

Discrete Structures (CS1005)

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Course Instructors

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Final Exam

Total Time: 3 Hours

Total Marks: 75

Total Questions: 5

Student Signature

Attempt all questions. Attach question paper to the answer sheet.

CLO #1: Express statements in terms of predicates, quantifiers and logical connectives.

Q. No 1:

[15=5+10]

- Show that $(p \rightarrow q) \wedge (q \rightarrow r) \rightarrow (p \rightarrow r)$ is a tautology.
- Translate each of these statements into logical expressions using predicates, quantifiers, and logical connectives.
 - All tools are in the correct place and are in excellent condition.
 - Nothing is in the correct place and is in excellent condition.
 - The negation of a contradiction is a tautology.
 - There is no one in this class who knows French and Russian.
 - At least one of your friends is perfect.

CLO #3: Apply fundamental concepts of number theory, such as divisibility, greatest common divisors, modular arithmetic, prime numbers, and congruences.

Q. No 2:

[15=5+10]

- Use the extended Euclidean algorithm to express $\gcd(252, 356)$ as a linear combination of 252 and 356.
- Use the construction in the proof of the Chinese remainder theorem to find all solutions to the system of congruences $x \equiv 1 \pmod{2}$, $x \equiv 2 \pmod{3}$, $x \equiv 3 \pmod{5}$, and $x \equiv 4 \pmod{11}$.

CLO #4: Apply mathematical induction to prove properties of sequences.

Q. No 3:

[15=5+5+5]

- Prove that $2^n > n^2$, if n is an integer greater than 4.
- Let m be an integer with $m > 1$. i. Show that the relation $R = \{(a, b) \mid a \equiv b \pmod{m}\}$ is an equivalence relation on the set of integers.
- Find the transitive closure of $\{(1, 1), (1, 4), (2, 1), (2, 3), (3, 1), (3, 2), (3, 4), (4, 2)\}$ on $\{1, 2, 3, 4\}$.

CLO #4: Apply mathematical techniques to solve recursive relation.

Q. No 4:

[15=5+10]

a. Solve these recurrence relations together with the given initial conditions.

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$$a_n = -6a_{n-1} - 9a_{n-2} \text{ for } n \geq 2, a_0 = 3, a_1 = -3$$

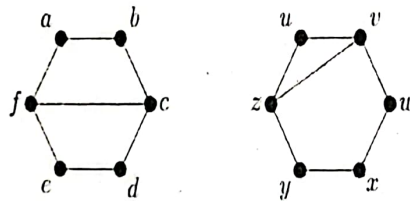
- ✱ b. How many different messages can be transmitted in n microseconds using three different signals if one signal requires 1 microsecond for transmittal, the other two signals require 2 microseconds each for transmittal, and a signal in a message is followed immediately by the next signal? [Use appropriate technique to find general solution of linear homogeneous recurrence relation).

CLO #6: Apply graph theory concepts to compute network related metrics and develop solutions for computing applications related to the program.

Q No 5:

[15=5+10]

a. Determine whether the given pair of graphs is isomorphic or not. Justify your answer.



- b. Define the following terminologies with one example for each term, i. Bipartite Graph ii. Wheel iii. Complete Graph iv. Degree sequence v. Directed Graph