

Engineering Mathematics and Computing

Task 1: Coursework Assessment

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Git Repo : <https://github.com/sakx7/mathcompuni>

Part A

Mathematics

A.1 Q1

Use the quotient rule to differentiate the function $y = \frac{\ln 3x}{2x}$

The quotient rule states that if

$$y = \frac{u}{v} \quad \text{then} \quad y' = \frac{u'v - uv'}{v^2}$$

Here:

$$u = \ln 3x$$

$$v = 2x$$

First, find the derivatives:

$$u = \ln(3x)$$

Let:

$$\delta = 3x \quad u = \ln(\delta)$$

$$\frac{du}{d\delta} = \frac{1}{\delta} \quad \frac{d\delta}{dx} = 3$$

Using the chain rule, we can find:

$$\frac{du}{dx} = \frac{du}{d\delta} \cdot \frac{d\delta}{dx}$$

$$\frac{du}{dx} = \frac{3}{\delta} = \frac{3}{3x} = \frac{1}{x}$$

General rule for composite/nested functions is solved via chain rule it's:

$$\frac{d}{dx}(f(g(x))) = f'(g(x)) \cdot g'(x)$$

$$v = 2x$$

$$v' = \frac{d}{dx}(2x) = 2$$

Now we can apply the quotient rule:

$$y' = \frac{\left(\frac{1}{x}\right)(2x) - (\ln 3x)(2)}{(2x)^2} = \frac{2 - 2 \ln 3x}{4x^2}$$

$$y' = \frac{1 - \ln 3x}{2x^2}$$

A.2 Q2

Find the angle between the vectors $2i - 11j - 10k$ and $5i + 8j + 7k$

The angle θ between two vectors \mathbf{a} and \mathbf{b} is given by:

$$\cos \theta = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|}$$

Calculate the dot product:

$$\mathbf{a} \cdot \mathbf{b} = \underbrace{(2)(5)}_i + \underbrace{(-11)(8)}_j + \underbrace{(-10)(7)}_k = -148$$

Calculate the magnitudes:

$$\|\mathbf{a}\| = \sqrt{2^2 + (-11)^2 + (-10)^2} = \sqrt{225} = 15$$

$$\|\mathbf{b}\| = \sqrt{5^2 + 8^2 + 7^2} = \sqrt{138}$$

Find $\cos \theta$:

$$\cos \theta = \frac{-148}{15 \times \sqrt{138}}$$

Thus, the angle θ is:

$$\theta = \cos^{-1} \left(\frac{-148}{15 \times \sqrt{138}} \right) \approx 147.1^\circ$$

A.3 Q3

Find the rate of change of $y = \ln(16t^2 + 19)$ at the specified point $t = 9$

Differentiate y with respect to t :

Note prior (q1) that the general rule for composite/nested functions is:

$$\frac{d}{dx}(f(g(x))) = f'(g(x)) \cdot g'(x)$$

Here for $y = \ln(16t^2 + 19)$

$$\frac{dy}{dt} = \frac{1}{16t^2 + 19} \cdot \frac{d}{dt}(16t^2 + 19)$$

$$\frac{d}{dt}(16t^2 + 19) = 32t$$

$$\frac{dy}{dt} = \frac{1}{16t^2 + 19} \cdot 32t = \frac{32t}{16t^2 + 19}$$

Evaluate at $t = 9$:

$$\left. \frac{dy}{dt} \right|_{t=9} = \frac{32(9)}{16(9)^2 + 19} = \frac{288}{1315} \approx 0.219$$

A.4 Q4

Express $\cos t - 8 \sin t$ in the form $A \cos(\omega t + \alpha)$, where $\alpha \geq 0$

you see the thing is the left side, $\cos t - 8 \sin t$, is standard, but the right side introduces a different frequency, ω , in $A \cos(\omega t + \alpha)$.

Since the left side has a frequency of 1, im just gonna assume $\omega = 1$ for simplicity. If ω were different, you would need to rewrite the left side in terms of ωt , but this isn't specified in the problem.

