QUESTIONS

1. Solve the following L.P.P. graphically:

Minimize
$$z = 20x_1 + 10x_2$$

 $subject\ to$ $x_1 + 2x_2 \le 40$,
 $3x_1 + x_2 \ge 30$,
 $4x_1 + 3x_2 \ge 60$,
 $x_1, x_2 \ge 0$.

2. Solve the following L.P.P. graphically:

$$\begin{array}{ll} \textit{Maximize} & z = 6x_1 + 4x_2 \\ \textit{subject to} & 7x_1 + 5x_2 \leq 35, \\ & 5x_1 + 7x_2 \leq 35, \\ & 4x_1 + 3x_2 \geq 12, \\ & 3x_1 + x_2 \geq 3, \\ & x_1, x_2 \geq 0. \end{array}$$

3. Solve the following L.P.P. graphically:

Maximize
$$z = 3x_1 + 4x_2$$

subject to $x_1 - x_2 \ge 0$,
 $-x_1 + 3x_2 \le 3$,
 $x_1, x_2 \ge 0$.

4. Solve the following L.P.P. graphically:

Maximize
$$z = 6x_1 + 10x_2$$

subject to $3x_1 + 5x_2 \le 10$,
 $5x_1 + 3x_2 \le 15$,
 $x_1, x_2 \ge 0$.

5. Find the basic feasible solutions of the following system of equations.

$$2x_1 + 3x_2 - x_3 + 4x_4 = 8;$$

$$x_1 - 2x_2 + 6x_3 - 7x_4 = -3;$$

$$x_1, x_2, x_3, x_4 \ge 0.$$

6. Find all the basic solutions of the following equations and identify the basic vectors and the basic variables in each case.

$$x_1 + x_2 + x_3 = 4;$$

$$2x_1 + 5x_2 - 2x_3 = 3.$$

7. Solve the following L.P.P. using $simplex\ method.$

Maximize
$$z = 4x_1 + 7x_2$$

subject to $2x_1 + x_2 \le 1000$,
 $10x_1 + 10x_2 \le 6000$,
 $2x_1 + 4x_2 \le 2000$,
 $x_1, x_2 \ge 0$.

8. Solve the following L.P.P. using simplex method.

$$\begin{array}{ll} \textit{Maximize} & z = 3x_1 + x_2 + 3x_3 \\ \textit{subject to} & 2x_1 + x_2 + x_3 \leq 2, \\ & x_1 + 2x_2 + 3x_3 \leq 5, \\ & 2x_1 + 2x_2 + x_3 \leq 6, \\ & x_1, x_2, x_3 \geq 0. \end{array}$$

9. Solve the following L.P.P. using penalty method.

Maximize
$$z = 2x_1 + 3x_2 + x_3$$

subject to $-3x_1 + 2x_2 + 3x_3 = 8$,
 $-3x_1 + 4x_2 + 2x_3 = 7$,
 $x_1, x_2, x_3 \ge 0$.

10. Solve the following L.P.P. using penalty method.

Maximize
$$z = -2x_1 + x_2 + 3x_3$$

subject to $x_1 - 2x_2 + 3x_3 = 2$,
 $3x_1 + 2x_2 + 4x_3 = 1$,
 $x_1, x_2, x_3 \ge 0$.