

>> IN THE NAME OF ALLAH, THE MOST GRACIOUS, THE MOST MERCIFUL <<

COMPREHENSIVE NONLINEAR SEISMIC ASSESSMENT OF STEEL A BEAM ELEMENT: AN OPENSEES FRAMEWORK FOR STATIC PUSHOVER, CYCLIC DEGRADATION, STATIC TIME-HISTORY AND DYNAMIC TIME-HISTORY ANALYSIS

THIS PROGRAM WRITTEN BY SALAR DELAVAR GHASHGHAEI (QASHQAI)

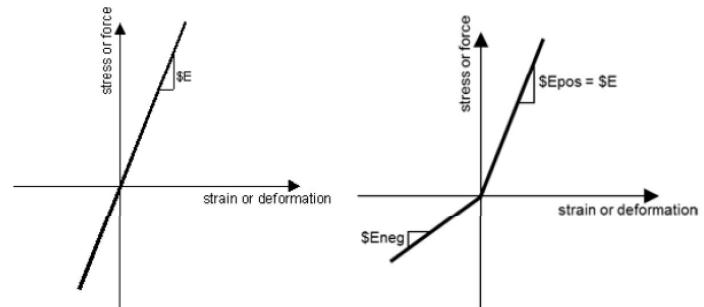
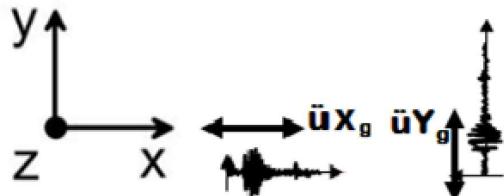
$$\text{Axial Ductility Damage Index} = \frac{\varepsilon_d - \varepsilon_y}{\varepsilon_u - \varepsilon_y}$$

$$\text{Structure Ductility Damage Index} = \frac{\Delta_d - \Delta_y}{\Delta_u - \Delta_y}$$

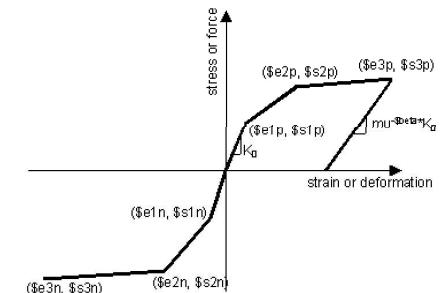


INCREMENTAL
DISPLACEMENT

Length

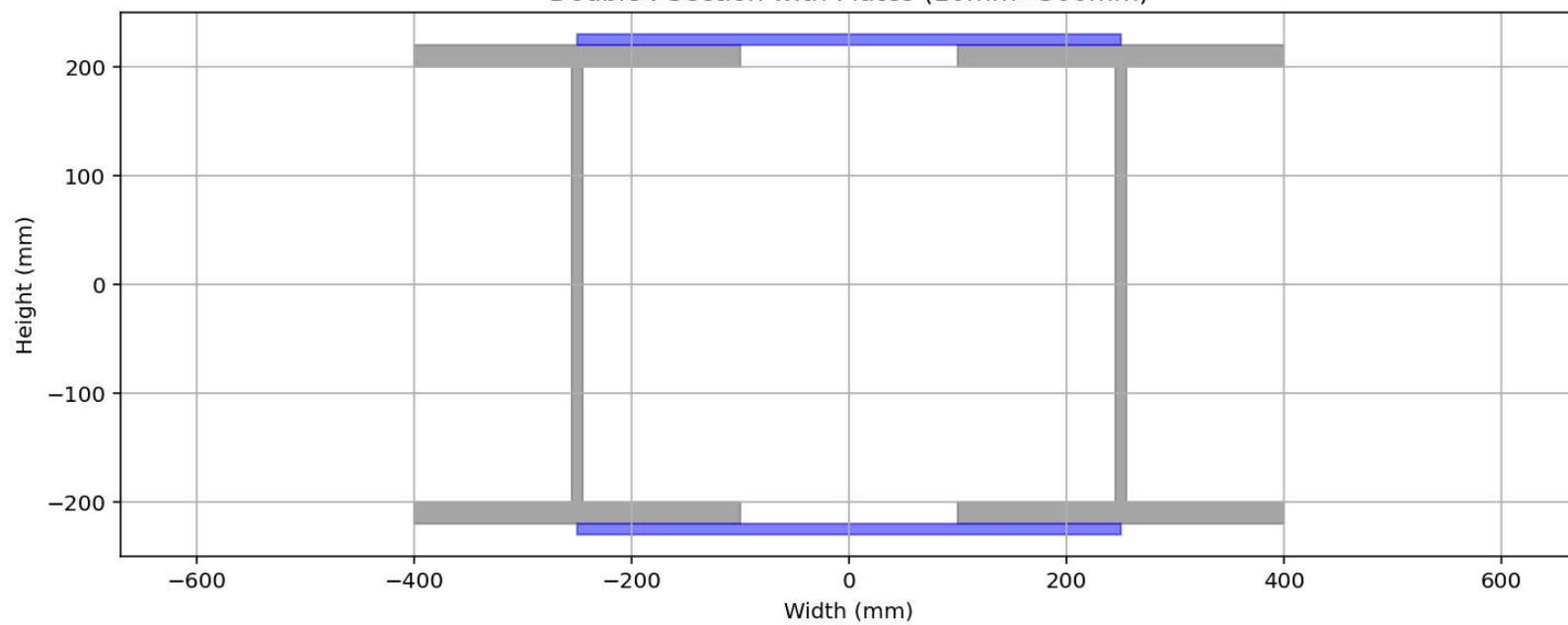


TRUSS ELEMENT ELASTIC MATERIAL



TRUSS ELEMENT INELASTIC MATERIAL

Double I-Section with Plates (10mm×500mm)



Spyder (Python 3.12)

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C:\Users\DELL\Desktop\OPENSEES_FILES\+TRUSS_ONE_E..E_ELEMENT_REALSE_M3\BEAM_ONE_ELEMENT_REALSE_M3.py

BEAM_ONE_ELEMENT_REALSE_M3.py

```

1 ##### >> IN THE NAME OF ALLAH, THE MOST GRACIOUS, THE MOST MERCIFUL <<
2 # COMPREHENSIVE NONLINEAR SEISMIC ASSESSMENT OF STEEL A BEAM ELEMENT : AN OPENSEES F
3 # STATIC PUSHOVER, CYCLIC DEGRADATION, STATIC TIME-HISTORY AND DYNAMIC TIME-HISTORY
4 #
5 #-----#
6 # ASSESSMENT OF DUCTILITY DAMAGE INDICES FOR STRUCTURAL ELEMENTS AND SYSTEMS AND E
7 # OF ENERGY DISSIPATION CAPACITY INDEX
8 #
9 #-----#
10 # THIS PROGRAM WRITTEN BY SALAR DELAVAR GHASHGHAEI (QASHQAI)
11 # EMAIL: salar.d.ghashghaei@gmail.com
12 """
13 Nonlinear Seismic Performance Assessment of a Beam Element:
14 An OpenSeesPy Framework for Material and Geometric Nonlinearity Under Static, Cyclic, and
15
16 This OpenSeesPy script performs rigorous nonlinear static and dynamic analysis of a Beam Element
17 for performance-based earthquake engineering. The 2D model incorporates both material nonlinearity
18 (elastic-perfectly plastic or hysteretic steel with strain hardening) and geometric nonlinearity to capture P-delta effects
19 and Large displacements—essential for collapse assessment.
20
21 The bridge spans 43m with 10-panel Warren configuration, assigning distinct cross-sectional
22 areas for chords and diagonals. Eigenvalue analysis tracks period elongation throughout
23 Loading, directly quantifying stiffness degradation and damage progression.
24
25 Eight analysis protocols are implemented:
26 (1) [PERIOD] : Structural Period
27 (2) [STATIC] : Gravity load analysis establishing dead load state
28 (3) [PUSHOVER] : Displacement-controlled pushover generating full capacity curves
29 and plastic mechanism identification
30 (4) [CYCLIC_DISPLACEMENT] : Symmetric cyclic displacement protocol capturing hysteresis,
31 pinching behavior, and energy dissipation degradation
32 (5) [STATIC_EXTERNAL_TIME-DEPENDENT_LOADING] : Static Analysis of External time-dependent
33 loading
34 (6) [DYNAMIC_EXTERNAL_TIME-DEPENDENT_LOADING] : Dynamic Analysis of External time-dependen

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Double I-Section with Plates (10mmx500mm)

Height (mm)

Width (mm)

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STATIC ANALYSIS

Spyder (Python 3.12)

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BEAM_ONE_ELEMENT_REALSE_M3.py

```
1009 AREA = 2*2040.0      # [mm^2] Section Area for diagonal elements - 2 x UNP140
1010 TOTAL_MASS = 0.0     # [kg] Total Mass of Structure
1011 #%%-----#
1012 # PERIOD ANALYSIS
1013 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1014 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1015 MAT_TYPE = 'INELASTIC'      # 'ELASTIC' OR 'INELASTIC'
1016 ANAL_TYPE = 'PERIOD'
1017
1018 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)
1019 (PERIOD_MIN_X, PERIOD_MAX_X) = DATA
1020 print('Structure First Period: ', PERIOD_MIN_X)
1021 print('Structure Second Period: ', PERIOD_MAX_X)
1022
1023 S01.PLOT_2D_FRAME(deformed_scale=1.0)
1024 #%%-----#
1025 # STATIC ANALYSIS
1026 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1027 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1028 MAT_TYPE = 'INELASTIC'      # 'ELASTIC' OR 'INELASTIC'
1029 ANAL_TYPE = 'STATIC'
1030
1031 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)
1032 (reaction, disp_mid,
1033 ele_force, ele_stress, ele_strain, ele_di,
1034 node_displacementsX, node_displacementsY,
1035 dispX, dispY) = DATA
1036
1037 S01.PLOT_2D_FRAME(deformed_scale=1.0)
1038 #%%-----#
1039 # PUSHOVER ANALYSIS (STATIC TIME-HISTORY ANALYSIS)
1040 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1041 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1042 MAT_TYPE = 'INELASTIC'      # 'ELASTIC' OR 'INELASTIC'
```

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19 %

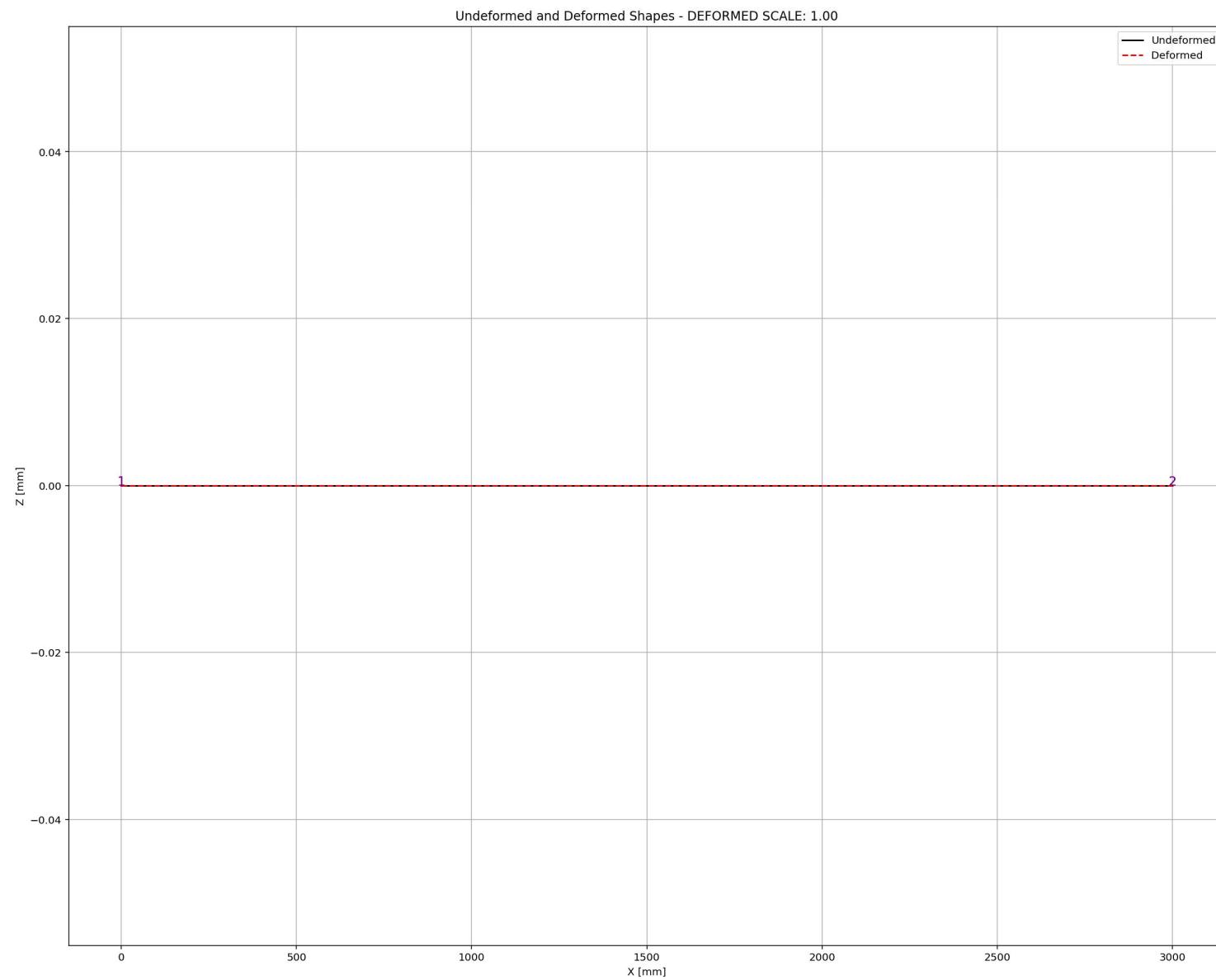
Undeformed and Deformed Shapes - DEFORMED SCALE: 1.00

2.00
1.00
0.00
-1.00
-2.00

8 1000 2000 2200 2400 2600 2800 3000

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PUSHOVER ANALYSIS

Spyder (Python 3.12)

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BEAM_ONE_ELEMENT_REALSE_M3.py