The angle subtraction formula is:

$$A \cos(t - \phi) = A \cos(\phi) \cos(t) + A \sin(\phi) \sin(t)$$

By comparing coefficients from both sides, we have:

$$a = A \cos(\phi)$$

$$b = A \sin(\phi)$$

To find A we use $A = \sqrt{a^2 + b^2}$

This arises from squaring both equations

$a = A \cos(\phi)$ and $b = A \sin(\phi)$:

$$\begin{aligned} a^2 + b^2 &= (A \cos(\phi))^2 + (A \sin(\phi))^2 = \\ &= A^2(\cos^2(\phi) + \sin^2(\phi)) = A^2 \end{aligned}$$

To find the phase shift ϕ , we use $\tan \phi = \frac{b}{a}$

This comes from the definitions of sine and cosine:

$$\tan \phi = \frac{A \sin(\phi)}{A \cos(\phi)} = \frac{b}{a}$$

In so we derive and make use of:

$$A \cos(t - \phi) = a \cos(t) + b \sin(t)$$

Where $A = \sqrt{a^2 + b^2}$ and $\tan \phi = \frac{b}{a}$

for $b = -8$ and $a = 2$

$$A = \sqrt{1^2 + (-8)^2} = \sqrt{65}$$

$$\tan \phi = \frac{-8}{1} = -8 \quad \phi = \arctan(-8) \approx -82.87^\circ$$

In so plugging in gives

$$\begin{aligned} \cos t - 8 \sin t &= A \cos(t - \phi) \\ &= \sqrt{65} \cos(t - \arctan(-8)) \\ &= \sqrt{65} \cos(t - (-82.87^\circ)) \end{aligned}$$

$$\boxed{\cos t - 8 \sin t \approx 8.06 \cos(t + 82.87^\circ)}$$

A.5 Q5

Solve the following system of three linear equations using Cramer's rule

$$\begin{cases} 11v_1 - v_2 + v_3 = 31.4 \\ v_1 + \frac{v_2}{2} - v_3 = 1.9 \\ -9v_1 + 11v_3 = -12 \end{cases}$$

The system can be written in matrix form $A\mathbf{v} = \mathbf{b}$, specifically because of the variable distributions where:

$$A = \begin{bmatrix} 11 & -1 & 1 \\ 1 & \frac{1}{2} & -1 \\ -9 & 0 & 11 \end{bmatrix}, \quad \mathbf{v} = \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}, \quad \mathbf{b} = \begin{bmatrix} 31.4 \\ 1.9 \\ -12 \end{bmatrix}$$

Calculate the determinant $\det(A)$.

$$\det(A) = 67$$

Now solve for each variable using Cramer's rule:

$$A_1 = \begin{bmatrix} 31.4 & -1 & 1 \\ 1.9 & \frac{1}{2} & -1 \\ -12 & 0 & 11 \end{bmatrix} \quad A_2 = \begin{bmatrix} 11 & 31.4 & 1 \\ 1 & 1.9 & -1 \\ -9 & -12 & 11 \end{bmatrix} \quad A_3 = \begin{bmatrix} 11 & -1 & 31.4 \\ 1 & \frac{1}{2} & 1.9 \\ -9 & 0 & -12 \end{bmatrix}$$

Calculate the determinants:

$$\det(A_1) \approx 187.6 \quad \det(A_2) \approx 40.2 \quad \det(A_3) \approx 80.4$$

\mathbf{v} can be found as:

$$v_1 = \frac{\det(A_1)}{\det(A)}, \quad v_2 = \frac{\det(A_2)}{\det(A)}, \quad v_3 = \frac{\det(A_3)}{\det(A)}$$

$$v_1 = \frac{187.6}{67} = 2.8$$

$$v_2 = \frac{40.2}{67} = 0.6$$

$$v_3 = \frac{80.4}{67} = 1.2$$

There are a few ways to calculate the determinants, but especially in this working out i chose not show the method i used since it's not the main focus of the question.

If you're curious about how I did it, the Sarrus method for simplicity.

A.6 Q6

Transpose $z = d + a\sqrt{y}$ to make y the subject.

