFA (m number of node) is:

a)  $O(m^2)$

b)  $O(2m)$

c)  $O(m)$

d)  $O(\log m)$

**SOLUTION**

**Answer: b**

**Explanation:** From the coded NFA-DFA conversion.

9. If n is the length of Input string and m is the number of nodes, the running time of DFA is x that of NFA. Find x?

a)  $1/m^2$

b)  $2m$

c)  $1/m$

d)  $\log m$

**SOLUTION**

**Answer: a**

**Explanation:** Running time of DFA:  $O(n)$  and Running time of NFA  $= O(m^2n)$ .

10. Which of the following option is correct?

a) NFA is slower to process and its representation uses more memory than DFA

b) DFA is faster to process and its representation uses less memory than NFA

c) NFA is slower to process and its representation uses less memory than DFA

d) DFA is slower to process and its representation uses less memory than NFA

**SOLUTION**

**Answer: c**

**Explanation:** NFA, while computing strings, take parallel paths, make different copies of input and goes along different paths in order to search for the result. This creates the difference in processing speed of DFA and NFA.

### TOPIC 5: Finite Automata with Epsilon Transitions

1. According to the given transitions, which among the following are the epsilon closures of  $q_1$  for the given NFA?

$$\Delta(q_1, \epsilon) = \{q_2, q_3, q_4\}$$

$$\Delta(q_4, 1) = q_1$$

$$\Delta(q_1, \epsilon) = q_1$$

- a)  $q_4$
- b)  $q_2$
- c)  $q_1$
- d)  $q_1, q_2, q_3, q_4$

**SOLUTION**

**Answer: d**

**Explanation:** The set of states which can be reached from  $q$  using  $\epsilon$ -transitions, is called the  $\epsilon$ -closure over state  $q$ .

2. State true or false?

Statement: An NFA can be modified to allow transition without input alphabets, along with one or more transitions on input symbols.

- a) True
- b) False

**SOLUTION**

**Answer: a**

**Explanation:** It is possible to construct an NFA with  $\epsilon$ -transitions, presence of no input symbols, and that is called NFA with  $\epsilon$ -moves.

3. State true or false?

Statement:  $\epsilon$  (Input) does not appear on Input tape.

- a) True
- b) False

**Answer: a**

**SOLUTION**

**Explanation:**  $\epsilon$  does not appear on Input tape,  $\epsilon$  transition means a transition without scanning a symbol i.e. without moving the read head.

4. Statement 1:  $\epsilon$  - transition can be called as hidden non-determinism.

Statement 2:  $\delta(q, \epsilon) = p$  means from  $q$  it can jump to  $p$  with a shift in read head.

Which among the following options is correct?

- a) Statement 1 and 2, both are correct
- b) Statement 1 and 2, both are wrong
- c) Statement 1 is correct while Statement 2 is wrong
- d) Statement 1 is wrong while Statement 2 is correct

**SOLUTION**

**Answer: c**

**Explanation:** The transition with  $\epsilon$  leads to a jump but without any shift in read head. Further, the method can be called one to introduce hidden non-determinism.

5.  $\epsilon$  - closure of  $q_1$  in the given transition graph:

- a)  $\{q_1\}$
- b)  $\{q_0, q_2\}$
- c)  $\{q_1, q_2\}$
- d)  $\{q_0, q_1, q_2\}$

**SOLUTION**

**Answer: c**

**Explanation:**  $\epsilon$  -closure is defined as the set of states being reached through  $\epsilon$  -transitions from a starting state.

6. Predict the total number of final states after removing the  $\epsilon$  -moves from the given NFA?

- a) 1
- b) 2
- c) 3
- d) 0

**SOLUTION**

**Answer: c**

**Explanation:** The NFA which would result after eliminating  $\epsilon$  -moves can be shown diagrammatically.

7. For NFA with  $\epsilon$  -moves, which among the following is correct?

- a)  $\Delta: Q \times (\Sigma \cup \{\epsilon\}) \rightarrow P(Q)$
- b)  $\Delta: Q \times (\Sigma) \rightarrow P(Q)$
- c)  $\Delta: Q \times (\Sigma^*) \rightarrow P(Q)$
- d) All of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Due to the presence of  $\epsilon$  symbol, or rather an epsilon-move, the input alphabets unites with it to form a set including  $\epsilon$ .

8. Which among the following is false?

$\epsilon$  -closure of a subset  $S$  of  $Q$  is:

- a) Every element of  $S \in Q$
- b) For any  $q \in \epsilon(S)$ , every element of  $\delta(q, \epsilon)$  is in  $\epsilon(S)$
- c) No other element is in  $\epsilon(S)$
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** All the mentioned are the closure properties of  $\epsilon$  and encircles all the elements if it satisfies the following options:

- a) Every element of  $S \in Q$
  - b) For any  $q \in \epsilon(S)$ , every element of  $\delta(q, \epsilon)$  is in  $\epsilon(S)$
  - c) No other element is in  $\epsilon(S)$
9. The automaton which allows transformation to a new state without consuming any

input symbols:

- a) NFA
- b) DFA
- c) NFA-I
- d) All of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** NFA-I or e-NFA is an extension of Non deterministic Finite Automata which are usually called NFA with epsilon moves or lambda transitions.

10. e-transitions are

- a) conditional
- b) unconditional
- c) input dependent
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** An epsilon move is a transition from one state to another that doesn't require any specific condition.

11. The \_\_\_\_\_ of a set of states, P, of an NFA is defined as the set of states reachable from any state in P following e-transitions.

- a) e-closure
- b) e-pack
- c) Q in the tuple
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** The e-closure of a set of states, P, of an NFA is defined as the set of states reachable from any state in P following e-transitions.

12. The e-NFA recognizable languages are not closed under :

- a) Union
- b) Negation
- c) Kleene Closure
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** The languages which are recognized by an epsilon Non deterministic automata are closed under the following operations:

- a) Union
- b) Intersection
- c) Concatenation
- d) Negation
- e) Star



f) Kleene closure

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## UNIT II REGULAR EXPRESSIONS AND LANGUAGES

### TOPIC 1: Regular Expressions

1. L is a regular Language if and only If the set of \_\_\_\_\_ classes of IL is finite.

- a) Equivalence
- b) Reflexive
- c) Myhill
- d) Nerode

**SOLUTION**

**Answer: a**

**Explanation:** According to Myhill Nerode theorem, the corollary proves the given statement correct for equivalence classes.

2. A language can be generated from simple primitive language in a simple way if and only if

- a) It is recognized by a device of infinite states
- b) It takes no auxiliary memory
- c) Both are correct
- d) Both are wrong

**SOLUTION**

**Answer: b**

**Explanation:** A language is regular if and only if it can be accepted by a finite automaton. Secondly, It supports no concept of auxiliary memory as it loses the data as soon as the device is shut down.

3. Which of the following does not represents the given language?

Language:  $\{0,01\}$

- a)  $0+01$
- b)  $\{0\} \cup \{01\}$
- c)  $\{0\} \cup \{0\}\{1\}$
- d)  $\{0\} \wedge \{01\}$

**SOLUTION**

**Answer: d**

**Explanation:** The given option represents  $\{0, 01\}$  in different forms using set operations and Regular Expressions. The operator like  $\wedge$ ,  $\vee$ , etc. are logical operation and they form invalid regular expressions when used.

4. According to the given language, which among the following expressions does it corresponds to?

Language  $L = \{x \in \{0,1\}^* \mid x \text{ is of length 4 or less}\}$

- a)  $(0+1+0+1+0+1+0+1)^4$
- b)  $(0+1)^4$

- c)  $(0+1)^4$
- d)  $(0+1+\epsilon)^4$

**SOLUTION**

**Answer: d**

**Explanation:** The extended notation would be  $(0+1)^4$  but however, we may allow some or all the factors to be  $\epsilon$ . Thus  $\epsilon$  needs to be included in the given regular expression.

5. Which among the following looks similar to the given expression?

$((0+1).(0+1))^*$

- a)  $\{x \in \{0,1\}^* \mid x \text{ is all binary number with even length}\}$
- b)  $\{x \in \{0,1\} \mid x \text{ is all binary number with even length}\}$
- c)  $\{x \in \{0,1\}^* \mid x \text{ is all binary number with odd length}\}$
- d)  $\{x \in \{0,1\} \mid x \text{ is all binary number with odd length}\}$

**SOLUTION**

**Answer: a**

**Explanation:** The given regular expression corresponds to a language of binary strings which is of even length including a length of 0.

6. If R represents a regular language, which of the following represents the Venn-diagram most correctly?

- a) An Irregular Set
- b)  $R^*$
- c) R complement
- d) R reverse

**SOLUTION**

**Answer: b**

**Explanation:** The given diagram represents the Kleene operation over the Regular Language R in which the final states become the initial and the initial state becomes final.

7. The given NFA corresponds to which of the following Regular expressions?

- a)  $(0+1)^*(00+11)(0+1)^*$
- b)  $(0+1)^*(00+11)^*(0+1)^*$
- c)  $(0+1)^*(00+11)(0+1)$
- d)  $(0+1)(00+11)(0+1)^*$

**SOLUTION**

**Answer: a**

**Explanation:** The transition states shown are the result of breaking down the given regular expression in fragments. For dot operation, we change a state, for union (plus) operation, we diverge into two transitions and for Kleene Operation, we apply a loop.

8. Concatenation Operation refers to which of the following set operations:

- a) Union
- b) Dot
- c) Kleene
- d) Two of the options are correct

**SOLUTION**

**Answer: b**

**Explanation:** Two operands are said to be performing Concatenation operation  $AB = A \cdot B = \{xy: x \in A \ \& \ y \in B\}$ .

9. Concatenation of R with  $\Phi$  outputs:

- a) R
- b)  $\Phi$
- c)  $R \cdot \Phi$
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** By distributive property (Regular expression identities), we can prove the given identity to be  $\Phi$ .

10.  $RR^*$  can be expressed in which of the forms:

- a)  $R^+$
- b)  $R^-$
- c)  $R^+ \cup R^-$
- d) R

**SOLUTION**

**Answer: a**

**Explanation:**  $RR^* = R^+$  as  $R^+$  means the occurrence to be at least once.

## TOPIC 2: FA and Regular Expressions

1. What kind of expressions do we used for pattern matching?

- a) Regular Expression
- b) Rational Expression
- c) Regular & Rational Expression
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** In automata theory, Regular Expression(sometimes also called the Rational Expression ) is a sequence or set of characters that define a search pattern, mainly for the use in pattern matching with strings or string matching.

2. Which of the following do Regexps do not find their use in?

- a) search engines
- b) word processors
- c) sed
- d) none of the mentioned

## SOLUTION

**Answer: d**

**Explanation:** Regexp processors are found in several search engines, search and replace mechanisms, and text processing utilities.

3. Which of the following languages have built in regexps support?

- a) Perl
- b) Java
- c) Python
- d) C++

## SOLUTION

**Answer: a**

**Explanation:** Many languages come with built in support of regexps like Perl, Javascript, Ruby etc. While some provide support using standard libraries like .NET, Java, Python, C++, C and POSIX.

4. The following is/are an approach to process a regexp:

- a) Construction of NFA and subsequently, a DFA.
- b) Thompson's Construction Algorithm
- c) Both (a) and (b)
- d) None of the mentioned

## SOLUTION

**Answer: c**

**Explanation:** A regexp processor translates the syntax into internal representation which can be executed and matched with a string and that internal representation can have several approaches like the ones mentioned.

5. Are the given two patterns equivalent?

- (1) gray|grey
- (2) gr(a|e)y

- a) yes
- b) no

## SOLUTION

**Answer: a**

**Explanation:** Paranthesis can be used to define the scope and precedence of operators. Thus, both the expression represents the same pattern.

6. Which of the following are not quantifiers?

- a) Kleene plus +
- b) Kleene star \*
- c) Question mark ?
- d) None of the mentioned

## SOLUTION

**Answer: d**

**Explanation:** A quantifier after a token specifies how often the preceding element is allowed to occur. ?, \*, +, {n}, {min, }, {min, max} are few quantifiers we use in regexps

implementations.

7. Which of the following cannot be used to decide whether and how a given regexp matches a string:

- a) NFA to DFA
- b) Lazy DFA algorithm
- c) Backtracking
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** There are at least three algorithms which decides for us, whether and how a regexp matches a string which included the transformation of Non deterministic automaton to deterministic finite automaton, The lazy DFA algorithm where one simulates the NFA directly, building each DFA on demand and then discarding it at the next step and the process of backtracking whose running time is exponential.

8. What does the following segment of code output?

```
$string1 = "Hello World\n";  
if ($string1 =~ m/(H..)(l..)/) {  
    print "We matched '$1' and '$2'.\n";  
}
```

- a) We matched 'Hel' and 'ld'
- b) We matched 'Hel' and 'lld'
- c) We matched 'Hel' and 'lo '
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** () groups a series of pattern element to a single element.

When we use pattern in parenthesis, we can use any of '\$1', '\$2' later to refer to the previously matched pattern.

9. Given segment of code:

```
$string1 = "Hello\nWorld\n";  
if ($string1 =~ m/d\nz/) {  
    print "$string1 is a string ";  
    print "that ends with 'd\\n'.\n";  
}
```

What does the symbol /z does?

- a) changes line
- b) matches the beginning of a string
- c) matches the end of a string
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** It matches the end of a string and not an internal line. The given segment of code outputs:

Hello

World

is a string that ends with 'd\n'

10. Conversion of a regular expression into its corresponding NFA :

a) Thompson's Construction Algorithm

b) Powerset Construction

c) Kleene's algorithm

d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Thompson construction algorithm is an algorithm in automata theory used to convert a given regular expression into NFA. Similarly, Kleene algorithm is used to convert a finite automaton to a regular expression.

### TOPIC 3: Proving Languages not to be regular

1. Relate the following statement:

Statement: All sufficiently long words in a regular language can have a middle section of words repeated a number of times to produce a new word which also lies within the same language.

a) Turing Machine

b) Pumping Lemma

c) Arden's theorem

d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Pumping lemma defines an essential property for every regular language in automata theory. It has certain rules which decide whether a language is regular or not.

2. While applying Pumping lemma over a language, we consider a string  $w$  that belongs to  $L$  and fragment it into \_\_\_\_\_ parts.

a) 2

b) 5

c) 3

d) 6

**SOLUTION**

**Answer: c**

**Explanation:** We select a string  $w$  such that  $w=xyz$  and  $|y|>0$  and other conditions. However, there exists an integer  $n$  such that  $|w| \geq n$  for any  $w \in L$ .

3. If we select a string  $w$  such that  $w \in L$ , and  $w = xyz$ . Which of the following portions cannot be an empty string?

- a)  $x$
- b)  $y$
- c)  $z$
- d) all of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The lemma says, the portion  $y$  in  $xyz$  cannot be zero or empty i.e.  $|y| > 0$ , this condition needs to be fulfilled to check the conclusion condition.

4. Let  $w = xyz$  and  $y$  refers to the middle portion and  $|y| > 0$ . What do we call the process of repeating  $y$  0 or more times before checking that they still belong to the language  $L$  or not?

