Statistical Computing and Numerical Analysis Using C Programming (STS-A-CC-3-7-P) Problem Set 4

Y. Write a program in C to find the value of the function y = f(x) for a given x and n pairs of values (x_i, y_i) , i = 1, 2, ..., n, using Lagrange's interpolation formula. Run the above program to find the value of (i) f(1.25), (ii) f(1.36) on the basis of the following data set.

120_lagrange_interpolation_formula.c

$$x$$
: 1.0 1.1 1.3 1.5 1.6 $y = f(x)$: 0.3639 0.3258 0.2612 0.2095 0.1876 (i) The value of f(1.250000) is 0.276024 (ii) The value of f(1.360000) is 0.244469

2. Write a program in C to compute the value of the following integral by Trapezoidal rule using 12 sub-intervals.

$$\int_{0.2}^{1.4} (\sin(x) - \ln(x) + e^x) dx$$

3. Write a program in C to compute the value of the following integral by Simpson's one third rule correct upto 8 significant figures.

$$\int_0^1 \frac{\log_e(1+x^2)}{(1+x^2)} dx.$$

- 4. Write a program in C to calculate the real root correct upto 5 places of decimal of the equation $10^x + x 4 = 0$ by the Newton-Raphson method. Take the initial value as 0.5.
- 5. Write a program in C to calculate the real root correct upto 6 places of decimal of the following equation by the method of iteration. Take the initial value as 3.5.

$$2x\text{-}\log_{10}x\text{-}7=0$$