

Thermodynamics, Wave Motion and Optics (PHYS201)
 Participation 1

Suppose a speaker is mounted to a stand and attached to a spring having spring constant $k = 10.0 \text{ N/m}$ (so it moves in a SHM). The total mass of the stand and speaker is 2.5 kg , and the amplitude of this unit's motion is 0.500 m .

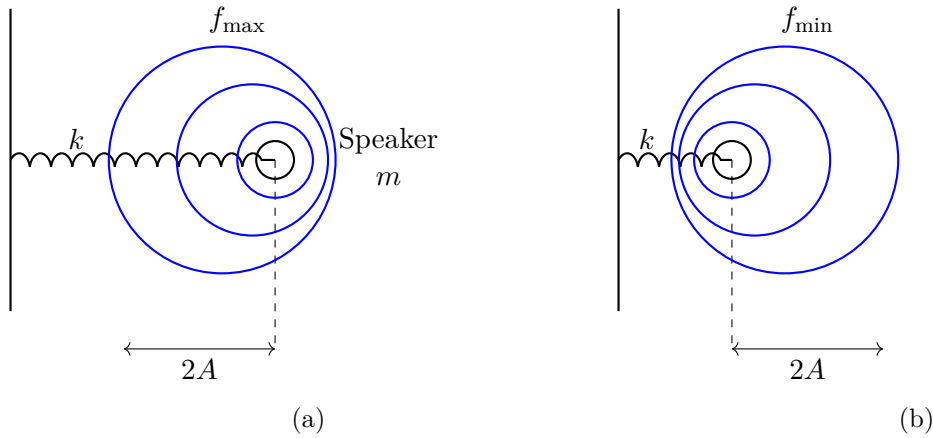


Figure 1

- (a) If the speaker emits sound waves of frequency 450 Hz , determine the highest and lowest frequencies heard by the person to the right of the speaker.

$$k = 10.0 \text{ N/m} \quad m = 2.5 \text{ kg} \quad A = 0.500 \text{ m} \quad f = 450 \text{ Hz}. \quad (1)$$

$$f' = f \left(\frac{v \pm v_s}{v \pm v_o} \right) \quad (2)$$

$$f_{\max} = f \left(\frac{v + v_s}{v} \right) \quad (3)$$

$$f_{\min} = f \left(\frac{v - v_s}{v} \right). \quad (4)$$

$$v_{\max} = -v_{\min} = A \sqrt{\frac{k}{m}} \quad (5)$$

$$= 0.500 \sqrt{\frac{10.0}{2.5}} \quad (6)$$

$$= 1 \text{ m/s} \quad (7)$$

$$\cdot \quad (8)$$

$$f_{\max} = 450 \left(\frac{343 + 1}{343} \right) \quad (9)$$

$$= 451 \text{ Hz} \quad (10)$$

$$f_{\min} = 450 \left(\frac{343 - 1}{343} \right) \quad (11)$$

$$= 449 \text{ Hz.} \quad (12)$$

- (b) If the maximum sound level heard by the person is 60.0 dB when he is closest to the speaker, 1.00 m away, what is the minimum sound level heard by the observer? Assume that the speed of sound is 343 m/s.

$$\beta_{\max} = 60.0 \text{ dB} \quad \beta = 10 \log_{10} \left(\frac{I}{I_0} \right) \quad I = \frac{P}{4\pi r^2}. \quad (13)$$

$$\beta_{\max} - \beta_{\min} = 10 \log_{10} \left(\frac{I_{\max}}{I_0} \right) - 10 \log_{10} \left(\frac{I_{\min}}{I_0} \right) \quad (14)$$

$$= 10 \log_{10} \left(\frac{I_{\max}}{I_{\min}} \right) \quad (15)$$

$$= 10 \log_{10} \left(\frac{r_{\min}}{r_{\max}} \right)^2 \quad (16)$$

$$= 20 \log_{10} \left(\frac{r_{\min}}{r_{\max}} \right) \quad (17)$$

$$= 20 \log_{10} \left(\frac{d + 2A}{d} \right) \quad (18)$$

$$= 20 \log_{10} \left(\frac{1 + 2(0.500)}{1} \right) \quad (19)$$

$$= 6.02 \text{ dB.} \quad (20)$$

$$\beta_{\min} = 60.0 - 6.02 \quad (21)$$

$$= 53.98 \text{ dB.} \quad (22)$$