- a) Generating
- b) Pumping
- c) Producing
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The process of repetition is called pumping and so, pumping is the process we perform before we check whether the pumped string belongs to  $L$  or not.

5. There exists a language  $L$ . We define a string  $w$  such that  $w \in L$  and  $w = xyz$  and  $|w| \geq n$  for some constant integer  $n$ . What can be the maximum length of the substring  $xy$  i.e.  $|xy| \leq ?$

- a)  $n$
- b)  $|y|$
- c)  $|x|$
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** It is the first conditional statement of the lemma that states that  $|xy| \leq n$ , i.e. the maximum length of the substring  $xy$  in  $w$  can be  $n$  only.

6. Fill in the blank in terms of  $p$ , where  $p$  is the maximum string length in  $L$ .

Statement: Finite languages trivially satisfy the pumping lemma by having  $n = \underline{\hspace{2cm}}$

- a)  $p+1$
- b)  $p-1$
- c)  $p-1$
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Finite languages trivially satisfy the pumping lemma by having  $n$  equal to the maximum string length in  $L$  plus 1.

7. Answer in accordance to the third and last statement in pumping lemma:

For all \_\_\_\_\_  $xyiz \in L$

- a)  $i > 0$
- b)  $i < 0$
- c)  $i \leq 0$
- d)  $i \geq 0$

**SOLUTION**

**Answer: d**

**Explanation:** Suppose  $L$  is a regular language. Then there is an integer  $n$  so that for any  $x \in L$  and  $|x| \geq n$ , there are strings  $u, v, w$  so that

$x = uvw$

$|uv| \leq n$

$|v| > 0$

for any  $m \geq 0$ ,  $uvmw \in L$ .

8. If  $d$  is a final state, which of the following is correct according to the given diagram?

- a)  $x=p, y=qr, z=s$
- b)  $x=p, z=qrs$
- c)  $x=pr, y=r, z=s$
- d) All of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** The FSA accepts the string  $pqrs$ . In terms of pumping lemma, the string  $pqrs$  is broken into an  $x$  portion  $p$ , a  $y$  portion  $qr$  and a  $z$  portion  $s$ .

9. Let  $w$  be a string and fragmented by three variable  $x, y$ , and  $z$  as per pumping lemma. What does these variables represent?

- a) string count
- b) string
- c) both (a) and (b)
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Given:  $w = xyz$ . Here,  $xyz$  individually represents strings or rather substrings which we compute over conditions to check the regularity of the language.

10. Which of the following one can relate to the given statement:

Statement: If  $n$  items are put into  $m$  containers, with  $n > m$ , then atleast one container must contain more than one item.

- a) Pumping lemma
- b) Pigeon Hole principle
- c) Count principle
- d) None of the mentioned



### SOLUTION

**Answer:** b

**Explanation:** Pigeon hole principle states the following example: If there exists  $n=10$  pigeons in  $m=9$  holes, then since  $10 > 9$ , the pigeonhole principle says that at least one hole has more than one pigeon.

### TOPIC 4: Proving Languages not to be regular (Pumping Lemma)

1. Relate the following statement:

Statement: All sufficiently long words in a regular language can have a middle section of words repeated a number of times to produce a new word which also lies within the same language.

- a) Turing Machine
- b) Pumping Lemma
- c) Arden's theorem
- d) None of the mentioned

### SOLUTION

**Answer:** b

**Explanation:** Pumping lemma defines an essential property for every regular language in automata theory. It has certain rules which decide whether a language is regular or not.

2. While applying Pumping lemma over a language, we consider a string  $w$  that belong to  $L$  and fragment it into \_\_\_\_\_ parts.

- a) 2
- b) 5
- c) 3
- d) 6

### SOLUTION

**Answer:** c

**Explanation:** We select a string  $w$  such that  $w=xyz$  and  $|y| > 0$  and other conditions. However, there exists an integer  $n$  such that  $|w| \geq n$  for any  $w \in L$ .

3. If we select a string  $w$  such that  $w \in L$ , and  $w=xyz$ . Which of the following portions cannot be an empty string?

- a)  $x$
- b)  $y$
- c)  $z$
- d) all of the mentioned

### SOLUTION

**Answer:** b

**Explanation:** The lemma says, the portion  $y$  in  $xyz$  cannot be zero or empty i.e.  $|y| > 0$ , this condition needs to be fulfilled to check the conclusion condition.

4. Let  $w = xyz$  and  $y$  refers to the middle portion and  $|y| > 0$ . What do we call the process of repeating  $y$  0 or more times before checking that they still belong to the language  $L$  or not?

- a) Generating
- b) Pumping
- c) Producing
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The process of repeatation is called pumping and so, pumping is the process we perform before we check whether the pumped string belongs to  $L$  or not.

5. There exists a language  $L$ . We define a string  $w$  such that  $w \in L$  and  $w = xyz$  and  $|w| \geq n$  for some constant integer  $n$ . What can be the maximum length of the substring  $xy$  i.e.  $|xy| \leq ?$

- a)  $n$
- b)  $|y|$
- c)  $|x|$
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** It is the first conditional statement of the lemma that states that  $|xy| \leq n$ , i.e. the maximum length of the substring  $xy$  in  $w$  can be  $n$  only.

6. Fill in the blank in terms of  $p$ , where  $p$  is the maximum string length in  $L$ .

Statement: Finite languages trivially satisfy the pumping lemma by having  $n = \underline{\hspace{2cm}}$

- a)  $p+1$
- b)  $p-1$
- c)  $p-1$
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Finite languages trivially satisfy the pumping lemma by having  $n$  equal to the maximum string length in  $L$  plus 1.

7. Answer in accordance to the third and last statement in pumping lemma:

For all  $\underline{\hspace{2cm}} xyiz \in L$

- a)  $i > 0$
- b)  $i < 0$
- c)  $i \leq 0$
- d)  $i \geq 0$

**SOLUTION**

**Answer: d**

**Explanation:** Suppose  $L$  is a regular language. Then there is an integer  $n$  so that for any  $x \in L$  and  $|x| \geq n$ , there are strings  $u, v, w$  so that

$$\begin{array}{l} x = uvw \\ |uv| \leq n \\ |v| > 0 \end{array}$$

for any  $m \geq 0$ ,  $uvmw \in L$ .

8. If d is a final state, which of the following is correct according to the given diagram?

- a)  $x=p$ ,  $y=qr$ ,  $z=s$
- b)  $x=p$ ,  $z=qrs$
- c)  $x=pr$ ,  $y=r$ ,  $z=s$
- d) All of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** The FSA accepts the string pqr. In terms of pumping lemma, the string pqr is broken into an x portion p, a y portion qr and a z portion s.

9. Let w be a string and fragmented by three variable x, y, and z as per pumping lemma. What do these variables represent?

- a) string count
- b) string
- c) both (a) and (b)
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Given:  $w = xyz$ . Here, xyz individually represents strings or rather substrings which we compute over conditions to check the regularity of the language.

10. Which of the following one can relate to the given statement:

Statement: If n items are put into m containers, with  $n > m$ , then at least one container must contain more than one item.

- a) Pumping lemma
- b) Pigeon Hole principle
- c) Count principle
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Pigeon hole principle states the following example: If there exists  $n=10$  pigeons in  $m=9$  holes, then since  $10 > 9$ , the pigeonhole principle says that at least one hole has more than one pigeon.

#### TOPIC 4: Closure Properties of Regular Languages

1. If  $L_1$ ,  $L_2$  are regular and  $op(L_1, L_2)$  is also regular, then  $L_1$  and  $L_2$  are said to be \_\_\_\_\_ under an operation op.

- a) open
- b) closed

- c) decidable
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** If two regular languages are closed under an operation  $op$ , then the resultant of the languages over an operation  $op$  will also be regular.

2. Suppose a regular language  $L$  is closed under the operation halving, then the result would be:

- a)  $1/4 L$  will be regular
- b)  $1/2 L$  will be regular
- c)  $1/8 L$  will be regular
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** At first stage  $1/2 L$  will be regular and subsequently, all the options will be regular.

3. If  $L_1'$  and  $L_2'$  are regular languages, then  $L_1.L_2$  will be

- a) regular
- b) non regular
- c) may be regular
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Regular language is closed under complement operation. Thus, if  $L_1'$  and  $L_2'$  are regular so are  $L_1$  and  $L_2$ . And if  $L_1$  and  $L_2$  are regular so is  $L_1.L_2$ .

4. If  $L_1$  and  $L_2'$  are regular languages,  $L_1 \cap (L_2' \cup L_1)'$  will be

- a) regular
- b) non regular
- c) may be regular
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** If  $L_1$  is regular, so is  $L_1'$  and if  $L_1'$  and  $L_2'$  are regular so is  $L_1' \cup L_2'$ . Further, regular languages are also closed under intersection operation.

5. If  $A$  and  $B$  are regular languages,  $!(A' \cup B')$  is:

- a) regular
- b) non regular
- c) may be regular
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** If  $A$  and  $B$  are regular languages, then  $A \cap B$  is a regular language and  $A$

$\cap B$  is equivalent to  $!(A' \cup B')$ .

6. Which among the following are the boolean operations that under which regular languages are closed?

- a) Union
- b) Intersection
- c) Complement
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Regular languages are closed under the following operations:

- a) Regular expression operations
- b) Boolean operations
- c) Homomorphism
- d) Inverse Homomorphism

7. Suppose a language  $L_1$  has 2 states and  $L_2$  has 2 states. After using the cross product construction method, we have a machine  $M$  that accepts  $L_1 \cap L_2$ . The total number of states in  $M$ :

- a) 6
- b) 4
- c) 2
- d) 8

**SOLUTION**

**Answer: 4**

**Explanation:**  $M$  is defined as:  $(Q, S, d, q_0, F)$   
where  $Q = Q_1 * Q_2$  and  $F = F_1 * F_2$

8. If  $L$  is a regular language, then  $(L')' \cup L$  will be :

- a)  $L$
- b)  $L'$
- c)  $\emptyset$
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:**  $(L')'$  is equivalent to  $L$  and  $L \cup L$  is subsequently equivalent to  $L$ .

9. If  $L$  is a regular language, then  $((L')^r)^*$  is:

- a) regular
- b) non regular
- c) may be regular
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** If  $L$  is regular so is its complement, if  $L'$  is regular so is its reverse, if  $(L')^r$  is regular so is its Kleene.

10. Which among the following is the closure property of a regular language?

- a) Emptiness
- b) Universality
- c) Membership
- d) None of the mentioned

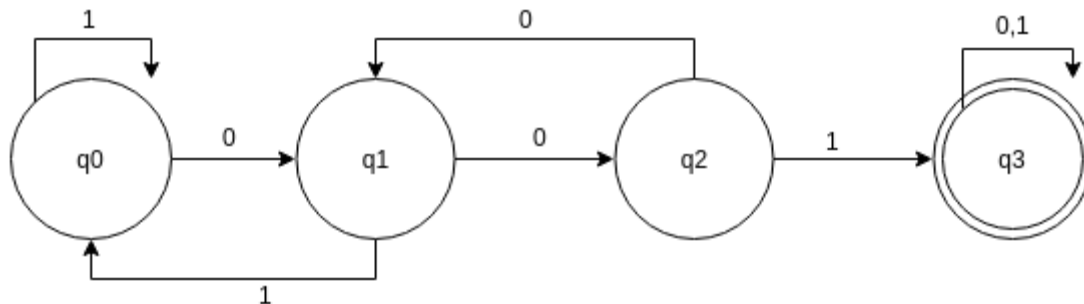
**SOLUTION**

**Answer: d**

**Explanation:** All the following mentioned are decidability properties of a regular language. The closure properties of a regular language include union, concatenation, intersection, Kleene, complement, reverse and many more operations.

### TOPIC 5: Equivalence and Minimization of Automata

1. Which of the following is same as the given DFA?



- a)  $(0+1)^*001(0+1)^*$
- b)  $1^*001(0+1)^*$
- c)  $(01)^*(0+0+1)(01)^*$
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** There needs to be 001 together in the string as an essential substring. Thus, the other components can be anything, 0 or 1 or e.

2. Which of the following statements is not true?

- a) Every language defined by any of the automata is also defined by a regular expression
- b) Every language defined by a regular expression can be represented using a DFA
- c) Every language defined by a regular expression can be represented using NFA with e moves
- d) Regular expression is just another representation for any automata definition

**SOLUTION**

**Answer: b**

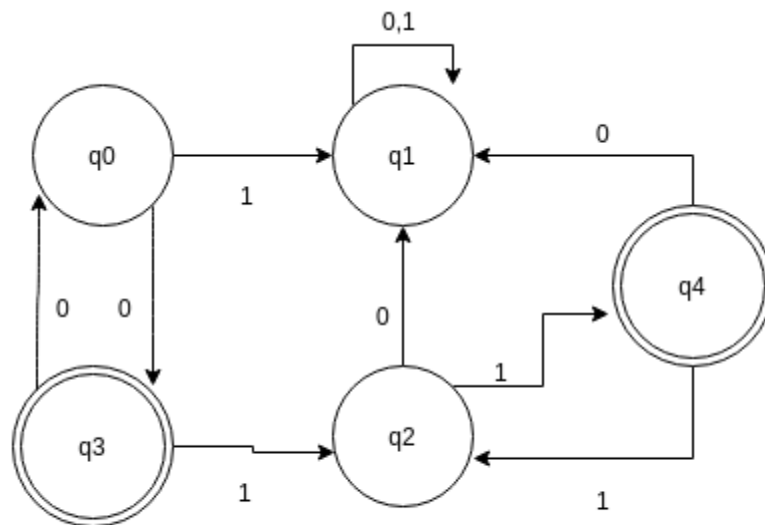
**Explanation:** Using NFA with e moves, we can represent all the regular expressions as an automata. As regular expressions include e, we need to use e moves.

3. The total number of states required to automate the given regular expression  $(00)^*(11)^*$

- a) 3
- b) 4
- c) 5
- d) 6

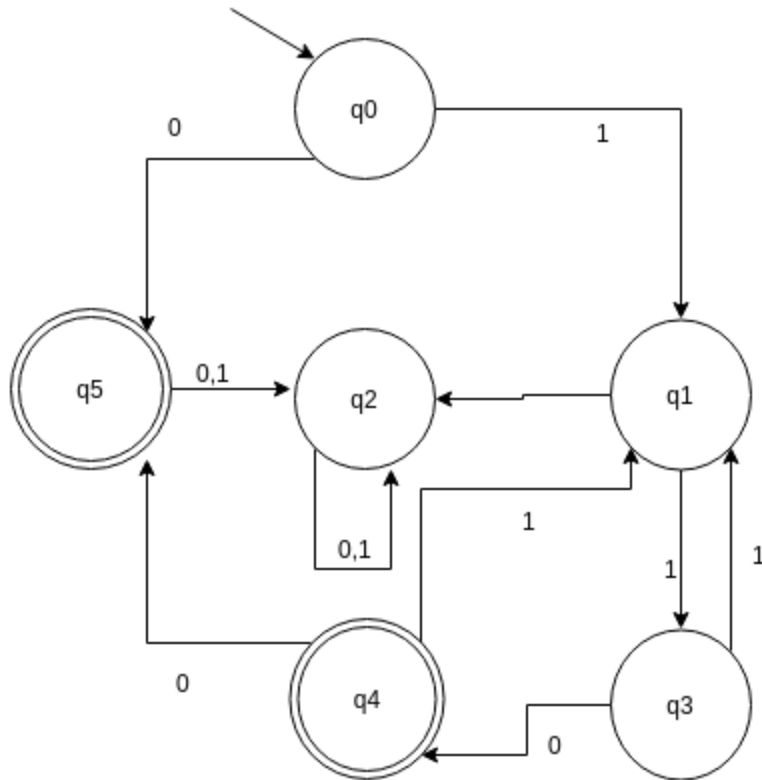
**SOLUTION**

**Answer: c**



**Explanation:**

4. Which of the given regular expressions correspond to the automata shown?



- a)  $(110+1)^*0$
- b)  $(11+110)^*1$
- c)  $(110+11)^*0$
- d)  $(1+110)^*1$

**SOLUTION**

**Answer: c**

**Explanation:** There is no state change for union operation, but has two different paths while for concatenation or dot operation, we have a state change for every element of the string.