```
1038 #%%-----  
1039 # PUSHOVER ANALYSIS (STATIC TIME-HISTORY ANALYSIS)  
1040 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY  
1041 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES  
1042 MAT_TYPE = 'INELASTIC'            # 'ELASTIC' OR 'INELASTIC'  
1043 ANAL_TYPE = 'PUSHOVER'  
1044  
1045 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)  
(reaction_PUSH, disp_mid_PUSH,  
ele_force_PUSH, ele_stress_PUSH, ele_strain_PUSH, ele_di_PUSH,  
node_displacementsX_PUSH, node_displacementsY_PUSH,  
dispX_PUSH, dispY_PUSH,  
PERIOD_MIN_PUSH, PERIOD_MAX_PUSH,  
STRESSb_PUSH, STRAINb_PUSH, STRESSt_PUSH, STRAINT_PUSH, CURVATURE_PUSH) = DATA  
1052  
1053  
1054 XDATA = disp_mid_PUSH  
1055 YDATA = reaction_PUSH  
1056 XLABEL = 'Displacement in Middle Span [mm]'  
1057 YLABEL = 'Base Reaction [N]'  
1058 TITLE = 'Base Reaction and Displacement of Structure During Pushover Analysis'  
1059 COLOR = 'black'  
1060 SEMILOGY = False  
1061 PLOT(XDATA, YDATA, TITLE, XLABEL, YLABEL, COLOR, SEMILOGY)  
1062  
1063 DATA = S07.BILINEAR_CURVE(np.abs(disp_mid_PUSH), np.abs(reaction_PUSH), SLOPE_NODE=10)  
(X_PUSH, Y_PUSH, Elastic_ST, Plastic_ST, Tangent_ST, Ductility_Rito, Over_Strength_Factor)  
1065  
1066  
# PLOT STRUCTURAL PERIOD DURING THE ANALYSIS  
1067 plt.figure(0, figsize=(12, 8))  
1068 plt.plot(disp_mid_PUSH, PERIOD_MIN_PUSH, linewidth=3)  
1069 plt.plot(disp_mid_PUSH, PERIOD_MAX_PUSH, linewidth=3)  
1070 plt.title('Period of Structure During Pushover Analysis')  
1071 plt.ylabel('Structural Period [s]')
```

...ENSEES_FILES\+TRUSS_ONE_ELEMENT\BEAM_ONE_ELEMENT_REALSE_M3

31 %

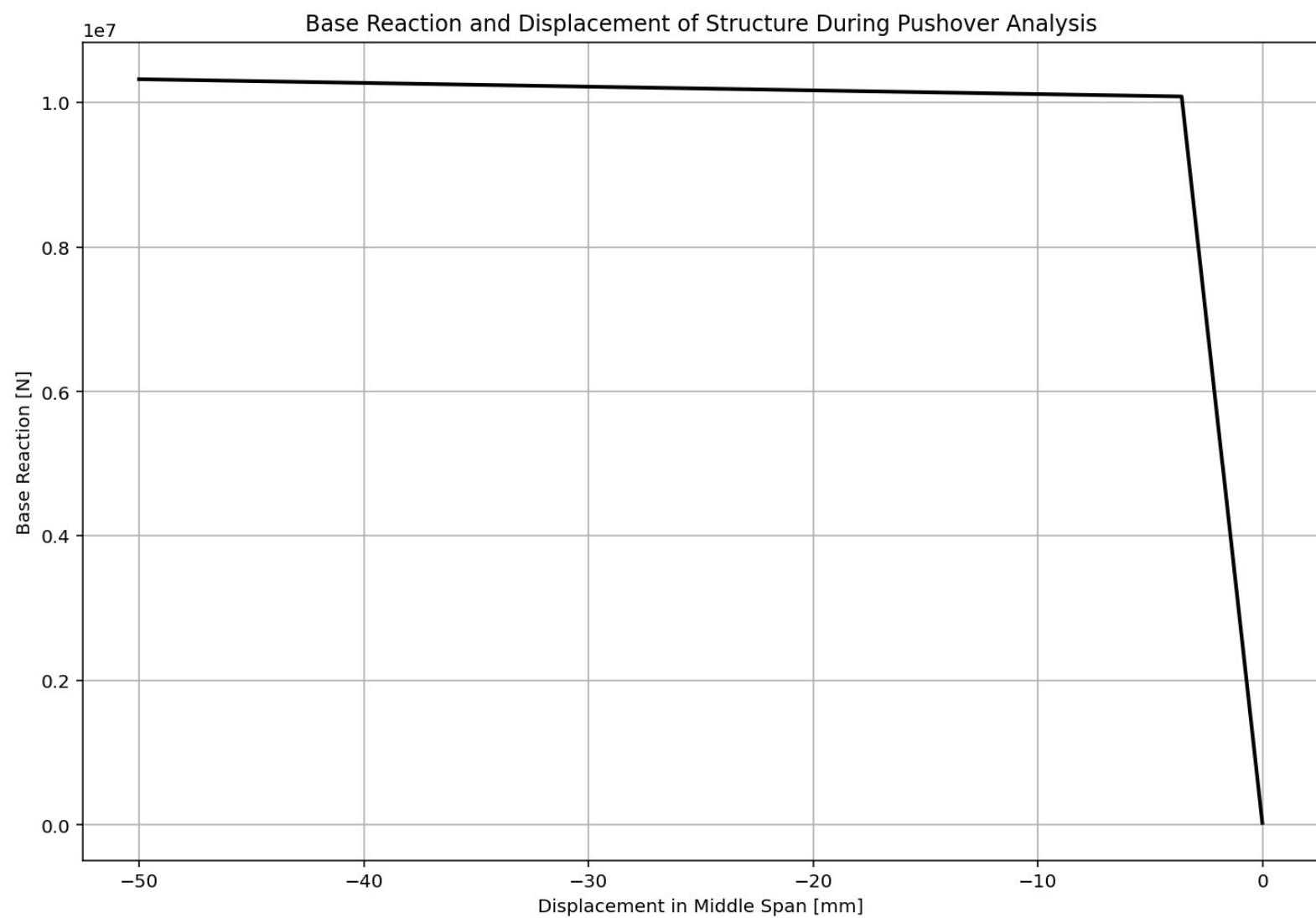
Base Reaction and Displacement of Structure During Pushover Analysis

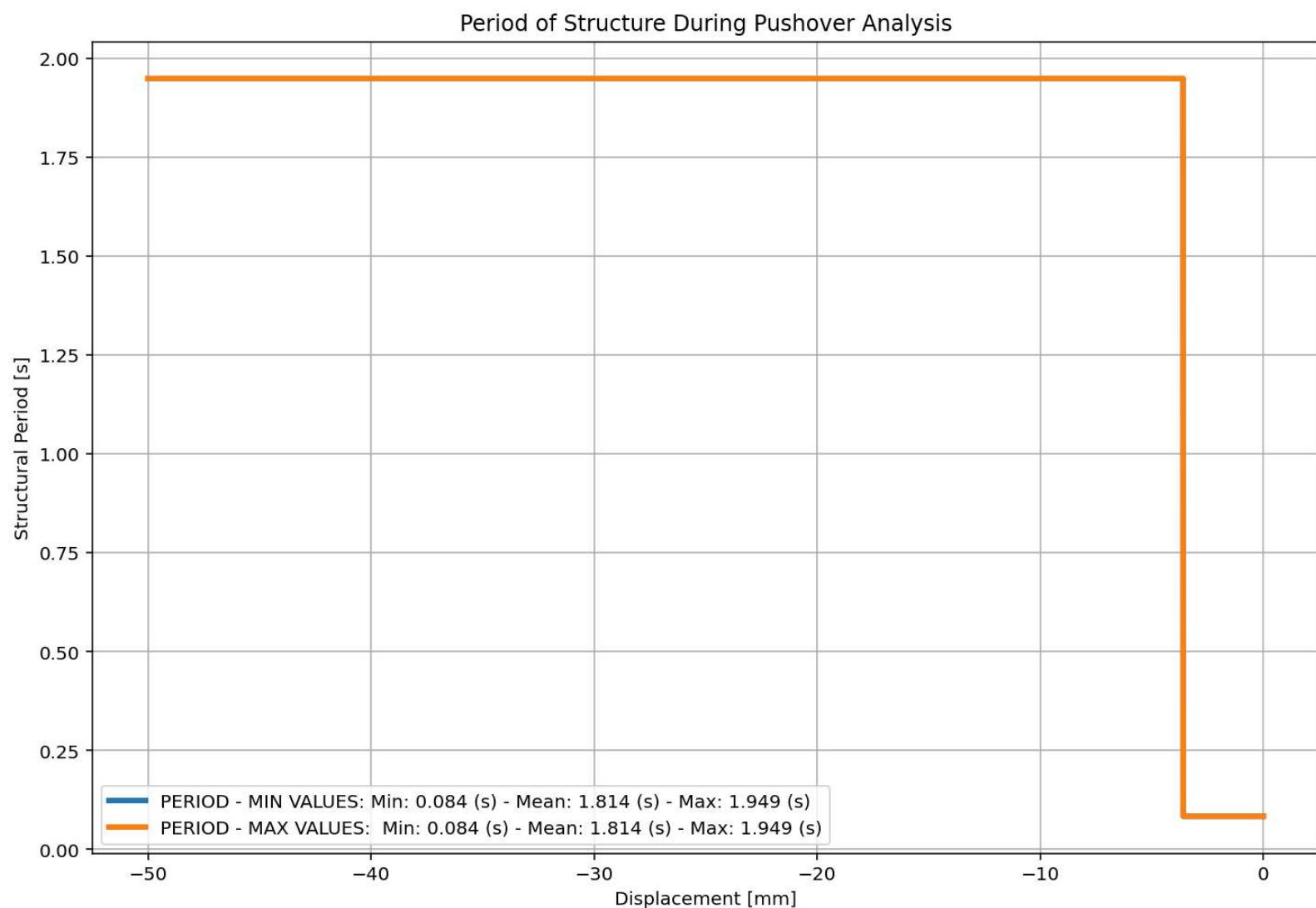
Base Reaction [N]

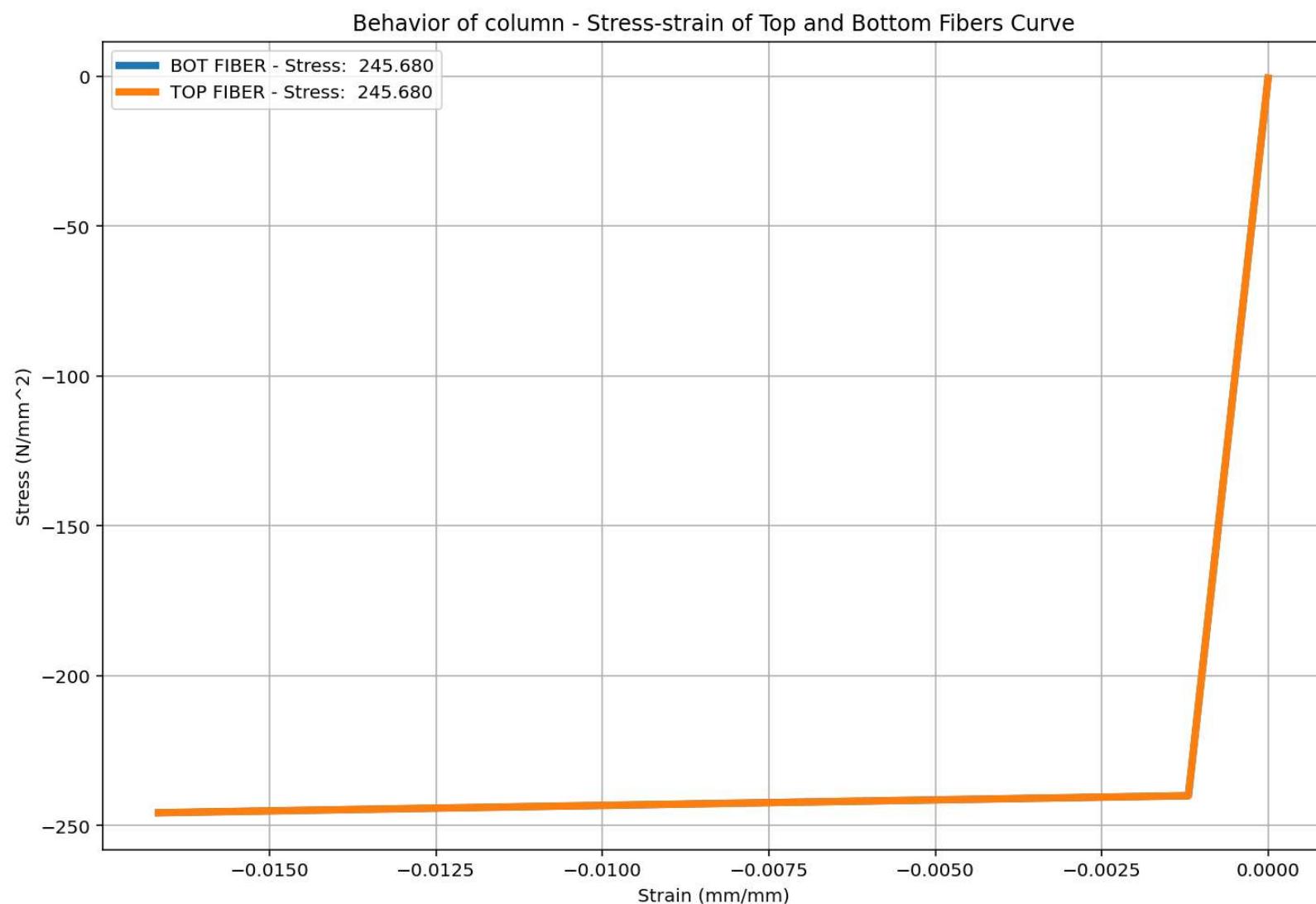
Displacement in Middle Span [mm]

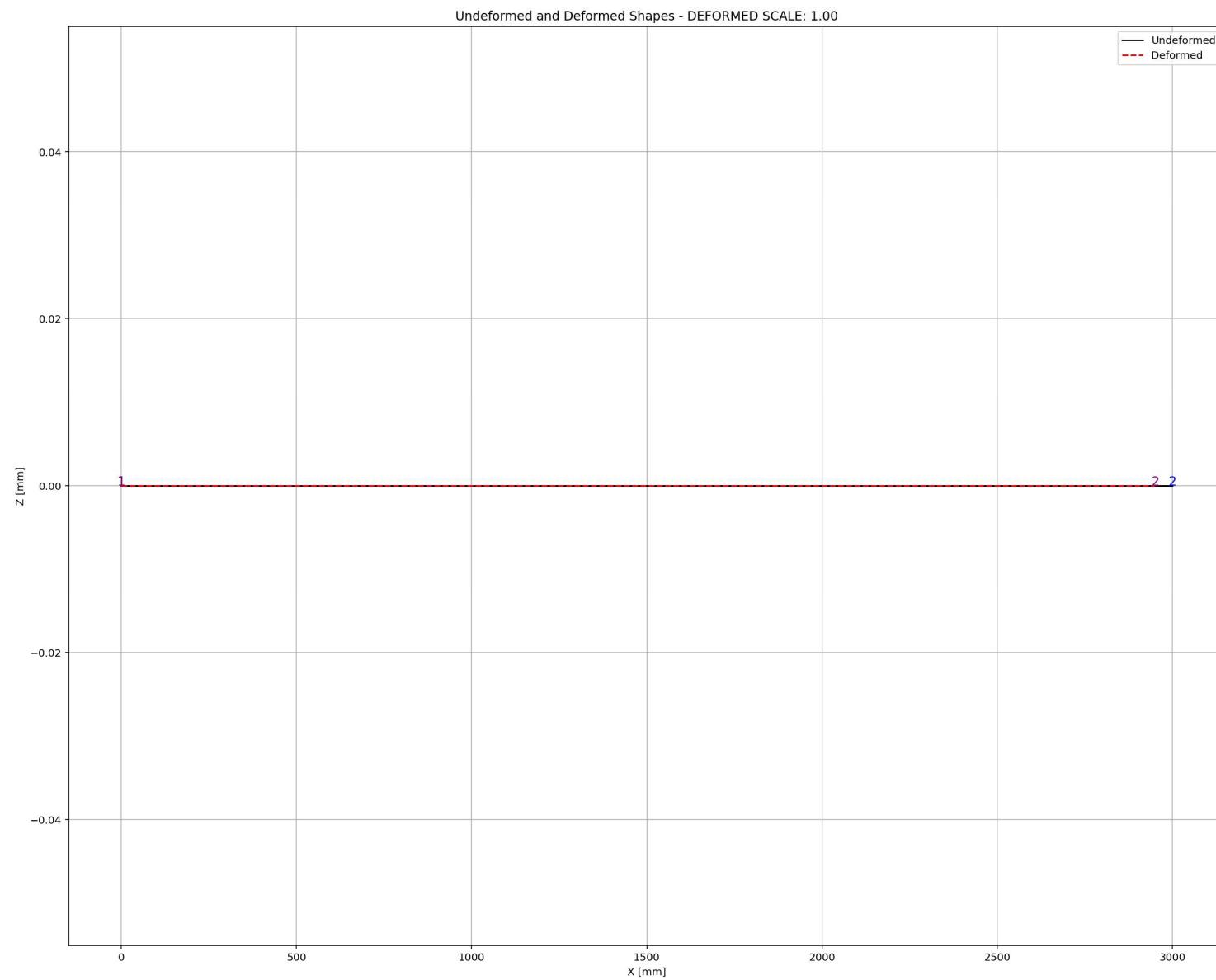
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CYCLIC DISPLACEMENT ANALYSIS

Spyder (Python 3.12)

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BEAM_ONE_ELEMENT_REALSE_M3.py X

