Team notebook

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```
//Batch Scheduling
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 100000007
#define IN freopen("nocross.in","r",stdin)
#define OUT freopen("nocross.out","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 200000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define LOG 19
#define off 2
using namespace __gnu_pbds;
using namespace std;
typedef tree< pair<int,int>, null_type, less< pair<int,int> >,
   rb_tree_tag, tree_order_statistics_node_update> ordered_set;
#define maxn 1000005
int dp[maxn] ;
int t[maxn] , f[maxn] ;
int n , s ;
```

```
int w( int i, int x )
   return ( t[x]-t[i]+s )*( f[n]-f[i] );
}
int main()
   scanf("%d %d",&n,&s);
   for(int i=1 ; i<=n ; i++)</pre>
       scanf("%d %d",&t[i],&f[i]);
      t[i] += t[i-1];
      f[i] += f[i-1];
   vector < pair<int,int> > vp ; // pos , best-k
   vp.pb( mp( 0 , 0 ) );
   for(int x=1 ; x<=n ; x++)</pre>
       int idx = upper_bound( vp.begin() , vp.end() , mp( x ,
          n+1 ) ) - vp.begin();
       idx--;
       dp[x] = dp[vp[idx].yy] + w(vp[idx].yy, x);
       while( (int)vp.size() > 0 )
          if( vp.back().xx > x && dp[x] + w(x, vp.back().xx)
              <= dp[ vp.back().yy ] + w( vp.back().yy ,</pre>
              vp.back().xx ) ) vp.pop_back();
           else break :
```

```
if( vp.size() == 0 ) vp.push_back( mp( 0 , x ) );
   else{
       int lo = max(vp.back().xx,x+1) , hi = n ;
       if( lo > hi || dp[ vp.back().yy ] + w( vp.back().yy ,
          hi) <= dp[x] + w(x, hi)) continue;
       while( lo < hi )</pre>
          int mid = (lo+hi)/2;
          if( dp[ vp.back().yy ] + w( vp.back().yy , mid )
              \leq dp[x] + w(x, mid)) lo = mid + 1;
          else hi = mid ;
       }
       vp.pb( mp( lo , x ) );
   }
}
printf("%d\n",dp[n]);
return 0;
```

2 BlockCutTree

