Lecture 7:
Shared Memory Parallelization

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Aims for this module

- Identify parts / blocks of code that are (easily) parallelizable
- Learn how to parallelize using
  - ThreadGroup (Posix threads)
  - Workstream (Threaded building blocks)

Reference material

- Tutorials
  - https://dealii.org/current/doxygen/deal.II/step_9.html
  - https://dealii.org/current/doxygen/deal.II/step_13.html
  - http://www.math.colostate.edu/~bangerth/videos.676.39.html
  - http://www.math.colostate.edu/~bangerth/videos.676.40.html
- Documentation:
  - https://dealii.org/current/doxygen/deal.II/group__threads.html
  - https://www.dealii.org/current/doxygen/deal.II/namespaceWorkStream.html
  - https://dealii.org/current/doxygen/deal.II/namespaceparallel.html

Identifying parallelizable code

- Consider this example:

```
template <int dim>
void MyProblem<dim>::setup_system (){
  dof_handler.distribute_dofs();
  DoFTools::make_hanging_node_constraints (…);    // 1
  DoFTools::make_sparsity_pattern (…);            // 2
  VectorTools::interpolate_boundary_values (…);   // 3
…
}
```

- Operations (1,2,3) are independent of one another
  - Could be reordered without consequence

Identifying parallelizable code

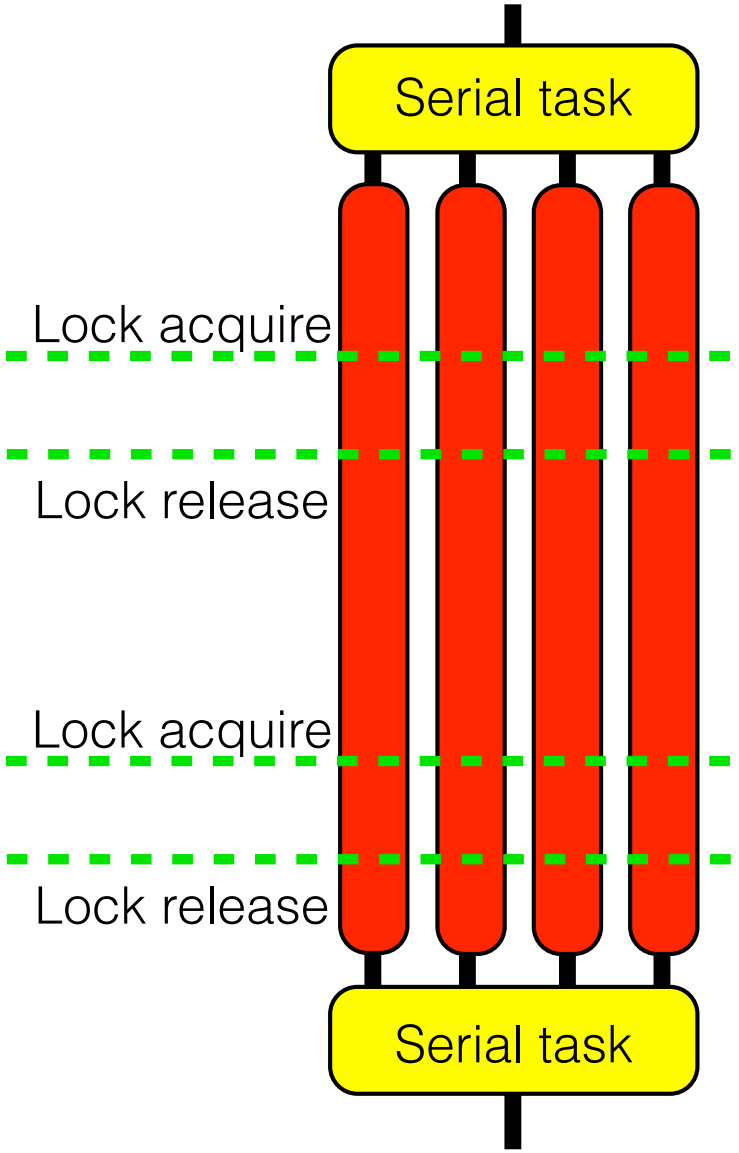
- "Embarrassingly parallelizable tasks"

```
template <int dim>
void MyProblem<dim>::assemble_system () {
…
for (auto cell : dof_handler.active_cells()) {
  fe_values.reinit (cell);
  ...assemble local contribution...
  ...copy local contribution into global matrix/rhs vector...
}
}
```