```

1093 # CYCLIC DISPLACEMENT ANALYSIS (STATIC TIME-HISTORY ANALYSIS)
1094 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1095 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1096 MAT_TYPE = 'INELASTIC'            # 'ELASTIC' OR 'INELASTIC'
1097 ANAL_TYPE = 'CYCLIC_DISPLACEMENT'
1098
1099 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)
1100 (reaction_CP, disp_mid_CP,
1101  ele_force_CP, ele_stress_CP, ele_strain_CP, ele_di_CP,
1102  node_displacementsX_CP, node_displacementsY_CP,
1103  dispX_CP, dispY_CP,
1104  PERIOD_MIN_CP, PERIOD_MAX_CP,
1105  STRESSb_CP, STRAINb_CP, STRESSst_CP, STRAINT_CP, CURVATURE_CP) = DATA
1106
1107
1108 XDATA = disp_mid_CP
1109 YDATA = reaction_CP
1110 XLABEL = 'Displacement in Middle Span [mm]'
1111 YLABEL = 'Base Reaction [N]'
1112 TITLE = 'Base Reaction and Displacement of Structure During Cyclic-Displacement Analysis'
1113 COLOR = 'black'
1114 SEMILOGY = False
1115 PLOT(XDATA, YDATA, TITLE, XLABEL, YLABEL, COLOR, SEMILOGY)
1116
1117 # PLOT STRUCTURAL PERIOD DURING THE ANALYSIS
1118 plt.figure(0, figsize=(12, 8))
1119 plt.plot(disp_mid_CP, PERIOD_MIN_CP, linewidth=3)
1120 plt.plot(disp_mid_CP, PERIOD_MAX_CP, linewidth=3)
1121 plt.title('Period of Structure During Cyclic Displacement Analysis')
1122 plt.ylabel('Structural Period [s]')
1123 plt.xlabel('Displacement [mm]')
1124 #plt.semilogy()
1125 plt.grid()
1126 plt.legend([f'PERIOD - MIN VALUES: Min: {np.min(PERIOD_MIN_CP):.3f} (s) - Mean: {np.mean(P

```

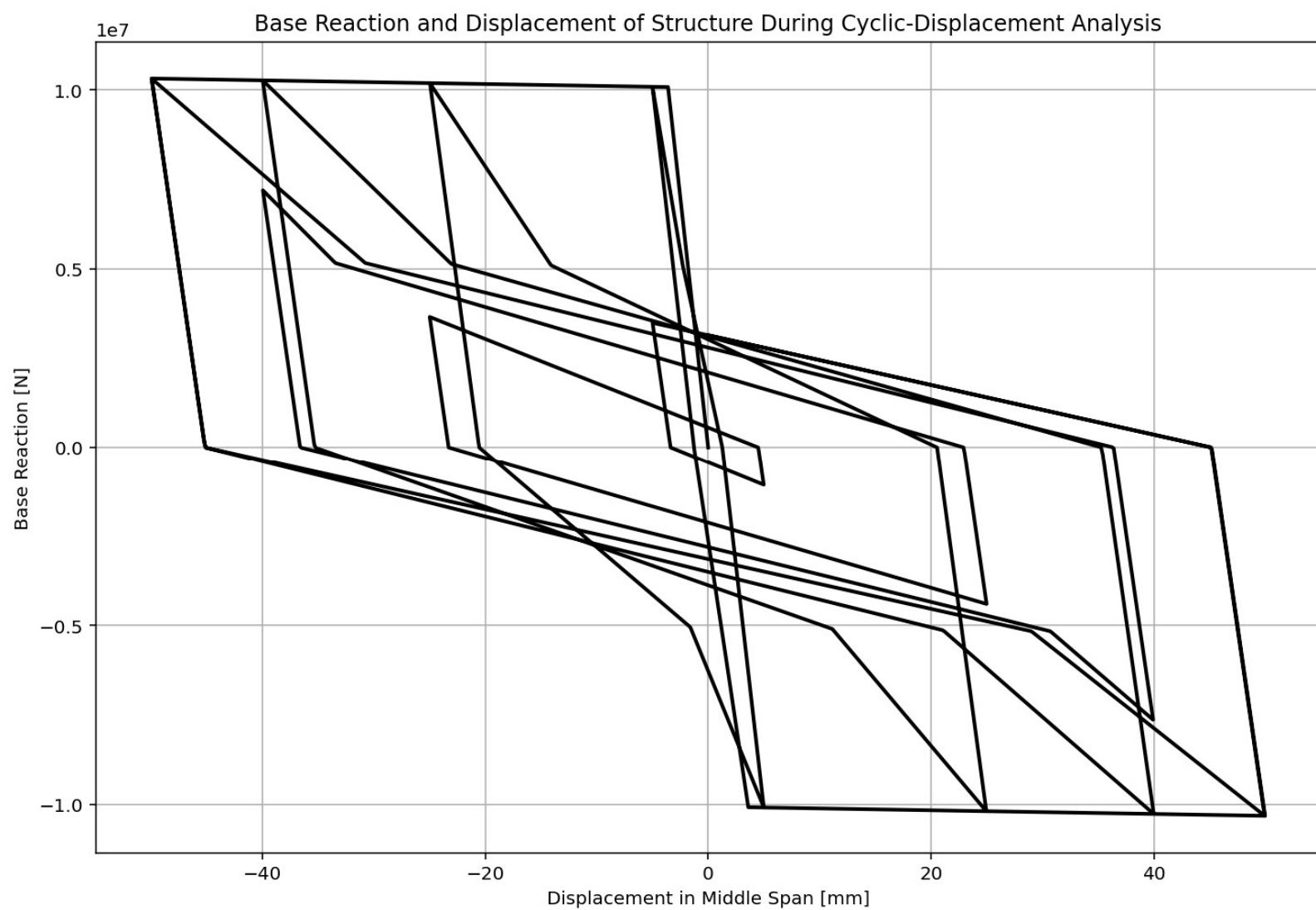
...ENSEES_FILES\+TRUSS_ONE_ELEMENT\BEAM_ONE_ELEMENT_REALSE_M3

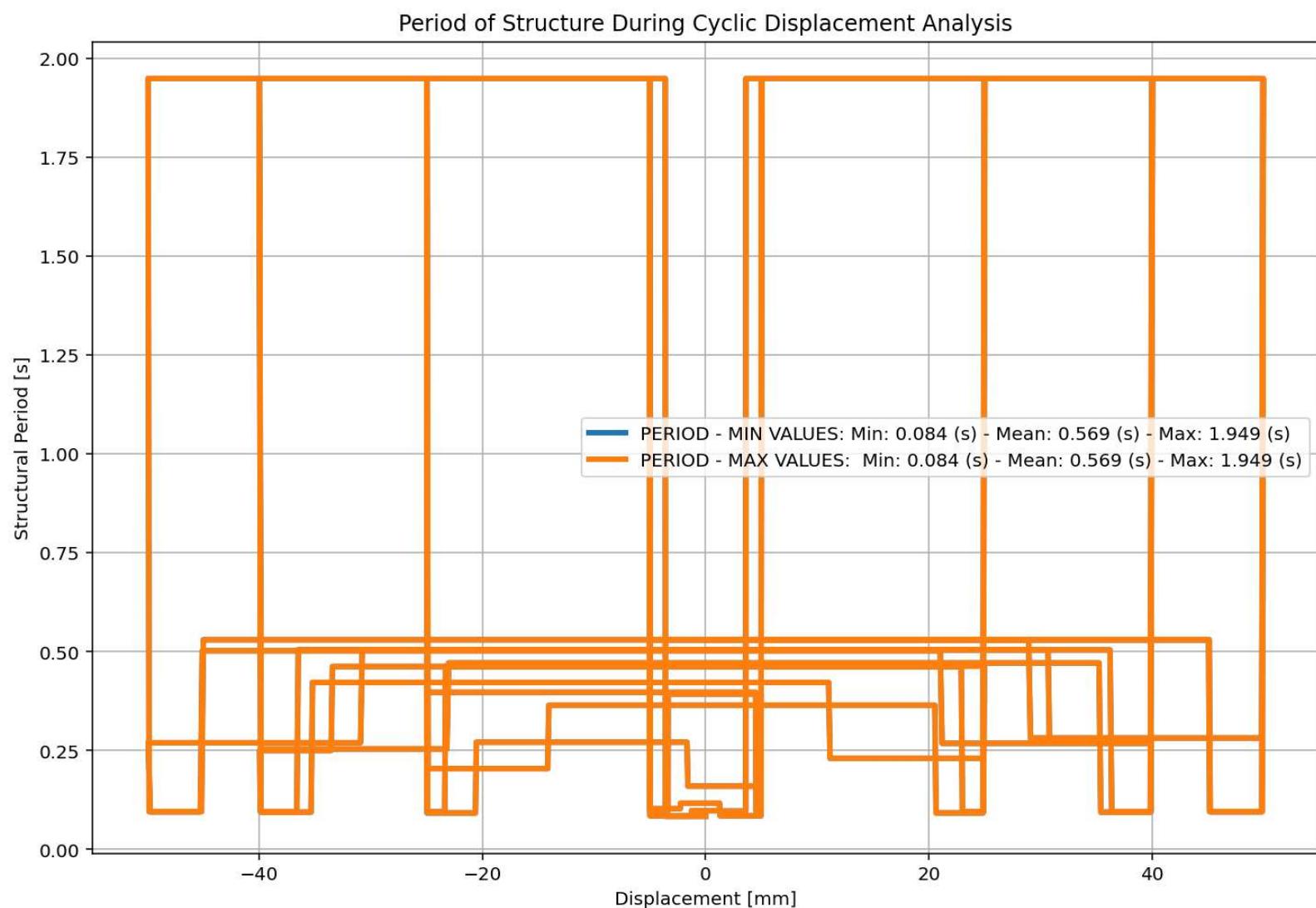
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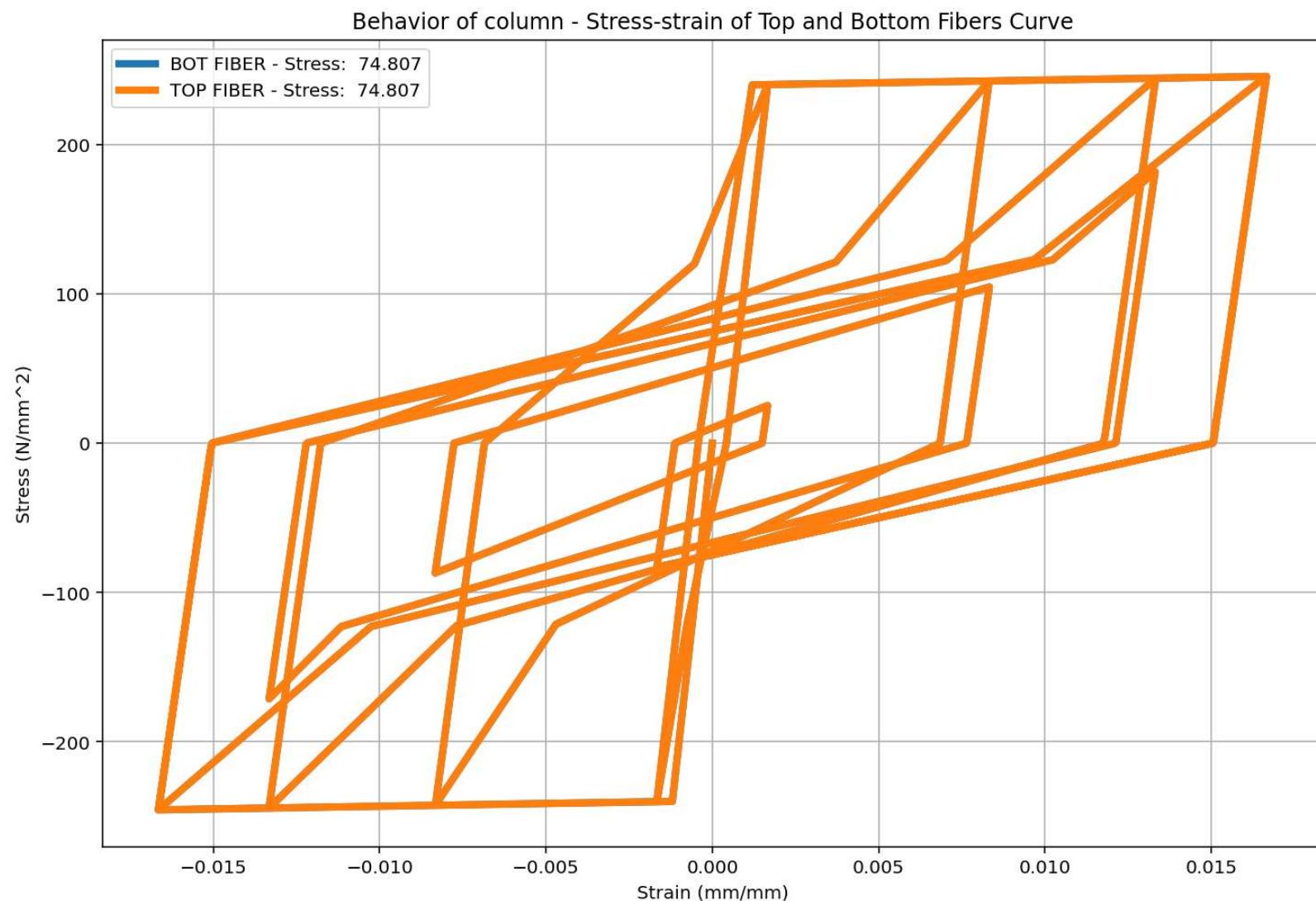
Base Reaction and Displacement of Structure During Cyclic-Displacement Analysis

