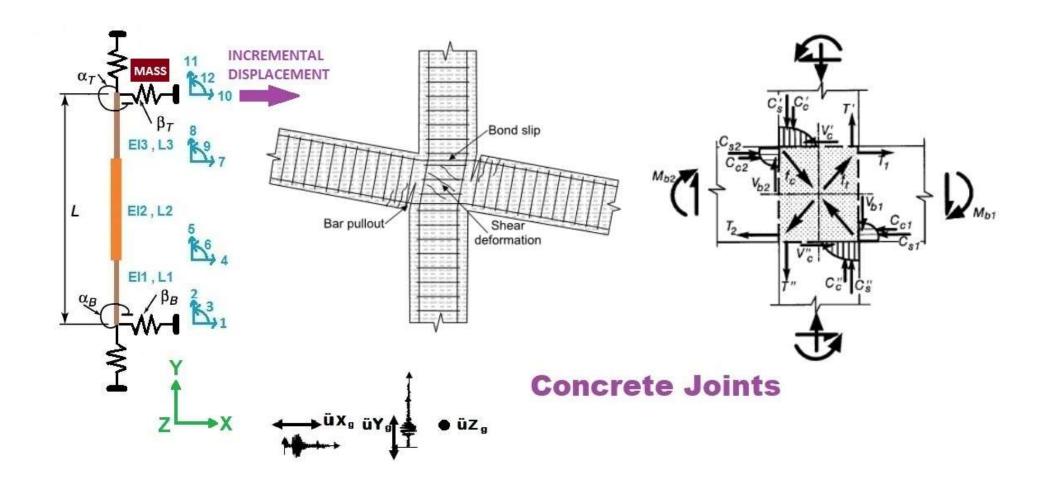
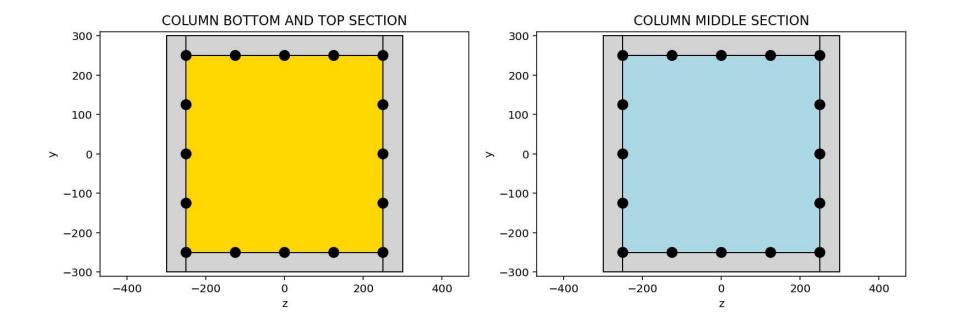
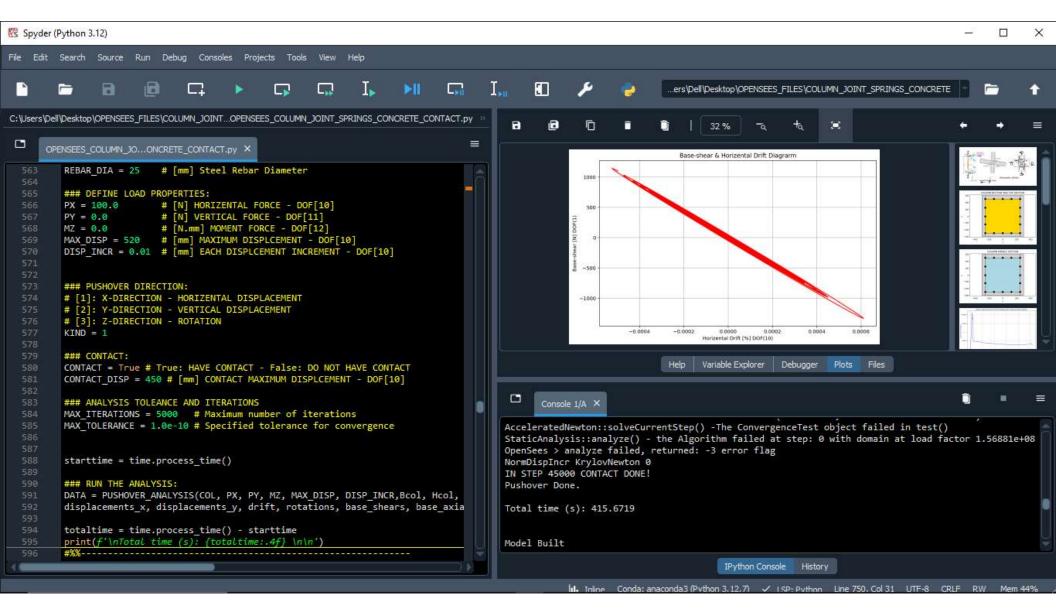
IN THE NAME OF ALLAH

