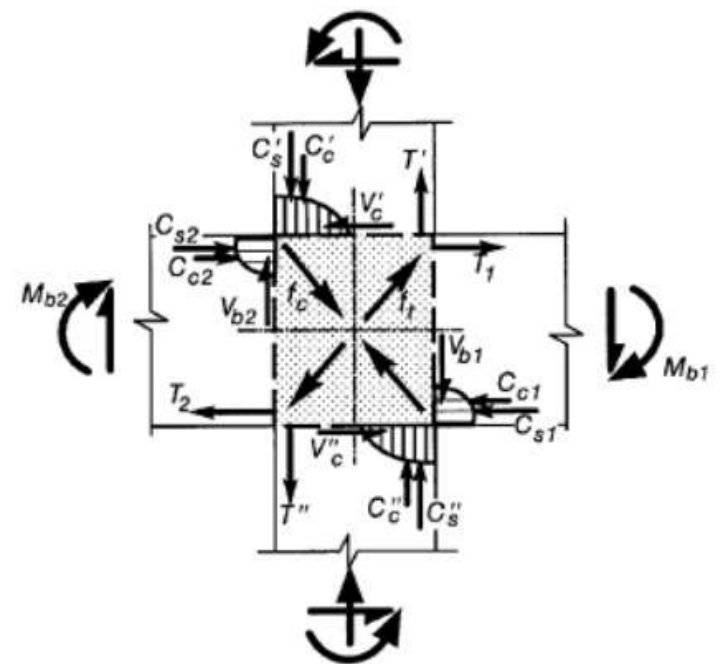
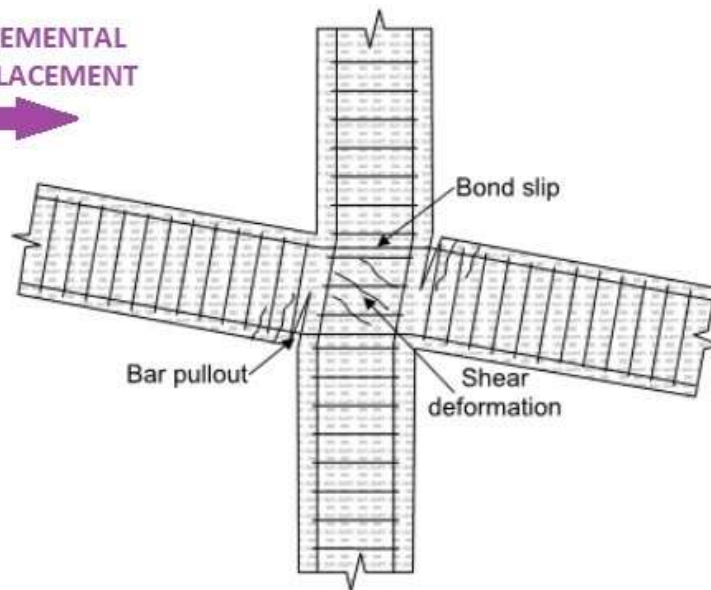
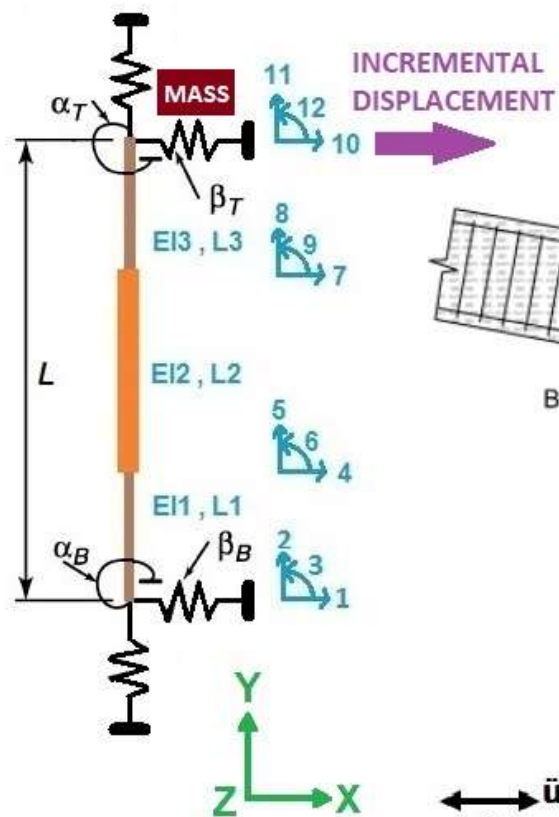


IN THE NAME OF ALLAH, THE MOST GRACIOUS, THE MOST MERCIFUL

PUSHOVER AND DYNAMIC ANALYSIS OF CONCRETE COLUMNS WITH AXIAL AND ROTATIONAL SPRINGS FOR MODELING BEAM COLUMN JOINTS

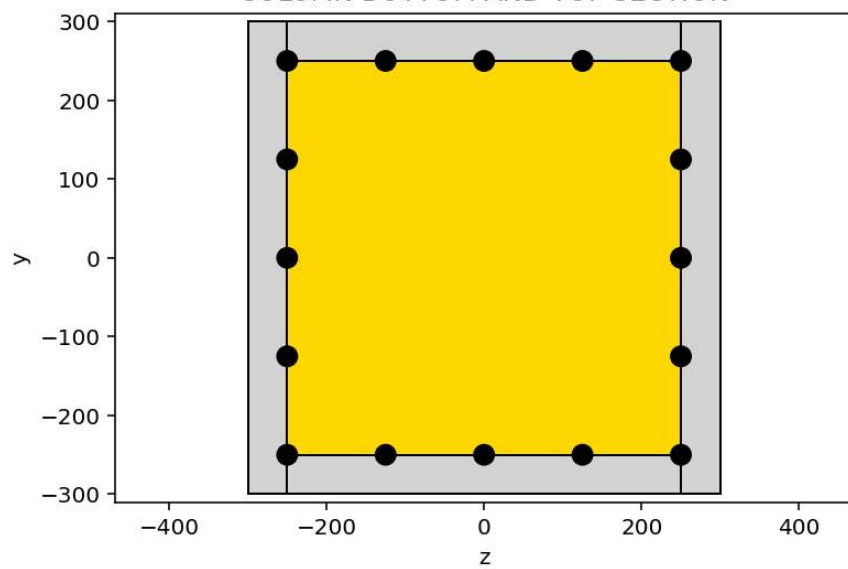
WRITTEN BY SALAR DELAVAR GHASHGHAEE (QASHQAI)