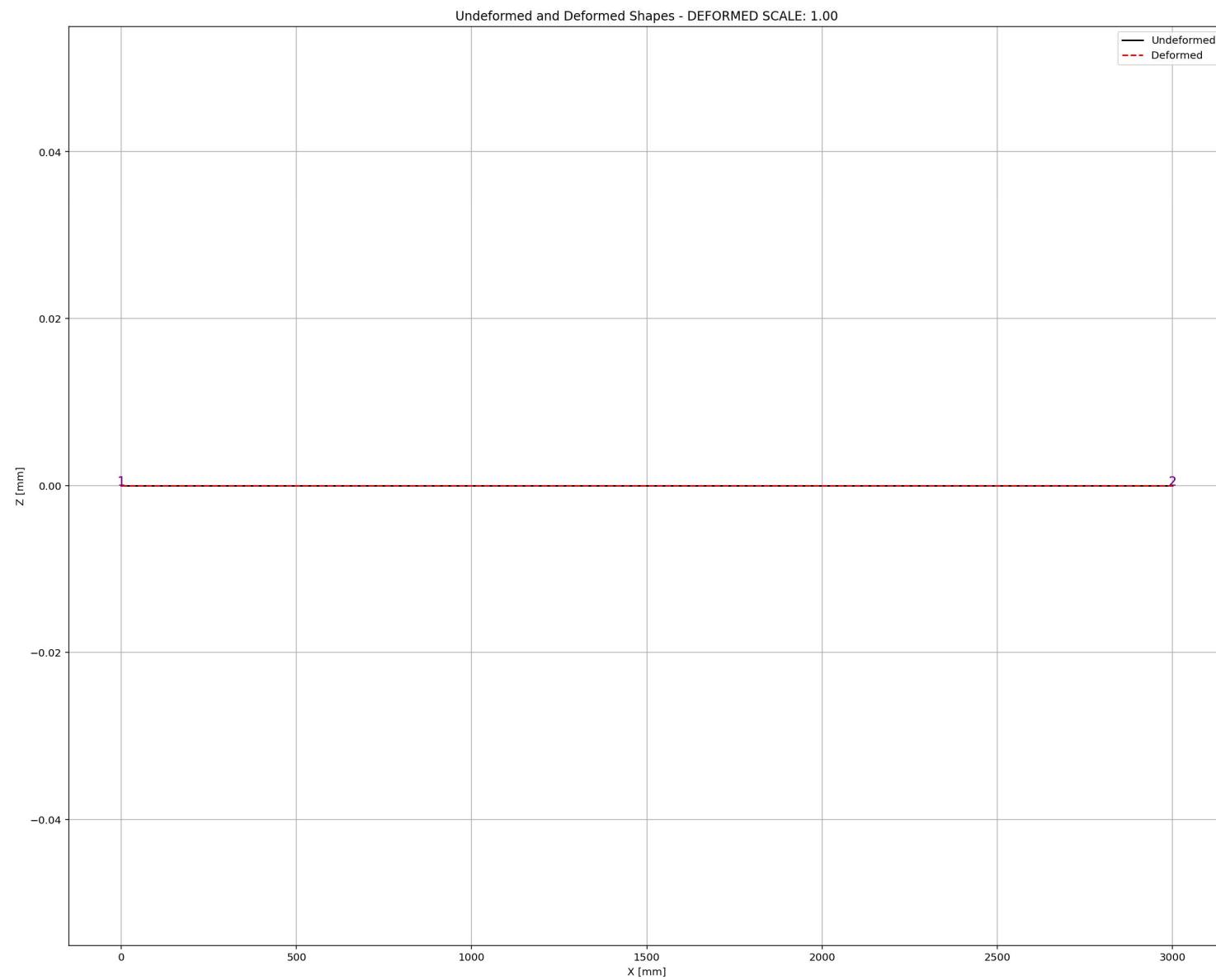
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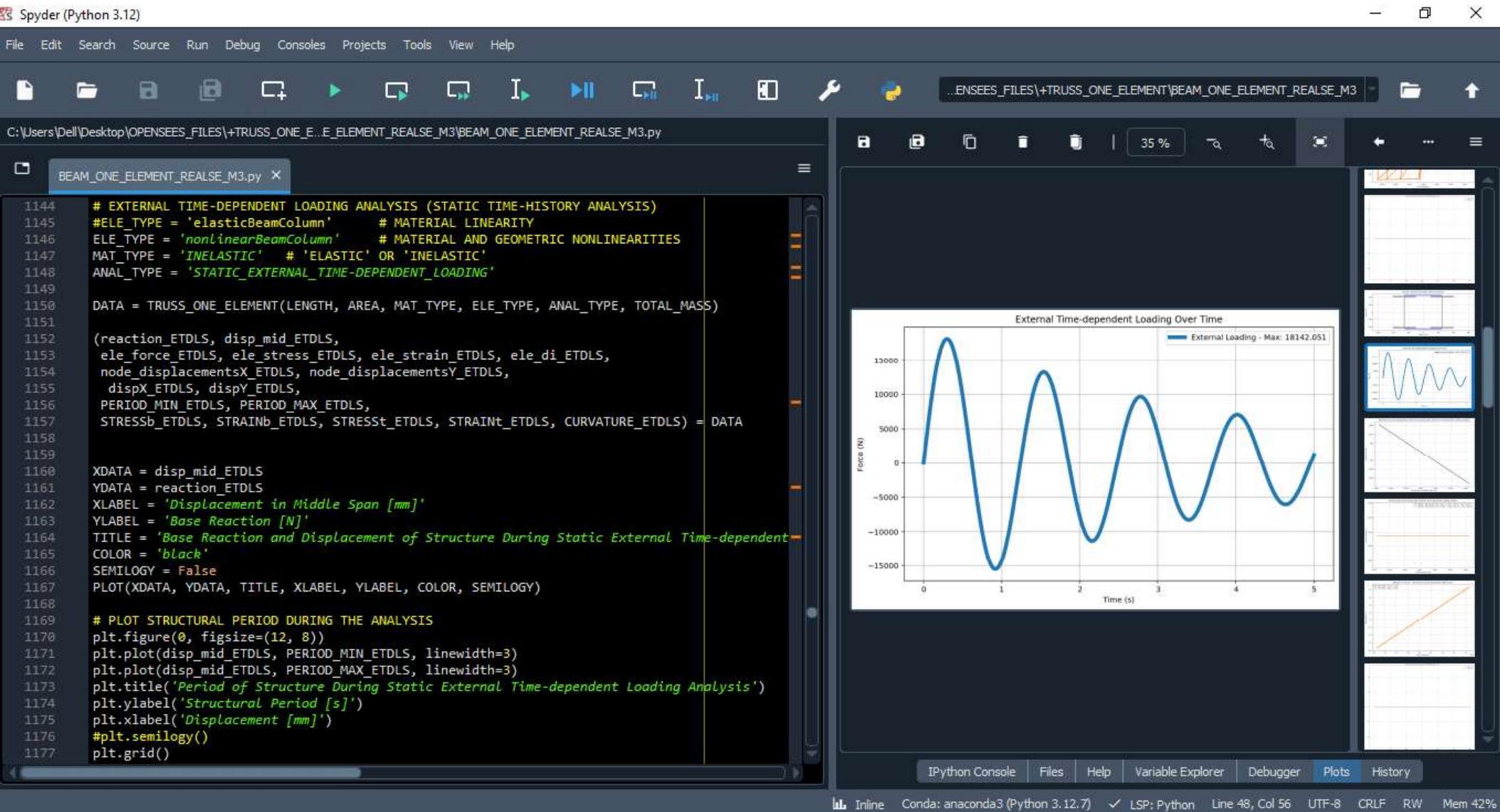




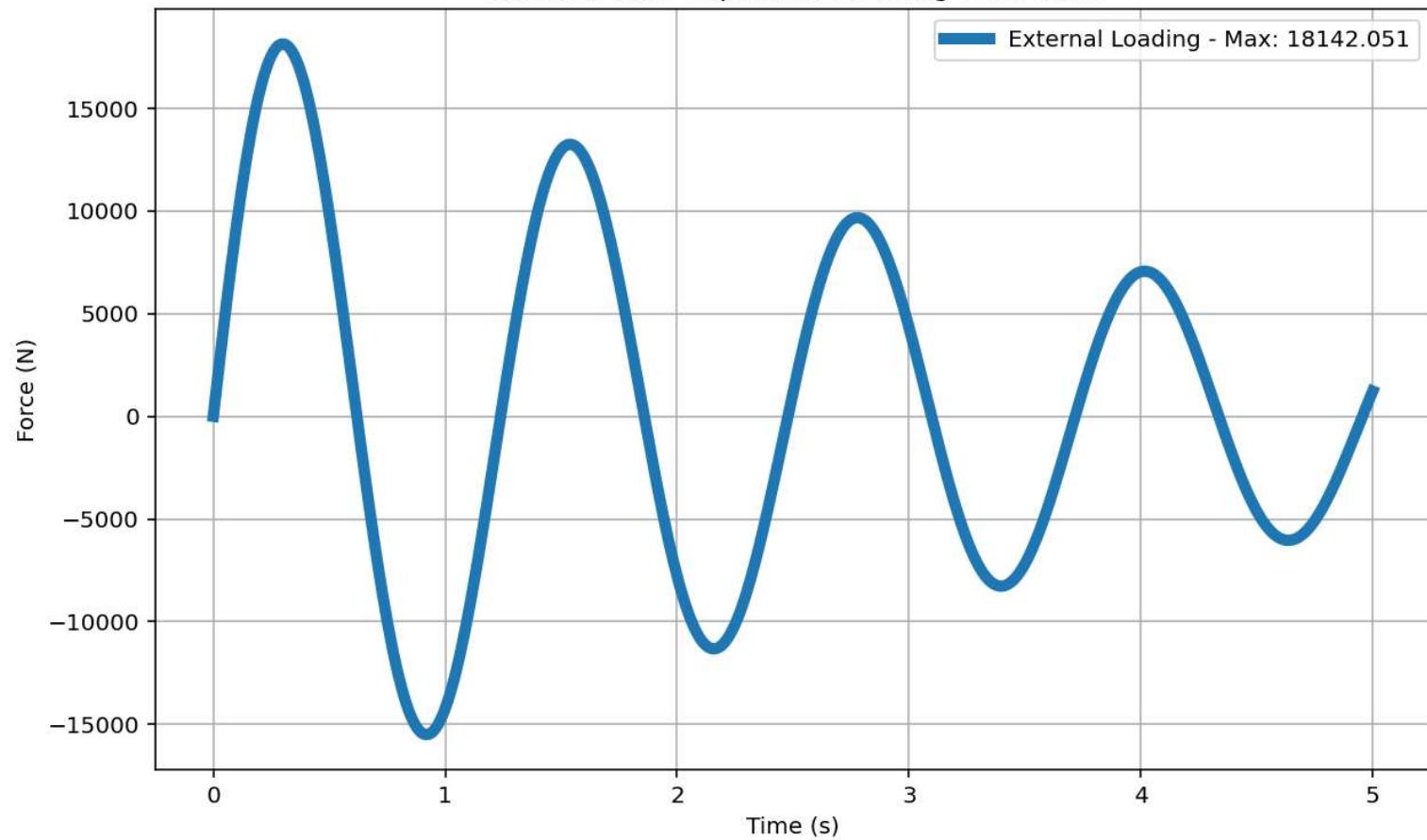




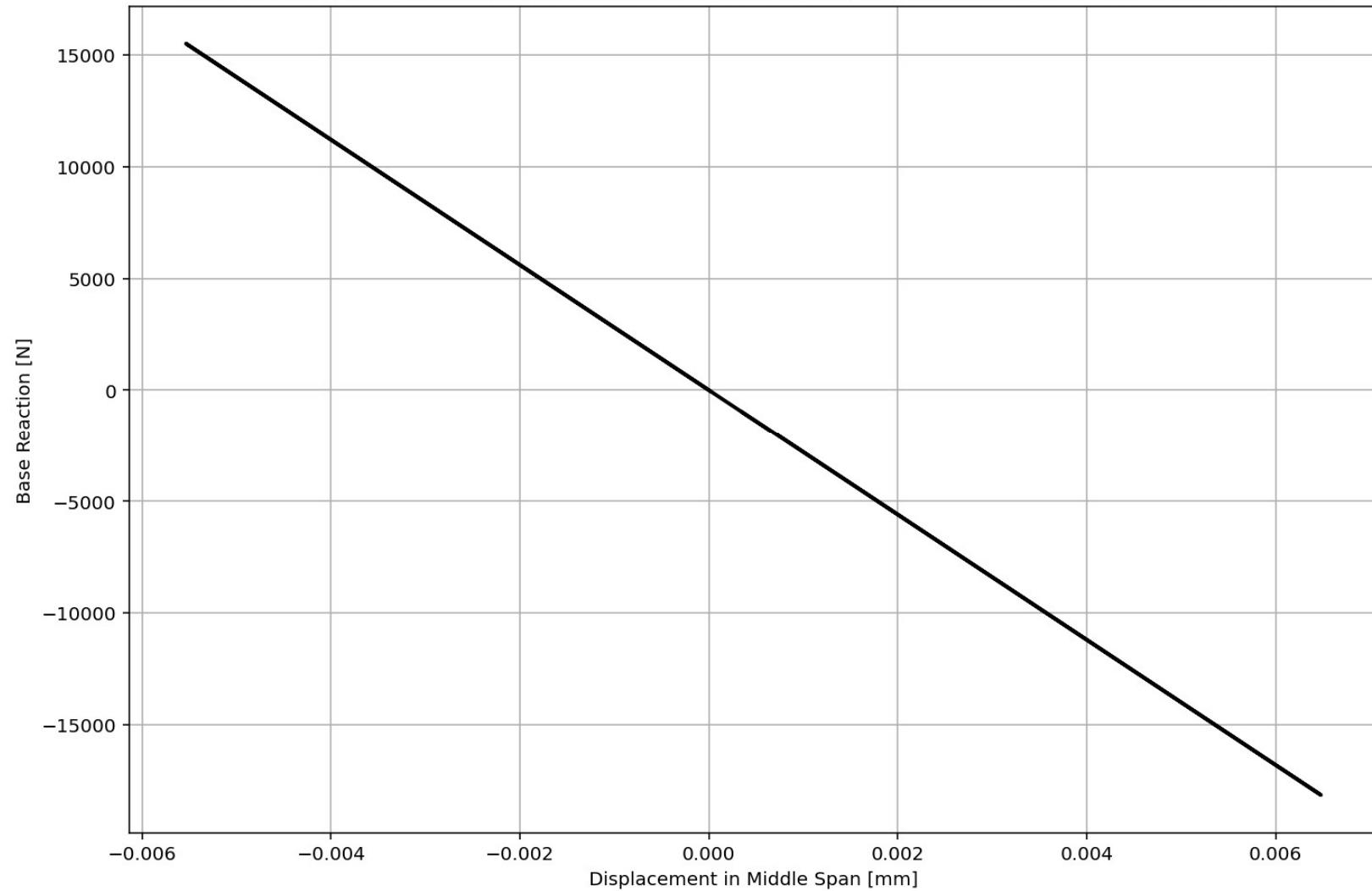
STATIC TIME-HISTORY WITH EXTERNAL TIME- DEPENDENT LOADING ANALYSIS



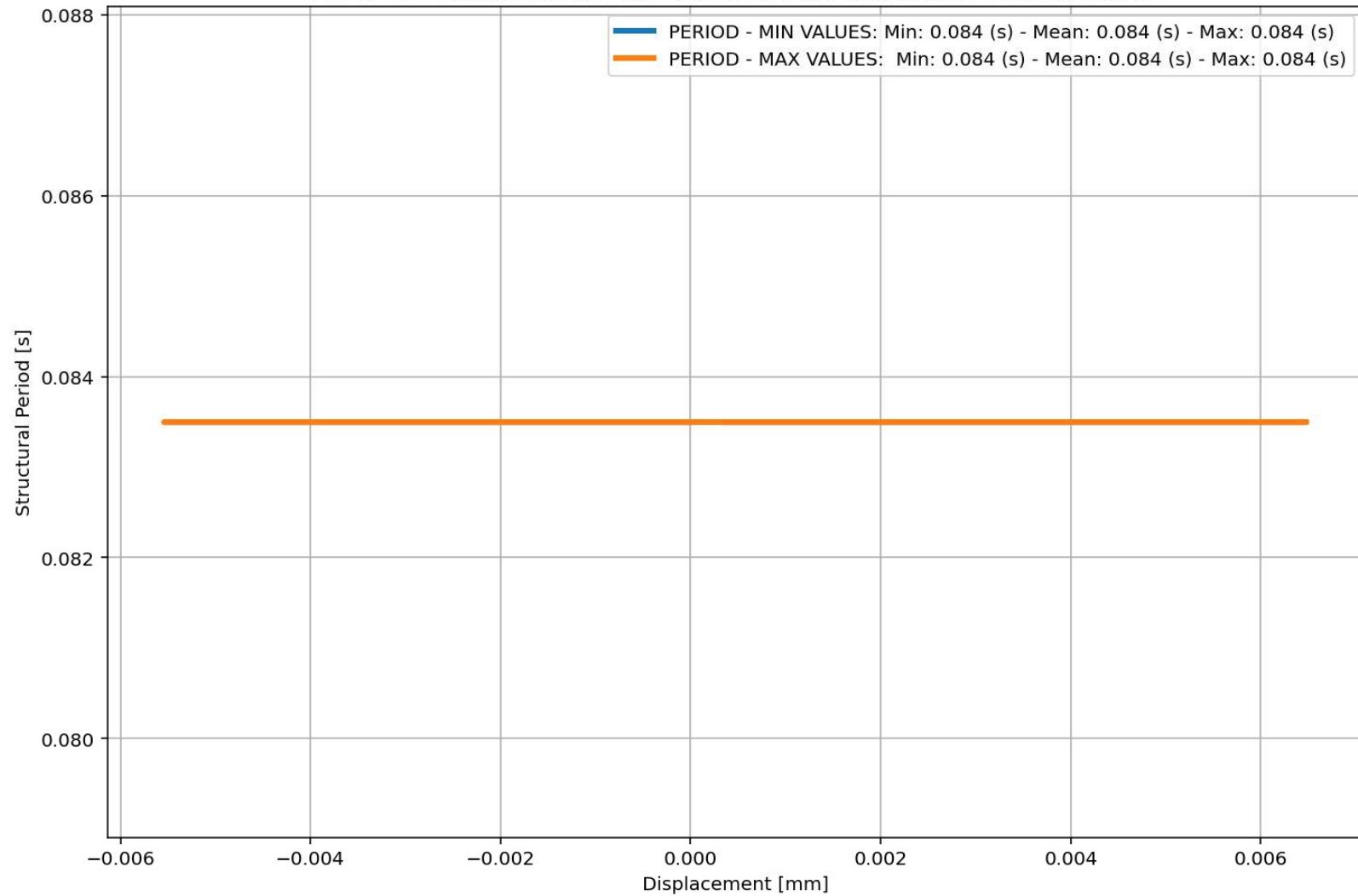
External Time-dependent Loading Over Time

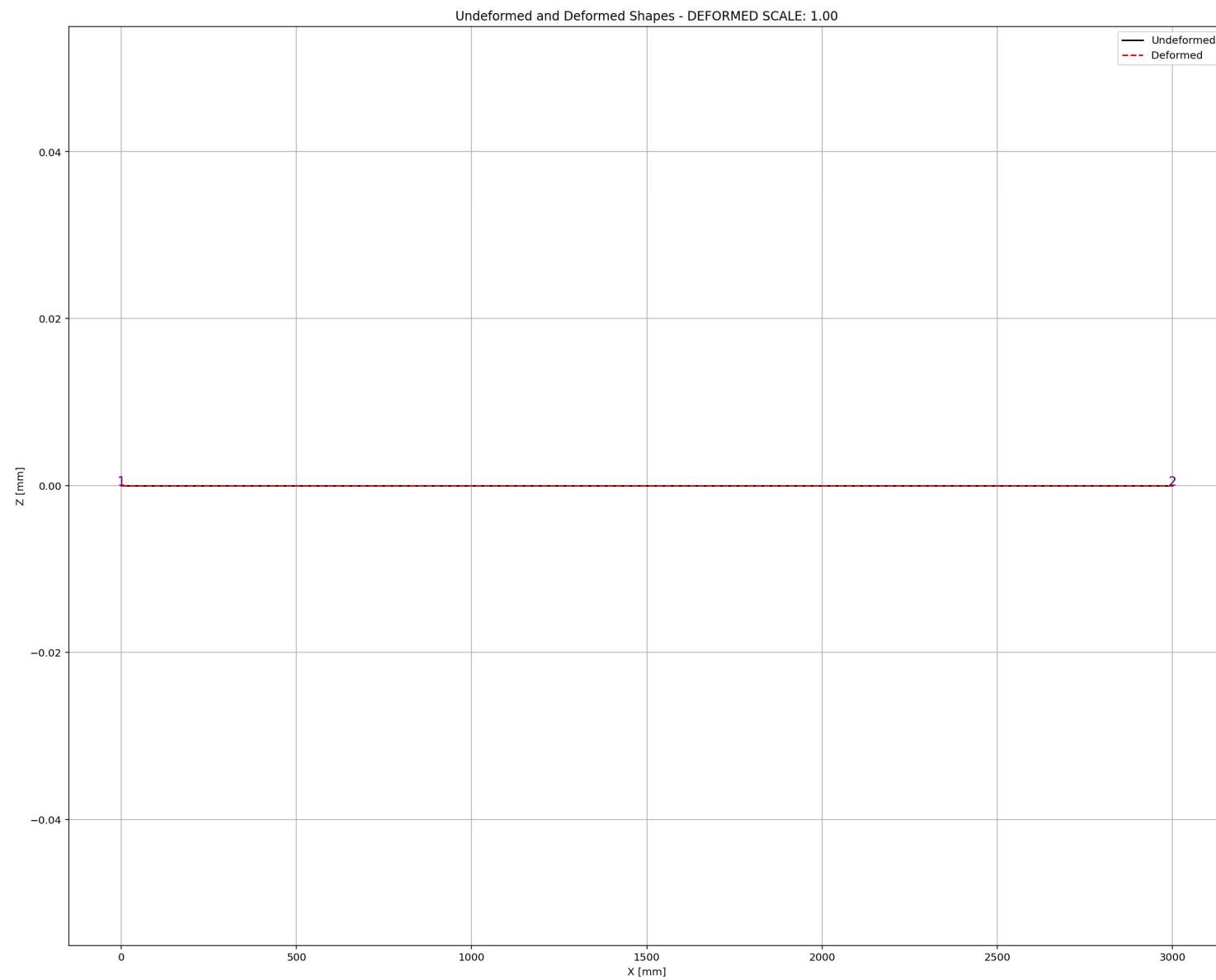


Base Reaction and Displacement of Structure During Static External Time-dependent Loading Analysis

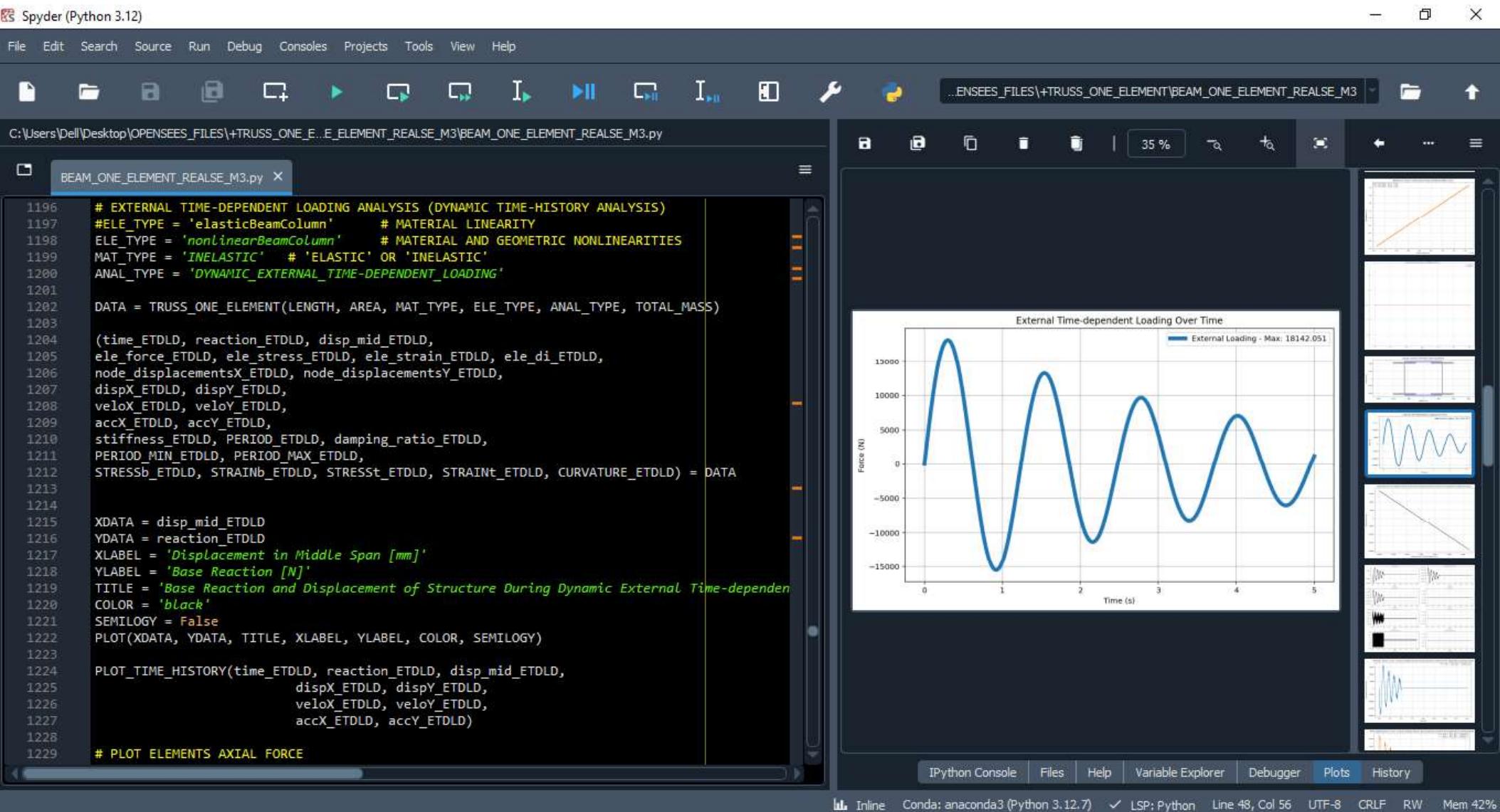


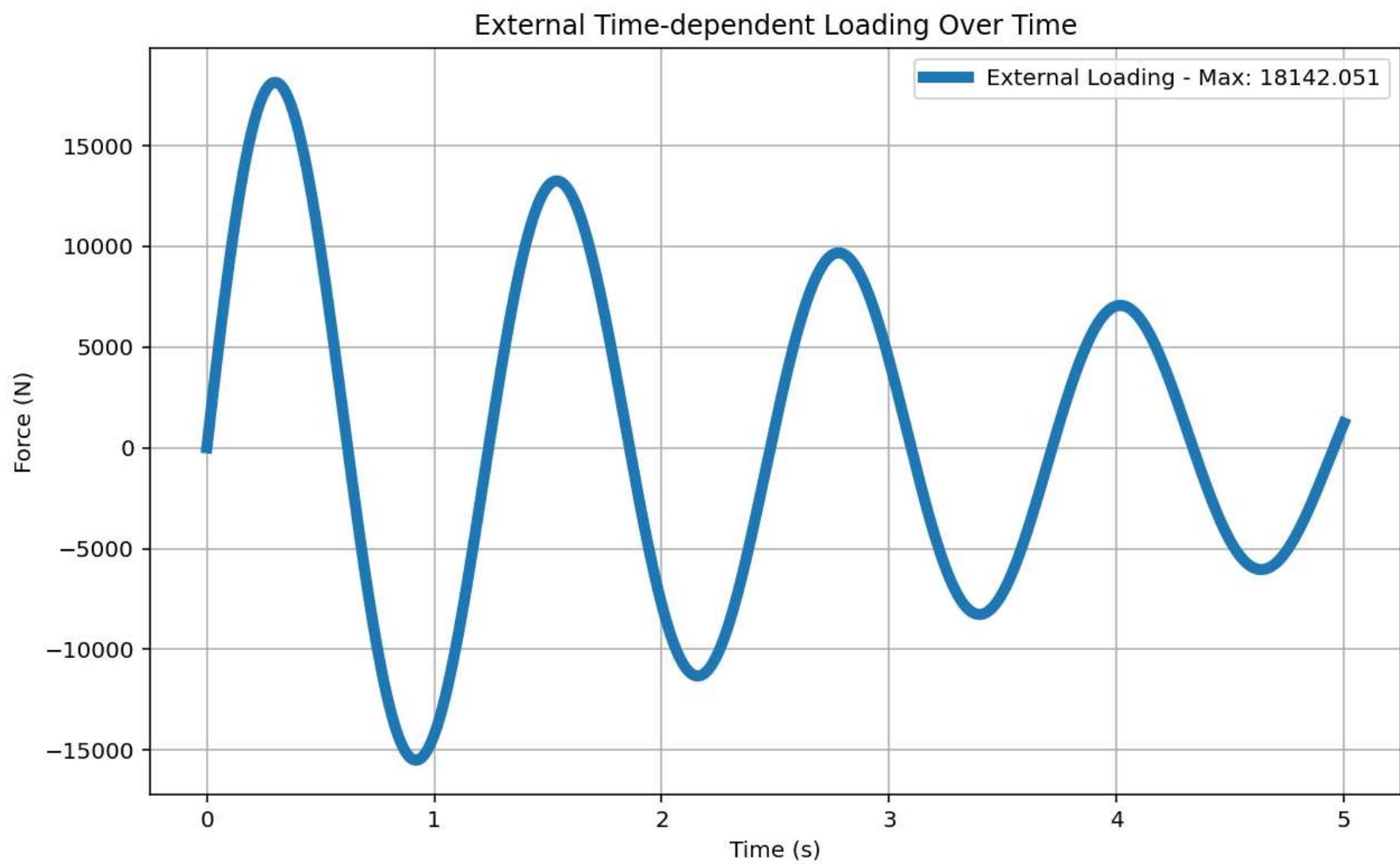
Period of Structure During Static External Time-dependent Loading Analysis



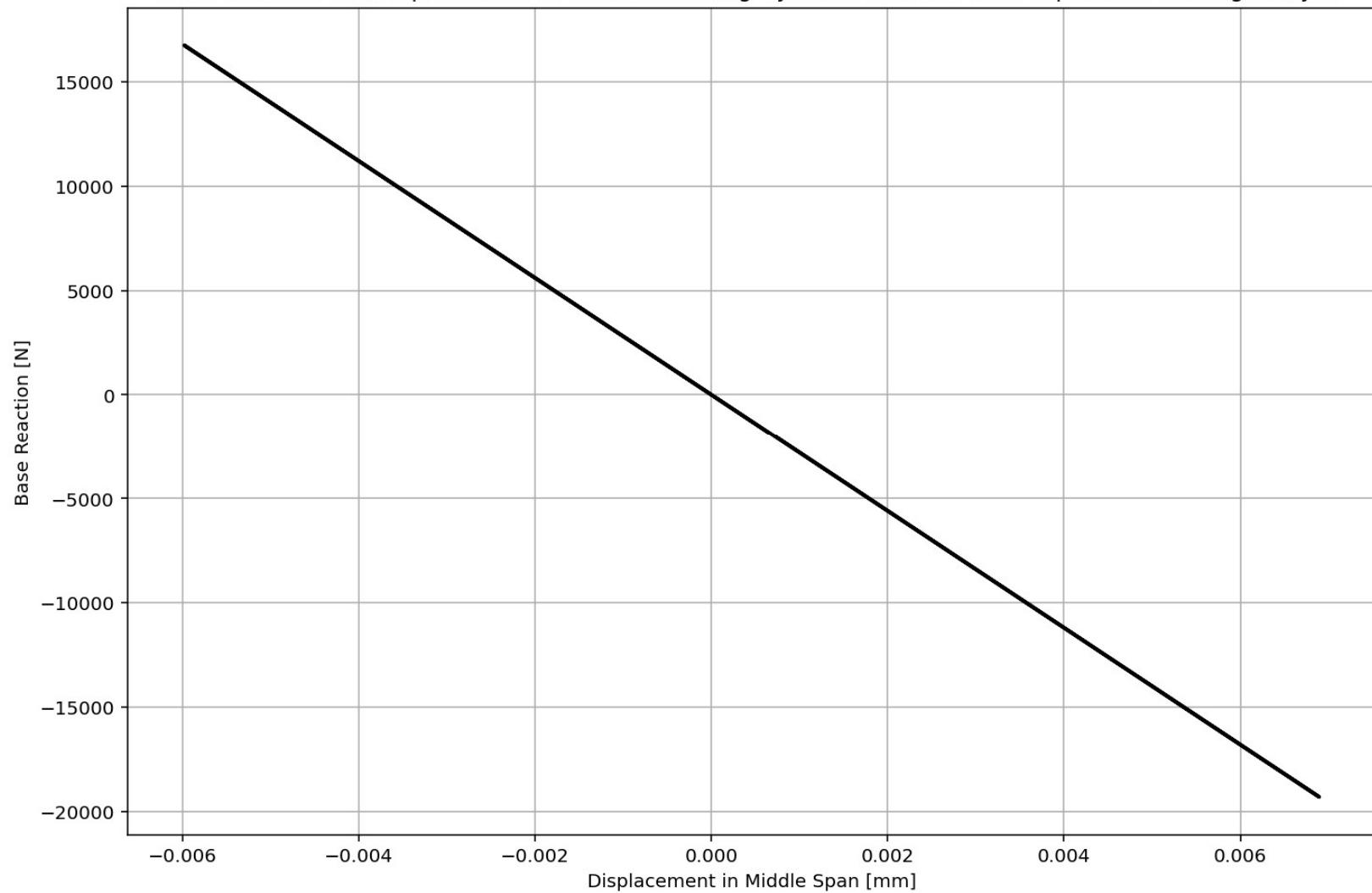


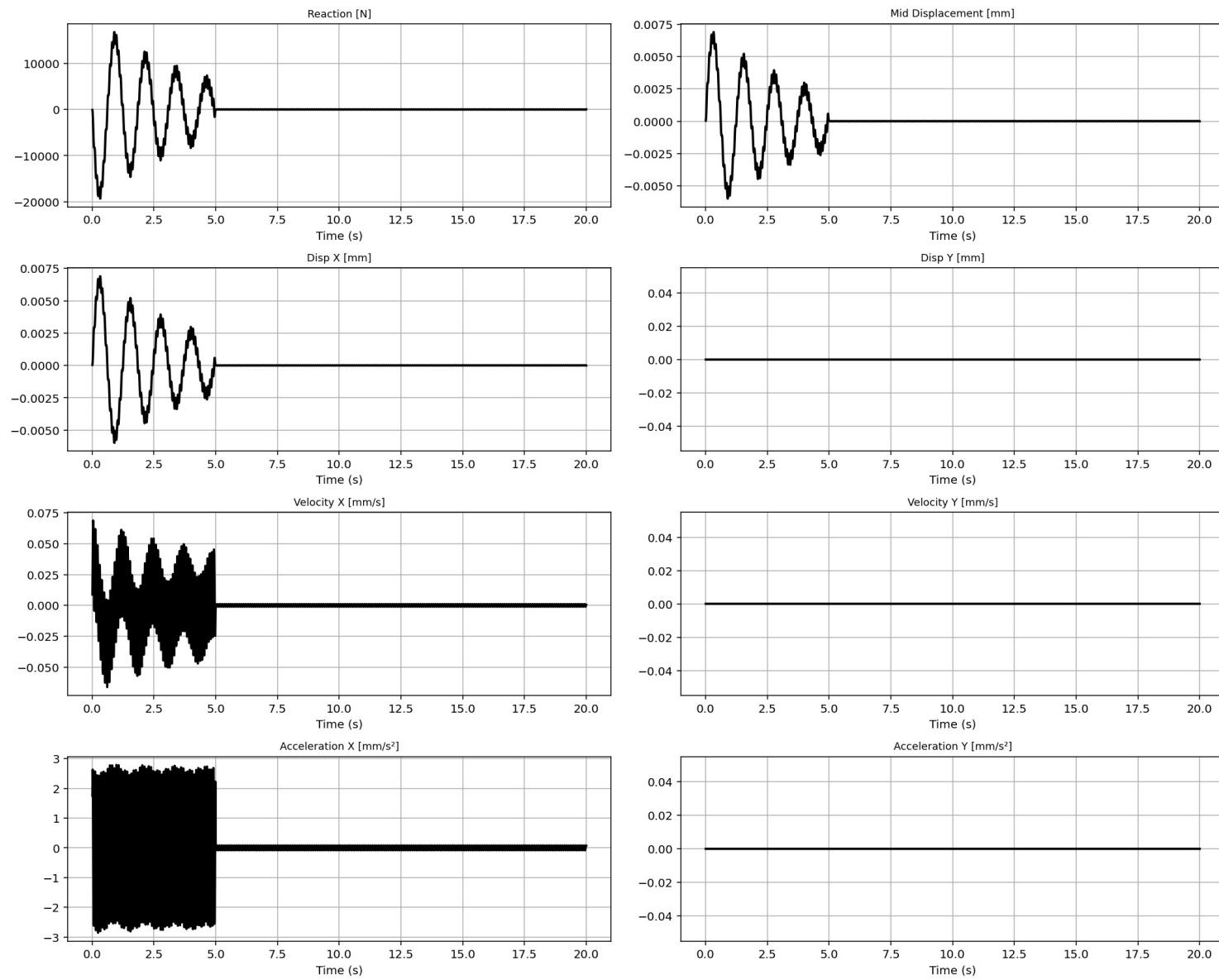
DYNAMIC TIME-HISTORY WITH EXTERNAL TIME- DEPENDENT LOADING ANALYSIS



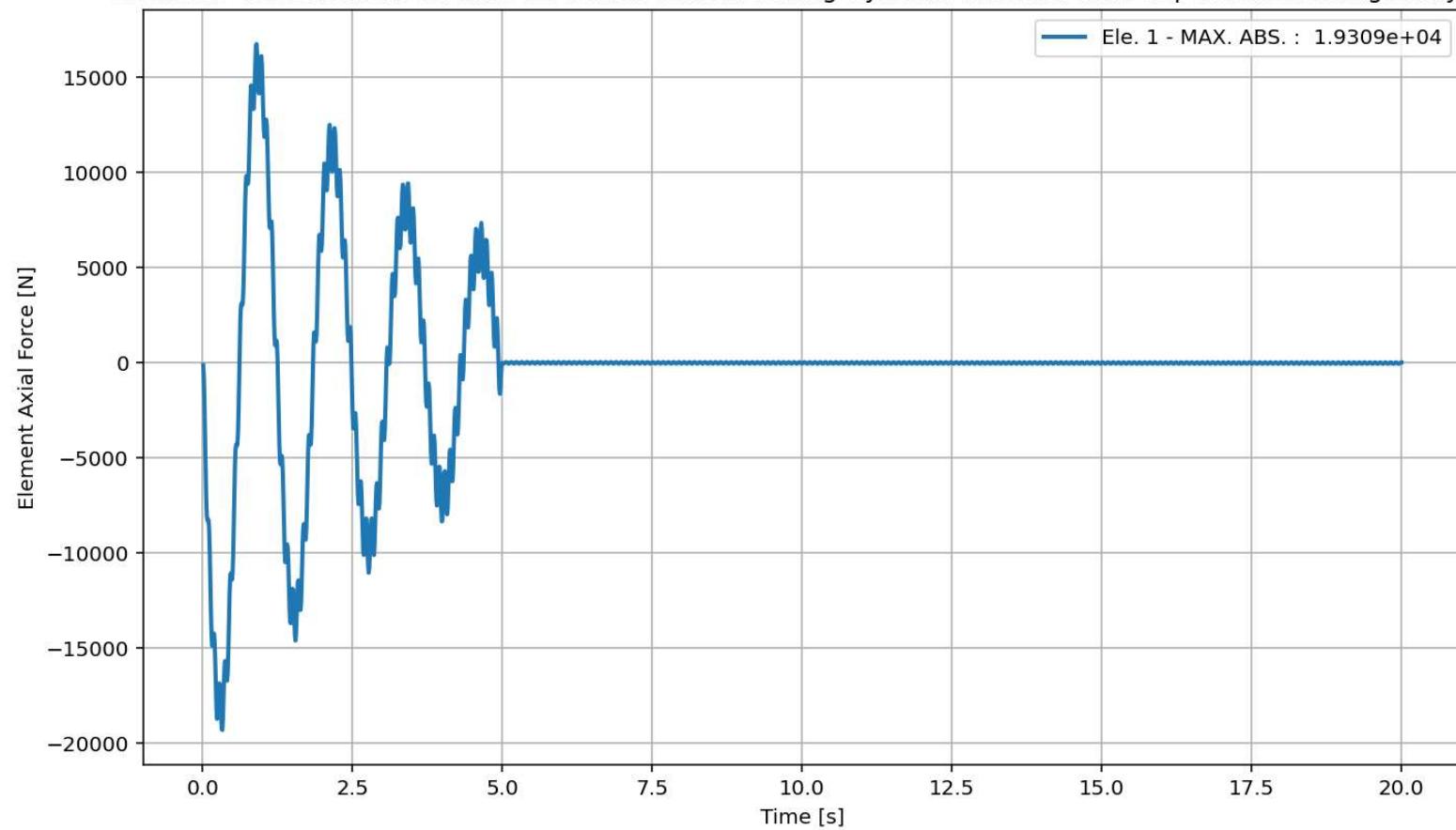