5. Generate a regular expression for the following problem statement:

Password Validation: String should be 8-15 characters long. String must contain a number, an Uppercase letter and a Lower case letter.

- a)  $^(?=.*[a-z])(?=.*[A-Z])(?=.*\d).\{8,15\}$$
- b)  $^(?=.*[a-z])(?=.*[A-Z])(?=.*\d).\{9,16\}$$
- c)  $^(?=.*[a-z])(?=.*[A-Z])(?=.*\d).\{8,15\}$$
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Passwords like abc123, 123XYZ, should not be accepted. If one also wants to include special characters as one of the constraint, one can use the following regular expression:

$^(?=.*[a-z])(?=.*[A-Z])(?=.*\d)(?=.*[^\da-zA-Z]).\{8,15\}$$



6. Generate a regular expression for the following problem statement:

P(x): String of length 6 or less for  $\Sigma = \{0,1\}^*$

- a)  $(1+0+e)^6$
- b)  $(10)^6$
- c)  $(1+0)(1+0)(1+0)(1+0)(1+0)(1+0)$
- d) More than one of the mentioned is correct

**SOLUTION**

**Answer: a**

**Explanation:** As the input variables are under Kleene Operation, we need to include e, thus option c is not correct, thereby option (a) is the right answer.

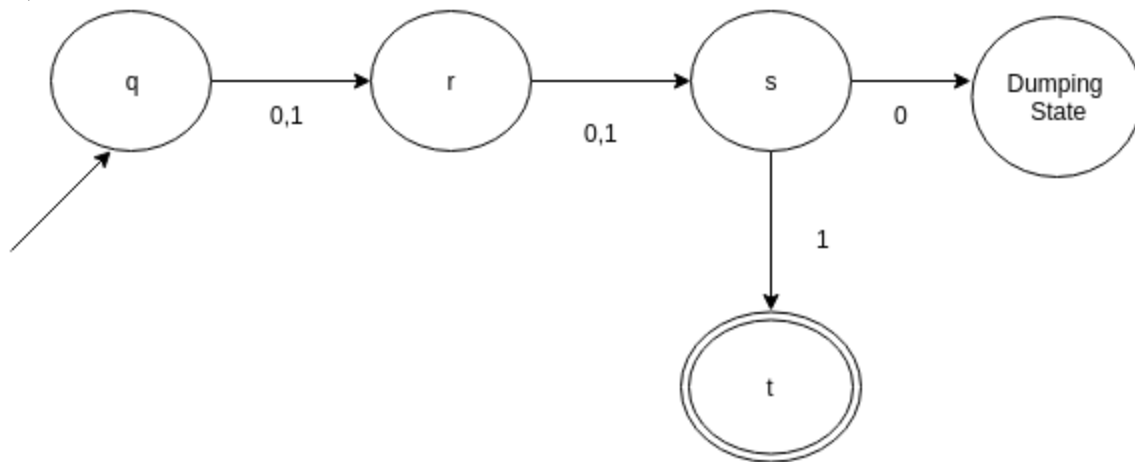
7. The minimum number of states required in a DFA (along with a dumping state) to check whether the 3rd bit is 1 or not for  $|n| \geq 3$

- a) 3
- b) 4
- c) 5
- d) 1

**SOLUTION**

**Answer: c**

**Explanation:**



8. Which of the regular expressions corresponds to the given problem statement:

P(x): Express the identifiers in C Programming language

l=letters

d=digits

- a)  $(l+_)(d+_)^*$
- b)  $(l+d+_)^*$
- c)  $(l+_)(l+d+_)^*$
- d)  $(_+d)(l+d+_)^*$

**SOLUTION**

**Answer: c**

**Explanation:** Identifiers in C Programming Language follows the following identifiers rule:

- a) The name of the identifier should not begin with a digit.
- b) It can only begin with a letter or an underscore.
- c) It can be of length 1 or more.

9. Generate a regular expression for the given language:

$L(x): \{x \in \{0,1\}^* \mid x \text{ ends with 1 and does not contain a substring 01}\}$

- a)  $(0+01)^*$
- b)  $(0+01)^*1$
- c)  $(0+01)^*(1+01)$
- d) All of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** (a) and (b) are the general cases where we restrict the acceptance of a string with substring 00 but we ignore the case where the string needs to end with 1 which thereby, does not allow the acceptance of e.

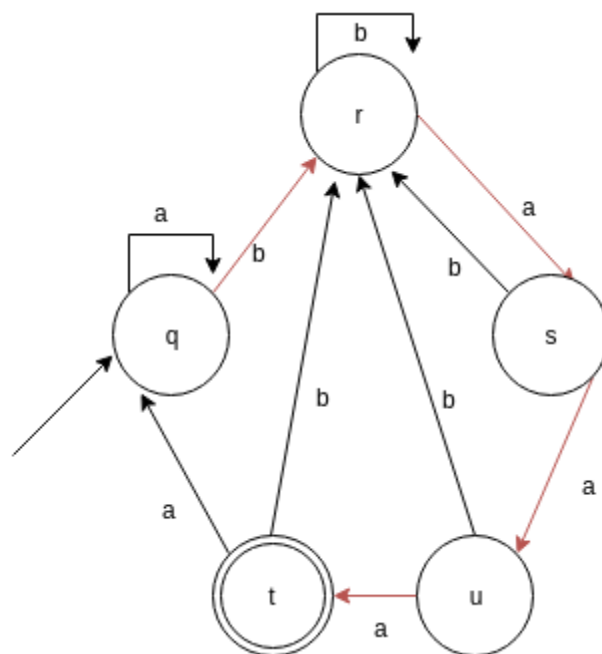
10. The minimum number of transitions to pass to reach the final state as per the following regular expression is:

$\{a,b\}^*\{baaa\}$

- a) 4
- b) 5
- c) 6
- d) 3

**SOLUTION**

**Answer: a**



**Explanation:**

## UNIT III CONTEXT FREE GRAMMAR AND LANGUAGES

### TOPIC 1: CFG

1. The entity which generate Language is termed as:

- a) Automata
- b) Tokens
- c) Grammar
- d) Data

#### SOLUTION

**Answer: c**

**Explanation:** The entity which accepts a language is termed as Automata while the one which generates it is called Grammar. Tokens are the smallest individual unit of a program.

2. Production Rule:  $aAb \rightarrow agb$  belongs to which of the following category?

- a) Regular Language
- b) Context free Language
- c) Context Sensitive Language
- d) Recursively Enumerable Language

#### SOLUTION

**Answer: c**

**Explanation:** Context Sensitive Language or Type 1 or Linearly Bounded Non deterministic Language has the production rule where the production is context dependent i.e.  $aAb \rightarrow agb$ .

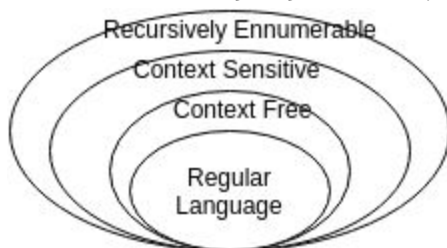
3. Which of the following statement is false?

- a) Context free language is the subset of context sensitive language
- b) Regular language is the subset of context sensitive language
- c) Recursively enumerable language is the super set of regular language
- d) Context sensitive language is a subset of context free language

#### SOLUTION

**Answer: d**

**Explanation:** Every regular language can be produced by context free grammar and context free language can be produced by context sensitive grammar and so on.



4. The Grammar can be defined as:  $G=(V, \Sigma, p, S)$

In the given definition, what does S represents?

- a) Accepting State
- b) Starting Variable
- c) Sensitive Grammar

d) None of these

**SOLUTION**

**Answer: b**

**Explanation:**  $G=(V, \Sigma, p, S)$ , here  $V$ =Finite set of variables,  $\Sigma$ = set of terminals,  $p$ = finite productions,  $S$ = Starting Variable.

5. Which among the following cannot be accepted by a regular grammar?

- a)  $L$  is a set of numbers divisible by 2
- b)  $L$  is a set of binary complement
- c)  $L$  is a set of string with odd number of 0
- d)  $L$  is a set of  $0^n1^n$

**SOLUTION**

**Answer: d**

**Explanation:** There exists no finite automata to accept the given language i.e.  $0^n1^n$ . For other options, it is possible to make a dfa or nfa representing the language set.

6. Which of the expression is appropriate?

For production  $p: a \rightarrow b$  where  $a \in V$  and  $b \in$  \_\_\_\_\_

- a)  $V$
- b)  $S$
- c)  $(V+\Sigma)^*$
- d)  $V+\Sigma$

**SOLUTION**

**Answer: c**

**Explanation:** According to the definition, the starting variable can produce another variable or any terminal or a variable which leads to terminal.

7. For  $S \rightarrow 0S1 \mid \epsilon$  for  $\Sigma=\{0,1\}^*$ , which of the following is wrong for the language produced?

- a) Non regular language
- b)  $0^n1^n \mid n \geq 0$
- c)  $0^n1^n \mid n \geq 1$
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:**  $L=\{\epsilon, 01, 0011, 000111, \dots, 0^n1^n\}$ . As epsilon is a part of the set, thus all the options are correct implying none of them to be wrong.

8. The minimum number of productions required to produce a language consisting of palindrome strings over  $\Sigma=\{a,b\}$  is

- a) 3
- b) 7
- c) 5
- d) 6

**SOLUTION**

**Answer: c**

**Explanation:** The grammar which produces a palindrome set can be written as:

$S \rightarrow aSa \mid bSb \mid e \mid a \mid b$

$L = \{e, a, b, aba, abbbbaabbba, \dots\}$

9. Which of the following statement is correct?

- a) All Regular grammar are context free but not vice versa
- b) All context free grammar are regular grammar but not vice versa
- c) Regular grammar and context free grammar are the same entity
- d) None of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** Regular grammar is a subset of context free grammar and thus all regular grammars are context free.

10. Are ambiguous grammar context free?

- a) Yes
- b) No

**SOLUTION**

**Answer:** a

**Explanation:** A context free grammar  $G$  is ambiguous if there is atleast one string in  $L(G)$  which has two or more distinct leftmost derivations.

## TOPIC 2: Parse Trees

1. The most suitable data structure used to represent the derivations in compiler:

- a) Queue
- b) Linked List
- c) Tree
- d) Hash Tables

**SOLUTION**

**Answer:** c

**Explanation:** The tree, known as "Parse tree" when used in a compiler, is the data structure of choice to represent the source program.

2. Which of the following statement is false in context of tree terminology?

- a) Root with no children is called a leaf
- b) A node can have three children
- c) Root has no parent
- d) Trees are collection of nodes, with a parent child relationship

**SOLUTION**

**Answer:** a

**Explanation:** A node has atmost one parent, drawn above the node, and zero or more children drawn below. Lines connect parents to children. There is one node, one root, that has no parent; this node appears to be at the top of the tree. Nodes with no children are called leaves. Nodes that are not leaves are called interior nodes.

3. In which order are the children of any node ordered?

- a) From the left
- b) From the right
- c) Arbitrarily
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** The children of a node are ordered from the left and drawn so. If N is to the left of node M, then all the descendents of N are considered to be to the left of all the descendents of M.

4. Which among the following is the root of the parse tree?

- a) Production P
- b) Terminal T
- c) Variable V
- d) Starting Variable S

**SOLUTION**

**Answer: d**

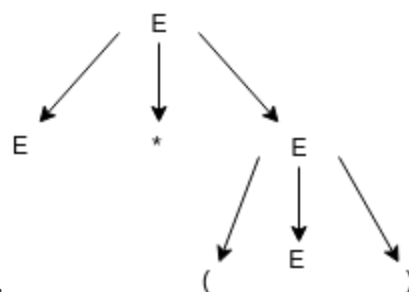
**Explanation:** The root is labelled by the start symbol. All the leaves are either labelled by a terminal or with e.

5. For the expression  $E^*(E)$  where \* and brackets are the operation, number of nodes in the respective parse tree are:

- a) 6
- b) 7
- c) 5
- d) 2

**SOLUTION**

**Answer: b**



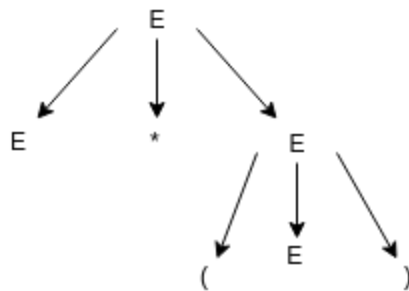
**Explanation:**

6. The number of leaves in a parse tree with expression  $E^*(E)$  where \* and () are operators

- a) 5
- b) 2
- c) 4
- d) 3

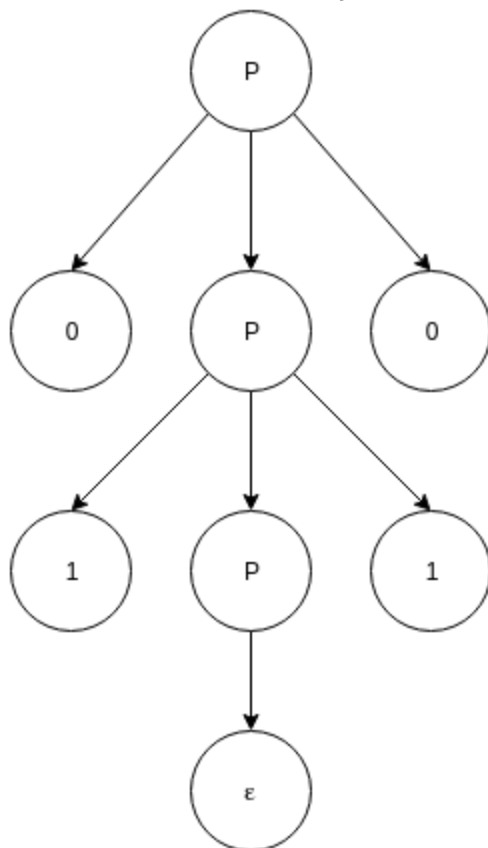
### SOLUTION

Answer: a



Explanation:

7. Which of the following does the given parse tree correspond to?



- a)  $P \rightarrow 1100$
- b)  $P \rightarrow 0110$
- c)  $P \rightarrow 1100 \epsilon$
- d)  $P \rightarrow 0101$

### SOLUTION

Answer: b

Explanation: The following is a parse tree for the production 0110 over  $\{0,1\}^*$ .