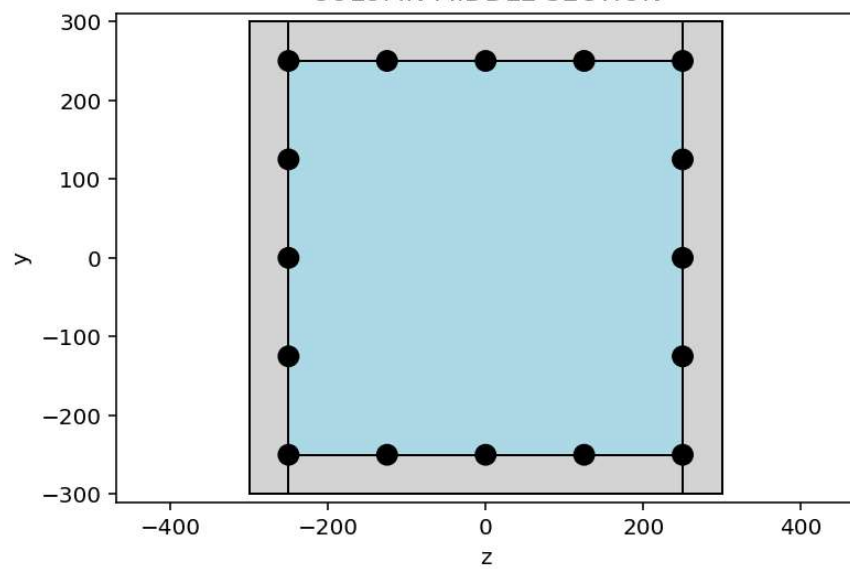
Concrete Joints



COLUMN BOTTOM AND TOP SECTION



COLUMN MIDDLE SECTION





CONCRETE_COLUMN_JOINTS_CONTACT.py

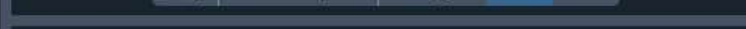
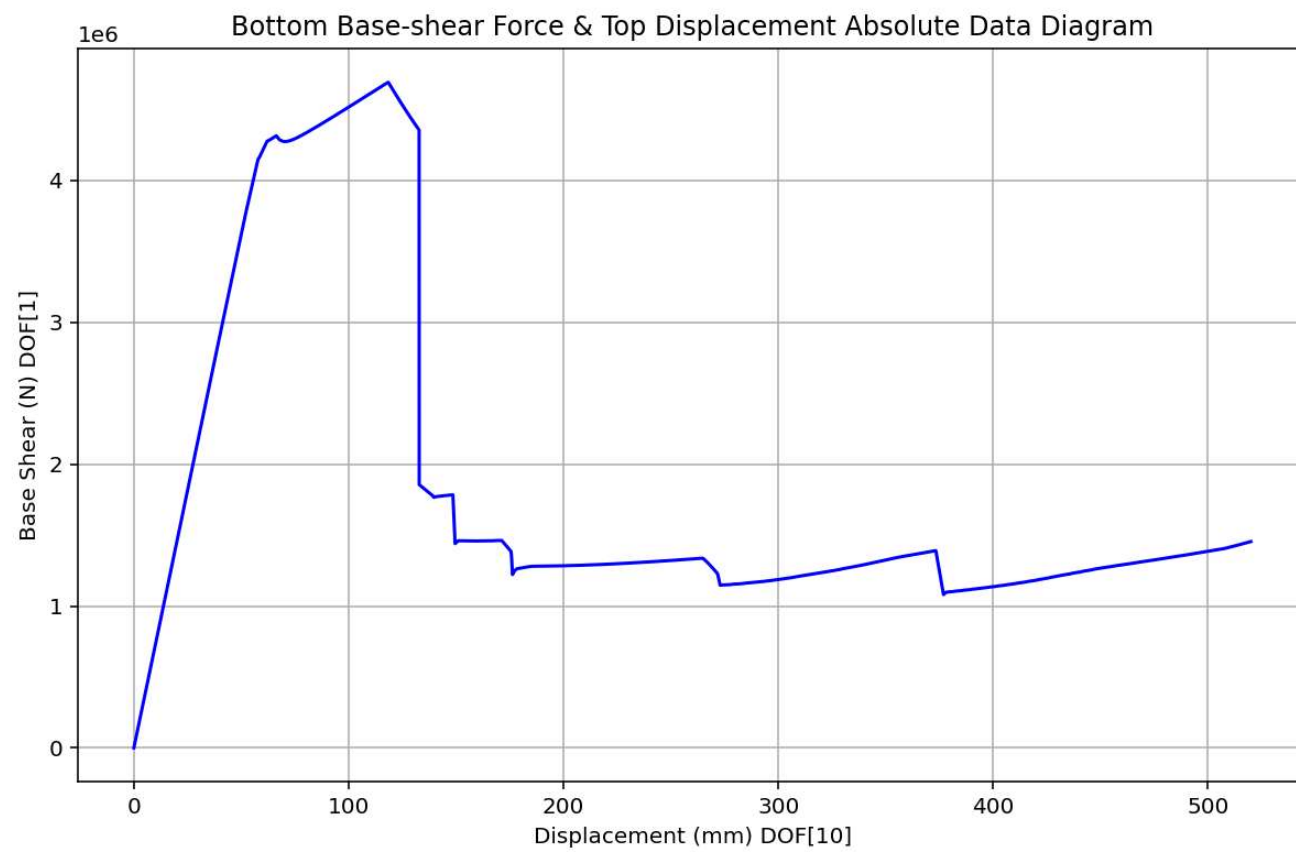
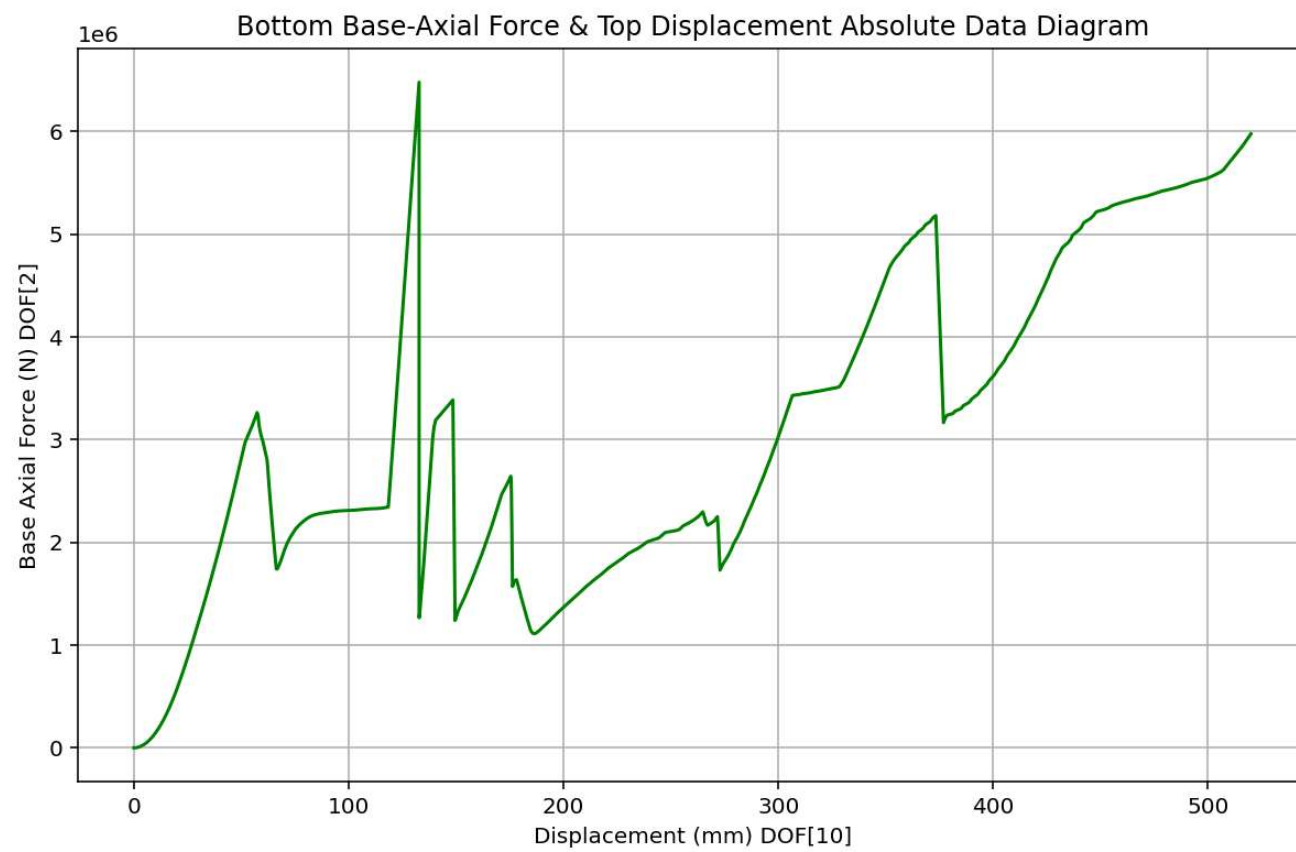
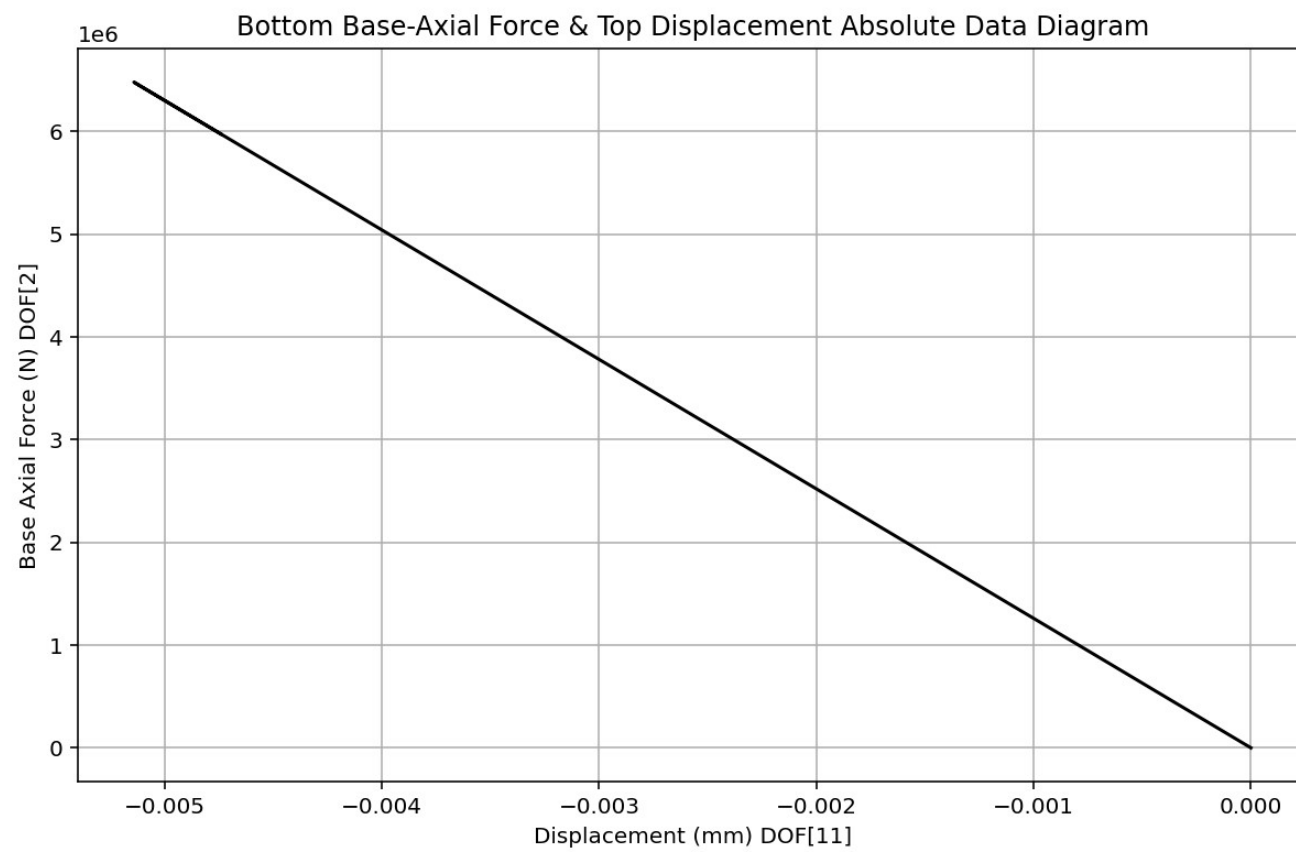