Base Reaction and Displacement of Structure During Dynamic External Time-dependent Loading Analysis

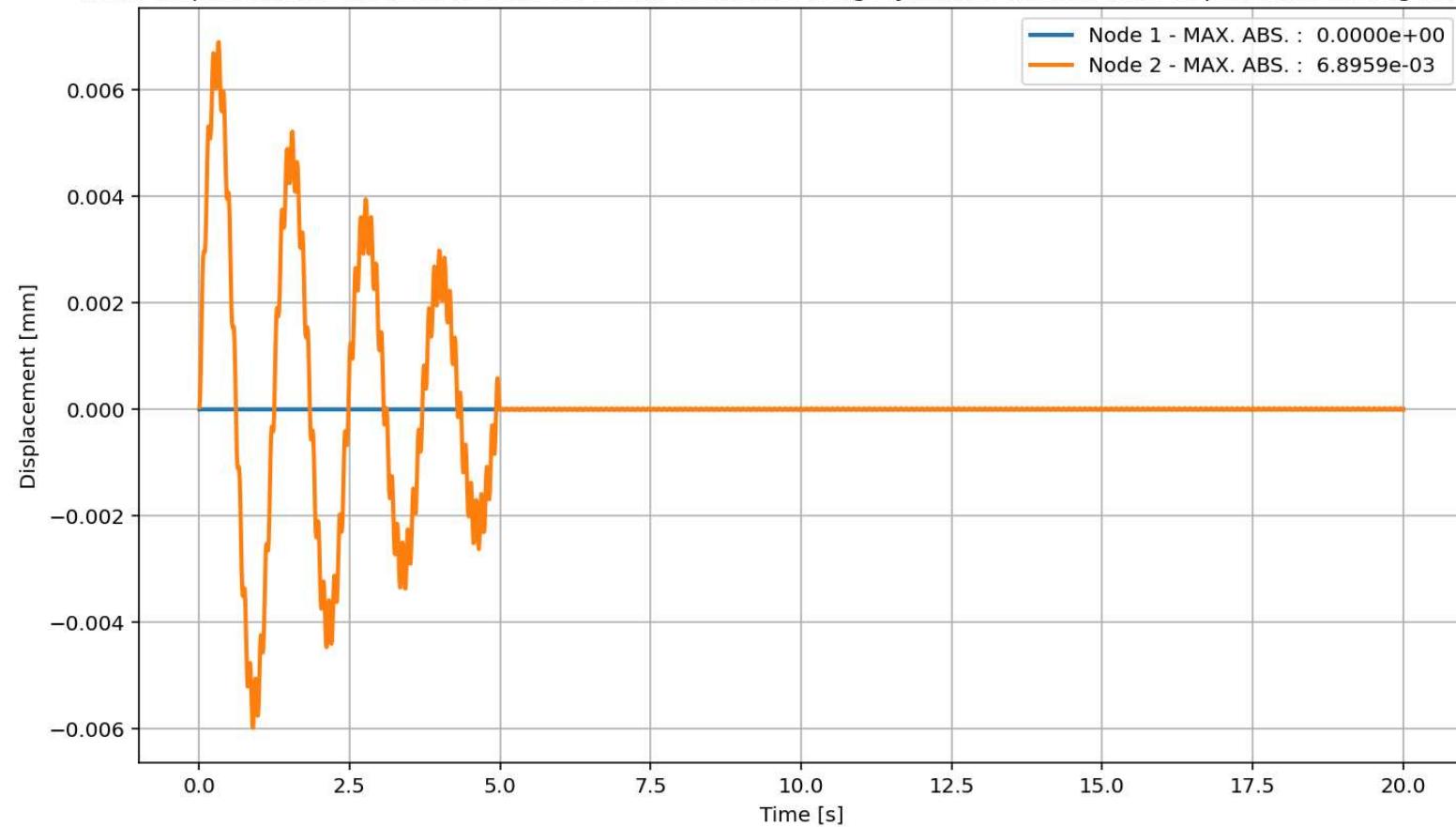




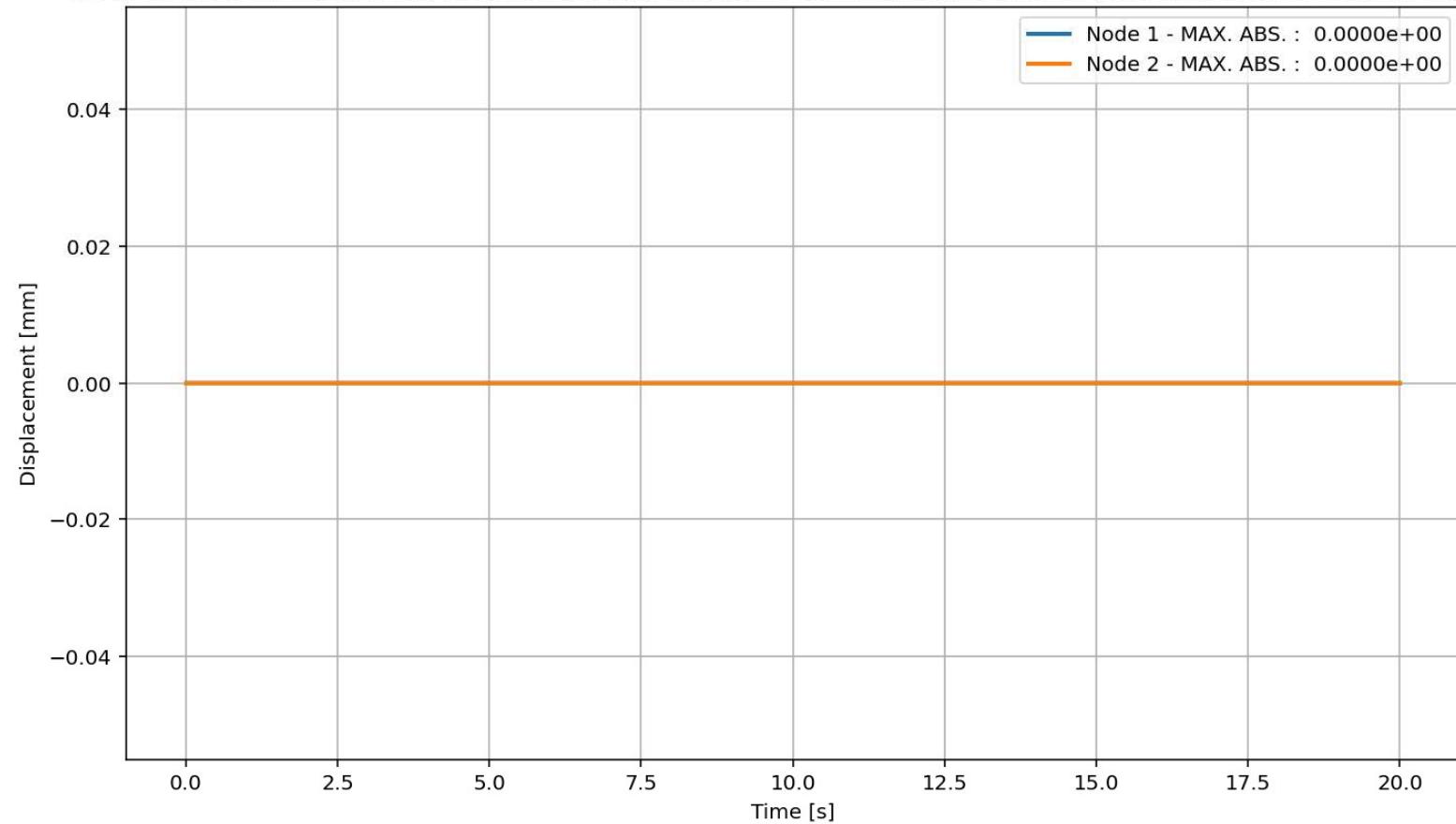
elements force in X Dir. vs Time for Beam Element During Dynamic External Time-dependent Loading Analysis



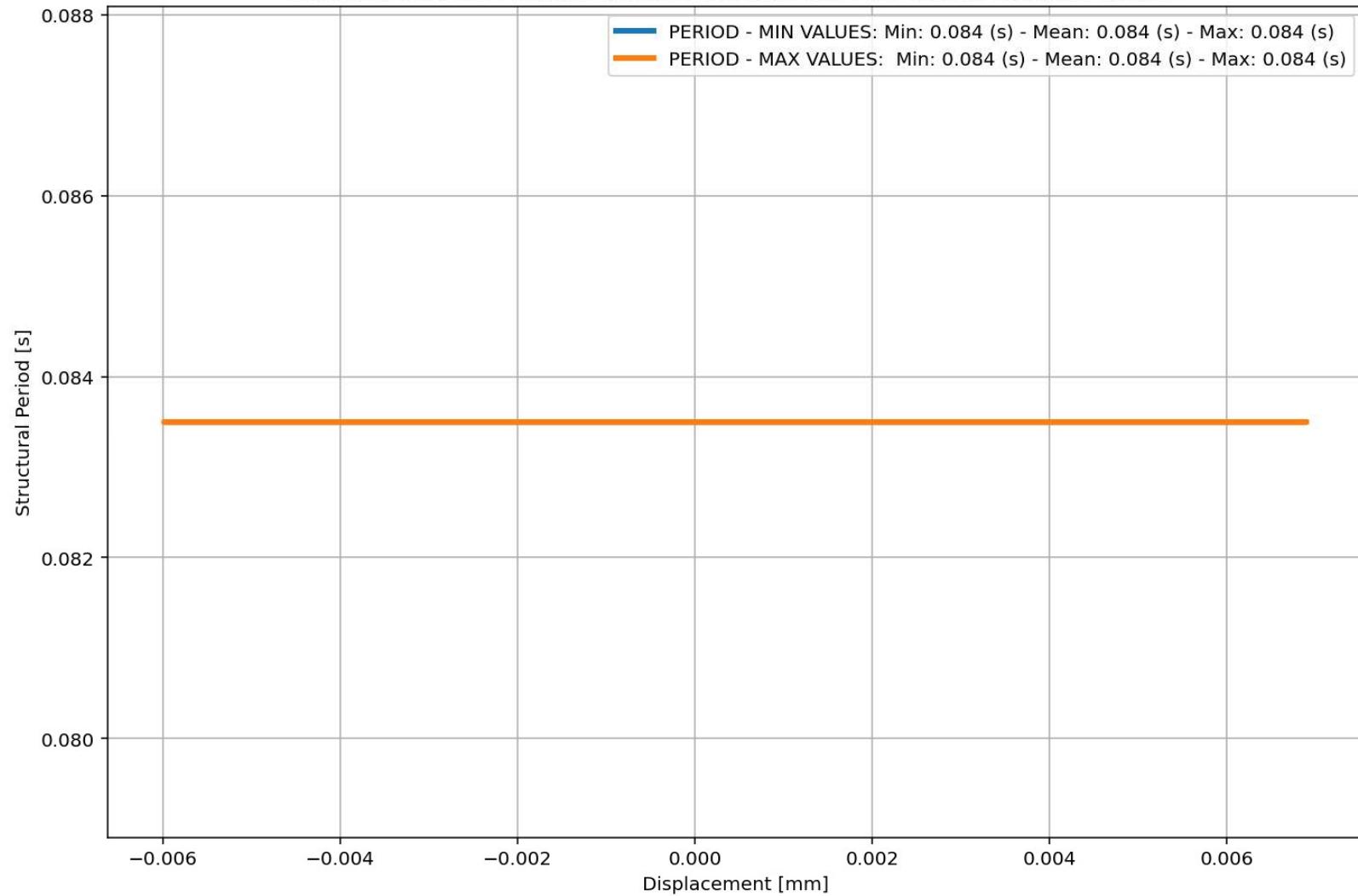
Node Displacements in X Dir. vs Time for Beam Element During Dynamic External Time-dependent Loading Analysis



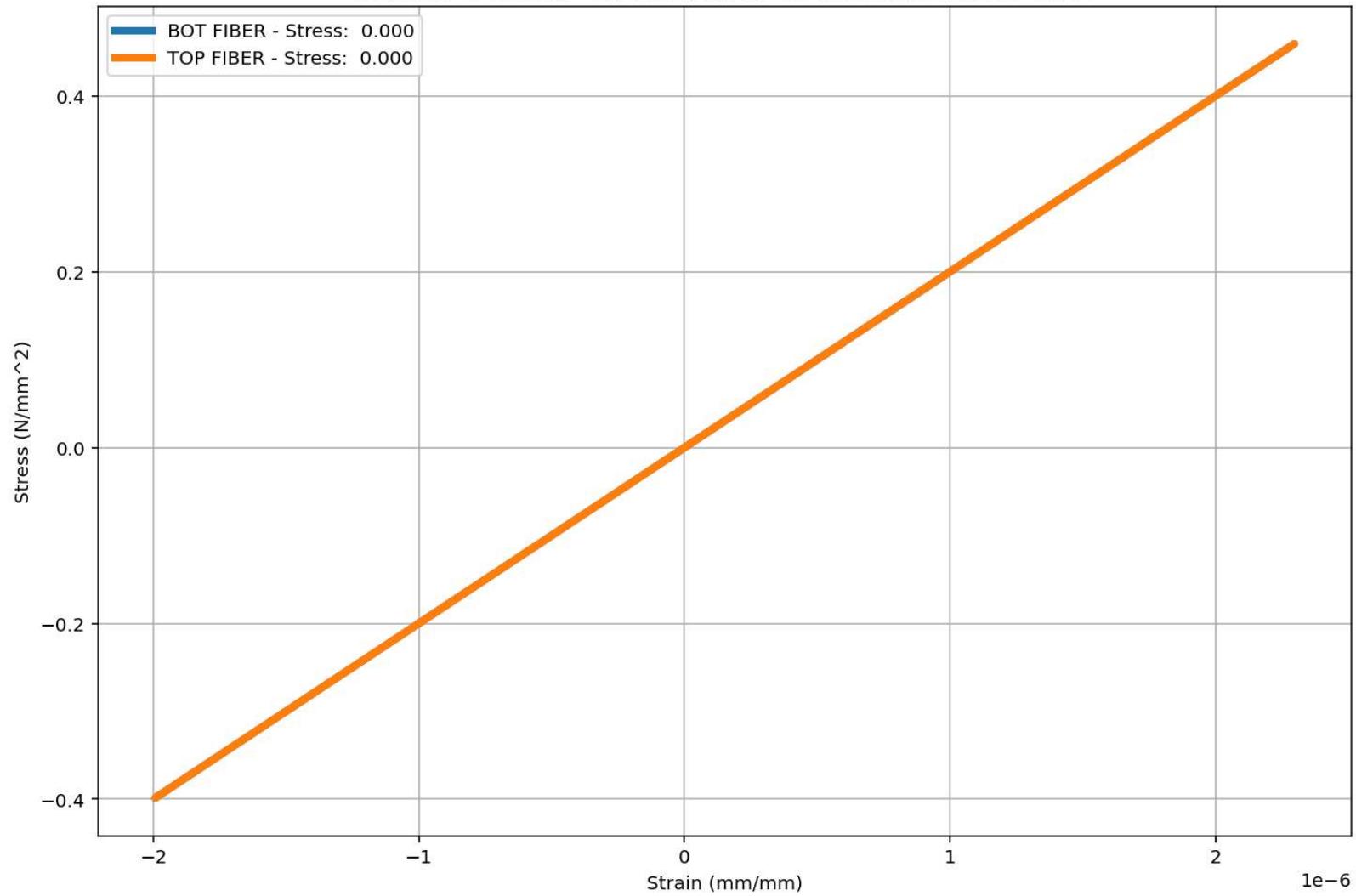
Node Displacements in Y Dir. vs Time for Beam Element During Dynamic External Time-dependent Loading Analysis

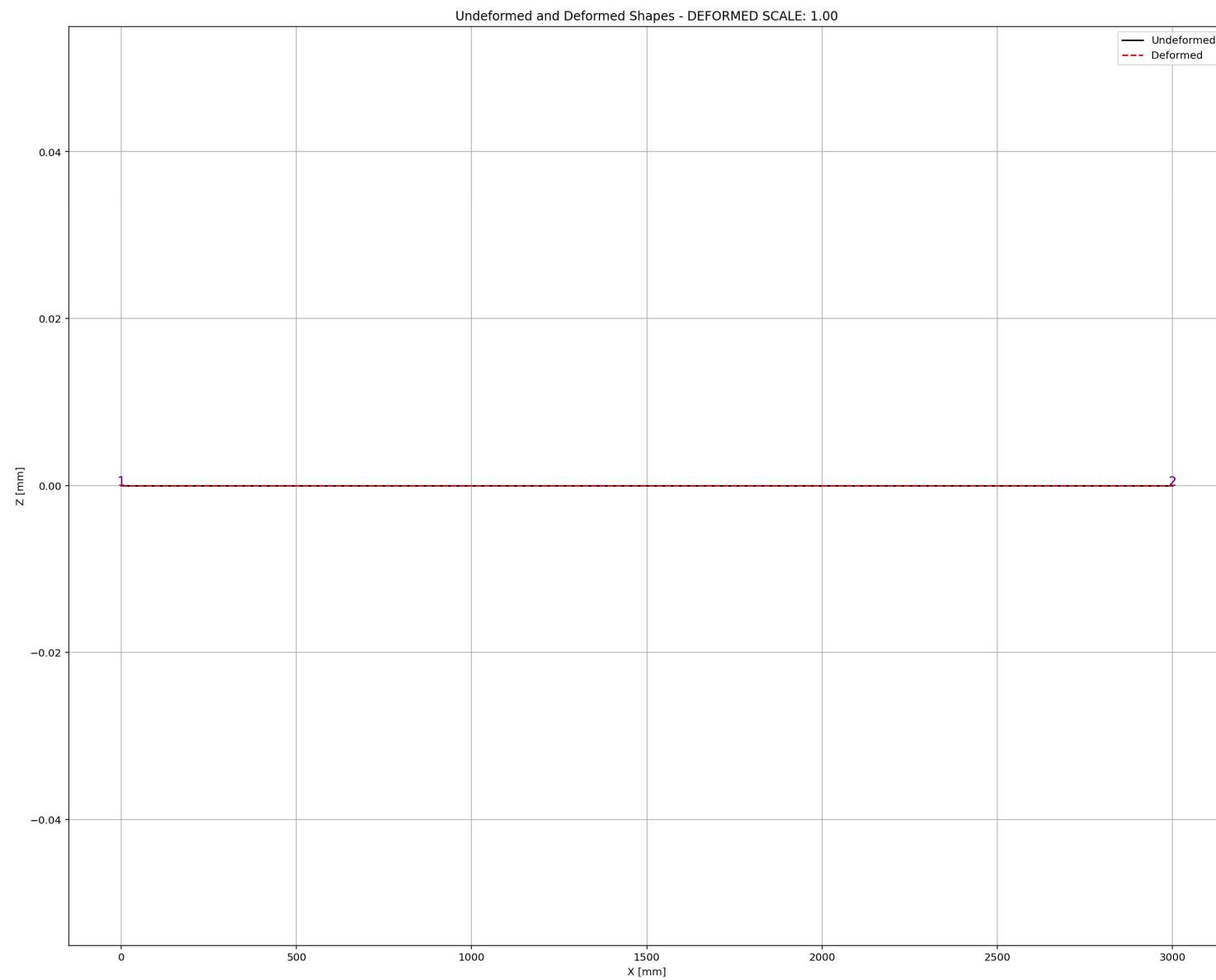


Period of Structure During Dynamic External Time-dependent Loading Analysis



Behavior of column - Stress-strain of Top and Bottom Fibers Curve





FREE-VIBRATION ANALYSIS

Spyder (Python 3.12)

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BEAM_ONE_ELEMENT_REALSE_M3.py X