- Many more cells than machine cores
- Computations of local matrices/vectors are mutually independent
- **Accumulation into global system matrix/vector is not!**

Independent threaded tasks: Option 1

- Code divergence with / without barriers (global / in-thread locks)
- Best used for small number of completely independent tasks
- Inside each thread: Shared data
  - Reading is a safe operation!
  - Use locks to allow data writing
    - Convergence point for threads (bottleneck)
    - Potential for deadlocks



Creating independent threaded tasks: the Thread class

```
template <int dim>
void MyProblem<dim>::setup_system (){
  dof_handler.distribute_dofs();

  Threads::Thread<void> thread1, thread2, thread3;

  thread1 = Threads::new_thread (&DoFTools::make_hanging_node_constraints,…);
  thread2 = Threads::new_thread (&DoFTools::make_sparsity_pattern, …);
  thread3 = Threads::new_thread (&VectorTools::interpolate_boundary_values,,…);

  thread1.join();     // and same for thread2, thread3
  …
}
```

- The call to join() is a blocking call
- Waits to the thread to finish before continuing

Creating independent threaded tasks: the ThreadGroup class

```
void MyProblem<dim>::assemble_on_one_cell (cell_iterator &cell) {…}

void MyProblem<dim>::assemble_system () {
  Threads::ThreadGroup<void> threads;

  for (cell=dof_handler.begin_active(); …)
    threads += Threads::new_thread (
      &MyProblem<dim>::assemble_on_one_cell,
      this, cell);

  threads.join_all ();
}
```

- Why is this inefficient?
- How do we prevent data races?

Creating independent threaded tasks: Ranged based assembly

- Less threads created = more efficient

```
void MyProblem<dim>::assemble_on_cell_range (
  cell_iterator &range_begin,
  cell_iterator &range_end) {…};

void MyProblem<dim>::assemble_system () {
  Threads::ThreadGroup<void> threads;

  std::vector<std::pair<cell_iterator, cell_iterator> >
    sub_ranges = Threads::split_range (
      dof_handler.begin_active(),
      dof_handler.end(),
      n_virtual_cores);

  for (t=0; t<n_virtual_cores; ++t)
    threads += Threads::new_thread (
      &MyProblem<dim>::assemble_on_cell_range,
      this,
      sub_ranges[t].first,
      sub_ranges[t].second);

  threads.join_all ();}
}
```

Independent threaded tasks

- How do we prevent data races?

