

ASSIGNMENT-7

TITLE: 0/1 KNAPSACK

PROBLEM STATEMENT: Write a program to solve 0/1 knapsack problem using DP.

THEORY:

• KNAPSACK PROBLEM:

- Knapsack is a problem in computational optimization:

Given a set of items, each with mass & a value, determine the no. of each item to include in a collection so that total weight is less than or equal to a given limit & the total value is as large as possible.

- It derives its name from the problem faced by someone who is constrained by a fixed-size knapsack & must fill it with most valuable items

• ALGORITHM:

- Let i be the highest numbered item in an optimal solution S for w .
- $S - \{i\}$ is an optimal solⁿ for $w - w_i$ & the value to solution S is $V_i + \text{value}(\text{sub-problem})$
- We can express the fact in the following formula define $c[i, w]$ to be solution for items $1, 2, \dots$ & the max weight w

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algorithm takes the following i/p:

i. Max weight w

ii. No. of items n

iii. Two sequences

$v = \langle v_1, v_2, \dots, v_n \rangle$

$w = \langle w_1, w_2, \dots, w_n \rangle$

ALGORITHM:

for $w = 0$ to w do

$c[0, w] = 0$

for $i = 1$ to n do

$c[i, 0] = 0$

for $w = 1$ to w do

if $w_i \leq w$ then

if $v_i + c[i-1, w-w_i]$ then

$c[i, w] = v_i + c[i-1, w-w_i]$

else

$c[i, w] = c[i-1, w]$

else

$c[i, w] = c[i-1, w]$

Q.1. $w = \{1, 2, 3\}$

$v = \{10, 15, 40\}$

max wt = 6

for 0 weight \Rightarrow all values = 0

$DP[1][1] = \max \{ DP[0][1], v_1 + DP[0][1-1] \}$

$= \max \{ 0, 10 + 0 \}$

$= 10$

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	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0
1	0	10	10	10	10	10	10
2	0						
3	0						

$$\therefore DP[1][0 \dots 6] = 10$$

Now,

$$DP[2][2] = \max \{ 10, 15 + 0 \} = 15$$

$$\text{also } DP[2][3] = \max \{ DP[2][2], 15 + DP[1][1] \}$$

$$= \max \{ 10, 15 + 10 \} = 25$$

	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0
1	0	10	10	10	10	10	10
2	0	10	15	25	25	25	25
3	0	10	15	40	50	55	65

Hence, max. possible value = 65

$$Q.2: W = \{ 1, 2, 5, 6, 7 \}$$

$$V = \{ 1, 6, 13, 22, 28 \}$$

$$DP[2][2] = \max \{ DP[1][2], 5 + DP[1][2] \}$$

$$= \max \{ 1, 6 + 0 \} = 6$$

$$DP[2][3] = 7$$

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	0	1	2	3	4	5	6	7	8	9	10	11
0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	1	6	7	7	7	7	7	7	7	7	7
5	0	1	6	7	7	18	19	24	25	25	25	25
6	0	1	6	7	7	18	19	24	25	28	29	29
7	0	1	6	7	7	18	22	28	29	34	35	35
7	0	1	6	7	7							

Hence max. possible value = 40

CONCLUSION:

Hence, I have learnt about 0/1 knapsack & implemented the same.