```
1278 # FREE-VIBRATION ANALYSIS (DYNAMIC TIME-HISTORY ANALYSIS)
1279 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1280 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1281 MAT_TYPE = 'INELASTIC'             # 'ELASTIC' OR 'INELASTIC'
1282 ANAL_TYPE = 'FREE-VIBRATION'
1283 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)
1284
1285 (time_FV, reaction_FV, disp_mid_FV,
1286 ele_force_FV, ele_stress_FV, ele_strain_FV, ele_di_FV,
1287 node_displacementsX_FV, node_displacementsY_FV,
1288 dispX_FV, dispY_FV,
1289 veloX_FV, veloY_FV,
1290 accX_FV, accY_FV,
1291 stiffness_FV, PERIOD_FV, damping_ratio_FV,
1292 PERIOD_MIN_FV, PERIOD_MAX_FV,
1293 STRESSb_FV, STRAINb_FV, STRESSt_FV, STRAINT_FV, CURVATURE_FV) = DATA
1294
1295 XDATA = disp_mid_FV
1296 YDATA = reaction_FV
1297 XLABEL = 'Displacement in Middle Span [mm]'
1298 YLABEL = 'Base Reaction [N]'
1299 TITLE = 'Base Reaction and Displacement of Structure During Free-vibration Analysis'
1300 COLOR = 'black'
1301 SEMILOGY = False
1302 PLOT(XDATA, YDATA, TITLE, XLABEL, YLABEL, COLOR, SEMILOGY)
1303
1304 PLOT_TIME_HISTORY(time_FV, reaction_FV, disp_mid_FV,
1305                     dispX_FV, dispY_FV,
1306                     veloX_FV, veloY_FV,
1307                     accX_FV, accY_FV)
1308
1309 # PLOT ELEMENTS AXIAL FORCE
1310 YLABEL = 'Element Axial Force [N]'
1311 TITLE = "elements force in X Dir. vs Time for Beam Element During Free-vibration Analysis"
```

...ENSEES_FILES\+TRUSS_ONE_ELEMENT\BEAM_ONE_ELEMENT_REALSE_M3

30 %

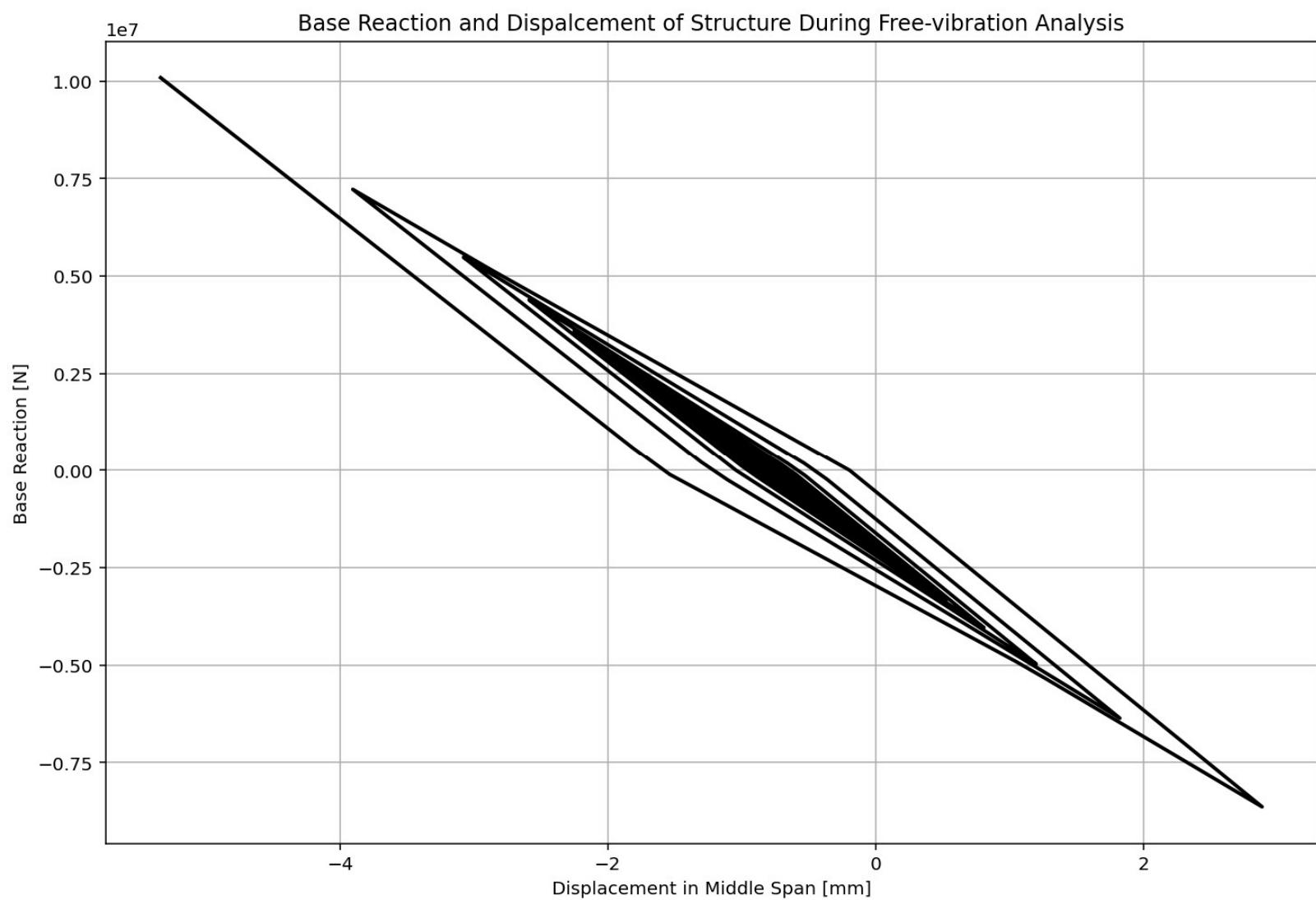
Base Reaction and Displacement of Structure During Free-vibration Analysis

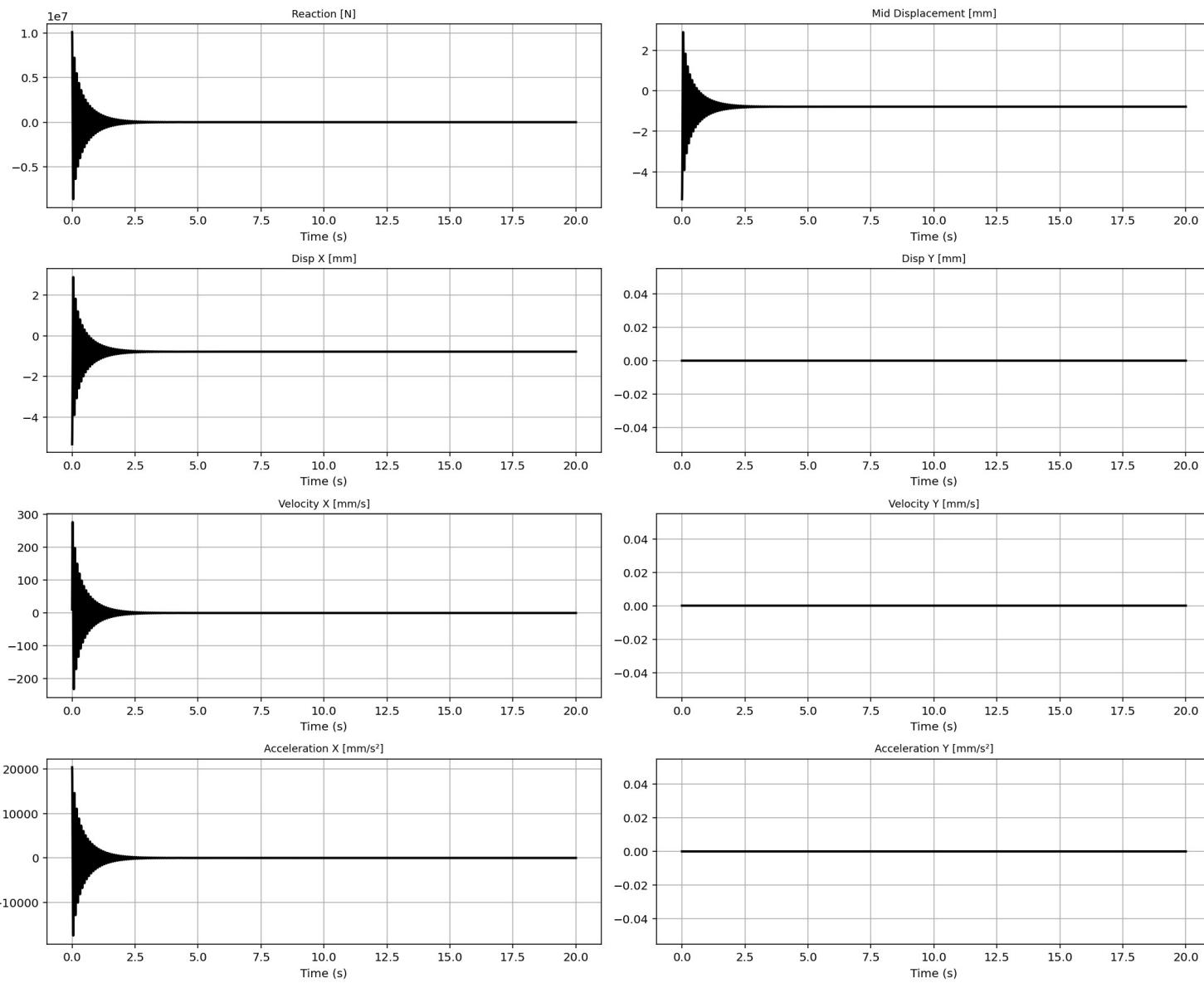
Base Reaction [N]

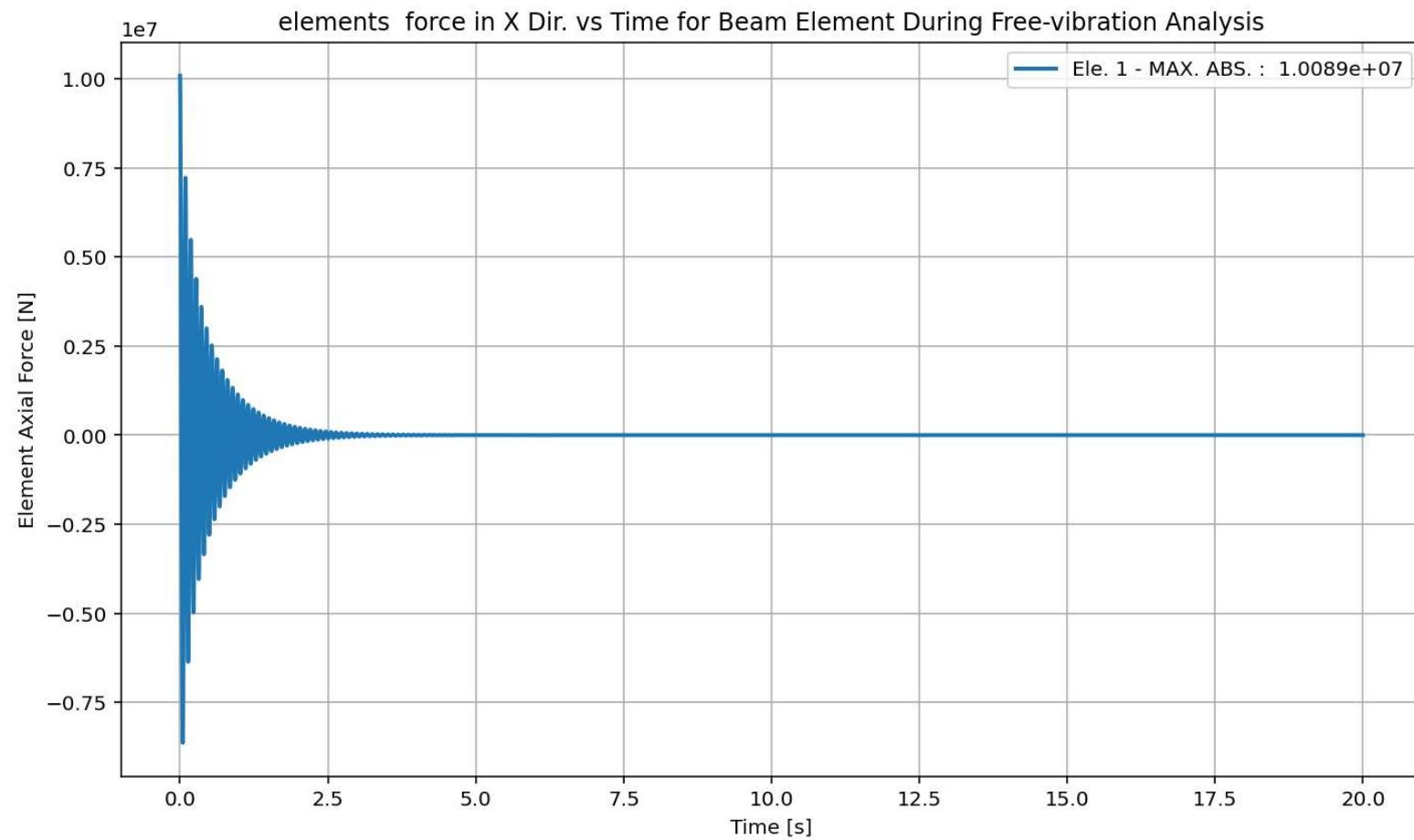
Displacement in Middle Span [mm]

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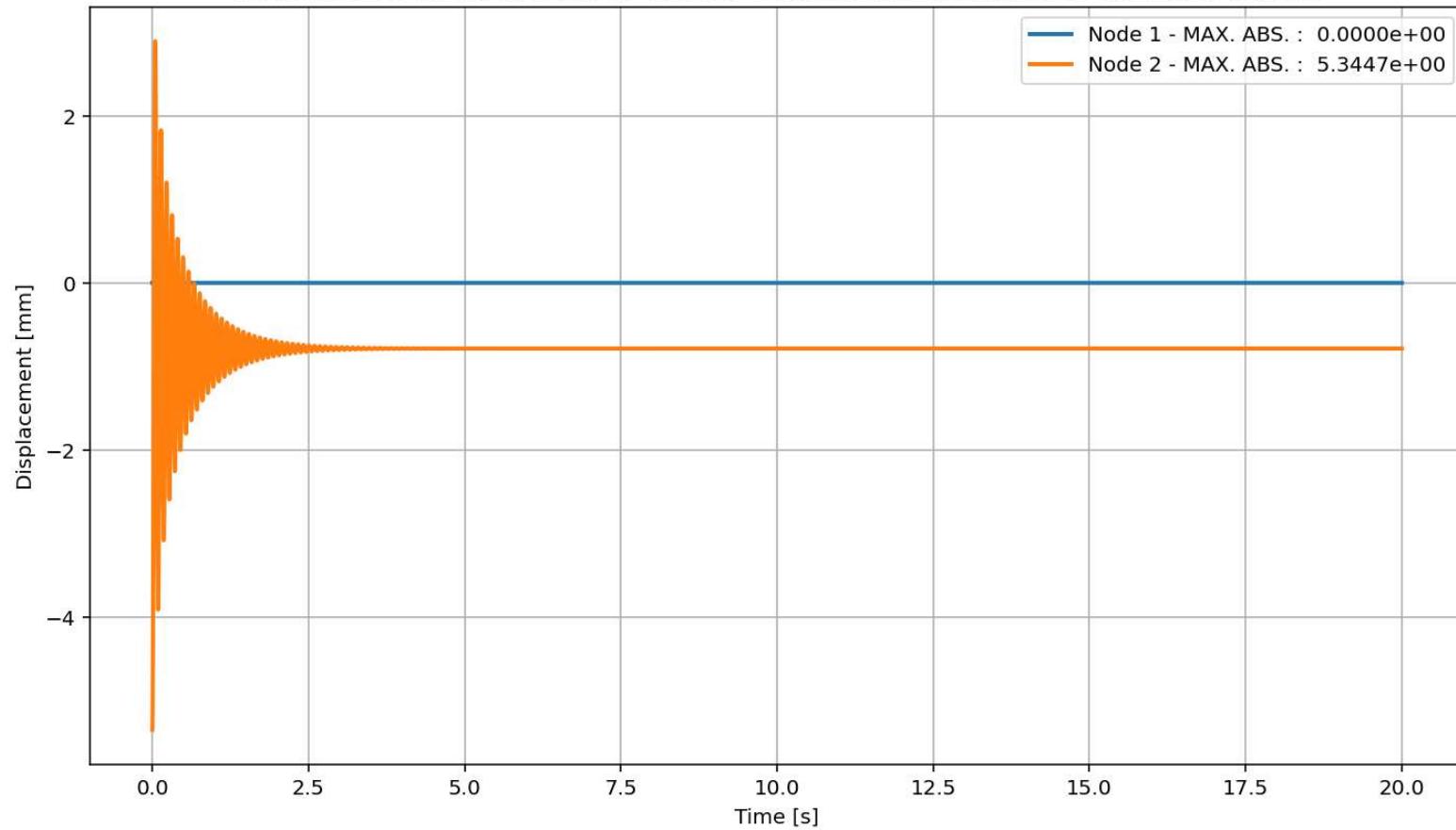
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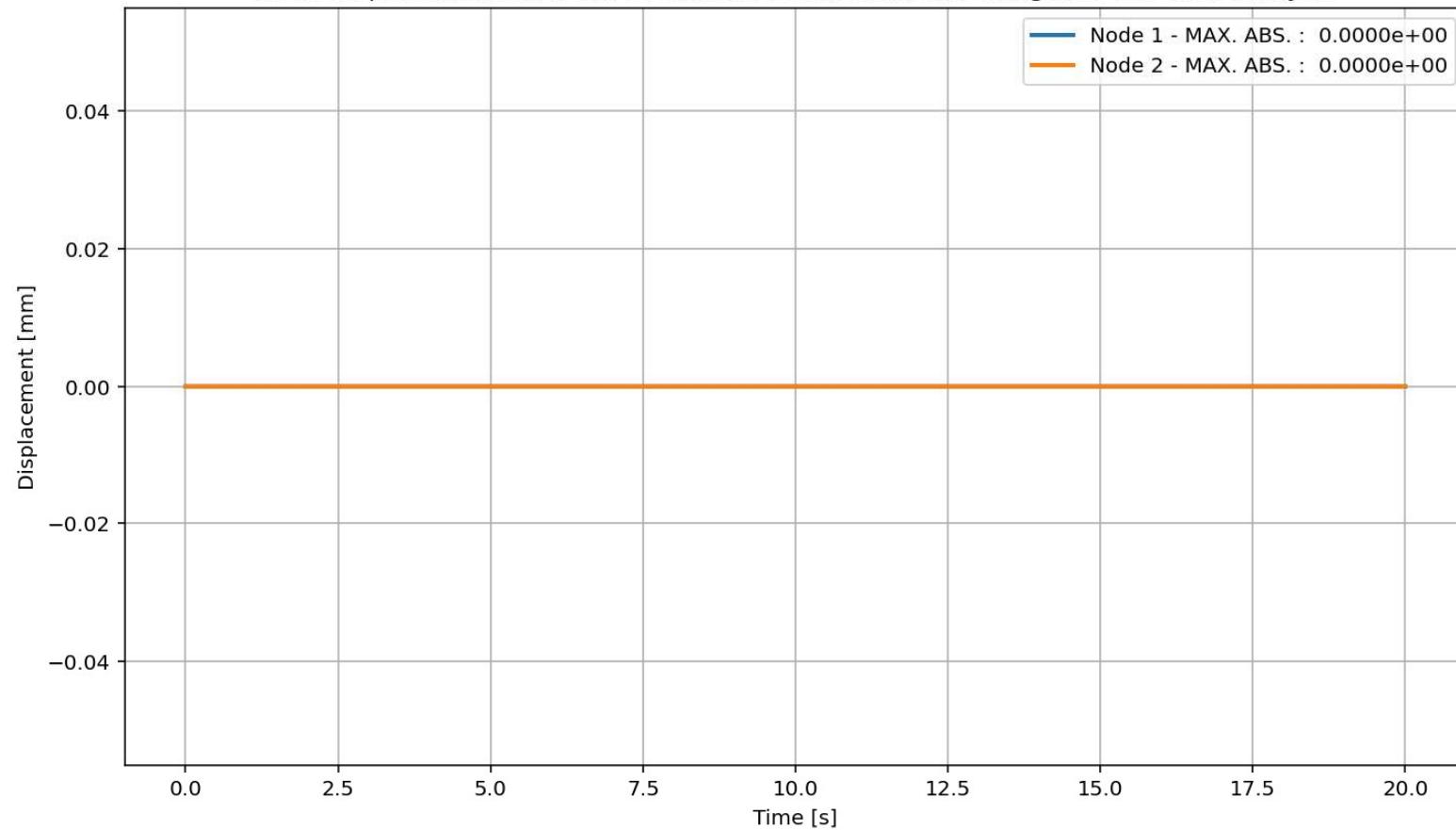


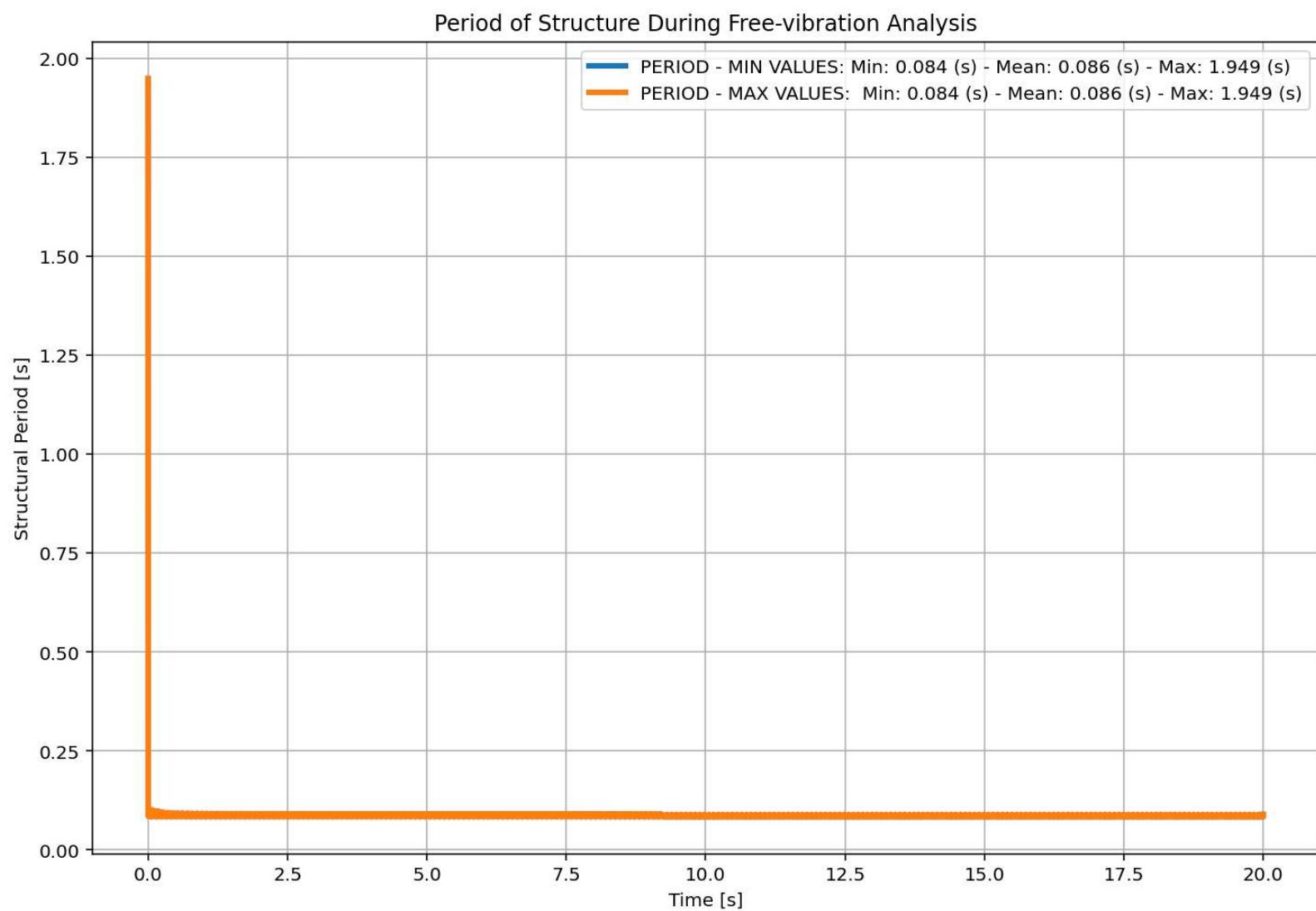


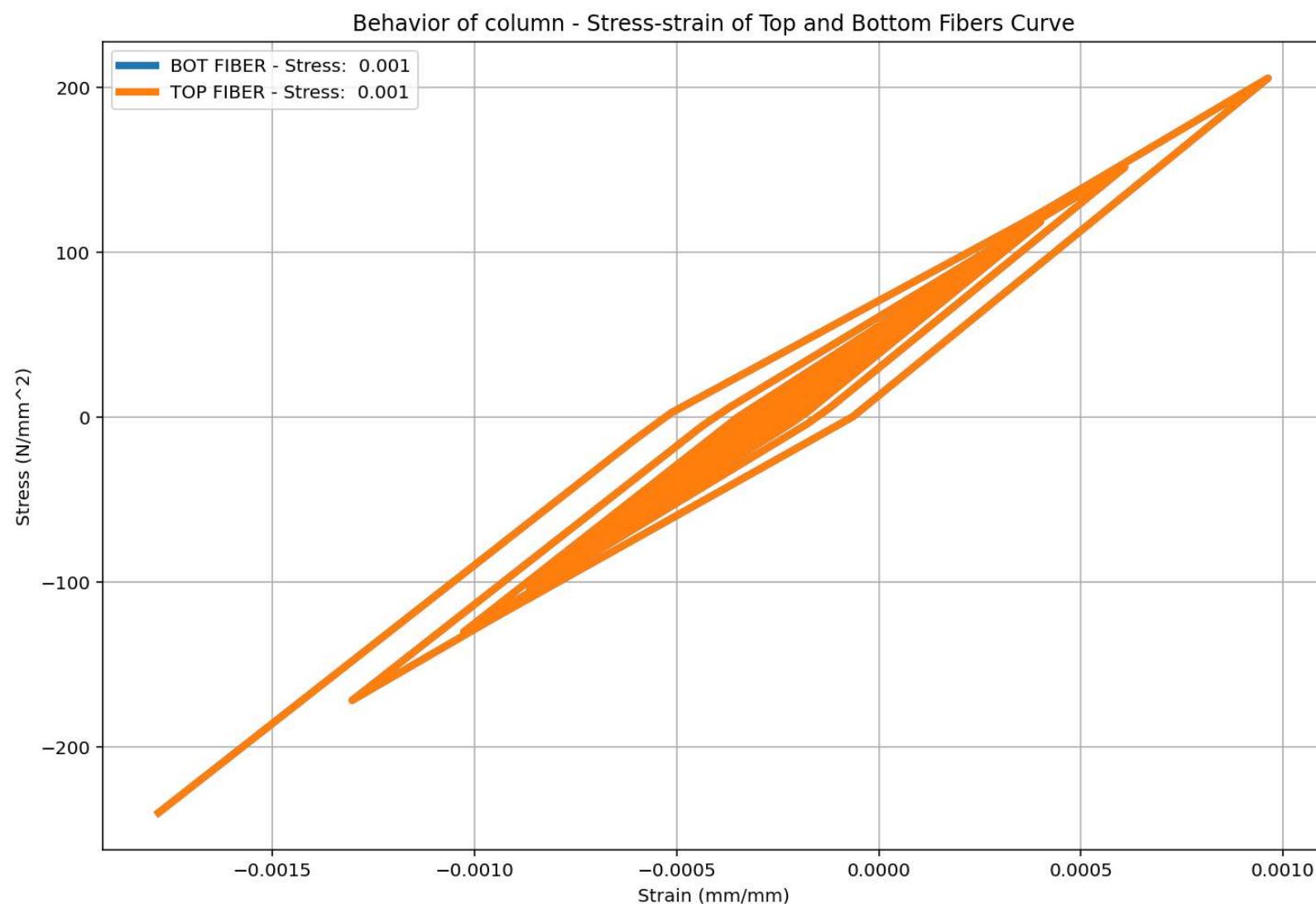
Node Displacements in X Dir. vs Time for Beam Element During Free-vibration Analysis

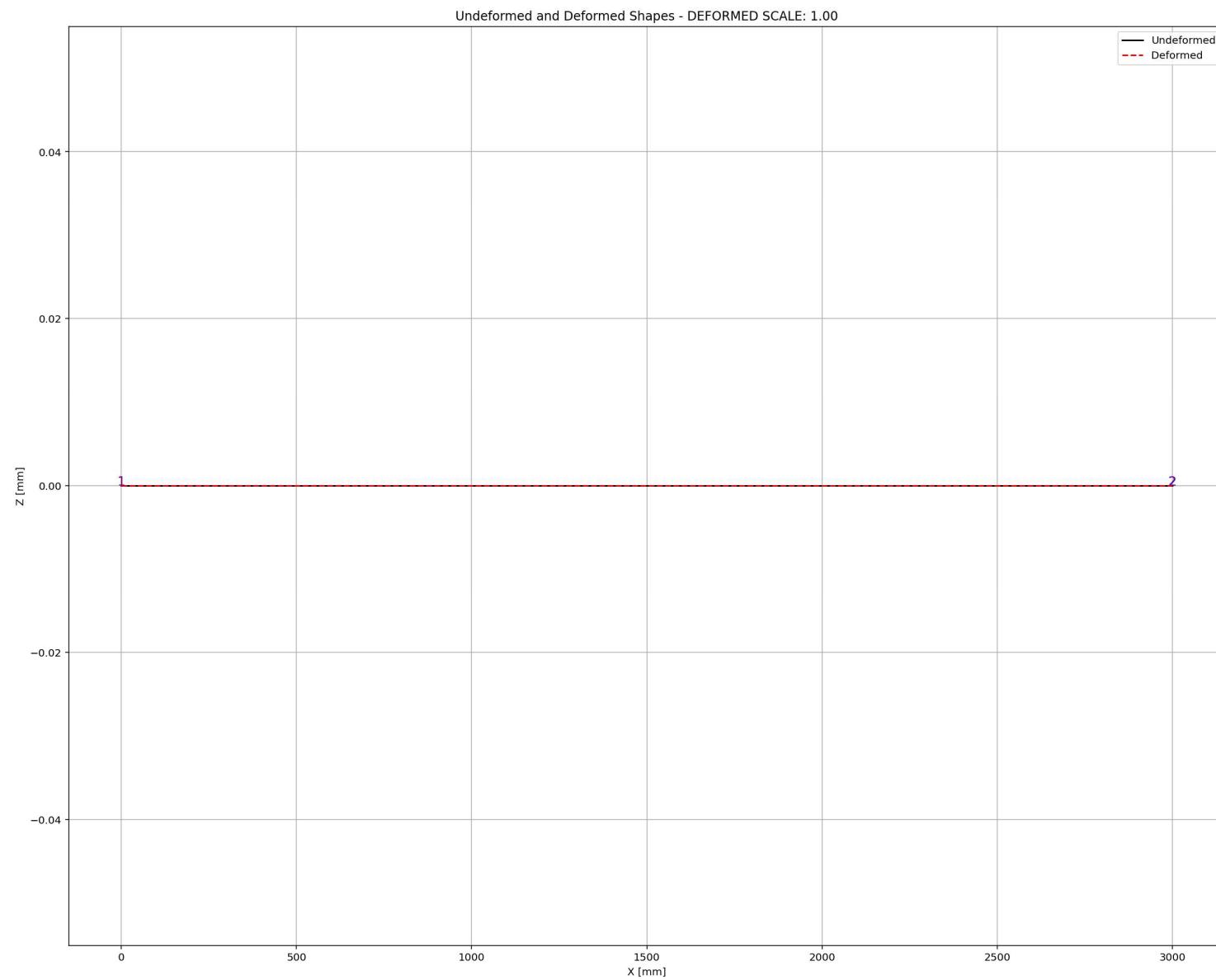


Node Displacements in Y Dir. vs Time for Beam Element During Free-vibration Analysis









SEISMIC ANALYSIS

Spyder (Python 3.12)

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BEAM_ONE_ELEMENT_REALSE_M3.py X

