

$$\frac{dx}{dt} = \dot{x} = v \cos(\theta) \quad \rightarrow (1)$$

$$\frac{dy}{dt} = \dot{y} = v \sin(\theta) \quad \rightarrow (2)$$

given

$$\frac{d\theta}{dt} = \dot{\theta} = \omega \quad \rightarrow (3)$$

$$x_p = x + L \cos(\theta) \quad \rightarrow (4)$$

$$y_p = y + L \sin(\theta) \quad \rightarrow (5)$$

$$x(t) = 10 \cos\left(\frac{\pi t}{5}\right) + 5 \sin\left(\frac{\pi t}{10}\right) \quad \rightarrow (6)$$

$$y(t) = 10 \sin\left(\frac{\pi t}{10}\right) - 5 \cos\left(\frac{\pi t}{10}\right) + 5 \quad \rightarrow (7)$$

$$\frac{dx(t)}{dt} = \dot{x} = -2\pi \sin\left(\frac{\pi t}{5}\right) + \frac{\pi}{2} \cos\left(\frac{\pi t}{10}\right) \quad \rightarrow (8)$$

$$\frac{dy(t)}{dt} = \dot{y} = \pi \cos\left(\frac{\pi t}{10}\right) + \frac{\pi}{2} \sin\left(\frac{\pi t}{10}\right) \quad \rightarrow (9)$$

$$v = \frac{\dot{x}}{\cos(\theta)} \quad \rightarrow (10)$$

$$v = \frac{\dot{y}}{\sin(\theta)} \quad \rightarrow (11)$$

$$\theta(t) = \tan^{-1} \left(\frac{2 \cos\left(\frac{\pi t}{10}\right) + \sin\left(\frac{\pi t}{10}\right)}{-4 \sin\left(\frac{\pi t}{5}\right) + \cos\left(\frac{\pi t}{10}\right)} \right) \quad \rightarrow (12)$$

$$\omega = \frac{\pi}{10} + \frac{\pi}{5} \sin\left(\frac{3\pi t}{10}\right) + \frac{2\pi}{10} \sin\left(\frac{\pi t}{10}\right) + \cos\left(\frac{\pi t}{10}\right) + \frac{\pi}{10} \cos\left(\frac{3\pi t}{10}\right) + \frac{\pi}{10} \cos\left(\frac{\pi t}{10}\right)$$

$$11 + 2 \cos\left(\frac{2\pi t}{10}\right) + 2 \sin\left(\frac{2\pi t}{10}\right) - 8 \cos\left(\frac{4\pi t}{10}\right) - 4 \sin\left(\frac{3\pi t}{10}\right) - 4 \sin\left(\frac{\pi t}{10}\right)$$