Aim: Implement curve: Bezier for n

Bezier Curve

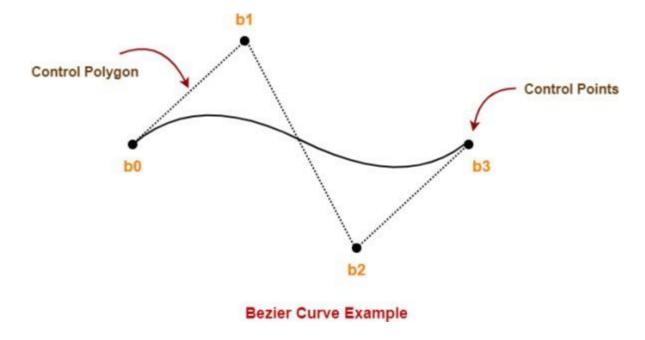
Bezier Curve may be defined as-

- •Bezier Curve is parametric curve defined by a set of control points.
- Two points are ends of the curve.
- Other points determine the shape of the curve.

The concept of bezier curves was given by Pierre Bezier.

Bezier Curve Example

The following curve is an example of a bezier curve:



Here,

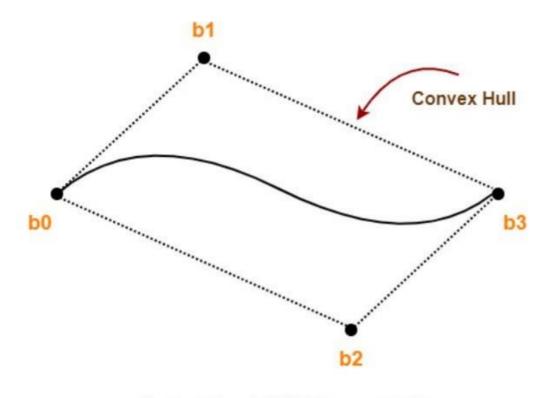
- This bezier curve is defined by a set of control points b0, b1, b2 and b3.
- Points b0 and b3 are ends of the curve.
- Points b1 and b2 determine the shape of the curve.

Bezier Curve PropertiesFew important properties of a bezier curve are

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Property-01:

Bezier curve is always contained within a polygon called as convex hull of its control points.



Bezier Curve With Convex Hull

Property-02:

- •Bezier curve generally follows the shape of its defining polygon.
- The first and last points of the curve are coincident with the first and last points of the defining polygon.

Property-03:

The degree of the polynomial defining the curve segment is one less than the total number of control points.

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Degree = Number of Control Points -1

Property-04:

The order of the polynomial defining the curve segment is equal to the total number of control points.

Order = Number of Control Points

Property-05:

- •Bezier curve exhibits the variation diminishing property.
- It means the curve do not oscillate about any straight line more often than the defining polygon.

Algorithm

The parametric equation of a bezier curve is-

$$P(t) = \sum_{i=0}^{n} B_{i} J_{n,i}(t)$$

Bezier Curve Equation

Here,

- t is any parameter where $0 \le t \le 1$
- P(t) = Any point lying on the bezier curve
- •Bi = ith control point of the bezier curve
- n = degree of the curve

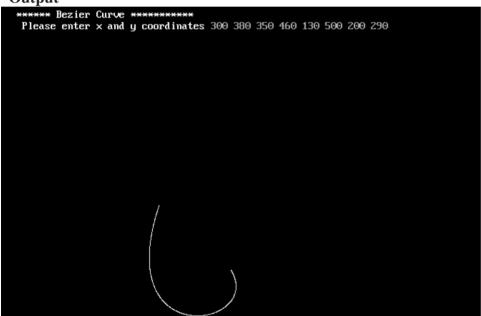
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```
• Jn,i(t) = Blending function = C(n,i)ti
(1-t)n-i where C(n,i) = n! / i!(n-i)!
Code
#include<graphics.h>
#include<math.h>
#include<conio.h>
#include<stdio.h>
void main()
{
int x[4],y[4],i;
double put_x,put_y,t;
int gr=DETECT,gm;
initgraph(&gr,&gm,"C:\\TURBOC3\\BGI");
printf("\n***** Bezier Curve *********);
printf("\n Please enter x and y coordinates ");
for(i=0;i<4;i++)
scanf("%d%d",&x[i],&y[i]);
putpixel(x[i],y[i],3); // Control Points
}
for(t=0.0; t <= 1.0; t = t + 0.001) // t always lies between 0 and 1
{
// Formula to draw curve
put_x = pow(1-t,3)*x[0] + 3*t*pow(1-t,2)*x[1] + 3*t*t*(1-t)*x[2] + pow(t,3)*x[3];
```

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```
put_y = pow(1-t,3)*y[0] + 3*t*pow(1-t,2)*y[1] + 3*t*t*(1-t)*y[2] + pow(t,3)*y[3];
putpixel(put_x,put_y, WHITE); // putting pixel
}
getch();
closegraph();
}
```

Output



Conclusion: LO1, mapped.