

1 LEVERAGING MULTI-MESSENGER ASTROPHYSICS FOR DARK MATTER SEARCHES

By

Daniel Nicholas Salazar-Gallegos

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Today

ABSTRACT

3 I did Dark Matter with HAWC and IceCube. I also used Graph Neural Networks

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⁶ Today

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8 I love my friends. Thanks to everyone that helped me figure this out. Amazing thanks to the people
9 at LANL who supported me. Eames, etc Dinner Parties Jenny and her child Kaydince Kirsten, Pat,
10 Andrea Family. You're so far but so critical to my formation. Unconditional love. Roommate

TABLE OF CONTENTS

12	LIST OF TABLES	vii
13	LIST OF FIGURES	viii
14	LIST OF ABBREVIATIONS	xv
15	CHAPTER 1 INTRODUCTION	1
16	CHAPTER 2 DARK MATTER IN THE COSMOS	2
17	2.1 Introduction	2
18	2.2 Dark Matter Basics	3
19	2.3 Evidence for Dark Matter	4
20	2.4 Searching for Dark Matter: Particle DM	11
21	2.5 Sources for Indirect Dark Matter Searches	16
22	2.6 Multi-Messenger Dark Matter	18
23	CHAPTER 3 MULTIMESSENGER ASTROPHYSICS: DETECTING HIGH EN-	
24	ERGY NEUTRAL MESSENGERS	21
25	3.1 Introduction	21
26	3.2 Charged Particles in a Medium	21
27	3.3 Photons (γ)	22
28	3.4 Neutrinos (ν)	22
29	3.5 Opportunities to Combine for Dark Matter	22
30	CHAPTER 4 HIGH ALTITUDE WATER CHERENKOV (HAWC) OBSERVATORY .	24
31	4.1 The Detector	24
32	4.2 Events Reconstruction and Data Acquisition	24
33	4.3 Remote Monitoring	24
34	CHAPTER 5 ICECUBE NEUTRINO OBSERVATORY	25
35	5.1 The Detector	25
36	5.2 Events Reconstruction and Data Acquisition	25
37	5.3 Northern Test Site	25
38	CHAPTER 6 GLORY DUCK: MULTI-WAVELENGTH SEARCH FOR DARK MATT-	
39	TER ANNIHILATION TOWARDS DWARF SPHEROIDAL GALAX-	
40	IES	26
41	6.1 Introduction	26
42	6.2 Dataset and Background	28
43	6.3 Analysis	29
44	6.4 Likelihood Methods	34
45	6.5 HAWC Results	40
46	6.6 Glory Duck Combined Results	43
47	6.7 HAWC Systematics	48

48	6.8 <i>J</i> -factor distributions	49
49	6.9 Discussion and Conclusions	55
50	CHAPTER 7 MULTITHREADING HAWC ANALYSES FOR DARK MATTER	
51	SEARCHES	59
52	7.1 Introduction	59
53	7.2 Dataset and Background	59
54	7.3 Analysis	61
55	7.4 Likelihood Methods	64
56	7.5 Computational Methods: Multithreading	65
57	7.6 Analysis Results	71
58	7.7 Systematics	72
59	7.8 Conclusion and Discussion	73
60	CHAPTER 8 HEAVY DARK MATTER ANNIHILATION SEARCH WITH ICE-	
61	CUBE'S NORTH SKY TRACK DATA	81
62	CHAPTER 9 NU DUCK	82
63	APPENDIX A MULTI-EXPERIMENT SUPPLEMENTARY FIGURES	83
64	APPENDIX B MULTITHREADING SUPPLEMENTARY FIGURES	84
65	B.1 <code>mpu_analysis.py</code>	85
66	BIBLIOGRAPHY	94

LIST OF TABLES

68	Table 6.1	Summary of the relevant properties of the dSphs used in the present work. Column 1 lists the dSphs. Columns 2 and 3 present their heliocentric distance and galactic coordinates, respectively. Columns 4 and 5 report the J -factors of each source given from the \mathcal{GS} and \mathcal{B} independent studies and their estimated $\pm 1\sigma$ uncertainties. The values $\log_{10} J$ (\mathcal{GS} set) [45] correspond to the mean J -factor values for a source extension truncated at the outermost observed star. The values $\log_{10} J$ (\mathcal{B} set) [47] are provided for a source extension at the tidal radius of each dSph. Bolded sources are within HAWC's field of view and provided to the Glory Duck analysis.	34
77	Table 6.2	Summary of dSph observations by each experiment used in this work. A '-' indicates the experiment did not observe the dSph for this study. For Fermi-LAT, the exposure at 1 GeV is given. For HAWC, $ \Delta\theta $ is the absolute difference between the source declination and HAWC latitude. HAWC is more sensitive to sources with smaller $ \Delta\theta $. For IACTs, we show the zenith angle range, the total exposure, the energy range, the angular radius θ of the signal or ON region, the ratio of exposures between the background-control (OFF) and signal (ON) regions (τ), and the significance of gamma-ray excess in standard deviations, σ .	35
86	Table 7.1	Summary of the relevant properties of the dSphs used in the present work. Column 1 lists the dSphs. Columns 2 and 3 present their heliocentric distance and galactic coordinates, respectively. Column 4 reports the J -factors of each source given from the \mathcal{LS} studies and estimated $\pm 1\sigma$ uncertainties. The values $\log_{10} J$ (\mathcal{LS} set) [65] correspond to the mean J -factor values for a source extension truncated at 0.5° .	65
92	Table 7.2	Timing summaries for analyses for serial and multithreaded processes. M tasks is the number of functional-parallel tasks ran for the computation. $T_{p,c}$ is a single run time in hours:minutes:seconds for runs utilizing p nodes and c threads. Runs are run interactively on the same computer to maximize consistency. Empty entries are indicated with '-'. (\cdot) entries are estimated entries extrapolated from data earlier in the column.	69
98	Table 7.3	Speed up summaries for analyses for serial and multithreaded processes. M tasks is the number of functional-parallel tasks ran for the computation. $S_{p,c}$ is a single speedup comparison for runs utilizing p nodes and c threads. $[\cdot]$ are the estimated speedups calculated from Tab. 7.2, Eq. (7.10), and Eq. (7.5). Empty entries are indicated with '-'.	71
103	Proof I know how to include		

LIST OF FIGURES

105	Figure 2.1	Rotation curve fit to NGC 6503 from [7]. Dashed line is the contribution 106 from visible matter. Dotted curves are from gas. Dash-dot curves are from 107 dark matter (DM). Solid line is the composite contribution from all matter 108 and DM sources. Data are indicated with bold dots with error bars. Data 109 agree strongly with a matter + DM composite prediction.	5
110	Figure 2.2	Light from distant galaxy is bent in unique ways depending on the distribution 111 of mass between the galaxy and Earth. Yellow dashed lines indicate where 112 the light would have gone if the matter were not present [8].	7
113	Figure 2.3	(left) Optical image of galactic cluster 1E0657-558. (right) X-ray image of the 114 cluster with redder meaning hotter and higher baryon density. (both) Green 115 contours are reconstruction of gravity contours from weak lensing. White 116 rings are the best fit mass maxima at 68.3%, 95.5%, and 99.7% confidence. 117 The matter maxima of the clusters are clearly separated from x-ray maxima. [9]	8
118	Figure 2.4	Plank CMB sky. Sky map features small variations in temperature in primor- 119 dial light. These anisotropies are used to make inferences about the universe's 120 energy budget and developmental history. [10]	9
121	Figure 2.5	Observed Cosmic Microwave Background power spectrum as a function of 122 multipole moment from Plank [10]. Blue line is best fit model from Λ CDM. 123 Red points and lines are data and error, respectively.	10
124	Figure 2.6	Predicted power spectra of CMB for different $\Omega_m h^2$ values for fixed baryon 125 density from [11]. (left) Low $\Omega_m h^2$ increases the prominence of first and 126 second peaks. (middle) $\Omega_m h^2$ is most similar to the observed power spectrum. 127 The second and third peaks are similar in height. (right) $\Omega_m h^2$ is large which 128 suppresses the first peak and raises the prominence of the third peak.	10
129	Figure 2.7	The Standard Model (SM) of particle physics. Figure taken from http://www.quantumdiaries.org/2014/03/14/the-standard-model-a-beautiful-but-flawed-theory/	12
132	Figure 2.8	Simplified Feynman diagram demonstrating with different ways DM can 133 interact with SM particles. The 'X's refer to the DM particles whereas the 134 SM refer to fundamental particles in the SM. The large circle in the center 135 indicates the vertex of interaction and is purposely left vague. The colored 136 arrows refer to different directions of time as well as their respective labels. 137 The arrows indicate the initial and final state of the DM -SM interaction in time.	13

138	Figure 2.9 A single jet event in ATLAS detector from 2017 [16]. Jet momentum was 139 observed to be 1.9 TeV. Missing transverse momentum was observed to be 140 1.9 TeV compared to the initial transverse momentum of the event was 0. 141 Implied MET is traced by a red dashed line in event display.	14
142	Figure 2.10 More detailed pseudo-Feynman diagram of particle cascade from dark matter 143 annihilation into 2 quarks. The quarks hadronize and down to stable particles 144 like γ or the anti-proton (p^-). Diagram pulled from ICRC 2021 presentation 145 on DM annihilation search [17].	15
146	Figure 2.11 Dark Matter (DM) decay spectrum for $b\bar{b}$ initial state and γ final state. Redder 147 spectra are for larger DM masses. Bluer spectra are light DM masses. x is a 148 unitless factor defined as the ratio of the mass of DM, m_χ , and the final state 149 particle energy E_γ . Figure from [19].	17
150	Figure 2.12 Different dark matter density profiles compared. Some models produce ex- 151 ceptionally large densities at small r [20].	18
152	Figure 2.13 The Milky Way Galaxy in photons (γ) and neutrinos (ν) [22]. The Galactic 153 center is at $l=0^\circ$ and is the brightest region in all panels. (top) An Optical 154 color image of the Milky Way galaxy seen from Earth. Clouds of gas and dust 155 obscure some light from stars. (2nd down) Integrated flux of γ -rays observed 156 by the Fermi-LAT telescope [23]. (middle) Expected neutrino emission 157 that corresponds with Fermi-LAT observations. (2nd up) Expected neutrino 158 emission profile after considering detector systematics of IceCube. (bottom) 159 Observed neutrino emission from region of the galactic plane. Substantial 160 neutrino emission was detected.	19
161	Figure 2.14 Dark Matter annihilation spectra for different final state particle and standard 162 model annihilation channels [24]. Photons (red), e^\pm (green), \bar{p} (blue), ν (black).	20
163	Figure 3.1 TODO: Show a nuclear reactor with cherenkov radiation[NEEDS A SOURCE][FACT 164 CHECK THIS]	22
165	Figure 3.2 TODO: absorption spectrum of liquid and solid water[NEEDS A SOURCE][FACT 166 CHECK THIS]	23

167	Figure 6.1 Sensitivities of five gamma-ray experiments compared to percentages of the 168 Crab nebula's emission and dark matter annihilation. Solid lines present 169 estimated sensitivities to power law spectra [FACT CHECK THIS]for each 170 experiment. Green lines are Fermi-LAT sensitivities where lighter green is 171 the sensitivity to the galactic center and dark green is its sensitivity to higher 172 declinations. Orange, red, and purple solid lines represent the MAGIC, HESS, 173 and VERITAS 50 hour sensitivities respectively. The maroon and brown lines 174 are the HAWC 1 year and 5 year sensitivities. Across four decades of gamma- 175 ray energy, these experiments have similar sensitivities on the order 10^{-12} 176 erg cm $^{-2}$ s $^{-1}$. The dotted lines are estimated dark matter fluxes assuming 177 $m_\chi = 5$ TeV DM annihilating to bottom quarks (red), tau leptons (blue), 178 and W bosons (green). Faded gray lines outline percentage flux of the Crab 179 nebula. Figure is an augmented version of [25]	27
180	Figure 6.2 Effect of Electroweak (EW) corrections on expected DM annihilation spec- 181 trum for $\chi\chi \rightarrow W^-W^+$. Solid lines are spectral models that consider EW 182 corrections. Dash-dot lines are spectral models without EW corrections. Red 183 lines are models for $M_\chi = 1$ TeV. Blue lines represent models for $M_\chi = 100$ 184 TeV. All models are sourced from the PPPC4DMID [44].	31
185	Figure 6.3 $\frac{dJ}{d\Omega}$ maps for Segue1 (top) and Coma Berenices (bottom). Origin is centered 186 on the specific dwarf spheroidal galaxies (dSph). X and Y axes are the 187 angular separation from the center of the dwarf. Plots of the remaining 11 188 dSph HAWC studied are linked in Fig. A.1.	33
189	Figure 6.4 Illustration of the combination technique showing a comparison between 190 $-2 \ln \lambda$ provided by four instruments (colored lines) from the observation 191 of the same dSph without any J nuisance and their sum, <i>i.e.</i> the resulting 192 combined likelihood (thin black line). According to the test statistics of 193 Equation (6.6), the intersection of the likelihood profiles with the line $-2 \ln \lambda$ 194 = 2.71 indicates the 95% C.L. upper limit on $\langle \sigma v \rangle$. The combined likelihood 195 (thin black line) shows a smaller value of upper limit on $\langle \sigma v \rangle$ than those 196 derived by individual instruments. We also show how the uncertainties on 197 the J factor effects the combined likelihood and degrade the upper limit on 198 $\langle \sigma v \rangle$ (thick black line). All likelihood profiles are normalized so that the global 199 minimum $\widehat{\langle \sigma v \rangle}$ is 0. We note that each profile depends on the observational 200 conditions in which a target object was observed. The sensitivity of a given 201 instrument can be degraded and the upper limits less constraining if the 202 observations are performed in non-optimal conditions such as a high zenith 203 angle or a short exposure time.	38
204	Figure 6.5 HAWC upper limits at 95% confidence level on $\langle \sigma v \rangle$ versus DM mass for 205 seven annihilation channels, using the set of J -factors from Ref. [53] The 206 solid line represents the observed combined limit. Dashed lines represent 207 limits from individual dSphs.	41

208	Figure 6.6 HAWC TS values for best fit $\langle\sigma v\rangle$ versus m_χ for seven SM annihilation channels with J factors from \mathcal{GS} . The solid black line shows the combined best fit TS values. The colored, dashed lines are the TS values for each of the 13 sources HAWC studied.	42
212	Figure 6.7 HAWC Brazil bands at 95% confidence level on $\langle\sigma v\rangle$ versus DM mass for seven annihilation channels with J -factors from \mathcal{GS} [53]. The solid line represents the combined limit from 13 dSphs. The dashed line is the expected limit. The green band is the 68% containment. The yellow band is the 95% containment.	43
217	Figure 6.8 Upper limits at 95% confidence level on $\langle\sigma v\rangle$ in function of the DM mass for eight annihilation channels, using the set of J factors from Ref. [53] (\mathcal{GS} set in Table 6.1). The black solid line represents the observed combined limit, the black dashed line is the median of the null hypothesis corresponding to the expected limit, while the green and yellow bands show the 68% and 95% containment bands. Combined upper limits for each individual detector are also indicated as solid, colored lines. The value of the thermal relic cross-section in function of the DM mass is given as the red dotted-dashed line [54].	44
226	Figure 6.9 Same as Fig. 6.8, using the set of J factors from Ref. [47, 55] (\mathcal{B} set in Table 6.1).	45
227	Figure 6.10 Comparisons of the combined limits at 95% confidence level for each of the eight annihilation channels when using the J factors from Ref. [53] (\mathcal{GS} set in Table 6.1), plain lines, and the J factor from Ref. [47, 55] (\mathcal{B} set in Table 6.1), dashed lines. The cross-section given by the thermal relic is also indicated [54].	47
231	Figure 6.11 Comparisons of the combined limits at 95% confidence level for a point source analysis and extended source using [53] \mathcal{GS} J-factor distributions and PPPC [44] annihilation spectra. Shown are the limits for Segue1 which will have the most significant impact on the combined limit. 6 of the 7 DM annihilation channels are shown. Solid lines are extended source studies. Dashed lines are point source studies. Overall, the extended source analysis improves the limit by a factor of 2.	49
238	Figure 6.12 Same as Fig. 6.11 on Coma Berenices. This dSph also contributes significantly to the limit. The limits are identical in this case.	50
240	Figure 6.13 Comparison of combined limits when correcting for HAWC's pointing systematic. All DM annihilation channels are shown. The solid black line is the ratio between published limit to the declination corrected limit. The blue solid line or "Combined_og" represented the limits computed for Glory Duck. The solid orange line or "Combined_ad" represented the limits computed after correcting for the pointing systematic.	51

246	Figure 6.14 Differential map of dJ/Ω from model built in Section 6.8.1 and profiles provided directly from authors. (Top) Differential from Segue1. (bottom) Differential from Coma Berenices. Note that their scales are not the same. Segue1 shows the deepest discrepancies which is congruent with its large uncertainties. Both models show anuli where unique models become apparent.	52
251	Figure 6.15 HAWC limits for Coma Berenices (top) and Segue1 (bottom) for two different map sets. Blue lines are limits calculated on maps with poor model representation. Orange lines are limits calculated on spatial profiles provided by the authors of [45]. Black line is the ratio of the poor spatial model limits to the corrected spatial models. The left y-axis measures $\langle\sigma v\rangle$ for the blue and orange lines. The right y-axis measures the ratio and is unitless.	53
257	Figure 6.16 Comparisons between the J -factors versus the angular radius for the computation of J factors from Ref. [53] (\mathcal{GS} set in Table 6.1) in blue and for the computation from Ref. [47, 55] (\mathcal{B} set in Tab. 6.1) in orange. The solid lines represent the central value of the J -factors while the shaded regions correspond to the 1σ standard deviation.	56
262	Figure 6.17 Comparisons between the J -factors versus the angular radius for the computation of J factors from Ref. [53] (\mathcal{GS} set in Tab. 6.1) in blue and for the computation from Ref. [47, 55] (\mathcal{B} set in Tab. 6.1) in orange. The solid lines represent the central value of the J -factors while the shaded regions correspond to the 1σ standard deviation.	57
267	Figure 7.1 Difference between spectral hypotheses from PPPC [44] and HDM [64]. Shown is the expected DM annihilation spectrum for $\chi\chi \rightarrow W^-W^+$. Solid lines are spectral models with EW corrections from the PPPC. Dash-dot lines are spectral models from HDM. Red lines are models for $M_\chi = 1$ TeV. Blue lines represent models for $M_\chi = 100$ TeV.	62
272	Figure 7.2 Photon spectra for $\chi\chi \rightarrow \gamma\gamma$ (left) and $\chi\chi \rightarrow ZZ$ (right) after gaussian convolution of line features. Both spectra have δ -features at photon energies equal to the DM mass. Bluer lines are annihilation spectra with lower DM mass. Redder lines are spectra from larger DM mass. All Spectral models are sourced from the Heavy Dark Matter models [64]. Axes are drawn roughly according to the energy sensitivity of HAWC.	63
278	Figure 7.3 $\frac{dJ}{d\Omega}$ maps for Coma Berenices, Draco, Segue1, and Sextans. Columns are divided for the $\pm 1\sigma$ uncertainties in $dJ/d\Omega$ around the mean value from \mathcal{LS} [65]. Origin is centered on the specific dwarf spheroidal galaxies (dSph). θ and ϕ axes are the angular separation from the center of the dwarf	64

282	Figure 7.4 Infographic on how jobs and DM computation was organized in Section 6.3.	66
283		
284		
285		
286		
287		
288		
289		
290	Figure 7.5 Graphic of Gustafson parallel coding pattern. f_s is the fraction of a program, in time, spent on serial computation. f_p is the fraction of computing time that is parallelizable. T_p is the total time for a parallel program to run. T_1 is the total time for a parallel program to run if only 1 processor is allocated. P_N is the N -th processor where it's row is the computation the processor performs. The Gustafson pattern is most similar to what is implemented for this analysis. Figure is pulled from [67].	67
291		
292		
293		
294		
295		
296		
297	Figure 7.6 Task chart for one multi-threaded job developed for this project. Green blocks indicate a shared resource across the threads AND computation performed serially. Red blocks indicate functional parallel processing within each thread. 3 threads are represented here, yet many more can be employed during the full analysis. Jobs are defined by the SOURCE as these require unique maps to be loaded into the likelihood estimator. The m_χ , CHAN, and $\langle\sigma v\rangle$ variables are entered into the thread pool and allocated as evenly as possible across the threads.	69
298		
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300		
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303		
304		
305	Figure 7.7 TODO: fill this out	72
306	Figure 7.8 TODO: fill this out	73
307	Figure 7.9 TODO: fill this out	74
308	Figure 7.10 TODO: fill this out	75
309	Figure 7.11 TODO: fill this out	76
310	Figure 7.12 TODO: fill this out	77
311	Figure 7.13 TODO: fill this out	78
312	Figure 7.14 TODO: show p1 and m1 limits around[NEEDS A SOURCE][FACT CHECK THIS]	79
313		
314	Figure 7.15 TODO: there will be 2[NEEDS A SOURCE][FACT CHECK THIS]	80

315	Figure A.1 Sister figure to Figure 6.3. Sources in the first row from left to right: Bootes 316 I, Canes Venatici I, II. In second row: Draco, Hercules, Leo I. In the first row: 317 Leo II, Leo IV, Sextans. In the final row: Ursa Major I, Ursa Major II.	83
318	Figure B.1 Sister figure to Figure 7.2 for remaining SM primary annihilation channels 319 studied for this thesis. These did not require any post generation smoothing 320 and so are directly pulled from [64] with a binning scheme most helpful for a 321 HAWC analysis.	84

LIST OF ABBREVIATIONS

- 323 **MSU** Michigan State University
324 **LANL** Los Alamos National Laboratory
325 **DM** Dark Matter
326 **SM** Standard Model
327 **HAWC** High Altitude Water Cherenkov Observatory
328 **dSph** Dwarf Spheroidal Galaxy

CHAPTER 1

INTRODUCTION

330 Is the text not rendering right? Ah ok it knows im basically drafting the doc still

CHAPTER 2

331

DARK MATTER IN THE COSMOS

332 **2.1 Introduction**

333 The dark matter problem can be summarized in part by the following thought experiment.

334 Let us say you are the teacher for an elementary school classroom. You take them on a field
335 trip to your local science museum and among the exhibits is one for mass and weight. The exhibit
336 has a gigantic scale, and you come up with a fun problem for your class.

337 You ask your class, "What is the total weight of the classroom? Give your best estimation to
338 me in 30 minutes, and then we'll check your guess on the scale. If your guess is within 10% of the
339 right answer, we will stop for ice cream on the way back."

340 The students are ecstatic to hear this, and they get to work. The solution is some variation of
341 the following strategy. The students should give each other their weight or best guess if they do
342 not know. Then, all they must do is add each student's weight and get a grand total for the class.
343 The measurement on the giant scale should show the true weight of the class. When comparing
344 the measured weight to your estimation, multiply the measurement by 1.0 ± 0.1 to get the $\pm 10\%$
345 tolerances for your estimation.

346 Two of your students, Sandra and Mario, return to you with a solution.

347 They say, "We weren't sure of everyone's weight. We used 65 lbs. for the people we didn't
348 know and added everyone who does know. There are 30 of us, and we got 2,000 lbs.! That's a ton!"

349 You estimated 1,900 lbs. assuming the average weight of a student in your class was 60 lbs.
350 So, you are pleased with Sandra's and Mario's answer. You instruct your students to all gather on
351 the giant scale and read off the weight together. To all your surprise, the scale reads *10,000 lbs.*!
352 10,000 is significantly more than a 10% error from 2,000. In fact, it is approximately 5 times more
353 massive than either your or your students' estimates. You think to yourself and conclude there
354 must be something wrong with the scale. You ask an employee to check the scale and verify it is
355 well calibrated. They confirm that the scale is in working order. You weigh a couple of students
356 individually to assess that the scale is well calibrated. Sandra weighs 59 lbs., and Mario weighs

357 62 lbs., typical weights for their age. You then weigh each student individually and see that their
358 weights individually do not deviate greatly from 60 lbs. So, where does all the extra weight come
359 from?

360 This thought experiment serves as an analogy to the Dark Matter problem. The important
361 substitution to make however is to replace the students with stars and the classroom with a galaxy,
362 say the Milky Way. Individually the mass of stars is well measured and defined with the Sun as our
363 nearest test case. However, when we set out to measure the mass of a collection of stars as large as
364 galaxies, our well-motivated estimation is wildly incorrect. There simply is no way to account for
365 this discrepancy except without some unseen, or dark, contribution to mass and matter in galaxies.
366 I set out in my thesis to narrow the possibilities of what this Dark Matter could be.

367 This chapter is organized like the following... **TODO: Text should look like ... Chapter x has**
368 **blah blah blah.**

369 2.2 Dark Matter Basics

370 Presently, a more compelling theory of cosmology that includes Dark Matter (DM) in order
371 to explain a variety of observations is Λ Cold Dark Matter, or Λ CDM. I present the evidence
372 supporting Λ CDM in Section 2.3 yet discuss the conclusions of the Λ CDM model here. According
373 to Λ CDM fit to observations on the Cosmic Microwave Background (CMB), DM is 26.8% of the
374 universe's current energy budget. Baryonic matter, stuff like atoms, gas, and stars, contributes to
375 4.9% of the universe's current energy budget [1, 2, 3].

376 DM is dark; it does not interact readily with light at any wavelength. DM also does not interact
377 noticeably with the other standard model forces (Strong and Weak) at a rate that is readily observed
378 [3]. DM is cold, which is to say that the average velocity of DM is below relativistic speeds [1].
379 'Hot' DM would not likely manifest the dense structures we observe like galaxies, and instead
380 would produce much more diffuse galaxies than what is observed [3, 1]. DM is old; it played a
381 critical role in the formation of the universe and the structures within it [1, 2].

382 Observations of DM have so far been only gravitational. The parameter space available to what
383 DM could be therefore is extremely broad. The broad DM parameter space is iteratively tested in

384 DM searches by supposing a hypothesis that has not yet been ruled out and performing observations
385 to test them. When the observations yield a null result, the parameter space is constrained further.
386 I present some approaches for DM searches in Section 2.4.

387 **2.3 Evidence for Dark Matter**

388 Dark Matter (DM) has been a looming problem in physics for almost 100 years. Anomalies
389 have been observed by astrophysicists in galactic dynamics as early as 1933 when Fritz Zwicky
390 noticed unusually large velocity dispersion in the Coma cluster. Zwicky's measurement was the
391 first recorded to use the Virial theorem to measure the mass fraction of visible and invisible matter
392 in celestial bodies [4]. From Zwicky in [5], "*If this would be confirmed, we would get the surprising*
393 *result that dark matter is present in much greater amount than luminous matter.*" Zwicky's and
394 others' observation did not instigate a crisis in astrophysics because the measurements did not
395 entirely conflict with their understanding of galaxies [4]. In 1978, Rubin, Ford, and Norbert
396 measured rotation curves for ten spiral galaxies [6]. Rubin et al.'s 1978 publication presented a
397 major challenge to the conventional understanding of galaxies that could no longer be dismissed by
398 measurement uncertainties. Evidence has been mounting ever since for this exotic form of matter.
399 The following subsections provide three compelling pieces of evidence in support of the existence
400 of DM.

401 **2.3.1 First Clues: Stellar Velocities**

402 Zwicky, and later Rubin, measured the stellar velocities of various galaxies to estimate their
403 virial mass. The Virial Theorem upon which these observations are interpreted is written as

$$2T + V = 0. \quad (2.1)$$

404 Where T is the kinetic energy and V is the potential energy in a self-gravitating system. The
405 classical Newton's law of gravity from stars and gas was used for gravitational potential modeled in
406 the observed galaxies:

$$V = -\frac{1}{2} \sum_i \sum_{j \neq i} \frac{m_i m_j}{r_{ij}}. \quad (2.2)$$

407 Zwicky et al. measured just the velocities of stars apparent in optical wavelengths [5]. Rubin et al.
 408 added by measuring the velocity of the hydrogen gas via the 21 cm emission line of Hydrogen [6].
 409 The velocities of the stars and gas are used to infer the total mass of galaxies and galaxy clusters
 410 via Equation (2.1). An inferred mass is obtained from the luminosity of the selected sources. The
 411 two inferences are compared to each other as a luminosity to mass ratio which typically yielded [1]

$$\frac{M}{L} \sim 400 \frac{M_{\odot}}{L_{\odot}} \quad (2.3)$$

412 M_{\odot} and L_{\odot} referring to stellar mass and stellar luminosity, respectively. These ratios clearly indicate
 413 a discrepancy in apparent light and mass from stars and gas and their velocities.

414 Rubin et al. [6] demonstrated that the discrepancy was unlikely to be an underestimation of
 415 the mass of the stars and gas. The inferred "dark" mass was up to 5 times more than the luminous
 416 mass. This dark mass also needed to extend well beyond the extent of the luminous matter.

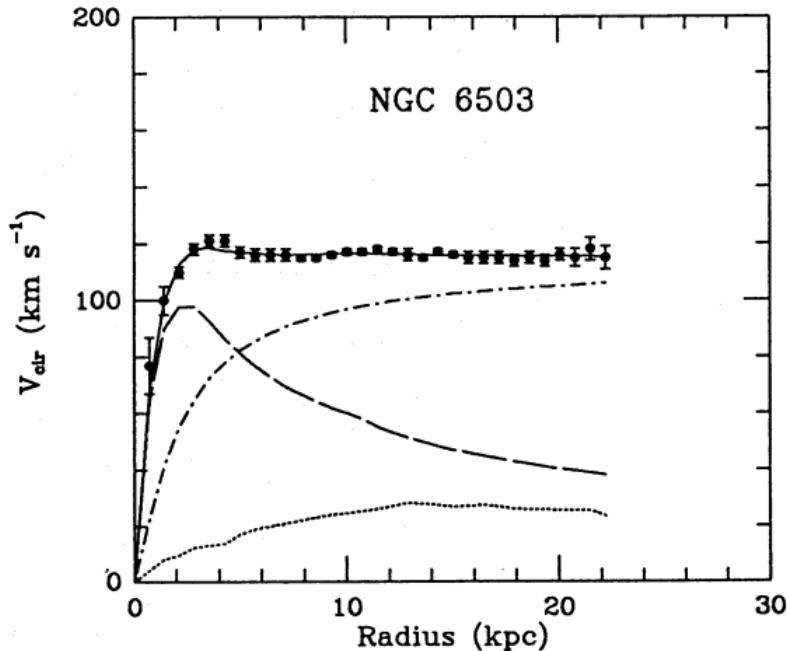


Figure 2.1 Rotation curve fit to NGC 6503 from [7]. Dashed line is the contribution from visible matter. Dotted curves are from gas. Dash-dot curves are from dark matter (DM). Solid line is the composite contribution from all matter and DM sources. Data are indicated with bold dots with error bars. Data agree strongly with a matter + DM composite prediction.

417 Figure 2.1 features one of many rotation curves plotted from the stellar velocities within galaxies.

418 The measured rotation curves mostly feature a flattening of velocities at higher radius which is not
419 expected if the gravity was only coming from gas and luminous matter. The extension of the
420 flat velocity region also indicates that the DM is distributed far from the center of the galaxy.
421 Modern velocity measurements include significantly larger objects, galactic clusters, and smaller
422 objects, dwarf galaxies. Yet, measurements along this regime are leveraging the Virial theorem
423 with Newtonian potential energies. We know Newtonian gravity is not a comprehensive description
424 of gravity. New observational techniques have been developed since 1978, and those are discussed
425 in the following sections.

426 **2.3.2 Evidence for Dark Matter: Gravitational Lensing**

427 Modern evidence for dark matter comes from new avenues beyond stellar velocities. Grav-
428 itational lensing from DM is a new channel from general relativity. General relativity predicts
429 aberrations in light caused by massive objects. In recent decades we have been able to measure the
430 lensing effects from compact objects and DM halos. Figure 2.2 shows how different massive ob-
431 jects change the final image of a faraway galaxy resulting from gravitational lensing. Gravitational
432 lensing developed our understanding of dark matter in two important ways.

433 Gravitational lensing provides additional compelling evidence for DM. The observation of two
434 merging galactic clusters in 2006, shown in Figure 2.3, provided a compelling argument for DM
435 outside the Standard Model. These clusters merged recently in astrophysical time scales. Galaxies
436 and star cluster have mostly passed by each other as the likelihood of their collision is low. Therefore,
437 these massive objects will mostly track the highest mass, dark and/or baryonic, density. Yet, the
438 intergalactic gas is responsible for the majority of the baryonic mass in the systems [4]. These gas
439 bodies will not phase through and will heat up as they collide together. The hot gas is located via
440 x-ray emission from the cluster. Two observations of the clusters were performed independently of
441 each other.

442 The first was the lensing of light around the galaxies due to their gravitational influences.
443 When celestial bodies are large enough, the gravity they exert bends space and time itself. The
444 warped space-time lenses light and will deflect in an analogous way to how glass lenses will bend

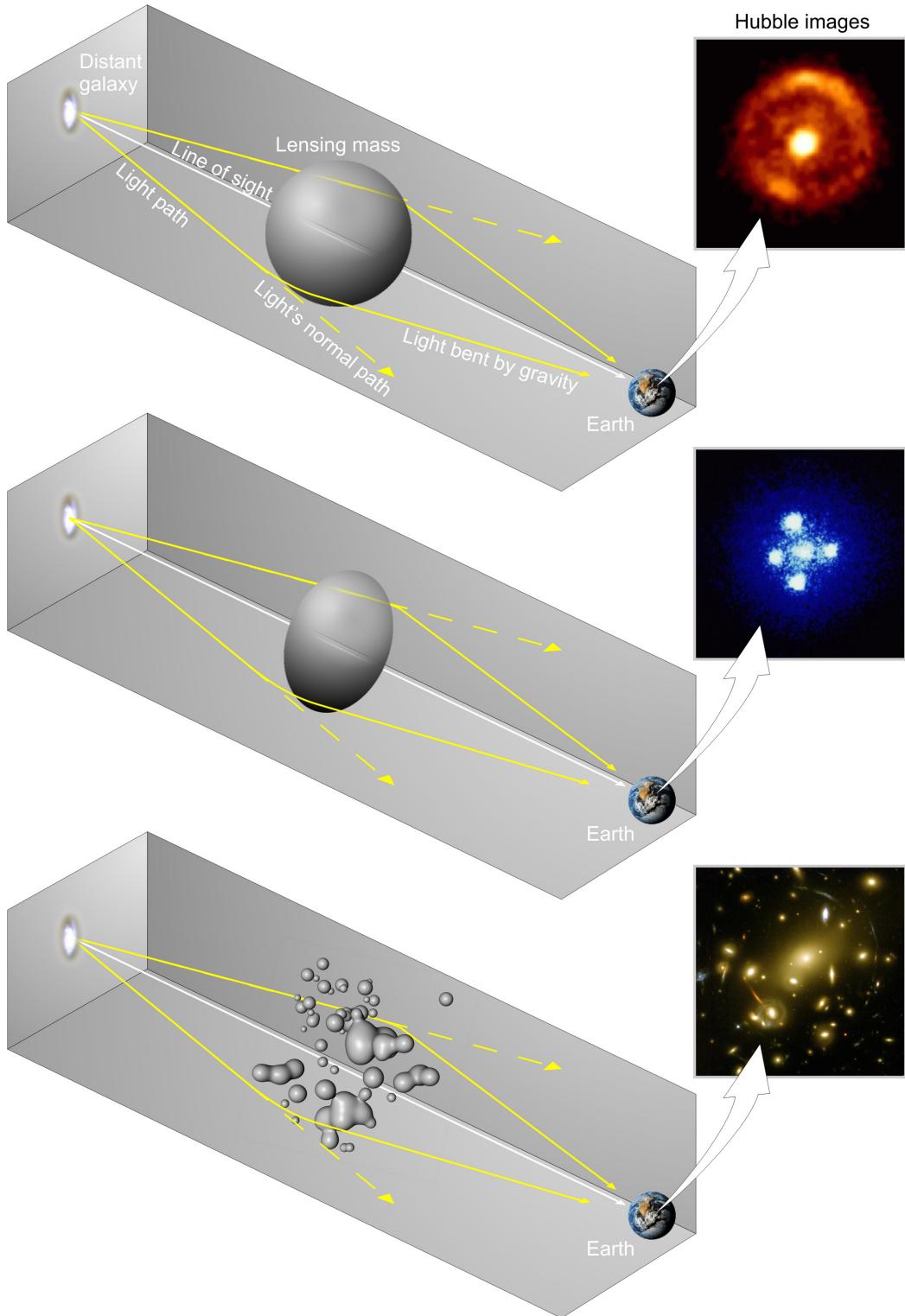


Figure 2.2 Light from distant galaxy is bent in unique ways depending on the distribution of mass between the galaxy and Earth. Yellow dashed lines indicate where the light would have gone if the matter were not present [8].

