


National University of Computer and Emerging Sciences, Lahore Campus				
	Course:	Theory of Automata	Course Code:	CS 301
	Program:	BS (CS)	Semester:	Fall 2019
	Duration:	60 minutes	Total Marks:	40
	Paper Date:	9 November, 2019	Weight:	
	Section:	-	Page(s)	2
	Exam:	Midterm 2		
Student Name: _____ Roll Number: _____				
Instruction/Notes	1. Solve in the space provided. Extra sheets will NOT be marked. 2. One A4 handwritten help sheet is allowed in the exam. 3. Make a reasonable assumption in case of ambiguity. Good luck!			

PROBLEM 1 (Marks: 10)

Write a context free grammar for the following language and clearly indicate the start symbol.

$$L = \{0^n 1^m \mid m \neq n, m \geq 0, n \geq 0\}$$

PROBLEM 2 (Marks: 10)

Construct a **deterministic PDA** to accept the following language. Show its state transition diagram.

$$L = \{0^i 1^j 2^k \mid i \geq 0, j \geq 0, i \geq 0, j = i + k\}$$

PROBLEM 3**(Marks: 10)**

Show the transition diagram of a **single tape deterministic Turing machine** to decide the following:

$L = \{x\#y \mid x \text{ and } y \text{ have the same number of zeros and } x \in \{0,1\}^* \text{ and } y \in \{0,1\}^*\}$

PROBLEM 4**(Marks: 5+5)**

1. Prove that the following is an ambiguous grammar using right most derivations:

$S \rightarrow S0S \mid 0SS \mid 0$

2. Remove unit productions from the following grammar and write the final grammar. S is the start symbol.

$S \rightarrow AB$
 $A \rightarrow C$
 $B \rightarrow D$
 $C \rightarrow C0 \mid D$
 $D \rightarrow 0 \mid 1 \mid AB$