PUSHOVER ANALYSIS OF CONCRETE COLUMNS WITH AXIAL AND ROTATIONAL SPRINGS FOR MODELING BEAM COLUMN JOINTS

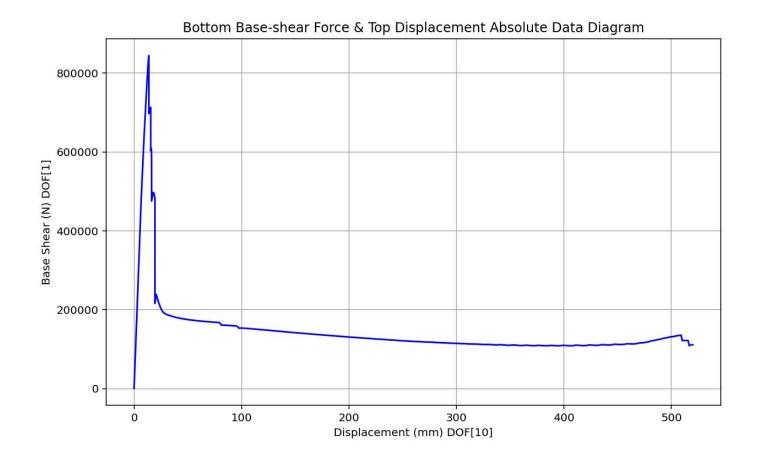
THIS PROGRAM WRITTEN BY SALAR DELAVAR GHASHGHAEI (QASHQAI)