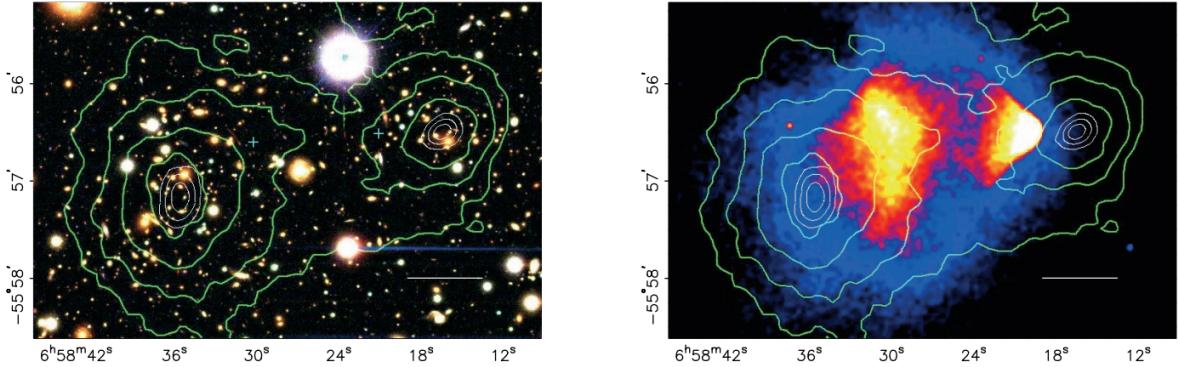


Figure 2.3 (left) Optical image of galactic cluster 1E0657-558. (right) X-ray image of the cluster with redder meaning hotter and higher baryon density. (both) Green contours are reconstruction of gravity contours from weak lensing. White rings are the best fit mass maxima at 68.3%, 95.5%, and 99.7% confidence. The matter maxima of the clusters are clearly separated from x-ray maxima. [9]

445 light, see Figure 2.2. With a sufficient understanding of light sources behind a massive object, we
 446 can reconstruct the contours of the gravitational lenses. The gradient of the contours shown in
 447 Figure 2.3 then indicates how dense the matter is and where it is.

448 The x-ray emission can then be observed from the clusters. Since these galaxies are mostly gas
 449 and are merging, then the gas should be getting hotter. If they are merging, the x-ray emissions
 450 should be the strongest where the gas is mostly moving through each other. Hence, X-ray emission
 451 maps out where the gas is in the merging galaxy cluster.

452 The lensing and x-ray observations were done on the Bullet cluster featured on Figure 2.3.
 453 The x-ray emissions do not align with the gravitational contours from lensing. The incongruence
 454 in mass density and baryon density suggests that there is a lot of matter somewhere that does
 455 not interact with light. Moreover, this dark matter cannot be baryonic [9]. The Bullet Cluster
 456 measurement did not really tell us what DM is exactly, but it did give the clue that DM also does
 457 not interact with itself very strongly. If DM did interact strongly with itself, then it would have been
 458 more aligned with the x-ray emission [9]. There have been follow-up studies of galaxy clusters with
 459 similar results. The Bullet Cluster and others like it provide a persuasive case against something
 460 possibly amiss in our gravitational theories.

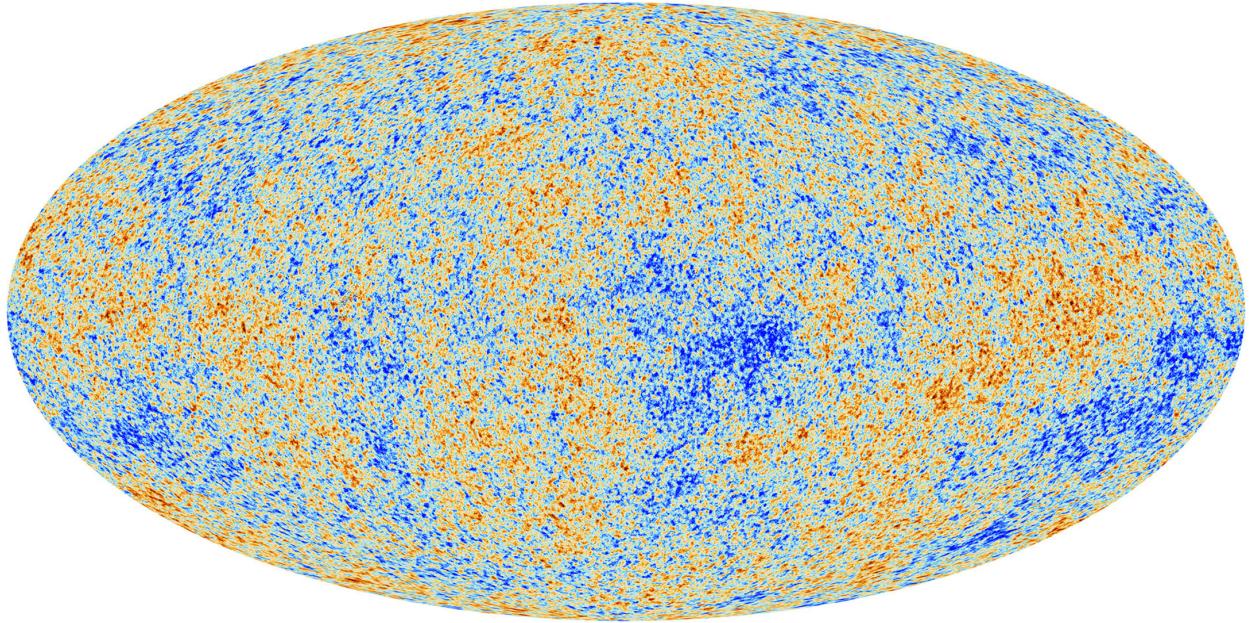


Figure 2.4 Plank CMB sky. Sky map features small variations in temperature in primordial light. These anisotropies are used to make inferences about the universe’s energy budget and developmental history. [10]

461 **2.3.3 Evidence for Dark Matter: Cosmic Microwave Background**

462 The Cosmic Microwave Background (CMB) is the primordial light from the early universe
463 when Hydrogen atoms formed from the free electron and proton soup in the early universe. The
464 CMB is the earliest light we can observe; released when the universe was about 380,000 years old.
465 Then we look at how the simulated universes look like compared to what we see. Figure 2.4 is the
466 most recent CMB image from the Plank satellite after subtracting the average value and masking the
467 galactic plane [10]. Redder regions indicate a slightly hotter region in the CMB, and blue indicates
468 colder. The intensity variations are on the order of 1 in 1000 with respect to the average value.

469 The Cosmic Microwave Background shows that the universe had DM in it from an incredibly
470 early stage. To measure the DM, Dark Energy, and matter fractions of the universe from the CMB,
471 the image is analyzed into a power spectrum, which shows the amplitude of the fluctuations as
472 a function of spherical multipole moments. Λ CDM provides the best fit to the power spectra of
473 the CMB as shown in Figure 2.5. The CMB power spectrum is quite sensitive to the fraction
474 of each energy contribution in the early universe. Low l modes are dominated by variations
475 in gravitational potential. Intermediate l emerge from oscillations in photon-baryon fluid from

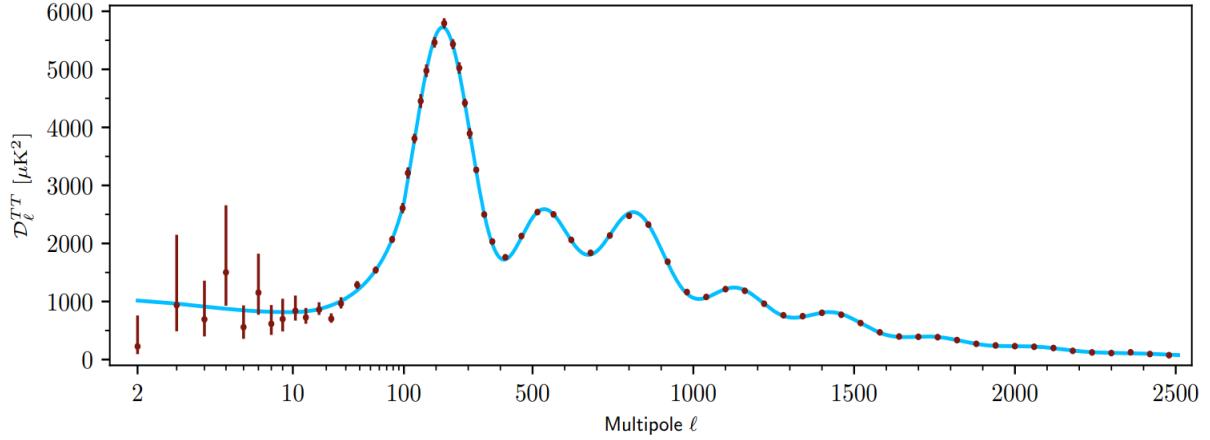


Figure 2.5 Observed Cosmic Microwave Background power spectrum as a function of multipole moment from Plank [10]. Blue line is best fit model from Λ CDM. Red points and lines are data and error, respectively.

476 competing baryon pressures and gravity. High l is a damped region from the diffusion of photons
 477 during electron-proton recombination. [1]

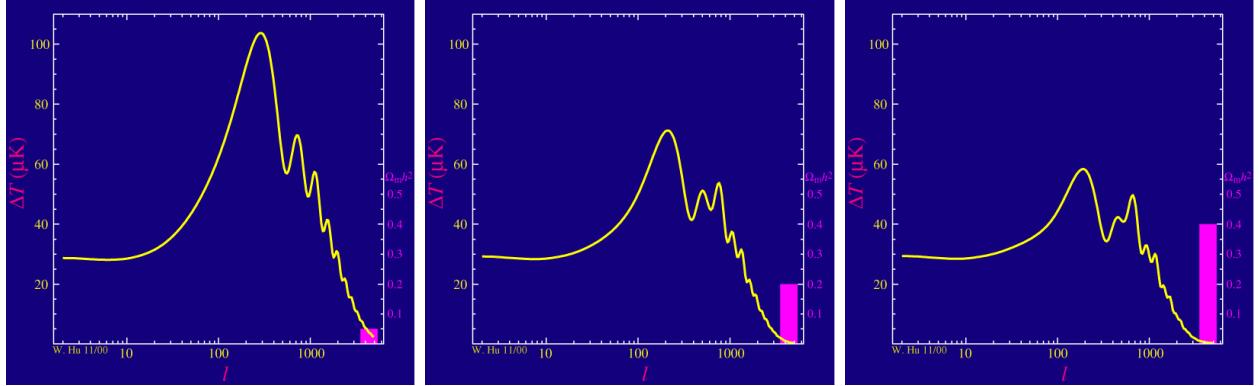


Figure 2.6 Predicted power spectra of CMB for different $\Omega_m h^2$ values for fixed baryon density from [11]. (left) Low $\Omega_m h^2$ increases the prominence of first and second peaks. (middle) $\Omega_m h^2$ is most similar to the observed power spectrum. The second and third peaks are similar in height. (right) $\Omega_m h^2$ is large which suppresses the first peak and raises the prominence of the third peak.

478 The harmonics would look quite different for a universe with less DM. Figure 2.6 demonstrates
 479 the effect $\Omega_m h^2$ has on the expected power spectrum for fixed baryon matter density. [11] Sweeping
 480 $\Omega_m h^2$ in this way clearly shows the effect dark matter has on the CMB power spectrum. The
 481 observations fit well with the Λ CDM model, and the derived fractions are as follows. The matter
 482 fraction: $\Omega_m = 0.3153$; and the baryon fraction: $\Omega_b = 0.04936$ [10]. Plank's observations also
 483 provide a measure of the Hubble constant, H_0 . H_0 especially has seen a growing tension in the

484 past decade that continues to deepened with observations from instruments like the James Webb
485 Telescope [12, 13]. As Hubble tensions deepen, we may find that perhaps Λ **CDM**, despite its
486 successes, is missing some critical physics.

487 Overall, the Newtonian motion of stars in galaxies, weak lensing from galactic clusters, and
488 power spectra from primordial light form a compelling body of research in favor of dark matter.
489 It takes another leap of theory and experimentation to make observations of DM that are non-
490 gravitational in nature. In Section 2.3, the evidence for DM implies strongly that the DM is matter
491 and not a lost parameter in the gravitational fields between massive objects. Finally, if we take one
492 axiom: that this matter has quantum behavior, such as being described by some Bohr wavelength
493 and abiding by some fermion or boson statistics; then we arrive at particle dark matter. One particle
494 DM hypothesis is the Weakly Interacting Massive Particle (WIMP). This DM candidate theory is
495 discussed further in the next section and is the focus of this thesis.

496 **2.4 Searching for Dark Matter: Particle DM**

497 Section 2.4 shows the Standard Model of particle physics and is currently the most accurate
498 model for the dynamics of fundamental particles like electrons and photons. The current status
499 of the SM does not have a viable DM candidate. When looking at the standard model, we can
500 immediately exclude any charged particle because charged particles interact strongly with light.
501 Specifically, this will rule out the following charged, fundamental particles: $e, \mu, \tau, W, u, d, s, c, t, b$
502 and their corresponding antiparticles. Recalling from Section 2.2 that DM must be long-lived and
503 stable over the age of the universe which excludes all SM particles with decay half-lives at or shorter
504 than the age of the universe. The lifetime constraint additionally eliminates the Z and H bosons.
505 Finally, the candidate DM needs to be somewhat massive. Recall from Section 2.2 that DM is cold
506 or not relativistic through the universe. This eliminates the remaining SM particles: $\nu_{e,\mu,\tau}, g, \gamma$ as
507 DM candidates. Because there are no DM candidates within the SM, the DM problem strongly
508 hints to physics beyond the SM (BSM).

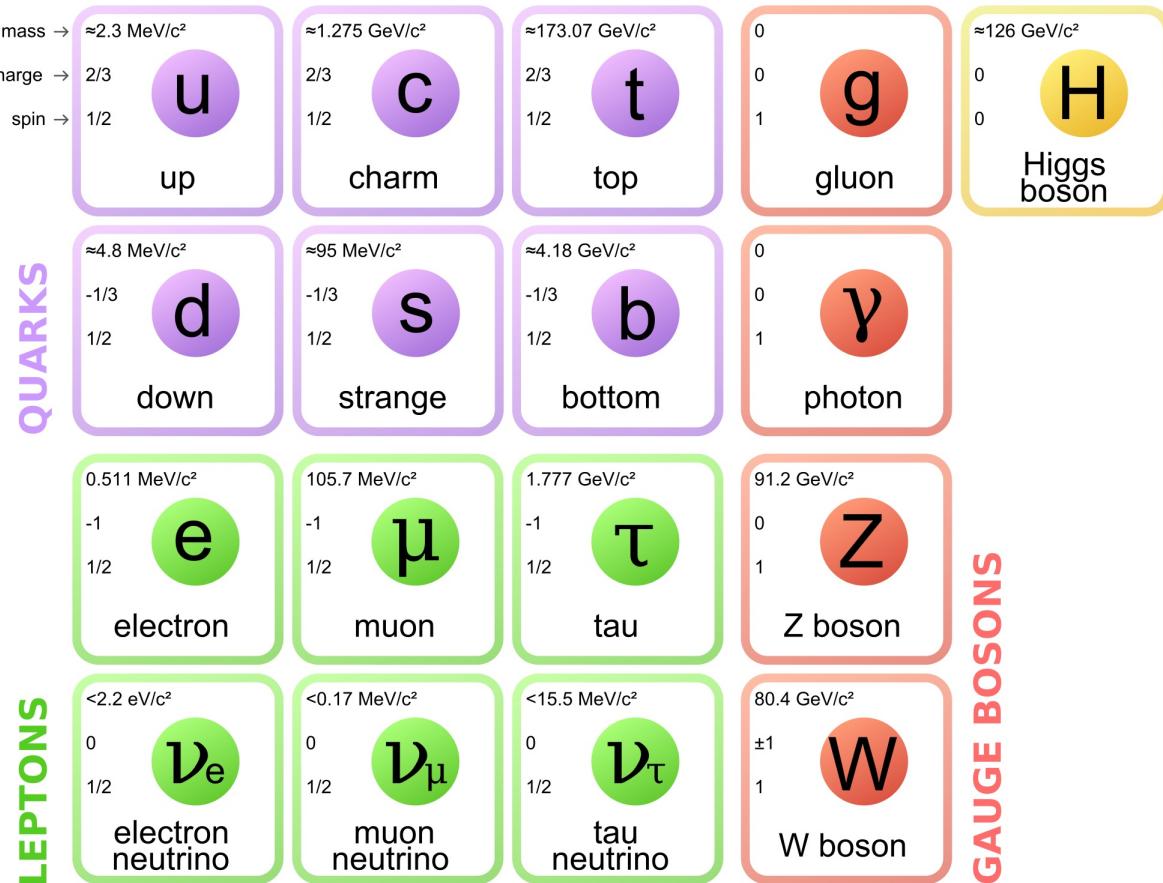


Figure 2.7 The Standard Model (SM) of particle physics. Figure taken from <http://www.quantumdiaries.org/2014/03/14/the-standard-model-a-beautiful-but-flawed-theory/>

509 2.4.1 Shake it, Break it, Make it

510 When considering DM that couples in some way with the SM, the interactions are roughly
 511 demonstrated by interaction demonstrated in Figure 2.8. The figure is a simplified Feynman
 512 diagram where the arrow of time represents the interaction modes of: **Shake it, Break it, Make it.**

513 **Shake it** refers to the direct detection of dark matter. Direct detection interactions start with
 514 a free DM particle and an SM particle. The DM and SM interact via elastic or inelastic collision
 515 and recoil away from each other. The DM remains in the dark sector and imparts some momentum
 516 onto the SM particle. The hope is that the momentum imparted onto the SM particle is sufficiently
 517 high enough to pick up with extremely sensitive instruments. Because we cannot create the DM in
 518 the lab, a direct detection experiment must wait until DM is incident on the detector. Most direct
 519 detection experiments are therefore placed in low-background environments with inert detection

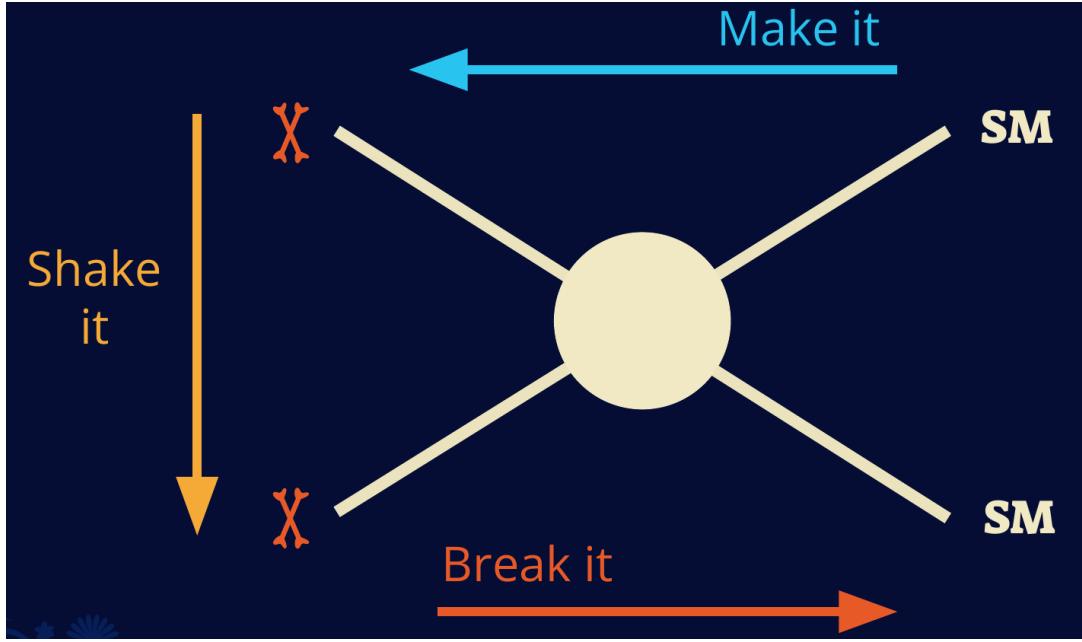


Figure 2.8 Simplified Feynman diagram demonstrating different ways DM can interact with SM particles. The 'X's refer to the DM particles whereas the SM refer to fundamental particles in the SM. The large circle in the center indicates the vertex of interaction and is purposely left vague. The colored arrows refer to different directions of time as well as their respective labels. The arrows indicate the initial and final state of the DM -SM interaction in time.

520 media like the noble gas Xenon. [14]

521 **Make it** refers to the production of DM from SM initial states. The experiment starts with
 522 particles in the SM. These SM particles are accelerated to incredibly high energies and then collide
 523 with each other. In the confluence of energy, DM hopefully emerges as a byproduct of the SM
 524 annihilation. Often it is the collider experiments that are energetic enough to hypothetically produce
 525 DM. These experiments include the world-wide collaborations ATLAS and CMS at CERN where
 526 proton collide together at extreme energies. The DM searches, however, are complex. DM likely
 527 does not interact with the detectors and lives long enough to escape the detection apparatus of
 528 CERN's colliders. This means any DM production experiment searches for an excess of events
 529 with missing momentum or energy in the events. An example event with missing transverse
 530 momentum is shown in Figure 2.9. The missing momentum with no particle tracks implies a
 531 neutral particle carried the energy out of the detector. However, there are other neutral particles
 532 in the SM, like neutrons or neutrinos, so any analysis has to account for SM signatures of missing

533 momentum. [15]

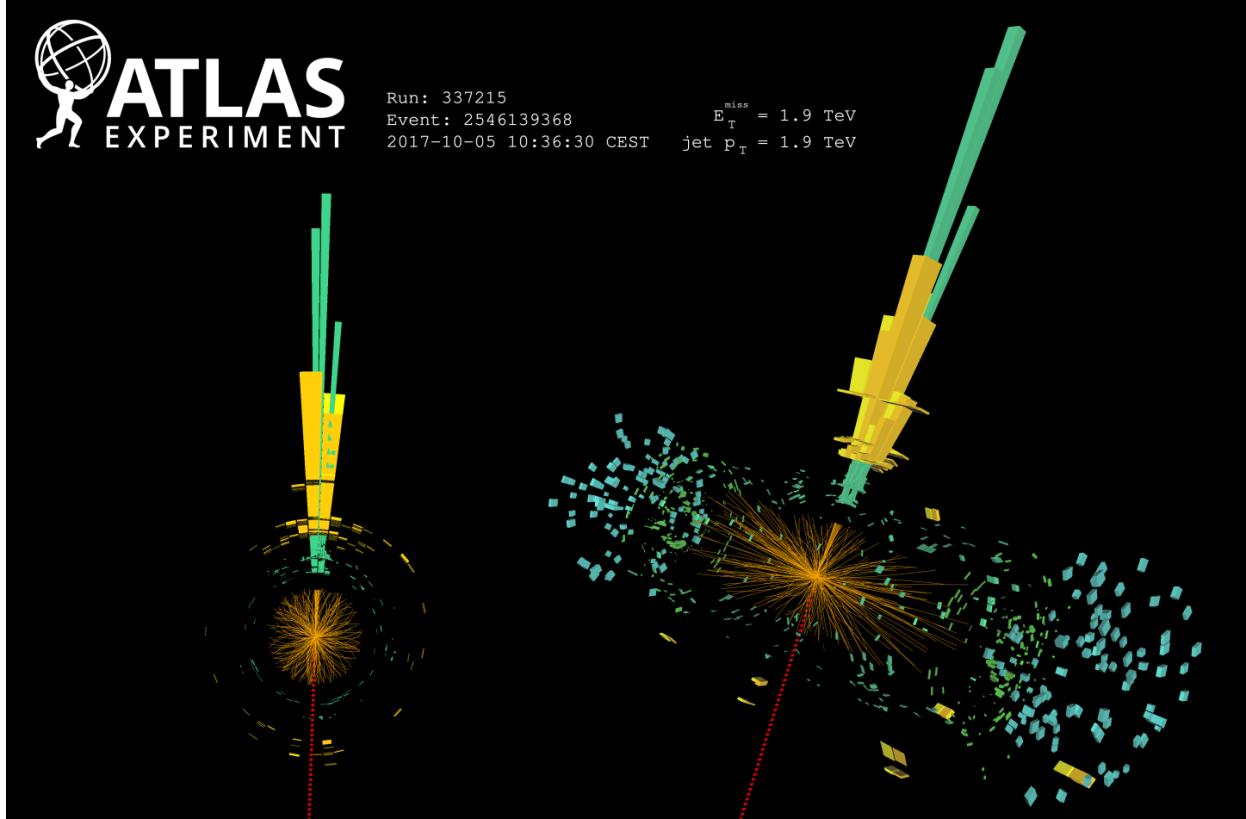


Figure 2.9 A single jet event in ATLAS detector from 2017 [16]. Jet momentum was observed to be 1.9 TeV. Missing transverse momentum was observed to be 1.9 TeV compared to the initial transverse momentum of the event was 0. Implied MET is traced by a red dashed line in event display.

534 2.4.2 Break it: Standard Model Signatures of Dark Matter through Indirect Searches

535 **Break it** refers to the creation of SM particles from the dark sector, and it is the primary focus
536 of this thesis. The interaction begins with DM or in the dark sector. The hypothesis is that this
537 DM will either annihilate with itself or decay and produce an SM byproduct. This method is
538 often referred to as the Indirect Detection of DM because we have no lab to directly control or
539 manipulate the DM. Therefore, most indirect DM searches are performed using observations of
540 known DM densities among the astrophysical sources. The strength is that we have the whole of the
541 universe and its 13.6-billion-year lifespan to use as a detector and particle accelerator. Additionally,
542 locations of dark matter are well cataloged since it was astrophysical observations that presented

543 the problem of DM in the first place.

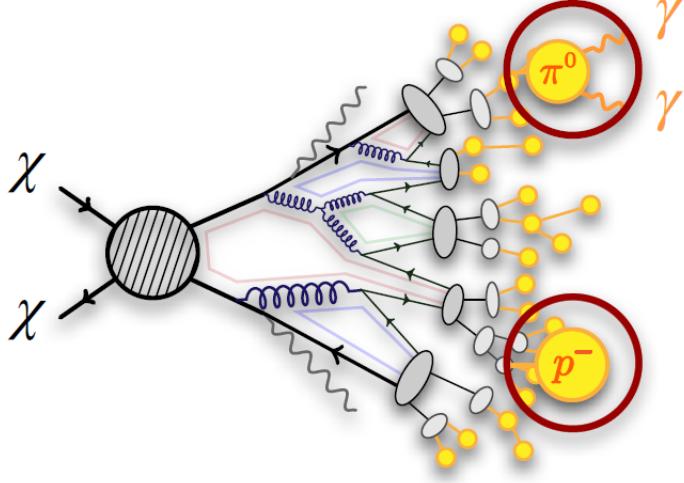


Figure 2.10 More detailed pseudo-Feynman diagram of particle cascade from dark matter annihilation into 2 quarks. The quarks hadronize and down to stable particles like γ or the anti-proton (p^-). Diagram pulled from ICRC 2021 presentation on DM annihilation search [17].

544 However, anything can happen in the universe. There are many difficult to deconvolve back-
545 grounds when searching for DM. One prominent example is the galactic center. We know the
546 galactic center has a large DM content because of stellar kinematics in our Milky Way and DM halo
547 simulations. Yet, any signal from the galactic center is challenging to parse apart from the extreme
548 environment of our supermassive black hole, unresolved sources, and diffuse emission from the
549 interstellar medium [18]. Despite the challenges, any DM model that yields evidence in the other
550 two observation methods, **Shake it or Make it** must be corroborated with indirect observations of
551 the known DM sources. Without corroborating evidence, DM observation in the lab is hard-pressed
552 to demonstrate that it is the model contributing to the DM seen at the universal scale.

553 In the case of WIMP DM, signals are described in terms of primary SM particles produced
554 from DM decay or annihilation. The SM initial state particles are then simulated down to stable
555 final states such as the γ , ν , p , or e which can traverse galactic lengths to reach Earth.

556 Figure 2.10 shows the quagmire of SM particles that emerges from SM initial states that are not
557 stable [17]. There are many SM particles with varying energies that can be produced in such an

558 interaction. For any arbitrary DM source and stable SM particle, the SM flux from DM annihilating
 559 to a neutral particle in the SM, ϕ , from a region in the sky is described by the following.

$$\frac{d\Phi_\phi}{dE_\phi} = \frac{\langle\sigma v\rangle}{8\pi m_\chi^2} \frac{dN_\phi}{dE_\phi} \times \int_{\text{source}} d\Omega \int_{l.o.s} \rho_\chi^2 dl(r, \theta') \quad (2.4)$$

560 In Equation (6.1), $\langle\sigma v\rangle$ is the velocity-weighted annihilation cross-section of DM to the SM. m_χ
 561 refers to the mass of DM, noted with Greek letter χ . $\frac{dN_\phi}{dE_\phi}$ is the N particle flux weighted by the
 562 particle energy. An example is provided in Figure 2.11 for the γ final state. The integrated terms
 563 are performed over the solid angle, $d\Omega$, and line of sight, l.o.s. ρ is the density of DM for a
 564 location (r, θ') in the sky. The terms left of the '×' are often referred to as the particle physics
 565 component. The terms on the right are referred to as the astrophysical component. For decaying
 566 DM, the equation changes to...

$$\frac{d\Phi_\phi}{dE_\phi} = \frac{1}{4\pi\tau m_\chi} \frac{dN_\phi}{dE_\phi} \times \int_{\text{source}} d\Omega \int_{l.o.s} \rho_\chi dl(r, \theta') \quad (2.5)$$

567 In Equation (7.1), τ is the decay lifetime of the DM. Just as in Equation (6.1), the left and right
 568 terms are the particle physics and the astrophysical components respectively. The integrated
 569 astrophysical component of Equation (6.1) is often called the J-Factor. Whereas the integrated
 570 astrophysical component of Equation (7.1) is often called the D-Factor.

571 Exact DM $\text{DM} \rightarrow \text{SM SM}$ branching ratios are not known, so it is usually assumed to go 100%
 572 into an SM particle/anti-particle. Additionally, when a DM annihilation or decay produces one of
 573 the neutral, long-lived SM particles (ν or γ), the particle is traced back to a DM source. For DM
 574 above GeV energies, there are very few SM processes that can produce particles with such a high
 575 energy. Seeing such a signal would almost certainly be an indication of the presence of dark matter.
 576 Fortunately, the universe provides us with the largest volume and lifetime ever for a particle physics
 577 experiment.

578 2.5 Sources for Indirect Dark Matter Searches

579 The first detection of DM relied on optical observations. Since then, we have developed new
 580 techniques to find DM dense regions. As described in Section 2.3.1, many DM dense regions were
 581 through observing galactic rotation curves. Our Milky Way galaxy is among DM dense regions

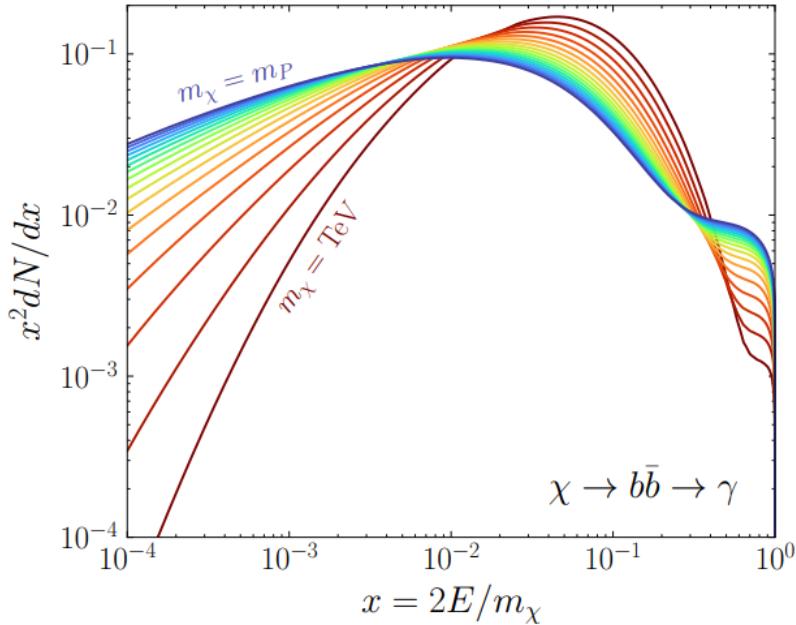


Figure 2.11 Dark Matter (DM) decay spectrum for $b\bar{b}$ initial state and γ final state. Redder spectra are for larger DM masses. Bluer spectra are light DM masses. x is a unitless factor defined as the ratio of the mass of DM, m_χ , and the final state particle energy E_γ . Figure from [19].

discovered, and it is the largest nearby DM dense region to look at. Additionally, the DM halo surrounding the Milky Way is clumpy [18]. There are regions in the DM halo of the Milky Way that have more DM than others that have captured gas over time. These sub-halos were dense enough collapse gas and form stars. These apparent sub galaxies are known as dwarf spheroidal galaxies and are the main sources studied in this thesis. Each source type comes with different trade-offs. Galactic Center studies will be very sensitive to the assumed distribution of DM. The central DM density can vary substantially as demonstrated in Figure 2.12. At distances close to the center of the galaxy, or small r , the differences in DM densities can be 3-4 orders of magnitude. Searches toward the galactic center will therefore be quite sensitive to the assumed DM distribution.