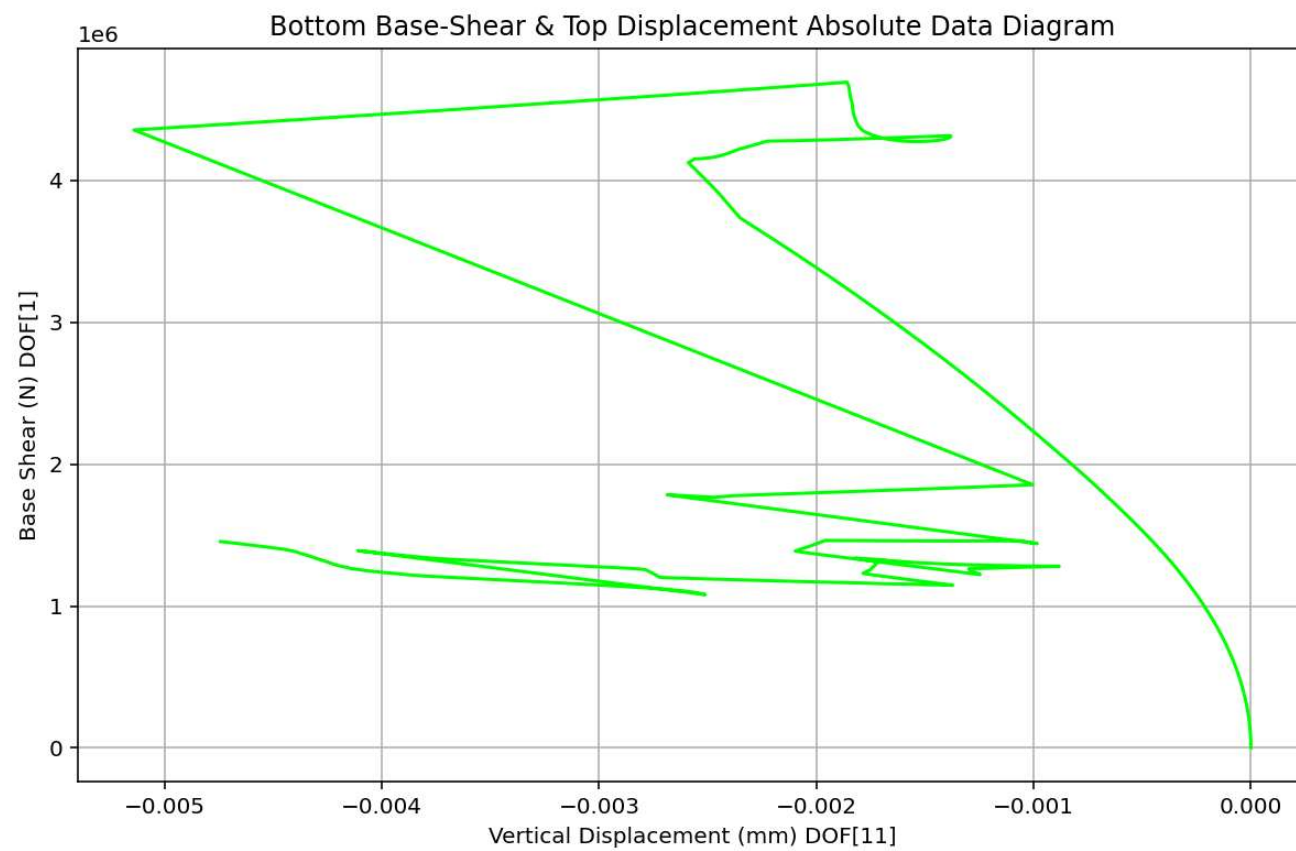
Figure 6. The effect of the number of iterations on the accuracy of the proposed algorithm. The results are averaged over 10 trials.

