Induced E-Field:  $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$ Coulomb's Law:  $\mathbf{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\mathbf{r}|^2} \hat{\mathbf{r}}$ Current Density:  $J = \sigma E$ Wave Equation:  $\nabla^2 \mathbf{E} - \mu \epsilon \frac{\partial^2 \mathbf{E}}{\partial t^2} = 0$ Electric Field:  $\mathbf{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{|\mathbf{r}|^2} \hat{\mathbf{r}}$ Continuity Eq.  $\nabla \cdot \mathbf{J} = -$ Ohm's Law: V = IRWave Speed:  $v = \frac{1}{\sqrt{\mu\epsilon}}$ Gauss's Law:  $\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$ Biot-Savart Law:  $\mathbf{B} = \frac{\mu_0}{4\pi} \int \frac{Id\mathbf{l} \times \hat{\mathbf{r}}}{|\mathbf{r}|^2}$ Electric Potential:  $V = -\int_{0}^{\epsilon_0} \mathbf{E} \cdot d\mathbf{l}$ Transmission Coeff:  $T = 1 + \Gamma$ Ampere's Law:  $\oint \mathbf{H} \cdot d\mathbf{l} = I_{\text{enc}}$ Impedance:  $Z = \sqrt{\frac{\mu}{\epsilon}}$ **E** and V:  $\mathbf{E} = -\nabla V$ Snell's Law:  $\frac{\sin \theta_1}{\sin \theta_2} = \frac{v_1}{v_2}$ Magnetic Flux Density:  $B = \mu H$ Laplace's Equation:  $\nabla^2 V = 0$ Faraday's Law:  $\mathcal{E} = -\frac{d\Phi}{dt}$ Poynting vector:  $S = E \times H$ Poisson's Equation:  $\nabla^2 V = -\frac{\rho_v}{\epsilon}$ Normal Incidence Reflection Coeff:  $\Gamma = \frac{Z_2 - Z_1}{Z_2 + Z_1}$ Lorentz force:  $\mathbf{F} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$ Maxwell's Equations:  $\nabla \cdot \mathbf{E} = \frac{\rho_v}{\epsilon_0}$ ,  $\nabla \cdot \mathbf{B} = 0$ ,  $\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$ ,  $\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$ General Interface Conditions:  $E_{1t} = E_{2t}, D_{1n} - D_{2n} = \rho_s; H_{1t} - H_{2t} = J_s^*, B_{1n} = B_{2n}$ \* Dielectric-Dielectric  $\implies \rho_s = J_s = 0$ . Dielectric-Conductor  $\implies E_t = B_n = 0, D_{1n} = \rho_s, H_{1t} = J_s^*$ .  $\int \frac{1}{(a^2 \pm x^2)^{3/2}} dx = \frac{x}{a^2 \sqrt{a^2 \pm x^2}}, \int \frac{x dx}{(a^2 + x^2)^{3/2}} = \frac{-1}{\sqrt{a^2 + x^2}}, \int \frac{1}{x^2 + a^2} = \frac{1}{a} \tan^{-1} \left(\frac{x}{a}\right), \int \frac{x^2 dx}{(a^2 + x^2)^{3/2}} = \frac{-x}{\sqrt{a^2 + x^2}} + \ln(x + \sqrt{a^2 + x^2})$ Cylindrical Coordinates: Spherical Coordinates: Vector Theorems: Cylinarical Coordinates: Spherical Coordinates.  $\nabla f = \frac{\partial f}{\partial r} \hat{\mathbf{r}} + \frac{1}{r} \frac{\partial f}{\partial \theta} \hat{\boldsymbol{\theta}} + \frac{\partial f}{\partial z} \hat{\mathbf{k}} \qquad \nabla f = \frac{\partial f}{\partial r} \hat{\mathbf{r}} + \frac{1}{r} \frac{\partial f}{\partial \theta} \hat{\boldsymbol{\theta}} + \frac{1}{r \sin \theta} \frac{\partial f}{\partial \phi} \hat{\boldsymbol{\phi}}$   $\nabla \cdot \mathbf{F} = \frac{1}{r} \frac{\partial}{\partial r} (rF_r) + \frac{1}{r} \frac{\partial F_{\theta}}{\partial \theta} + \frac{\partial F_z}{\partial z} \qquad \nabla \cdot \mathbf{F} = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 F_r) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (\sin \theta F_{\theta}) + \frac{1}{r \sin \theta} \frac{\partial F_{\phi}}{\partial \phi}$   $\nabla \times \mathbf{F} = \frac{1}{r} \begin{vmatrix} \hat{\mathbf{r}} & r \hat{\boldsymbol{\theta}} & \hat{\mathbf{z}} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \theta} & \frac{\partial}{\partial z} \\ F_r & rF_{\theta} & F_z \end{vmatrix} \qquad \nabla \times \mathbf{F} = \frac{1}{r^2 \sin \theta} \begin{vmatrix} \hat{\mathbf{r}} & r \hat{\boldsymbol{\theta}} & r \sin \theta \hat{\boldsymbol{\phi}} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \theta} & \frac{\partial}{\partial \phi} \\ F_r & rF_{\theta} & r \sin \theta F_{\phi} \end{vmatrix}$   $\nabla^2 f = \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial f}{\partial r}) + \frac{1}{r^2} \frac{\partial^2 f}{\partial \theta^2} + \frac{\partial^2 f}{\partial z^2} \qquad \nabla^2 f = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \frac{\partial f}{\partial r}) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} (\sin \theta \frac{\partial f}{\partial \theta}) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 f}{\partial \phi^2}$  $\int_{V} (\nabla \cdot \mathbf{F}) \, dV = \int_{S} \mathbf{F} \cdot \hat{\mathbf{n}} \, dA$  $\int_{S} (\nabla \times \mathbf{F}) \cdot \hat{\mathbf{n}} \, dA = \int_{C} \mathbf{F} \cdot d\mathbf{r}$ **Vector Identities:**  $\nabla \cdot (\nabla \times \mathbf{F}) = 0$ 

 $\nabla \times (\nabla f) = 0$  $\nabla \cdot (\nabla f) = \nabla^2 f$ 

 $abla imes (
abla imes \mathbf{F}) = 
abla (
abla \cdot \mathbf{F}) - 
abla^2 \mathbf{F}$