```
//LOJ-1308 Ant Network
#include <bits/stdc++.h>
```

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 100000007LL
#define IN freopen("testing.txt","r",stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 1000000000000000000LL
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
using namespace __gnu_pbds;
using namespace std;
typedef pair<pair<i64, i64>,int> pi ;
typedef tree< pi, null_type, less<pi>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
#define maxn 100005
namespace BCT
    const int mx = 100005 ; // max( number of edge , number of
       node )
   bool isCutPoint[mx] ;
```

```
int low[mx] , pre[mx] , cnt2vcc , used[mx] , Timer = 0 ;
vector <int> biComp[mx] ;
int n , m ;
struct Edge{
   int v , id ;
};
vector <Edge> g[mx] ;
vector <int> bridges ; //for bridge
stack <int> stk ;
void init(int _n, int _m)
   n = _n ; m = _m ;
   for(int i=1; i<=max(n,m); i++) g[i].clear() ,</pre>
       biComp[i].clear();
   bridges.clear() ; // for bridge
}
void addEdge( int u, int v, int id )
{
   g[u].pb( {v,id} ); g[v].pb({u,id});
}
void dfs(int u , int par )
     printf("node-> %d par: %d edgeId: %d\n",u,par,edgeId) ;
   pre[u] = ++Timer ; low[u] = pre[u] ;
   int chCnt = 0 ;
   for(int i=0 ; i<g[u].size() ; i++)</pre>
       int edgeId = g[u][i].id ;
       if( used[ edgeId ] ) continue ;
```

```
used[ edgeId ] = true ;
   stk.push( edgeId ) ;
   int v = g[u][i].v ;
   if( pre[v] ==-1 )
      dfs( v , u );
      low[u] = min(low[u], low[v]);
      if( low[ v ] == pre[ v ] ) bridges.pb(edgeId) ;
      if( low[v] >= pre[u] )
      {
          cnt2vcc++ ;
          while( stk.size() > 0 ) //making component
          {
              biComp[cnt2vcc].pb( stk .top() );
              stk.pop();
              if( biComp[cnt2vcc].back()==edgeId ) break
          }
          if(par!=0) isCutPoint[u] = true ; //checking
              if non-root
      }
       chCnt++;
   else low[u] = min( low[u] , pre[v] );
if(chCnt > 1 && par==0) isCutPoint[u] = true ; //checking
   for root
return ;
```

```
}
   int find2VCC()
       int i , j ;
       Timer = 0;
       for(i=1 ; i<=m ; i++) used[i] = false ;</pre>
       for(i=1 ; i<=n ; i++)</pre>
           isCutPoint[i] = false ;
           pre[i] = -1;
       cnt2vcc = 0;
       for(i=1; i<=n; i++)</pre>
       {
           if( pre[i] == -1 ) dfs(i,0);
   }
}
struct Edge{
   int u , v , id ;
}edge[maxn];
int main()
{
   int i , j , k , l , m , n , t=1 , tc ;
   scanf("%d", &tc);
   while( t<=tc )</pre>
       scanf("%d %d",&n,&m);
       BCT::init(n,m);
```

```
for(i=1; i<=m ; i++)</pre>
   int u , v ;
   scanf("%d %d",&u,&v);
   u++ ; v++ ;
   edge[i] = \{u,v,i\};
   BCT::addEdge(u,v,i);
BCT::find2VCC();
int cntVcc = BCT::cnt2vcc ;
int ans1 ;
unsigned long long int ans2;
if( cntVcc==1 )
   ans1 = 2; ans2 = (n*(n-1))/2LL;
else{
   ans1 = 0 , ans2=1LL ;
   for(i=1; i<=cntVcc ; i++)</pre>
       set <int> nodes ;
       for(j=0; j<BCT::biComp[i].size(); j++)</pre>
           int id= BCT::biComp[i][j] ;
           nodes.insert( edge[id].u ) ; nodes.insert(
              edge[id].v);
       set<int> :: iterator it = nodes.begin() ;
       int artCnt = 0 ;
       while( it!=nodes.end() )
```

```
{
                  if( BCT::isCutPoint[*it] ) artCnt++ ;
                  it++ ;
              if( artCnt==1 )
                  ans1++ ;
                  ans2 *= (1LL*( (int)nodes.size() - artCnt )) ;
           }
       }
       printf("Case %d: %d %llu\n",t++,ans1,ans2);
         for(i=1; i<=n; i++)
 /*
           printf("%d-->%d\n",i,BCT::isCutPoint[i]);
       for(i=1; i<=cntVcc; i++)</pre>
           for(j=0; j<BCT::biComp[i].size(); j++ ) printf("%d</pre>
              ",BCT::biComp[i][j]);
          printf("\n") ;
*/
   }
   return 0 ;
}
14 17
1 2
1 3
2 3
```

```
3 4
4 6
5 6
3 5
6 7
6 8
7 8

9 10
9 11
9 12
11 12
10 13
13 14
10 14
*/
```

3 Blossom(randomized)

```
#include <bits/stdc++.h>
using namespace std;
const int N=510;
vector<int>to[N];
int lnk[N],vis[N],tim=0;
inline void ae(int u,int v){
        to[u].push_back(v);
}
bool dfs(int x){
        if(x==0)return true;
        vis[x]=tim;
        vector<int>::iterator it=to[x].begin(),ti=to[x].end();
        random_shuffle(it,ti);
        for(int u,v;it!=ti;it++){
```

```
u=*it,v=lnk[u];
               if(vis[v]<tim){</pre>
                       lnk[x]=u, lnk[u]=x, lnk[v]=0;
                       if(dfs(v))return true;
                       lnk[u]=v, lnk[v]=u, lnk[x]=0;
               }
       }
       return false;
int main(){
       int n,e,ans=0;
       scanf("%d%d",&n,&e);
       for(int u,v;e--;scanf("%d%d",&u,&v),ae(u,v),ae(v,u));
       srand(time(0));
       memset(lnk+1,0,n<<2);
       for(int tot=5;tot--;){
               for(int i=1;i<=n;i++){</pre>
                       if(!lnk[i]){
                              tim++,ans+=dfs(i);
               }
       }
       printf("%d\n",ans);
       for(int i=1;i<=n;i++){</pre>
               printf("%d ",lnk[i]);
       putchar('\n');
       return 0;
}
```