Searches toward Dwarf Spheroidal Galaxies (dSph's) suffer from uncertainties in the DM density less than the galactic center studies. This is mostly from their diminutive size being smaller than the angular resolution of most γ -ray observatories [18]. The DM content dSph's are typically determined with the Virial theorem, Equation (2.1), and are usually majority DM [18] in mass. DSph's tend to be ideal sources to look at for DM searches. Their environments are quiet with little

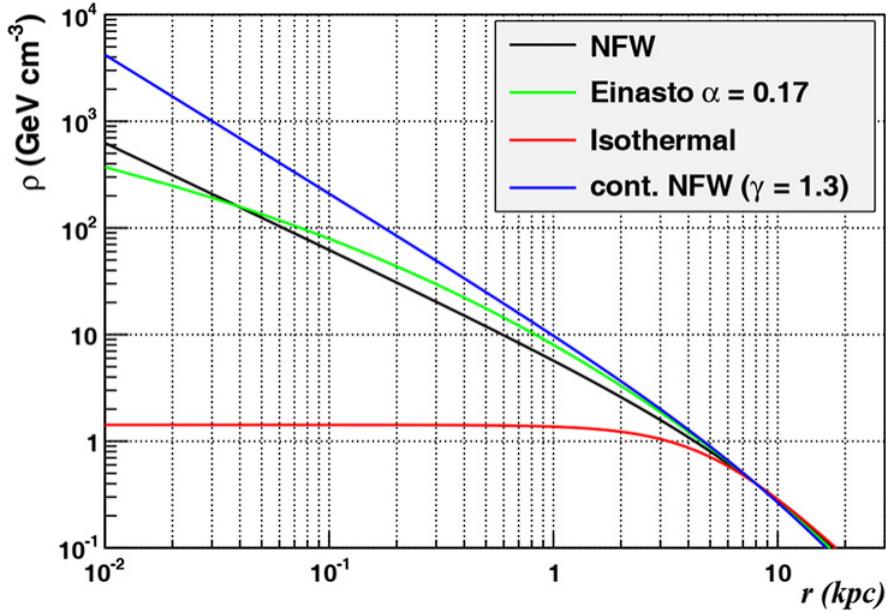


Figure 2.12 Different dark matter density profiles compared. Some models produce exceptionally large densities at small r [20].

596 astrophysical background. Unlike the galactic center, the most active components of dSph's are the
 597 stars within them versus a violent accretion disc around a black hole. All this together means that
 598 dSph's are among the best sources to look at for indirect DM searches. dSph's are the targets of
 599 focus for this thesis.

600 2.6 Multi-Messenger Dark Matter

601 Astrophysics entered a new phase in the past few decades that leverages our increasing sensitivity
 602 to SM channels and general relativity (GR). Up until the 21st century, astrophysical observations
 603 were performed with photons (γ) only. Astrophysics with this 'messenger' is fairly mature now.
 604 Novel observations of the universe have since only adjusted the sensitivity of the wavelength of
 605 light that is observed except at MeV energies. Gems like the CMB [10], and more have ultimately
 606 been observations of different wavelengths of light. Multi-messenger astrophysics proposes using
 607 other SM particles such the $p^{+/-}$, or ν or gravitation waves predicted by general relativity.

608 The experiment LIGO had a revolutionary discovery in 2016 with the first detection of a binary
 609 black hole merger [21]. This opened the collective imagination to observing the universe through
 610 gravitational waves. There has also been a surge of interest in the neutrino (ν) sector. IceCube

611 demonstrated that we are sensitive to neutrinos in regions that correlate with significant photon
 612 emission like the galactic plane [22]. Neutrinos, like gravitational waves and light, travel mostly
 613 unimpeded from their source to our observatories. This makes pointing to the originating source
 614 of these messengers much easier than it is for cosmic rays which are deflected from their source by
 615 magnetic fields.

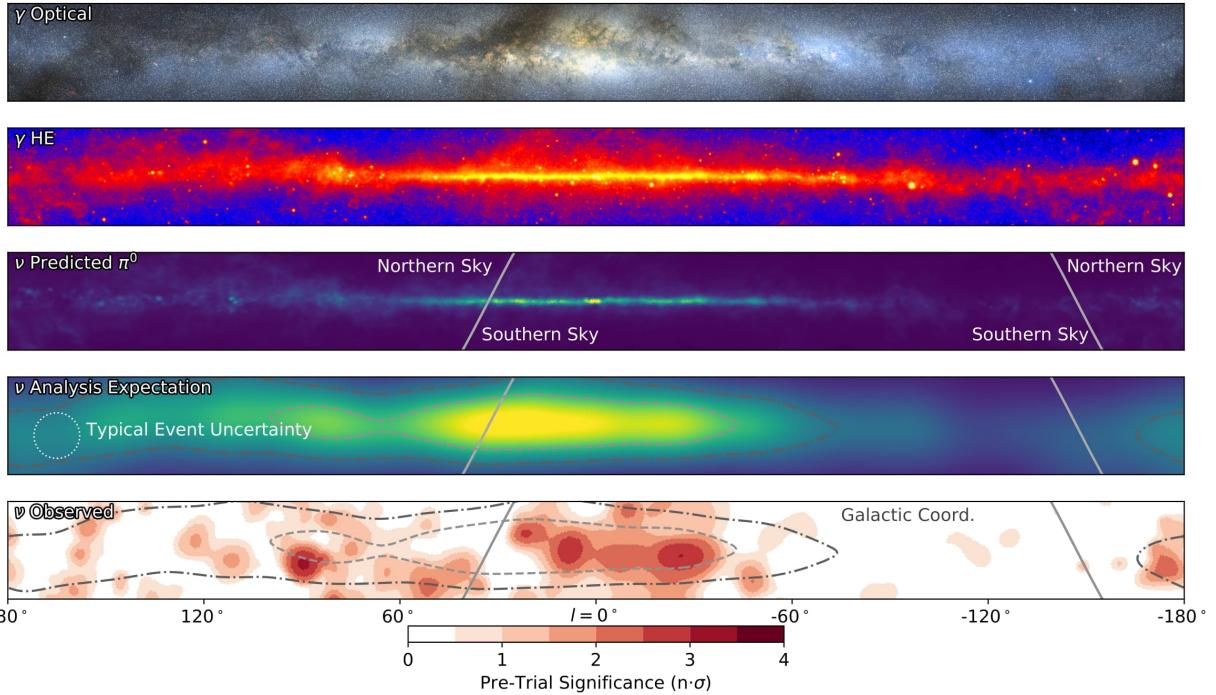


Figure 2.13 The Milky Way Galaxy in photons (γ) and neutrinos (ν) [22]. The Galactic center is at $l=0^\circ$ and is the brightest region in all panels. (top) An Optical color image of the Milky Way galaxy seen from Earth. Clouds of gas and dust obscure some light from stars. (2nd down) Integrated flux of γ -rays observed by the Fermi-LAT telescope [23]. (middle) Expected neutrino emission that corresponds with Fermi-LAT observations. (2nd up) Expected neutrino emission profile after considering detector systematics of IceCube. (bottom) Observed neutrino emission from region of the galactic plane. Substantial neutrino emission was detected.

616 The IceCube collaboration recently published a groundbreaking result of the Milky Way in
 617 neutrinos. The recent result from IceCube, shown in Figure 2.13, proves that we can make
 618 observations under different messenger regimes. The top two panels show the appearance of the
 619 galactic plane to different wavelengths of light. Some sources are more apparent in some panels,
 620 while others are not. This new channel is powerful because neutrinos are readily able to penetrate
 621 through gas and dust in the Milky Way. This new image also refines our understanding of how high

622 energy particles are produced. For example, the fit to IceCube data prefers neutrino production
 623 from the decay of π^0 [22].

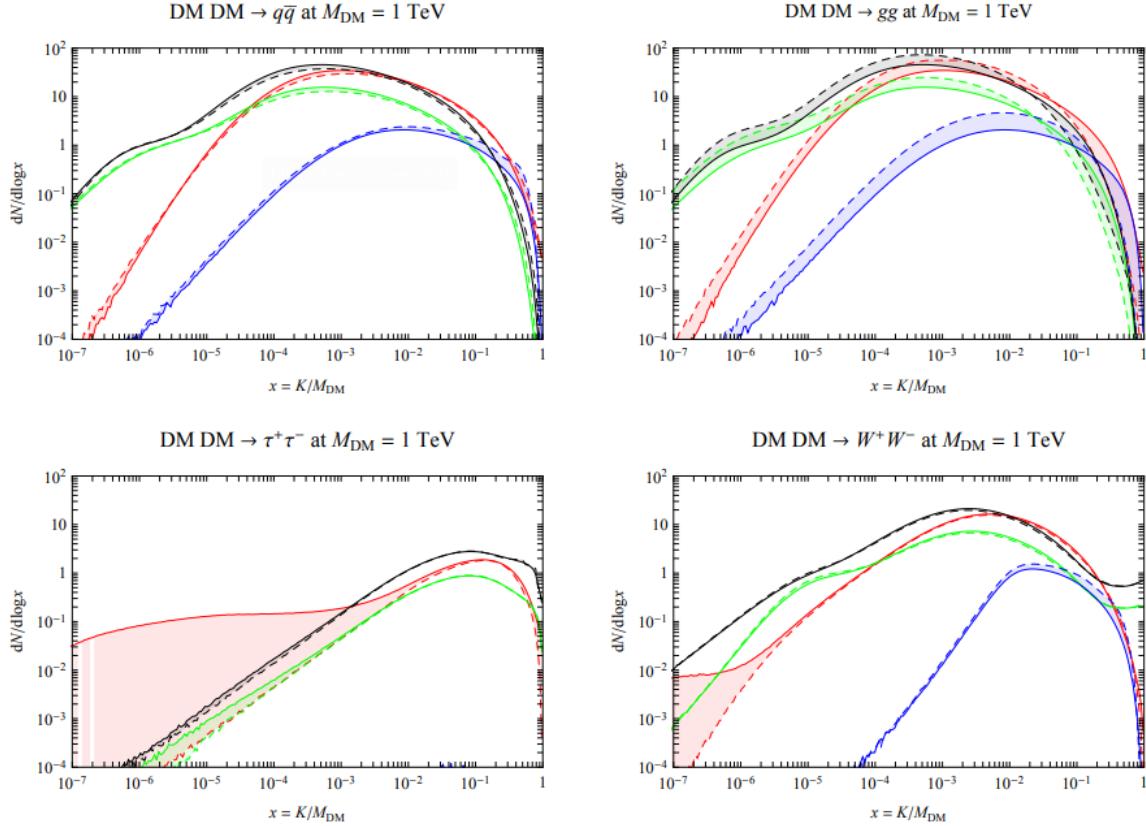


Figure 2.14 Dark Matter annihilation spectra for different final state particle and standard model annihilation channels [24]. Photons (red), e^\pm (green), \bar{p} (blue), ν (black).

624 Exposing our observations to more cosmic messengers greatly increases our sensitivity to
 625 rare processes. In the case of DM, Figure 2.14, there are many SM particles produced in DM
 626 annihilation. Among the final state fluxes are gammas and neutrinos. Charged particles are also
 627 produced however they would not likely make it to Earth since they will be deflected by magnetic
 628 fields between the source and Earth. This means observatories that can see the neutral messengers
 629 are especially good for DM searches and for combining data for a multi-messenger DM search.

CHAPTER 3

630 MULTIMESSENGER ASTROPHYSICS: DETECTING HIGH ENERGY NEUTRAL 631 MESSENGERS

632 3.1 Introduction

633 Before the 20th century, all astrophysics observations were optical in nature. We literally only
634 saw things with highly magnified optical observations. Then we discovered cosmic rays. cosmic
635 rays are charged particles, typically naked protons or H+. This was seen by Victor Hess in 19??.
636 Around the same time we discovered neutrinos from beta decay. Sometime around 1950 we started
637 to build neutrino detectors which were mostly sensitive to neutrinos from the sun. Finally, it was
638 theorized that compact objects like black holes and neutron stars would create waves in space-time
639 when they experience mergers or collisions.

640 In the 21st century, we have developed new observation techniques and detectors that are no only
641 sensitive to these four messengers - photons ([TODO: photon](#)), neutrinos ([TODO: nu](#)), Cosmic
642 Rays (CR), and Gravitational Wave (WV) - we're collect high energy versions of these events.
643 For the standad model particles, we're now sensitive to all messengers above the MeV eneryg
644 range. Additionally, the GW's were sensitive to are in the stellar mass black hole region and above
645 within our galactic neighborhood. This means were becoming sensitive to the fundamental physics
646 occuring within the universe and we can rely on the universe as a TeV+ particle accelerator. We
647 also have the abaility to correlate high energy events across messengers and gain new insights on
648 the processes that occur in our universe.

649 This thesis focuses on very high energy (VHE) gamma rays and neutrinos. These can both be
650 observed through the water cherenkov detection technique altho not exclusively. Methods on how
651 to detect and observe these neutral messengers are discussed Section 3.3 and Section 3.4

652 3.2 Charged Particles in a Medium

653 For high enery gamma-rays and neutrinos, we can exploit the same effect that charged particles
654 have with water. This effect is known as Cherenkov radiation. Cherenkov Radiation occurs when a
655 charged particle, usually electrons (e) or muons (μ), traverse a medium, like water, faster than the

656 speed of light in that medium. This is similar to sonic boom where an object moves through air
657 faster than the speed of sound in air. Cherenkov radiation can therefore be thought of as an 'optic
658 boom'. Many astro-particle physics experiments will use water as the medium as because water
659 has a unique set of properties ideal for charged particle tracking.



Figure 3.1 TODO: Show a nuclear reactor with cherenkov radiation[NEEDS A SOURCE][FACT CHECK THIS]

660 The frequency of light emitted due to cherenkov radiation follows the equation:

$$INSERT\ Cherenkov\ wavelength\ calc\ HERE. \quad (3.1)$$

661 The absorption spectra is shown in the following figure:

662 **3.3 Photons (γ)**

663 **3.4 Neutrinos (ν)**

664 **3.5 Opportunities to Combine for Dark Matter**



Figure 3.2 TODO: absorption spectrum of liquid and solid water[NEEDS A SOURCE][FACT CHECK THIS]

CHAPTER 4

665 **HIGH ALTITUDE WATER CHERENKOV (HAWC) OBSERVATORY**

666 **4.1 The Detector**

667 **4.2 Events Reconstruction and Data Acquisition**

668 **4.2.1 G/H Discrimination**

669 **4.2.2 Angle**

670 **4.2.3 Energy**

671 **4.3 Remote Monitoring**

672 **4.3.1 ATHENA Database**

673 **4.3.2 HOMER**

674

CHAPTER 5

ICECUBE NEUTRINO OBSERVATORY

675 **5.1 The Detector**

676 **5.2 Events Reconstruction and Data Acquisition**

677 **5.2.1 Angle**

678 **5.2.2 Energy**

679 **5.3 Northern Test Site**

680 **5.3.1 PIgeon remote dark rate testing**

681 **5.3.2 Bulkhead Construction**

CHAPTER 6

GLORY DUCK: MULTI-WAVELENGTH SEARCH FOR DARK MATTTER ANNIHILATION TOWARDS DWARF SPHEROIDAL GALAXIES

6.1 Introduction

The field of astrophysics now has several instruments and observatories sensitive to high energy gamma-rays. The energy sensitivity for the modern gamma-ray program spans many orders of magnitude. Figure 6.1 demonstrates these similar sensitivities across energies for the five experiments: Fermi-LAT, HAWC, HESS, MAGIC, and VERITAS.

Each of the five experiments featured in Figure 6.1 have independently searched for DM annihilation from dwarf spheroidal galaxies (dSph) and set limits. Intriguingly, there are regions of substantial overlap in their energy sensitivities. This clearly motivates an analysis that combines data from these five. Each experiment has unique gamma-ray detection methods and their weaknesses and strengths can be leveraged with each other. The HAWC gamma-ray observatory is extensively introduced in chapter 4, so it is not introduced here. A brief description of the remaining experiments are in the following paragraphs.

The Large Area Telescope (LAT) is a pair conversion telescope mounted on the NASA Fermi satellite in orbit \sim 550 km above the Earth [26]. LAT's field of view covers about 20% of the whole sky, and it sweeps the whole sky approximately every 3 hours. LAT's gamma-ray energy sensitivity ranges from 20 MeV up to 1 TeV. Previous DM searches towards dSphs using Fermi-LAT are published in [27] and [28]

The High Energy Spectroscopic System (HESS), Major Atmospheric Gamma Imaging Cherenkov (MAGIC), and Very Energetic Radiation Imaging Telescope Array System (VERITAS) are arrays of Imaging Atmospheric Cherenkov Telescopes (IACT). These telescopes observe the Cherenkov light emitted from gamma-ray showers in the Earth's atmosphere. The field of view for these telescopes is no larger than 5° with energy sensitivities ranging from 30 GeV up to 100 TeV [29, 30, 31]. IACTs are able to make precise observations in selected regions of the sky, however can only be operated in ideal dark conditions. HESS's observations of the dwarves

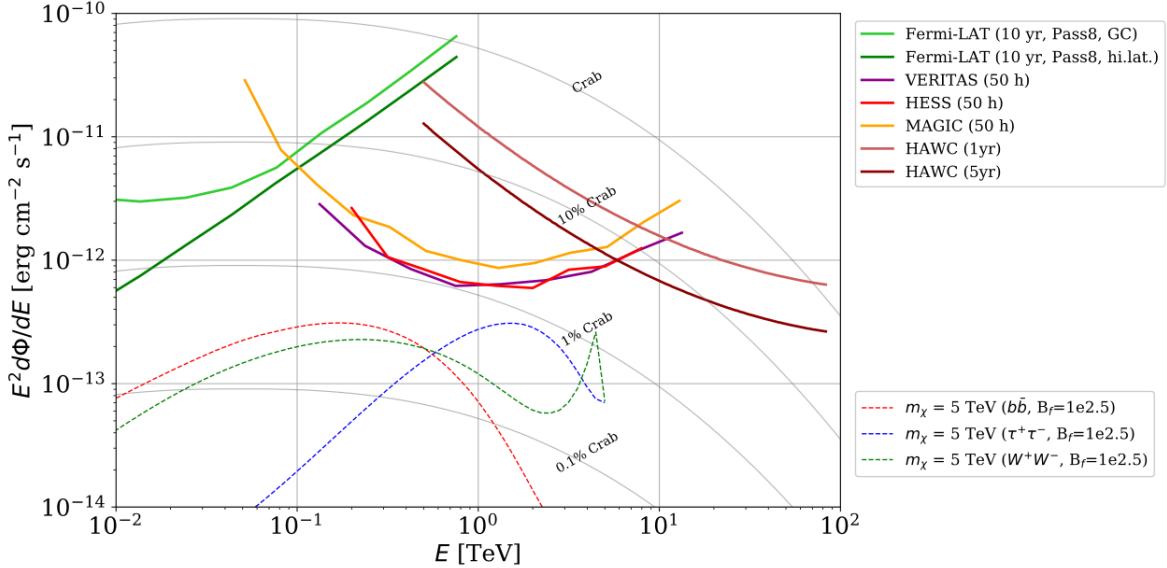


Figure 6.1 Sensitivities of five gamma-ray experiments compared to percentages of the Crab nebula’s emission and dark matter annihilation. Solid lines present estimated sensitivities to power law spectra [FACT CHECK THIS] for each experiment. Green lines are Fermi-LAT sensitivities where lighter green is the sensitivity to the galactic center and dark green is its sensitivity to higher declinations. Orange, red, and purple solid lines represent the MAGIC, HESS, and VERITAS 50 hour sensitivities respectively. The maroon and brown lines are the HAWC 1 year and 5 year sensitivities. Across four decades of gamma-ray energy, these experiments have similar sensitivities on the order 10^{-12} erg $\text{cm}^{-2}\text{s}^{-1}$. The dotted lines are estimated dark matter fluxes assuming $m_\chi = 5$ TeV DM annihilating to bottom quarks (red), tau leptons (blue), and W bosons (green). Faded gray lines outline percentage flux of the Crab nebula. Figure is an augmented version of [25]

708 Sculptor and Carina were between January 2008 and December 2009. HESS’s observations of
 709 Coma Berenices were from 2010 to 2013, and Fornax was observed in 2010 [32, 33, 34]. MAGIC
 710 provided deep observations of Segue1 between 2011 and 2013 [35]. MAGIC also provides data
 711 for three dwarves: Coma Berenices, Draco, and Ursa Major II where observations were made
 712 in: January - June 2019 [36], March - September 2018 [36], and 2014 - 2016 [37] respectively.
 713 VERITAS provided data for Boötes I, Draco, Segue 1, and Ursa Minor from 2009 to 2016 [38].

714 This chapter presents the Glory Duck analysis, the name given for the search for dark matter
 715 annihilation from dSph by combining data from the five gamma-ray observatories: Fermi-LAT,
 716 HAWC, HESS, MAGIC, and VERITAS. Specifically, the methods in analysis and modeling are
 717 presented for the HAWC gamma-ray observatory. This work was published to the Journal of
 718 Cosmology and Astroparticle Physics and presented at the International Cosmic Ray Conference

719 in 2019, 2021, and 2023 [39, 40, 41] and others.

720 **6.2 Dataset and Background**

721 This section enumerates the data and background methods used for HAWC’s study of dSphs.
722 Section 6.2.1 and Section 6.2.2 are most useful for fellow HAWC collaborators looking to replicate
723 the Glory Duck analysis.

724 **6.2.1 Itemized HAWC files**

- 725 • Detector Resolution: `response_aerie_svn_27754_systematics_best_mc_test_no`
726 `broadpulse_10pctlogchargesmearing_0.63qe_25kHzNoise_run5481_curvatu`
727 `re0_index3.root`
- 728 • Data Map: `maps-20180119/liff/maptree_1024.root`
- 729 • Spectral Dictionary: `DM_CirrelliSpectrum_dict_gammas.npy`
- 730 • Analysis wiki: https://private.hawc-observatory.org/wiki/index.php/Glory_Duck_Multi-Experiment_Dark_Matter_Search

732 **6.2.2 Software Tools and Development**

733 This analysis was performed using HAL and 3ML [42, 43] in Python version 2. I built software
734 to implement the *A Poor Particle Physicist Cookbook for Dark Matter Indirect Detection* (PPPC)
735 [44] DM spectral model and dSphs spatial model from [45] for HAWC analysis. A NumPy version
736 of this dictionary was made for both Py2 and Py3. The code base for creating this dictionary is
737 linked on my GitLab sandbox:

- 738 • Py2: [Dictionary Generator \(Deprecated\)](#)
- 739 • Py3: [PPPC2Dict](#)

740 The analysis was performed using the f_{hit} framework performed in the HAWC Crab paper
741 [42]. The Python2 NumPy dictionary file for gamma-ray final states is `dmCirSpecDict.npy`. The
742 corresponding Python3 file is `DM_CirrelliSpectrum_dict_gammas.npy`. These files can also

743 be used for decay channels and the PPPC describes how [44]. All other software used for data
744 analysis, DM profile generation, and job submission to SLURM are also kept in my sandbox for
745 [the Glory Duck](#) project.

746 6.2.3 Data Set and Background Description

747 The HAWC data maps used for this analysis contain 1017 days of data between runs 2104
748 (2014-11-26) and 7476 (2017-12-20). They were generated from pass 4.0 reconstruction. The
749 analysis is performed using the f_{hit} energy binning scheme with bins (1-9) similar to what was done
750 for the Crab and previous HAWC dSph analysis [42, 46]. Bin 0 was excluded as it has substantial
751 hadronic contamination and poor angular resolution.

752 This analysis was done on dSphs because of their large DM mass content relative to baryonic
753 mass. We consider the following to estimate the background to this study.

- 754 • The dSphs are small in HAWC’s field of view, so the analysis is not sensitive to large or small
755 scale anisotropies.
- 756 • The dSphs used in this analysis are off the galactic plane.
- 757 • The dSphs are baryonically faint relative to their expected dark matter content and are not
758 expected to contain high energy gamma-ray sources.

759 Therefor we make no additional assumptions on the background from our sources and use
760 HAWC’s standard direct integration method for background estimation [42]. It is possible for
761 gamma rays from DM annihilation to scatter in transit to HAWC via Inverse Compton Scattering
762 (ICS). This was investigated and its impact on the flux is basically zero. Supporting information
763 on this is in Section 6.7.1

764 6.3 Analysis

765 The expected differential photon flux from DM-DM annihilation to standard model particles,
766 $d\Phi_\gamma/dE_\gamma$, over solid angle, Ω is described by the familiar equation.

$$\frac{d\Phi_\gamma}{dE_\gamma} = \frac{\langle\sigma v\rangle}{8\pi m_\chi^2} \frac{dN_\gamma}{dE_\gamma} \times \int_{\text{source}} d\Omega \int_{l.o.s} \rho_\chi^2 dl(r, \theta') \quad (6.1)$$

767 Where $\langle \sigma v \rangle$ is the velocity weighted annihilation cross-section. $\frac{dN}{dE}$ is the expected differential
 768 number of photons produced at each energy per annihilation. m_χ is the rest mass of the supposed
 769 DM particle. ρ_χ is the DM density. J is the astrophysical J-factor and is defined as

$$J = \int d\Omega \int_{l.o.s} dl \rho_\chi^2(r, \theta') \quad (6.2)$$

770 l is the distance to the source from Earth. r is the radial distance from the center of the source. θ' is
 771 the half angle defining a cone containing the DM source. How each component is synthesized and
 772 considered for HAWC's analysis is presented in the following sections. Section 6.3.1 presents the
 773 particle physics model for DM annihilation. Section 6.3.2 presents the spatial distributions built
 774 for each dSph.

775 6.3.1 $\frac{dN_\gamma}{dE_\gamma}$ - Particle Physics Component

776 For these spectra, we import the PPPC with Electroweak (EW) corrections [44]. The spectrum
 777 is implemented as a model script in astromodels for 3ML. The EW corrections were previously not
 778 considered for HAWC and are significant for DM annihilating to EW coupled SM particles such
 779 as all leptons, and the γ , Z , and W bosons [46]. Figure 6.2 demonstrates the significance of EW
 780 corrections for W boson annihilation. Across EW SM channels, the gamma-ray spectra become
 781 harder than spectra without EW corrections. Tables from the PPPC were reformatted into Python
 782 NumPy dictionaries for collaboration-wide use. A class in astromodels was developed to include
 783 the EW correction from the PPPC and is aptly named `PPPCSpectra` within `DM_models.py`.

784 6.3.2 J - Astrophysical Component

785 The J-factor profiles for each source are imported from Geringer-Sameth (referred to with \mathcal{GS})
 786 [45]. These were pulled from the publication as $J(\theta)$, where θ is the angular separation from the
 787 center of the source. HAWC requires maps in terms of $\frac{dJ}{d\Omega}$, so the conversion from the maps was
 788 done in the following way...

789 First, convert the angular distances to solid angles

$$\Omega = 2 \cdot \pi(1 - \cos(\theta)) \quad (6.3)$$

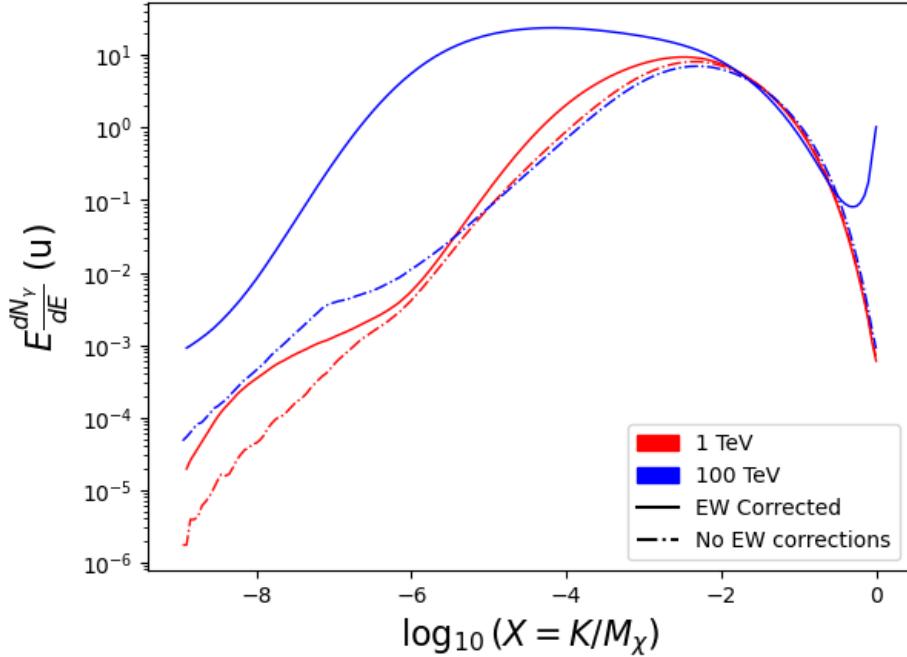


Figure 6.2 Effect of Electroweak (EW) corrections on expected DM annihilation spectrum for $\chi\chi \rightarrow W^-W^+$. Solid lines are spectral models that consider EW corrections. Dash-dot lines are spectral models without EW corrections. Red lines are models for $M_\chi = 1$ TeV. Blue lines represent models for $M_\chi = 100$ TeV. All models are sourced from the PPPC4DMID [44].

which reduces with a small angle approximation to $\pi\theta^2$. Next, the central difference for both the ΔJ and $\Delta\Omega$ value were calculated from the discretized $J(\theta)$ with the central difference stencil:

$$\Delta\phi_i = \phi_{i+1} - \phi_{i-1} \quad (6.4)$$

Where ϕ is either Ω or J . These were done separately in case the grid spacing in θ was not uniform. Finally, these lists are divided so that we are left with an approximation of the $dJ/d\Omega$ profile that is a function of θ . Admittedly, this is an approximation method for the map which introduces small errors compared to the true profile estimate. This was checked as a systematic against the author's profiling of the spatial distribution and is documented in Section 6.8.1.

With $\frac{dJ}{d\Omega}(\theta)$, a map is generated, first by filling in the north-east quadrant of the map. This quadrant is then reflected twice, vertically then horizontally, to fill the full map. Maps are then normalized by dividing the discrete 2D integral of the map. The 2D integral was a simple height

800 of bins, Newton's integral:

$$p^2 \cdot \sum_{i,j=0}^{N,M} \frac{dJ}{d\Omega}(\theta_{i,j}, \phi_{i,j}) \quad (6.5)$$

801 These maps are HEALpix maps with NSIDE 16384 and saved in the `.fits` format.

802 Another DM spatial distribution model from Bonnivard (\mathcal{B}) [47] was used for the Glory Duck
803 study. However, to save computational time, limits from \mathcal{GS} were scaled to \mathcal{B} instead of each
804 experiment performing a full study a second time. How these models compare is demonstrated
805 for each dSph in Figure 6.16 and Figure 6.17 Plots of these maps are provided for each source
806 in chapter A Examples of the two most impactful dSphs derived from \mathcal{GS} , Segue1 and Coma
807 Berenices are featured in Figure 6.3

808 **6.3.3 Source Selection and Annihilation Channels**

809 We use many of the dSphs presented in HAWC's previous dSph DM search [46]. HAWC's
810 sources for Glory Duck include Boötes I, Coma Berenices, Canes Venatici I + II, Draco, Hercules,
811 Leo I, II, + IV, Segue 1, Sextans, and Ursa Major I + II. A full description of all sources used
812 in Glory Duck is found in Table 6.1. Triangulum II was excluded from the Glory Duck analysis
813 because of large uncertainties in its J factor. Ursa Minor was excluded from HAWC's contribution
814 to the combination because the source extension model extended Ursa Minor beyond HAWC's field
815 of view. Ursa Minor was not expected to contribute significantly to the combined limit, so work
816 was not invested in a solution to include Ursa Minor.

817 This analysis improves on the previous HAWC dSph paper [46] in the following ways. Pre-
818 viously, the dSphs were treated and implemented as point sources. For this analysis, dSphs are
819 modeled and treated as extended source. The impact of this change with respect to the upper limit
820 is source dependent and is explored in Section 6.7.2. Previously, the particle physics model used for
821 gamma-ray spectra from DM annihilation did not have EW corrections where the PPPC includes
822 them. Finally, the gamma-ray ray dataset is much larger. The study performed here analyzes over
823 1000 days of data compared to 507.

824 The SM annihilation channels probed for the Glory Duck combination include $b\bar{b}$, $e\bar{e}$, $\mu\bar{\mu}$, $\tau\bar{\tau}$,
825 $t\bar{t}$, W^+W^- , and ZZ . A summary of all sources, with a description of each experiments' sensitivity

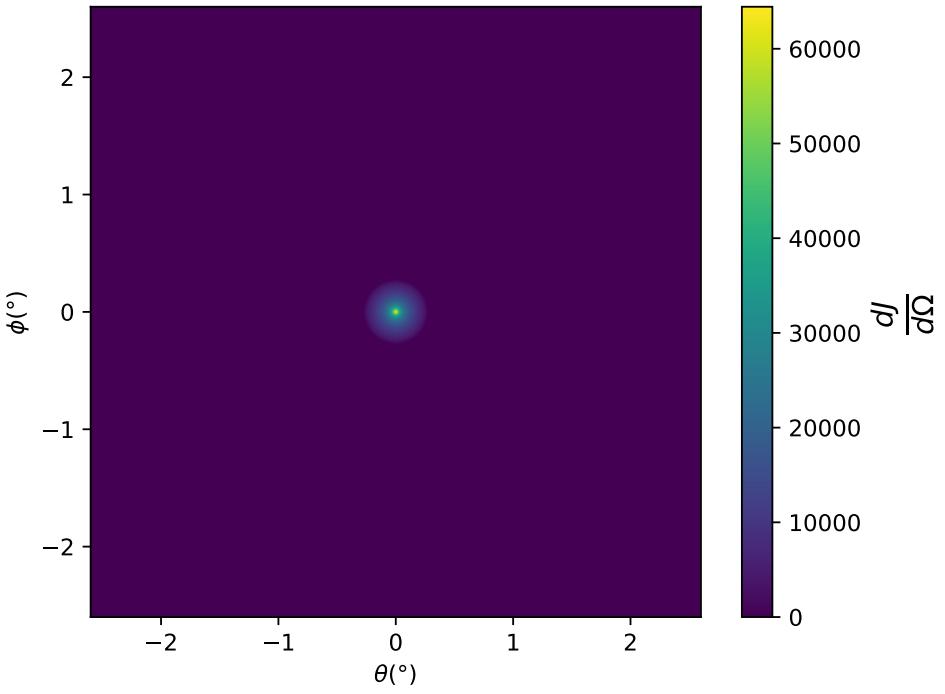
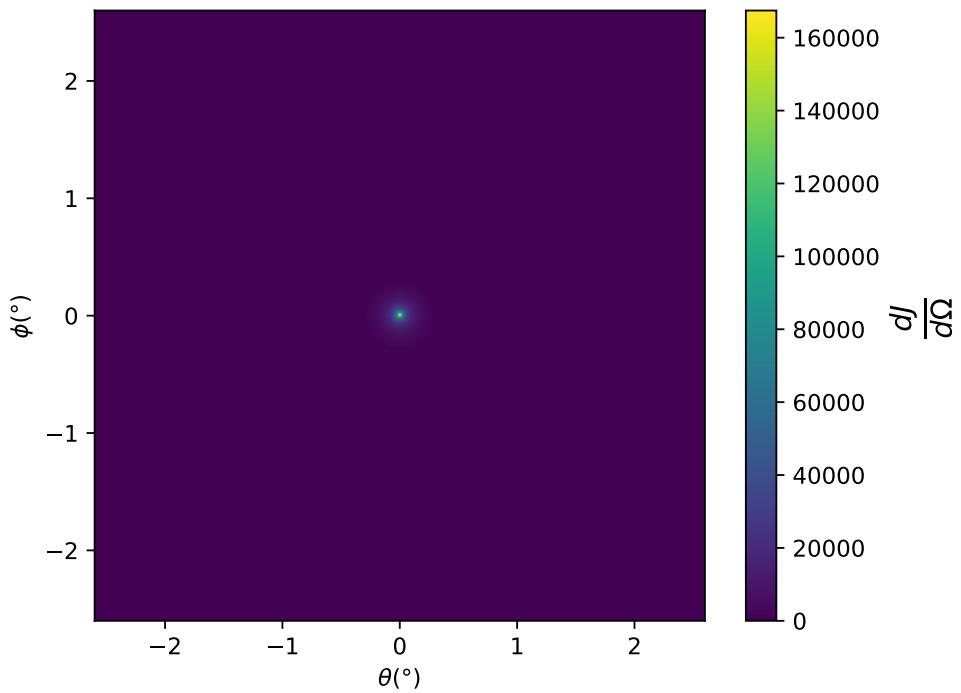


Figure 6.3 $\frac{dJ}{d\Omega}$ maps for Segue1 (top) and Coma Berenices (bottom). Origin is centered on the specific dwarf spheroidal galaxies (dSph). X and Y axes are the angular separation from the center of the dwarf. Plots of the remaining 11 dSph HAWC studied are linked in Fig. A.1.

