

CS 201: DISCRETE STRUCTURES
SECTION G

September 18, 2018.

Quiz 2 Solution

Translate the following English sentences into propositional logic using the following propositions:

$P(x)$: x is a Pakistani

$O(x)$: x is an office

$W(x,y)$: x works at y

Operators you are allowed to use: $\{\wedge, \vee, \neg, \rightarrow, \leftrightarrow\}$. Quantifiers you are allowed to use are: $\{\forall, \exists\}$

PROBLEM 1

All Pakistanis work in some office.

$$\forall x (\exists y (O(y) \wedge (P(x) \rightarrow W(x,y)))$$

PROBLEM 2

Osama does not work in any office.

(All the following solutions are correct)

$$\neg \exists x (O(x) \wedge W(\text{osama}, x))$$

$$\forall x (O(x) \rightarrow \neg W(\text{osama}, x))$$

$$\forall x (O(x) \wedge \neg W(\text{osama}, x))$$

PROBLEM 3

There is an office in which no Pakistani works.

$$\exists y (O(y) \wedge \forall x (P(x) \rightarrow \neg W(x,y)))$$