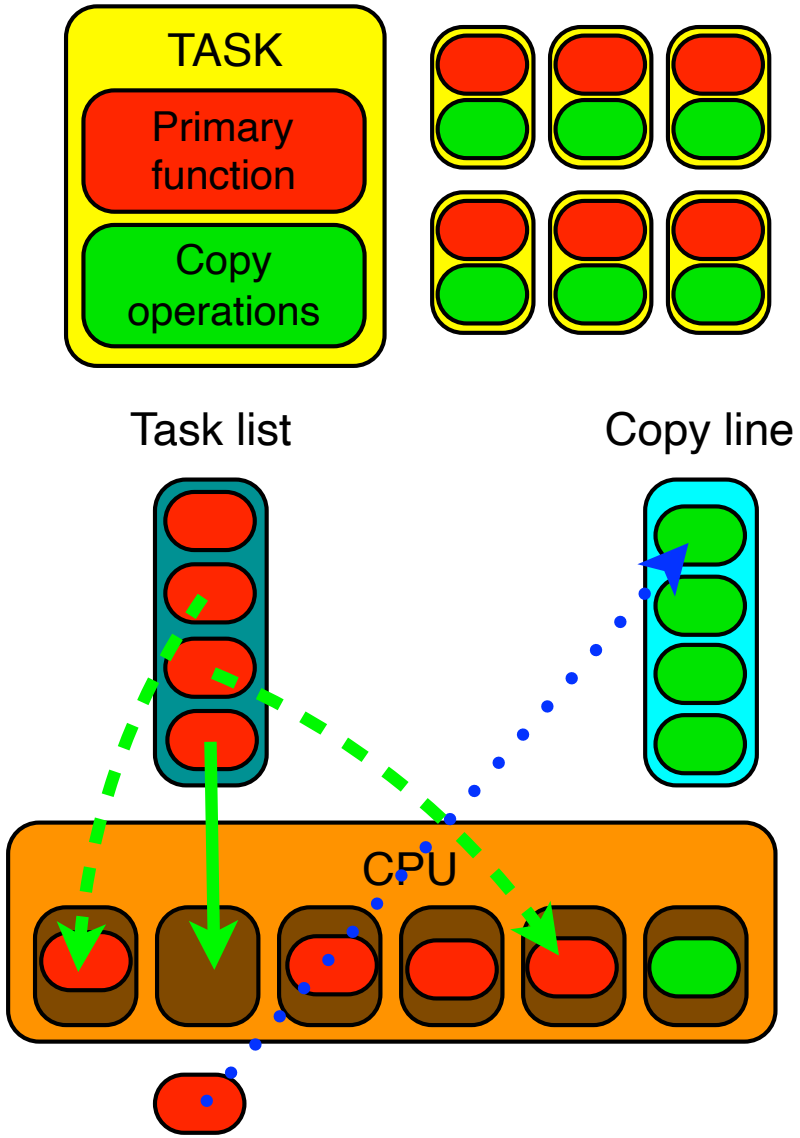
```
void MyProblem<dim>::assemble_on_one_cell (cell_iterator &cell) {

  static Threads::Mutex mutex;

  mutex.acquire ();
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)
      system_matrix.add (dof_indices[i], dof_indices[j],
                         cell_matrix(i,j));
  ...same for rhs...
  mutex.release ();
}
```

Creating independent threaded tasks: the WorkStream class

- Task-based threading
  - Continuous use of free CPU cores
  - Create a list of tasks
  - When core free, use it to perform next task
    - Expensive operations continually executed
  - Perform blocking tasks independently
    - Data copied to shared objects serially
  - Optimizations:
    - “Automatic” load balancing
    - Overhead reduction: Works on data chunks