Table 6.1 Summary of the relevant properties of the dSphs used in the present work. Column 1 lists the dSphs. Columns 2 and 3 present their heliocentric distance and galactic coordinates, respectively. Columns 4 and 5 report the J -factors of each source given from the \mathcal{GS} and \mathcal{B} independent studies and their estimated $\pm 1\sigma$ uncertainties. The values $\log_{10} J$ (\mathcal{GS} set) [45] correspond to the mean J -factor values for a source extension truncated at the outermost observed star. The values $\log_{10} J$ (\mathcal{B} set) [47] are provided for a source extension at the tidal radius of each dSph. **Bolded sources are within HAWC's field of view and provided to the Glory Duck analysis.**

Name	Distance (kpc)	l, b ($^{\circ}$)	$\log_{10} J$ (\mathcal{GS} set) $\log_{10}(\text{GeV}^2 \text{cm}^{-5} \text{sr})$	$\log_{10} J$ (\mathcal{B} set) $\log_{10}(\text{GeV}^2 \text{cm}^{-5} \text{sr})$
Boötes I	66	358.08, 69.62	$18.24^{+0.40}_{-0.37}$	$18.85^{+1.10}_{-0.61}$
Canes Venatici I	218	74.31, 79.82	$17.44^{+0.37}_{-0.28}$	$17.63^{+0.50}_{-0.20}$
Canes Venatici II	160	113.58, 82.70	$17.65^{+0.45}_{-0.43}$	$18.67^{+1.54}_{-0.97}$
Carina	105	260.11, -22.22	$17.92^{+0.19}_{-0.11}$	$18.02^{+0.36}_{-0.15}$
Coma Berenices	44	241.89, 83.61	$19.02^{+0.37}_{-0.41}$	$20.13^{+1.56}_{-1.08}$
Draco	76	86.37, 34.72	$19.05^{+0.22}_{-0.21}$	$19.42^{+0.92}_{-0.47}$
Fornax	147	237.10, -65.65	$17.84^{+0.11}_{-0.06}$	$17.85^{+0.11}_{-0.08}$
Hercules	132	28.73, 36.87	$16.86^{+0.74}_{-0.68}$	$17.70^{+1.08}_{-0.73}$
Leo I	254	225.99, 49.11	$17.84^{+0.20}_{-0.16}$	$17.93^{+0.65}_{-0.25}$
Leo II	233	220.17, 67.23	$17.97^{+0.20}_{-0.18}$	$18.11^{+0.71}_{-0.25}$
Leo IV	154	265.44, 56.51	$16.32^{+1.06}_{-1.70}$	$16.36^{+1.44}_{-1.65}$
Leo V	178	261.86, 58.54	$16.37^{+0.94}_{-0.87}$	$16.30^{+1.33}_{-1.16}$
Leo T	417	214.85, 43.66	$17.11^{+0.44}_{-0.39}$	$17.67^{+1.01}_{-0.56}$
Sculptor	86	287.53, -83.16	$18.57^{+0.07}_{-0.05}$	$18.63^{+0.14}_{-0.08}$
Segue I	23	220.48, 50.43	$19.36^{+0.32}_{-0.35}$	$17.52^{+2.54}_{-2.65}$
Segue II	35	149.43, -38.14	$16.21^{+1.06}_{-0.98}$	$19.50^{+1.82}_{-1.48}$
Sextans	86	243.50, 42.27	$17.92^{+0.35}_{-0.29}$	$18.04^{+0.50}_{-0.28}$
Ursa Major I	97	159.43, 54.41	$17.87^{+0.56}_{-0.33}$	$18.84^{+0.97}_{-0.43}$
Ursa Major II	32	152.46, 37.44	$19.42^{+0.44}_{-0.42}$	$20.60^{+1.46}_{-0.95}$
Ursa Minor	76	104.97, 44.80	$18.95^{+0.26}_{-0.18}$	$19.08^{+0.21}_{-0.13}$

826 to the source, is provided in Table 6.2.

827 6.4 Likelihood Methods

828 6.4.1 HAWC Likelihoods

829 For every analysis bin in energy, f_{hit} bins (1-9), and location, we can expect N signal events and
830 B background events. The expected number of excess signal events from dark matter annihilation,

Table 6.2 Summary of dSph observations by each experiment used in this work. A ‘-’ indicates the experiment did not observe the dSph for this study. For Fermi-LAT, the exposure at 1 GeV is given. For HAWC, $|\Delta\theta|$ is the absolute difference between the source declination and HAWC latitude. HAWC is more sensitive to sources with smaller $|\Delta\theta|$. For IACTs, we show the zenith angle range, the total exposure, the energy range, the angular radius θ of the signal or ON region, the ratio of exposures between the background-control (OFF) and signal (ON) regions (τ), and the significance of gamma-ray excess in standard deviations, σ .

Source name	Fermi-LAT	HAWC	H.E.S.S, MAGIC, VERITAS						
	Exposure (10^{11} s m 2)	$ \Delta\theta $ ($^\circ$)	IACT	Zenith ($^\circ$)	Exposure (h)	Energy range (GeV)	θ ($^\circ$)	τ	S (σ)
Boötes I	2.6	4.5	VERITAS	15 – 30	14.0	100–41000	0.10	8.6	-1.0
Canes Venatici I	2.9	14.6	–	–	–	–	–	–	–
Canes Venatici II	2.9	15.3	–	–	–	–	–	–	–
Carina	3.1	–	H.E.S.S.	27 – 46	23.7	310 – 70000	0.10	18.0	-0.3
Coma Berenices	2.7	4.9	H.E.S.S.	47 – 49	11.4	550 – 70000	0.10	14.4	-0.4
Draco	3.8	38.1	MAGIC	5 – 37	49.5	60 – 10000	0.17	1.0	–
			MAGIC	29 – 45	52.1	70 – 10000	0.22	1.0	–
			VERITAS	25 – 40	49.8	120 – 70000	0.10	9.0	-1.0
Fornax	2.7	–	H.E.S.S.	11 – 25	6.8	230 – 70000	0.10	45.5	-1.5
Hercules	2.8	6.3	–	–	–	–	–	–	–
Leo I	2.5	6.7	–	–	–	–	–	–	–
Leo II	2.6	3.1	–	–	–	–	–	–	–
Leo IV	2.4	19.5	–	–	–	–	–	–	–
Leo V	2.4	–	–	–	–	–	–	–	–
Leo T	2.6	–	–	–	–	–	–	–	–
Sculptor	2.7	–	H.E.S.S.	10 – 46	11.8	200 – 70000	0.10	19.8	-2.2
Segue I	2.5	2.9	MAGIC	13 – 37	158.0	60 – 10000	0.12	1.0	-0.5
			VERITAS	15 – 35	92.0	80 – 50000	0.10	7.6	0.7
Segue II	2.7	–	–	–	–	–	–	–	–
Sextans	2.4	20.6	–	–	–	–	–	–	–
Ursa Major I	3.4	32.9	–	–	–	–	–	–	–
Ursa Major II	4.0	44.1	MAGIC	35 – 45	94.8	120 – 10000	0.30	1.0	-2.1
Ursa Minor	4.1	–	VERITAS	35 – 45	60.4	160 – 93000	0.10	8.4	-0.1

831 S , is estimated by convolving Equation (6.1) with HAWC's energy response and pixel point spread
 832 functions. I then compute the test statistic (TS) with the log-likelihood ratio test,

$$\text{TS} = -2 \ln \left(\frac{\mathcal{L}_0}{\mathcal{L}^{\max}} \right) \quad (6.6)$$

834 where \mathcal{L}_0 is the null hypothesis, or no DM emission, likelihood. \mathcal{L}^{\max} is the best fit signal
 835 hypothesis where $\langle \sigma v \rangle$ maximizes the likelihood. We calculate the likelihood of each source and
 836 model, assuming events are Poisson distributed, with

$$\mathcal{L} = \prod_i \frac{(B_i + S_i)^{N_i} e^{-(B_i + S_i)}}{N_i!} \quad (6.7)$$

837 where S_i is the sum of expected number of signal counts. B_i is the number of background counts
 838 observed. N_i is the total number of counts.

839 I also calculate an upper limit on $\langle \sigma v \rangle$ by calculating the 95% confidence level (CL). For the
 840 CL, we define a parameter, TS_{95} , as

$$\text{TS}_{95} \equiv \sum_{\text{bins}} \left[2N \ln \left(1 + \frac{\epsilon S_{\text{ref}}}{B} \right) - 2\epsilon S_{\text{ref}} \right] \quad (6.8)$$

841 where the expected signal counts from a dSph is scaled by ϵ . S_{ref} is the expected number of excess
 842 counts in a bin from DM emission from a dSph with a corresponding annihilation cross-section,
 843 $\langle \sigma v \rangle$. We scan ϵ such that

$$2.71 = \text{TS}_{\max} - \text{TS}_{95} \quad (6.9)$$

844 6.4.2 Glory Duck Joint Likelihood

845 The joint likelihood for the 5-experiment combination was done similarly as Section 6.4.1. We
 846 calculate upper limits on $\langle \sigma v \rangle$ from the TS, Eq. (6.6), and define the likelihood ratio more generally

$$\lambda(\langle \sigma v \rangle | \mathcal{D}_{\text{dSphs}}) = \frac{\mathcal{L}(\langle \sigma v \rangle; \hat{\nu} | \mathcal{D}_{\text{dSphs}})}{\mathcal{L}(\widehat{\langle \sigma v \rangle}; \hat{\nu} | \mathcal{D}_{\text{dSphs}})} \quad (6.10)$$

847 $\mathcal{D}_{\text{dSphs}}$ is the totality of observations across experiments and dSphs. ν are the nuisance parameters
 848 which are the J factors in this study. $\widehat{\langle \sigma v \rangle}$ and $\hat{\nu}$ are the respective estimate that maximize \mathcal{L}
 849 globally. Finally, $\hat{\nu}$ is the set of nuisance parameters that maximize \mathcal{L} for a fixed value of $\langle \sigma v \rangle$.

850 The *complete* joint likelihood, \mathcal{L} that encompasses all observations from all instruments and
 851 dSphs can be factorized into *partial* functions for each dSph l (with $\mathcal{L}_{\text{dSph},l}$) and its J factor (\mathcal{J}_l):

$$\mathcal{L} (\langle \sigma v \rangle; \nu | \mathcal{D}_{\text{dSphs}}) = \prod_{l=1}^{N_{\text{dSphs}}} \mathcal{L}_{\text{dSph},l} (\langle \sigma v \rangle; J_l, \nu_l | \mathcal{D}_l) \times \mathcal{J}_l (J_l | J_{l,\text{obs}}, \sigma_{\log J_l}). \quad (6.11)$$

852 For this study, $N_{\text{dSphs}} = 20$ is the number of dSphs studied. \mathcal{D}_l are the gamma-ray observations
 853 of dSph, l . ν_l are the nuisance parameters modifying the gamma-ray observations of dSph, l ,
 854 but excludes \mathcal{J}_l . \mathcal{J}_l is the J factor for dSph, l , as defined in Equation (6.2), and it is a nuisance
 855 parameter whose value is unknown. $\log_{10} J_{l,\text{obs}}$ and $\sigma_{\log J_l}$ are obtained from fitting a log-normal
 856 function of $J_{l,\text{obs}}$ to the posterior distribution of J_l [48]. $\log_{10} J_{l,\text{obs}}$ and $\sigma_{\log J_l}$ values are provided
 857 in Table 6.1. The term \mathcal{J}_l constraining J_l is written as:

$$\mathcal{J}_l (J_l | J_{l,\text{obs}}, \sigma_{\log J_l}) = \frac{1}{\ln(10) J_{l,\text{obs}} \sqrt{2\pi} \sigma_{\log J_l}} \exp\left(-\frac{(\log_{10} J_l - \log_{10} J_{l,\text{obs}})^2}{2\sigma_{\log J_l}^2}\right). \quad (6.12)$$

858 Both the \mathcal{GS} and \mathcal{B} , displayed in Table 6.1, sets of J factors are used in this analysis. Equation (6.12)
 859 is also normalized, so it can also be interpreted as a probability density function (PDF) for $J_{l,\text{obs}}$.
 860 From Equation (6.1), we can also see that $\langle \sigma v \rangle$ and J_l are degenerate when computing $\mathcal{L}_{\text{dSph},l}$.
 861 Therefore, as noted in [49], it is sufficient to compute $\mathcal{L}_{\text{dSph},l}$ versus $\langle \sigma v \rangle$ for a fixed value of J_l .
 862 We used $J_{l,\text{obs}}(\mathcal{GS})$ reported in Tab. 6.1, in order to perform the profile of \mathcal{L} with respect to J_l .
 863 The degeneracy implies that for any $J'_l \neq J_{l,\text{obs}}$ (in practice in our case we used $J'_l = J_{l,\text{obs}}(\mathcal{B})$ to
 864 compute results from a different set of J factors):

$$\mathcal{L}_{\text{dSph},l} (\langle \sigma v \rangle; J'_l, \nu_l | \mathcal{D}_l) = \mathcal{L}_{\text{dSph},l} \left(\frac{J'_l}{J_{l,\text{obs}}} \langle \sigma v \rangle; J_{l,\text{obs}}, \nu_l | \mathcal{D}_l \right), \quad (6.13)$$

865 which is a straightforward rescaling operation that reduces the computational needs of the profiling
 866 operation since:

$$\mathcal{L} (\langle \sigma v \rangle; \hat{\nu} | \mathcal{D}_{\text{dSphs}}) = \prod_{l=1}^{N_{\text{dSphs}}} \max_{J_l} \left[\mathcal{L}_{\text{dSph},l} (\langle \sigma v \rangle; J_l, \hat{\nu}_l | \mathcal{D}_l) \times \mathcal{J}_l (J_l | J_{l,\text{obs}}, \sigma_{\log J_l}) \right]. \quad (6.14)$$

867 In addition, Eq. (6.13) enables the combination of data from different gamma-ray instruments and
 868 observed dSphs via tabulated values of $\mathcal{L}_{\text{dSph},l}$, or equivalently of λ from Eq. (6.10) as was done in

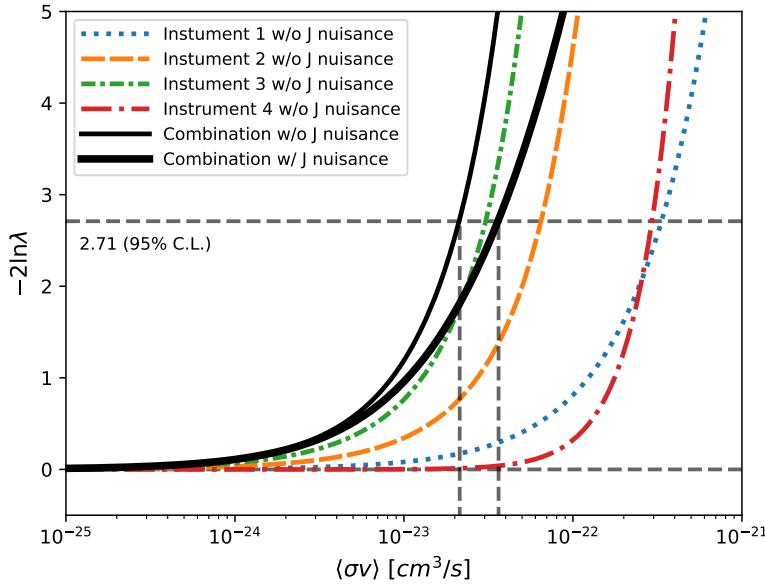


Figure 6.4 Illustration of the combination technique showing a comparison between $-2 \ln \lambda$ provided by four instruments (colored lines) from the observation of the same dSph without any J nuisance and their sum, *i.e.* the resulting combined likelihood (thin black line). According to the test statistics of Equation (6.6), the intersection of the likelihood profiles with the line $-2 \ln \lambda = 2.71$ indicates the 95% C.L. upper limit on $\langle \sigma v \rangle$. The combined likelihood (thin black line) shows a smaller value of upper limit on $\langle \sigma v \rangle$ than those derived by individual instruments. We also show how the uncertainties on the J factor effects the combined likelihood and degrade the upper limit on $\langle \sigma v \rangle$ (thick black line). All likelihood profiles are normalized so that the global minimum $\widehat{\langle \sigma v \rangle}$ is 0. We note that each profile depends on the observational conditions in which a target object was observed. The sensitivity of a given instrument can be degraded and the upper limits less constraining if the observations are performed in non-optimal conditions such as a high zenith angle or a short exposure time.

869 this work, versus $\langle \sigma v \rangle$. $\mathcal{L}_{dSph,l}$ is computed for a fixed value of J_l and profiled with respect to all
 870 instrumental nuisance parameters ν_l , these nuisance parameters are discussed in more detail below.
 871 These values are produced by each detector independently and therefore there is no need to share
 872 sensitive low-level information used to produce them, such as event lists. Figure 6.4 illustrates the
 873 multi-instrument combination technique used in this study with a comparison of the upper limit
 874 on $\langle \sigma v \rangle$ obtained from the combination of the observations of four experiments towards one dSph
 875 versus the upper limit from individual instruments. It also shows graphically the effect of the
 876 J -factor uncertainty on the combined observations.

877 The *partial* joint likelihood function for gamma-ray observations of each dSph ($\mathcal{L}_{dSph,l}$) is

written as the product of the likelihood terms describing the $N_{\text{exp},l}$ observations performed with any of our observatories:

$$\mathcal{L}_{\text{dSph},l} (\langle \sigma v \rangle; J_l, \nu_l | \mathcal{D}_l) = \prod_{k=1}^{N_{\text{exp},l}} \mathcal{L}_{lk} (\langle \sigma v \rangle; J_l, \nu_{lk} | \mathcal{D}_{lk}), \quad (6.15)$$

where each \mathcal{L}_{lk} term refers to an observation of the l -th dSph with associated k -th instrument responses. $N_{\text{exp},l}$ varies from dSph to dSph and can be inferred from Table 6.2.

Each collaboration separately analyzes their data for \mathcal{D}_{lk} corresponding to dSph l and gamma-ray detector k , using as many common assumptions as possible in the analysis. HAWC’s treatment was described earlier in Section 6.4.1 whereas the specifics of the remaining experiments is left to the publication. We compute the values for the likelihood functions \mathcal{L}_{lk} (see Eq. (6.15)) for a fixed value of J_l and profile over the rest of the nuisance parameters ν_{lk} . Then, values of λ from Eq. (6.10) are computed as a function of $\langle \sigma v \rangle$, and shared using a common format. Results are computed for seven annihilation channels, W^+W^- , ZZ , $b\bar{b}$, $t\bar{t}$, e^+e^- , $\mu^+\mu^-$, and $\tau^+\tau^-$ over 62 m_χ values between 5 GeV and 100 TeV provided in [44]. The $\langle \sigma v \rangle$ range is defined between 10^{-28} and $10^{-18} \text{cm}^3 \cdot \text{s}^{-1}$, with 1001 logarithmically spaced values. The likelihood combination, i.e. Equation (6.11), and profile over the J -factor to compute the profile likelihood ratio λ , Equation (6.10), are carried out with two different public analysis software packages, namely `gLike` [50] and `LklCom` [51], that provide the same results [52].

As mentioned previously, each experiment computes the \mathcal{L}_{lk} from Equation (6.10) differently. The remainder of this section highlights the differences in this calculation across the experiments. Four experiments, namely *Fermi*-LAT, H.E.S.S., HAWC and MAGIC, use a binned likelihood to compute the \mathcal{L}_{lk} . For these experiments, for each observation \mathcal{D}_{lk} of a given dSph l carried out using a given gamma-ray detector k , the binned likelihood function is:

$$\mathcal{L}_{lk} (\langle \sigma v \rangle; J_l, \nu_{lk} | \mathcal{D}_{lk}) = \prod_{i=1}^{N_E} \prod_{j=1}^{N_P} \left[\mathcal{P}(s_{lk,ij}(\langle \sigma v \rangle, J_l, \nu_{lk}) + b_{lk,ij}(\nu_{lk}) | N_{lk,ij}) \right] \times \mathcal{L}_{lk,\nu} (\nu_{lk} | \mathcal{D}_{\nu_{lk}}) \quad (6.16)$$

where N_E and N_P are the number of considered bins in reconstructed energy and arrival direction, respectively; \mathcal{P} represents a Poisson PDF for the number of gamma-ray candidate events $N_{lk,ij}$

901 observed in the i -th bin in energy and j -th bin in arrival direction, when the expected number is
 902 the sum of the expected mean number of signal events s_{ij} (produced by DM annihilation) and of
 903 background events b_{ij} ; $\mathcal{L}_{lk,\nu}$ is the likelihood term for the extra ν_{lk} nuisance parameters that vary
 904 from one instrument k to another. The expected counts for signal events s_{ij} for a given dSph l and
 905 detector k is given by:

$$s_{ij}(\langle\sigma\nu\rangle, J) = \int_{E'_{\min,i}}^{E'_{\max,i}} dE' \int_{P'_{\min,j}}^{P'_{\max,j}} d\Omega' \int_0^\infty dE \int_{\Delta\Omega_{tot}} d\Omega \int_0^{T_{\text{obs}}} dt \frac{d^2\Phi(\langle\sigma\nu\rangle, J)}{dEd\Omega} \text{IRF}(E', P' | E, P, t) \quad (6.17)$$

906 where E' and E are the reconstructed and true energies, P' and P the reconstructed and true
 907 arrival directions; $E'_{\min,i}$, $P'_{\min,j}$, $E'_{\max,i}$, and $P'_{\max,j}$ are their lower and upper limits of the i -th
 908 energy bin and the j -th arrival direction bin; T_{obs} is the (dead-time corrected) total observation
 909 time; t is the time along the observations; $d^2\Phi/dEd\Omega$ is the DM flux in the source region (see
 910 Equation (6.1)); and $\text{IRF}(E', P' | E, P, t)$ is the IRF, which can be factorized as the product of the
 911 effective collection area of the detector $A_{\text{eff}}(E, P, t)$, the PDFs for the energy estimator $f_E(E' | E, t)$,
 912 and arrival direction $f_P(P' | E, P, t)$ estimators. Note that for Fermi-LAT, HAWC, MAGIC, and
 913 VERITAS the effect of the finite angular resolution is taken into account through the convolution
 914 of $d\Phi/dEd\Omega$ with f_P in Equation (6.17), whereas in the cases of H.E.S.S. f_P is approximated by a
 915 delta function. This approximation has been made in order to maintain compatibility of the result
 916 with what has been previously published. The difference introduced by this approximation is $< 5\%$
 917 for all considered dSphs. A more comprehensive review of the differences between the analyses of
 918 different instruments can be found in [25].

919 6.5 HAWC Results

920 13 of the 20 dSphs considered for the Glory Duck analysis are within HAWC's field of view.
 921 These dSph are analyzed for emission from DM annihilation according to the likelihood method
 922 described in Section 6.4. The 13 likelihood profiles are then stacked to synthesize a combined
 923 limit on the dark matter cross-section, $\langle\sigma\nu\rangle$. This combination is done for the 7 SM annihilation
 924 channels used in the Glory Duck analysis. Figure 6.5 shows the combined limit for all annihilation
 925 channels with HAWC only observations. We also perform 300 studies of Poisson trials on the

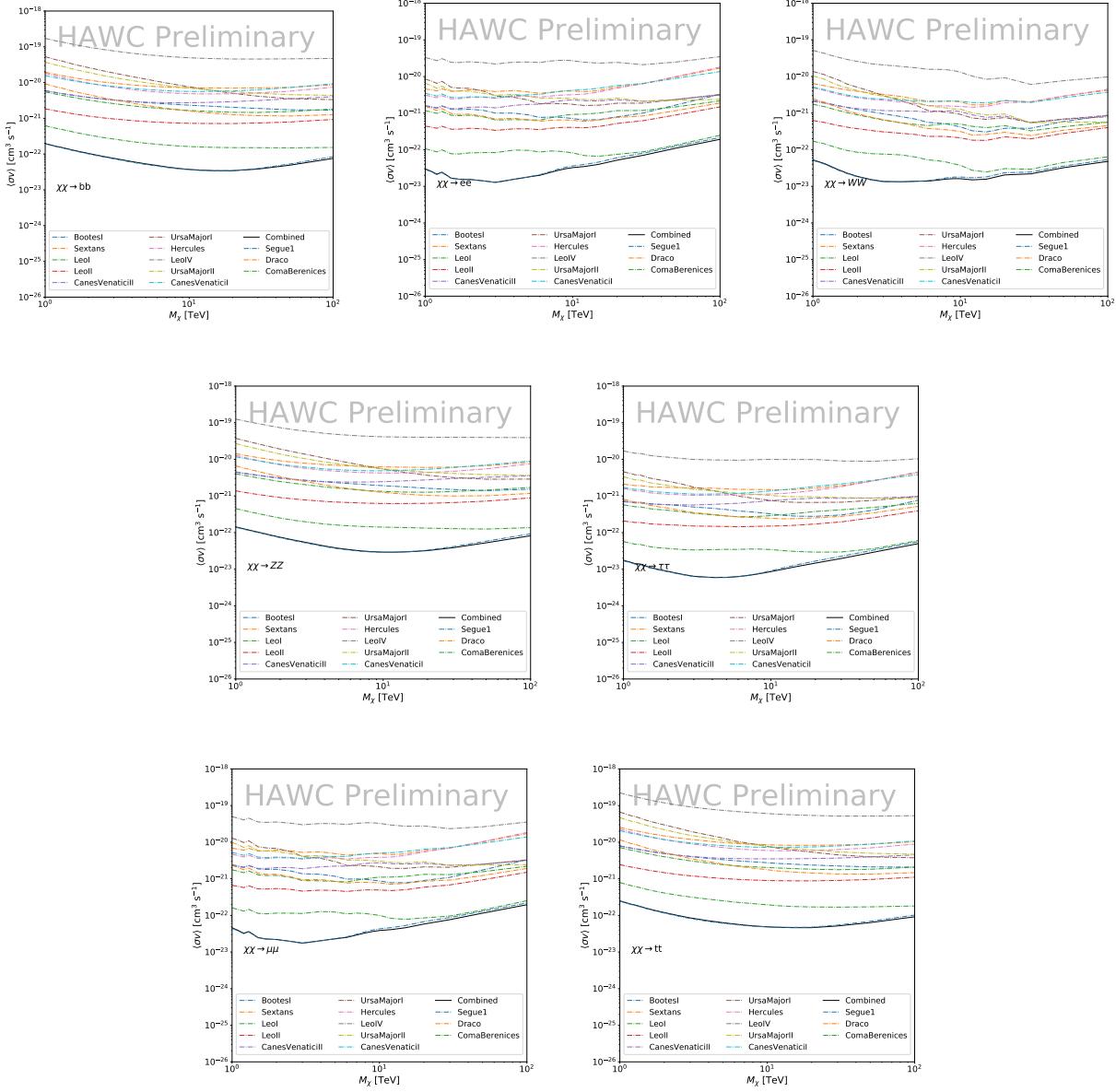


Figure 6.5 HAWC upper limits at 95% confidence level on $\langle\sigma v\rangle$ versus DM mass for seven annihilation channels, using the set of J -factors from Ref. [53]. The solid line represents the observed combined limit. Dashed lines represent limits from individual dSphs.

background. These trials are used to produce HAWC Brazil bands which were shared with the other collaborators for combined Brazil Bands. The results on fitting to HAWC's Poisson trials of the DM hypothesis is shown in Figure 6.7 for all the DM annihilation channels studied for Glory Duck.

No DM was found in HAWC observations. HAWC's limits are dominated by the dSphs Segue1

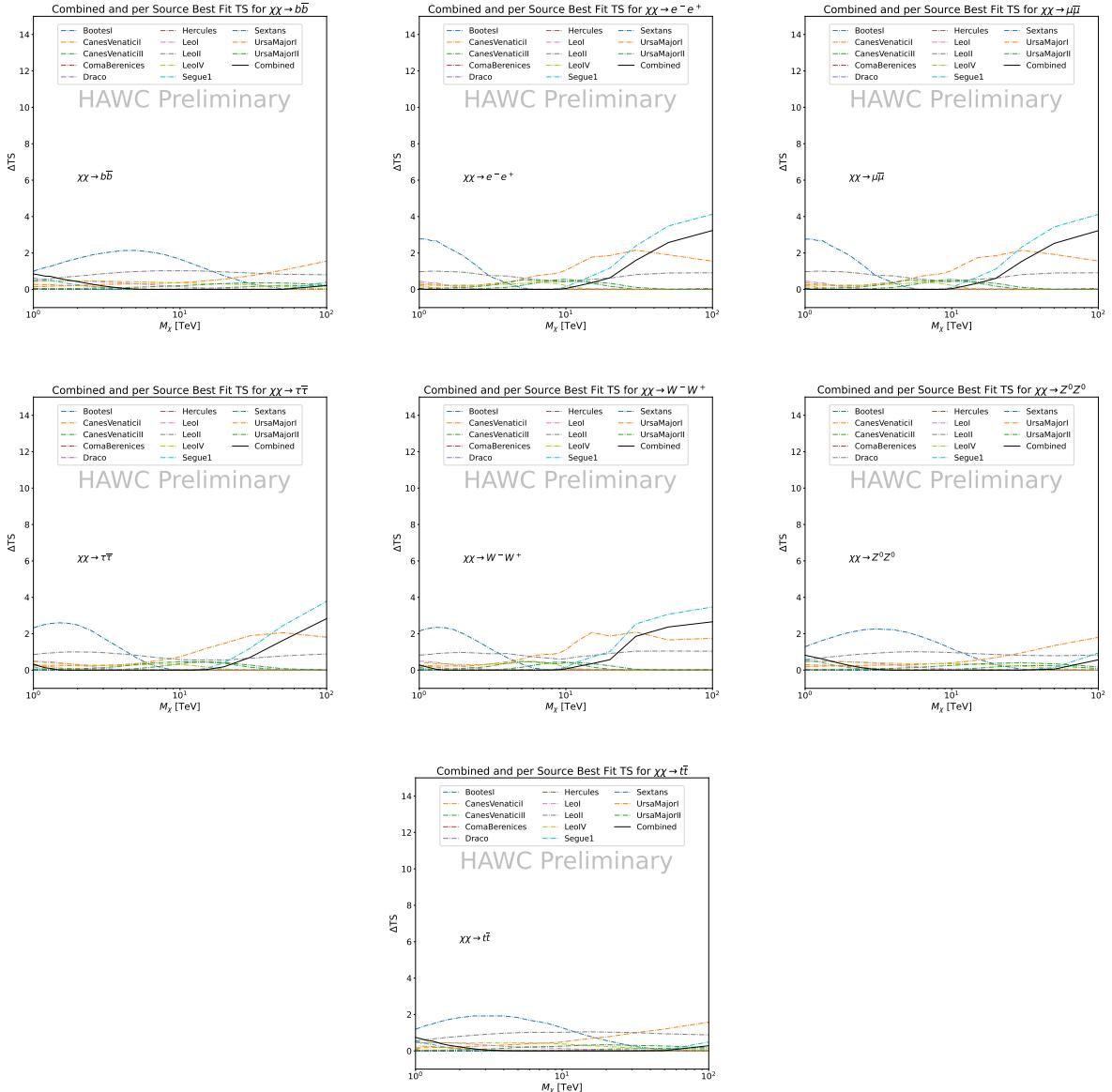


Figure 6.6 HAWC TS values for best fit $\langle \sigma v \rangle$ versus m_χ for seven SM annihilation channels with J factors from \mathcal{GS} . The solid black line shows the combined best fit TS values. The colored, dashed lines are the TS values for each of the 13 sources HAWC studied.

and Coma Berenices. The remaining 11 dSphs do not contribute significantly to the limit because they are at high zenith and/or have much smaller J factors. Even though some remaining dSphs have large J factors, they are towards the edge of HAWC's field of view where HAWC analysis is less sensitive.