4 Blossom

```
const int MAXN = 2020 + 1;
```

```
struct GM // 1-based Vertex index
   int vis[MAXN], par[MAXN], orig[MAXN], match[MAXN],
       aux[MAXN], t, N;
   vector<int> conn[MAXN];
   queue<int> Q;
   void addEdge(int u, int v)
       conn[u].push_back(v);
       conn[v].push_back(u);
   void init(int n)
       N = n;
       t = 0;
       for(int i=0; i<=n; ++i)</pre>
           conn[i].clear();
           match[i] = aux[i] = par[i] = 0;
   }
   void augment(int u, int v)
       int pv = v, nv;
       do
           pv = par[v];
           nv = match[pv];
           match[v] = pv;
          match[pv] = v;
           v = nv;
       while(u != pv);
```

```
int lca(int v, int w)
{
   ++t;
   while(true)
       if(v)
       {
           if(aux[v] == t) return v;
           aux[v] = t;
           v = orig[par[match[v]]];
       swap(v, w);
   }
}
void blossom(int v, int w, int a)
{
   while(orig[v] != a)
       par[v] = w;
       w = match[v];
       if(vis[w] == 1) Q.push(w), vis[w] = 0;
       orig[v] = orig[w] = a;
       v = par[w];
bool bfs(int u)
{
   fill(vis+1, vis+1+N, -1);
   iota(orig + 1, orig + N + 1, 1);
   Q = queue<int> ();
   Q.push(u);
   vis[u] = 0;
   while(!Q.empty())
   {
```

```
int v = Q.front();
       Q.pop();
       for(int x: conn[v])
          if(vis[x] == -1)
              par[x] = v;
              vis[x] = 1;
              if(!match[x]) return augment(u, x), true;
              Q.push(match[x]);
              vis[match[x]] = 0;
          }
          else if(vis[x] == 0 && orig[v] != orig[x])
          {
              int a = lca(orig[v], orig[x]);
              blossom(x, v, a);
              blossom(v, x, a);
          }
       }
   return false;
int Match()
   int ans = 0;
   //find random matching (not necessary, constant
       improvement)
   vector<int> V(N-1);
   iota(V.begin(), V.end(), 1);
   shuffle(V.begin(), V.end(), mt19937(0x94949));
   for(auto x: V) if(!match[x])
          for(auto y: conn[x]) if(!match[y])
              {
                  match[x] = y, match[y] = x;
```

```
++ans;
break;
}

for(int i=1; i<=N; ++i) if(!match[i] && bfs(i)) ++ans;
return ans;
}
};</pre>
```