Starting with:

$$z = d + a\sqrt{y}$$

$$z - d = a\sqrt{y}$$

$$\frac{z - d}{a} = \sqrt{y}$$

$$\left(\frac{z - d}{a}\right)^2 = y$$

Thus, the expression for y is:

$$y = \frac{(z - d)^2}{a^2}$$

i generally consider this the most concise and general expression for y .

im aware you could expand $(z - d)^2$:

$$y = \frac{z^2 - 2zd + d^2}{a^2}$$

and additionally take into account of both possible factorisations:

$$y = \frac{z^2 + d(d - 2z)}{a^2}$$

$$y = \frac{d^2 + z(z - 2d)}{a^2}$$

A.7 Q7

Find a vector that is perpendicular to both of the vectors

$$\mathbf{a} = 4\mathbf{i} + 3\mathbf{j} + 5\mathbf{k}$$

$$\mathbf{b} = 3\mathbf{i} + 4\mathbf{j} - 6\mathbf{k}$$

Hence find a unit vector that is perpendicular to both \mathbf{a} and \mathbf{b} .

The unit vector is

$$\hat{\mathbf{r}} = \frac{\vec{r}}{\|\vec{r}\|}$$

Here we want to define \vec{r} as a vector perpendicular to both \mathbf{a} and \mathbf{b} , to do that we take there cross product $\mathbf{a} \times \mathbf{b}$

$$\vec{r} = \mathbf{a} \times \mathbf{b} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 4 & 3 & 5 \\ 3 & 4 & -6 \end{vmatrix} = -38\mathbf{i} + 39\mathbf{j} + 7\mathbf{k}$$

Find the magnitude:

$$\|\vec{r}\| = \|\mathbf{a} \times \mathbf{b}\| = \sqrt{(-38)^2 + 39^2 + 7^2} = \sqrt{3014}$$

The unit vector is:

$$\frac{-38\mathbf{i} + 39\mathbf{j} + 7\mathbf{k}}{\sqrt{3014}}$$

A.8 Q8

If $M = \begin{pmatrix} 7 & 9 \\ 1 & -2 \end{pmatrix}$ and $N = \begin{pmatrix} 2 & 1 \\ -2 & 6 \end{pmatrix}$ find MN and NM

Calculate MN :

$$\begin{aligned} MN &= \begin{bmatrix} 7 & 9 \\ 1 & -2 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ -2 & 6 \end{bmatrix} \\ &= \begin{bmatrix} 7 \cdot 2 + 9 \cdot (-2) & 7 \cdot 1 + 9 \cdot 6 \\ 1 \cdot 2 + (-2) \cdot (-2) & 1 \cdot 1 + (-2) \cdot 6 \end{bmatrix} \\ &= \boxed{\begin{bmatrix} -4 & 61 \\ 6 & -11 \end{bmatrix}} \end{aligned}$$

Calculate NM :

$$\begin{aligned} NM &= \begin{bmatrix} 2 & 1 \\ -2 & 6 \end{bmatrix} \begin{bmatrix} 7 & 9 \\ 1 & -2 \end{bmatrix} \\ &= \begin{bmatrix} 2 \cdot 7 + 1 \cdot 1 & 2 \cdot 9 + 1 \cdot (-2) \\ -2 \cdot 7 + 6 \cdot 1 & -2 \cdot 9 + 6 \cdot (-2) \end{bmatrix} \\ &= \boxed{\begin{bmatrix} 15 & 16 \\ -8 & -30 \end{bmatrix}} \end{aligned}$$

A.9 Q9

If $y = x^4 - 4x^3 - 90x^2$, find the values of x for which $y'' = 0$

First, find the first derivative:

$$y' = \frac{d}{dx}(x^4 - 4x^3 - 90x^2) = 4x^3 - 12x^2 - 180x$$

Find the second derivative:

$$y'' = \frac{d}{dx}(4x^3 - 12x^2 - 180x) = 12x^2 - 24x - 180$$

Set $y'' = 0$:

$$12x^2 - 24x - 180 = 0$$

Divide by 12:

$$x^2 - 2x - 15 = 0$$

Factor:

$$(x - 5)(x + 3) = 0$$

$$\boxed{x = 5, \quad x = -3}$$

A.10 Q10

Transpose $b = g + t(a - 3)$ to make a the subject

Starting with:

$$b = g + t(a - 3)$$

this is easily rearranged to isolate a :

$$b - g = t(a - 3)$$

$$\frac{b - g}{t} = a - 3$$

$$a = \frac{b - g}{t} + 3$$

Part B

Computing

Notes:

- All graphs and images in the questions are created using TikZ PGF by yours truly.
- Code implementations are original and written primarily in MATLAB to adhere to guidelines, with some sections in Python. **For easy code access, please refer to my [GitHub repository](#).**
 - While I am required to use MATLAB for this module, relying solely on it feels somewhat short-sighted. It is a temporary student license, and focusing exclusively on MATLAB means missing out on essential programming skills and their broader applicability. Although I must use MATLAB for this course, it does not fully align with my long-term goals.
- To develop a universal and user-friendly code for this Part, it is essential to enhance usability and accessibility. Here, I outline two main approaches that can effectively address these requirements:
 1. **Approach 1: Maximising the users experience.**
Creating a Graphical User Interface (GUI) can significantly improve the user experience, especially for those who are not familiar with coding.
 2. **Approach 2: Interactive Programming Environment**
For users who prefer coding but still seek simplicity and clarity, an interactive programming environment can be a valuable alternative.

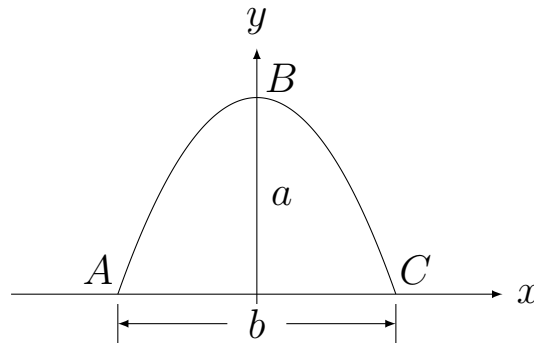
Each code excerpt aims to accomplish one of these facets or strategies. For every question, I will offer at least one polished version of my response; its up to you to decide what that may be.

- Finally, please consider the answers as a whole.

B.1 Q1

The arc length of a segment of a parabola ABC of an ellipse with semi-minor axes a and b is given approximately by:

$$L_{ABC} = \frac{1}{2} \sqrt{b^2 + 16a^2} + \frac{b^2}{8a} \ln \left(\frac{4a + \sqrt{b^2 + 16a^2}}{b} \right)$$



Write a universal, user-friendly code, test your programme and determine L_{ABC} if $a = 11$ cm and $b = 9$ cm.

matlab scripts/q1.m

```

1
2 %make a function to call for the calculation
3
4 % In MATLAB, when defining a function that returns a value,
5 % you must specify an output argument in the function declaration
6 % and assign the result to this output argument,
7 % rather than using return %
8
9 function L_ABC = calculate_arc_length(a, b)
10     %write in ascci math using matlab built in functions
11     L_ABC = (1/2) * sqrt(b^2 + 16 * a^2) + (b^2 / (8 * a)) * log((4 * a + sqrt(b^2 +
12         16 * a^2)) / b);
13 end
14
15 %prompt the user for input values
16 a = input('Enter the value of a (height in cm): ');
17 b = input('Enter the value of b (width in cm): ');
18
19 %calculate the arc length by calling the function
20 L_ABC = calculate_arc_length(a, b);
21
22 %display the result by printing
23 fprintf('The arc length L_ABC is: %.2f\n', L_ABC);
24
25 %realistically not much error handling is inputed but i dont think that is the goal
26 here

```

Name	Value	Size	Class	>> q1
a	11	1×1	double	Enter the value of a (height in cm): 11
b	9	1×1	double	Enter the value of b (width in cm): 9
L_ABC	24.5637	1×1	double	The arc length L_ABC is: 24.56 >>

B.1.1 Advanced version

We are tasked with analyzing a parabola where:

- a represents the height of the parabola
- b represents the width of the parabola

My goal is to plot the parabola, first by formulating an equation in terms of these factors. Initially, we begin with a simple parabola in the general shape (x^2) similar to shown in the graph. Our goal is to select a reasonable function, with variables associated with the x scale and y location of the parabola:

$$y = -(\beta x)^2 + \gamma$$

Given our problem statement:

- γ represents the height, so $\gamma = a$
- The width is related to the roots of the equation when $y = 0$

To find β , we solve:

$$0 = -(\beta x)^2 + \gamma$$

$$\beta = \frac{2\sqrt{\gamma}}{b}$$

since we know γ :

$$\beta = \frac{2\sqrt{a}}{b}$$

Note: This requires $b \neq 0$ and $\sqrt{a} \neq 0$ (i.e., $a > 0$).