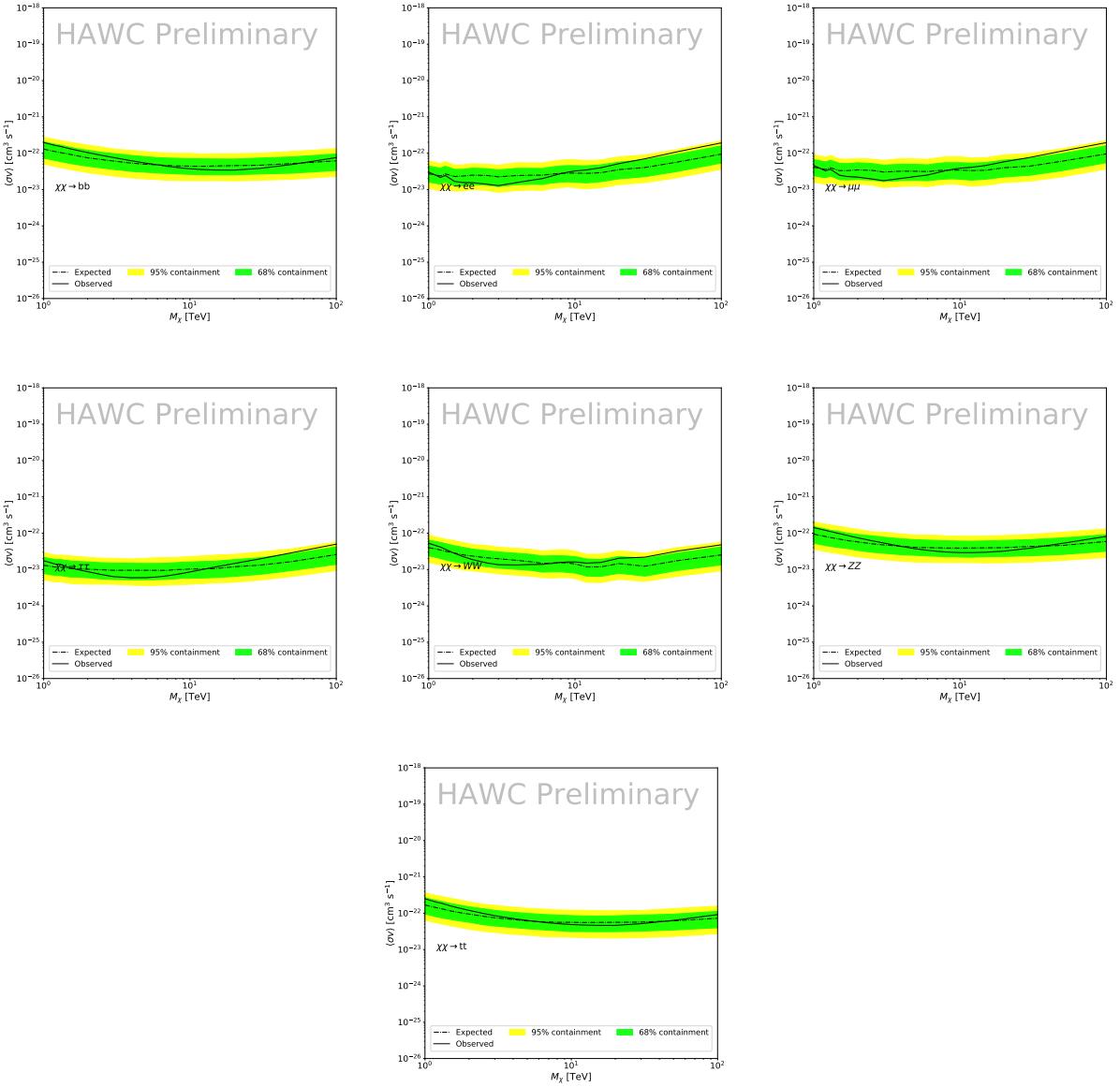


Figure 6.7 HAWC Brazil bands at 95% confidence level on $\langle\sigma v\rangle$ versus DM mass for seven annihilation channels with J -factors from \mathcal{GS} [53]. The solid line represents the combined limit from 13 dSphs. The dashed line is the expected limit. The green band is the 68% containment. The yellow band is the 95% containment.

935 6.6 Glory Duck Combined Results

936 The crux of this analysis is that HAWC's results are combined with 4 other gamma-ray observa-
 937 tories: Fermi-LAT, H.E.S.S., MAGIC, and VERITAS. No significant DM emission was observed
 938 by any of the five instruments. We present the upper limits on $\langle\sigma v\rangle$ assuming seven independent
 939 DM self annihilation channels, namely W^+W^- , Z^+Z^- , $b\bar{b}$, $t\bar{t}$, e^+e^- , $\mu^+\mu^-$, and $\tau^+\tau^-$. The 68%

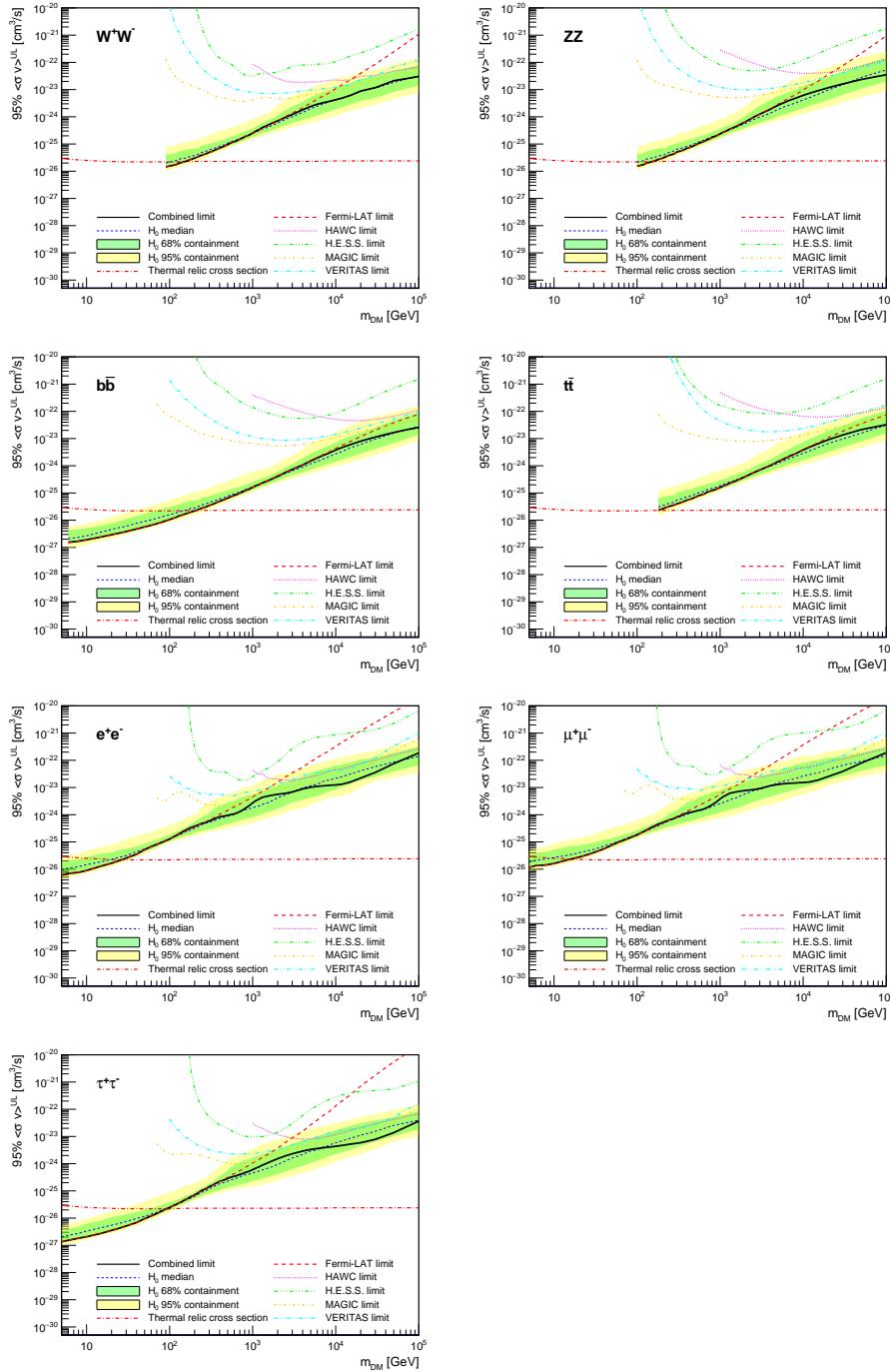


Figure 6.8 Upper limits at 95% confidence level on $\langle\sigma v\rangle$ in function of the DM mass for eight annihilation channels, using the set of J factors from Ref. [53] (\mathcal{GS} set in Table 6.1). The black solid line represents the observed combined limit, the black dashed line is the median of the null hypothesis corresponding to the expected limit, while the green and yellow bands show the 68% and 95% containment bands. Combined upper limits for each individual detector are also indicated as solid, colored lines. The value of the thermal relic cross-section in function of the DM mass is given as the red dotted-dashed line [54].

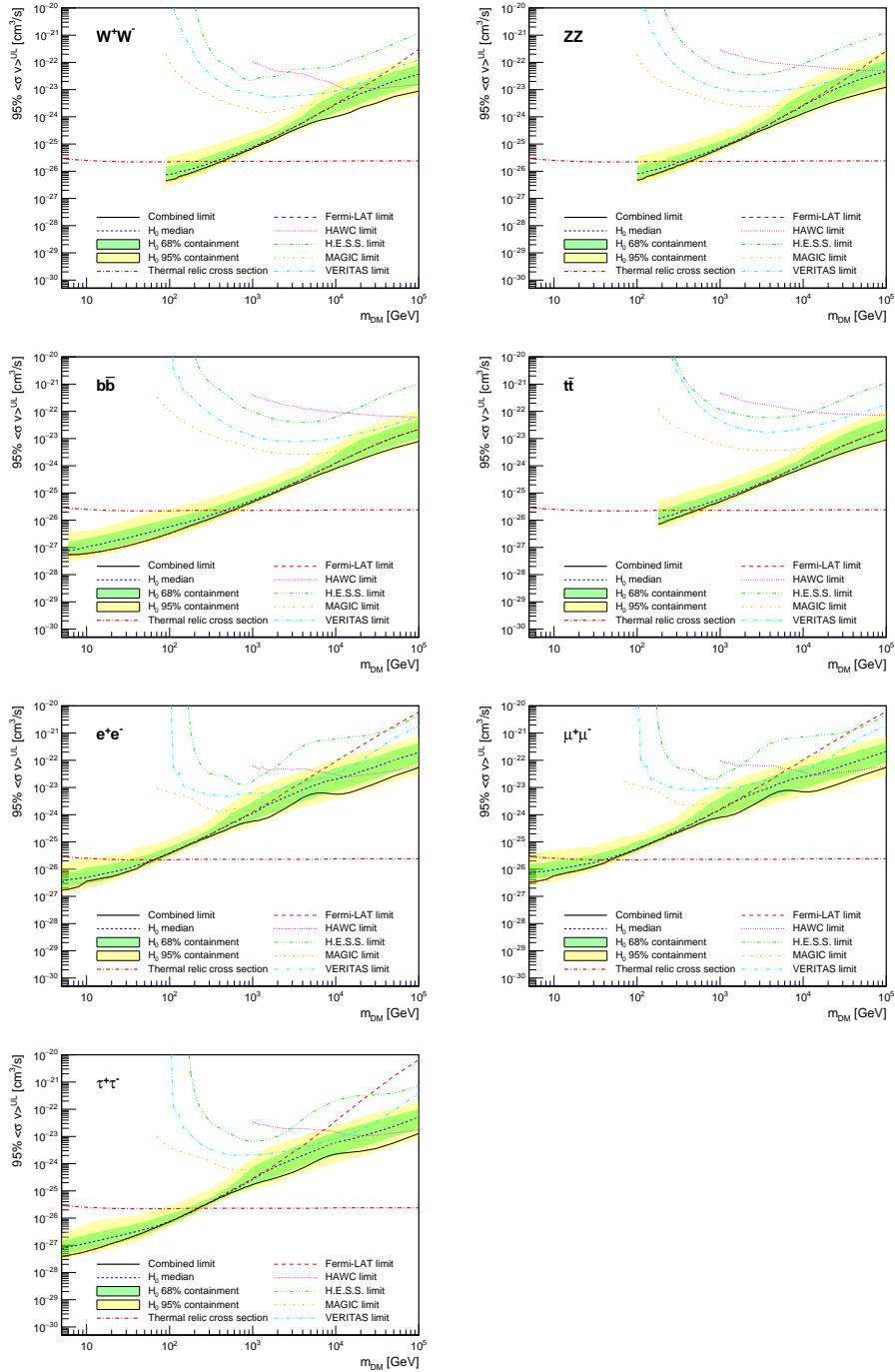


Figure 6.9 Same as Fig. 6.8, using the set of J factors from Ref. [47, 55] (\mathcal{B} set in Table 6.1).

and 95% containment bands are produced from 300 Poisson realizations of the null hypothesis corresponding to each of the combined datasets. These 300 realizations are combined identically to dSph observations. The containment bands and the median are extracted from the distribution of resulting limits on the null hypothesis. These 300 realizations are obtained either by fast simu-

944 lations of the OFF observations, for H.E.S.S., MAGIC, VERITAS, and HAWC, or taken from real
945 observations of empty fields of view in the case of Fermi-LAT [48, 56, 57].

946 The obtained limits are shown in Figure 6.8 for the $\mathcal{G}\mathcal{S}$ set of J -factors [53] and in Figure 6.9
947 for the \mathcal{B} set of J -factors [47, 55]. The combined limits are presented with their 68% and 95%
948 containment bands, and are expected to be close to the median limit when no signal is present.
949 We observe agreement with the null hypothesis for all channels, within 2σ standard deviations,
950 between the observed limits and the expectations given by the median limits. Limits obtained from
951 each detector are also indicated in the figures, where limits for all dSphs observed by the specific
952 instrument have been combined.

953 Below ~ 300 GeV, the *Fermi*-LAT dominates the DM limits for all annihilation channels. From
954 ~ 300 GeV to ~ 2 TeV, *Fermi*-LAT continues to dominate for the hadronic and bosonic DM channels,
955 yet the IACTs (H.E.S.S., MAGIC, and VERITAS) and *Fermi*-LAT all contribute to the limit for
956 leptonic DM channels. For DM masses between ~ 2 TeV to ~ 10 TeV, the IACTs dominate leptonic
957 DM annihilation channels, whereas both the *Fermi*-LAT and the IACTs dominate bosonic and
958 hadronic DM annihilation channels. From ~ 10 TeV to ~ 100 TeV, both the IACTs and HAWC
959 contribute significantly to the leptonic DM limit. For hadronic and bosonic DM, the IACTs and
960 *Fermi*-LAT both contribute strongly.

961 We notice that the limits computed using the \mathcal{B} set of J -factor are always better compared to the
962 ones calculated with the $\mathcal{G}\mathcal{S}$ set. For the W^+W^- , Z^+Z^- , $b\bar{b}$, and $t\bar{t}$ channels, the ratio between the
963 limits computed with the two sets of J -factor is varying between a factor of ~ 3 and ~ 5 depending
964 on the energy, with the largest ratio around 10 TeV. For the channels e^+e^- , $\mu^+\mu^-$, and $\tau^+\tau^-$, the
965 ratio lies between ~ 2 to ~ 6 , being maximum around 1 TeV. Examining Figure 6.16 and Figure 6.17
966 in Section 6.8, these differences are explained by the fact that the \mathcal{B} set provides higher J -factors
967 for the majority of the studied dSphs, with the notable exception of Segue I. The variation on the
968 ratio of the limits for the two sets is due to different dSph dominating the limits depending on the
969 energy. This pushes the range of thermal cross-section which can be excluded to higher mass. This
970 comparison demonstrates the magnitude of systematic uncertainties associated with the choice of

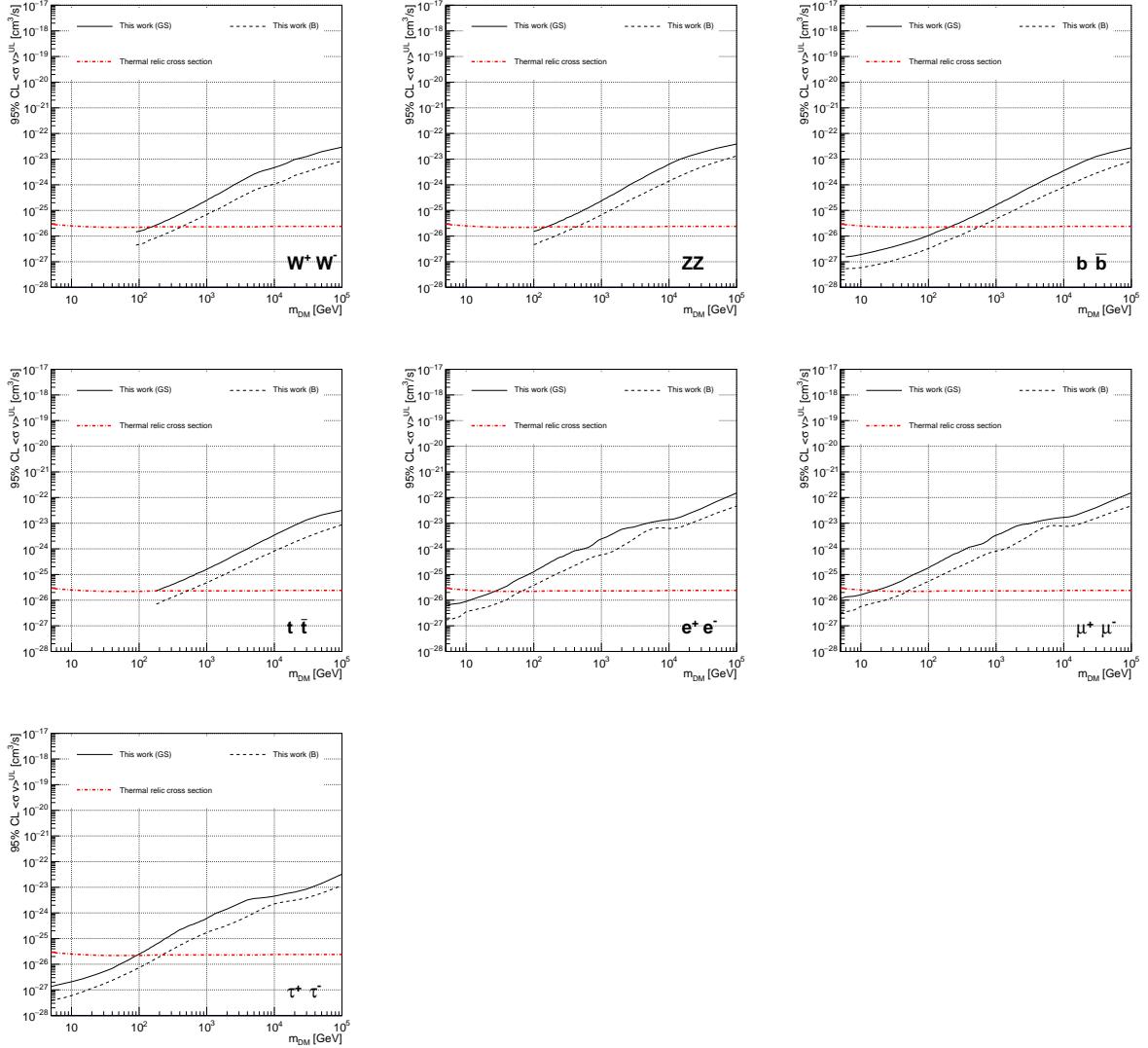


Figure 6.10 Comparisons of the combined limits at 95% confidence level for each of the eight annihilation channels when using the J factors from Ref. [53] (\mathcal{GS} set in Table 6.1), plain lines, and the J factor from Ref. [47, 55] (\mathcal{B} set in Table 6.1), dashed lines. The cross-section given by the thermal relic is also indicated [54].

971 the J -factor

972 This comparison demonstrates the magnitude of systematic uncertainties associated with the
 973 choice of the J -factor calculation. The \mathcal{GS} and \mathcal{B} sets present a difference in the limits for all
 974 channels of about This difference is explained, see Figure 6.16 and Figure 6.17 in Appendix, by the
 975 fact that the \mathcal{B} set provides higher J factors for all dSph except for Segue I. This pushes the range
 976 of thermal cross-section which can be excluded to higher mass.

977 **6.7 HAWC Systematics**

978 **6.7.1 Inverse Compton Scattering**

979 The DM-DM annihilation channels produce many high energy electrons regardless of the
980 primary annihilation channel. These high energy electrons can produce high energy gamma-rays
981 through Inverse Compton Scattering (ICS). If this effect is strong, it would change the morphology
982 of the source and increase the total expected gamma-ray counts from any source. The PPPC [44]
983 provides tools in Mathematica for calculating the impact of ICS for an arbitrary location in the
984 sky for a specified annihilation channel. We calculated the change in gamma-ray counts for DM
985 annihilation to primary $e\bar{e}$ for RA and Dec corresponding to Segue1 and Coma Berenices. These
986 dSphs were chosen because they are the strongest contributors to the limit. $e\bar{e}$ was selected because
987 it would have the largest number of high energy electrons. The effect was found to be on the order
988 of 10^{-7} on the gamma-ray spectrum. As a result, this systematic is not considered in our analysis.

989 **6.7.2 Point Source Versus Extended Source Limits**

990 The previous DM search toward dSph approximated the dSphs as point sources [46]. In
991 this analysis, the dSphs are implemented as extended with J-factor distributions following those
992 produced by [53]. The resolution of the cited map is much finer than HAWC's angular resolution.
993 The vast majority of the J-factor distribution is represented on the central HAWC pixel of the dSph
994 spatial map. However, the neighboring 8 pixels are not negligible and contribute to our limit.

995 Figure 6.11 shows a substantial improvement to the limit for Segue1. Fig. 6.12 however showed
996 identical limits. These disparities are best explained by the relative difference in their J-Factors.
997 Both dSphs pass almost overhead the HAWC detector, however Segue1 has the larger J-Factor
998 between the two. Adjacent pixels to the central pixel will therefore contribute to the limits. This is
999 the case for other dSph that are closer to overhead the HAWC detector.

1000 Comparison plots for all sources and the combined limit can be found in the sandbox for the
1001 Glory Duck project.

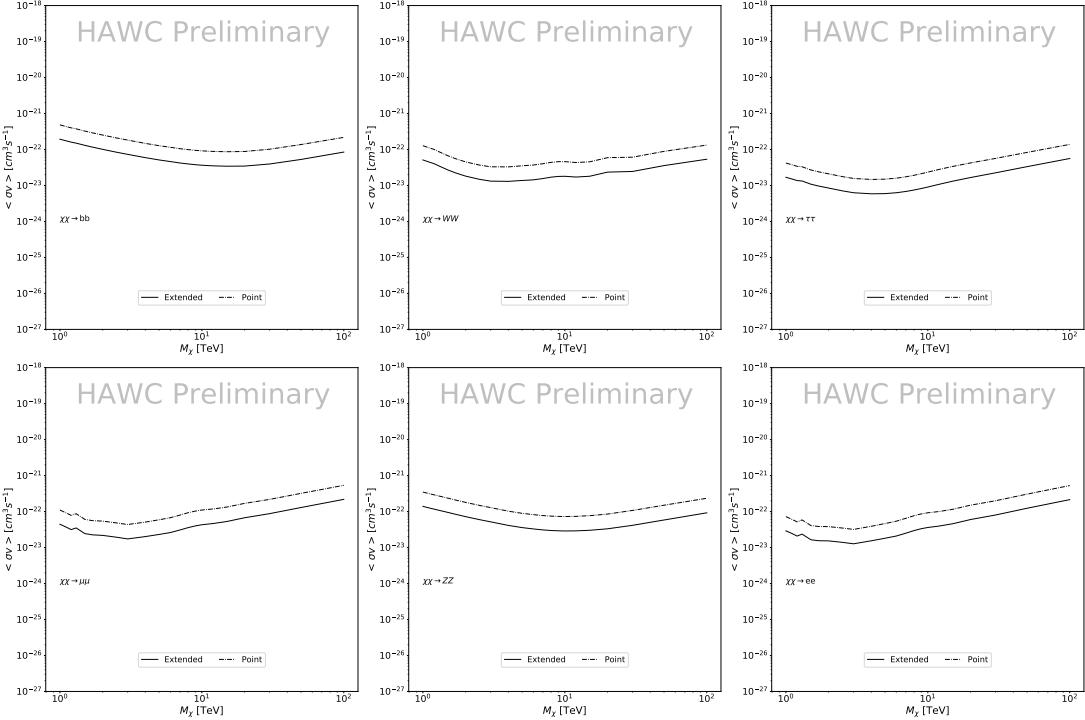


Figure 6.11 Comparisons of the combined limits at 95% confidence level for a point source analysis and extended source using [53] \mathcal{GS} J-factor distributions and PPPC [44] annihilation spectra. Shown are the limits for Segue1 which will have the most significant impact on the combined limit. 6 of the 7 DM annihilation channels are shown. Solid lines are extended source studies. Dashed lines are point source studies. Overall, the extended source analysis improves the limit by a factor of 2.

1002 6.7.3 Impact of Pointing Systematic

1003 During the analysis it was discovered that reconstruction of gamma-rays. Slides describing this
 1004 systematic can be found [here](#). Shown on the presentation is dependence on the pointing systematic
 1005 on declination. New spatial profiles were generated for every dSph and limits were computed for
 1006 the adjusted declination.

1007 Section 6.7.3 demonstrates the impact of this systematic for all DM annihilation channels
 1008 studied by HAWC. The impact is a tiny improvement, yet mostly identical, to the combined limits.

1009 6.8 J-factor distributions

1010 6.8.1 Numerical integration of \mathcal{GS} maps

1011 It was discovered well after the HAWC analysis was completed that the published tables from
 1012 \mathcal{GS} [45] quoted median J-factors were computed in a non-trivial manner. The assumption myself

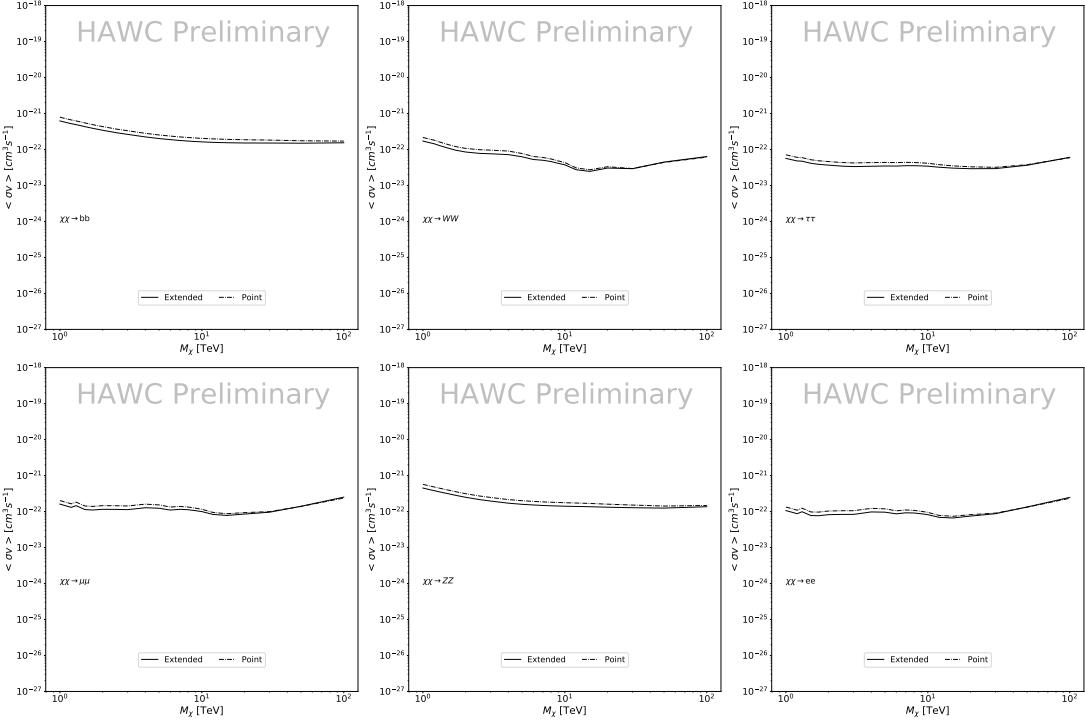


Figure 6.12 Same as Fig. 6.11 on Coma Berenices. This dSph also contributes significantly to the limit. The limits are identical in this case.

and collaborators had been that the published tables represented the J -factor as a function of θ for the best global fit model on a per-source basis. However, this is not the case. Instead, what is published are the best fit model for each dwarf that only considers stars up to the angular separation θ . Therefore, the model is changing for each value of θ for each dwarf. Yet, the introduced features from unique models at each θ are much smaller than the angular resolution of HAWC. It is not expected for these effects to impact the limits and TS greatly as a result.

Median J -factor model profiles were provided by the authors. New maps were generated and analyzed for Segue1 and Coma Berenices. Figure 6.14 shows the differential between maps generated with the method from Section 6.8.1 and from the authors of [45]. These maps were reanalyzed for all SM DM annihilation channels. Upper limits for these channels are shown in Figure 6.15

From Figure 6.15, we can see that the impact of these model difference was no substantial. The observed impact was a fractional effect which is much smaller than the impact from selecting another DM spatial distribution model as was shown in Figure 6.10.

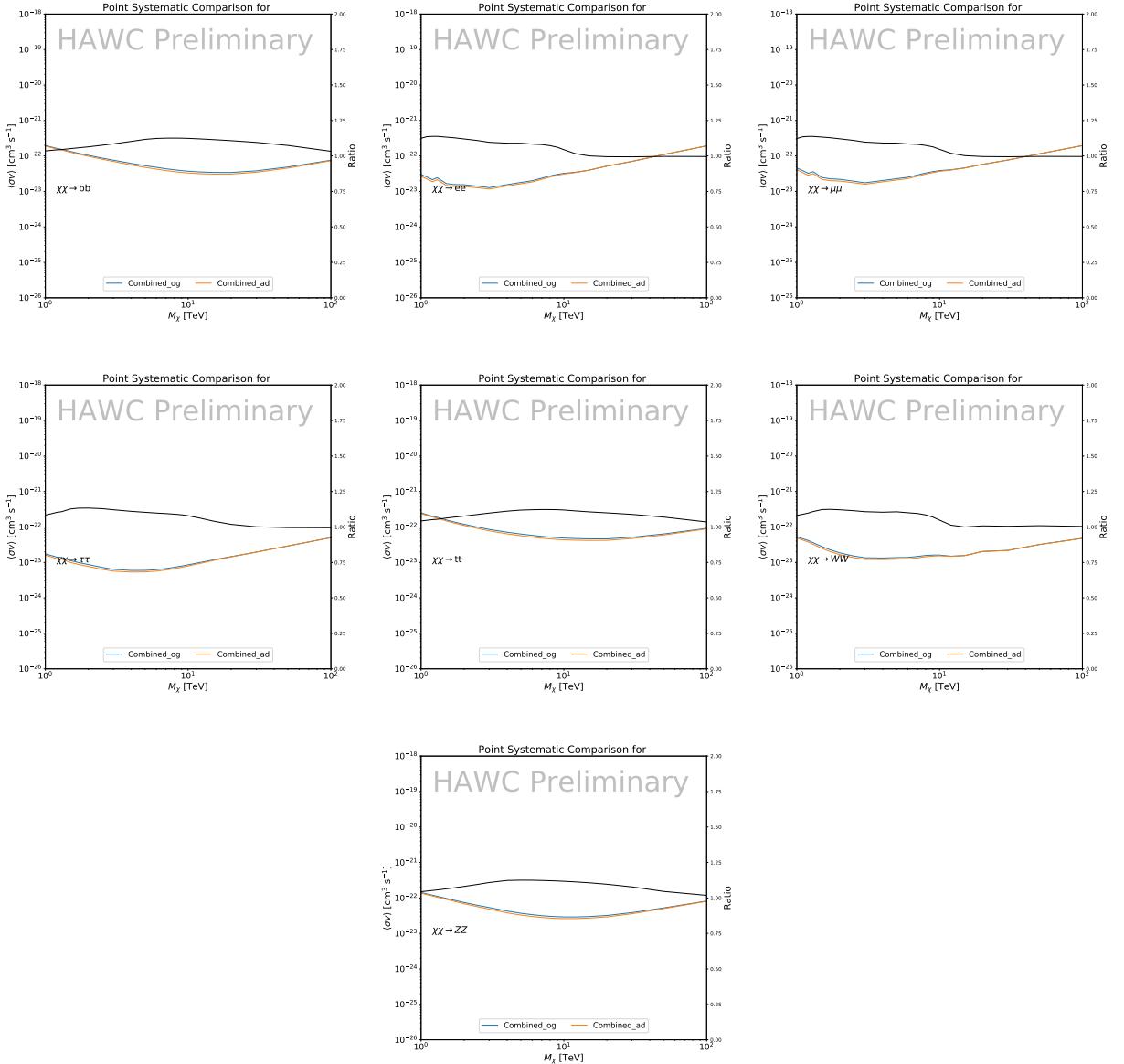


Figure 6.13 Comparison of combined limits when correcting for HAWC’s pointing systematic. All DM annihilation channels are shown. The solid black line is the ratio between published limit to the declination corrected limit. The blue solid line or “Combined_{og}” represented the limits computed for Glory Duck. The solid orange line or “Combined_{ad}” represented the limits computed after correcting for the pointing systematic.

1027 6.8.2 $\mathcal{G}\mathcal{S}$ Versus \mathcal{B} spatial models

1028 We show in this appendix a comparison between the J -factors computed by Geringer-Sameth
 1029 *et al.* [53] (the $\mathcal{G}\mathcal{S}$ set) and the ones computed by Bonnivard *et al.* [47, 55] (the \mathcal{B} set). The
 1030 $\mathcal{G}\mathcal{S}$ J -factors are computed through a Jeans analysis of the kinematic stellar data of the selected

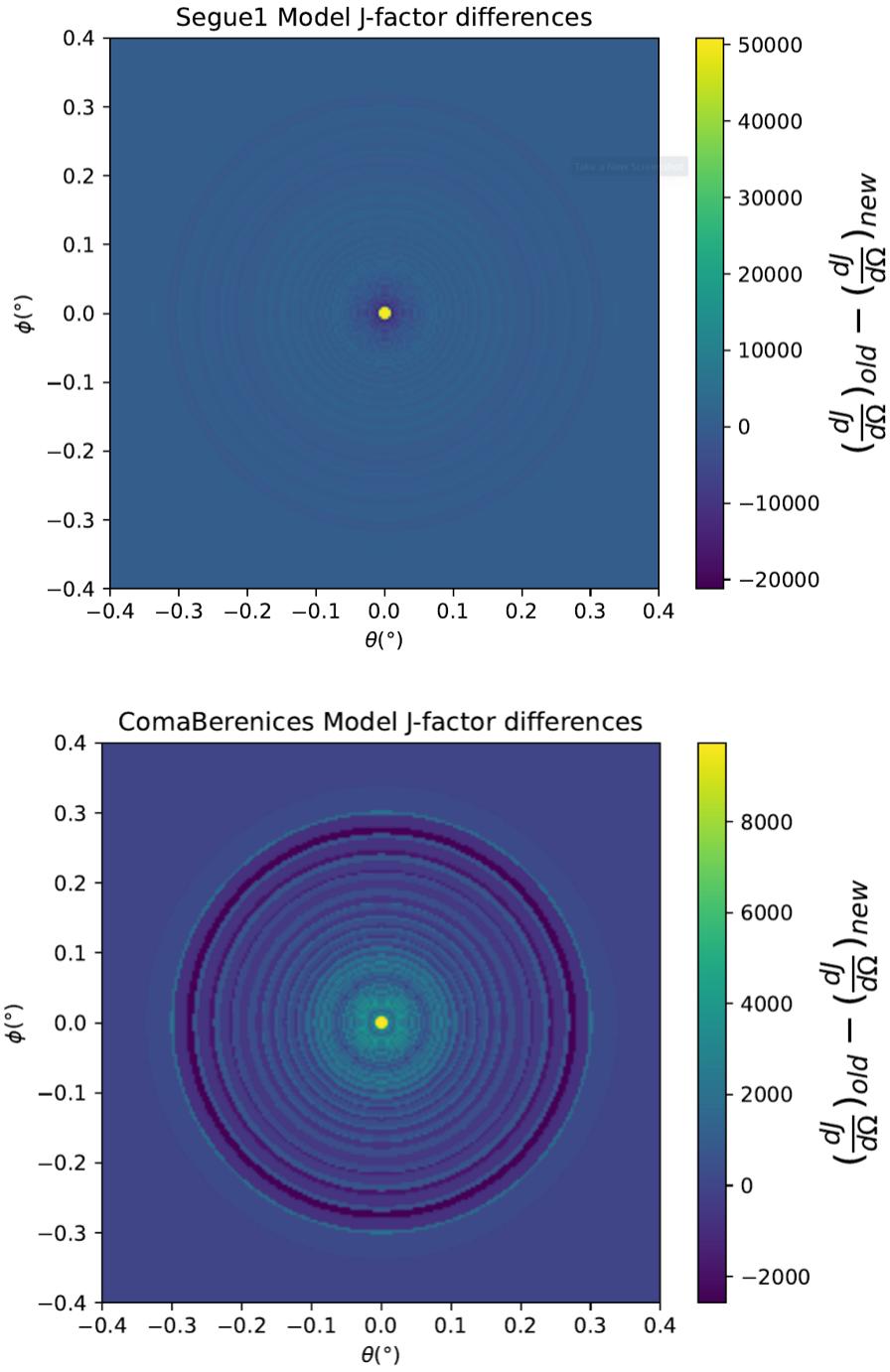


Figure 6.14 Differential map of dJ/Ω from model built in Section 6.8.1 and profiles provided directly from authors. (Top) Differential from Segue1. (bottom) Differential from Coma Berenices. Note that their scales are not the same. Segue1 shows the deepest discrepancies which is congruent with its large uncertainties. Both models show anuli where unique models become apparent.