5 CHT Linear(example)

```
#include <bits/stdc++.h>
//#include <ext/pb_ds/assoc_container.hpp>
//#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define IN freopen("input.txt", "r", stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 1000000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
//using namespace __gnu_pbds;
```

```
using namespace std;
typedef pair<int, int> pi ;
//typedef tree< pi, null_type, less<pi>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
const i64 mod = 1000000007LL ;
#define maxn 200005
/*
    *os.find_by_order(k) -> returns the k'th smallest element
        (indexing starts from 0)
     os.order_of_key(v) -> returns how many elements are
         strictly smaller than v
*/
struct Line{
   i64 m , c , id ;
   i64 f(i64 x){ return x*m + c ; }
   i64 iSect( Line other ) {
        // floored division
        i64 = c - other.c, b = other.m - m;
              return a / b - ((a ^ b) < 0 && a % b);
   bool operator<(const Line& o)const{</pre>
       return mp(c,id) < mp(o.c,o.id) ;</pre>
};
//for minimization
// slope increasing , query point increasing
struct chtLinear{
```

```
deque <Line> dq ;
   void addLine( i64 m , i64 c , i64 id )
       if( !dq.empty() && m==dq.front().m ) dq[0] = min( dq[0] ,
          {m,c,id} );
       else dq.push_front( {m,c,id} );
      Line 1 = dq[0] ; dq.pop_front() ;
       while( (int)dq.size() >= 2 && 1.iSect(dq[0]) >
          dq[0].iSect(dq[1]) ) dq.pop_front();
       dq.push_front(1);
   pair<i64,i64> f(i64 x)
   {
       while((int)dq.size() > 1 && dq[0].f(x) >= dq[1].f(x))
          dq.pop_front();
      return mp( dq[0].id , dq[0].f(x) );
   }
}ch;
int main()
{
/*
   cout<<dq[0]<<" "<<dq[1]<<endl ;</pre>
   ch.addLine(1,-1,1);
   ch.addLine( -1, 1 , 2 );
   pair<11,11> p1 = ch.query(0) , p2 = ch.query(1) , p3 =
      ch.query(2);
   cout<<p1.xx<<" "<<p2.xx<<" "<<p3.xx<<endl ;</pre>
   cout<<p1.yy<<" "<<p2.yy<<" "<<p3.yy<<endl ;
*/
```

```
i64 n , m ;
scanf("%lld %lld",&n,&m);
ch.addLine(0,0,1);
i64 S = 0 , B = 0 , Sum = n ;
for(int i=1 ; i<=m ; i++)</pre>
   int q;
   scanf("%d",&q);
   if (q==1)
       S = 0 , B = 0 ;
       ch.dq.clear();
       ch.addLine(0,0,1);
       i64 a ;
       scanf("%lld",&a) ;
       Sum += a ;
   if(q==2)
       i64 a ;
       scanf("%11d",&a);
       ch.addLine((Sum), ( - B - Sum*S), Sum+1 );
       Sum += a ;
   if(q==3)
       i64 b, s;
       scanf("%lld %lld",&b,&s);
       B += b;
       S += s ;
```

```
}
    pair<i64,i64> p = ch.f(S) ;
    printf("%lld %lld\n",p.xx, p.yy + B) ;
}

return 0 ;
}
/*
5 100
3 4 5
2 1
*/
```

6 ConncetedComponentDP

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 1000000007I.I.
#define IN freopen("strings.in","r",stdin)
#define OUT freopen("strings.out","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
```

```
#define xx first
#define yy second
#define ln 17
#define off 2
using namespace __gnu_pbds;
using namespace std;
typedef pair<int, int> pi ;
typedef tree< pi, null_type, less<pi>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
i64 dp[102][32][12][12][2][2], M;
int a[102] ;
i64 f(int n ,int r , int k , int c , int st , int en )
   if( n==0 || c < 0 || st < 0 || en < 0 ) return 0;</pre>
   r = (r + a[n]*(2*c + st + en))%M;
// printf("%d %d %d %d %d %d \n",n,r,k,c,st,en);
   if( dp[n][r][k][c][st][en] != -1 ) return
       dp[n][r][k][c][st][en] ;
// int rem = r;
   i64 ans = f(n-1,r,k,c,st,en); /* it is not used */
   if( k==1 )
       if ( c==0 && (st||en) && r==0 ) ans++; /* if this is the
          last element to take
       then is should either connect st and en , or be the first
          element or last */
   }
   else{
```

```
if(st==0) ans += ( f( n-1, r , k-1 , c , 1 , en ) + f(
          n-1 , r , k-1 , c-1 , 1 , en )*c ); // this is
          starting element
      if(en==0) ans += (f(n-1,r,k-1,c,st,1) + f(
          n-1,r,k-1,c-1,st,1)*c); // this is ending element
       ans += f(n-1, r, k-1, c+1, st, en); // created &
          independent
      ans += f(n-1, r, k-1, c, st, en)*2*c +
          f(n-1,r,k-1,c,st,en)*(st+en); /* created and
          connected with some other component
      possibly start or end component */
      ans += (f(n-1, r, k-1, c-1, st, en)*c*(c-1) + f(
          n-1 , r , k-1 , c-1 , st, en )*c*(st+en) ) ;/* created
       and connected between two component */
   }
   return dp[n][r][k][c][st][en] = ans%mod ;
}
int main()
{
   int n , k ;
   scanf("%d %d %d",&n,&M,&k);
   for(int i=1; i<n; i++) scanf("%d",&a[i]);</pre>
   a[n] = 0:
   memset(dp,-1,sizeof(dp));
   i64 \text{ ans} = f(n, 0, k, 0, 0, 0);
```