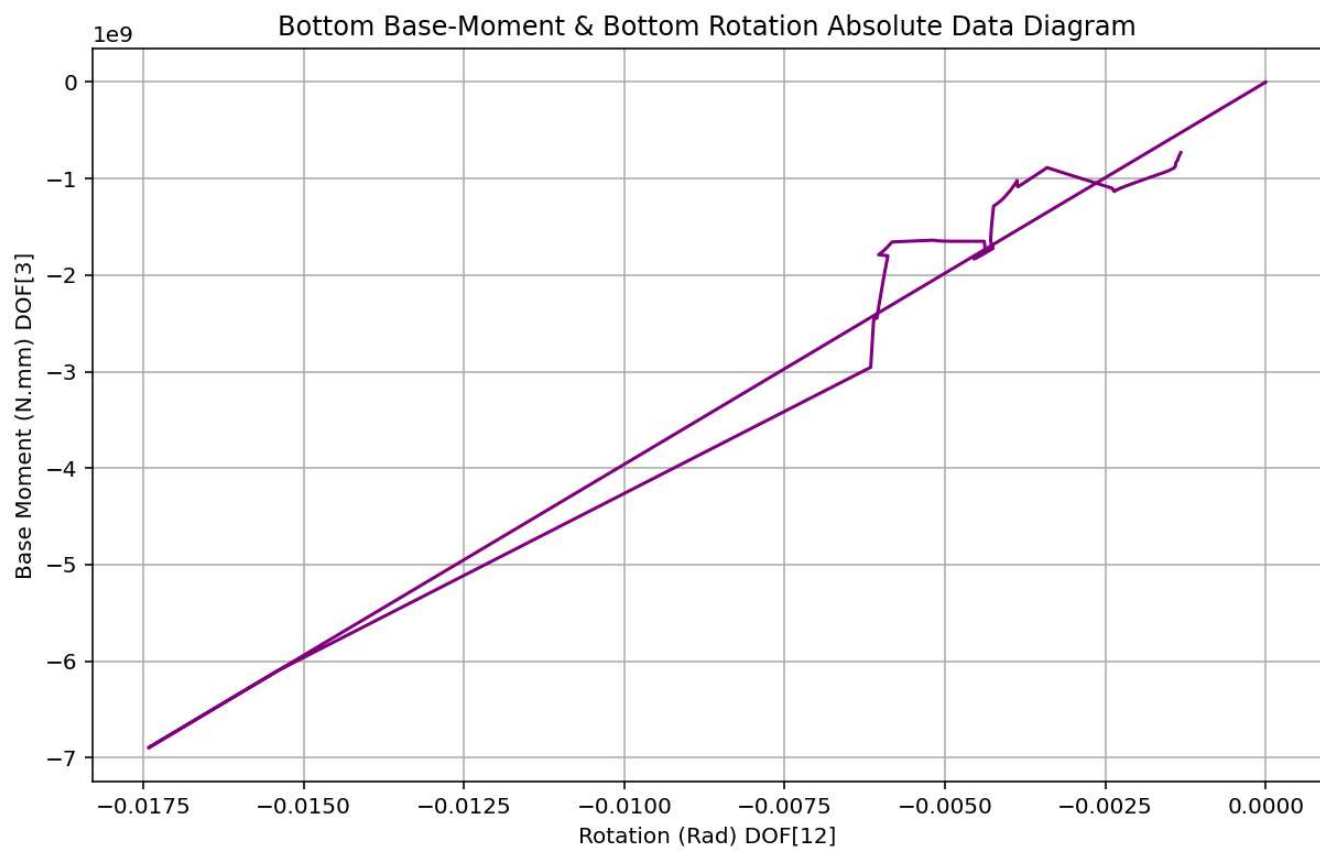
**PUSHOVER ANALYSIS OF
CONCRETE COLUMNS WITH
AXIAL AND ROTATIONAL
SPRINGS FOR MODELING BEAM
COLUMN JOINTS**