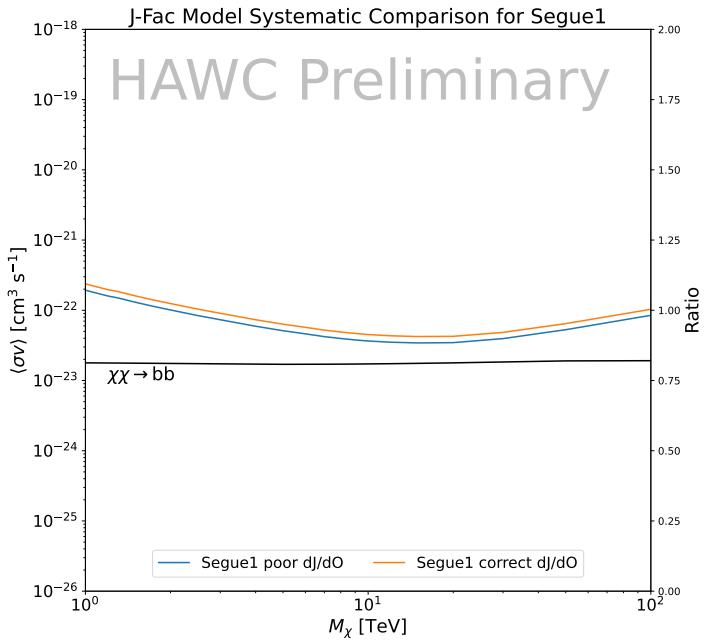
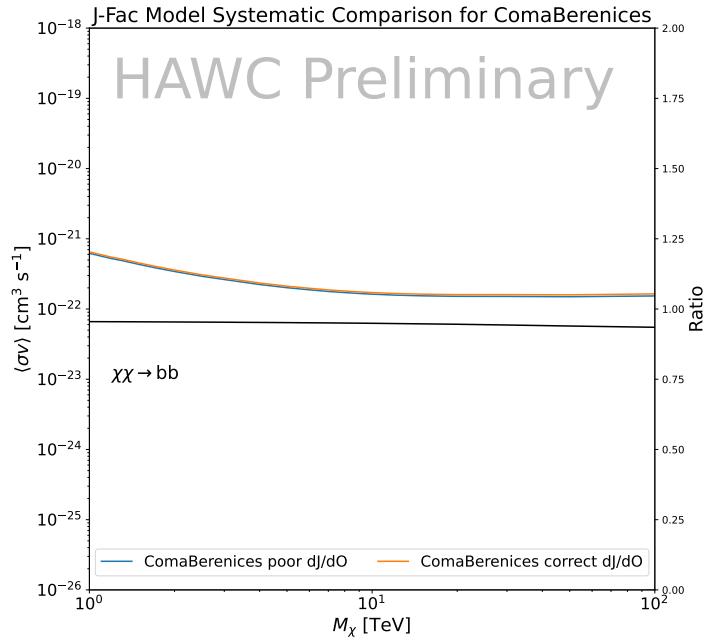


Figure 6.15 HAWC limits for Coma Berenices (top) and Segue1 (bottom) for two different map sets. Blue lines are limits calculated on maps with poor model representation. Orange lines are limits calculated on spatial profiles provided by the authors of [45]. Black line is the ratio of the poor spatial model limits to the corrected spatial models. The left y-axis measures $\langle \sigma v \rangle$ for the blue and orange lines. The right y-axis measures the ratio and is unitless.

1031 dSphs, assuming a dynamic equilibrium and a spherical symmetry for the dSphs. They adopted
1032 the generalized DM density distribution, known as Zhao-Hernquist, introduced by [58], carrying
1033 three additional index parameters to describe the inner and outer slopes, and the break of the
1034 density profile. Such a profile parametrization allows the reduction of the theoretical bias from
1035 the choice of a specific radial dependency on the kinematic data. In other words, the increase of
1036 free parameters with the use of the Zhao-Hernquist profile allows a better description of the mass
1037 density distribution of dark matter.

1038 In addition, a constant velocity anisotropy profile and a Plummer light profile [59] for the stellar
1039 distribution were assumed. The velocity anisotropy profile depends on the radial and tangential
1040 velocity dispersion. However, its determination remains challenging since only the line-of-sight
1041 velocity dispersion can be derived from velocity measurements. Therefore, the parametrization of
1042 the anisotropy profile is obtained from simulated halos (see [60] for more details). They provide the
1043 values of the J -factors of regions extending to various angular radius up to the outermost member
1044 star.

1045 The \mathcal{B} J -factors were computed through a Jeans analysis taking into account the systematic
1046 uncertainties induced by the DM profile parametrization, the radial velocity anisotropy profile, and
1047 the triaxiality of the halo of the dwarf galaxies. They performed a more complete study of the dSph
1048 kinematics and dynamics than \mathcal{GS} for the determination of the J -factor. Conservative values of the
1049 J -factors where obtained using an Einasto DM density profile [61], a realistic anisotropy profile
1050 known as the Baes & Van Hese profile [62] which takes into account that the inner regions can be
1051 significantly non-isotropic, and a Zhao-Hernquist light profile [58].

1052 For both sets, J -factor values are provided for all dSphs as a function of the radius of the
1053 integration region [53, 47, 55]. Table 6.1 shows the heliocentric distance and Galactic coordinates
1054 of the twenty dSphs, together with the two sets of J -factor values integrated up to the outermost
1055 observed star for \mathcal{GS} and the tidal radius for \mathcal{B} . Both J -factor sets were derived through a Jeans
1056 analysis based on the same kinematic data, except for Draco where the measurements of [63] have
1057 been adopted in the computation of the \mathcal{B} value. The computations for producing the \mathcal{GS} and \mathcal{B}

1058 samples differ in the choice of the DM density, velocity anisotropy, and light profiles, for which the
1059 set \mathcal{B} takes into account some sources of systematic uncertainties.

1060 Figure 6.16 and Figure 6.17 show the comparisons for the J -factor versus the angular radius
1061 for each of the 20 dSphs used in this study. The uncertainties provided by the authors are also
1062 indicated in the figures. For the \mathcal{GS} set, the computation stops at the angular radius corresponding
1063 to the outermost observed star, while for the \mathcal{B} set, the computation stops at the angular radius
1064 corresponding to the tidal radius.

1065 6.9 Discussion and Conclusions

1066 In this multi-instrument analysis, we have used observations of 20 dSphs from the gamma-ray
1067 telescopes Fermi-LAT, H.E.S.S., MAGIC, VERITAS, and HAWC to perform a collective DM
1068 search annihilation signals. The data were combined across sources and detectors to significantly
1069 increase the sensitivity of the search. We have observed no significant deviation from the null, no
1070 DM hypothesis, and so present our results in terms of upper limits on the annihilation cross-section
1071 for seven potential DM annihilation channels.

1072 Fermi-LAT brings the most stringent constraints for continuum channels below approximately
1073 1 TeV. The remaining detectors dominate at higher energies. Overall, for multi-TeV DM mass,
1074 the combined DM constraints from all five telescopes are 2-3 times stronger than any individual
1075 telescope for multi-TeV DM.

1076 Derived from observations of many dSphs, our results produce robust limits given the DM
1077 content of the dSphs is relatively well constrained. The obtained limits span the largest mass
1078 range of any WIMP DM search. Our combined analysis improves the sensitivity over previously
1079 published results from each detector which produces the most stringent limits on DM annihilation
1080 from dSphs. These results are based on deep exposures of the most promising known dSphs with
1081 the currently most sensitive gamma-ray instruments. Therefore, our results constitute a legacy of
1082 a generation of gamma-ray instruments on WIMP DM searches towards dSphs. Our results will
1083 remain the reference in the field until a new generation of more sensitive gamma-ray instruments
1084 begin operations, or until new dSphs with higher J -factors are discovered.

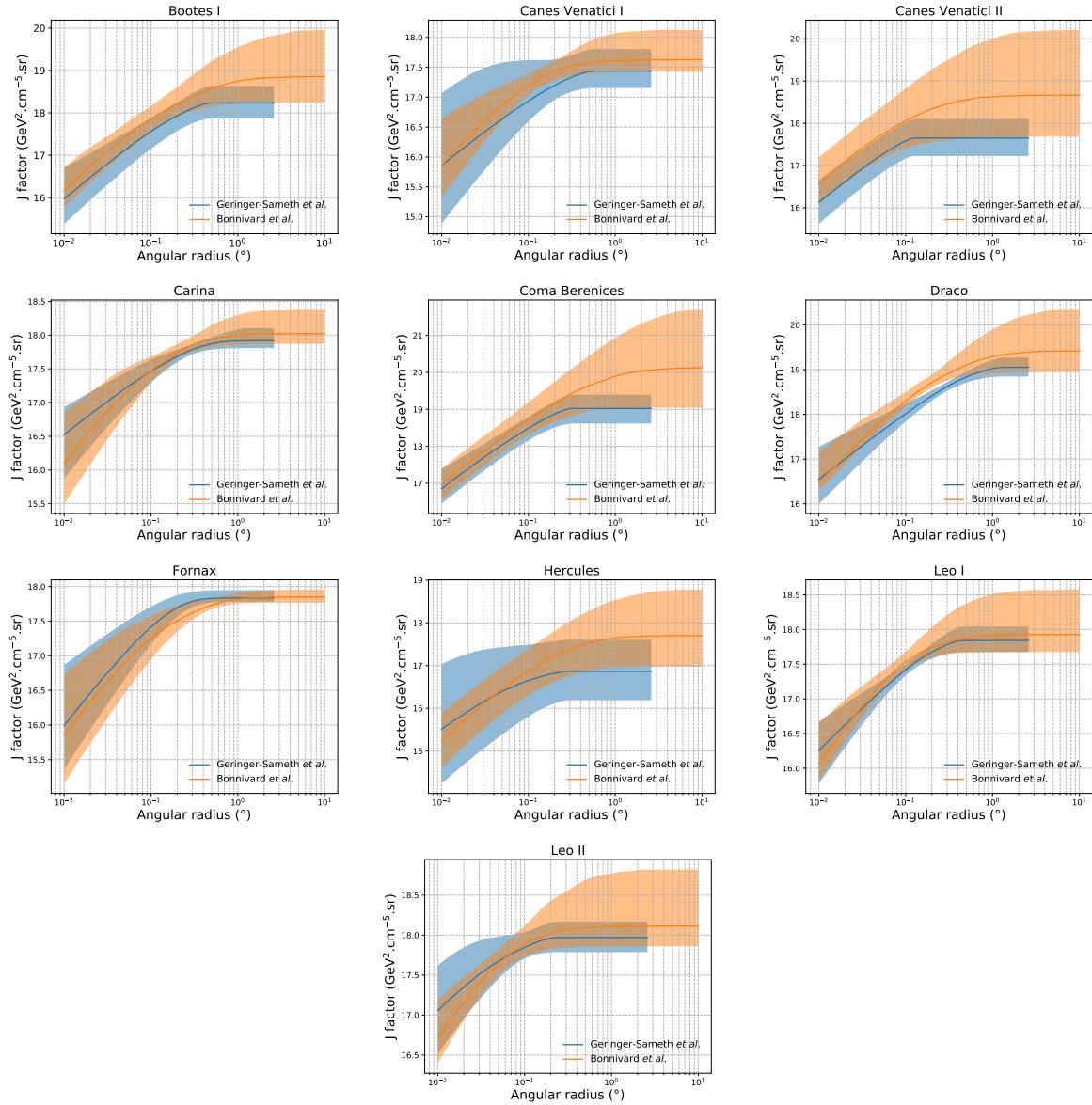


Figure 6.16 Comparisons between the J -factors versus the angular radius for the computation of J factors from Ref. [53] (\mathcal{GS} set in Table 6.1) in blue and for the computation from Ref. [47, 55] (\mathcal{B} set in Tab. 6.1) in orange. The solid lines represent the central value of the J -factors while the shaded regions correspond to the 1σ standard deviation.

1085 This analysis serves as a proof of concept for future multi-instrument and multi-messenger

1086 combination analyses. With this collaborative effort, we have managed to sample over four orders

1087 in magnitude in gamma-ray energies with distinct observational techniques. Determining the nature

1088 of DM continues to be an elusive and difficult problem. Larger datasets with diverse measurement

1089 techniques could be essential to tackling the DM problem. A future collaboration using similar

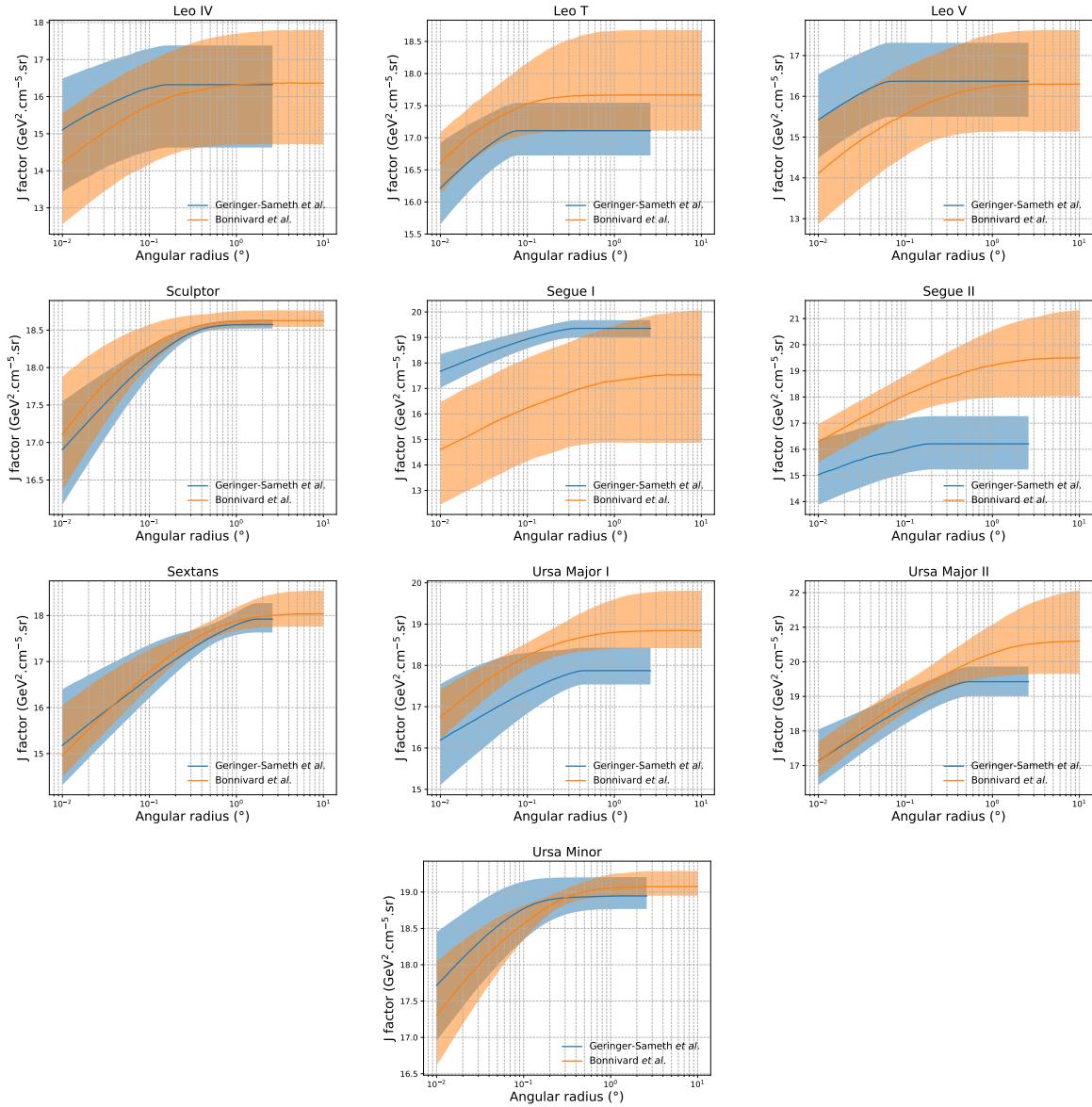


Figure 6.17 Comparisons between the J -factors versus the angular radius for the computation of J factors from Ref. [53] (\mathcal{GS} set in Tab. 6.1) in blue and for the computation from Ref. [47, 55] (\mathcal{B} set in Tab. 6.1) in orange. The solid lines represent the central value of the J -factors while the shaded regions correspond to the 1σ standard deviation.

techniques as the ones described in this paper could grow even beyond gamma rays. The models we used for this study include annihilation channels with neutrinos in the final state. Advanced studies could aim to merge our results with those from neutrino observatories with large data sets. Efforts are already underway to add data from the IceCube, ANTARES, and KM3NeT observatories to these gamma-ray results.

1095 From this work, a selection of the best candidates for observations, according to the latest
1096 knowledge on stellar dynamics and modelling techniques for the derivation of the J -factors on
1097 the potential dSphs targets, is highly desirable at the time that new experiments are starting their
1098 dark matter programs using dSphs. Given the systematic uncertainty inherent to the derivation of
1099 the J -factors, an informed observational strategy would be to select both objects with the highest
1100 J -factors that could lead to DM signal detection, and objects with robust J -factor predictions, i.e.
1101 with kinematic measurements on many bright stars, which would strengthen the DM interpretation
1102 reliability of the observation outcome.

1103 This analysis combines data from multiple telescopes to produce strong constraints on astro-
1104 physical objects. From this perspective, these methods can be applied beyond just DM searches.
1105 Almost every astrophysical study can benefit from multi-telescope, multi-wavelength gamma-ray
1106 studies. We have enabled these telescopes to study the cosmos with greater precision and detail.
1107 Many astrophysical searches can benefit from multi-instrument gamma-ray studies, for which our
1108 analysis lays the foundation.

CHAPTER 7

MULTITHREADING HAWC ANALYSES FOR DARK MATTER SEARCHES

7.1 Introduction

HAWC's current software suite, plugins to 3ML, does not fully utilize computational advancements of recent decades. Said advancements include the proliferation of Graphical Processing Units (GPUs), and multithreading on multi-core processors. The analysis described in chapter 6 took up to 3 months of human time waiting for the full gambit of data analysis and simulation of background to run. Additionally, with the addition of a 2D binning scheme, f_{hit} and NN, the compute time is expected to grow. Although excessive computing time was, in part, from an intense use of a shared computing cluster, it was evident that there was room for improvement. In HAWC's next generation dSph DM search, I decided to develop codes that would utilize the multi-core processors on modern high performance computing clusters. The results of this work are featured in this chapter and brought a human timing improvement to computation that scales as $1/N$ where N is the number of threads.

7.2 Dataset and Background

This section enumerates the data and background methods used for HAWC's multi-threaded study of dSphs. Section 7.2.1 and Section 7.2.2 are most useful for fellow HAWC collaborators looking to replicate a multithreaded dSph DM search.

7.2.1 Itemized HAWC files

- Detector Resolution: `refit-Pass5-Final-NN-detRes-zenith-dependent.root`
- Data Map: `Pass5-Final-NN-maptree-ch103-ch1349-zenith-dependent.root`
- Spectral Dictionary: `HDMspectra_dict_gamma.npy`

7.2.2 Software Tools and Development

This analysis was performed using HAL and 3ML [42, 43] in Python version 3. I built software in collaboration with Michael Martin and Letrell Harris to implement the *Dark Matter Spectra from*

1133 *the Electroweak to the Planck Scale* (HDM) [64] and dSphs spatial model from [65] for HAWC
1134 analysis. A NumPy dictionary of HDM was made for Py3. The corresponding Python3 file is
1135 `HDMspectra_dict_gamma.npy`. These files can also be used for decay channels and tools are
1136 provided in HDM’s [git repository](#) [64]. The analysis was performed using the Neural Network
1137 energy estimator for Pass 5.F. A description of this estimator was provided in chapter 4. **TODO:**
1138 **define a subsection when it’s written**, and its key improvements are an improved energy estimation
1139 and improved sensitivities at higher zenith angles. All other software used for data analysis, DM
1140 profile generation, and job submission to SLURM are also kept in my sandbox in the [Dark Matter](#)
1141 [HAWC](#) project. The above repository also incorporates the model inputs used previously in Glory
1142 Duck, described in chapter 6

1143 **7.2.3 Data Set and Background Description**

1144 The HAWC data maps used for this analysis contain 2565 days of data between runs 2104 (

1145 **TODO: Day start**) and 7476 (**TODO: day end**). They were generated from pass 5.f reconstruction.

1146 The analysis is performed using the NN energy estimator with bin list:

1147 `B1C0Ea, B1C0Eb, B1C0Ec, B1C0Ed, B1C0Ee, B2C0Ea, B2C0Eb, B2C0Ec, B2C0Ed, B2C0Ee,`
1148 `B3C0Ea, B3C0Eb, B3C0Ec, B3C0Ed, B3C0Ee, B3C0Ef, B4C0Eb, B4C0Ec, B4C0Ed, B4C0Ee,`
1149 `B4C0Ef, B5C0Ec, B5C0Ed, B5C0Ee, B5C0Ef, B5C0Eg, B6C0Ed, B6C0Ee, B6C0Ef, B6C0Eg,`
1150 `B6C0Eh, B7C0Ee, B7C0Ef, B7C0Eg, B7C0Eh, B7C0Ei, B8C0Ee, B8C0Ef, B8C0Eg, B8C0Eh,`
1151 `B8C0Ei, B8C0Ej, B9C0Ef, B9C0Eg, B9C0Eh, B9C0Ei, B9C0Ej, B10C0Eg, B10C0Eh,`
1152 `B10C0Ei, B10C0Ej, B10C0Ek, B10C0El`

1153 Bin 0 was excluded as it has substantial hadronic contamination and poor angular resolution.

1154 Background considerations and source selection was identical to Section 6.2, and no additional
1155 arguments are provided here. Many of the HAWC systematics explored in Section 6.7 also apply
1156 for this DM search and are not added upon here.

1157 **7.3 Analysis**

1158 The analysis and its systematics are almost identical to Section 6.3. Importantly, we use the
1159 same Equation (6.1) and Equation (6.2) for estimating the gamma-ray flux at HAWC from our
1160 sources. We add on to the previous study with a search for DM decay. The flux equations for DM
1161 decay are

$$\frac{d\Phi_\gamma}{dE_\gamma} = \frac{1}{4\pi\tau m_\chi} \frac{dN_\gamma}{dE_\gamma} \times \int_{\text{source}} d\Omega \int_{l.o.s} \rho_\chi dl(r, \theta') \quad (7.1)$$

1162 with a new quantity, the D factor, defined as

$$D = \int d\Omega \int_{l.o.s} dl \rho_\chi(r, \theta') \quad (7.2)$$

1163 Software was written to accomodate DM decay from dSphs, however decay profiles were not
1164 received from $\mathcal{L}\mathcal{S}$ by the time of writing this tehsis.

1165 **7.3.1 $\frac{dN_\gamma}{dE_\gamma}$ - Particle Physics Component**

1166 For these spectra, we import HDM with Electroweak (EW) corrections and additional correc-
1167 tions for neutrinos above the EW scale [64]. The spectrum is implemented as a model script in
1168 astromodels for 3ML. A comprehensive description of EW corrections and neutrino considerations
1169 are provided later in **TODO: refeance MM nu duck.**

1170 Figure 7.1 demonstrates the impact of changes from HDM on DM annihilation to W bosons.
1171 A class in astromodels was developed to include HDM and is aptly named **HDMspectra** within
1172 **DM_models.py**. The SM DM annihilation channels studied here are $\chi\chi \rightarrow:$

1173 e^+e^- , $\mu^+\mu^-$, $\tau^+\tau^-$, $b\bar{b}$, $t\bar{t}$, gg , W^+W^- , ZZ , $c\bar{c}$, $u\bar{u}$, $d\bar{d}$, $s\bar{s}$, $\nu_e\bar{\nu}_e$, $\nu_\mu\bar{\nu}_\mu$, $\nu_\tau\bar{\nu}_\tau$, $\gamma\gamma$, hh .

1174 For $\gamma\gamma$ and ZZ , a substantial fraction of the signal photons are expected to have total energy equal
1175 m_χ [64]. This introduces a δ -function that is much narrower than the energy resolution of the
1176 HAWC detector. To ensure that this feature is not lost in the likelihood fits, the 'line' feature is
1177 convolved with a gaussian kernel with a 1σ width of $0.05 \cdot m_\chi$ and total kernel window of $\pm 4\sigma$.
1178 This difers from HAWC's previous line study where 30% of HAWC's energy resolution was used
1179 for the kernel [66]. The NN energy estimator's strength compared to f_{hit} at low gamma-ray energy

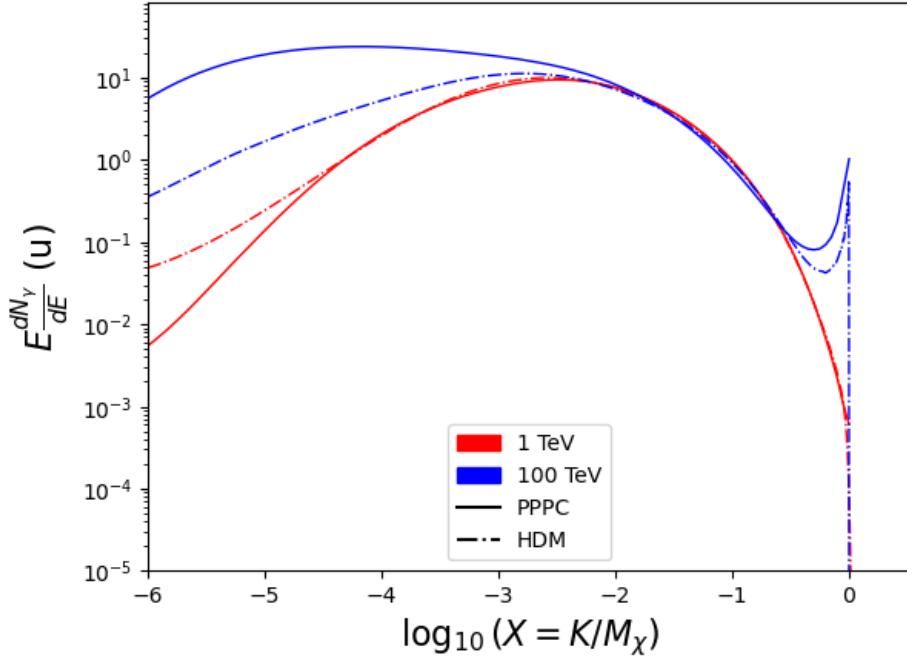


Figure 7.1 Difference between spectral hypotheses from PPPC [44] and HDM [64]. Shown is the expected DM annihilation spectrum for $\chi\chi \rightarrow W^-W^+$. Solid lines are spectral models with EW corrections from the PPPC. Dash-dot lines are spectral models from HDM. Red lines are models for $M_\chi = 1$ TeV. Blue lines represent models for $M_\chi = 100$ TeV.

enables smaller resolutions in addition to low energy tails in the spectral models [64]. $\chi\chi \rightarrow \gamma\gamma$ and ZZ spectral hypotheses are shown in Figure 7.2. Spectral models for the remaining annihilation channels are plotted for each m_χ in Figure B.1.

7.3.2 J and D- Astrophysical Components

The J-factor profiles for each source are imported from Louis Strigari et al. (referred to with \mathcal{LS}) [65]. Profiles in $\frac{dJ}{d\Omega}(\theta)$ up to $\theta = 0.5^\circ$ were provided directly from the authors. Map generation from these profiles were almost identical to Section 6.3.2 except that a higher order trapezoidal integral was used for the normalization of the square, uniformly-spaced map:

$$p^2 \cdot \sum_{i=0}^N \sum_{j=0}^M w_{i,j} \frac{d\mathcal{K}}{d\Omega}(\theta_{i,j}, \phi_{i,j}) \quad (7.3)$$

\mathcal{K} is either J or D for the spatial distributions of annihilation or decay respectively. p is the angular side of one pixel in the map. $w_{i,j}$ is a weight assigned the following ways:

$w_{i,j} = 1$ if $(\theta_{i,j}, \phi_{i,j})$ is fully within the region of integration

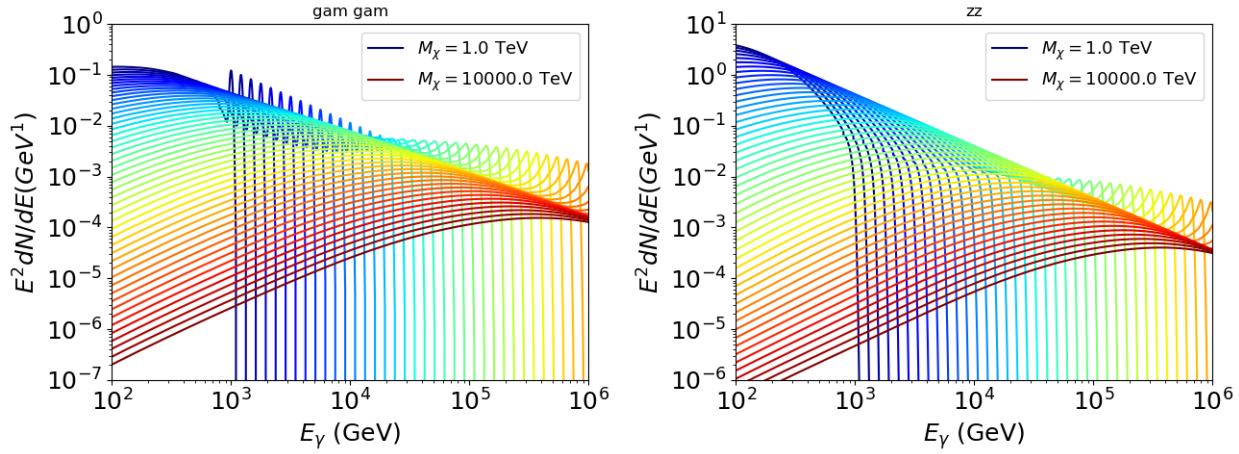


Figure 7.2 Photon spectra for $\chi\chi \rightarrow \gamma\gamma$ (left) and $\chi\chi \rightarrow ZZ$ (right) after gaussian convolution of line features. Both spectra have δ -features at photon energies equal to the DM mass. Bluer lines are annihilation spectra with lower DM mass. Redder lines are spectra from larger DM mass. All Spectral models are sourced from the Heavy Dark Matter models [64]. Axes are drawn roughly according to the energy sensitivity of HAWC.

1191 $w_{i,j} = 1/2$ if $(\theta_{i,j}, \phi_{i,j})$ is on an edge of the region of integration

1192 $w_{i,j} = 1/4$ if $(\theta_{i,j}, \phi_{i,j})$ is on a corner of the region of integration

1193 Figure 7.3 shows the median and $\pm 1\sigma$ maps used as input for DM annihilation studied by \mathcal{LS} .

1194 **7.3.3 Source Selection and Annihilation Channels**

1195 HAWC's sources for this multithreaded analysis include Coma Berenices, Draco, Segue 1, and

1196 Sextans \mathcal{LS} observes up to 43 sources in its publication, however only 4 of the best fit profiles were
1197 provided at the time this thesis was written. A full description of each source used in this analysis
1198 is found in Table 7.1.

1199 This analysis improves on chapter 6 in the following ways. Previously, the particle physics

1200 model used for gamma-ray spectra from DM annihilation was from the PPPC [44] which missed
1201 important considerations relevant for the neutrino sector. HDM is used to account for this shortfall

1202 [64]. HDM also models DM to the Planck scale which permits HAWC to probe PeV scale DM.

