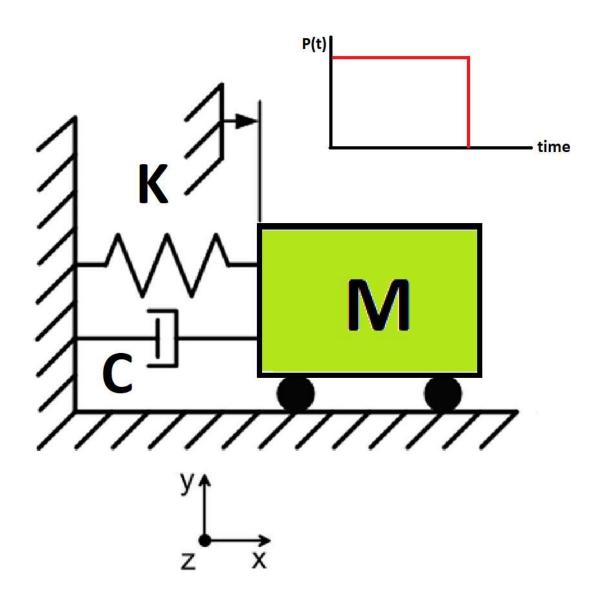
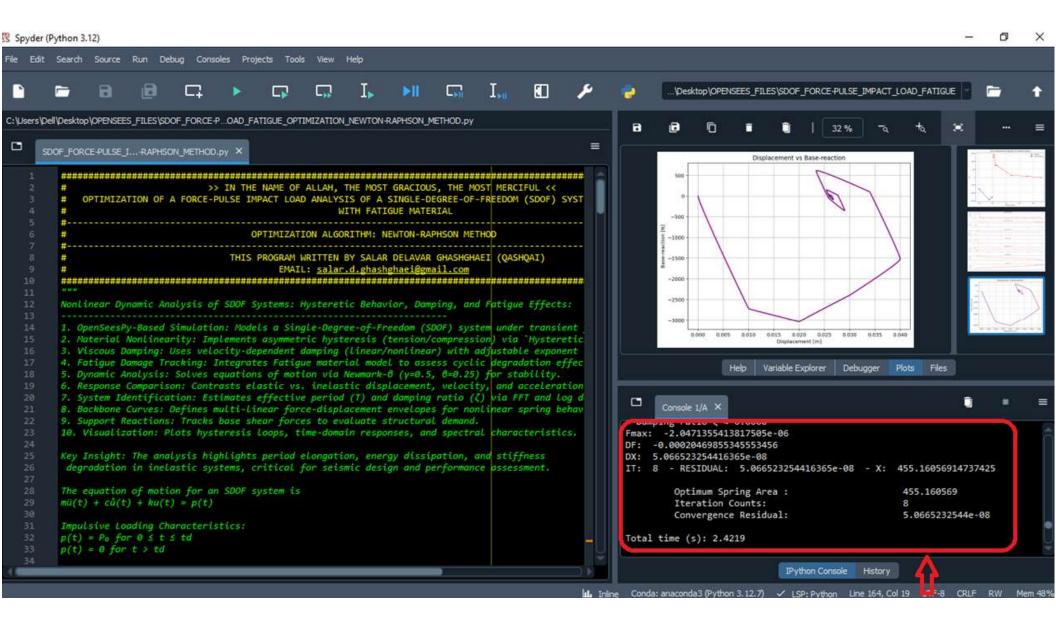
>> IN THE NAME OF ALLAH, THE MOST GRACIOUS, THE MOST MERCIFUL <<

## OPTIMIZATION OF A FORCE-PULSE IMPACT LOAD ANALYSIS OF A SINGLE-DEGREE-OF-FREEDOM (SDOF) SYSTEM USING OPENSEES

WRITTEN BY SALAR DELAVAR GHASHGHAEI (QASHQAI)





## IT: 6 - RESIDUAL: 1.2674278050826335 - X: 455.15496531261266

Period T ≈ 3.847 s

Damping ratio ζ ≈ 0.0000 SUPPLY: 0.04000115

F: 1.147050329011745e-06

Period T ≈ 3.847 s

Damping ratio ζ≈ 0.0000

Fmin: 3.1938197959102688e-06

**Period T** ≈ 3.847 s

Damping ratio ζ≈ 0.0000

Fmax: -8.999481584462399e-07 DF: -0.00020468839771782543 DX: -0.0056038854268282414

IT: 7 - RESIDUAL: 0.0056038854268282414 - X: 455.16056919803947

**Period T** ≈ 3.847 s

Damping ratio ζ≈ 0.0000

SUPPLY: 0.04000000

F: -1.0371099812278572e-11

**Period T** ≈ 3.847 s

Damping ratio ζ≈ 0.0000

Fmin: 2.0468355277289407e-06

**Period T** ≈ 3.847 s

Damping ratio ζ≈ 0.0000

Fmax: -2.0471355413817505e-06 DF: -0.00020469855345553456 DX: 5.066523254416365e-08

IT: 8 - RESIDUAL: 5.066523254416365e-08 - X: 455.16056914737425

Optimum Spring Area: 455.160569

Iteration Counts: 8

Convergence Residual: 5.0665232544e-08

Total time (s): 2.4219

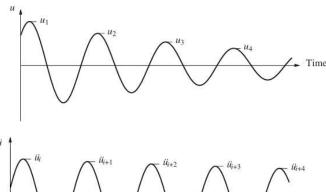
## VISCOUSLY DAMPED FREE VIBRATION

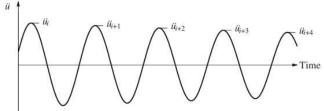
$$m\ddot{u} + c\dot{u} + ku = 0$$

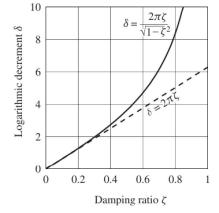
$$\ddot{u} + 2\zeta \omega_n \dot{u} + \omega_n^2 u = 0$$

$$\omega_n = \sqrt{k/m}$$
  $\zeta = \frac{c}{2m\omega_n} = \frac{c}{c_{cr}}$   $\omega_D = \omega_n \sqrt{1 - \zeta^2}$ 

$$u(t) = e^{-\zeta \omega_n t} \left[ u(0) \cos \omega_D t + \frac{\dot{u}(0) + \zeta \omega_n u(0)}{\omega_D} \sin \omega_D t \right]$$







## **Decay of Motion**

$$\delta = \ln \frac{u_i}{u_{i+1}} = 2\pi \zeta$$
 (approximate relation)

$$\delta = \ln \frac{u_i}{u_{i+1}} = \frac{2\pi \, \zeta}{\sqrt{1-\zeta^2}}$$
 (EXACT RELATION)

**EXACT AND APPROXIMATE RELATIONS BETWEEN LOGARITHMIC DECREMENT AND DAMPING RATIO** 

