

QUESTIONS

1. Solve the following L.P.P. graphically :

$$\begin{array}{ll}\text{Minimize} & z = 20x_1 + 10x_2 \\ \text{subject to} & x_1 + 2x_2 \leq 40, \\ & 3x_1 + x_2 \geq 30, \\ & 4x_1 + 3x_2 \geq 60, \\ & x_1, x_2 \geq 0.\end{array}$$

2. Solve the following L.P.P. graphically :

$$\begin{array}{ll}\text{Maximize} & z = 6x_1 + 4x_2 \\ \text{subject to} & 7x_1 + 5x_2 \leq 35, \\ & 5x_1 + 7x_2 \leq 35, \\ & 4x_1 + 3x_2 \geq 12, \\ & 3x_1 + x_2 \geq 3, \\ & x_1, x_2 \geq 0.\end{array}$$

3. Solve the following L.P.P. graphically :

$$\begin{array}{ll}\text{Maximize} & z = 3x_1 + 4x_2 \\ \text{subject to} & x_1 - x_2 \geq 0, \\ & -x_1 + 3x_2 \leq 3, \\ & x_1, x_2 \geq 0.\end{array}$$

4. Solve the following L.P.P. graphically :

$$\begin{array}{ll}\text{Maximize} & z = 6x_1 + 10x_2 \\ \text{subject to} & 3x_1 + 5x_2 \leq 10, \\ & 5x_1 + 3x_2 \leq 15, \\ & x_1, x_2 \geq 0.\end{array}$$

5. Find the basic feasible solutions of the following system of equations.

$$\begin{array}{l}2x_1 + 3x_2 - x_3 + 4x_4 = 8; \\ x_1 - 2x_2 + 6x_3 - 7x_4 = -3; \\ x_1, x_2, x_3, x_4 \geq 0.\end{array}$$

6. Find all the basic solutions of the following equations and identify the basic vectors and the basic variables in each case.

$$\begin{array}{l}x_1 + x_2 + x_3 = 4; \\ 2x_1 + 5x_2 - 2x_3 = 3.\end{array}$$

7. Solve the following *L.P.P.* using *simplex method*.

$$\begin{array}{ll}\text{Maximize} & z = 4x_1 + 7x_2 \\ \text{subject to} & 2x_1 + x_2 \leq 1000, \\ & 10x_1 + 10x_2 \leq 6000, \\ & 2x_1 + 4x_2 \leq 2000, \\ & x_1, x_2 \geq 0.\end{array}$$

8. Solve the following *L.P.P.* using *simplex method*.

$$\begin{array}{ll}\text{Maximize} & z = 3x_1 + x_2 + 3x_3 \\ \text{subject to} & 2x_1 + x_2 + x_3 \leq 2, \\ & x_1 + 2x_2 + 3x_3 \leq 5, \\ & 2x_1 + 2x_2 + x_3 \leq 6, \\ & x_1, x_2, x_3 \geq 0.\end{array}$$

9. Solve the following *L.P.P.* using *penalty method*.

$$\begin{array}{ll}\text{Maximize} & z = 2x_1 + 3x_2 + x_3 \\ \text{subject to} & -3x_1 + 2x_2 + 3x_3 = 8, \\ & -3x_1 + 4x_2 + 2x_3 = 7, \\ & x_1, x_2, x_3 \geq 0.\end{array}$$

10. Solve the following *L.P.P.* using *penalty method*.

$$\begin{array}{ll}\text{Maximize} & z = -2x_1 + x_2 + 3x_3 \\ \text{subject to} & x_1 - 2x_2 + 3x_3 = 2, \\ & 3x_1 + 2x_2 + 4x_3 = 1, \\ & x_1, x_2, x_3 \geq 0.\end{array}$$

11. Use duality to find the optimal solution, if any, of the following *L.P.P.*

$$\begin{array}{ll}\text{Maximize} & z = 3x_1 + 2x_2 \\ \text{subject to} & 2x_1 + x_2 \leq 2, \\ & x_1 + x_2 \leq 1, \\ & x_1, x_2 \geq 0.\end{array}$$

12. Use duality to find the optimal solution, if any, of the following *L.P.P.*

$$\begin{array}{ll}\text{Maximize} & z = 15x_1 + 10x_2 \\ \text{subject to} & 3x_1 + 5x_2 \geq 5, \\ & 5x_1 + 2x_2 \geq 3, \\ & x_1, x_2 \geq 0.\end{array}$$

13. At a cattle breeding firm it is prescribed that the food ration for one animal must contain at least 14, 22 and 1 units of nutrients A , B , and C respectively. Two different kinds of fodder are available. Each unit weight of these two contains the following amounts of the three nutrients :

	Fodder 1	Fodder 2
Nutrient A	2	1
Nutrient B	2	3
Nutrient C	1	1

It is given that the costs of unit quantity of fodder 1 and 2 are 3 and 2 monetary units respectively. Pose a linear programming problem in terms of minimizing the cost of purchasing the fodders for the above cattle breeding firm.

14. Three products are processed through three different operations. The times (in minutes) required per unit of each product, the daily capacity of the operations (in minutes per day) and the profit per unit sold for each product (in rupees) are as follows :

Operation	Time per unit			Operation Capacity
	Product 1	Product 2	Product 3	
1	3	4	3	42
2	5	0	3	45
3	3	6	2	41
Profit	3	2	1	

The zero time indicates that the product does not require the given operation. The problem is to determine the optimum daily production for three products that maximizes the profit.

Formulate the above production planning problem as a linear programming problem assuming that all units produced are sold.