



Course:	Applied Physics	Course Code:	EE117
Program:	BS (CS)	Semester:	Fall 2019
Duration:	60 minutes	Total Marks:	40
Paper Date:	08-11-2019	Weight	15%
Section:	All	Page(s):	4
Exam:	Midterm 2	Roll No:	N.II
Name	M. Shiraz Ahmad	Section:	B/F

Instruction/Notes: Attempt All Questions. Write your answer within the space provided only.
Do not attach any rough sheet with the paper.

Question 1(a): Three point charges lie along the x axis as shown in the figure below. The positive charge $q_1=15\mu\text{C}$ is at $x=2\text{m}$, the positive charge $q_2=6\mu\text{C}$ is at the origin, and the resultant force acting on q_3 is zero. **What is the x coordinate of q_3 ?** (10 marks)

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$$

Solution:

$$F_{13} = k \frac{|q_1||q_3|}{(2-x)^2}; F_{23} = k \frac{|q_2||q_3|}{x^2}$$

$$F_{13} = F_{23} \rightarrow 2 \text{ marks}$$

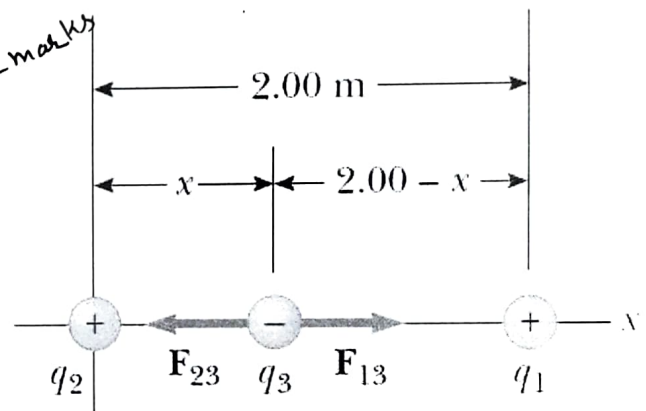
$$k \frac{|q_1||q_3|}{(2-x)^2} = k \frac{|q_2||q_3|}{x^2}$$

$$(2.00-x)^2 |q_2| = x^2 |q_1|$$

$$(4 - 4x + x^2)(6 \times 10^{-6} \text{ C}) = x^2 (15.0 \times 10^{-6} \text{ C})$$

$$\Rightarrow 3x^2 + 8x - 8 = 0 \rightarrow 2 \text{ marks}$$

$$\Rightarrow \text{roots: } \left\{ \begin{array}{l} x = 0.775 \text{ m} \\ x = -3.44 \text{ m} \end{array} \right\} \rightarrow 2 \text{ marks}$$



Question 1(b): Find the (a) **magnitude** and (b) **direction (θ)** of the total electric field at the origin of the coordinate system due to two point charges, q_1 and q_2 . The two charges are located at the xy-coordinate position of: (0 cm, -2 cm) and (+4 cm, 0 cm), respectively. **Draw the resultant of Net Electric field on the given figure.** (10 marks)

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$$

$$|E_1| = k \frac{|q_1|}{r_1^2}$$

$$= (9 \times 10^9) \frac{5 \times 10^{-9} \text{ C}}{(2 \times 10^{-2})^2}$$

$$|E_1| = 1.125 \times 10^5 \text{ N/C} \rightarrow 2 \text{ marks}$$

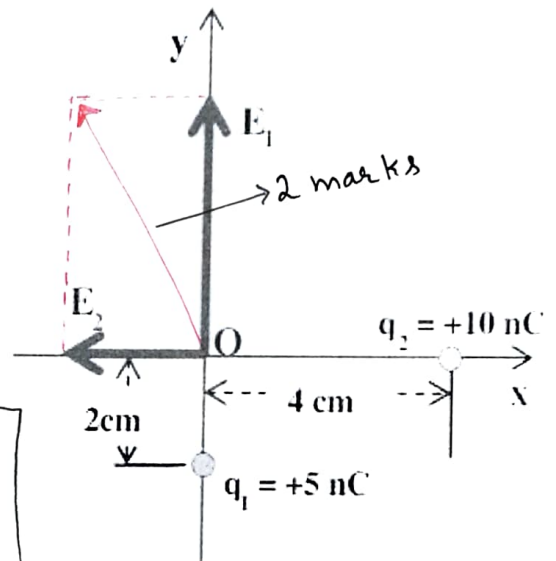
$$|E_2| = k \frac{|q_2|}{r_2^2}$$

$$= (9 \times 10^9) \frac{10 \times 10^{-9} \text{ C}}{(4 \times 10^{-2})^2}$$

$$|E_2| = 0.5625 \times 10^5 \text{ N/C} \rightarrow 2 \text{ marks}$$

$$E = \sqrt{E_1^2 + E_2^2}$$

$$|E| = 1.25 \times 10^5 \text{ N/C} \rightarrow 4 \text{ marks}$$



$$\theta = \tan^{-1}\left(\frac{E_1}{E_2}\right) = -63.4^\circ \text{ or } (180^\circ - 63.4^\circ) = 116.6^\circ \rightarrow 4 \text{ marks}$$

→ This marking Scheme may vary case to case.