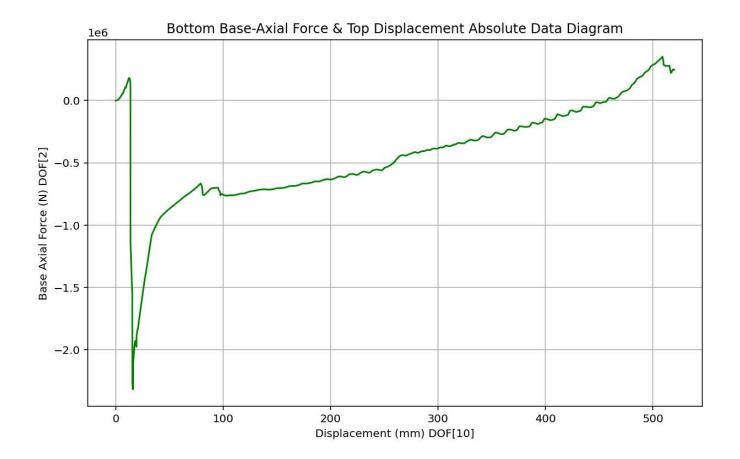


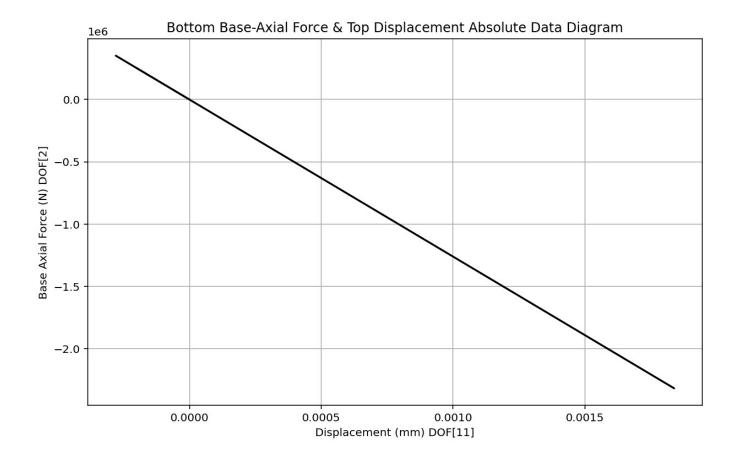


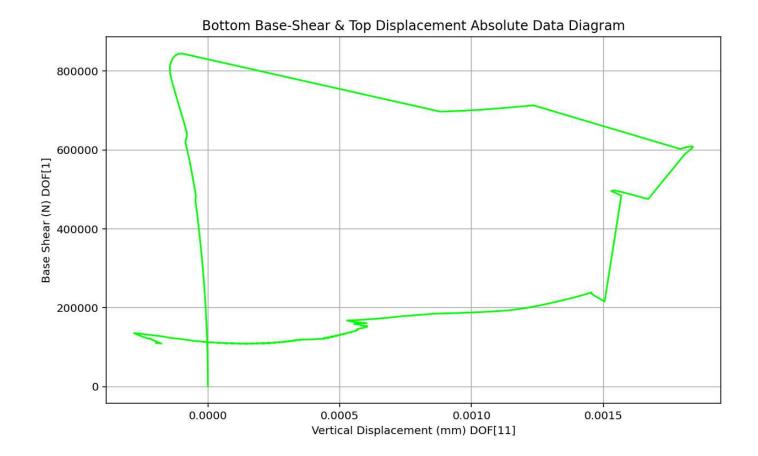


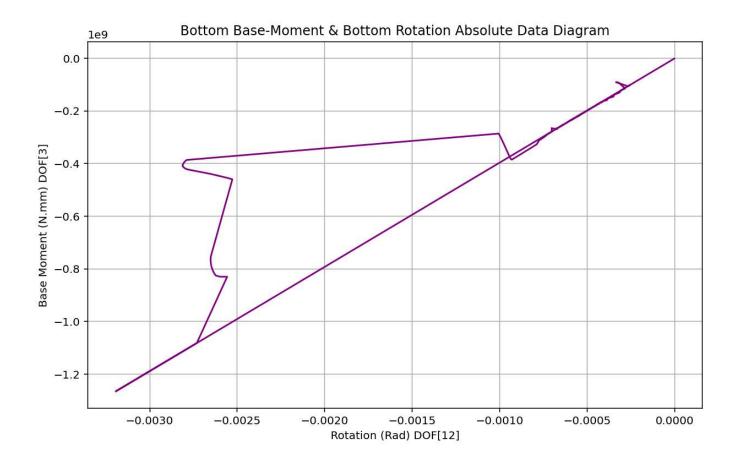
PUSHOVER ANALYSIS OF CONCRETE COLUMNS WITH AXIAL AND ROTATIONAL SPRINGS FOR MODELING BEAM COLUMN JOINTS