Creating independent threaded tasks: parallelization of (per-cell) assembly

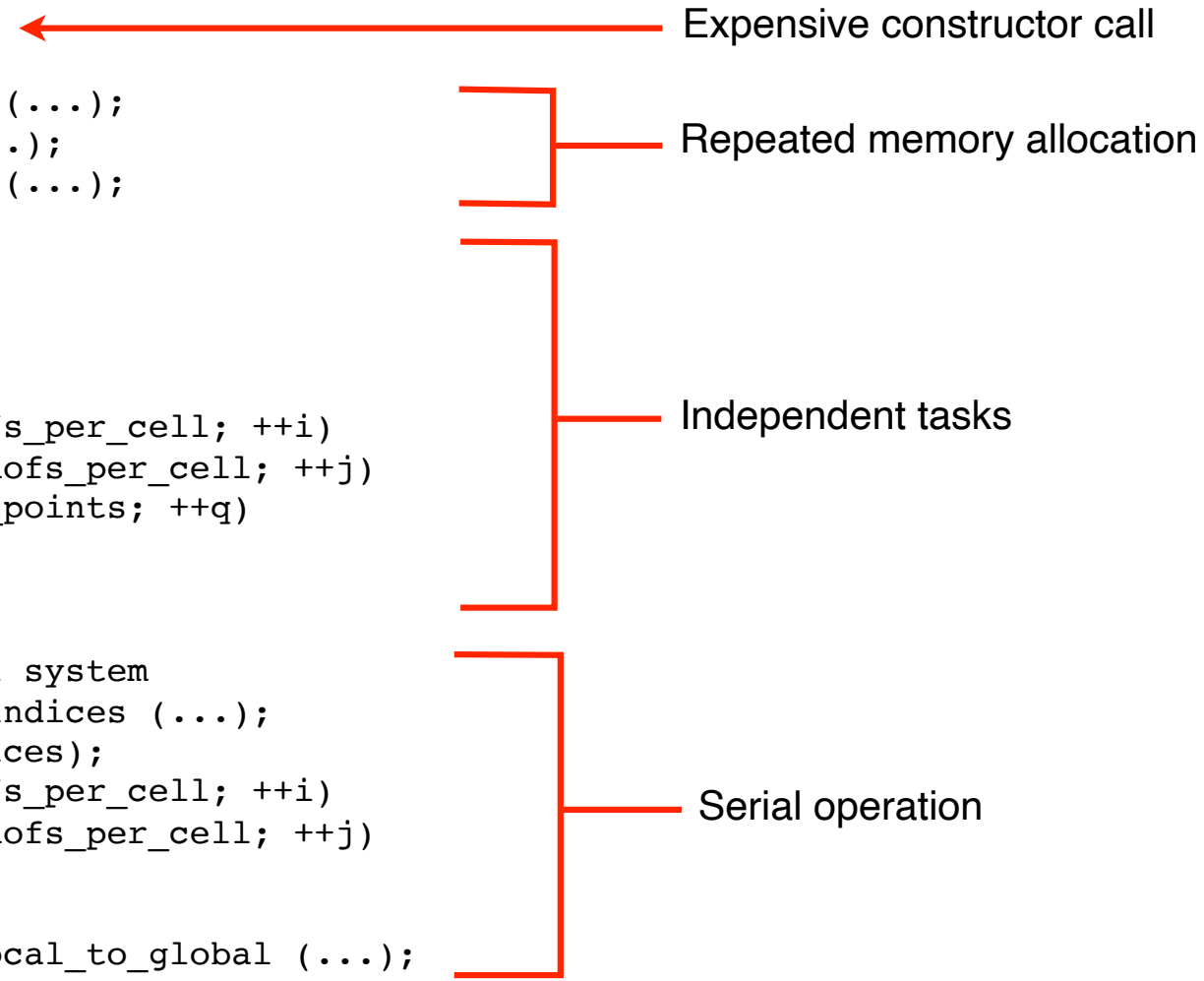
```
template <int dim>
void MyClass<dim>::assemble_on_one_cell (
   const typename DoFHandler<dim>::active_cell_iterator &cell)
{
  FEValues<dim> fe_values (...);

  FullMatrix<double> cell_matrix (...);
  Vector<double>     cell_rhs (...);
  std::vector<double> rhs_values (...);

  rhs_function.value_list (...)

  // assemble local contributions
  fe_values.reinit (cell);
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)
      for (unsigned int q=0; q<n_points; ++q)
        cell_matrix(i,j) += ...;
  ...same for cell_rhs...

  // now copy results into global system
  std::vector<unsigned int> dof_indices (...);
  cell->get_dof_indices (dof_indices);
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)
      system_matrix.add (...);
  ...same for rhs...
  // or constraints.distribute_local_to_global (...);
}
```



Threading using WorkStream: the ScratchData class

- Assistant struct / class
- Contains reused data structures
  - FEValues objects
  - Helper vectors and storage containers
  - Precomputed data
- Needs a constructor and a copy constructor
  - Some objects must be manually reconstructed
  - We create one initial instance of the class
  - TBB duplicates as required (queue_length)

```
struct ScratchData {
  std::vector<double>       rhs_values;
  FEValues<dim>             fe_values;

  ScratchData (
    const FiniteElement<dim> &fe,
    const Quadrature<dim>    &quadrature,
    const UpdateFlags         update_flags)
    : rhs_values (quadrature.size()),
      fe_values (fe, quadrature, update_flags)
    {}

   ScratchData (const ScratchData &rhs)
   : rhs_values (rhs.rhs_values),
     fe_values (rhs.fe_values.get_fe(),
                rhs.fe_values.get_quadrature(),
                rhs.fe_values.get_update_flags())
    {}
}
```