Substituting γ and β into our original equation:

$$y = -\left(\frac{2\sqrt{a}}{b}x\right)^2 + a$$

This is our final parabola equation in terms of a and b . The arc length of the parabola from $x = -\frac{b}{2}$ to $x = \frac{b}{2}$ is given by:

$$L_{ABC} = \frac{1}{2}\sqrt{b^2 + 16a^2} + \frac{b^2}{8a} \ln\left(\frac{4a + \sqrt{b^2 + 16a^2}}{b}\right)$$

When implementing this in a program:

- Ensure that when there are no limit parameters for the inputs a and b , the conditions $a > 0$ and $b \neq 0$ are appropriately handled.
- Update the plot of $y = -\left(\frac{2\sqrt{a}}{b}x\right)^2 + a$ so that the sliders for a and b directly control the height and width, respectively.
- Calculate the arc length of the parabola using a function with inputs a and b , and display the result in the plot.

The rest is just nitpicky presentation, all just preference i tried to do this in MATLAB but it don't really feel nice just finicky. ao i did in py, it is possible in MATLAB though.

py scripts/ql_advanced.py

```

1  """
2  Requirements to run:
3      - Python 3.x (https://www.python.org/)
4      - NumPy and Matplotlib (install with cmd prmp: pip install numpy matplotlib)
5  """
6
7  import numpy as np
8  import matplotlib.pyplot as plt
9  from matplotlib.widgets import Slider, Button
10
11 def arc_length_parabola(a, b):
12     L_ABC=(1/2)*np.sqrt(b**2+16*a**2)+(b**2/(8*a))*np.log((4*a+np.sqrt(b**2+16*a**2))
13         /b)
14     return L_ABC
15
16 fig, ax = plt.subplots(figsize=(10, 6))
17 plt.subplots_adjust(left=0.1, bottom=0.3, right=0.9, top=0.9)
18 initial_a = 11.0
19 initial_b = 9.0
20
21 ax_slider_a = plt.axes([0.1, 0.15, 0.8, 0.03])
22 ax_slider_b = plt.axes([0.1, 0.1, 0.8, 0.03])
23
24 slider_a = Slider(ax_slider_a, 'a (height)', 0.1, 20, valinit=initial_a, valfmt='%0.2f')
25 slider_b = Slider(ax_slider_b, 'b (width)', 0.1, 20, valinit=initial_b, valfmt='%0.2f')
26
27 x = np.linspace(-10, 10, 1000)
28
29 def update(val):
30     a = slider_a.val
31     b = slider_b.val
32     L_ABC = arc_length_parabola(a, b)
33
34     ax.clear()
35     # should add if a > 0 and b != 0: but im not going to since i set the slider
36     # limits accordingly
37     y = -((2*np.sqrt(a))*x/b)**2 + a
38     ax.plot(x, y, label=r'$y = -\left(\frac{2\sqrt{a}}{b}x\right)^2 + a$', color='blue')
39
40     ax.vlines(0, 0, a, color='red', linewidth=2, zorder=10, label=r'$a$ (height)')