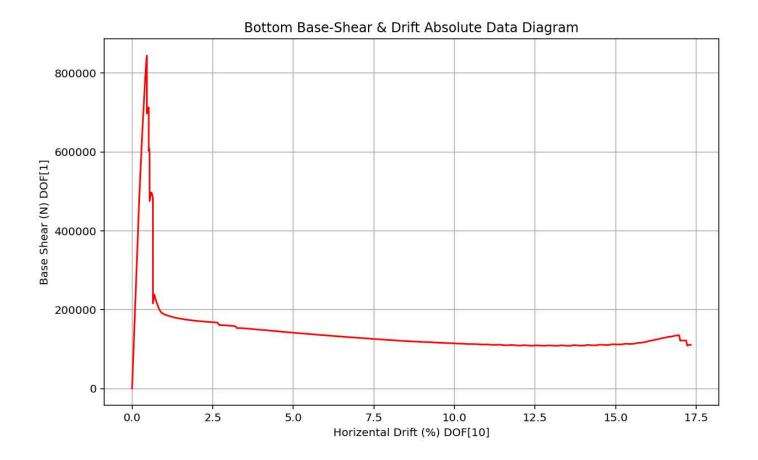




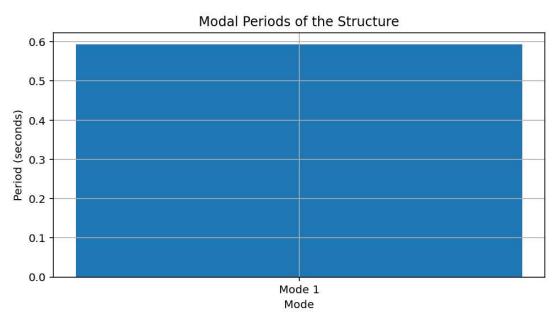






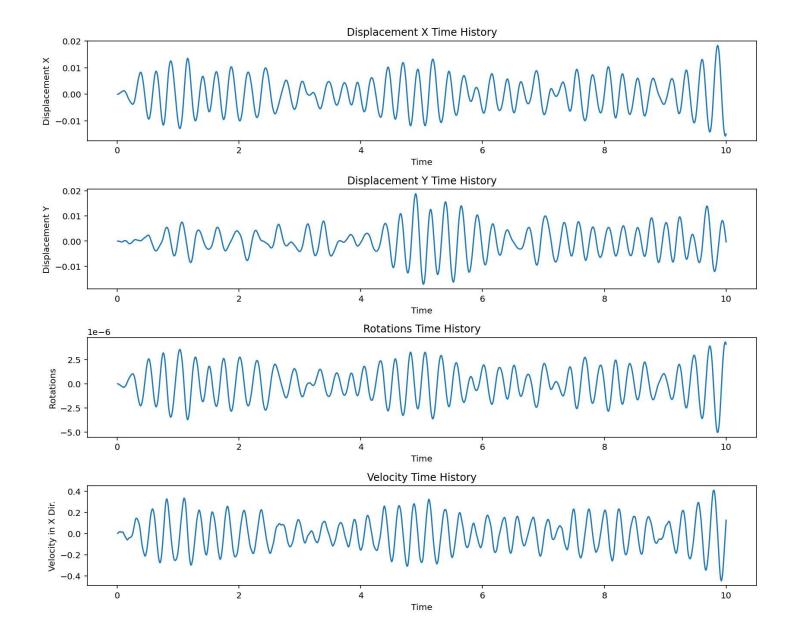


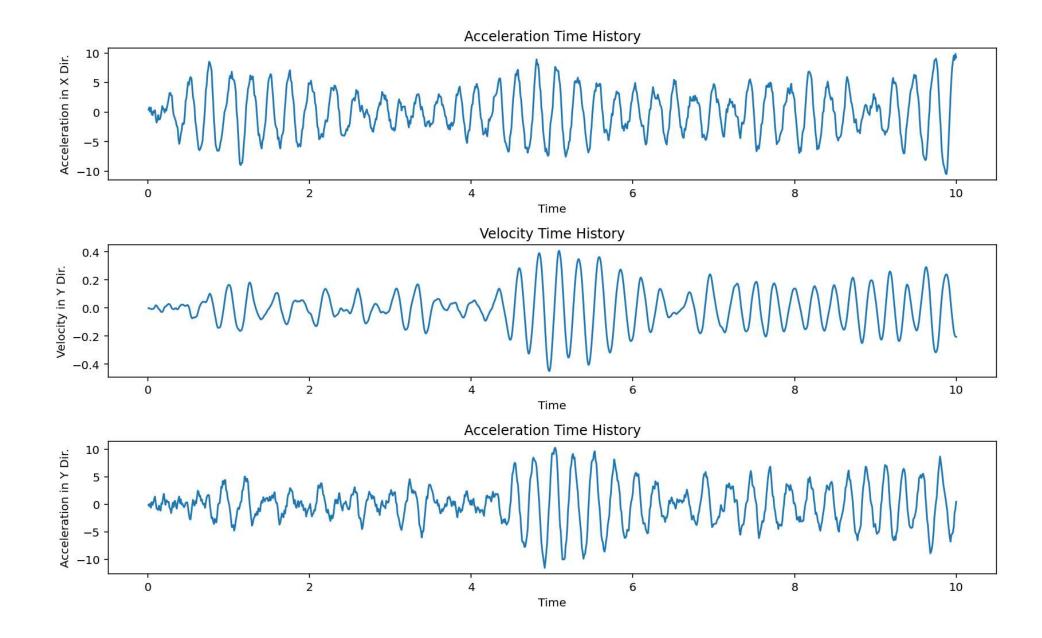
DYNAMIC ANALYSIS OF CONCRETE COLUMNS WITH AXIAL AND ROTATIONAL SPRINGS FOR MODELING BEAM COLUMN JOINTS