```
ans = (ans%mod + mod)%mod;
printf("%lld\n",ans);
return 0;
}
```

7 DominatorTree

```
#include <bits/stdc++.h>
#define mp make_pair
#define pb push_back
#define xx first
#define yy second
#define i64 long long int
#define MEM(a,x) memset(a,x,sizeof(x))
#define INF 100000000
#define maxn 200005
using namespace std;
namespace DominatorTree{
Dominator Tree for General Graph ,Tr[u] stores all the
immediate children of node u (does not store the parent) in
the dominator tree. at first initialize with number of nodes.
then add edges(directed edges). call buildDominatorTree(r),
where r is the root. then just call dominator(u,v) to check
if v is u's dominator it returns false in case either u or v
is not connected to the root
```

```
*/
const int N = 202400;
vector <int> G[N] , pred[N] , dom[N] , Tr[N] ;
int old[N] , dfn[N] , up[N] , f[N] , semi[N] , g[N] , idom[N] ,
   cnt;
int n , m ;
int Time , st[N] , en[N] ;
void init(int _n) {
   for (int i = 0; i < N; i++) G[i].clear(), pred[i].clear()</pre>
       , dom[i].clear() , Tr[i].clear() ;
   memset (old , 0 , sizeof old) ;
   memset (dfn , 0 , sizeof dfn) ;
   memset (f , 0 , sizeof f);
   memset (up , 0 , sizeof up) ;
   memset (old , 0 , sizeof old) ;
   memset (g , 0 , sizeof g);
   memset (idom , 0 , sizeof idom) ;
   memset (st , -1 , sizeof st) ;
   memset (en , -1 , sizeof en) ;
   n = _n ;
   cnt = 0 ; Time = 0 ;
}
void addEdge(int u , int v){ return G[u].push_back(v) ; }
void dfs(int u){
       old[dfn[u]=++cnt] = u;
       semi[cnt] = g[cnt] = f[cnt] = cnt;
       for(int v : G[u]){
              if(!dfn[v]){
                      dfs(v);
                      up[dfn[v]] = dfn[u];
              }
              pred[dfn[v]].push_back(dfn[u]);
```

```
}
int ff(int x) {
       if(x == f[x]) return x;
       int y = ff(f[x]);
       if(semi[g[x]] > semi[g[f[x]]])
              g[x] = g[f[x]];
       return f[x] = y;
}
void dfs1(int u)
   Time++:
   st[u] = Time ;
   for(int i=0 ; i<Tr[u].size() ; i++)</pre>
       dfs1( Tr[u][i] ); //par is not stored in Tr[u]
   Time++;
   en[u] = Time ;
void buildDominatorTree(int r){
       dfs(r);
       for(int y = cnt ; y >= 2 ; y--){
              for(int z : pred[y]) {
                      ff(z):
                      semi[y]=min(semi[y],semi[g[z]]);
               dom[semi[y]].push_back(y);
              int x=f[y]=up[y];
              for(int z:dom[x]){
                      ff(z);
                      idom[z] = semi[g[z]] < x? g[z]:x;
```

```
dom[x].clear();
       }
       for(int y = 2; y \le cnt; ++y){
              if(idom[y]!=semi[y])
                      idom[y]=idom[idom[y]];
              dom[idom[y]].push_back(y);
       }
       idom[r] = 0;
       for (int i = 1 ; i <= n ; i++) {</pre>
       for (int j = 0 ; j < dom[i].size() ; j++) {</pre>
           Tr[old[i]].push_back(old[dom[i][j]]);
       }
       }
       dfs1(r);
   }
   bool dominator( int u,int v )
       //returns true if v is u's dominator
       if(st[u]==-1 || st[v]==-1) return false ;//if u or v is
           not connected to the root
       if( st[u] >= st[v] && st[u] <= en[v] ) return true ;</pre>
       return false;
   }
}
vector <int> g[maxn], e[maxn];
int dis[maxn] ;
void dijkstra(int n)
{
   int i, j, k, l, m;
   priority_queue < pair<int,int> > pq ;
   for(i=1; i<=n; i++) dis[i] = INF;</pre>
   dis[1] = 0;
   pq.push(mp(0,1));
```