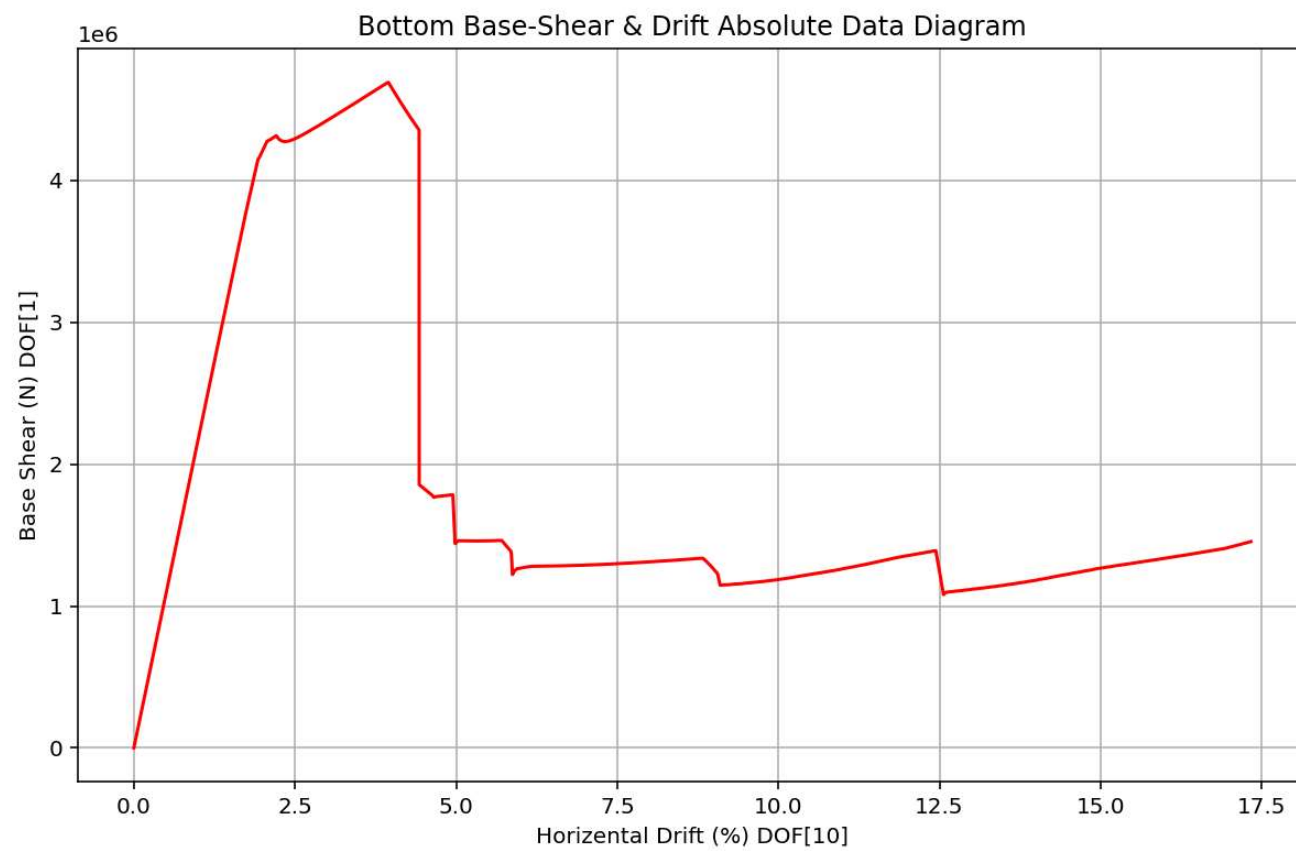




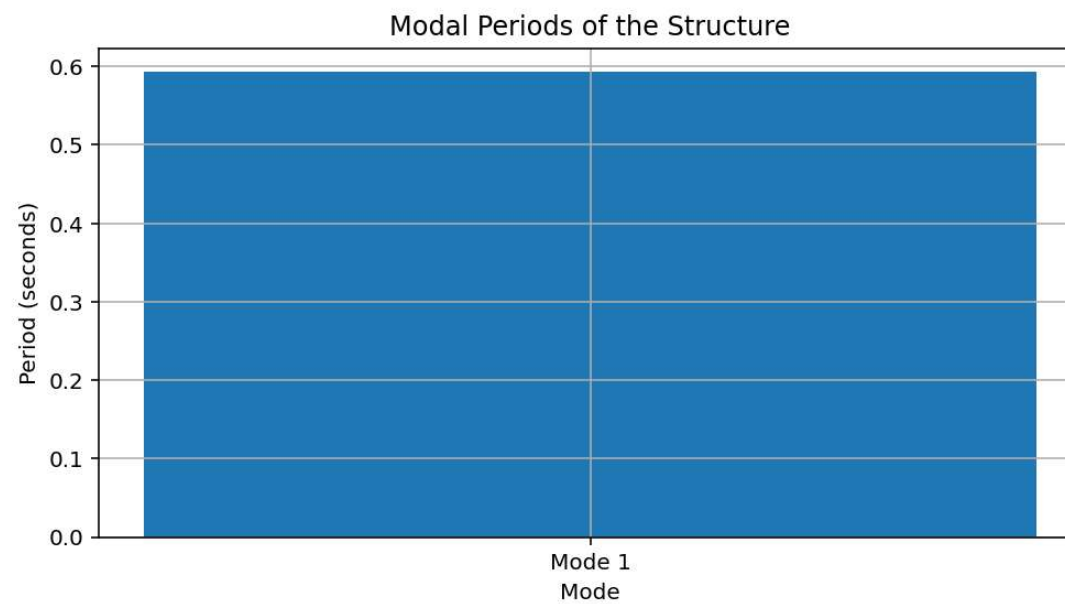






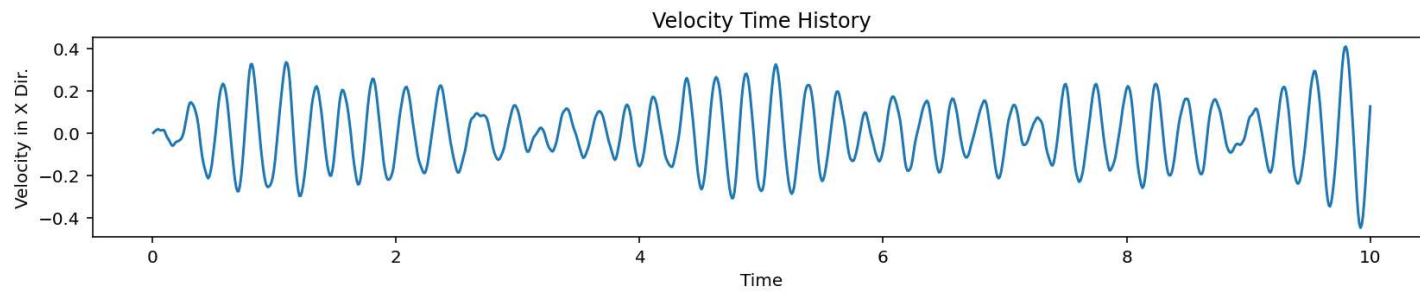
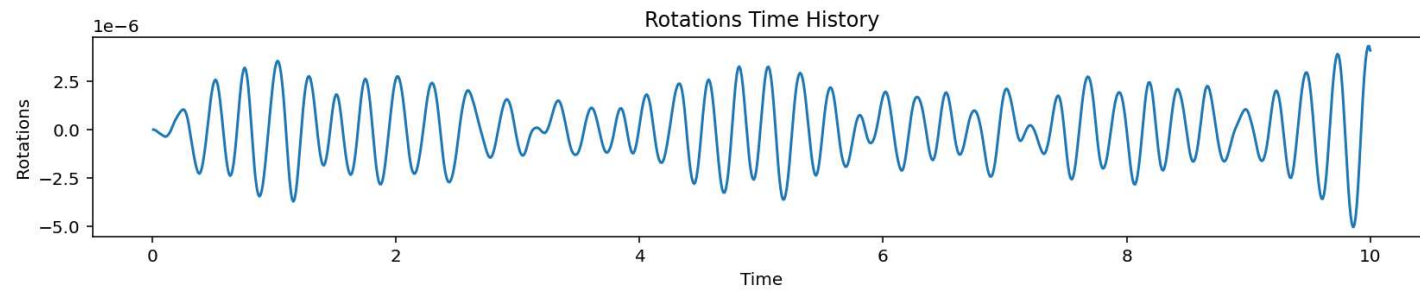
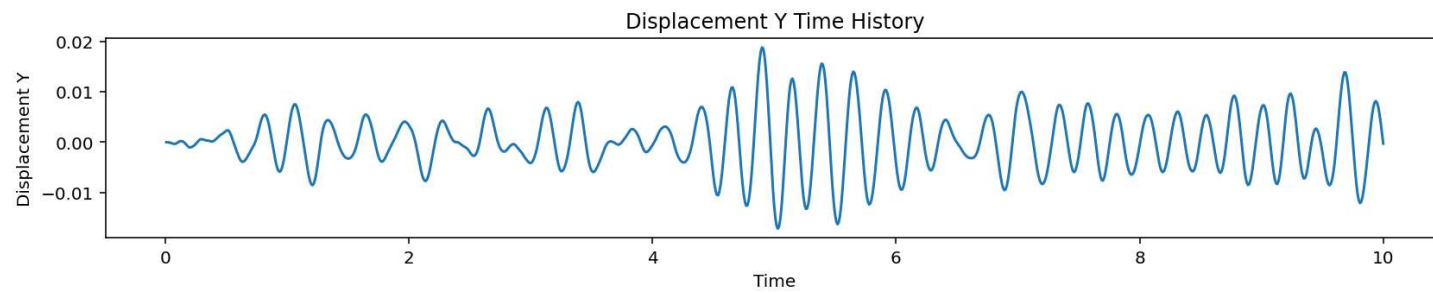
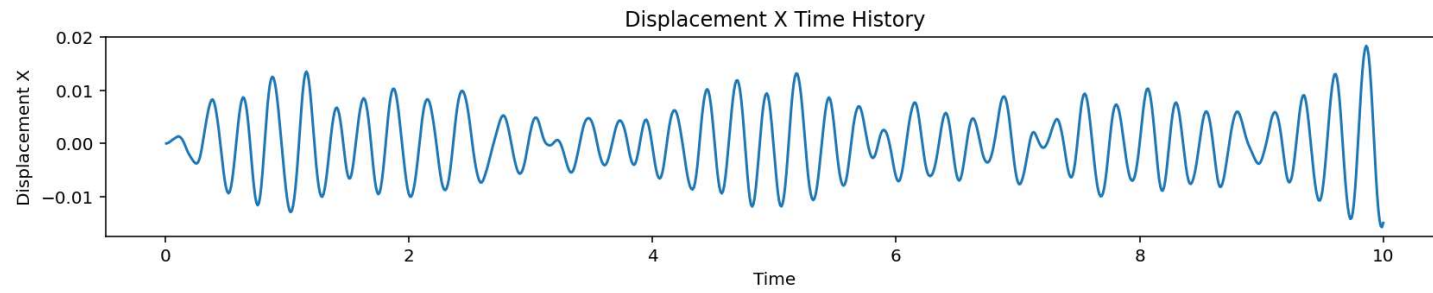


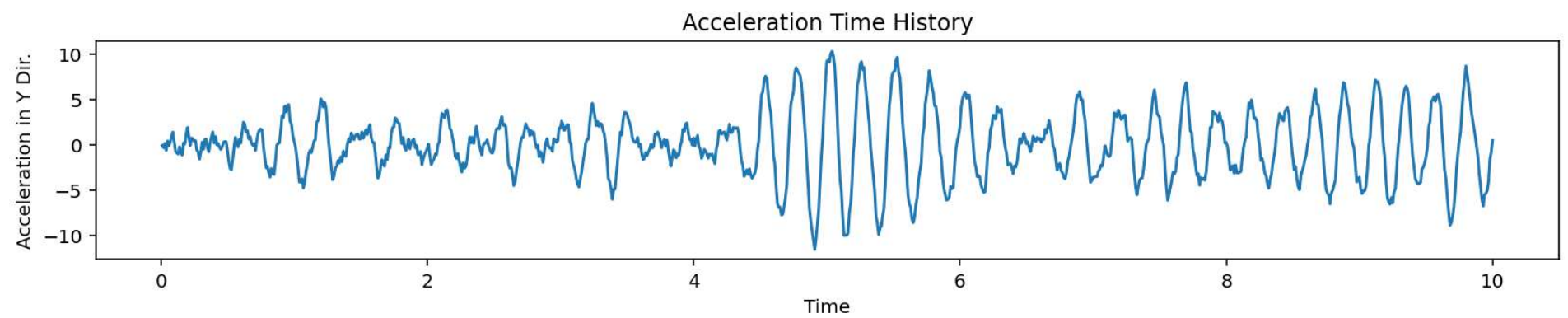
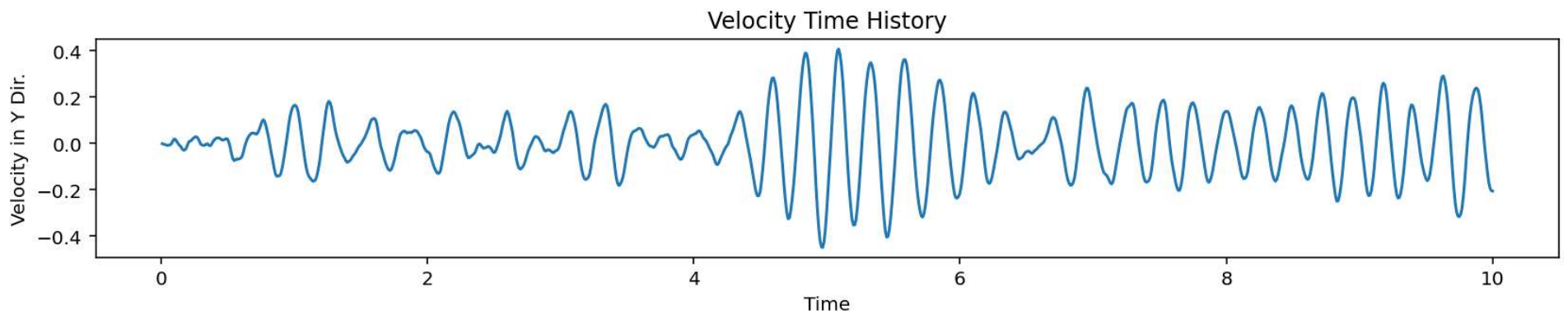
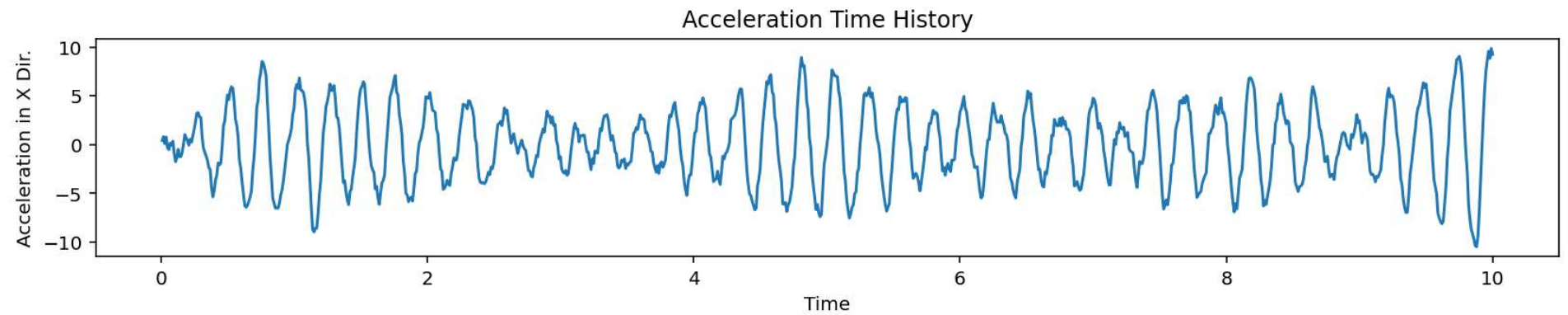
**DYNAMIC ANALYSIS OF
CONCRETE COLUMNS WITH
AXIAL AND ROTATIONAL
SPRINGS FOR MODELING BEAM
COLUMN JOINTS**