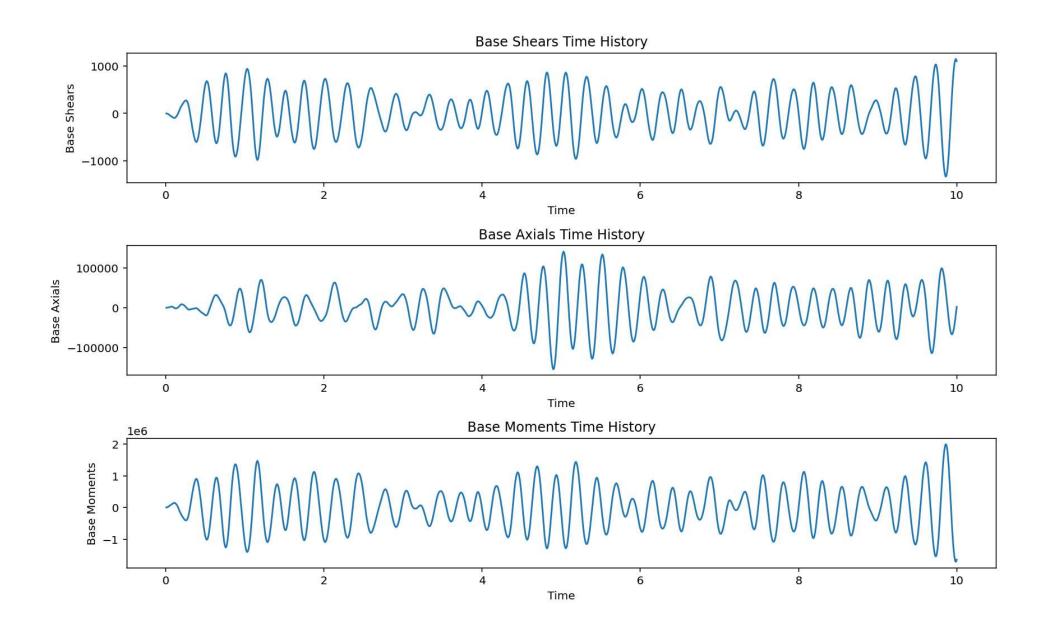


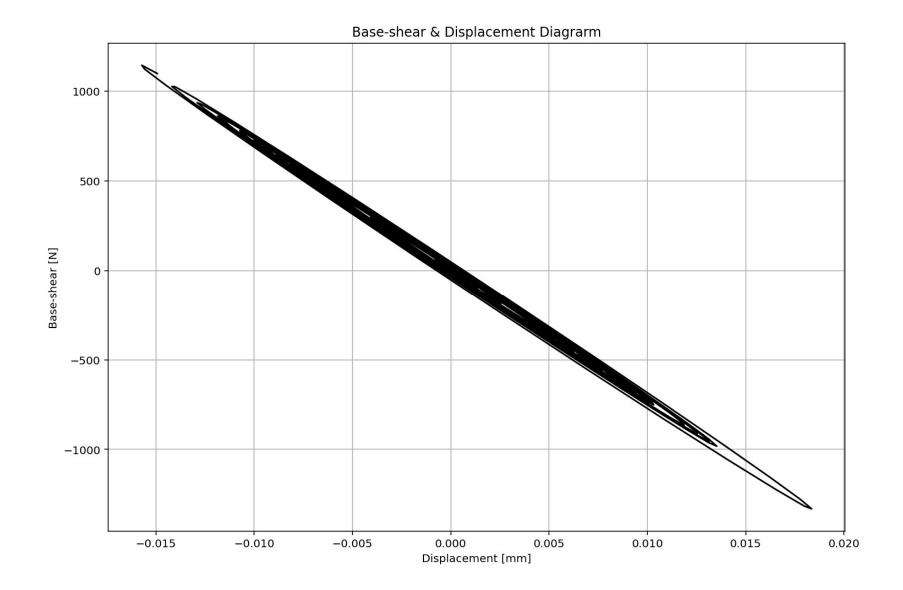
Period: 