```
while( !pq.empty() )
   ₹
       pair<int,int> p = pq.top() ;
       pq.pop();
       if( dis[p.yy] != -p.xx ) continue ;
       for(i=0 ; i<g[p.yy].size() ; i++)</pre>
       {
           int city = g[ p.yy ][i] ;
           if( dis[city] > -p.xx + e[ p.yy][i] )
               dis[city] = -p.xx + e[p.yy][i];
              pq.push( mp( -dis[city], city ) );
           }
       }
   }
   return ;
struct data
   int u, v, w;
} edge[maxn];
int main()
{
   int i, j, k, l, m, n, t=1, tc;
   scanf("%d", &tc);
   while(t<=tc)</pre>
       scanf("%d %d",&n,&m);
       for(i=1; i<=n; i++) g[i].clear(), e[i].clear();</pre>
```

```
for(i=1 ; i<=m ; i++)</pre>
         int u , v , w ;
         scanf("%d %d %d",&u,&v,&w);
         edge[i].u = u ; edge[i].v = v ; edge[i].w = w ;
         g[u].pb(v);
         e[u].pb(w);
     }
     dijkstra(n) ;
//
       for(i=1; i<=n; i++) printf("dis[%d]: %d\n",i,dis[i]);</pre>
     DominatorTree::init(n+m) ;
     for(i=1 ; i<=m ; i++)</pre>
         int u = edge[i].u , v = edge[i].v , w=edge[i].w ;
         if( dis[u] + w == dis[ v ] )
         {
            DominatorTree::addEdge(u,n+i) ;
            DominatorTree::addEdge(n+i,v) ;
         }
     DominatorTree::buildDominatorTree(1);
       for(i=1; i<=n+m ; i++)
         printf("%d:",i);
         for(j=0; j<dmt.Tr[i].size(); j++) printf("</pre>
            %d",dmt.Tr[i][j]);
         printf("\n") ;
     }
```

```
for(i=1; i<=n+m; i++) printf("st[%d]: %d en[%d]:
   %d\n",i,dmt.st[i],i,dmt.en[i]); */
long long int ans = OLL ;
for(i=1 ; i<=m ; i++)</pre>
{
   int u = edge[i].u, v = edge[i].v, w = edge[i].w ;
   long long int a, b;
   if( dis[u] == dis[v] )
       if(w==0)
       {
          b = 0;
          if( DominatorTree::dominator(v,n+i) )
              a = 0;
          else a = -1;
       }
       else
          a = -1;
          b = w;
       }
   }
   else
       if( dis[u] + w == dis[v] )
          b = 0;
          if( DominatorTree::dominator(v,n+i) ) a = 0 ;
```

```
else a = -1;
}
else
{
    a = -1;
    b = dis[u] + w - dis[v];
}

ans += (i64)i*a + (i64)i*(i64)i*b;

// printf("%d %lld %lld\n",i,a,b);
}
printf("Case %d: %lld\n",t++,ans);
}

return 0;
```

8 EulerPath

```
#include <bits/stdc++.h>

//#include <ext/pb_ds/assoc_container.hpp>
//#include <ext/pb_ds/tree_policy.hpp>

#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define IN freopen("testing.txt","r",stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a; i<=b; i++)</pre>
```

```
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
//using namespace __gnu_pbds;
using namespace std;
typedef pair<int, int> pi ;
//typedef tree< pi, null_type, less<pi>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
const i64 mod = 1000000007LL ;
#define maxn 500005
/*
    *os.find_by_order(k) -> returns the k'th smallest element
        (indexing starts from 0)
     os.order_of_key(v) -> returns how many elements are
         strictly smaller than v
*/
int c[maxn] , d[maxn] ;
map< int , multiset<int> > g ;
map <int,int> vis ;
void dfs1(int u)
```