8. A grammar with more than one parse tree is called:

- a) Unambiguous
- b) Ambiguous

- c) Regular
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** A context free grammar  $G$  is ambiguous if there is at least one string in  $L(G)$  having two or more distinct derivation trees or equivalently, two or more distinct leftmost derivations.

9. \_\_\_\_\_ is the acyclic graphical representation of a grammar.

- a) Binary tree
- b) Oct tree
- c) Parse tree
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** In order to graphically represent a derivation of a grammar we need to use parse trees.

10. Grammar is checked by which component of compiler

- a) Scanner
- b) Parser
- c) Semantic Analyzer
- d) None of the mentioned

**SOLUTION**

**Answer:** Parser or syntax analyzer is the one responsible for checking the grammar and reporting errors. In this phase, parse tree is generated and syntax is analyzed.

**TOPIC 3: Ambiguity in Grammars and Languages**

1. Which of the following is not a notion of Context free grammars?

- a) Recursive Inference
- b) Derivations
- c) Sentential forms
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** The following are the notions to express Context free grammars:

- a) Recursive Inferences
- b) Derivations
- c) Sentential form
- d) Parse trees

2. State true or false:

Statement: The recursive inference procedure determines that string  $w$  is in the language of the variable  $A$ ,  $A$  being the starting variable.

- a) true
- b) false



### SOLUTION

**Answer: a**

**Explanation:** We apply the productions of CFG to infer that certain strings are in the language of a certain variable.

3. Which of the following is/are the suitable approaches for inferencing?

- a) Recursive Inference
- b) Derivations
- c) Both Recursive Inference and Derivations
- d) None of the mentioned

### SOLUTION

**Answer: c**

**Explanation:** Two inference approaches:

- 1. Recursive inference, using productions from body to head
  - 2. Derivations, using productions from head to body
4. If  $w$  belongs to  $L(G)$ , for some CFG, then  $w$  has a parse tree, which defines the syntactic structure of  $w$ .  $w$  could be:
- a) program
  - b) SQL-query
  - c) XML document
  - d) All of the mentioned

### SOLUTION

**Answer: d**

**Explanation:** Parse trees are an alternative representation to derivations and recursive inferences. There can be several parse trees for the same string.

5. Is the following statement correct?

Statement: Recursive inference and derivation are equivalent.

- a) Yes
- b) No

### SOLUTION

**Answer: a**

**Explanation:** Yes, they are equivalent. Both the terminologies represent the two approaches of recursive inferencing.

6.  $A \rightarrow aA \mid a \mid b$

The number of steps to form  $aab$ :

- a) 2
- b) 3
- c) 4
- d) 5

### SOLUTION

**Answer: b**

**Explanation:**  $A \rightarrow aA \Rightarrow aaA \Rightarrow aab$

7. An expression is mentioned as follows. Figure out number of incorrect notations or

symbols, such that a change in those could make the expression correct.

$$L(G) = \{w \text{ in } T^* \mid S \rightarrow^* w\}$$

- a) 0 Errors
- b) 1 Error
- c) 2 Error
- d) Invalid Expression

**SOLUTION**

**Answer: a**

**Explanation:** For the given expression,  $L(G) = \{w \text{ in } T^* \mid S \rightarrow^* w\}$ , If  $G(V, T, P, S)$  is a CFG, the language of  $G$ , denoted by  $L(G)$ , is the set of terminal strings that have derivations from the start symbol.

8. The language accepted by Push down Automaton:

- a) Recursive Language
- b) Context free language
- c) Linearly Bounded language
- d) All of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Push down automata accepts context free language.

9. Which among the following is the correct option for the given grammar?

$$G \rightarrow X111 \mid G1, X \rightarrow X0 \mid 00$$

- a)  $\{0a1b \mid a=2, b=3\}$
- b)  $\{0a1b \mid a=1, b=5\}$
- c)  $\{0a1b \mid a=b\}$
- d) More than one of the mentioned is correct

**SOLUTION**

**Answer: a**

**Explanation:** Using the recursive approach, we can conclude that option a is the correct answer, and its not possible for a grammar to have more than one language.

10. Which of the following the given language belongs to?

$$L = \{ambmcm \mid m \geq 1\}$$

- a) Context free language
- b) Regular language
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** The given language is neither accepted by a finite automata or a push down automata. Thus, it is neither a context free language nor a regular language.

11. Choose the correct option:

Statement: There exists two inference approaches:

- a) Recursive Inference

- b) Derivation
- a) true
- b) partially true
- c) false
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** We apply the productions of a CFG to infer that certain strings are in a language of certain variable.

12. Choose the correct option:

Statement 1: Recursive Inference, using productions from head to body.

Statement 2: Derivations, using productions from body to head.

- a) Statement 1 is true and Statement 2 is true
- b) Statement 1 and Statement 2, both are false
- c) Statement 1 is true and Statement 2 is false
- d) Statement 2 is true and Statement 1 is true

**SOLUTION**

**Answer: b**

**Explanation:** Both the statements are false. Recursive Inference, using productions from body to head. Derivations, using productions from head to body.

13. Which of the following statements are correct for a concept called inherent ambiguity in CFL?

- a) Every CFG for L is ambiguous
- b) Every CFG for L is unambiguous
- c) Every CFG is also regular
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A CFL L is said to be inherently ambiguous if every CFG for L is ambiguous.

14. Which of the theorem defines the existence of Parikh's theorem?

- a) Parikh's theorem
- b) Jacobi theorem
- c) AF+BG theorem
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Rohit Parikh in 1961 proved in his MIT research paper that some context free language can only have ambiguous grammars.

#### **TOPIC 4: Definition of the Pushdown Automata**

1. The production of the form  $A \rightarrow B$ , where A and B are non terminals is called

- a) Null production
- b) Unit production
- c) Greibach Normal Form
- d) Chomsky Normal Form

**SOLUTION**

**Answer: b**

**Explanation:**  $A \rightarrow \epsilon$  is termed as Null production while  $A \rightarrow B$  is termed as Unit production.

2. Halting states are of two types. They are:

- a) Accept and Reject
- b) Reject and Allow
- c) Start and Reject
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Halting states are the new tuple members introduced in turing machine and is of two types: Accept Halting State and Reject Halting State.

3. A push down automata can be represented as:

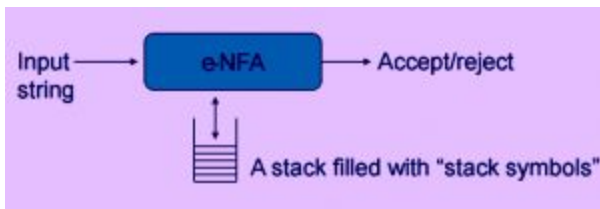
PDA =  $\epsilon$ -NFA + [stack] State true or false:

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:**



4. A pushdown automata can be defined as:  $(Q, \Sigma, G, q_0, z_0, A, \delta)$

What does the symbol  $z_0$  represents?

- a) an element of  $G$
- b) initial stack symbol
- c) top stack alphabet
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:**  $z_0$  is the initial stack symbol, is an element of  $G$ . Other symbols like  $\delta$  represents the transition function of the machine.

5. Which of the following correctly recognize the symbol ' $\delta$ ' in context to PDA?

- a) Moves
- b) transition function

- c) or/not symbol
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Using this notation, we can define moves and further acceptance of a string by the machine.

6. Which among the following is true for the given statement?

Statement :If there are strings R and T in a language L so that R is prefix of T and R is not equivalent to T.

- a) No DPDA can accept L by empty stack
- b) DPDA can accept L by an empty stack
- c) L is regular
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** If M is a DPDA accepting L by an empty stack, R and T are distinct strings in L, and R is a prefix of T, then the sequence of moves M must make in order to accept R leaves the stack empty, since  $R \in L$ . But then T cannot be accepted, since M can't move with an empty stack.

7. Which of the following can be accepted by a DPDA?

- a) The set of even length palindrome over {a,b}
- b) The set of odd length palindrome over {a,b}
- c)  $\{xxc \mid \text{where } c \text{ stands for the complement, } \{0,1\}\}$
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Theorem: The language pal of palindromes over the alphabet {0,1} cannot be accepted by any finite automaton, and it is therefore not regular.

8. For a counter automaton, with the symbols A and Z0, the string on the stack is always in the form of \_\_\_\_\_

- a) A
- b)  $AnZ0, n \geq 0$
- c)  $Z0An, n \geq 0$
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The possible change in the stack contents is a change in the number of A's on the stack.

9. State true or false:

Statement: Counter Automaton can exist for the language  $L = \{0^i 1^j \mid j \geq 0\}$

- a) true
- b) false

### SOLUTION

**Answer:** a

**Explanation:** The PDA works as follows. Instead of saving excess 0's or 1's on the stack, we save \*'s and use two different states to indicate which symbol there is currently a surplus of. The state  $q_0$  is the initial state and the only accepting state.

10. Let  $\Sigma = \{0,1\}^*$  and the grammar G be:

$S \rightarrow \epsilon$

$S \rightarrow SS$

$S \rightarrow 0S1 \mid 1S0$

State which of the following is true for the given

- a) Language of all and only Balanced strings
- b) It contains equal number of 0's and 1's
- c) Ambiguous Grammar
- d) All of the mentioned

### SOLUTION

**Answer:** d

**Explanation:** A string is said to be balanced if it consist of equal number of 0's and 1's.

### TOPIC 5: Languages of a Pushdown Automata

1. Context free grammar is called Type 2 grammar because of \_\_\_\_\_ hierarchy.

- a) Greibach
- b) Backus
- c) Chomsky
- d) None of the mentioned

### SOLUTION

**Answer:** c

**Explanation:** Chomsky hierarchy decide four type of language :Type 3- Regular Language, Type 2-Context free language, Type 1-Context Sensitive Language, Type 0- Unrestricted or Recursively Enumerable language.

2.  $a \rightarrow b$

Restriction: Length of b must be atleast as much length of a.

Which of the following is correct for the given assertion?

- a) Greibach Normal form
- b) Context Sensitive Language
- c) Chomsky Normal form
- d) Recursively Enumerable language

### SOLUTION

**Answer:** b

**Explanation:** A context-sensitive grammar (CSG) is a formal grammar in which the left-hand sides and right-hand sides of any production rules may be surrounded by a context of terminal and non terminal symbols. Context-sensitive grammars are more

general than context-free grammars, in the sense that there are some languages that cannot be described by context-free grammars, but can be described by CSG.

3. From the definition of context free grammars,

$G=(V, T, P, S)$

What is the solution of  $V \cap T$ ?

- a) Null
- b) Not Null
- c) Cannot be determined, depends on the language
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** V is the set of non terminal symbols while T is the st of terminal symbols, their intersection would always be null.

4. If P is the production, for the given statement, state true or false.

P:  $V \rightarrow (V \Sigma^*)^*$  represents that the left hand side production rule has no right or left context.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** Here the production P is from the definition of Context free grammar and thus, has no right or left context.

5. There exists a Context free grammar such that:

$X \rightarrow aX$

Which among the following is correct with respect to the given assertion?

- a) Left Recursive Grammar
- b) Right Recursive Grammar
- c) Non Recursive Grammar
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The grammar with right recursive production is known as Right recursive grammar. Right recursive production is of the form  $X \rightarrow aX$  where a is a terminal and X is a non terminal.

6. If the partial derivation tree contains the root as the starting variable, the form is known as:

- a) Chomsky hierarchy
- b) Sentential form
- c) Root form
- d) None of the mentioned

**SOLUTION**

**Answer: b**

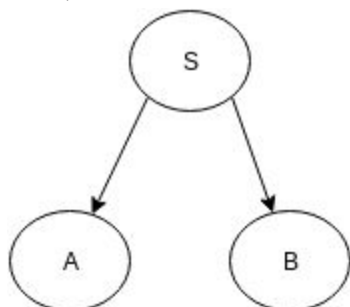
**Explanation:** Example: For any grammar, productions be:

$S \rightarrow AB$

$A \rightarrow aaA \mid ^\wedge$

$B \rightarrow Bb \mid ^\wedge$

The partial derivation tree can be drawn as:



Since it has the root as S, this can be said to be in sentential form.

7. Find a regular expression for a grammar which generates a language which states :  
L contains a set of strings starting with an a and ending with a b, with something in the middle.

a)  $a(a^*Ub^*)b$

b)  $a^*(aUb)b^*$

c)  $a(a^*b^*)b$

d) None of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** The grammar for the same language can be stated as :

(1)  $S \rightarrow aMb$

(2)  $M \rightarrow A$

(3)  $M \rightarrow B$

(4)  $A \rightarrow e$

(5)  $A \rightarrow aA$

(6)  $B \rightarrow e$

(7)  $B \rightarrow bB$

8. Which of the following is the correct representation of grammar for the given regular expression?

$a(aUb)^*b$

a) (1)  $S \rightarrow aMb$

(2)  $M \rightarrow e$

(3)  $M \rightarrow aM$

(4)  $M \rightarrow bM$

b) (1)  $S \rightarrow aMb$

(2)  $M \rightarrow Mab$

(3)  $M \rightarrow aM$

(4)  $M \rightarrow bM$



- c) (1)  $S \rightarrow aMb$   
(2)  $M \rightarrow e$   
(3)  $M \rightarrow aMb$   
(4)  $M \rightarrow bMa$   
d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:**

The basic idea of grammar formalisms is to capture the structure of string by

- a) using special symbols to stand for substrings of a particular structure
- b) using rules to specify how the substrings are combined to form new substrings.

9. A CFG consist of the following elements:

- a) a set of terminal symbols
- b) a set of non terminal symbols
- c) a set of productions
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** A CFG consists of:

- a) a set of terminals, which are characters of alphabets that appear in the string generated by the grammar.
- b) a set of non terminals, which are placeholders for patterns of terminal symbols that can be generated by the nonterminal symbols.
- c) a set of productions, which are set of rules to transit from one state to other forming up the string
- d) a start symbol, a special non terminal symbol that appears in the initial string generated in the grammar.

10. A CFG for a program describing strings of letters with the word “main” somewhere in the string:

- a)  $\rightarrow main$   
 $\rightarrow \epsilon$   
 $\rightarrow A | B | \dots | Z | a | b \dots | z$
- b)  $\rightarrow main$   
 $\rightarrow$   
 $\rightarrow A | B | \dots | Z | a | b \dots | z$
- c)  $\rightarrow main$   
 $\rightarrow \epsilon$   
 $\rightarrow A | B | \dots | Z | a | b \dots | z$
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** None.