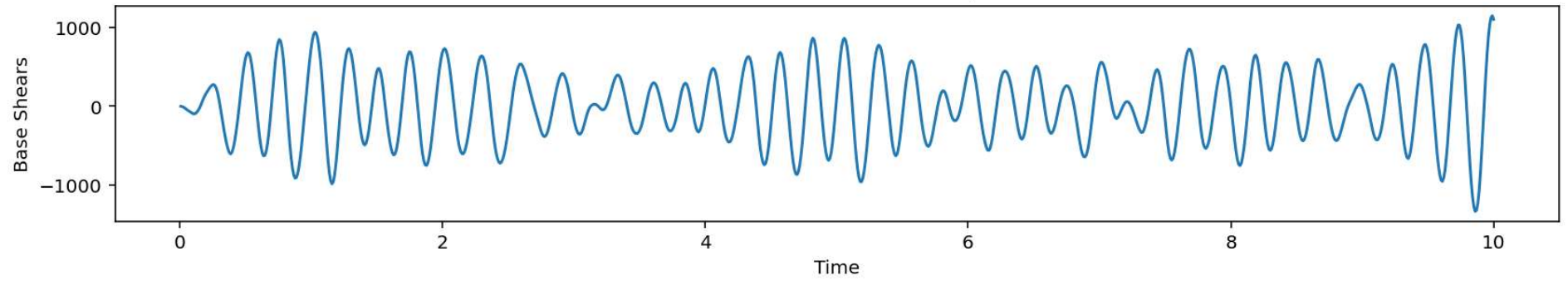
Period: 0.12475926338077073 (s)

Natural Frequency: 8.015436873396377 (Hz)

