

## ASSIGNMENT-1

**AIM:** Write a program in C++ to implement RSA algorithm for key generation & cipher verification.

**OBJECTIVES:**

- Concept of public key & private key
- Public key algorithm
- Working of RSA algorithm

### THEORY:

- Public key algorithm is used to solve the problem of key distribution in symmetric algorithm.
- It is achieved by using one key for encryption & a different but related key for decryption.
- RSA like algorithms use either of the two related keys for encryption, while the other is used for decryption.
- Public key encryption scheme has:
  - i. **Plaintext:**  
A readable message that is fed into algorithm, as input.
  - ii. **Encryption algorithm:**  
It performs various transformations on plain-text.
  - iii. **Public & private key:**  
This is a pair of keys that have been selected for encryption & decryption process.
  - iv. **Ciphertext:**  
It is the scrambled message produced as o/p.

v. Decryption Algorithm:

decrypt ciphertext & matching key & produce the original plaintext.

RSA ALGORITHM:

It is an algorithm for public key cryptography involves 3-step key generation, encryption & decryption.

It is a block cipher with each block having binary value less than some no. 'n'. Encryption & decryption are of the following form, for some plaintext block m & ciphertext block c,

$$C = m^e \pmod n$$

$$m = C^d \pmod n$$

$$= (m^e)^d \pmod n$$

$$= m^{ed} \pmod n$$

Thus public key generated,  $PV = \{e, n\}$   
 & private key generated,  $PR = \{d, n\}$

Both sender & receiver must know the value n & sender knows the value of e & receiver knows the value of d

i. Key Generation:

a. Choose 2 distinct prime nos. p & q

b. Compute  $n = p \cdot q$

c. Compute  $\phi(n) = (p-1)(q-1)$

d. Choose an integer  $e$  such that  $1 < e < \phi(n)$   
 $\gcd(e, \phi(n)) = 1$ , i.e.,  $e$  &  $\phi(n)$  are co-prime

e. Determine  $d = (e-1) \bmod \phi(n)$   
public key =  $\{e, n\}$   
private key =  $\{d, n\}$

ii. Encryption:

a.  $C = M^e \bmod n$

iii. Decryption:

$M = C^d \bmod n$

- Example:

$p = 17$  &  $q = 11$

$n = p \cdot q = 17 \times 11 = 187$

$\phi(n) = (p-1)(q-1) = 16 \times 10 = 160$

$e$  should be co-prime to  $\phi(n)$ , i.e.,  $e = 7$

$d$  should be modular inverse of  $e$ ,  $\therefore d = 23$

$\therefore PV = \{7, 187\}$

$PR = \{23, 187\}$

CONCLUSION:

Thus, in this assignment, we learnt & understood the RSA algorithm for key generation & cipher verification & successfully implemented it.