### TOPIC 6: Equivalence of Pushdown Automata and CFG, Deterministic Pushdown Automata.

1. The transition a Push down automaton makes is additionally dependent upon the:

- a) stack
- b) input tape
- c) terminals
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A PDA is a finite machine which has an additional stack storage. Its transitions are based not only on input and the current state but also on the stack.

2. A PDA machine configuration  $(p, w, \gamma)$  can be correctly represented as:

- a) (current state, unprocessed input, stack content)
- b) (unprocessed input, stack content, current state)
- c) (current state, stack content, unprocessed input)
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A machine configuration is an element of  $K \times \Sigma^* \times \Gamma^*$ .

$(p, w, \gamma) = (\text{current state, unprocessed input, stack content}).$

3.  $|^*_-$  is the \_\_\_\_\_ closure of  $|_-$

- a) symmetric and reflexive
- b) transitive and reflexive
- c) symmetric and transitive
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** A string  $w$  is accepted by a PDA if and only if  $(s, w, e) \vdash^* (f, e, e)$

4. With reference of a DPDA, which among the following do we perform from the start state with an empty stack?

- a) process the whole string
- b) end in final state
- c) end with an empty stack
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** The empty stack in the end is our requirement relative to finite state automata.

5. A DPDA is a PDA in which:

- a) No state  $p$  has two outgoing transitions
- b) More than one state can have two or more outgoing transitions
- c) Atleast one state has more than one transitions

d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A Deterministic Push Down Automata is a Push Down Automata in which no state  $p$  has two or more transitions.

6. State true or false:

Statement: For every CFL,  $G$ , there exists a PDA  $M$  such that  $L(G) = L(M)$  and vice versa.

a) true

b) false

**SOLUTION**

**Answer: a**

**Explanation:** There exists two lemma's such that:

a) Given a grammar  $G$ , construct the PDA and show the equivalence

b) Given a PDA, construct a grammar and show the equivalence

7. If the PDA does not stop on an accepting state and the stack is not empty, the string is:

a) rejected

b) goes into loop forever

c) both (a) and (b)

d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** To accept a string, PDA needs to halt at an accepting state and with a stack empty, else it is called rejected. Given a PDA  $M$ , we can construct a PDA  $M'$  that accepts the same language as  $M$ , by both acceptance criteria.

8. A language accepted by Deterministic Push down automata is closed under which of the following?

a) Complement

b) Union

c) Both (a) and (b)

d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Deterministic Context free languages(one accepted by PDA by final state), are drastically different from the context free languages. For example they are closed under complementation and not union.

9. Which of the following is a simulator for non deterministic automata?

a) JFLAP

b) Gedit

c) FAUTO

d) None of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** JFLAP is a software for experimenting with formal topics including NFA, NPDA, multi-tape turing machines and L-systems.

10. Finite-state acceptors for the nested words can be:

- a) nested word automata
- b) push down automata
- c) ndfa
- d) none of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** The linear encodings of languages accepted by finite nested word automata gives the class of 'visibly pushdown automata'.

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## UNIT IV PROPERTIES OF CONTEXT FREE LANGUAGES

### TOPIC 1: Normal Forms for CFG

1. The format:  $A \rightarrow aB$  refers to which of the following?

- a) Chomsky Normal Form
- b) Greibach Normal Form
- c) Backus Naur Form
- d) None of the mentioned

**SOLUTION**

**Answer:** b

**Explanation:** A context free grammar is in Greibach Normal Form if the right hand sides of all the production rules start with a terminal, optionally followed by some variables.

2. Which of the following does not have left recursions?

- a) Chomsky Normal Form
- b) Greibach Normal Form
- c) Backus Naur Form
- d) All of the mentioned

**SOLUTION**

**Answer:** b

**Explanation:** The normal form is of the format:

$A \rightarrow aB$  where the right hand side production tends to begin with a terminal symbol, thus having no left recursions.

3. Every grammar in Chomsky Normal Form is:

- a) regular
- b) context sensitive
- c) context free
- d) all of the mentioned

### SOLUTION

**Answer: c**

**Explanation:** Conversely, every context free grammar can be converted into Chomsky Normal form and to other forms.

4. Which of the production rule can be accepted by Chomsky grammar?

- a)  $A \rightarrow BC$
- b)  $A \rightarrow a$
- c)  $S \rightarrow e$
- d) All of the mentioned

### SOLUTION

**Answer: d**

**Explanation:** in CNF, the production rules are of the form:

$A \rightarrow BC$

$A \rightarrow a$

$S \rightarrow e$

5. Given grammar G:

- (1)  $S \rightarrow AS$
- (2)  $S \rightarrow AAS$
- (3)  $A \rightarrow SA$
- (4)  $A \rightarrow aa$

Which of the following productions denies the format of Chomsky Normal Form?

- a) 2,4
- b) 1,3
- c) 1, 2, 3, 4
- d) 2, 3, 4

### SOLUTION

**Answer: a**

**Explanation:** The correct format:  $A \rightarrow BC$ ,  $A \rightarrow a$ ,  $X \rightarrow e$ .

6. Which of the following grammars are in Chomsky Normal Form:

- a)  $S \rightarrow AB|BC|CD$ ,  $A \rightarrow 0$ ,  $B \rightarrow 1$ ,  $C \rightarrow 2$ ,  $D \rightarrow 3$
- b)  $S \rightarrow AB$ ,  $S \rightarrow BCA|0|1|2|3$
- c)  $S \rightarrow ABa$ ,  $A \rightarrow aab$ ,  $B \rightarrow Ac$
- d) All of the mentioned

### SOLUTION

**Answer: a**

**Explanation:** We can eliminate the options on the basis of the format we are aware of:  $A \rightarrow BC$ ,  $B \rightarrow b$  and so on.

7. With reference to the process of conversion of a context free grammar to CNF, the number of variables to be introduced for the terminals are:

- $S \rightarrow ABa$
- $A \rightarrow aab$
- $B \rightarrow Ac$

- a) 3
- b) 4
- c) 2
- d) 5

**SOLUTION**

**Answer: a**

**Explanation:** According to the number of terminals present in the grammar, we need the corresponding that number of terminal variables while conversion.

8. In which of the following, does the CNF conversion find its use?

- a) CYK Algorithm
- b) Bottom up parsing
- c) Preprocessing step in some algorithms
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Besides the theoretical significance of CNF, its conversion scheme is helpful in algorithms as a preprocessing step, CYK algorithms and the bottom up parsing of context free grammars.

9. Let G be a grammar. When the production in G satisfy certain restrictions, then G is said to be in \_\_\_\_\_.

- a) restricted form
- b) parsed form
- c) normal form
- d) all of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** When the production in G satisfy certain restrictions, then G is said to be in 'normal form'.

10. Let G be a grammar:  $S \rightarrow AB|e$ ,  $A \rightarrow a$ ,  $B \rightarrow b$

Is the given grammar in CNF?

- a) Yes
- b) No

**SOLUTION**

**Answer: a**

**Explanation:**  $e$  is allowed in CNF only if the starting variable does not occur on the right hand side of the derivation.

**TOPIC 2: Pumping Lemma for CFL**

1. Which of the following is called Bar-Hillel lemma?

- a) Pumping lemma for regular language
- b) Pumping lemma for context free languages
- c) Pumping lemma for context sensitive languages
- d) None of the mentioned

### SOLUTION

**Answer: b**

**Explanation:** In automata theory, the pumping lemma for context free languages, also known as the Bar-Hillel lemma, represents a property of all context free languages.

2. Which of the expressions correctly is an requirement of the pumping lemma for the context free languages?

- a)  $uvnwxny$
- b)  $uvnwnxny$
- c)  $uv^2nwx^2ny$
- d) All of the mentioned

### SOLUTION

**Answer: b**

**Explanation:** Let  $L$  be a CFL. Then there is an integer  $n$  so that for any  $u$  that belong to language  $L$  satisfying  $|t| \geq n$ , there are strings  $u, v, w, x, y$  and  $z$  satisfying

$t = uvwxy$

$|vx| > 0$

$|vwx| \leq n$  For any  $m \geq 0, uvnwxny \in L$

3. Let  $L$  be a CFL. Then there is an integer  $n$  so that for any  $u$  that belong to language  $L$  satisfying

$|t| \geq n$ , there are strings  $u, v, w, x, y$  and  $z$  satisfying

$t = uvwxy$ .

Let  $p$  be the number of variables in CNF form of the context free grammar. The value of  $n$  in terms of  $p$  :

- a)  $2p$
- b)  $2p$
- c)  $2p+1$
- d)  $p^2$

### SOLUTION

**Answer: c**

**Explanation:** This inequation has been derived from derivation tree for  $t$  which must have height at least  $p+2$  (It has more than  $2p$  leaf nodes, and therefore its height is  $> p+1$ ).

4. Which of the following gives a positive result to the pumping lemma restrictions and requirements?

- a)  $\{aibici \mid i \geq 0\}$
- b)  $\{0i1i \mid i \geq 0\}$
- c)  $\{ss \mid s \in \{a,b\}^*\}$
- d) None of the mentioned

### SOLUTION

**Answer: b**

**Explanation:** A positive result to the pumping lemma shows that the language is a

CFL and its contradiction or negative result shows that the given language is not a Context Free language.

5. Using pumping lemma, which of the following cannot be proved as 'not a CFL'?

- a)  $\{aibici \mid i \geq 0\}$
- b)  $\{ss \mid s \in \{a,b\}^*\}$
- c) The set legal C programs
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** There are few rules in C that are context dependent. For example, declaration of a variable before it can be used.

6. State true or false:

Statement: We cannot use Ogden's lemma when pumping lemma fails.

- a) true
- b) false

**SOLUTION**

**Answer: b**

**Explanation:** Although the pumping lemma provides some information about  $v$  and  $x$  that are pumped, it says little about the location of these substrings in the string  $t$ . It can be used whenever the pumping lemma fails. Example:  $\{apbqcrds \mid p=0 \text{ or } q=r=s\}$ , etc.

7. Which of the following cannot be filled in the blank below?

Statement: There are CFLs  $L_1$  and  $L_2$  so that \_\_\_\_\_ is not a CFL.

- a)  $L_1 \cap L_2$
- b)  $L_1'$
- c)  $L_1^*$
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** A set of context free language is closed under the following operations:

- a) Union
- b) Concatenation
- c) Kleene

8. The pumping lemma is often used to prove that a language is:

- a) Context free
- b) Not context free
- c) Regular
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The pumping lemma is often used to prove that a given language  $L$  is non-context-free, by showing that arbitrarily long strings  $s$  are in  $L$  that cannot be



“pumped” without producing strings outside L.

9. What is the pumping length of string of length x?

- a)  $x+1$
- b)  $x$
- c)  $x-1$
- d)  $x^2$

**SOLUTION**

**Answer: a**

**Explanation:** There exists a property of all strings in the language that are of length  $p$ , where  $p$  is the constant-called the pumping length. For a finite language  $L$ ,  $p$  is equal to the maximum string length in  $L$  plus 1.

10. Which of the following does not obey pumping lemma for context free languages ?

- a) Finite languages
- b) Context free languages
- c) Unrestricted languages
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Finite languages (which are regular hence context free ) obey pumping lemma where as unrestricted languages like recursive languages do not obey pumping lemma for context free languages.

### TOPIC 3: Closure Properties of CFL

1. The context free languages are closed under:

- a) Intersection
- b) Complement
- c) Kleene
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Context free languages are closed under the following operation: union, kleene and concatenation. For regular languages, we can add intersection and complement to the list.

2. Given Grammar  $G_1$ :

$S \rightarrow aSb$

$S \rightarrow e$

Grammar  $G_2$ :

$R \rightarrow cRd$

$R \rightarrow e$

If  $L(G) = L(G_1) \cup L(G_2)$ , the number of productions the new starting variable would have:

- a) 2
- b) 3

c) 4

d) 1

**SOLUTION**

**Answer:** a

**Explanation:**

$T \rightarrow S \mid R$

$S \rightarrow aSb$

$S \rightarrow e$

$R \rightarrow cRd$

$R \rightarrow e$

3. Context free languages are not closed under:

a) Intersection

b) Intersection with Regular Language

c) Complement

d) All of the mentioned

**SOLUTION**

**Answer:** d

**Explanation:** It is a theorem which states that, Context free languages are not closed under operations like intersection and complement.

4. Which of the following is incorrect?

There exists algorithms to decide if:

a) String  $w$  is in CFL  $L$

b) CFL  $L$  is empty

c) CFL  $L$  is infinite

d) All of the mentioned

**SOLUTION**

**Answer:** d

**Explanation:** These properties are termed as decision properties of a CFL and include a set of problems like infiniteness problem, emptiness problem and membership problem.

5. If the start symbol is one of those symbols which produce no terminal through any sequence, the CFL is said to be

a) nullable

b) empty

c) eliminated

d) none of the mentioned

**SOLUTION**

**Answer:** b

**Explanation:** In the process of removing useless symbols, if the starting symbol is also a part, the CFL can be then termed as empty; otherwise not.

6. Using the pumping constant  $n$ , If there is a string in the language of length between \_\_\_\_ and \_\_\_\_ then the language is infinite else not.

- a)  $n, 2n-1$
- b)  $2n, n$
- c)  $n+1, 3n+6$
- d)  $0, n+1$

**SOLUTION**

**Answer: a**

**Explanation:** If there is a string in the language of length between  $n$  and  $2n-1$  then the language is infinite else not. The idea is essentially the same for regular languages.

7. Which of the following is/are CFL not closed under?

- a) Reverse
- b) Homomorphism
- c) Inverse Homomorphism
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** CFL is closed under union, concatenation and Kleene closure along with the properties reversal, homomorphism and inverse homomorphism but not difference and intersection.

8. If  $L_1$  and  $L_2$  are context free languages,  $L_1 - L_2$  are context free:

- a) always
- b) sometimes
- c) never
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Context free languages are not closed under difference, intersection and complement operations.

9. A \_\_\_\_\_ is context free grammar with at most one non terminal in the right handside of the production.

- a) linear grammar
- b) linear bounded grammar
- c) regular grammar
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A simple linear grammar is  $G$  with  $N = \{S\}$ ,  $\Sigma = \{a, b\}$ ,  $P$  with start symbol  $S$  and rules

$S \rightarrow aSb$

$S \rightarrow \epsilon$

10. There is a linear grammar that generates a context free grammar

- a) always
- b) never

- c) sometimes
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Linear grammar is a subset of context free grammar which has atmost one non terminal symbol in the right hand side of the production. Thus, there exists some languages which are generated by Linear grammars.

**TOPIC 4: Turing Machines**

1. A turing machine is a
- a) real machine
  - b) abstract machine
  - c) hypothetical machine
  - d) more than one option is correct

**SOLUTION**

**Answer: d**

**Explanation:** A turing machine is abstract or hypothetical machine thought by mathematician Alan Turing in 1936 capable of simulating any algorithm, however complicated it is.

2. A turing machine operates over:
- a) finite memory tape
  - b) infinite memory tape
  - c) depends on the algorithm
  - d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The turing machine operates on an infinite memory tape divided into cells. The machine positions its head over the cell and reads the symbol.