Threading using WorkStream: the PerTaskData class

- Contains data structures required for serial operations
  - Multiple copies made (queue_length*chunk_size)
  - Must be “self-contained”
- Used in two places
  - Threaded function
    - Bound to an instance of the threaded function
    - Used as a “data-in” object
  - Serial function
    - A used instance is passed to this function
    - Used as a “data-out” object

```
struct PerTaskData {
  FullMatrix<double>        cell_matrix;
  Vector<double>            cell_rhs;
  std::vector<unsigned int> dof_indices;

  PerTaskData (const FiniteElement<dim> &fe)
  : cell_matrix (fe.dofs_per_cell,
                 fe.dofs_per_cell),
    cell_rhs (fe.dofs_per_cell),
    dof_indices (fe.dofs_per_cell)
  {}
}
```

Threading using WorkStream: Revised assembly

```
template <int dim>
void MyClass<dim>::assemble_on_one_cell (
   const typename DoFHandler<dim>::active_cell_iterator &cell,
   ScratchData &scratch,
   PerTaskData &data)
{
  // reinitialise data
  scratch.fe_values.reinit (cell);
  rhs_function.value_list (scratch.fe_values.get_quadrature_points,
                           scratch.rhs_values);
  ...
  data.cell_matrix = 0;
  data.cell_rhs    = 0;

  // assemble local contributions
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)
      for (unsigned int q=0; q<fe_values.n_quadrature_points; ++q)
        data.cell_matrix(i,j) += ...;
  ...
}
```

- Now use objects contained within ScratchData and PerTaskData structs

Threading using WorkStream: Serial copy operation

```
template <int dim>
void MyClass<dim>::copy_local_to_global (const PerTaskData &data)
{
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)
      system_matrix.add (data.dof_indices[i], data.dof_indices[j],
                         data.cell_matrix(i,j));
  ...same for rhs…
  // or constraints.distribute_local_to_global (...);
}
```

- Uses writes “fixed” data in PerTaskData to single class object system_matrix (and whatever else)
- Has to be a serially performed operation

Threading (not) using WorkStream: Manual assembly using these data structures

```
ScratchData scratch_data (…);
PerTaskData per_task_data (…);

DoFHandler<deal_II_dimension>::active_cell_iterator
   cell = dof_handler.begin_active(),
   endc = dof_handler.end();
   for (; cell != endc; ++cell)
{
   assemble_system_one_cell(cell,
                            scratch_data,
                            per_task_data);
   copy_local_to_global(per_task_data);
}
```

- This performs the same serial assembly as we had before
  - More efficient though (use of ScratchData)

Threading using WorkStream

```
ScratchData scratch_data (…);
PerTaskData per_task_data (…);

WorkStream::run ( dof_handler.begin_active(),
                  dof_handler.end(),
                  *this,
                  &MyClass::assemble_system_one_cell,
                  &MyClass::copy_local_to_global,
                  scratch_data,
                  per_task_data );
```

- Execute function in threaded manner
- Only operates on functions with a specific prototype
  - Theadable function:
    void function_name(cell, scratch, per_task_data)
  - Serial function:
    void function_name(per_task_data)

Threading using WorkStream

```
WorkStream::run ( dof_handler.begin_active(),
                  dof_handler.end(),
                  std::bind(&Solid::assemble_residual_one_cell,
                            this,
                            _1,  // cell
                            _2,  // scratch
                            _3), // data
                  std::bind(&Solid::copy_local_to_global_residual,
                            this,
                            _1, // data
                           &in_vector),
                  scratch_data,
                  per_task_data_residual);
```

- copy_local_to_global_F function prototype:
  void function (per_task_data, vector)
- std::bind only binds memory addresses
  - Will make copies of objects not sent in via memory address
  - Need to send in pointers if wish to work on an existing object
  - “std::_1, _2, _3” are placeholders for expected data