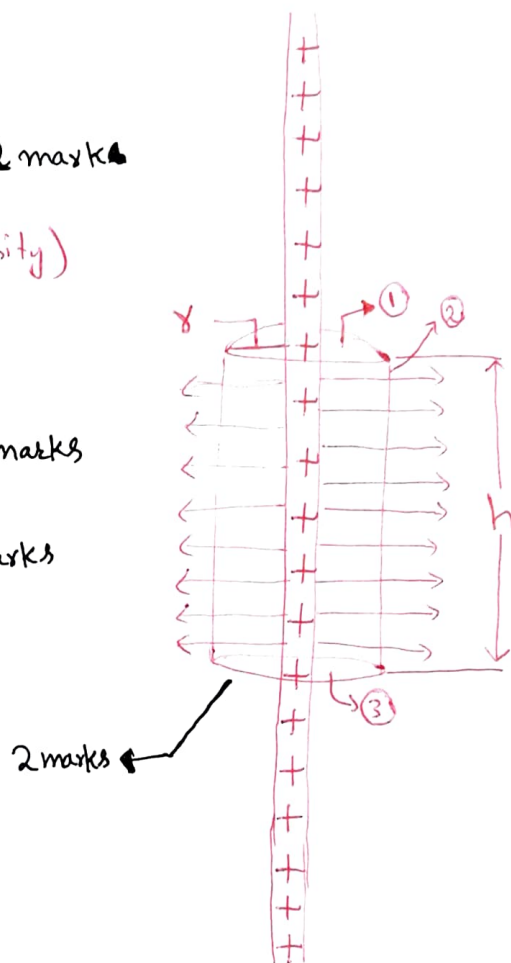
Question 2(a): A Gaussian surface in the form of a closed cylinder surrounds a section of a very long, uniformly charged, cylindrical plastic rod. Calculate electric field for this rod by applying Gauss law. Make a diagram as well. (7 marks).

$$\oint \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} q_{\text{enc}} \longrightarrow 1 \text{ mark}$$

$$E \oint dA = \frac{1}{\epsilon_0} (\lambda h) \quad \text{Linear Charge Density}$$

$$0 + E(2\pi r h) + 0 = \frac{1}{\epsilon_0} (\lambda h) \longrightarrow 2 \text{ marks}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r} \longrightarrow 2 \text{ marks}$$



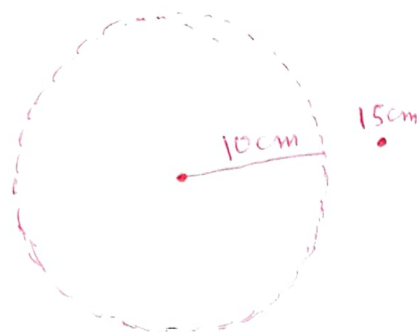
Question 2(b): An unknown charge sits on a conducting solid sphere of radius 10 cm. If the electric field 15 cm from the center of the sphere has the magnitude $3.0 \times 10^3 \text{ N/C}$ and is directed radially inward, what is the net charge on the sphere? (5 marks).

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$$

$$|q| = 4\pi\epsilon_0 r^2 E \longrightarrow 3 \text{ marks}$$

$$= \frac{(0.15 \text{ m})^2 (3.0 \times 10^3 \text{ N/C})}{8.99 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2}$$

$$\left. \begin{aligned} |q| &= 7.5 \times 10^{-9} \text{ C} \\ q &= -7.5 \times 10^{-9} \text{ C} \end{aligned} \right\} \longrightarrow 2 \text{ marks}$$



Question 3: Charge $Q_1 = 20e$ Coulombs is at point $P_1 (2, 3, 4)$ m; Charge $Q_2 = 40e$ Coulombs is at point $P_2 (5, -3, 6)$ m, where e = elementary electron's charge (1.60×10^{-19} C). $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$

Write a MATLAB program to find:

- (a) Coulomb's force acting on charge Q_1 (F_1),
 - (b) Coulomb's force acting on charge Q_2 (F_2)
- (8 marks).

- No predefined grading scheme; if a student is solving by himself & just writing in MATLAB syntax, zero marks will be given.
- Marks will be given if code relies more on MATLAB in determining the solution.
- Using built in functions will be appreciated!

Extended Solution:

```

1 %-----%
2 % Declaring Variables %
3 %-----%
4 clear all % clear all variables, etc. from memory
5 P = 1.602e-19; % electrical charge of proton, C
6 Ep0 = 8.85e-12; % Air permittivity, F/m
7 Q1 = 20*P; % 1st charge
8 Q2 = 40*P; % 2nd charge
9 P1 = [2 3 4]; % location of 1st charge
10 P2 = [5 -3 6]; % location of 2nd charge
11 %-----%
12 % Computing the forces %
13 %-----%
14 R12 = P2-P1; % a vector from point P1 to point P2
15 R21 = P1-P2; % a vector from point P2 to point P1
16 R = norm(R12); % norm of vector R12, also norm of vector R21
17 a12= R12/R; % a unit vector in the direction of vector R12
18 a21= R21/R; % a unit vector in the direction of vector R12
19 % Coulomb's law: F = (Q1 Q2)/(4 * pi * epsilon_0 R^2 ) a_r
20 F21 = Q1*Q2/(4*pi*Ep0*R^2)*a12; % Force acting on Q2 due to Q1
21 F12 = Q1*Q2/(4*pi*Ep0*R^2)*a21; % Force acting on Q1 due to Q2
22 % Display results
23 F12
24 F21

```

OP:

$$F_{12} = -1.6147e-27 \quad 3.2294e-27 \quad -1.0765e-27$$

$$F_{21} = 1.6147e-27 \quad -3.2294e-27 \quad +1.0765e-27$$