# Invariant and Equivariant Neural Networks

Adrian Salewsky

Technische Universität Berlin

12.05.2023

### Introduction

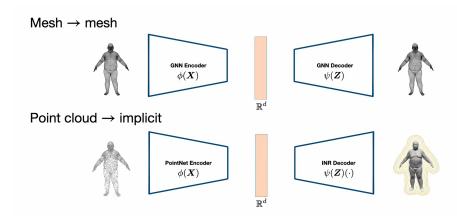
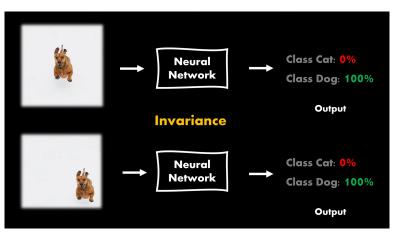


Figure: https://www.youtube.com/watch?v=Lft6r5oVyXM

#### Invariance



 $\label{eq:Figure:https://www.youtube.com/watch?v=2bP\_KuBrXSc} Figure: https://www.youtube.com/watch?v=2bP\_KuBrXSc$ 

# Equivariance

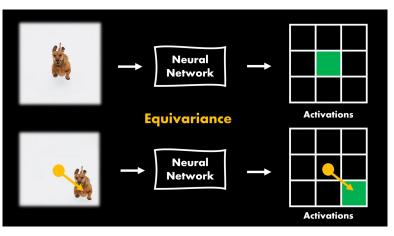


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- ullet If frame invariant/equivariant o only averaging over frame needed

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- FAUST Dataset