1203 For this study, we sample DM masses: 1 TeV - 10 PeV with 6 mass bins per decade in DM mass.

1204 In the case of line spectra ($\chi\chi \rightarrow \gamma\gamma$, or ZZ), we double the mass binning to 12 DM mass bins

1205 per decade in DM mass. A larger source catalog is used that uses a Navarro–Frenk–White (NFW)

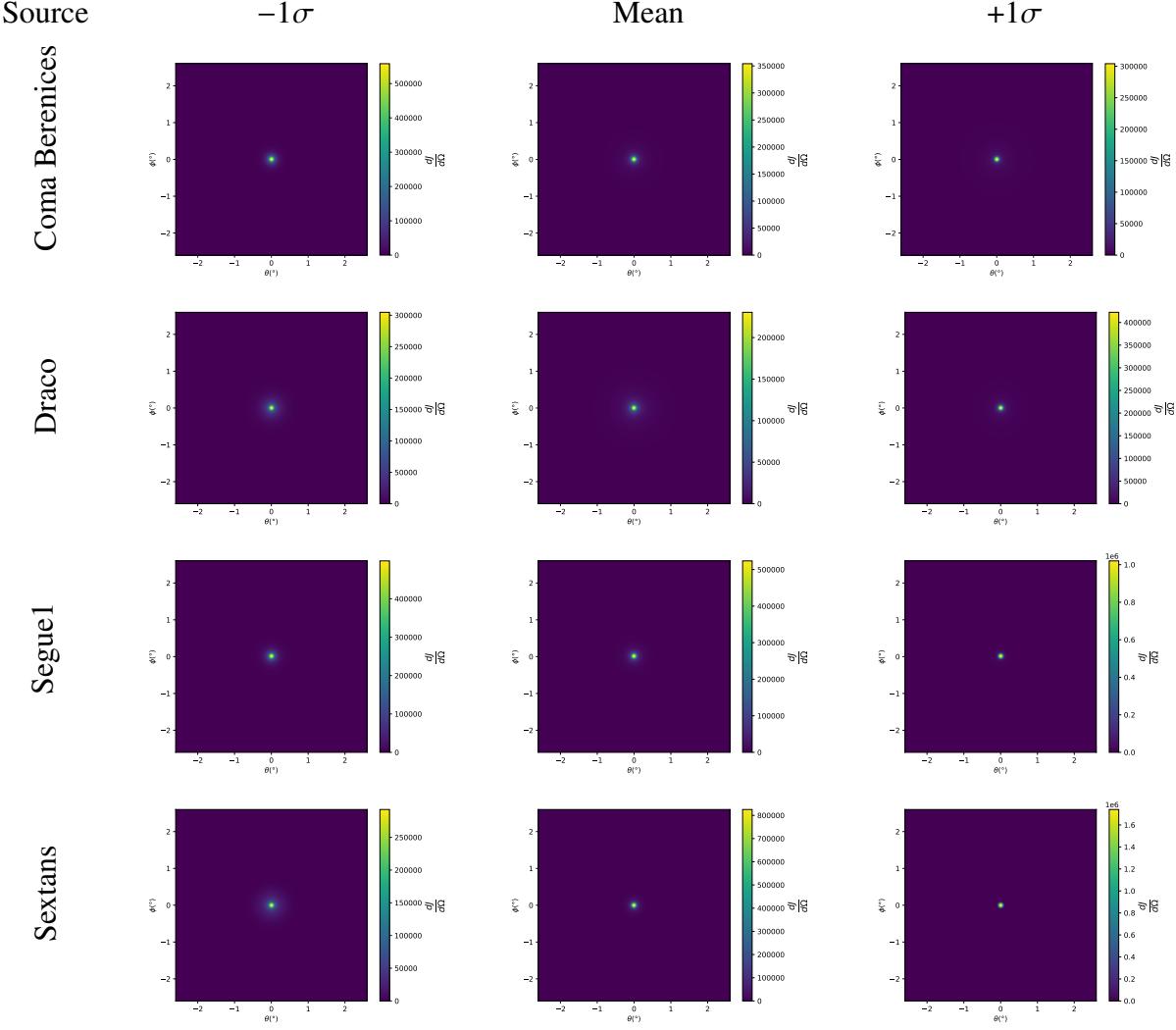


Figure 7.3 $\frac{dJ}{d\Omega}$ maps for Coma Berenices, Draco, Segue1, and Sextans. Columns are divided for the $\pm 1\sigma$ uncertainties in $dJ/d\Omega$ around the mean value from \mathcal{LS} [65]. Origin is centered on the specific dwarf spheroidal galaxies (dSph). θ and ϕ axes are the angular separation from the center of the dwarf

1206 spatial DM distribution from \mathcal{LS} [65]. Because NFW has fewer parameters than what is used
 1207 for \mathcal{GS} , \mathcal{LS} is able to fit ultra-faint dwarves, expanding the number of sources available for DM
 1208 searches. Finally, the gamma-ray ray dataset is much larger. The study performed here analyzes
 1209 2565 days of data compared to 1017 days analyzed in chapter 6.

1210 7.4 Likelihood Methods

1211 These are identical to Section 6.4.1 and no additional changes are made to the likelihood. Bins
 1212 in this analysis are expanded to include HAWC’s NN energy estimator.

1213 **7.5 Computational Methods: Multithreading**

1214 Previously, as in Section 6.3, the likelihood was minimized for one model at a time. One
 1215 model in this case representing a DM annihilation channel, DM mass, and dSph. In an effort
 1216 to conserve human and CPU time, jobs submitted for high performance computing contained a
 1217 list of DM masses to iterate over for likelihood fitting. Jobs were then trivially parallelized for
 1218 each permutation of the two lists: CHANS (SM annihilation channel) and SOURCES (dSph spatial
 1219 templates). The lists for CHANS and SOURCES are found in Section 7.3.1 and Table 7.1, respectively.
 1220 Initially, 11 DM mass bins were serially sampled for one job defined by a [SM channel, dSph] set.
 1221 Computing the likelihoods would take between 1.5 to 2 hrs, stocastically, for a job. We expect to
 1222 compute likelihoods for data and 300 Poisson background trials. The estimated CPU time based on
 1223 the above for all SM annihilation channels (17) and 25 sources (all \mathcal{LS} sources withing HAWC's
 1224 field of view) amounted to 127,925 jobs. In total, 1,407,175 likelihood fits and profiles would be
 1225 computed for the 11 mass bins we wished to study. The estimated CPU time ranged between 10k
 1226 CPU days - 8k CPU days. Human time is more challenging to estimate as job allocation is stochastic
 1227 and highly dependant on what other users are submitting, yet it is unlikely that all jobs would run
 1228 simultaneously. Therefore we can expect human time to be about as long as was seen in chapter 6
 1229 which was on the order of months to fully compute on a smaller analysis. A visual aid to describe
 1230 how jobs were organized is provided in Figure 7.4.

Name	Distance (kpc)	l, b ($^{\circ}$)	$\log_{10} J$ (\mathcal{LS} set) $\log_{10}(\text{GeV}^2\text{cm}^{-5}\text{sr})$
Coma Berenices	44	241.89, 83.61	$19.00^{+0.36}_{-0.35}$
Draco	76	86.37, 34.72	$18.83^{+0.12}_{-0.12}$
Segue I	23	220.48, 50.43	$19.12^{+0.49}_{-0.58}$
Sextans	86	243.50, 42.27	$17.73^{+0.13}_{-0.12}$

Table 7.1 Summary of the relevant properties of the dSphs used in the present work. Column 1 lists the dSphs. Columns 2 and 3 present their heliocentric distance and galactic coordinates, respectively. Column 4 reports the J -factors of each source given from the \mathcal{LS} studies and estimated $\pm 1\sigma$ uncertainties. The values $\log_{10} J$ (\mathcal{LS} set) [65] correspond to the mean J -factor values for a source extension truncated at 0.5° .

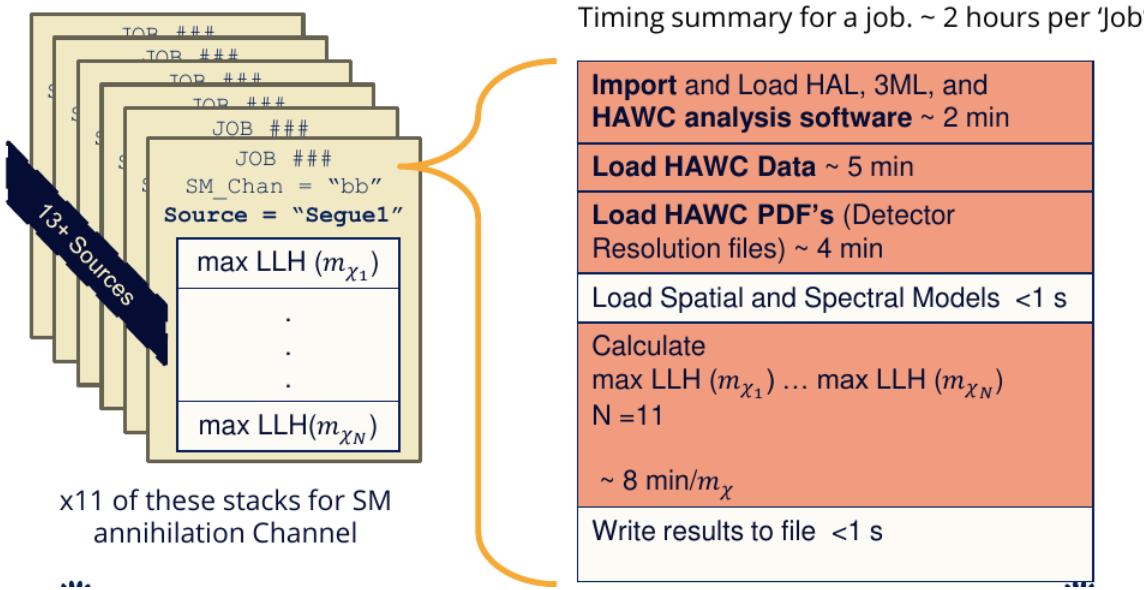


Figure 7.4 Infographic on how jobs and DM computation was organized in Section 6.3. Jobs were built for each permutation of CHANS and SOURCES shown by the left block in the figure. Each job, which took on the order 2 hrs to compute, had the following work flow: 1. Import HAWC analysis software, 2 min to run. 2. Load HAWC count maps, 5 min to run. 3. Load HAWC energy and spatial resolutions, 4 min. 5. Load DM spatial source templates and spectral models, less than 1 s. 6. Perform likelihood fit on data and model, about 8 min per DM mass. 7. Write results to file, less than 1s.

1231 The computational needs for this next generation DM analysis are extreme and is unlike other
 1232 analyses performed on HAWC. It became clear that there was a lot to gain from optimzing how
 1233 the likelihoods are computed. This section discusses how multi-threading was applied to solve and
 1234 reduce HAWC's computing of likelihoods for large parameter spaces like in DM searches.

1235 7.5.1 Relevant Foundational Information

1236 The profiling of the likelihood for HAWC is done via gradient descent where the nomarilization
 1237 of Equation (6.1) (linearly correlated with $\langle \sigma v \rangle$) is rescaled in the descent. Additionaly, we sample
 1238 the likelihood space for a defined list of $\langle \sigma v \rangle$'s described in Section 6.4.2. The time to compute
 1239 these values is not predictable or consistent because many variables can change across the full
 1240 model-space. comprehensively, these variables are:

- 1241 • m_{χ} : DM rest mass
- 1242 • CHAN : DM SM annihilation channel.

1243 • SOURCE : dSph within HAWC's field of view. This involves a spatial template AND coordinate
 1244 in HAWC data.

1245 • $\langle \sigma v \rangle$: Effectevly the flux normalization and free parameter in the likelihood fit.

1246 Therefore, we develop an asynchronous, functional-parallel coding pattern. Asynchronous meaning
 1247 that the instructions and computing within a function are independent and permitted to be out of sync
 1248 with sibling computations. Functional-parallel meaning that instructions are the subject of parral-
 1249 lelization rather than threading the likelihood computation. This is close to trivial parametrization
 1250 seen in Figure 7.4 except that we seek to consolidate the loading stages (software, data, and detector
 1251 resolution loading). Reducing the total instances of loading stages and distributing access to the
 1252 reduced loads across multiple asynchronous threads is expected to reduce serial processing time and
 1253 the overhead implicit to each job in addition to saving human time.

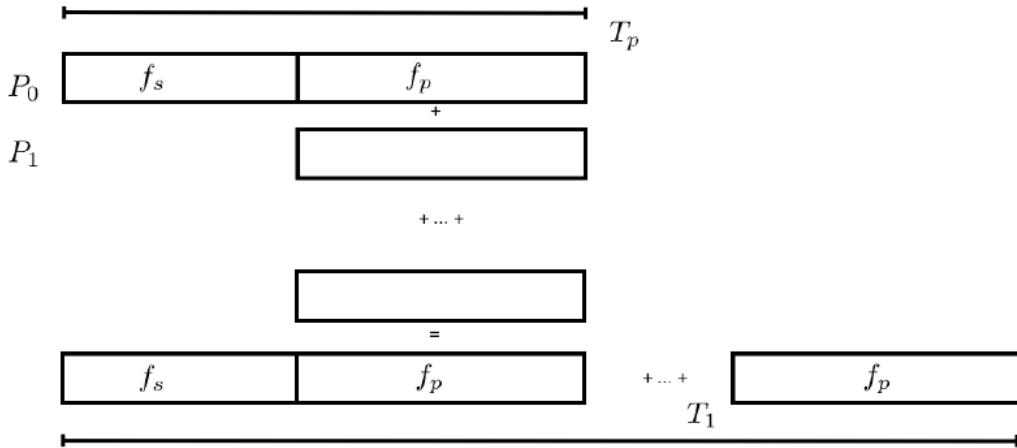


Figure 7.5 Graphic of Gustafson parallel coding pattern. f_s is the fraction of a program, in time, spent on serial computation. f_p is the fraction of computing time that is parallelizable. T_p is the total time for a parallel program to run. T_1 is the total time for a parallel program to run if only 1 processor is allocated. P_N is the N -th processor where it's row is the computation the processor performs. The Gustafson pattern is most similar to what is implemented for this analysis. Figure is pulled from [67].

1254 We need a way to measure and compare the expected speedup and efficiency gain for this
 1255 asynchronous coding pattern. I pull inspiration for timing measurement from [67] and use *Amdahl's law with hybrid programming*. Hybrid programming meaning that the computation is a mix of

1257 distributed and shared memory programming. If we assume the code is fully parallelizable over p
1258 processors and c threads, the ideal speedup is simply pc and ideal run-time is $T_1/(pc)$. T_1 is the
1259 total time for a parallel program to run if only 1 processor is allocated. However, the coding pattern
1260 contains some amount of unavoidable serial computation, as shown in Figure 7.5. In our case, the
1261 run time is estimated to be

$$T_{p,c} = \frac{T_1}{pc} (1 + F_s(c - 1)). \quad (7.4)$$

1262 F_s is the fraction of CPU time dedicated to serial computation. The expected speedup is

$$S_{p,c} \equiv \frac{T_1}{T_{p,c}} = \frac{pc}{1 + F_s(c - 1)}. \quad (7.5)$$

1263 From Equation (7.5), we can see that the speed up scales with p/F_s . We are free to minimize
1264 F_s asymptotically by enlarging the total models that are submitted to the thread pool, thereby
1265 shrinking the CPU fraction dedicated to serial operation. We are also free to define exactly how
1266 many threads and processors we utilize, yet eventually hit a hard cap at the hardware available on
1267 our computing cluster. HAWC uses Intel Xeon processors with 48 cores and 96 threads. This
1268 means when N-threads (c) are defined, $N \bmod 2$ cores (p) are needed. We see that a successful
1269 code scales well as the expected speedup is inversely correlated with F_s . As the total number of
1270 models sampled grows, the speedup will also.

1271 7.5.2 Implementation

1272 The multithreaded code was written in Python3 and is documented in the `dark_matter_hawc`
1273 [repository](#) within the script named `mpu_analysis.py`. A version of the script as of April 25
1274 **TODO: make sure to update on this date** is also provided in Section B.1 It has many dependancies
1275 including the HAWC analysis software. Figure 7.6 displays the workflow of a job with 3 threads.
1276 Within a job, SOURCE is kept fixedh . CHAN(S) remains 17 elements long. More m_χ are sampled
1277 from 11 bins up to 49 (for $\gamma\gamma$ and ZZ) and 25 (for remaining CHANS) which amounts to 12 or 6
1278 mass bins per decade. The DM mass, m_χ , and SM annihilation channels, CHANS, are permuted into
1279 a 473 element list which is split evenly across N threads where N ranges between 5 - 16. Within a
1280 thread, for each m_χ -CHAN tuple, 1001 $\langle\sigma v\rangle$ values are sampled in the likelihood, and the value of

Timing summary for a multi-threaded job.

Import and Load HAL, 3ML, and HAWC analysis software ~ 2 min		
Load HAWC Data ~ 5 min		
Load HAWC PDF's (Detector Resolution files) ~ 4 min		
Load Spatial Model < 1s		
Load Spectra Models <1 s	Load Spectra Models <1 s	Load Spectra Models <1 s
Calculate max LLH (Chan_0, m_{χ_1}) ... max LLH (Chan_?, m_{χ_N}) N = TOTAL/N_THREADS ~ 8 min/Spec_model	Calculate max LLH (Chan_?, m_{χ_1}) ... max LLH (Chan_?, m_{χ_N}) N = TOTAL/N_THREADS ~ 8 min/Spec_model	Calculate max LLH (Chan_?, m_{χ_1}) ... max LLH (Chan_?, m_{χ_N}) N = TOTAL/N_THREADS ~ 8 min/Spec_model
Write results to file <1 s	Write results to file <1 s	Write results to file <1 s
Join Threads and terminate < 1s		

Figure 7.6 Task chart for one multi-threaded job developed for this project. Green blocks indicate a shared resource across the threads AND computation performed serially. Red blocks indicate functional parallel processing within each thread. 3 threads are represented here, yet many more can be employed during the full analysis. Jobs are defined by the SOURCE as these require unique maps to be loaded into the likelihood estimator. The m_{χ} , CHAN, and $\langle \sigma v \rangle$ variables are entered into the thread pool and allocated as evenly as possible across the threads.

1281 $\langle \sigma v \rangle$ that maximizes the likelihood is found. Although rare, fits that failed are handled on a case
1282 by case basis.

1283 7.5.3 Performance

M Tasks	$T_{p,c}$ (hr:min:s)			
	$T_{1,1}$	$T_{1,2}$	$T_{1,8}$	$T_{1,16}$
50	1:40:37.5	0:52:43.7	0:19:13.8	0:13:44.0
74	2:22:30.0	1:15:00.6	0:25:21.3	0:15:49.8
100	(3:07:51.9)	1:40:10.5	0:30:44.4	0:20:01.4
200	(6:02:20.6)	-		0:30:35.0
473	(13:58:40.3)	-		1:09:42.9

Table 7.2 Timing summaries for analyses for serial and multithreaded processes. M tasks is the number of functional-parallel tasks ran for the computation. $T_{p,c}$ is a single run time in hours:minutes:seconds for runs utilizing p nodes and c threads. Runs are run interactively on the same computer to maximize consistency. Empty entries are indicated with '-'. (·) entries are estimated entries extrapolated from data earlier in the column.

1284 We see a tremendous reduction to human time waiting for our dSph analyses to run. Table 7.2

1285 shows the timing summaries for analyses of different sizes and thread counts. Additionally, the
 1286 efficiency gained when consolidating the serial loading of data is also apparent in our ability to
 1287 study many more tasks in about the same amount of wall time as a smaller serial computation. Trials
 1288 represented in the table were run on an AMD Opteron® processor 6344 with 48 cores, 2 threads
 1289 per core; 2.6 GHz clock. This is not the same architecture used for analysis on the computing
 1290 cluster however they are similar enough that results shown here are reasonably representative of
 1291 computing on the HAWC computing cluster. I use the Tab. 7.2 for the inferences and conclusions
 1292 in the following paragraphs.

1293 First, we want to find T_s , the time of serial computation. From Fig. 7.5, the timing for our
 1294 coding pattern can be written as

$$T_s + Mt_p = T_{1,1}^M. \quad (7.6)$$

1295 M is the number of functional-parallel tasks (represented as column 1 of Tab. 7.2), and t_p is the
 1296 average time to complete a single parallel task. $T_{1,1}^M$ is the total time for a parallel program to run if
 1297 only 1 processor is allocated for M parallel task. With two runs of different M ($M1$ and $M2$), we
 1298 can use a system of equations to derive

$$T_s = T_{1,1}^{M1} - M1 \left(\frac{T_{1,1}^{M1} - T_{1,1}^{M2}}{M1 - M2} \right). \quad (7.7)$$

1299 We also extract t_p using the same methods:

$$t_p = \frac{T_{1,1}^{M1} - T_{1,1}^{M2}}{M1 - M2}. \quad (7.8)$$

1300 From Tab. 7.2, we set $M1 = 50$ and $M2 = 74$ and take their corresponding $T_{1,1}$ from the table to
 1301 calculate T_s and t_p .

$$T_s = 803.1\text{s} \text{ and } t_p = 104.6\text{s} \quad (7.9)$$

1302 Now, we have specific estimation for the fraction of serial computing time, F_s :

$$F_s = \frac{803.1}{803.1 + 104.6 \cdot M}. \quad (7.10)$$

1303 The maximum M for this study is 473 which evaluates Eq. (7.10): $F_s = 0.016$ or 1.6% of computing
 1304 time. Table 7.3 shows the resulting speedups.

		$S_{p,c}$		
M Tasks	F_s	$S_{1,2}$	$S_{1,8}$	$T_{1,16}$
50		1.90 [1.76]	5.23 [4.14]	6.35 [5.34]
74		1.90 [1.83]	5.62 [4.82]	9.00 [6.64]
100		-		
200		-		
473		-		1:09:42.9

Table 7.3 Speed up summaries for analyses for serial and multithreaded processes. M tasks is the number of functional-parallel tasks ran for the computation. $S_{p,c}$ is a single speedup comparison for runs utilizing p nodes and c threads. $[\cdot]$ are the estimated speedups calculated from Tab. 7.2, Eq. (7.10), and Eq. (7.5). Empty entries are indicated with '-'.

1305 We see a speedup that exceeds expectations from Eq. (7.5) for real trail runs. **TODO: reflect**

1306 **on results when the tables are totally filled in.** We also see that there are diminishing returns as
 1307 the number of threads increases. For small jobs with large c , both the expected and observed
 1308 speedup are significantly smaller than c . One thing not considered in Eq. (7.5) is the time incurred
 1309 via communication latency. Communication latency increases with the number of threads and
 1310 contributes to diminishing returns. Therefor, these results are not conclusive. Each entry in
 1311 Tab. 7.2 represent only one run of the script and therefore the data are not precise and lacks the
 1312 full scope of timing costs. Yet, they do give us a good idea of what HAWC gains in multithreading
 1313 analysis software. We see very clearly that there is a lot to gain, and this new coding pattern will
 1314 expand HAWC's analysis capabilities.

1315 7.6 Analysis Results

1316 **TODO: talk about the results**

1317 We were not able to generate background trials in time of writing this thesis. These are not

1318 shown and are an immediate next step for this analysis before publication.

1319 We did not see DM, but we did see some interesting excesses in the 10 Tev range at order 2σ .

1320 Draco was not included as the PDF of some of our analysis bins were wider than what is reasonable
 1321 for a point source analysis. Draco is at a high zenith for HAWC, so the effort required to include it
 1322 was not justified by the benefits.

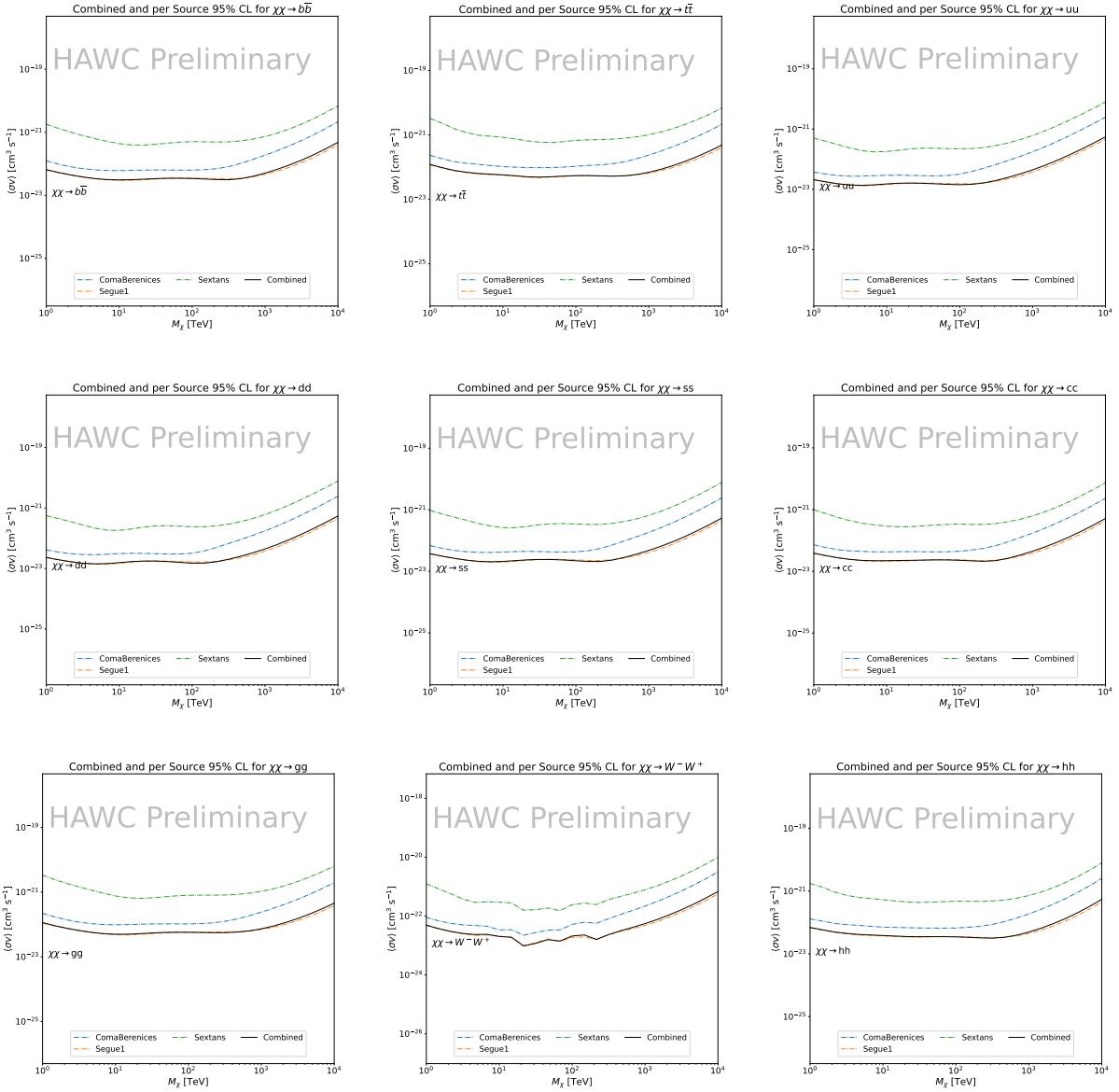


Figure 7.7 TODO: fill this out

1323 7.7 Systematics

1324 These are identical to what was performed earlier in Glory Duck, Section 6.7. We are also
 1325 sensitive to the choice in spatial template, and this was explored in Section 6.7.2 and Section 6.8.2.
 1326 LS also provided the uncertainty on their mean spatial models. We perform a study on the
 1327 $\pm 1\sigma$ spatial templates and show corresponding confidence limits in TODO: link to figure

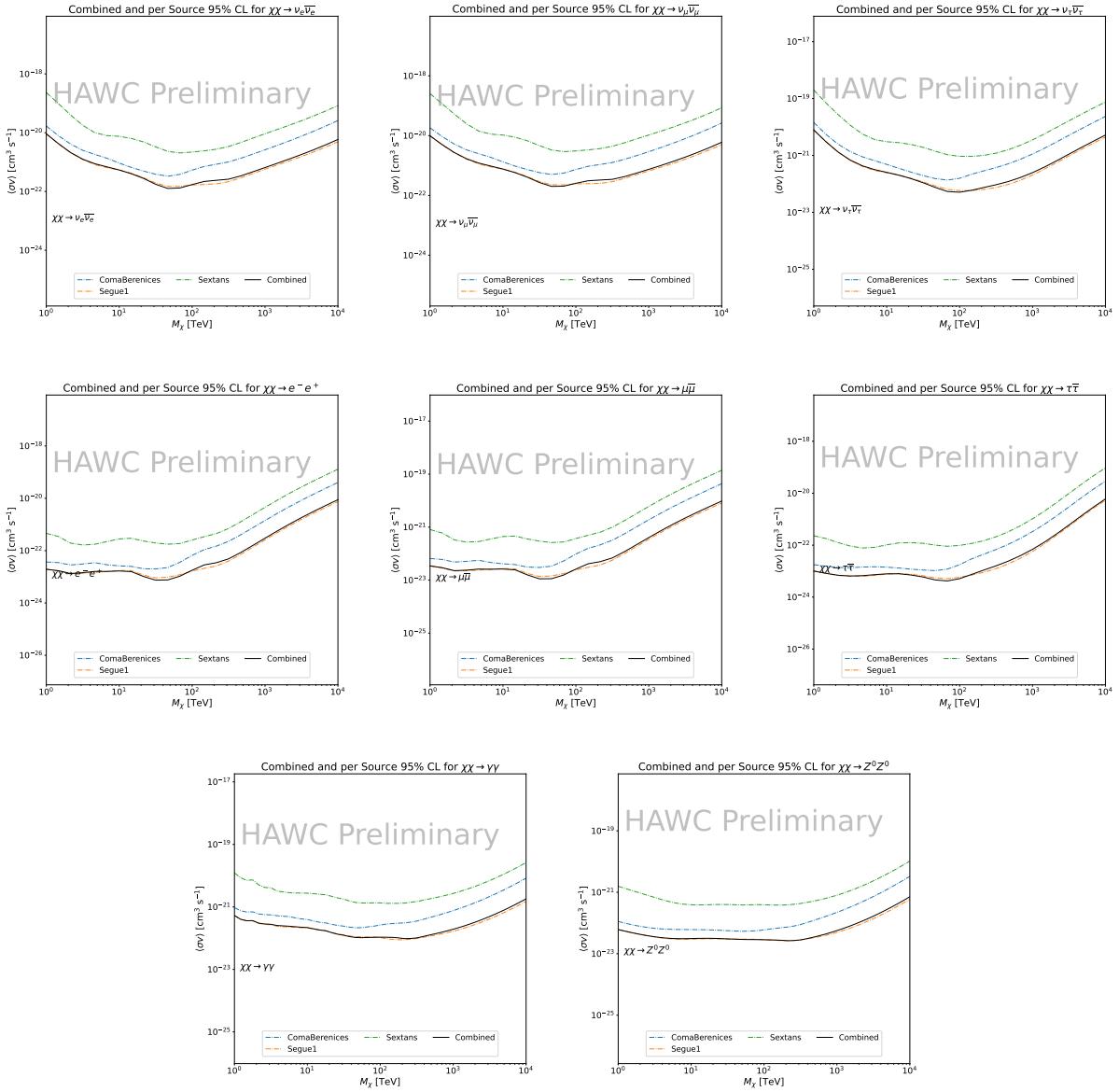


Figure 7.8 TODO: fill this out

1328 7.8 Conclusion and Discussion

1329 We want to include the remaining dSph and DM decay from the dSphs. We saw an improvement
 1330 of TODO: value compared to Glory Duck which had many more dSphs. TODO: copy some text
 1331 from earlier section.