0.12475926338077073 (s)

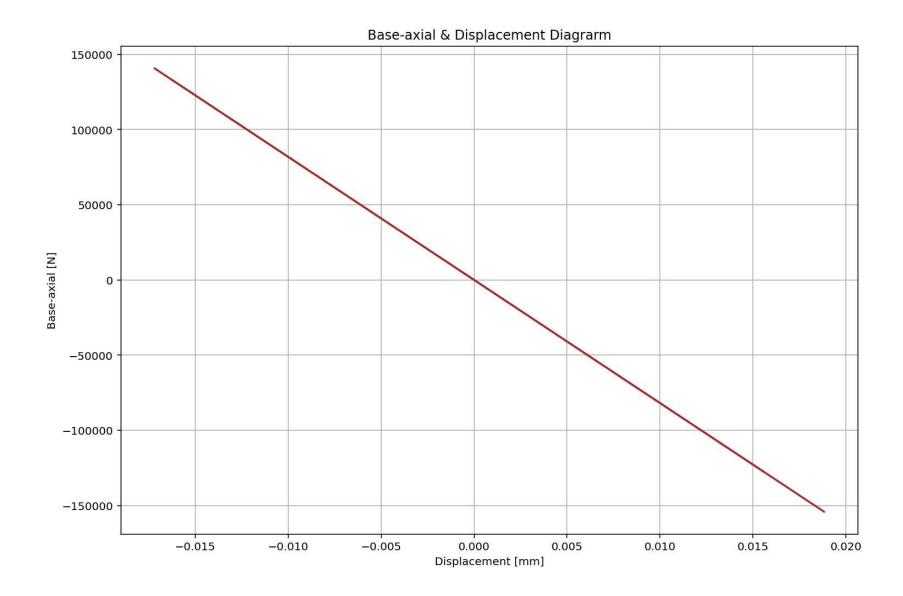
Natural Frequency: 8.015436873396377 (Hz)