3. Which of the functions are not performed by the turing machine after reading a symbol?
- a) writes the symbol
  - b) moves the tape one cell left/right
  - c) proceeds with next instruction or halts
  - d) none of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** After the read head reads the symbol from the input tape, it performs the following functions:

- a) writes a symbol (some model allow symbol erasure/no writing)
- b) moves the tape left or right (some models allows no motion)
- c) proceeds with subsequent instruction or goes either into accepting halting state or rejecting halting state.

4. 'a' in a-machine is :

- a) Alan
- b) arbitrary
- c) automatic
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** The turing machine was invented by Alan turing in 1936. He named it as a-machine(automatic machine).

5. Which of the problems were not answered when the turing machine was invented?

- a) Does a machine exists that can determine whether any arbitrary machine on its tape is circular.
- b) Does a machine exists that can determine whether any arbitrary machine on its tape is ever prints a symbol
- c) Hilbert Entscheidungs problem
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Invention of turing machine answered a lot of questions which included problems like decision problem, etc.) . Alan was able to prove the properties of computation using such model.

6. The ability for a system of instructions to simulate a Turing Machine is called

- 
- a) Turing Completeness
  - b) Simulation
  - c) Turing Halting
  - d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Turing Completeness the ability for a system of instructions to simulate a Turing machine. A programming language that is Turing complete is theoretically capable of expressing all tasks accomplishable by computers; nearly all programming languages are Turing complete.

7. Turing machine can be represented using the following tools:

- a) Transition graph
- b) Transition table
- c) Queue and Input tape
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** We can represent a turing machine, graphically, tabularly and diagrammatically.

8. Which of the following is false for an abstract machine?

- a) Turing machine
- b) theoretical model of computer
- c) assumes a discrete time paradigm
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** An abstract machine also known as abstract computer, is a theoretical model of computer or hardware system in automata theory. Abstraction in computing process usually assumes a discrete time paradigm.

9. Fill in the blank with the most appropriate option.

Statement: In theory of computation, abstract machines are often used in \_\_\_\_\_ regarding computability or to analyze the complexity of an algorithm.

- a) thought experiments
- b) principle
- c) hypothesis
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** A thought experiment considers some hypothesis, theory or principle for the purpose of thinking through its consequences.

10. State true or false:

Statement: RAM model allows random access to indexed memory locations.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** In computer science, Random access machine is an abstract machine in the general class of register machines. Random access machine should not be confused with Random access memory.

## **TOPIC 5: Programming Techniques for TM.**

This set of Automata Theory Multiple Choice Questions & Answers (MCQs) focuses on "Programming Techniques-Storage and Subroutines".

1. A Turing machine has \_\_\_\_\_ number of states in a CPU.

- a) finite
- b) infinite
- c) May be finite
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A Turing machine has finite number of states in its CPU. However the

states are not small in number. Real computer consist of registers which can store values (fixed number of bits).

2. Suppose we have a simple computer with control unit holding a PC with a 32 bit address + Arithmetic unit holding one double length 64 bit Arithmetic Register. The number of states the finite machine will hold:

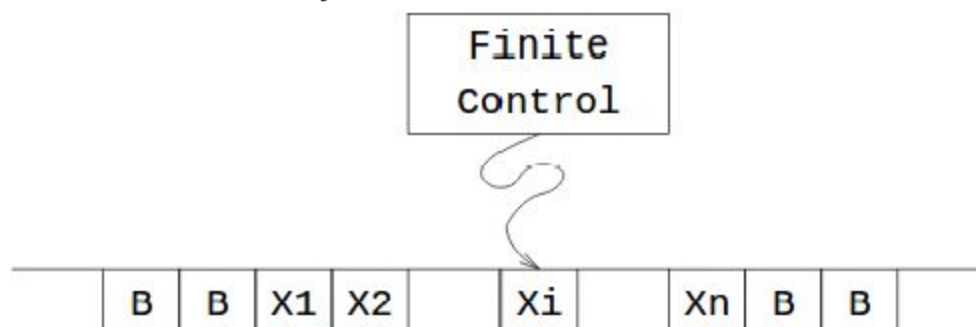
- a)  $2(32*64)$
- b) 296
- c) 96
- d) 32

**SOLUTION**

**Answer: b**

**Explanation:** According to the statistics of the question, we will have a finite machine with  $2^{96}$  states.

3. In one move a turing machine will:



- a) Change a state
- b) Write a tape symbol in the cell scanned
- c) Move the tape head left or right
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** A move of a turing machine is the function of the state of finite control and the tape symbol just scanned.

4. State true or false:

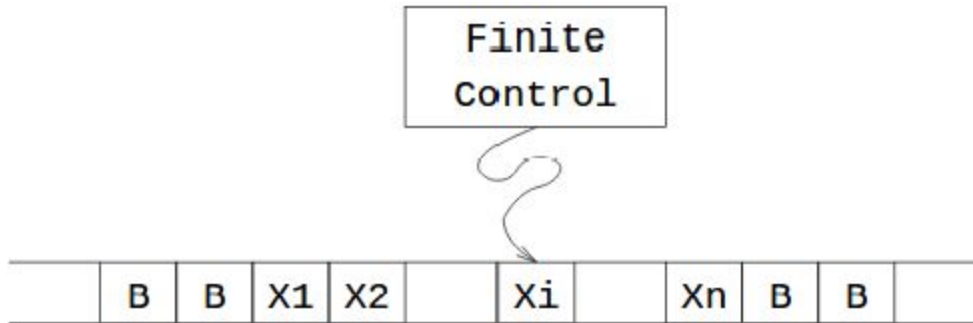
Statement: We can use the finite control of turing machine to hold a finite amount of data.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:**



The finite control not only contains state  $q$  but also three data, A, B, C. The following technique requires no extension to the Turing Machine model. Shaping states this way allows to describe transitions in more systematic way and often to simplify the strategy of the program.

5. Statement 1: Multitrack Turing machine.

Statement 2: Gamma is Cartesian product of a finite number of finite sets.

Which among the following is the correct option?

- a) Statement 1 is the assertion and Statement 2 is the reason
- b) Statement 1 is the reason and Statement 2 is the assertion
- c) Statement 1 and Statement 2 are independent from each other
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Cartesian product works like a struct in C/C++. For Example: Computer tape storage is something like 8 or 9 bits in each cell. One can recognize a multi track tape machine by looking at the transitions because each will have tuples as the read and write symbols.

6. A multi track turing machine can described as a 6-tuple  $(Q, X, S, d, q_0, F)$  where X represents:

- a) input alphabet
- b) tape alphabet
- c) shift symbols
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The 6-tuple  $(Q, X, S, d, q_0, F)$  can be explained as:

Q represents finite set of states,

X represents the tape alphabet,

S represents the input alphabet

d represents the relation on states and the symbols

$q_0$  represents the initial state

F represents the set of final states.

7. Which of the following statements are false?

- a) A multi track turing machine is a special kind of multi tape turing machine



- b) 4-heads move independently along 4-tracks in standard 4-tape turing machine
- c) In a n-track turing machine, n head reads and writes on all the tracks simultaneously.
- d) All of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** In a n-track turing machine, one head reads and writes on all the tracks simultaneously.

8. State true or false:

Statement: Two track turing machine is equivalent to a standard turing machine.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** This can be generalized for n- tracks and can be proved equivalent using enumerable languages.

9. Which of the following is/are not true for recursively enumerable language?

- a) partially decidable
- b) Turing acceptable
- c) Turing Recognizable
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** In automata theory, a formal language is called recursively enumerable language or partially decidable or semi decidable or turing acceptable or turing recognizable if there exists a turing machine which will enumerate all valid strings of the language.

10. According to Chomsky hierarchy, which of the following is adopted by Recursively Enumerable language?

- a) Type 0
- b) Type 1
- c) Type 2
- d) Type 3

**SOLUTION**

**Answer: a**

**Explanation:** Recursively Enumerable languages are type 0 languages in the Chomsky hierarchy. All regular, context free, context sensitive languages are recursively enumerable language.

## UNIT V UNDECIDABILITY

### TOPIC 1: Non Recursive Enumerable (RE) Language

1. Which of the following technique is used to find whether a natural language is recursive enumerable?

- a) Diagonalization
- b) Recursive Induction
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** To find a non recursively enumerable language, we use the technique of diagonalization.

2. Diagonalization can be useful in:

- a) To find a non recursively enumerable language
- b) To prove undecidability of halting problem
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Diagonalization is a technique we use for the following operations:

- a) To find a non recursively enumerable language.
  - b) To prove undecidability of halting problem.
3. Which of the following are undecidable problems?
- a) Determining whether two grammars generate the same language
  - b) Determining whether a grammar is ambiguous
  - c) Both (a) and (b)
  - d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** In contrast we can put up an algorithm for checking whether two FA's are equivalent and this program can be implemented as a program.

4. Which of the following are incorrect options?

- a) Informally, problem is a yes/no question about an infinite set of possible instances
- b) Formally, a problem is a language
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Example: Does a graph G has a Hamilton cycle?

=>Each undirected graph is an instance of Hamilton cycle problem.

5. If a problem has an algorithm to answer it, we call it \_\_\_\_\_

- a) decidable
- b) solved
- c) recognizable
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** An algorithm is a TM that halts on all inputs, accepted or not. Putting other way, decidable problems are recursive languages.

6. Which of the following are decidable problems?

- a) Can a particular line of code in a program ever be executed?
- b) Do two given CFG's generate the same language
- c) Is a given CFG ambiguous?
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** All of the mentioned problems are undecidable.

7. Which one of the following is true for the given?

$A = \{(M, w) \mid M \text{ is a Turing machine that accepts string } w\}$

- a) A concrete undecidable problem
- b) A is recognizable but not decidable
- c)  $\neg A$  is not recognizable
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** We can prove A to be undecidable using the contradiction method.

8. Which of the following are correct statements?

- a) TMs that always halt are known as Decidable problems
- b) TMs that are guaranteed to halt only on acceptance are recursive enumerable.
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** There are two types of TMs on the basis of halting: Recursive and Recursively Enumerable (TM may or may not halt, could loop forever).

9. Statement: If L is R.E.,  $L_c$  needs to be R.E. Is it correct?

- a) Yes
- b) No
- c) Maybe
- d) Cannot predict

**SOLUTION**

**Answer: b**

**Explanation:** Any recursive enumerable language is not closed under

complementation.

10. Which of the following is true for The Halting problem?

- a) It is recursively enumerable
- b) It is undecidable
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Halting problem: Does a given Turing machine  $M$  halt on a given input  $w$ ?

11. With reference to binary strings, state true or false:

Statement: For any turing machine, the input alphabet is restricted to  $\{0,1\}$ .

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** When turing machines are coded as Binary strings, we are restricted to take any input alphabet except  $\{0,1\}$ .

12. With reference to enumeration of binary strings, the conversion of binary strings to integer is possible by treating the resulting string as a base \_\_\_\_ integer.

- a) 2
- b) 8
- c) 16
- d) All of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** It makes sense to talk about the  $i$ -th binary string” and about “the  $i$ -th Turing machine. If  $i$  makes no sense as a TM, assume the  $i$ -th TM accepts nothing.

## TOPIC 2: Undecidable Problem with RE

1. The decision problem is the function from string to \_\_\_\_\_

- a) char
- b) int
- c) boolean
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** The decision problem requires checking of input (string) has some property or not. That is a string to boolean transaction.

2. A language  $L$  is said to be \_\_\_\_\_ if there is a turing machine  $M$  such that  $L(M)=L$  and  $M$  halts at every point.

- a) Turing acceptable

- b) decidable
- c) undecidable
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Decidability refers to the decision problem and existence of an effective method for determining membership, and return true and false accordingly rather than going into a loop forever.

3. Which among the following are undecidable theories?

- a) The first order theory of boolean algebra
- b) The first order theory of Euclidean geometry
- c) The first order theory of hyperbolic geometry
- d) The first order theory of the natural number with addition, multiplication, and equality

**SOLUTION**

**Answer: d**

**Explanation:** Tarski and Mostowski in 1949, established that the first order theory of natural numbers with addition, multiplication, and equality is an undecidable theory. Others mentioned are decidable theories.

4.  $\text{Rec-DFA} = \{ \mid M \text{ is a DFA and } M \text{ recognizes input } w \}$ .

Fill in the blank:

Rec-DFA is \_\_\_\_\_

- a) Undecidable
- b) Decidable
- c) Non finite
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Under decidability of regular language properties we have the following lemma which states that a DFA which recognizes an input  $w$  is decidable.

5. Which among the following are semi decidable?

- a) Empty-DFA
- b) Rec-NFA
- c) Infinite-DFA
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** All are the properties of regular languages and all are decidable languages.

6. The language accepted by a Turing machine is called \_\_\_\_\_

- a) Recursive Enumerable
- b) Recursive

- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** The language accepted by Turing machines are called recursively enumerable (RE), and the subset of RE languages that are accepted by a Turing machine that always halts are called recursive.

7. Decidable can be taken as a synonym to:

- a) recursive
- b) non recursive
- c) recognizable
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** We can refer to languages as 'recursive' and problems as 'decidable'. If a language is not recursive, then we call the problem expressed by that language undecidable.

8. The problems which have no algorithm, regardless of whether or not they are accepted by a Turing machine that fails to halt on some input are referred as:

- a) Decidable
- b) Undecidable
- c) Computable
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** The problems that can be solved by a Turing machine can be divided into two classes:

- a) Those that have an algorithm
- b) Intractable problems: Those that are only solved by a Turing machine that may run forever on inputs they do not accept.

9. An algorithm is called efficient if it runs in \_\_\_\_\_ time on a serial computer.

- a) polynomial
- b) non polynomial
- c) logarithmic
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** Example: Runtimes of efficient algorithms

$O(n)$ ,  $O(n \log n)$ ,  $O(n^3 \log^2 n)$

Runtimes of inefficient algorithms

$O(2^n)$ ,  $O(n!)$

10. A problem is called \_\_\_\_\_ if it has an efficient algorithm for itself.

- a) tractable
- b) intractable
- c) computational
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A problem is called intractable iff there is an efficient (i.e. polynomial time) algorithm that solves it. A problem is called intractable iff there exists no efficient algorithm that solves it.

11. A formal language is recursive if :

- a) a total turing machine exists
- b) a turing machine that halts for every input
- c) turing machine rejects if the input does not belong to the language
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** A formal language is called recursive if it is a recursive subset of the set of all possible finite sequences over the alphabet of the language.

12. Recursive languages are also known as:

- a) decidable
- b) undecidable
- c) sometimes decidable
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A language is recursive if there exists a turing machine such that it halts i.e. accepts if the input belongs to the language else rejects. It is better called Turing decidable language.

13. The class of recursive language is known as:

- a) R
- b) RC
- c) RL
- d) All of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** R is the set of all recursive languages, a class of decision problems solvable by turing machines. Although, R is also used for the class RP.