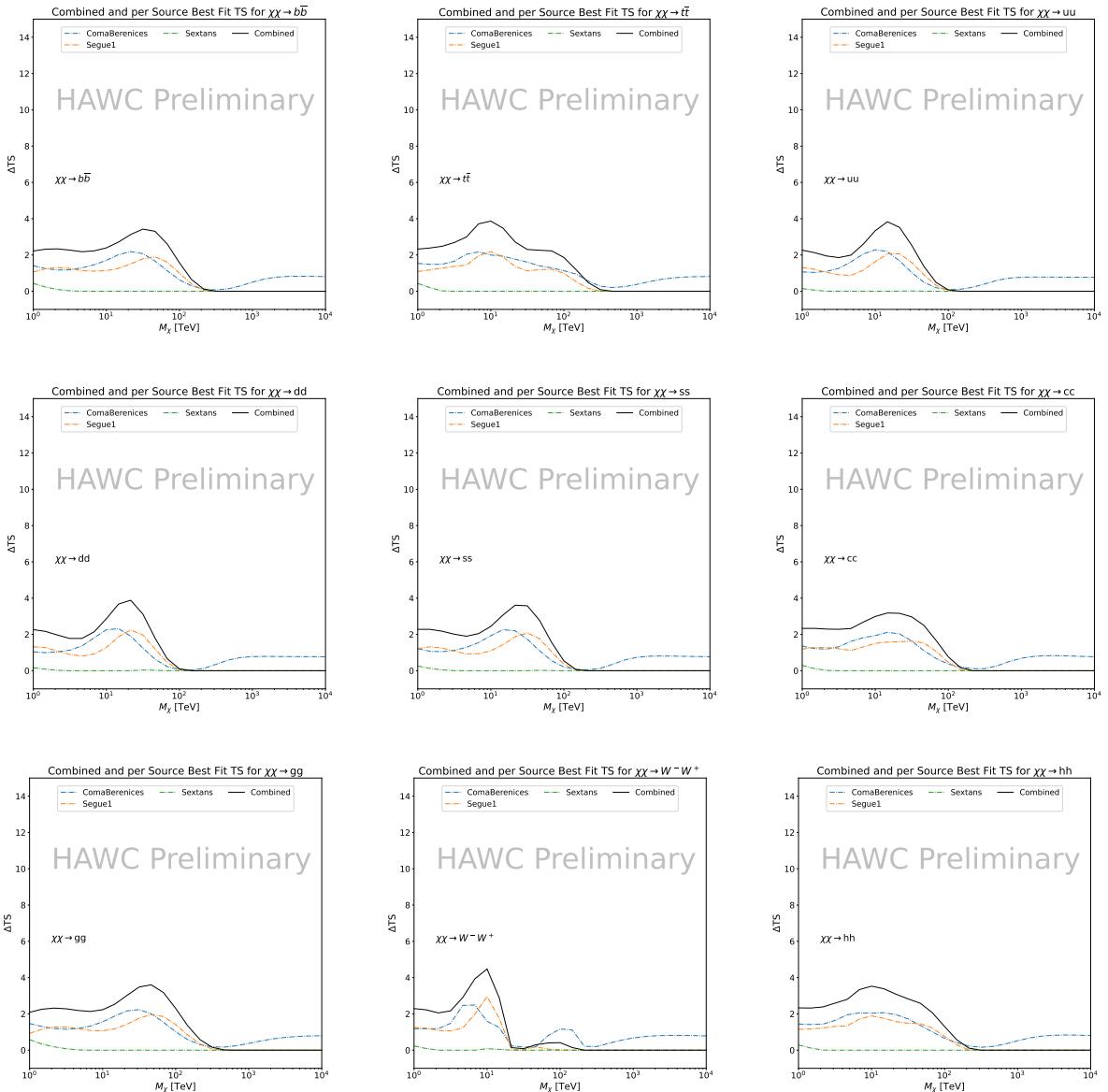


Figure 7.9 TODO: fill this out

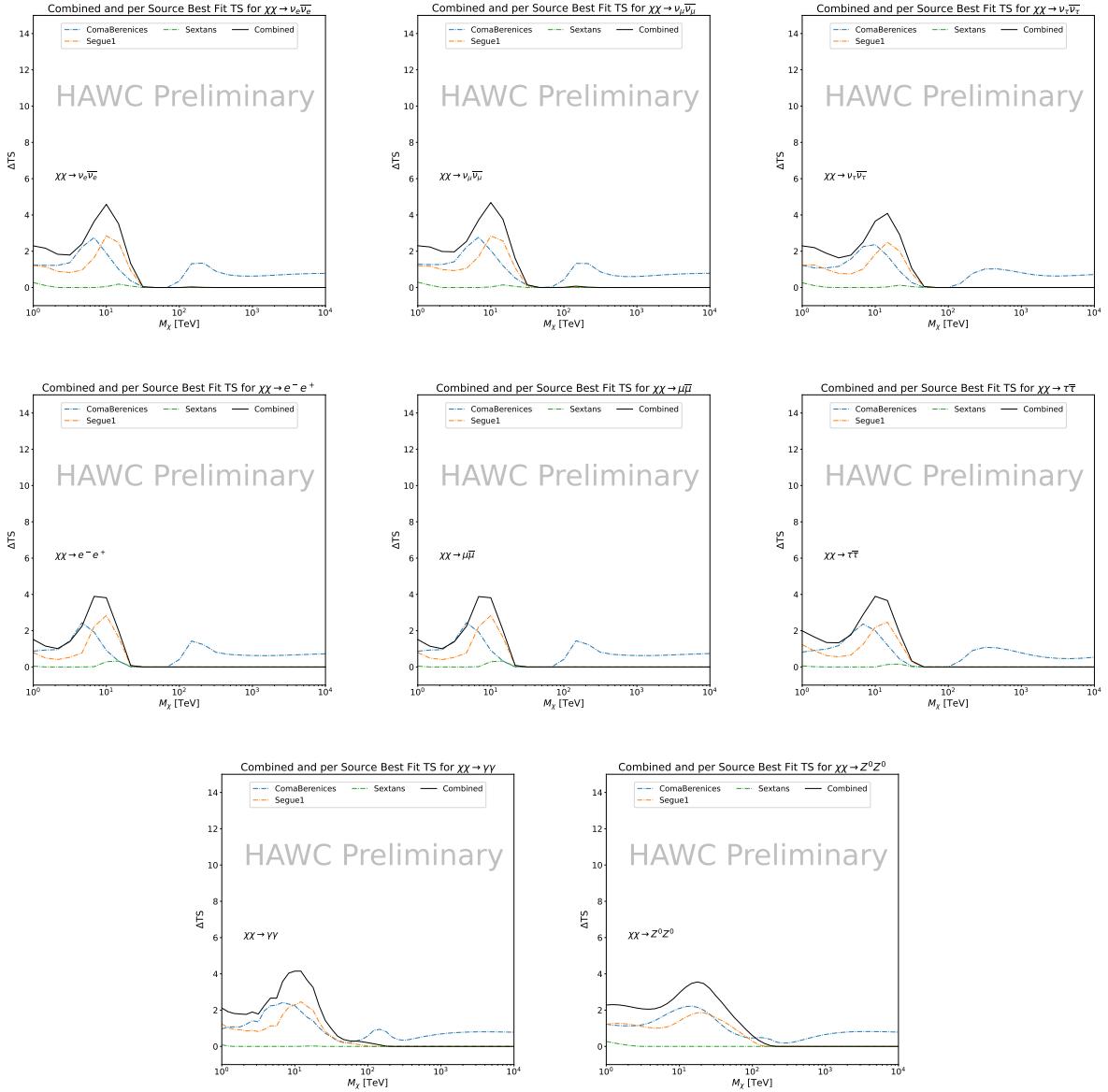


Figure 7.10 TODO: fill this out

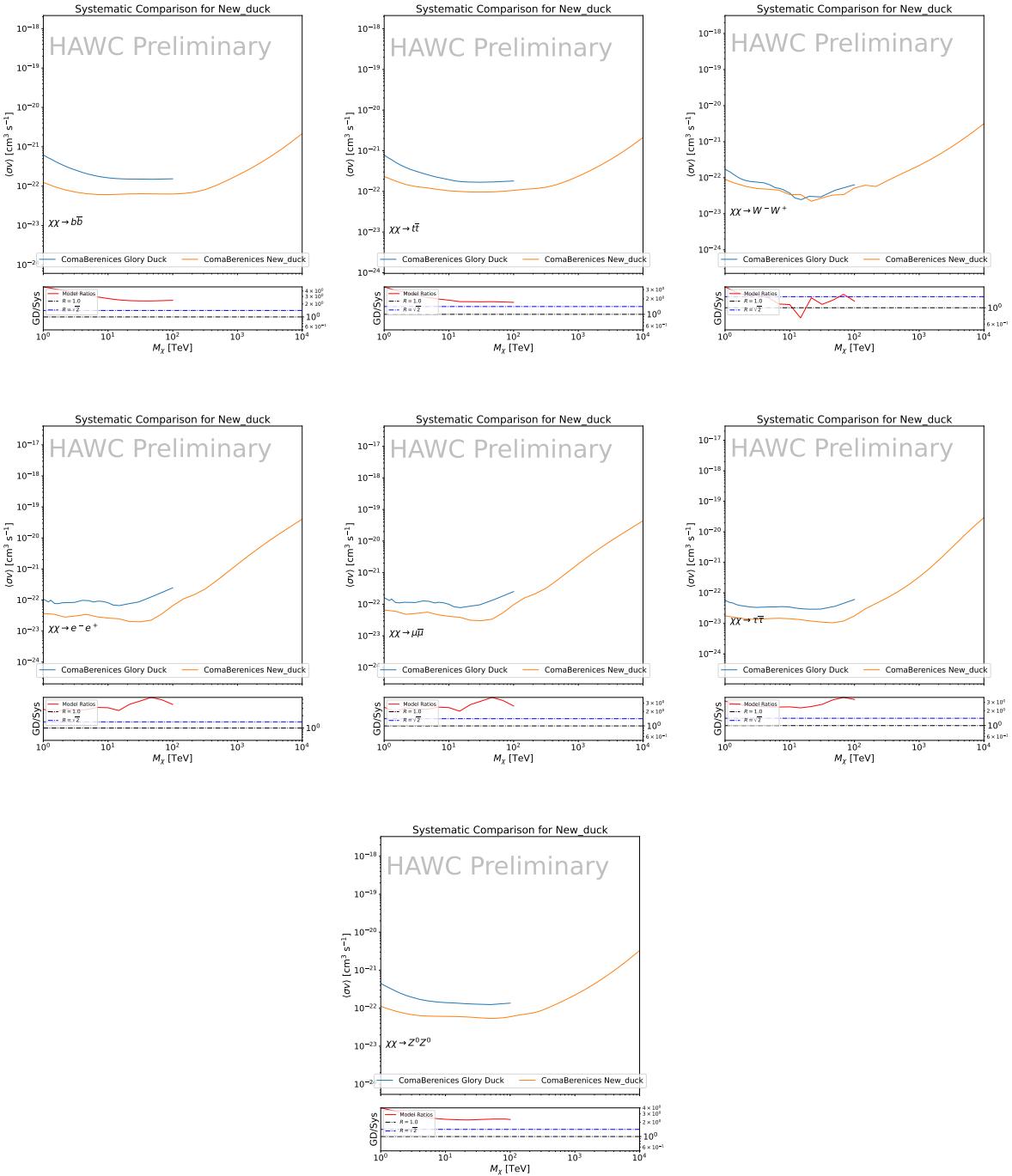


Figure 7.11 TODO: fill this out

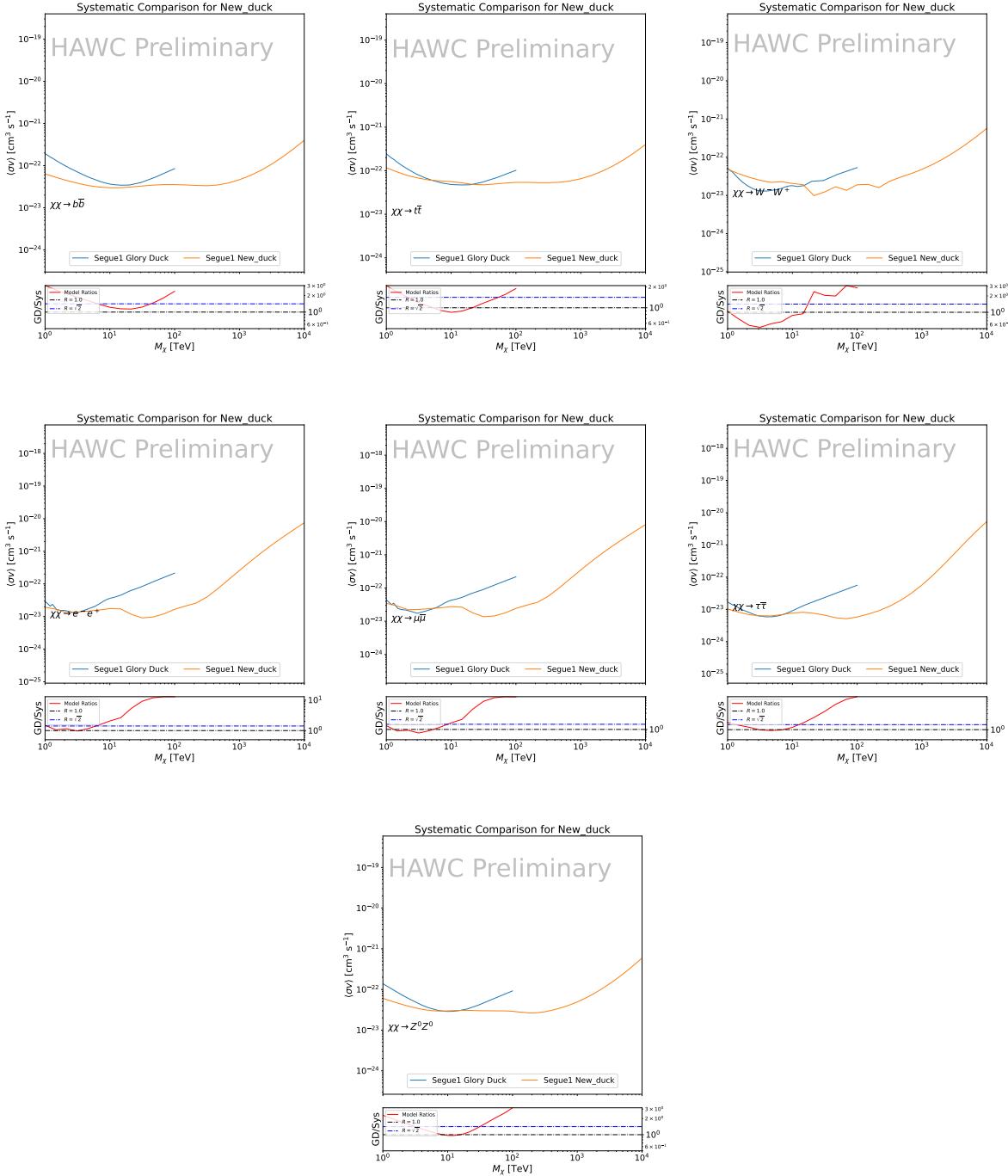


Figure 7.12 TODO: fill this out

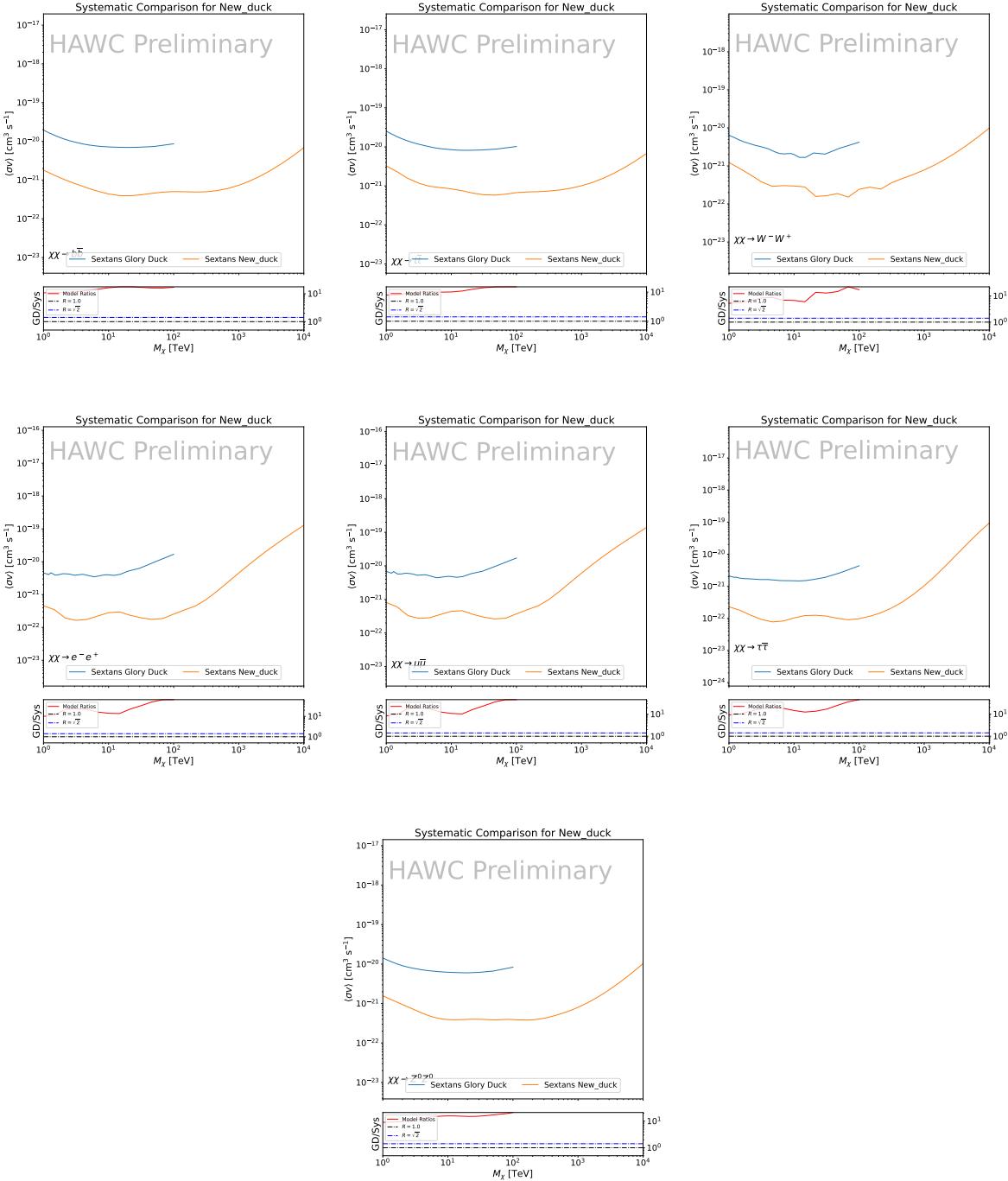


Figure 7.13 TODO: fill this out



Figure 7.14 TODO: show p1 and m1 limits around[NEEDS A SOURCE][FACT CHECK THIS]



Figure 7.15 TODO: there will be 2[NEEDS A SOURCE][FACT CHECK THIS]

CHAPTER 8

**1332 HEAVY DARK MATTER ANNIHILATION SEARCH WITH ICECUBE'S NORTH SKY
1333 TRACK DATA**

CHAPTER 9

NU DUCK

1334

APPENDIX A

MULTI-EXPERIMENT SUPPLEMENTARY FIGURES

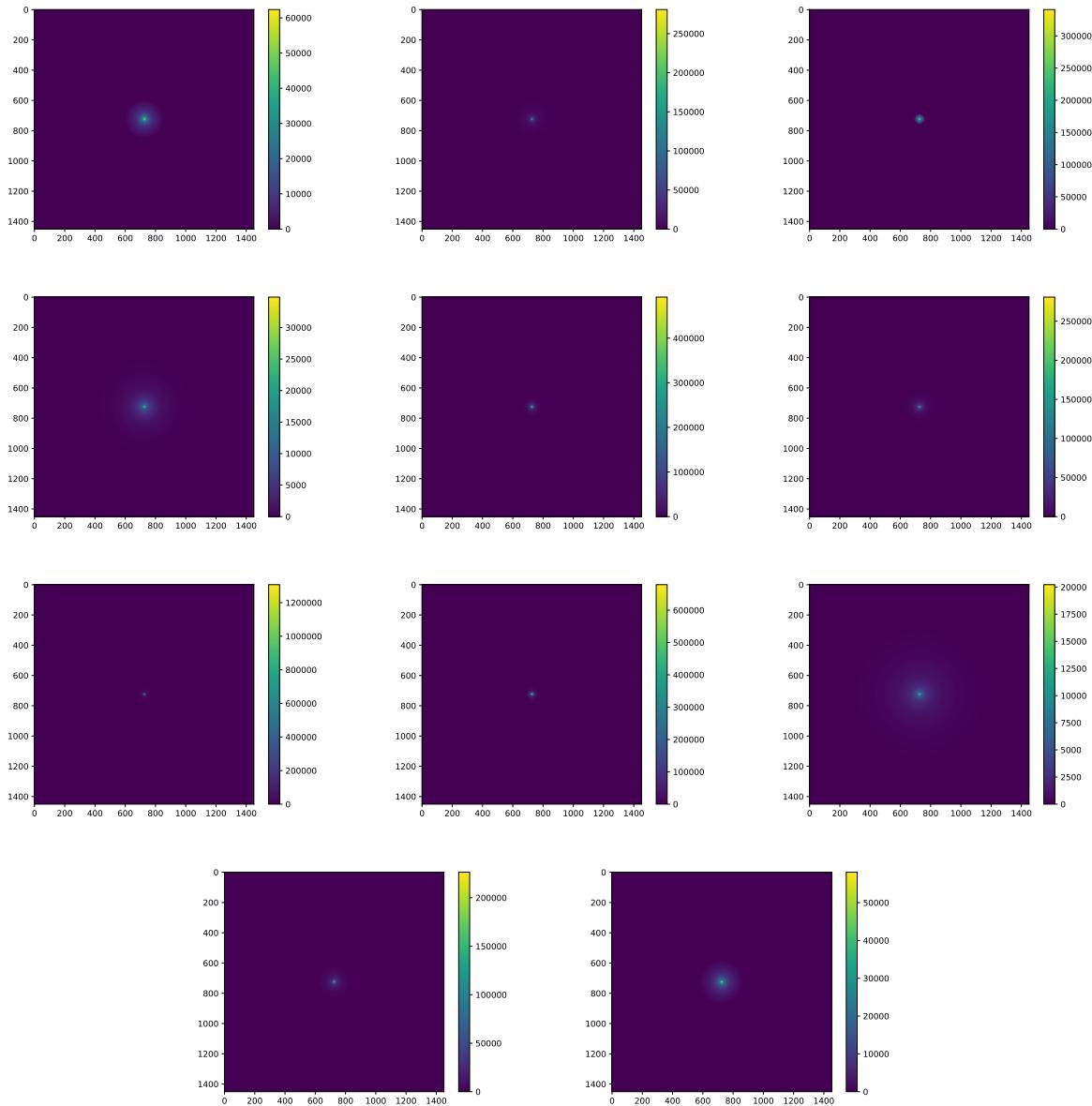


Figure A.1 Sister figure to Figure 6.3. Sources in the first row from left to right: Bootes I, Canes Venatici I, II. In second row: Draco, Hercules, Leo I. In the first row: Leo II, Leo IV, Sextans. In the final row: Ursa Major I, Ursa Major II.

APPENDIX B

1336

MULTITHREADING SUPPLEMENTARY FIGURES

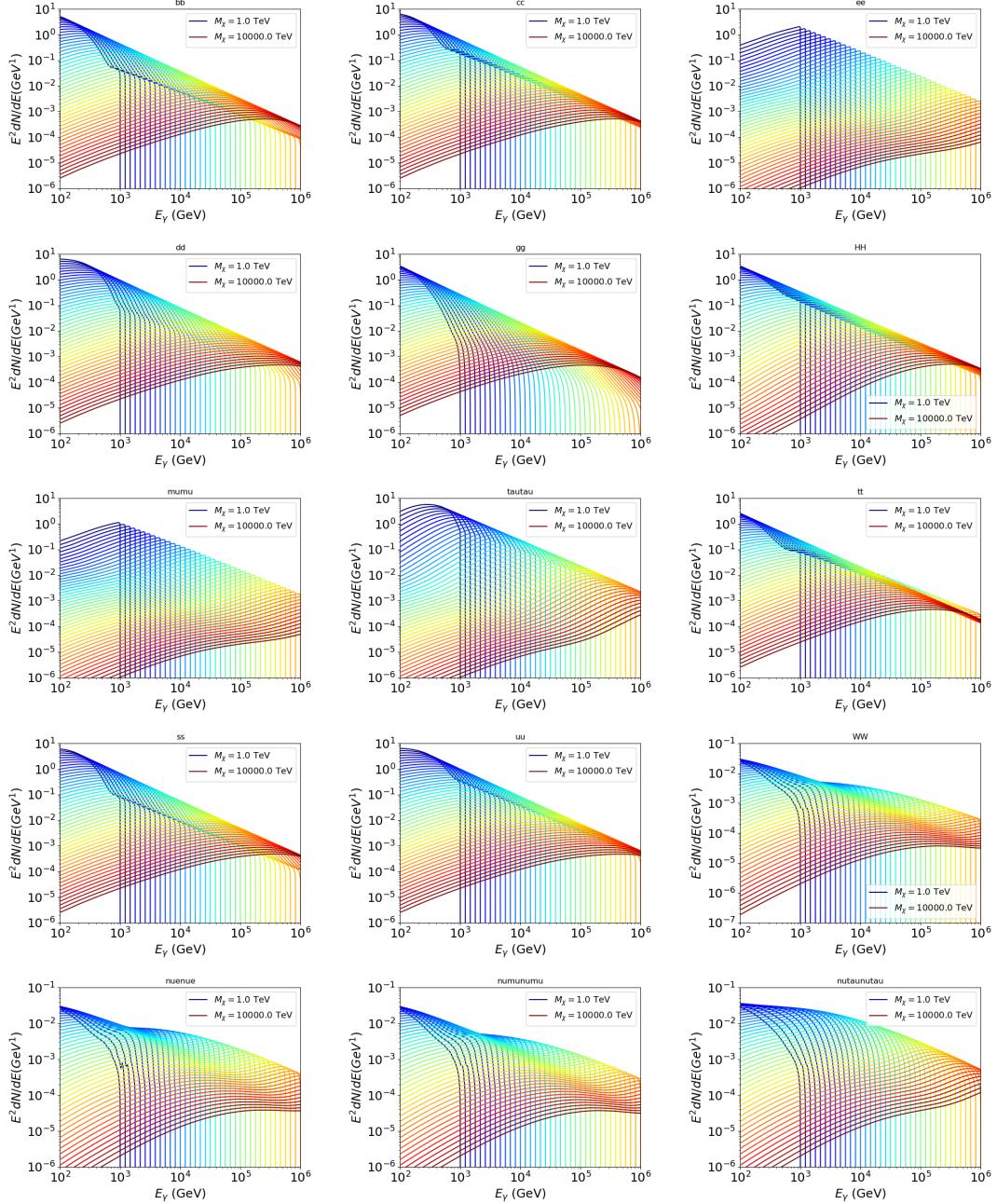


Figure B.1 Sister figure to Figure 7.2 for remaining SM primary annihilation channels studied for this thesis. These did not require any post generation smoothing and so are directly pulled from [64] with a binning scheme most helpful for a HAWC analysis.

1337 B.1 mpu_analysis.py

```
13381 import warnings
13392 with warnings.catch_warnings():
13403     warnings.simplefilter("ignore")
13414 # Python base libraries
13425 import os
13436 import sys
13447 import time
13458 # Import general libraries with namespace
13469 import matplotlib
13470 # Necessary for computing on cluster
13481 matplotlib.use("agg")
13492 import numpy as np
13503 import multiprocessing as mp
13514 # Import HAWC software
13525 sys.path.insert(1, os.path.join(os.environ['HOME'], 'hawc_software', 'threeML-
1353     analysis-scripts', 'fitModel'))
13546 from analysis_modules import *
13557 from threeML import *
13568 from hawc_hal import HAL, HealpixConeROI
13579 from threeML.minimizer.minimization import FitFailed
13580 # Import Dark Matter HAWC Libraries
13591 import analysis_utils as au
13602 import spectra as spec
13613 import sources as srcs
13624
13635 #* READ ONLY PATHS This block will change eventually
13646 MASS_LIST = './plotting/studies/nd/masses.txt'
13657 CHAN_LIST = './plotting/studies/nd/chans.txt'
13668
13679 #* WRITE PATHS, default location is to scratch
13680 OUT_PATH = os.path.join(os.environ["SCRATCH"], os.environ["USER"], 'New_duck')
```

```

13691 print('Our out path is going to be {}'.format(OUT_PATH))
13702
13713 # Define parallel Function. Can also be run serially
13724 def some_mass_fit(sigVs, datalist, shape, dSph, jfactor, mass_chan,
13735                 progress=None, log_file='', queue=None, i_job=0):
13746
13757     if progress is None:
13768         progress = [0]
13779     else: # Create log files for each thread
13780         log_file = log_file.replace('.log', '_ThreadNo_')
13791         log_file = log_file + str(i_job) + ".log"
13802         sys.stdout = open(log_file, "w")
13813
13824     fits = []
13835
13846     try:
13857         for m_c in mass_chan:
13868             print(f'Mass chan tuple: {m_c}')
13879             mass = int(m_c[0])
13880             ch = m_c[1]
13891             # Build path to output files
13902             outPath = os.path.join(OUT_PATH, ch, dSph)
13913             au.ut.ensure_dir(outPath)
13924
13935             if progress[i_job] < 0:
13946                 # If the master gets a Keyboard interrupt, commit suicide.
13957                 break
13968
13979                 ### Start Model Building for DM mass and SM channel #####
13980                 spectrum = spec.DM_models.HDMSpectra()
13991                 spectrum.set_channel(ch)
14002
14013                 myDwarf = ExtendedSource(dSph, spatial_shape=shape,

```

```

14024                     spectral_shape=spectrum)
14035
14046             spectrum.J = jfactor * u.GeV**2 / u.cm**5
14057             spectrum.sigmav = 1e-24 * u.cm**3 / u.s
14068             spectrum.set_dm_mass(mass * u.GeV)
14079
14080             spectrum.sigmav.bounds = (1e-30, 1e-12)
14091             model = Model(myDwarf)
14102             ##### End model Building #####
14113
14124             jl = JointLikelihood(model, datalist, verbose=False)
14135
14146             try:
14157                 result, lhdf = jl.fit(compute_covariance=False)
14168                 ts = -2.* (jl.minus_log_like_profile(1e-30) - jl.
1417 _current_minimum)
14189                 # Also profile the LLH vs sv
14190                 ll = jl.get_contours(spectrum.sigmav, sigVs[0],
14201                                 sigVs[-1], len(sigVs),
14212                                 progress=False, log=['False'])
14223
14234                 sigv_ll = au.ut.calc_95_from_profile(ll[0], ll[2])
14245                 # Write results to file
14256                 outFileLL = outPath+f"/LL_{dSph}_{ch}_mass{int(mass)}_GD.txt"
14267                 np.savetxt(outFileLL, (sigVs, ll[2]),
14278                               delimiter='\t', header='sigV\tLL\n')
14289
14290                 with open(outPath+f"/results_{dSph}_{ch}_mass{int(mass)}_GD.
1430 txt", "w") as results_file:
14311                     results_file.write("mDM [GeV]\tsigV_95\tsigV_B.F.\n")
14322
14333                     results_file.write("%i\t%.5E\t%.5E\t%.5E"%(mass, sigv_ll,
14344                                         ts, result.value[0]))

```

```

14355             # End write to file
14356
14357         except FitFailed: # Don't kill all threads if a fit fails
14358             print("Fit failed. Go back and calculate this spectral model
14359             later")
14360
14361             fits.append((ch, mass, -1, -1))
14362
14363             with open(log_file+'.fail', 'w') as f_file:
14364                 f_file.write(f'{ch}, {mass}\n')
14365
14366             progress[i_job] += 1
14367
14368             matplotlib.pyplot.close() # Prevent leaky memory
14369
14370
14371             fits.append((ch, mass, result.value[0], ts))
14372
14373             progress[i_job] += 1
14374
14375             matplotlib.pyplot.close()
14376
14377         except KeyboardInterrupt:
14378             progress[i_job] = -1
14379
14380
14381             fits = np.array(fits)
14382
14383             if queue is None:
14384
14385                 return fits
14386
14387             else:
14388
14389                 queue.put((i_job, fits))
14390
14391
14392     def main(args):
14393
14394         masses = np.loadtxt(MASS_LIST, dtype=int)
14395
14396         chans = np.loadtxt(CHAN_LIST, delimiter=',', dtype=str)
14397
14398         mass_chan = au.ut.permute_lists(chans, masses)
14399
14400
14401         print(f"DM masses for this study are: {masses}")
14402
14403         print(f"SM Channels for this study are XX -> {chans}")
14404
14405         print(mass_chan)
14406
14407
14408     # extract information from input argument

```

```

14687 dSph = args.dSph
14698 data_mngr = au.ut.Data_Selector('P5_NN_2D')
14709 dm_profile = srcts.Spatial_DM(args.catalog, dSph, args.sigma, args.decay)
14710
14721     ### Extract Source Information ####
14732 if dm_profile.get_dec() < -22.0 or dm_profile.get_dec() > 62.0:
14743     raise ValueError("HAWC can't see this source D: Exitting now...")
14754
14765 print(f'{dSph} information')
14776 print(f'jfac: {dm_profile.get_factor()}\tRA: {dm_profile.get_ra()}\tDec: {dm_profile.get_dec()}\n')
14797
14808 shape = SpatialTemplate_2D(fits_file=dm_profile.get_src_fits())
14819     ### Finish Extract Source Information ####
14820
14831     ### LOAD HAWC DATA ####
14842 roi = HealpixConeROI(data_radius=2.0, model_radius=8.0,
14853                         ra=dm_profile.get_ra(), dec=dm_profile.get_dec())
14864 bins = choose_bins.analysis_bins(args, dec=dm_profile.get_dec())
14875
14886 hawc = HAL(dSph, data_mngr.get_datmap(), data_mngr.get_detres(), roi)
14897 hawc.set_active_measurements(bin_list=bins)
14908 datalist = DataList(hawc)
14919     ### FINISH LOAD HAWC DATA ####
14920
14931 # set up SigV sampling. This sample is somewhat standardized
14942 sigVs = np.logspace(-28,-18, 1001, endpoint=True) # NOTE This will change
1495 whith HDM
14963
14974 if args.n_threads == 1:
14985     # No need to start || programming just iterate over the masses
14996     kw_arg = dict(sigVs=sigVs, datalist=datalist, shape=shape, dSph=dSph,
15007                     jfactor=dm_profile.get_factor(), mass_chan=mass_chan,

```

```

15018                 log_file=args.log)
15029             some_mass_fit(**kw_arg)
15030         else:
15041             # I Really want to suppress TQMD output
15052             from tqdm import tqdm
15063             from functools import partialmethod
15074             tqdm.__init__ = partialmethod(tqdm.__init__, disable=True)
15085
15096             x = np.array_split(mass_chan, args.n_threads)
15107             n_jobs = len(x)
15118
15129             print("Thread jobs summary by mass and SM channel")
15130             for xi in x:
15141                 print(f'{xi}')
15152
15163             queue = mp.Queue()
15174             progress = mp.Array('i', np.zeros(n_jobs, dtype=int))
15185
15196             # Define task pool that will be split amongsts threads
15207             kw_args = [dict(sigVs=sigVs, datalist=datalist, shape=shape,
15218                             dSph=dSph, jfactor=dm_profile.get_factor(),
15229                             mass_chan=mass_chan, progress=progress,
15230                             queue=queue, i_job=i, log_file=args.log)
15241                 for i, mass_chan in enumerate(x)]
15252
15263             # Define each process
15274             procs = [mp.Process(target=some_mass_fit, kwargs=kw_args[i]) \
15285                 for i in range(n_jobs)]
15296
15307             ### Start MASTER Thread only code block ###
15318             # Begin running all child threads
15329             for proc in procs: proc.start()
15330

```

```

15341     try:
15352         # In this case, the master does nothing except monitor progress of
1536         the threads
15373         # In an ideal world, the master thread also does some computation.
15384         n_complete = np.sum(progress)
15395         while_count = 0
15406
15417         while n_complete < len(mass_chan):
15428
15439             if np.any(np.asarray(progress) < 0):
15440                 # This was no threads are stranded when killing the script
15451                 raise KeyboardInterrupt()
15462             if while_count%1000 == 0:
15473                 print(f"{np.sum(progress)} of {len(mass_chan)} finished")
15484
15495             n_complete = np.sum(progress)
15506             time.sleep(.25)
15517             while_count += 1
15528
15539         except KeyboardInterrupt:
15540             # signal to jobs that it's time to stop
15551                 for i in range(n_jobs):
15562                     progress[i] = -2
15573                     print('\nKeyboardInterrupt: terminating early.')
15584             ### End MASTER Thread only code block ###
15595
15606             fitss = [queue.get() for proc in procs]
15617             print(fitss)
15628             print(f'Thread statuses: {progress[:]}')
15639
15640             # putting results in a file
15651
15662             print("QUACK! All Done!")

```

```

15673
15684
15695 if __name__ == '__main__':
15706     import argparse
15717
15728     p = argparse.ArgumentParser(description="Run a DM annihilation analysis on
1573         a dwarf spheroidal for a specific SM channel for DM masses [1 TeV to 10
1574         PeV]")
15759
15760     # Dwarf spatial modeling arguements
15771     p.add_argument("-ds", "--dSph", type=str,
15782             help="dwarf spheroidal galaxy to be studied", required=
1579     True)
15803     p.add_argument("-cat", "--catalog", type=str, choices=['GS15', 'LS20'],
15814             default='LS20', help="source catalog used")
15825     p.add_argument("-sig", "--sigma", type=int, choices=[-1, 0, 1], default=0,
15836             help="Spatial model uncertainty. 0 corresponds to the
1584 median. +/-1 correspond to the +/-1sigma uncertainty respectively.")
15857
15868     # Arguements for the energy estimators
15879     p.add_argument("-e", "--estimator", type=str,
15880             choices=['P5_NHIT', 'P5_NN_2D'],
15891             default="P5_NN_2D", required=False,
15902             help="The energy estimator choice. Options are: P5_NHIT,
1591 P5_NN_2D. GP not supported (yet).")
15923     p.add_argument("--use-bins", default=None, nargs="*",
15934             help="Bins to use for the analysis", dest="use_bins")
15945     p.add_argument('--select_bins_by_energy', default=None, nargs="*",
15956             help="Does nothing. May fill in later once better
1596 understood")
15977     p.add_argument('--select_bins_by_fhit', default=None, nargs="*",
15988             help="Also does nothing see above")
15999     p.add_argument( '-ex', "--exclude", default=None, nargs="*",

```

```

16000         help="Exclude Bins", dest="exclude")

16011

16022 # Computing and logging arguements.

16033 p.add_argument('-nt', '--n_threads', type=int, default=1,
16044                         help='Maximum number of threads spawned by script. Default
16055 is 4')

16065 p.add_argument('-log', '--log', type=str, required=True,
16076                         help='Name for log files. Especially needed for threads')

16087

16098 p.add_argument('--decay', action="store_true",
16109                         help='Set spectral DM hypothesis to decay')

16110

16121 args = p.parse_args()

16132 print(args.decay)

16143 if args.exclude is None: # default exclude bins 0 and 1
16154     args.exclude = ['B0C0Ea', 'B0C0Eb', 'B0C0Ec', 'B0C0Ed', 'B0C0Ee']

16165

16176 if args.decay: OUT_PATH += '_dec'
16187 else: OUT_PATH += '_ann'

16198

16209 OUT_PATH = OUT_PATH + '_' + args.catalog
16210 if args.sigma != 0: OUT_PATH += f'_{args.sigma}sig'

16221

16232 main(args)

```

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