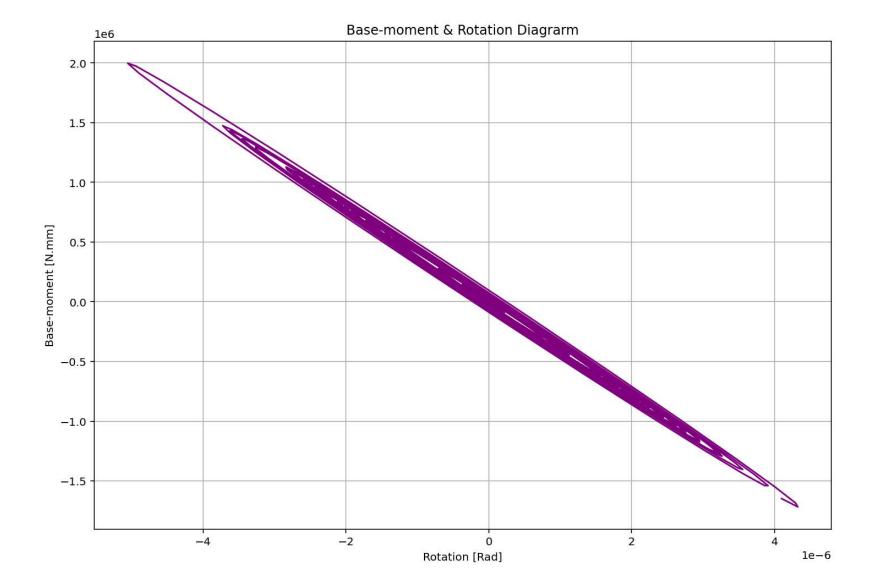


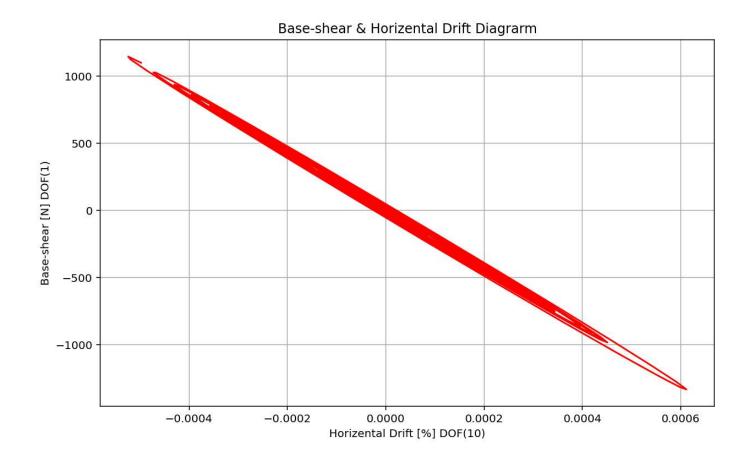












VISCOUSLY DAMPED FREE VIBRATION

$$m\ddot{u} + c\dot{u} + ku = 0$$

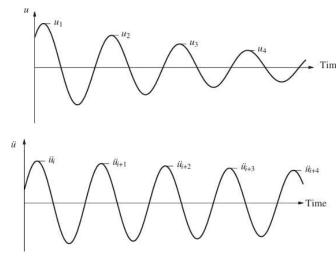
$$\ddot{u} + 2\zeta \omega_n \dot{u} + \omega_n^2 u = 0$$

10

Logarithmic decrement δ

$$\omega_n = \sqrt{k/m}$$
 $\zeta = \frac{c}{2m\omega_n} = \frac{c}{c_{cr}}$ $\omega_D = \omega_n \sqrt{1 - \zeta^2}$

$$u(t) = e^{-\zeta \omega_n t} \left[u(0) \cos \omega_D t + \frac{\dot{u}(0) + \zeta \omega_n u(0)}{\omega_D} \sin \omega_D t \right]$$

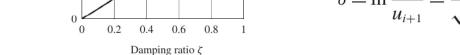


Exact Damping Ratio: 1.06798624e-02

Decay of Motion

$$\delta = \ln \frac{u_i}{u_{i+1}} = 2\pi \, \zeta$$
 (approximate relation)

$$\delta = \ln \frac{u_i}{u_{i+1}} = \frac{2\pi \, \zeta}{\sqrt{1-\zeta^2}}$$
 (EXACT RELATION)



EXACT AND APPROXIMATE RELATIONS BETWEEN LOGARITHMIC DECREMENT AND DAMPING RATIO