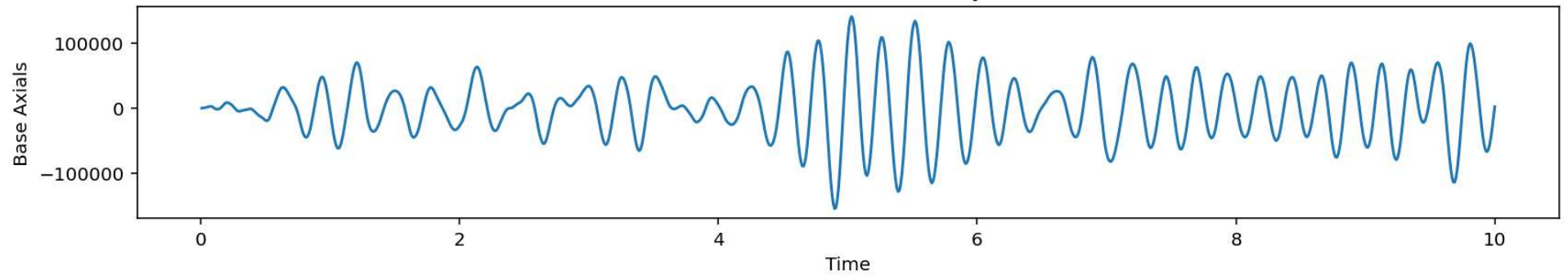




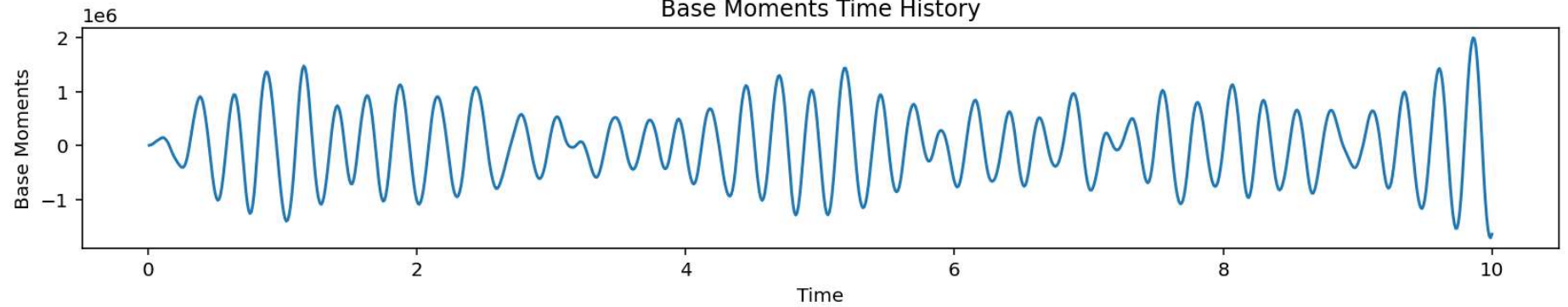
Base Shears Time History

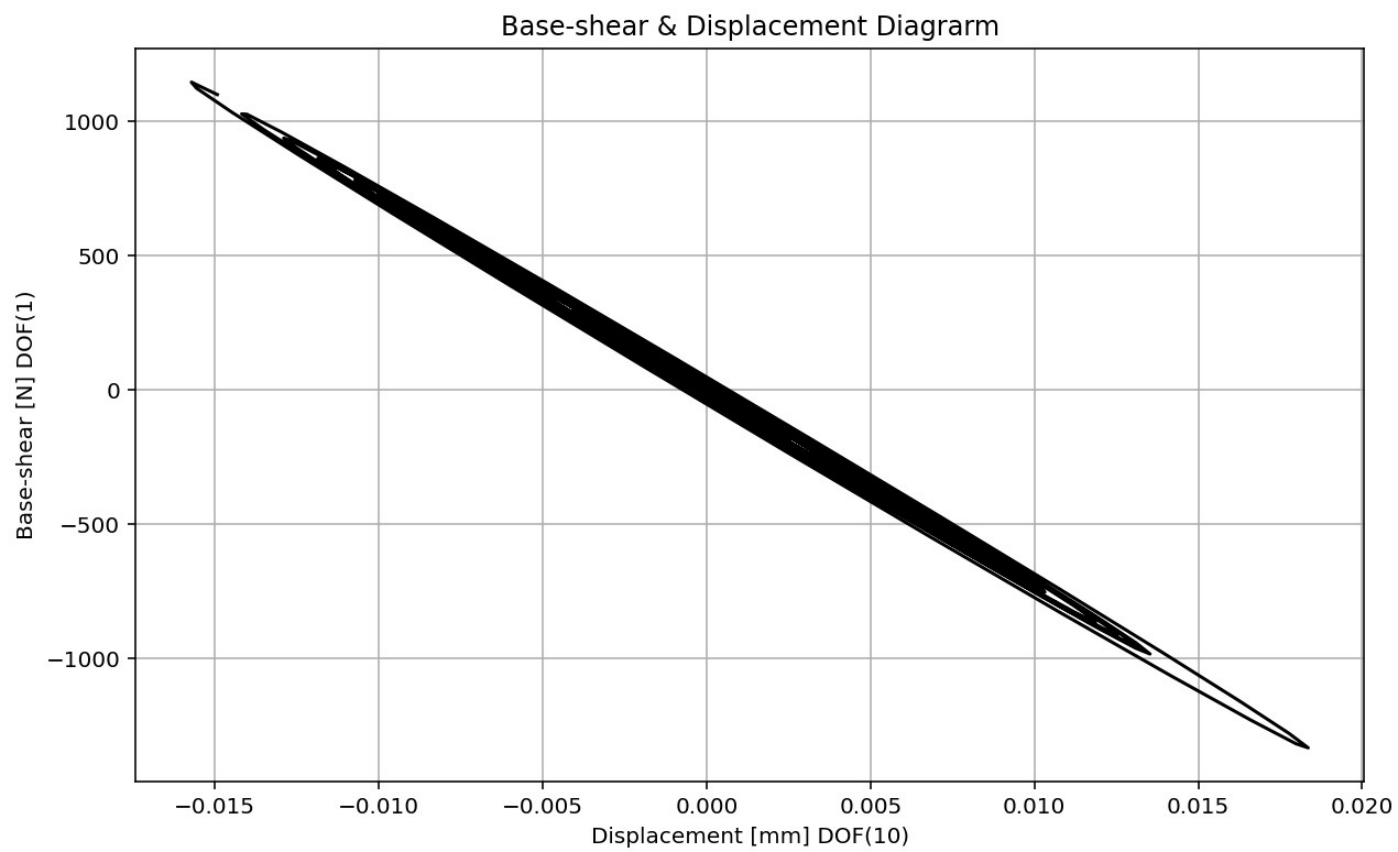


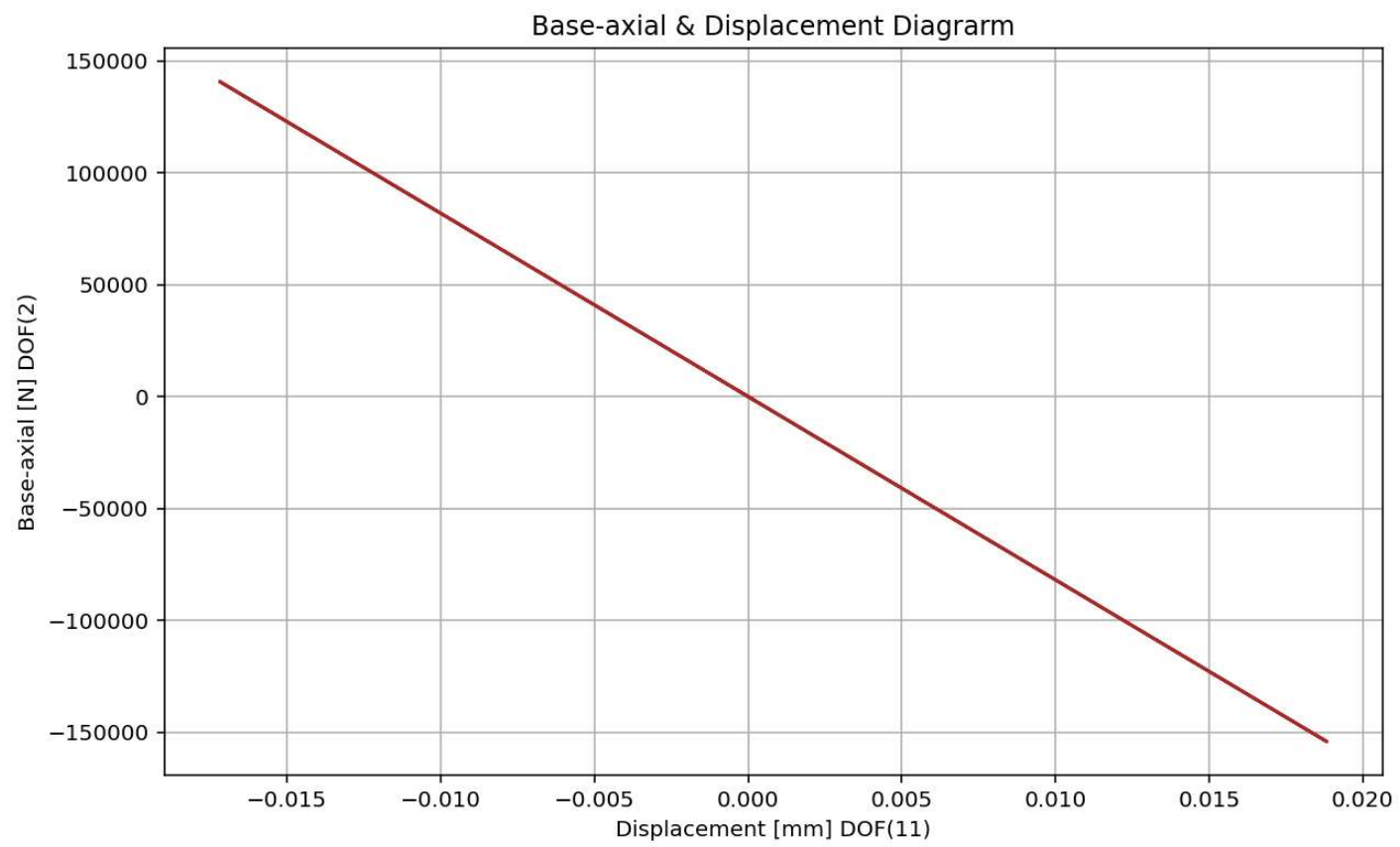
Base Axials Time History

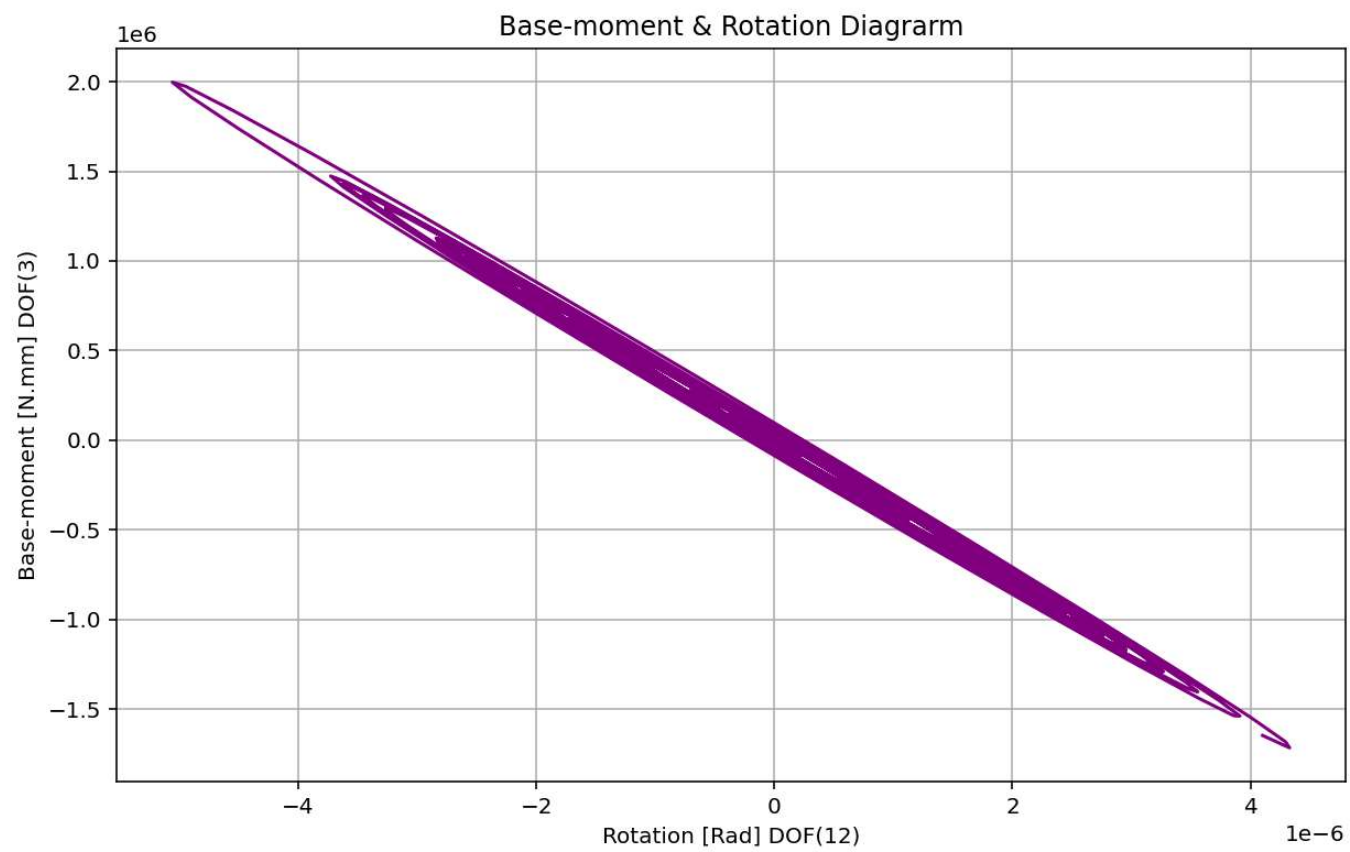


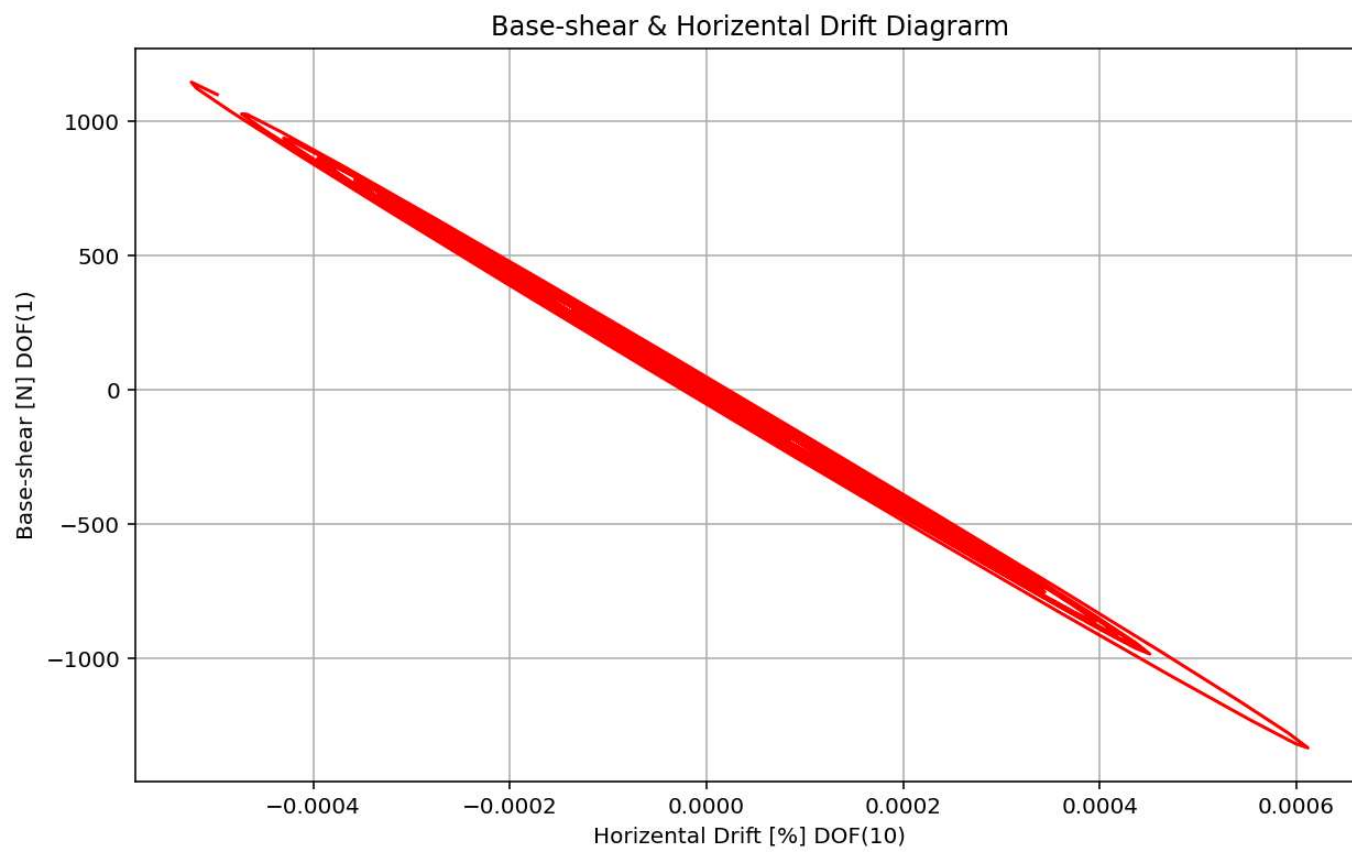
Base Moments Time History











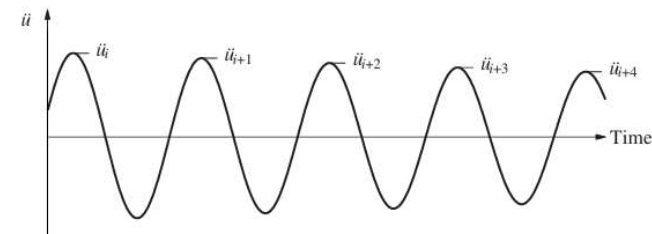
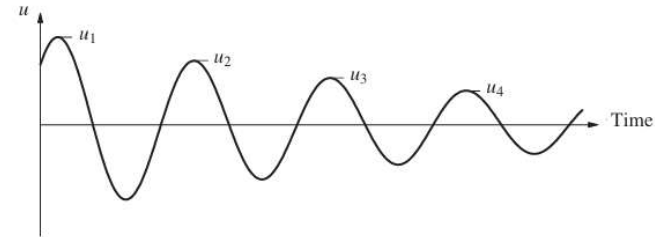
VISCOUSLY DAMPED FREE VIBRATION

$$m\ddot{u} + c\dot{u} + ku = 0$$

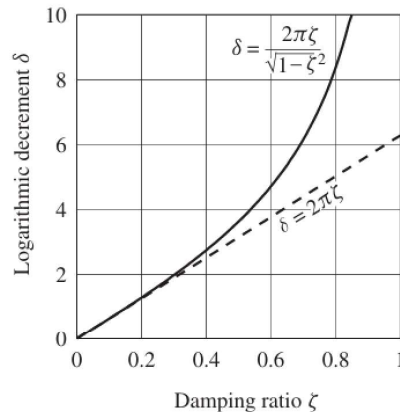
$$\ddot{u} + 2\zeta\omega_n\dot{u} + \omega_n^2 u = 0$$

$$\omega_n = \sqrt{k/m} \quad \zeta = \frac{c}{2m\omega_n} = \frac{c}{c_{cr}} \quad \omega_D = \omega_n \sqrt{1 - \zeta^2}$$

$$u(t) = e^{-\zeta\omega_n t} \left[u(0) \cos \omega_D t + \frac{\dot{u}(0) + \zeta\omega_n u(0)}{\omega_D} \sin \omega_D t \right]$$



Exact Damping Ratio: 1.06798624e-02



Decay of Motion

$$\delta = \ln \frac{u_i}{u_{i+1}} = 2\pi\zeta \quad (\text{APPROXIMATE RELATION})$$

$$\delta = \ln \frac{u_i}{u_{i+1}} = \frac{2\pi\zeta}{\sqrt{1-\zeta^2}} \quad (\text{EXACT RELATION})$$

EXACT AND APPROXIMATE RELATIONS BETWEEN LOGARITHMIC DECREMENT AND DAMPING RATIO