```
1357 # SEISMIC ANALYSIS (DYNAMIC TIME-HISTORY ANALYSIS)
1358 #ELE_TYPE = 'elasticBeamColumn'      # MATERIAL LINEARITY
1359 ELE_TYPE = 'nonlinearBeamColumn'    # MATERIAL AND GEOMETRIC NONLINEARITIES
1360 MAT_TYPE = 'INELASTIC'            # 'ELASTIC' OR 'INELASTIC'
1361 ANAL_TYPE = 'SEISMIC'
1362
1363 DATA = TRUSS_ONE_ELEMENT(LENGTH, AREA, MAT_TYPE, ELE_TYPE, ANAL_TYPE, TOTAL_MASS)
1364
1365 (time_SEI, reaction_SEI, disp_mid_SEI,
1366 ele_axialforce_SEI, ele_stress_SEI, ele_strain_SEI, ele_di_SEI,
1367 node_displacementsX_SEI, node_displacementsY_SEI,
1368 dispX_SEI, dispY_SEI,
1369 veloX_SEI, veloY_SEI,
1370 accX_SEI, accY_SEI,
1371 stiffness_SEI, PERIOD_SEI, damping_ratio_SEI,
1372 PERIOD_MIN_SEI, PERIOD_MAX_SEI,
1373 STRESSb_SEI, STRAINb_SEI, STRESSt_SEI, STRAINT_SEI, CURVATURE_SEI) = DATA
1374
1375
1376 XDATA = disp_mid_SEI
1377 YDATA = reaction_SEI
1378 XLABEL = 'Displacement in Middle Span [mm]'
1379 YLABEL = 'Base Reaction [N]'
1380 TITLE = 'Base Reaction and Displacement of Structure During Seismic Analysis'
1381 COLOR = 'black'
1382 SEMILOGY = False
1383 PLOT(XDATA, YDATA, TITLE, XLABEL, YLABEL, COLOR, SEMILOGY)
1384
1385 PLOT_TIME_HISTORY(time_SEI, reaction_SEI, disp_mid_SEI,
1386                     dispX_SEI, dispY_SEI,
1387                     veloX_SEI, veloY_SEI,
1388                     accX_SEI, accY_SEI)
1389
1390 # PLOT ELEMENTS AXIAL FORCE
```

..\\ENSEES_FILES\\+TRUSS_ONE_ELEMENT\\BEAM_ONE_ELEMENT_REALSE_M3

30 %

Base Reaction and Displacement of Structure During Seismic Analysis

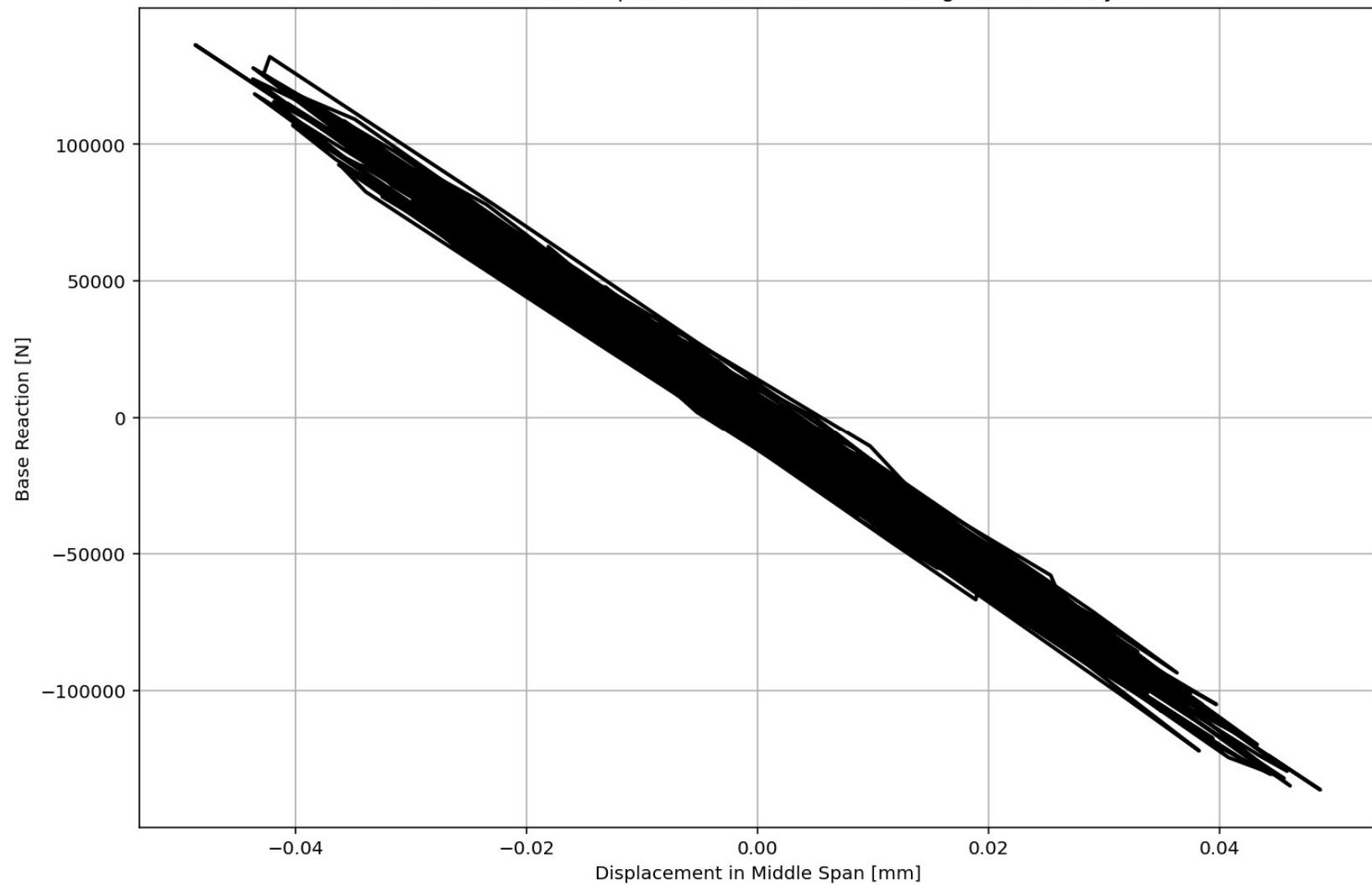
Base Reaction [N]

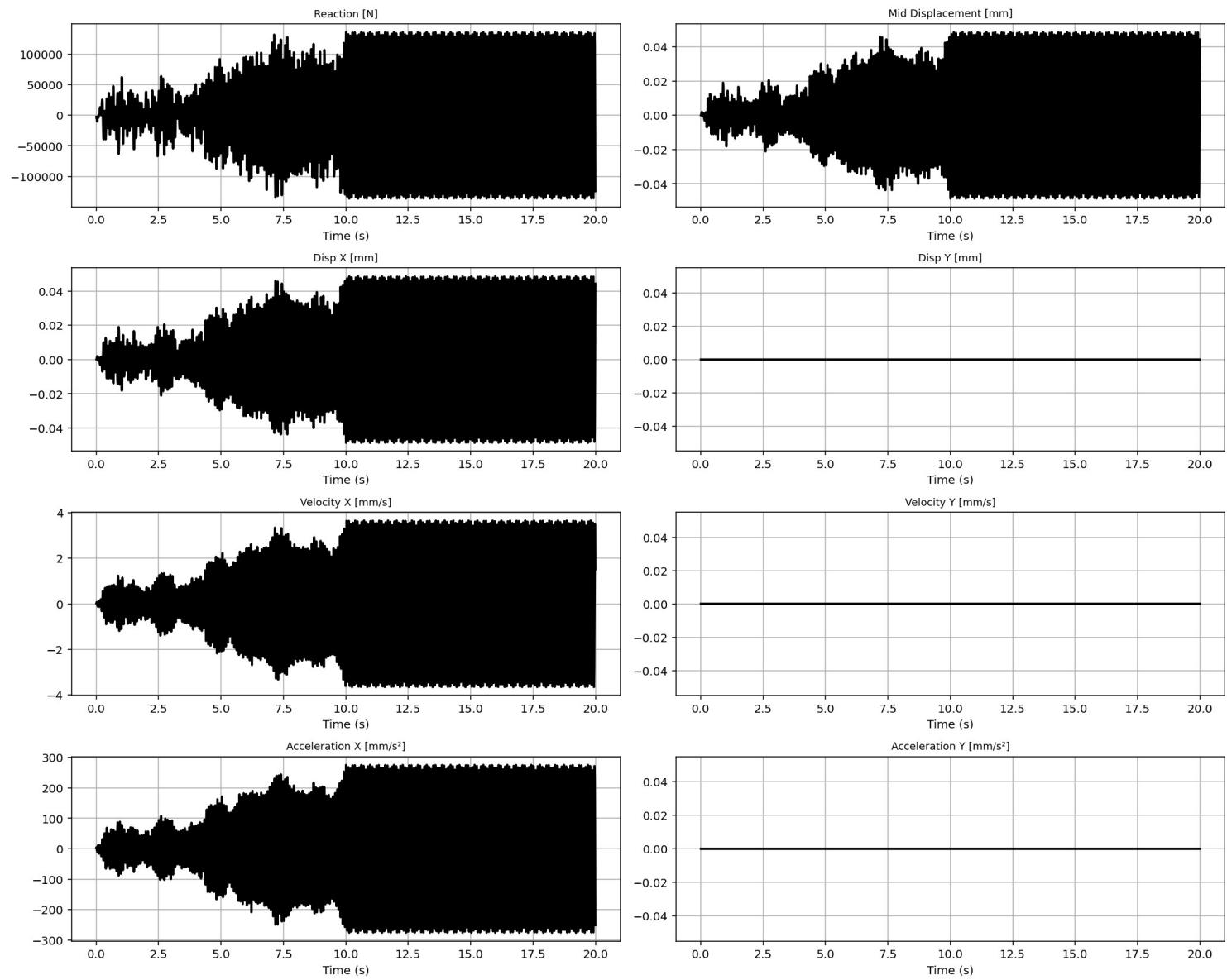
Displacement in Middle Span [mm]

IPython Console Files Help Variable Explorer Debugger Plots History

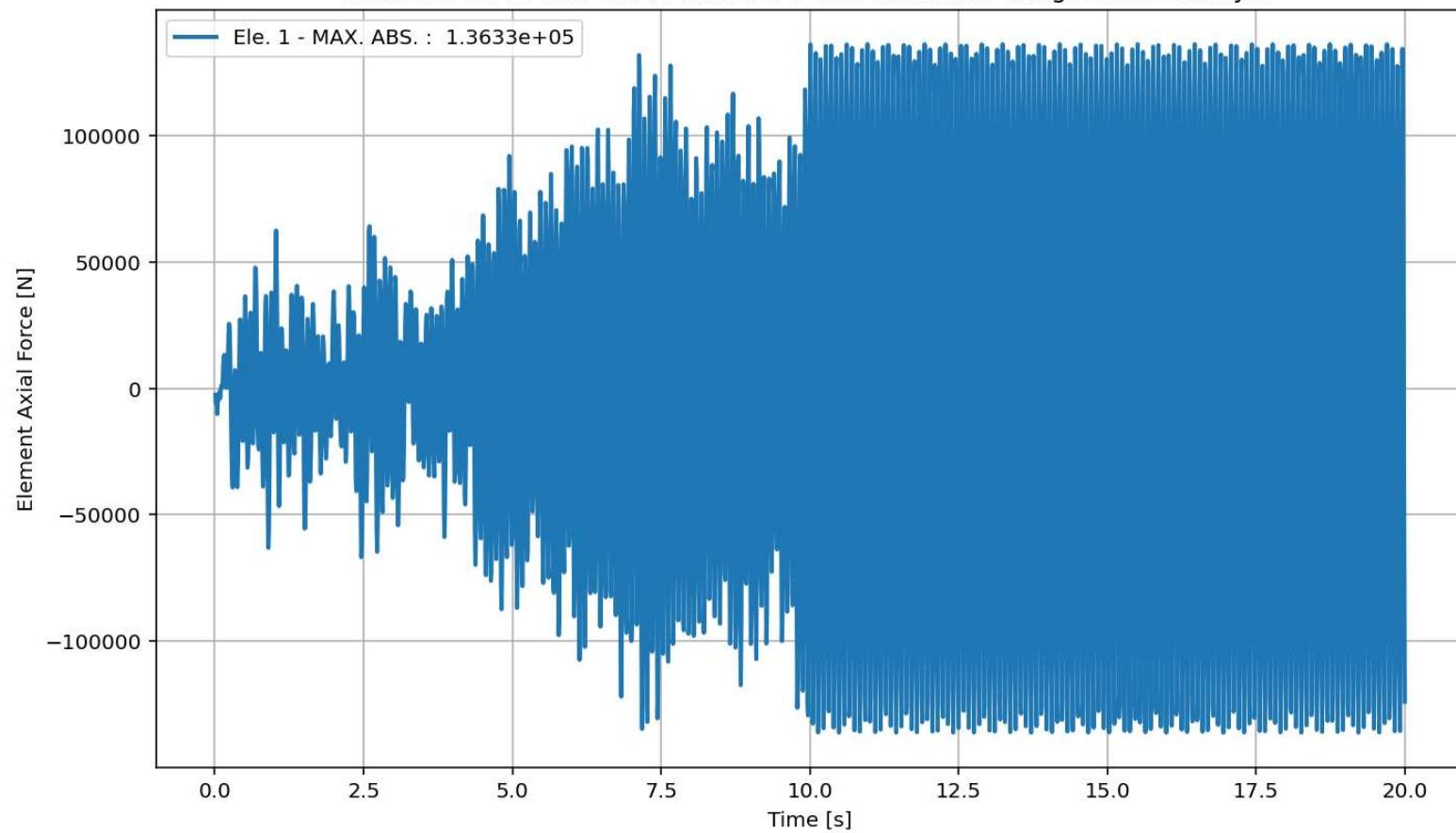
Inline Conda: anaconda3 (Python 3.12.7) ✓ LSP: Python Line 48, Col 56 UTF-8 CRLF RW Mem 38%

Base Reaction and Displacement of Structure During Seismic Analysis

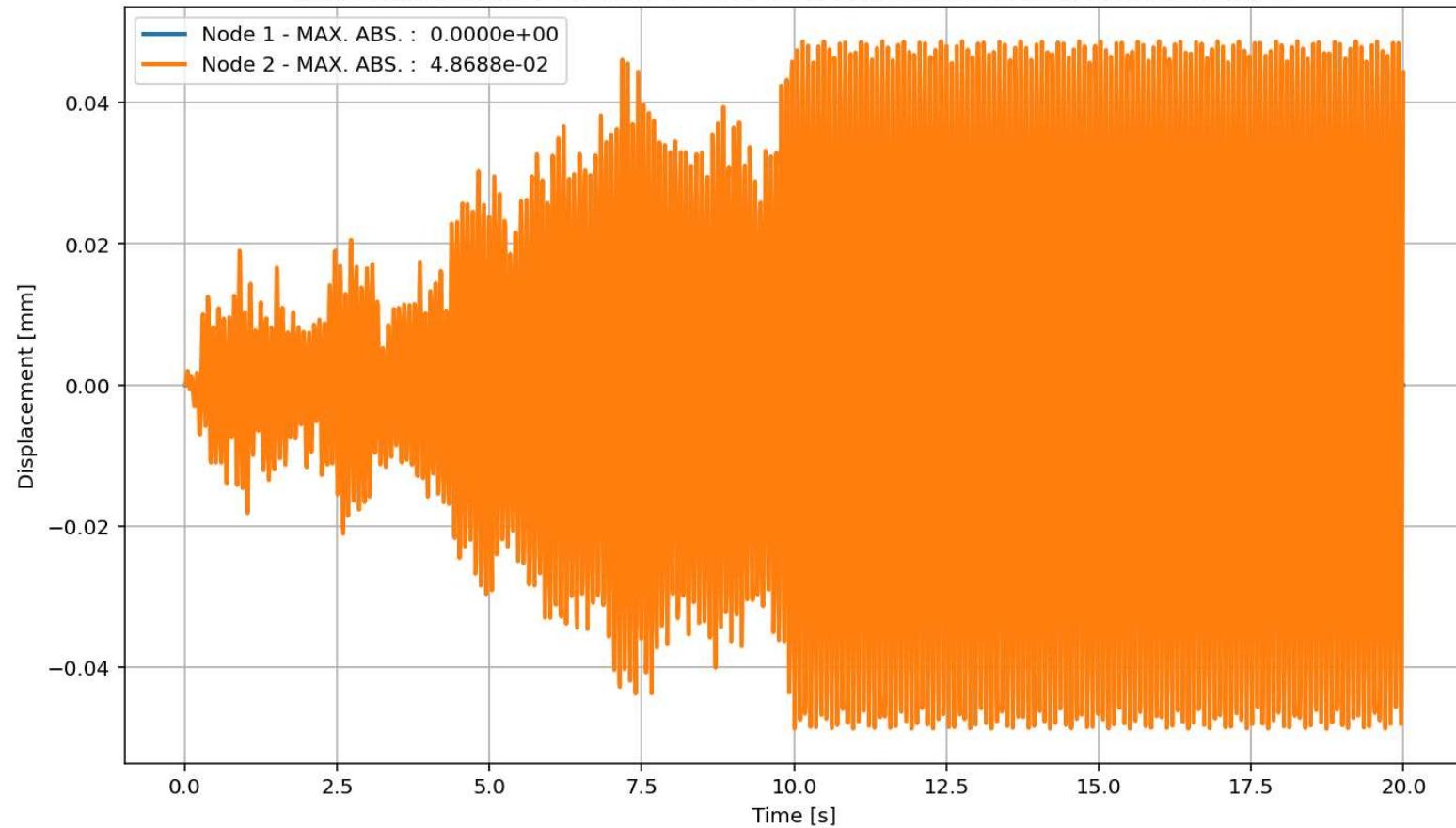




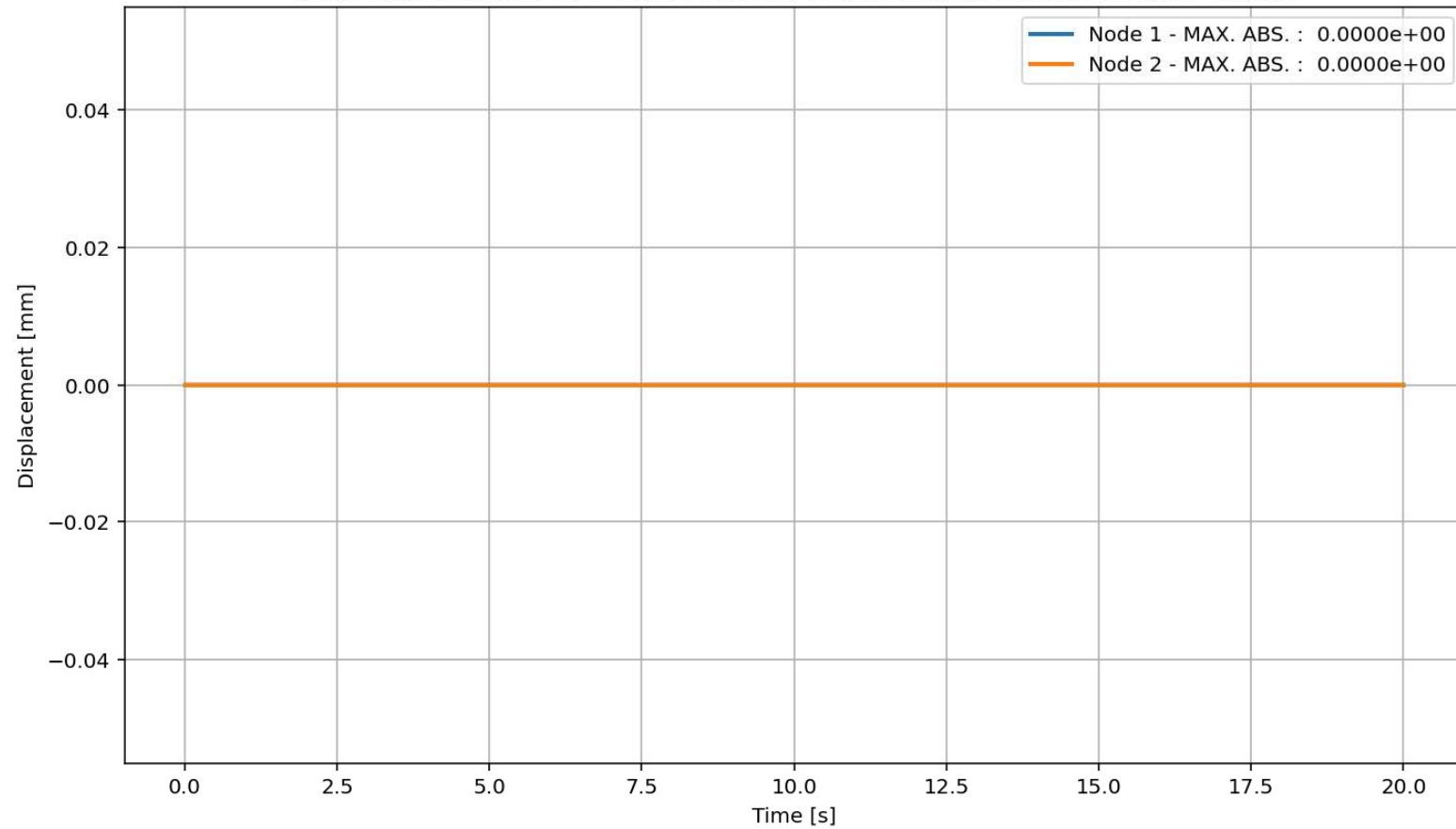
elements force in X Dir. vs Time for Beam Element During Seismic Analysis

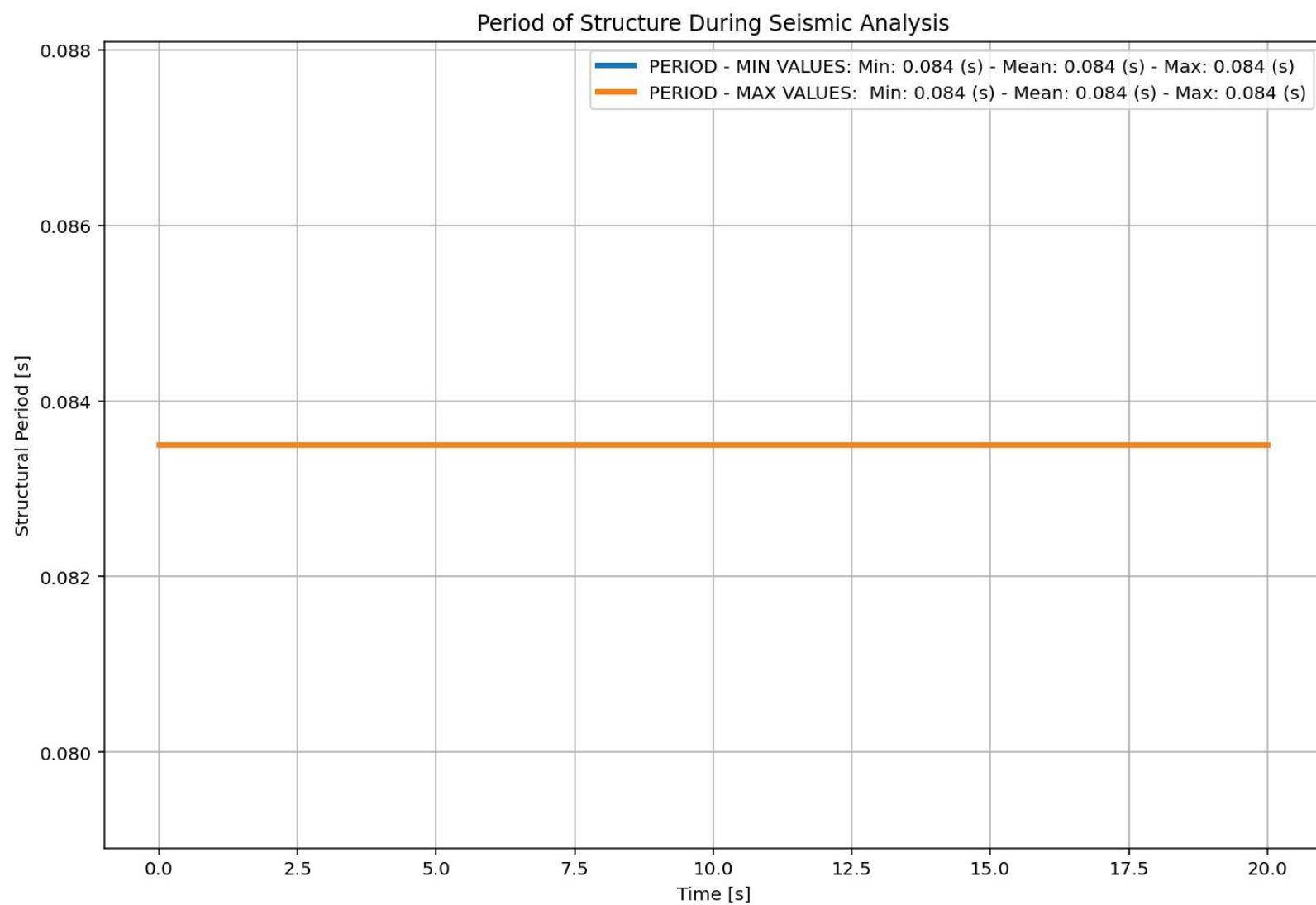


Node Displacements in X Dir. vs Time for Beam Element During Seismic Analysis

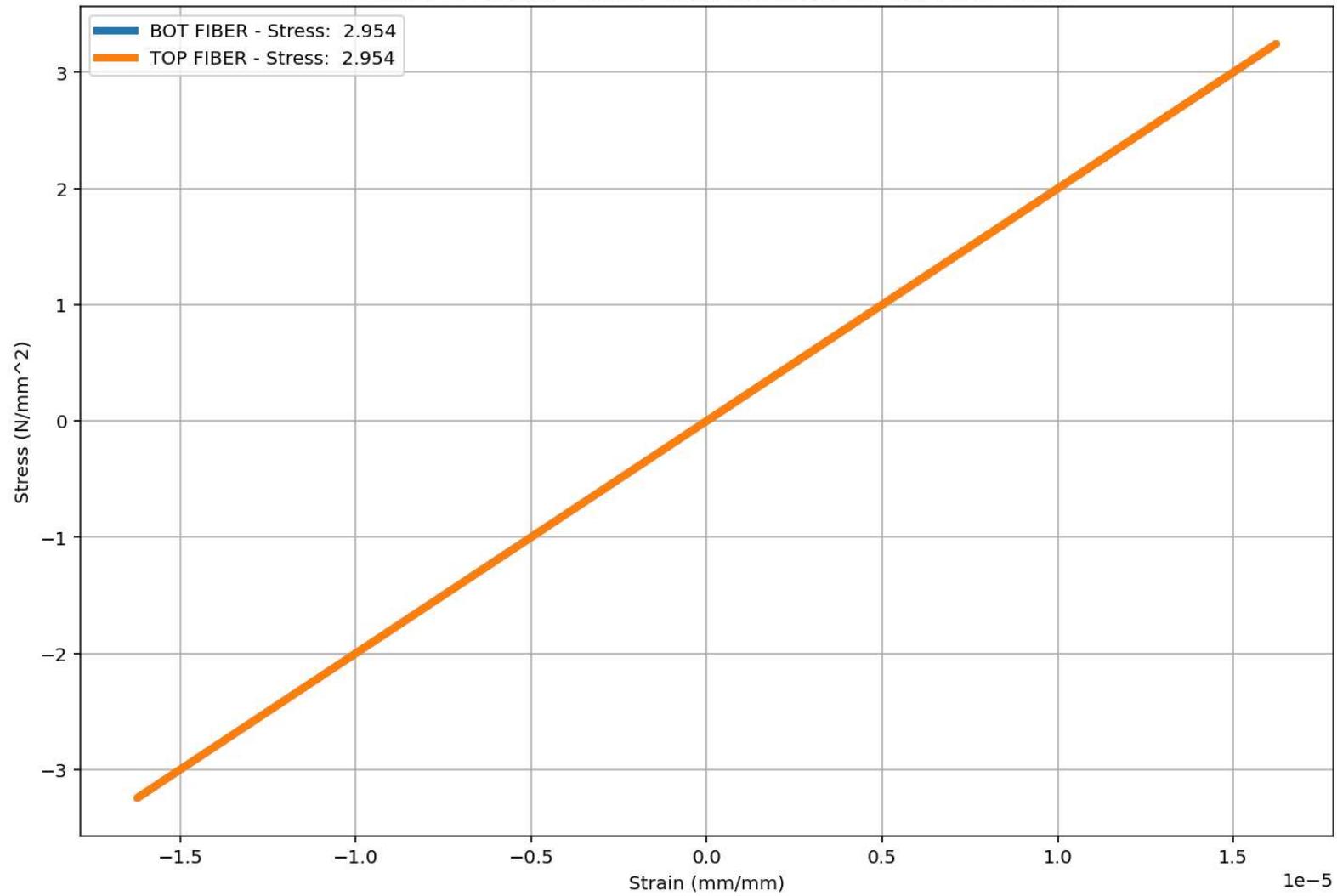


Node Displacements in Y Dir. vs Time for Beam Element During Seismic Analysis





Behavior of column - Stress-strain of Top and Bottom Fibers Curve



1e7 Last Data of Base Axial-Displacement Analysis - Ductility Ratio: 13.8889 - Over Strength Factor: 1.0237