14. Which of the following was not a part of Chomsky hierarchy ?

- a) Context sensitive grammar
- b) Unrestricted grammar
- c) Recursive grammar
- d) None of the mentioned

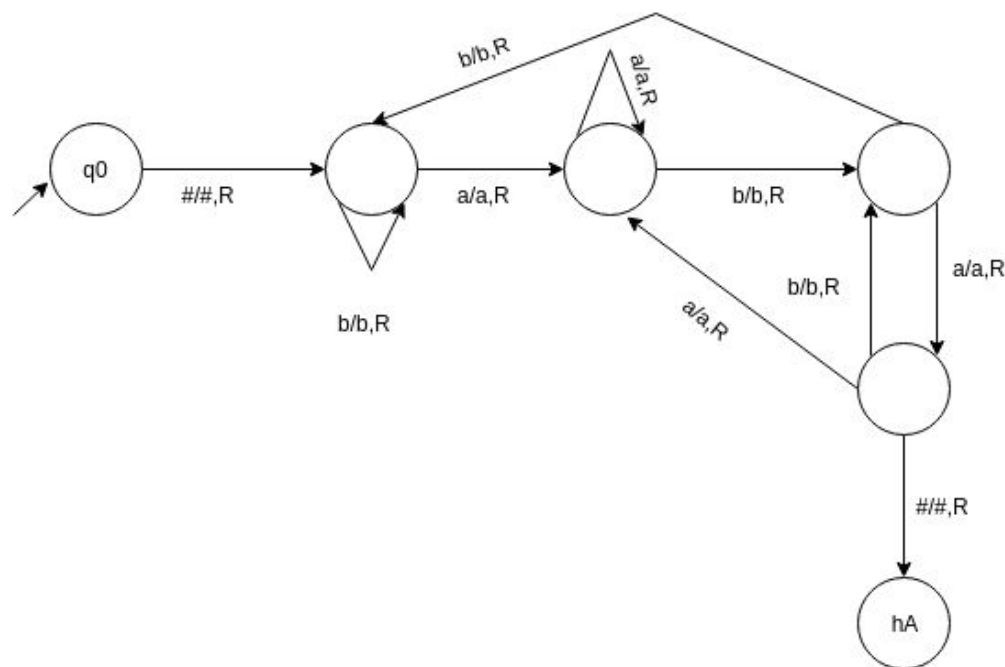
## SOLUTION

**Answer: c**

**Explanation:** All recursive languages are recursively enumerable. All regular, context free and context sensitive languages are recursive.

## TOPIC 3: Undecidable Problems about T M

1. Which of the following regular expression resembles the given diagram?



- a)  $\{a\}^*\{b\}^*\{a,b\}$
- b)  $\{a,b\}^*\{aba\}$
- c)  $\{a,b\}^*\{bab\}$
- d)  $\{a,b\}^*\{a\}^*\{b\}^*$

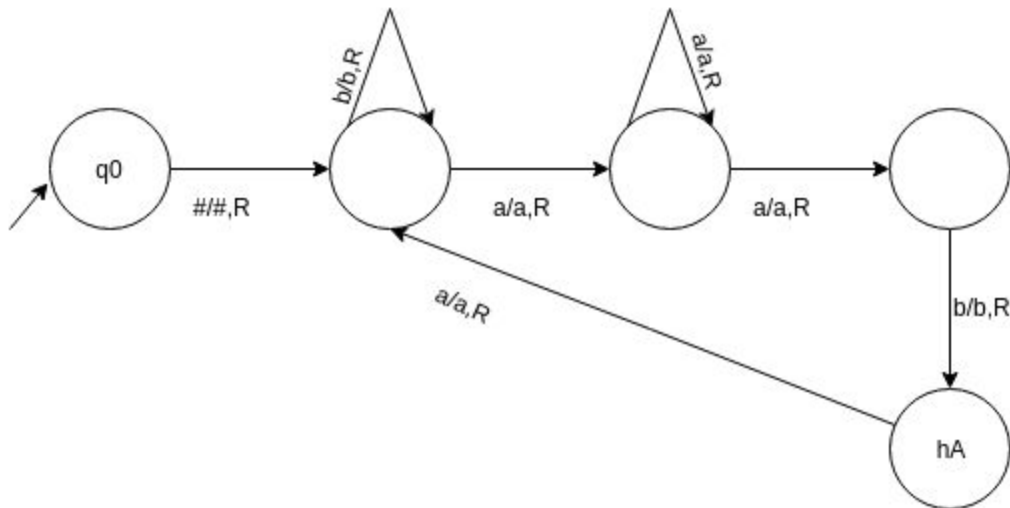
## SOLUTION

**Answer: b**

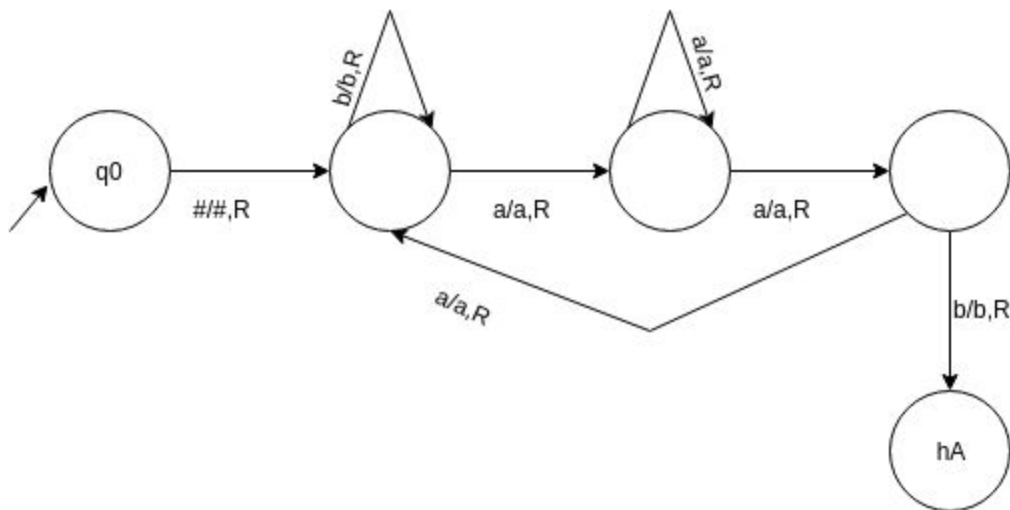
**Explanation:** The given diagram is a transition graph for a turing machine which accepts the language with the regular expression  $\{a,b\}^*\{aba\}$ .

2. Construct a turing machine which accepts a string with 'aba' as its substring.

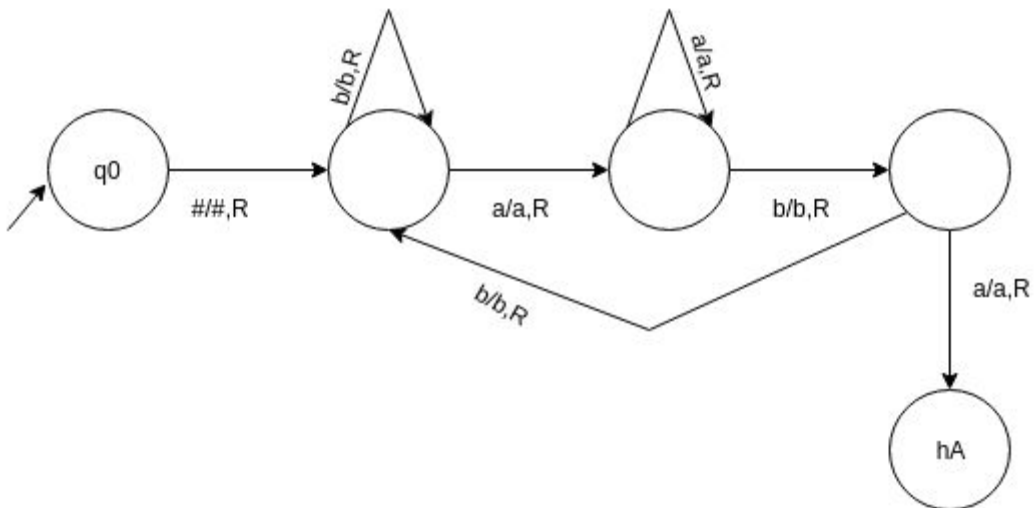




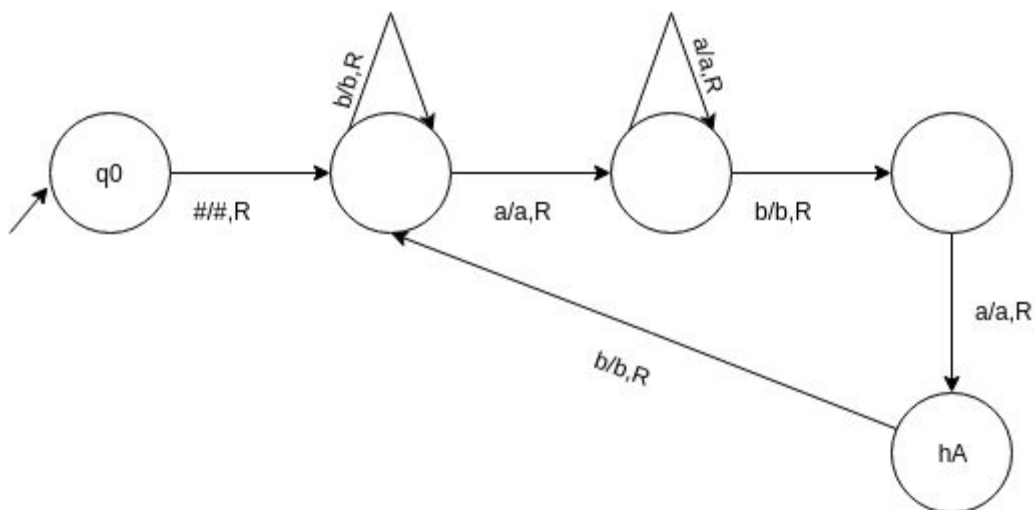
a)



b)



c)

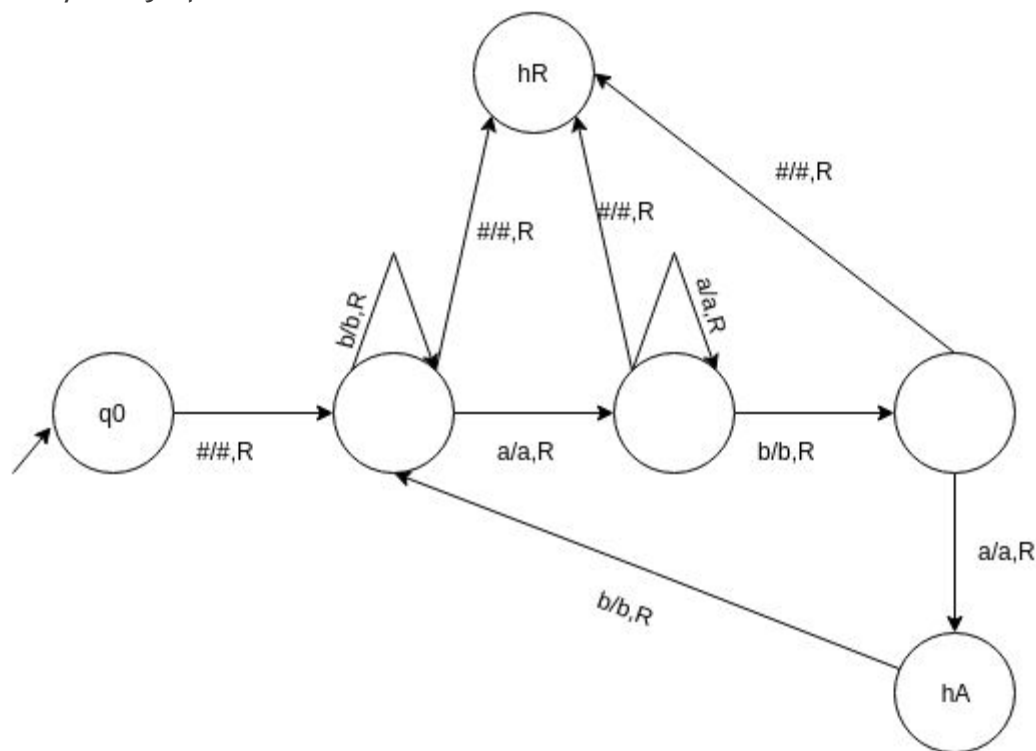


d)

#### SOLUTION

**Answer: c**

**Explanation:** The language consist of strings with a substring 'aba' as fixed at its end and the left part can be anything including epsilon. Thus the turing machine uses five states to express the language excluding the rejection halting state which if allowed can modify the graph as:



3. The number of states required to automate the last question i.e.  $\{a,b\}^*\{aba\}\{a,b\}^*$  using finite automata:

- a) 4
- b) 3

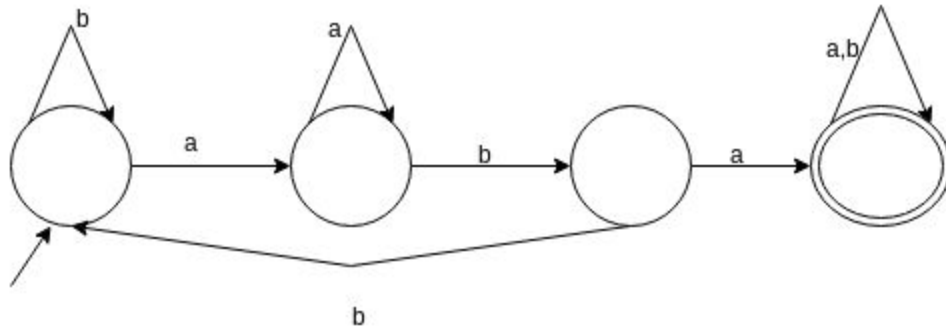
c) 5

d) 6

**SOLUTION**

**Answer: a**

**Explanation:** The finite automata can be represented as:



4. The machine accept the string by entering into hA or it can:

a) explicitly reject x by entering into hR

b) enter into an infinte loop

c) Both (a) and (b)

d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Three things can occur when a string is tested over a turing machine:

a) enter into accept halting state

b) enter into reject halting state

c) goes into loop forever

5.  $d(q,X)=(r,Y,D)$  where D cannot be:



a) L

b) R

c) S

d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** D represents the direction in which automata moves forward as per the queue which surely cannot be a starting variable.

6. Which of the following can accept even palindrome over  $\{a,b\}$

a) Push down Automata

b) Turing machine

c) NDFA

d) All of the mentioned

### SOLUTION

**Answer: c**

**Explanation:** A language generating strings which are palindrome is not regular, thus cannot be represented using a finite automaton.

7. Which of the functions can a Turing machine not perform?

- a) Copying a string
- b) Deleting a symbol
- c) Accepting a pal
- d) Inserting a symbol

### SOLUTION

**Answer: d**

**Explanation:** Different Turing machines exist for operations like copying a string, deleting a symbol, inserting a symbol and accepting palindromes.

