## Why the allpho or alldrg has a small variance?

It depends on how we do the cross validation, i.e.

- we give them labels as 1 to 10 at the beginning of each repetation, or
- within each repetation, we mark the labels 10 times.

For example,

subj	changescore	treatment assignment	CV group
i	$Y_i$	$t_i$	$l_i \in \{1, 2,, 10\}$

If we label all subject as pbo group or drg group, all the change scores  $Y_i$ s will be included.

For the jth repetation, we conduct a 10 fold cross validation and label the subjects in group 1 to 10. We calculate the mean of  $Y_i$  whose label is from k = 1, 2, ... 10 respectively. Then we get the mean values  $\bar{Y}_k$ .

$$\bar{Y}_k = \frac{1}{n_k} \sum_{l \in k} Y_i$$

where  $n_k$  is the number of subjects whose label is k. The mean value across the 10 CV is

$$\bar{Y}_j = \frac{1}{10} \sum_{k=1}^{10} \bar{Y}_k = \frac{1}{10} \sum_{k=1}^{10} \frac{1}{n_k} \sum_{l \in k} Y_l \approx \bar{Y}_l$$

. Therefore, the overall mean value is just the mean value of the dataset's change score. The variance is

$$Var(\bar{Y}_j) = Var(\bar{Y}) = \frac{var(Y)}{n}$$
, if  $n_k$ s have the same value

We run the whole steps for N times, the mean value of the change score is just

$$\bar{Y}_N = \frac{1}{N} \sum_{j=1}^N \bar{Y}_j$$

$$Var(\bar{Y}_N) = \frac{var(Y)}{nN}$$

However, if we resample the labels at each times of the cross validation, the mean value will not change, but the variance can be larger.

```
set.seed(1)
n = 100
meanY = c()
for(iters in 1:100){
    y = rnorm(n,0,1)
    label = sample(1:10, n, replace = TRUE) # cross validation groups
    meany_cv = c()
    for(i in 1:10){
        meany_cv = c(meany_cv, mean(y[label == i]))
    }
    meanY = c(meanY, mean(meany_cv))
}
mean(meanY)
```

## [1] -0.006439615

```
sd(meanY)
## [1] 0.0906425
set.seed(2)
n = 100
meanY = c()
for(iters in 1:100){
 y = rnorm(n,0,1)
 meany_cv = c()
 for(i in 1:10){
   label = sample(1:10, n, replace = TRUE) # cross validation groups
   meany_cv = c(meany_cv, mean(y[label == i]))
 meanY = c(meanY, mean(meany_cv))
}
mean(meanY)
## [1] 0.02032141
sd(meanY)
## [1] 0.1285985
```