

MSBA Program
Quantitative Management Modeling
Assignment number 2 (Q1-Q2-Q3)

Question number 1: (Computer Center Staffing)

Decision Variables:

Z: This is the objective variable to maximize profit

P1: The Number of Part time consultants who work for the first shift (8am – noon)

P2: The Number of Part time consultants who work for the second shift (noon – 4pm)

P3: The Number of Part time consultants who work for the third shift (4pm – 8pm)

P4: The Number of Part time consultants who work for the fourth shift (8pm – midnight)

F1: The Number of full-time consultants who work for the first shift (8am – 4pm)

F2: The Number of full-time consultants who work for the second shift (noon – 8pm)

F3: The Number of full-time consultants who work for the third shift (4pm – midnight)

Objective Function:

Max profit $Z = 48 (P1 + P2 + P3 + P4) + 112 (F1 + F2 + F3)$

Constraints

$$F1 + P1 \geq 4$$

$$F1 + F2 + P2 \geq 8$$

$$F2 + F3 + P3 \geq 10$$

$$F3 + P4 \geq 6$$

$$P1 \geq F1$$

$$P_2 \geq F_1 + F_2$$

$$P_3 \geq F_2 + F_3$$

$$P_4 \geq F_3$$

$$P_1, P_2, P_3, P_4 \geq 0$$

$$F_1, F_2, F_3 \geq 0$$

b) We need to add more full-time consultants to the three shifts

so, we will add three more fs F_4, F_5, F_6

F_4 represents the new staff of the first shift

F_5 represents the new staff of the first shift

F_6 represents the new staff of the first shift

Objective Function:

$$\text{Max profit } Z = 48 (P_1 + P_2 + P_3 + P_4) + 112 (F_1 + F_2 + F_3 + F_4 + F_5 + F_6)$$

Constraints

$$F_1 + F_4 + P_1 \geq 4$$

$$F_1 + F_2 + F_4 + F_5 + P_2 \geq 8$$

$$F_2 + F_3 + F_5 + F_6 + P_3 \geq 10$$

$$F_5 + F_6 + P_4 \geq 6$$

$$P_1 \geq F_1$$

$$P_2 \geq F_1 + F_2$$

$$P_3 \geq F_2 + F_3$$

$$P_4 \geq F_3$$

$$P_1, P_2, P_3, P_4 \geq 0$$

$$F_1, F_2, F_3, F_4, F_5, F_6 \geq 0$$

Q2: The Decision Variables:

Z: objective variable to maximize profit

X1: represents the number of units produced from model “Collegiate”

X2: represents the number of units produced from model “Mini”

Objective Function: Max. $Z = 32X_1 + 24X_2$

The constraints are:

1. $3X_1 + 2X_2 \leq 5000$
2. $45X_1 + 40X_2 \leq 84,000$
3. $X_1 \leq 1000$
4. $X_2 \leq 1200$
5. $X_1, X_2 \geq 0$

Solution:

1- $3X_1 + 2X_2 = 5000$

(0, 2500)

(1,666.66, 0)