8. If  $T_1$  and  $T_2$  are two Turing machines. The composite can be represented using the expression:

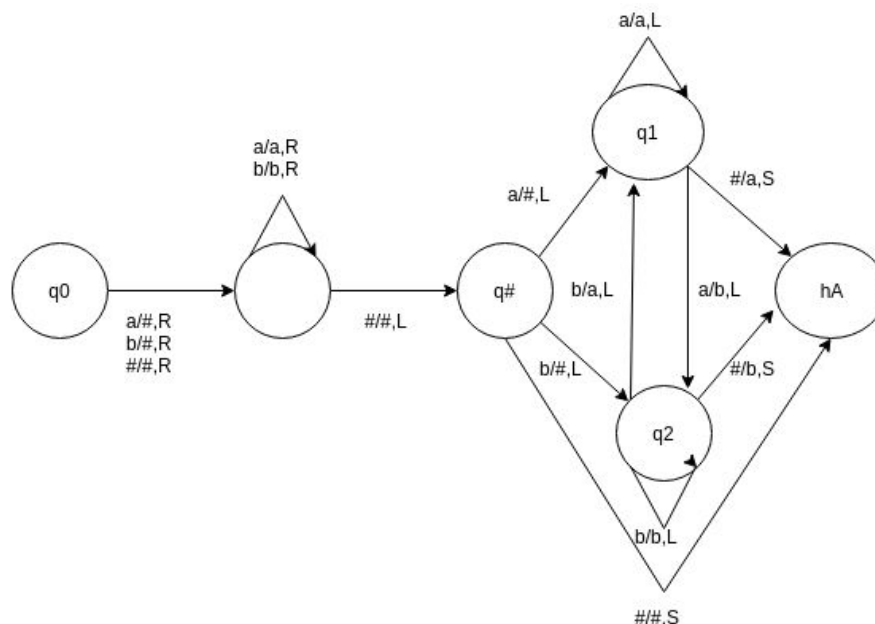
- a)  $T_1 T_2$
- b)  $T_1 \cup T_2$
- c)  $T_1 \times T_2$
- d) None of the mentioned

### SOLUTION

**Answer: a**

**Explanation:** If  $T_1$  and  $T_2$  are TMs, with disjoint sets of non halting states and transition function  $d_1$  and  $d_2$ , respectively, we write  $T_1 T_2$  to denote this composite TM.

9. The following Turing machine acts like:



- a) Copies a string

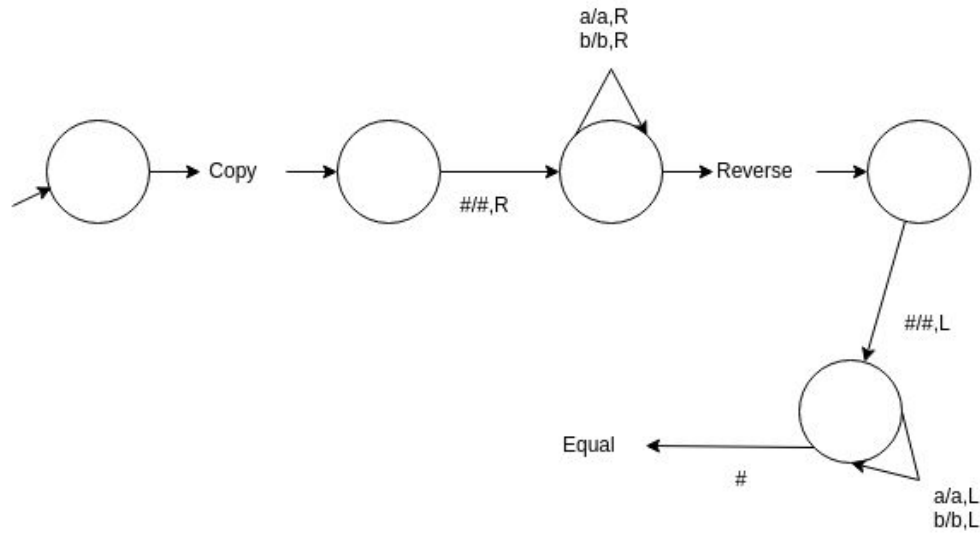
- b) Delete a symbol
- c) Insert a symbol
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** A turing machine does the deletion by changing the tape contents from yaz to yz, where y belongs to  $(S \cup \{\#\})^*$ .

10. What does the following transition graph shows:



- a) Copies a symbol
- b) Reverses a string
- c) Accepts a pal
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** The composite TM accepts the language of palindromes over  $\{a, b\}$  by comparing the input string to its reverse and accepting if and only if the two are equal.

**TOPIC 4: Post's Correspondence Problem**

1. According to the rice's theorem, If P is a non trivial property, Lp is :

- a) infinite
- b) decidable
- c) undecidable
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** Rice's theorem states that 'Any non trivial property about the language recognized by a turing machine is undecidable'.

2. Fill in the blank with reference to Rice's theorem.

For any non-trivial property of \_\_\_\_\_ no general or effective method can decide

whether an algorithm computes it with that property.

- a) partial functions
- b) piecewise functions
- c) both (a) and (b)
- d) none of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A property of partial functions is called trivial if it holds for all partial computable functions or for none, and an effective decision method is called general if it decides correctly for every algorithm.

3. Which of the following is incorrect according to rice theorem?

Let  $S$  be a set of language that is non trivial:

- a) there exists a TM that recognizes the language in  $S$
- b) there exists a TM that recognizes the language not in  $S$
- c) both (a) and (b)
- d) none of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** According to rice theorem, it is undecidable to determine whether the language recognized by an arbitrary turing machine lies in  $S$ .

4. Which of the following set of computable functions are decidable?

- a) The class of computable functions that are constant, and its complement
- b) The class of indices for computable functions that are total
- c) The class of indices for recursively enumerable sets that are cofinite
- d) All of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** According to Rice's theorem, if there exists atleast one computable function in a particular class  $C$  of computable functions and another computable function not in  $C$  then the problem deciding whether a particular program computes a function in  $C$  is undecidable.

5. Which of the following statements are undecidable?

For a given Turing Machine  $M$ ,

- a) does  $M$  halt on an empty input tape
- b) does  $M$  halt for any inputs at all?
- c) is  $L(M)$  regular? Context free? Turing decidable?
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** All of the following mentioned are immediate results of Rice's theorem and thus, undecidable.

6. Post Correspondence problem is

- a) decidable decision problem
- b) undecidable decision problem
- c) not a decision problem
- d) none of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Post Correspondence problem is an undecidable decision problem that was introduced by Emil Post in 1946. Being simpler than halting problem, it can be used in proofs of undecidability.

7. State true or false:

Statement: The difference between PCP and MPCP is that in MPCP, a solution is required to start with the first string on each list.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** The MPCP is : Given lists A and B of K strings ,say  $A = w_1, w_2, \dots, w_k$  and  $B = x_1, x_2, \dots, x_k$  does there exists a sequence of integers  $i_1, i_2, \dots, i_r$  such that  $w_{i_1}w_{i_2}\dots w_{i_r} = x_{i_1}x_{i_2}\dots x_{i_r}$ ?

8. PCP stands for?

- a) Post Correspondence Problem
- b) Post Corresponding Problem
- c) Pre Correspondence problem
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** PCP or Post Correspondence problem is an undecidable decision problem.

9. Can a Modified PCP problem be reduced to PCP?

- a) yes
- b) no

**SOLUTION**

**Answer: a**

**Explanation:** Yes, it can be. There exists a theorem and as well as its proof which supports the assertion.

10. Consider three decision problem A, B, C. A is decidable and B is not. Which of the following is a correct option?

- a) C is undecidable if C is reducible to B
- b) C is undecidable if B is reducible to C
- c) C is decidable if A is reducible to C
- d) C is decidable if C is reducible to B's complement.

**SOLUTION**

**Answer:** b

**Explanation:** As B is undecidable and it can be reduced to C, C is also an undecidable problem.

### TOPIC 5.1: The Class P Problem

1. If the number of steps required to solve a problem is  $O(nk)$ , then the problem is said to be solved in:

- a) non-polynomial time
- b) polynomial time
- c) infinite time
- d) none of the mentioned

**SOLUTION**

**Answer:** b

**Explanation:** Most of the operations like addition, subtraction, etc as well as computing functions including powers, square roots and logarithms can be performed in polynomial time. In the given question,  $n$  is the complexity of the input and  $k$  is some non negative integer.

2. The value of constants like  $p$  and  $e$  can be calculated in:

- a) polynomial time
- b) non-polynomial time
- c) cannot be calculated
- d) none of the mentioned

**SOLUTION**

**Answer:** a

**Explanation:** The value of such constants can be calculated using algorithms which have time complexity in terms of  $O(nk)$  i.e polynomial time.

3. Which of the following cannot be solved using polynomial time?

- a) Linear Programming
- b) Greatest common divisor
- c) Maximum matching
- d) None of the mentioned

**SOLUTION**

**Answer:** d

**Explanation:** In graph theory, a matching or independent edge set in a graph  $G$  is a set of edges without common vertices. Given a graph  $(V, E)$ , a matching  $M$  in  $G$  is a set of pairwise non adjacent edges i.e. no two edges share a common vertex.

4. The complexity class P consist of all the decision problems that can be solved by \_\_\_\_\_ using polynomial amount of computation time.

- a) Push Down automata
- b) DFA
- c) NDFA
- d) Deterministic Turing machine

**SOLUTION**



**Answer: d**

**Explanation:** All the decision problems that can be solved using a Deterministic turing machine using polynomial time to compute, all belong to the complexity class P.

5. A generalization of P class can be:

- a) PTIME
- b) DTIME
- c) NP
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** P is a specific case of NP class, which is the class of decidable problems decidable by a non deterministic turing machine that runs in polynomial time.

6. Which of the following options are correct with reference to P-complete problems?

- a) used for the problems which are difficult to solve in limited space
- b) every problem in P can be reduced to it using proper reductions
- c) complete problem for complexity class P
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:**

The notion of P-complete decision problems is useful in the analysis of:

- a) which problems are tough to parallelize effectively
- b) which problems are difficult to solve in limited space

7. A problem X belongs to P complexity class if there exist \_\_\_\_\_ algorithm to solve that problem, such that the number of steps of the algorithms bounded by a polynomial in n, where n is the length of the input.

- a) 1
- b) 2
- c) 3
- d) all of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** A problem X belongs to P complexity class if there exist atleast 1 algorithm to solve that problem, such that the number of steps of the algorithms bounded by a polynomial in n, where n is the length of the input. Thus, all the options are correct.

8. Which of the following is a P-complete type of problem?

- a) Circuit Value problem
- b) Linear programming
- c) Context free grammar membership
- d) All of the mentioned

### SOLUTION

**Answer: d**

**Explanation:** Given a context free grammar and a string, can the string be generated by the grammar? Such problems fall in the category of P-complete.

9. State true or false?

Statement: Given a turing machine, an input for the machine, and a number  $T(\text{unary})$ , does that machine halt on that input within the first  $T$ -steps?

The given problem is P-complete.

- a) true
- b) false

### SOLUTION

**Answer: a**

**Explanation:** If we can parallelize a general simulation of a sequential computer, then we will be able to parallelize any program that runs on that computer. If this problem is in NC, then so every other problem in P.

10. In the above problem, if the input is binary, the class the problem belongs?

- a) EXPSPACE
- b) DLOGTIME
- c) EXPTIME-complete
- d) All of the mentioned

### SOLUTION

**Answer: c**

**Explanation:** It is the set of all decision problems that have exponential run time i.e. solvable by deterministic turing machine in  $O(2^{p(n)})$  time, where  $p(n)$  is a polynomial function of  $n$ .

## TOPIC 5.2: The Class NP Problem

1. What does NP stands for in complexity classes theory?

- a) Non polynomial
- b) Non-deterministic polynomial
- c) Both (a) and (b)
- d) None of the mentioned

### SOLUTION

**Answer: b**

**Explanation:** NP is said to be one of the most fundamental complexity classes. NP is an acronym for Non deterministic polynomial time.

2. The hardest of NP problems can be:

- a) NP-complete
- b) NP-hard
- c) P
- d) None of the mentioned

### SOLUTION

**Answer: a**

**Explanation:** NP class contains many important problems, the hardest of which is NP-complete, whose solution is sufficient to deal with any other NP problem in polynomial time.

3. Which of the following contains NP?

- a) PSPACE
- b) EXPSPACE
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** It is sufficient to construct a PSPACE machine that loops over all proof strings and feeds each one to a polynomial time verifier. It is also contained in EXPTIME, since the same algorithm operates in exponential time.

4. Travelling sales man problem belongs to which of the class?

- a) P
- b) NP
- c) Linear
- d) None of the mentioned

**SOLUTION**

**Answer: b**

**Explanation:** Travelling Salesman Problem: Given an input matrix of distances between n cities, this problem is to determine if there is a route visiting all cities with total distance less than k.

5. State true or false?

Statement: If a problem X is in NP and a polynomial time algorithm for X could also be used to solve problem Y in polynomial time, then Y is also in NP.

- a) true
- b) false

**SOLUTION**

**Answer: a**

**Explanation:** This is just a commutative property of NP complexity class where a problem is said to be in NP if it can be solved using an algorithm which was used to solve another NP problem in polynomial amount of time.

6. A problem which is both \_\_\_\_\_ and \_\_\_\_\_ is said to be NP complete.

- a) NP, P
- b) NP, NP hard
- c) P, P complete
- d) None of the mentioned

**SOLUTION**

**Answer: a**

**Explanation:** A problem is said to be NP Hard if an algorithm for solving the problem

can be translated from for solving any other problem. It is easier to show a problem NP than showing it NP Hard.

7. Which of the following is incorrect for the given phrase

Phrase : 'solvable by non deterministic algorithms in polynomial time'

- a) NP Problems
- b) During control flow, non deterministic algorithm may have more than one choice
- c) If the choices that non deterministic algorithm makes are correct, the amount of time it takes is bounded by polynomial time.
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** Primality testing is a simple example. To decide whether a number is prime or not, one simply selects non deterministically a number checks whether factors exist for the number or not.

8. In terms of NTIME, NP problems are the set of decision problems which can be solved using a non deterministic machine in \_\_\_\_\_ time.

- a)  $O(n)$
- b)  $O(n^{1/2})$
- c)  $O(n^k)$ ,  $k \in \mathbb{N}$
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** The complexity class NP can be defined in terms of NTIME as:  
 $NP = O(n^k)$  for  $k \in \mathbb{N}$ .

9. Which of the following can be used to define NP complexity class?

- a) Verifier
- b) Polynomial time
- c) Both (a) and (b)
- d) None of the mentioned

**SOLUTION**

**Answer: c**

**Explanation:** NP can be defined using deterministic turing machines as verifiers.

10. Which of the following are not in NP?

- a) All problems in P
- b) Boolean Satisfiability problems
- c) Integer factorization problem
- d) None of the mentioned

**SOLUTION**

**Answer: d**

**Explanation:** This is a list of some problems which are in NP:

- a) All problems in P
- b) Decision version of Integer factorization method

- c) Graph Isomorphism Problem
- d) All NP complete problems, etc.

11. Which of the following does not belong to the closure properties of NP class?

- a) Union
- b) Concatenation
- c) Reversal
- d) Complement

**SOLUTION**

**Answer:** d

**Explanation:** It is unknown about the closure property-complement for the complexity class NP. The question is so called NP versus co-NP problem.

~OoO~