41     ax.hlines(0, -b/2, b/2, color='green', linewidth=2, zorder=10, label=r'$b$ (width)')
42
43     ax.text(0.05, a/2, f'a = {a:.2f} cm', color='red', fontsize=10, verticalalignment='bottom')
44     ax.text(0, 0.05, f'b = {b:.2f} cm', color='green', fontsize=10, horizontalalignment='right')
45
46     A_x = -b/2
47     C_x = b/2
48
49     ax.plot(A_x, 0, 'o', zorder=10, color='purple', label=r'Point $A = (-\frac{b}{2}, 0)$')
50     ax.plot(0, a, 'o', zorder=10, color='orange', label=r'Point $B = (0, a)$')
51     ax.plot(C_x, 0, 'o', zorder=10, color='purple', label=r'Point $C = (\frac{b}{2}, 0)$')

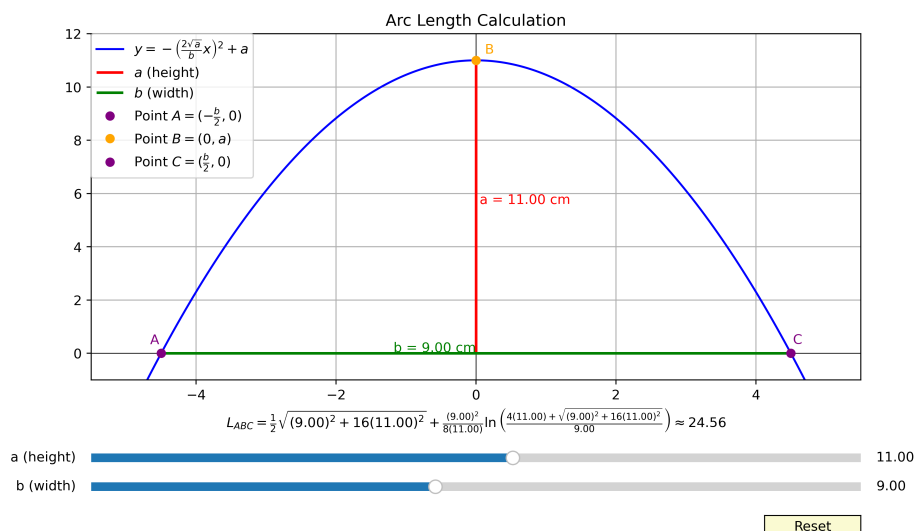
```



```

51 ax.annotate('A', (A_x, 0), textcoords="offset points", xytext=(-5,7), ha='center',
52             , color='purple')
53 ax.annotate('B', (0, a), textcoords="offset points", xytext=(10,5), ha='center',
54             color='orange')
55 ax.annotate('C', (C_x, 0), textcoords="offset points", xytext=(5,7), ha='center',
56             color='purple')
57
58 ax.set_title(f'Arc Length Calculation')
59 ax.set_xlabel(r'$L_{ABC} = \frac{1}{2}\sqrt{{b:.2f}^2 + 16({a:.2f})^2} + \frac{{b:.2f}^2 + r'}{8({a:.2f} + r)}\ln\left(\frac{4({a:.2f} + r) + \sqrt{{b:.2f}^2 + 16({a:.2f})^2} + r'}{{b:.2f} + r}\right) \approx {L_{ABC}:.2f}$')
60
61 ax.set_ylim(-1, a + 1)
62 ax.set_xlim(-b/2 - 1, b/2 + 1)
63
64 ax.legend(bbox_to_anchor=(0, 1), loc='upper left', borderaxespad=0.)
65
66 ax.grid(True)
67 ax.axhline(y=0, color='k', linestyle='-', linewidth=0.5)
68 ax.axvline(x=0, color='k', linestyle='-', linewidth=0.5)
69 plt.draw()
70
71 slider_a.on_changed(update)
72 slider_b.on_changed(update)
73
74 resetax = plt.axes([0.8, 0.025, 0.1, 0.04])
75 button = Button(resetax, 'Reset', color='lightgoldenrodyellow', hovercolor='0.975')
76
77 def reset(event):
78     slider_a.reset()
79     slider_b.reset()
80     update(None)
81
82 button.on_clicked(reset)
83
84 update(None)
85
86 plt.savefig('images/Figure_1.png', dpi=400)
87 plt.show()

```



With the sliders, you can interactively update the plot and change a and b values in real time!

B.2 Q2

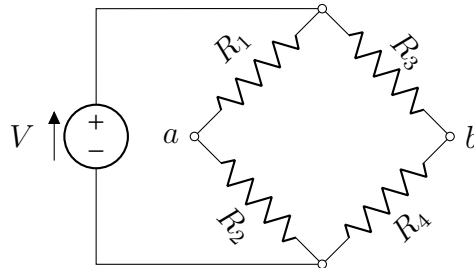
The voltage difference V_{ab} between points a and b in the Wheatstone bridge circuit is:

$$V_{ab} = V \left(\frac{R_1 R_3 - R_2 R_4}{(R_1 + R_2)(R_3 + R_4)} \right)$$

Write a universal, user-friendly program that calculates the voltage difference V_{ab} .