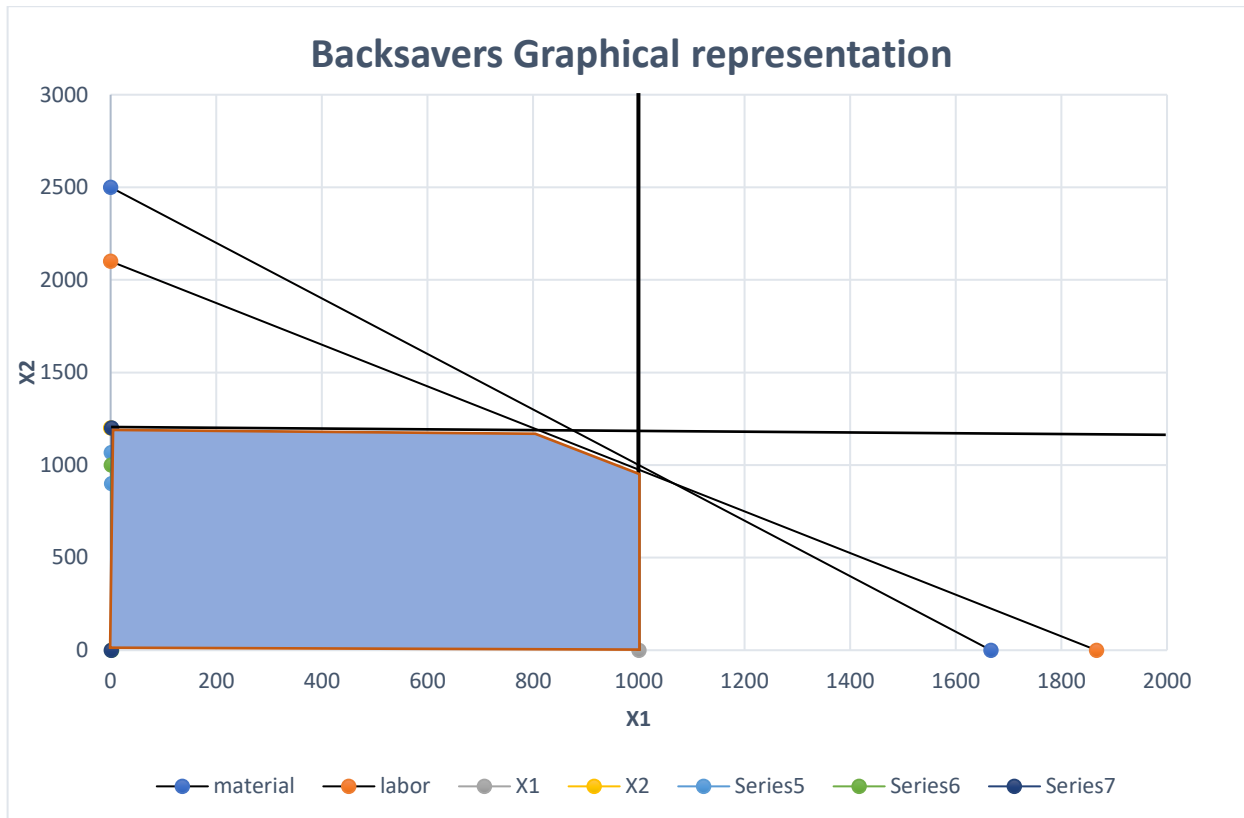
2- $45X_1 + 40X_2 = 84,000$

(0, 2100)

(1866.66, 0)

3- $X_1 \leq 1000$

4- $X_2 \leq 1200$



$X1 = 1000$, and $X2 = 1000$

Q3:

Decision Variables:

Z: objective variable to maximize profit

L_i : represents the total number of units produced from “Large-Size” ($Lp1 + Lp2 + Lp3$)

M_i : represents the total number of units produced from “Medium-Size” ($Mp1 + Mp2 + Mp3$)

S_i : represents the total number of units produced from “Small-Size” ($Sp1 + Sp2 + Sp3$)

Lp_1 : Number of Large-Size units produced by Plant (1)

Lp_2 : Number of Large-Size units produced by Plant (2)

Lp_3 : Number of Large-Size units produced by Plant (3)

Mp_1 : Number of Medium-Size units produced by Plant (1)

Mp_2 : Number of Medium-Size units produced by Plant (2)

Mp_3 : Number of Medium-Size units produced by Plant (3)

Sp_2 : Number of Small-Size units produced by Plant (1)

Sp_1 : Number of Small-Size units produced by Plant (2)

Sp_3 : Number of Small-Size units produced by Plant (3)

Objective Function:

Max. $Z = 420 (Lp_1 + Lp_2 + Lp_3) + 360 (Mp_1 + Mp_2 + Mp_3) + 300 (Mp_1 + Mp_2 + Mp_3)$

S.T

$$Lp_1 + Mp_1 + Sp_1 \leq 750$$

$$Lp_2 + Mp_2 + Sp_2 \leq 900$$

$$Lp_3 + Mp_3 + Sp_3 \leq 450$$

$$20 Lp_1 + 15 Mp_1 + 12 Sp_1 \leq 13000$$

$$20 Lp_2 + 15 Mp_2 + 12 Sp_2 \leq 12000$$

$$20 Lp_3 + 15 Mp_3 + 12 Sp_3 \leq 5000$$

$$Lp_1 + Lp_2 + Lp_3 \leq 900$$

$$Mp_1 + Mp_2 + Mp_3 \leq 1200$$

$$Sp_1 + Sp_2 + Sp_3 \leq 750$$

$$Lp_1, Lp_2, Lp_3, Mp_1, Mp_2, Mp_3, Sp_1, Sp_2, Sp_3 \geq 0$$