Test your program using the following values:

- $V = 14$ volts
- $R_1 = 120.6 \, \Omega$
- $R_2 = 119.3 \, \Omega$
- $R_3 = 121.2 \, \Omega$
- $R_4 = 118.8 \, \Omega$



matlab scripts/q2.m

```

1 function wheatstone_bridge_ui()
2     % create a UI figure
3     fig = uifigure('Name', 'Wheatstone Bridge Circuit Calculator', 'Position', [100,
4         100, 600, 400]);
5
6     % image stuff dont worry bout this
7     imgURL = 'https://raw.githubusercontent.com/sakx7/mathcompuni/main/images/
8         wheatstone_bridge.jpg';
9     localImgPath = fullfile(pwd, 'wheatstone_bridge.jpg');
10    if ~isfile(localImgPath)
11        try
12            websave(localImgPath, imgURL);
13        catch
14            uialert(fig, 'Failed to download the image.', 'Download Error');
15            return;
16        end
17    end
18    img = uiimage(fig);
19    img.Position = [25, 75, 250, 250];
20    img.ImageSource = localImgPath;
21
22    % add input labels and fields on the right side
23    voltageLabel = uilabel(fig, 'Text', '$V$ ($V$/volts):', 'Position', [333, 300, 10
24        0, 30], 'Interpreter', 'latex');
25    voltageField = uieditfield(fig, 'numeric', 'Position', [405, 300, 100, 30]);
26
27    r1Label = uilabel(fig, 'Text', '$R_1$ ($\Omega$/ohms):', 'Position', [325, 250, 1
28        00, 30], 'Interpreter', 'latex');
29    r1Field = uieditfield(fig, 'numeric', 'Position', [405, 250, 100, 30]);
30
31    r2Label = uilabel(fig, 'Text', '$R_2$ ($\Omega$/ohms):', 'Position', [325, 200, 1
32        00, 30], 'Interpreter', 'latex');
33    r2Field = uieditfield(fig, 'numeric', 'Position', [405, 200, 100, 30]);
34
35    r3Label = uilabel(fig, 'Text', '$R_3$ ($\Omega$/ohms):', 'Position', [325, 150, 1
36        00, 30], 'Interpreter', 'latex');

```

```

31 r3Field = uieditfield(fig, 'numeric', 'Position', [405, 150, 100, 30]);
32
33 r4Label = uilabel(fig, 'Text', '$R_4$ ($\Omega$/ohms):', 'Position', [325, 100, 1
34 00, 30], 'Interpreter', 'latex');
35 r4Field = uieditfield(fig, 'numeric', 'Position', [405, 100, 100, 30]);
36
37 % add label for result
38 outputLabel = uilabel(fig, 'Position', [25, 20, 250, 50], 'Text', 'Output will be
39 displayed here.', 'FontSize', 14, 'Interpreter', 'latex');
40
41 % add button
42 calcButton = uibutton(fig, 'push', ...
43 'Text', 'Calculate $V_{ab}$', ...
44 'Position', [375, 50, 150, 30], ...
45 'Interpreter', 'latex', ...
46 'ButtonPushedFcn', @(calcButton,event) calculate_V_ab(fig, voltageField, r1
47 Field, r2Field, r3Field, r4Field, outputLabel)); % Use outputLabel
48 end
49
50 % Main function to calculate weat (V_ab) and display the result
51 function calculate_V_ab(fig, voltageField, r1Field, r2Field, r3Field, r4Field,
52 outputLabel)
53 % get values from the input fields
54 V = voltageField.Value;
55 R_1 = r1Field.Value;
56 R_2 = r2Field.Value;
57 R_3 = r3Field.Value;
58 R_4 = r4Field.Value;
59
60 % input validation error handles
61 inputs = [V, R_1, R_2, R_3, R_4];
62 if any(isnan(inputs)) || any(inputs <= 0)
63     uialert(fig, 'enter valid values.', 'Input Error');
64     return;
65 end
66
67 % the weat
68 V_ab = V * (R_1 * R_3 - R_2 * R_4) / ((R_1 + R_2) * (R_3 + R_4));
69
70 % final display result in the label
71 msg = sprintf('The output voltage $V_{ab}$ is: %.4f V', V_ab);
72 outputLabel.Text = msg; % update the label with the output message
73 end

```