```
vis[u] = 1;
   for( auto v : g[u] ) if( vis.find(v) == vis.end() ) dfs1(v) ;
}
///-----Euler path printing-----///
//just call dfs2 with the node you want to start your path
//at first you need to make sure, the graph is connected and
   euler path exist
vector <int> ans ;
void dfs2(int u)
   while( (int)g[u].size() !=0 )
       int v = *g[u].begin() ;
       g[u].erase( g[u].find(v) );
       g[v].erase( g[v].find(u) );
       dfs2(v);
   ans.pb(u);
}
///----Euler path printing-----///
int main()
   int n;
   scanf("%d",&n);
   for(int i=1; i<n; i++) scanf("%d",&c[i]);</pre>
   for(int i=1; i<n; i++) scanf("%d",&d[i]);</pre>
   for(int i=1 ; i<n ; i++)</pre>
   {
       if( c[i] > d[i] )
```

```
{
       printf("-1\n");
       return 0 ;
   g[ c[i] ].insert( d[i] );
   g[ d[i] ].insert( c[i] );
}
int src = c[1], cnt = 0;
for( auto it : g )
   if( (int)it.second.size() & 1 )
       cnt++;
       src = it.first ;
}
dfs1( src );
if( vis.size() != g.size() || ( cnt!=0 && cnt!=2 ) )
   printf("-1\n");
   return 0 ;
//call for printing euler path
dfs2(src);
for(int i=0 ; i<ans.size() ; i++)</pre>
   printf("%d",ans[i]);
   if( i == (int)ans.size() - 1) printf("\n");
   else printf(" ");
```

```
return 0 ;
}
```

9 Four Divisor Trick

```
/*
Let S(v,m) be the count of integers in the range 2..v that
   remain after sieving with all primes smaller
or equal than m. That is S(v,m) is the count of integers up to v
   that
are either prime or the product of primes larger than m.
S(v, p) is equal to S(v, p-1) if p is not prime or v is smaller
   than p2. Otherwise (p prime, p2<=v) S(v,p)
can be computed from S(v,p-1) by finding the count of integers
   that are removed while sieving with p.
An integer is removed in this step if it is the product of p
   with another integer that has no
divisor smaller than p. This can be expressed as
S(v,p) = S(v, p1)
                  (S(v/p, p1) S(p1, p1)).
During computation of S(N,p) it is sufficient to compute S(v,p)
   for all positive integers v that
are representable as floor(N/k) for some integer k and all p
   v1/2.
NOTE: Pi(N) = S(N,N). When you call S(N,N) it will need to
   compute S(N/k, N/k) in its lower substate.
Hence you can have all required values of Pi(N/k).
```

```
In my code DSUM(N,P) do the job of calculating S(N,P).
I used two arrays H[] and L[] for storing the values of S(N/k,p)
   in H[k] for k \le N1/2 and
for k \ge N^(1/2) I stored the values of S(N/k,p) in L[N/k].
For computation I started with p=2 and changed the values of all
   the state which is going to
be affected by this particular prime. Continue doing this for
   all prime till N1/2 and
at the end for k \le N1/2, H[k] will contain the values of Pi(N/k)
   and L[k] will contain the values of Pi(k).
PS: My complexity is O(N3/4).
*/
#include <bits/stdc++.h>
#define PI (acos(-1.0))
#define DBG printf("Hi\n")
#define loop(i,n) for(i =1; i<=n; i++)</pre>
#define mp make_pair
#define pb push_back
#define mod 998244353LL
#define INF 100000000
#define xx first
#define yy second
#define sq(x) ((x)*(x))
#define eps 0.000000001
#define i64 long long int
#define ui64 unsigned long long int
using namespace std;
#define maxn 1000000
```

```
i64 Lo[maxn+5] , Hi[maxn+5] ;
void primeCount( i64 N )
   i64 i , j , k , l , m ;
   i64 s = sqrt(N+0.0) + 1;
   for(i=1; i<=s; i++) Lo[i] = i-1;</pre>
   for(i=1; i<=s; i++) Hi[i] = (N/i) - 1;</pre>
   for(i=2 ; i<=s ; i++)</pre>
       if( Lo[i] == Lo[i-1] ) continue ;
       i64 isq = i*i , lim = N/isq ;
       // we need , ( N/j ) >= i*i
       // => j <= ( N/(i*i) )
       for( j=1 ; j<=lim && j<=s ; j++ )</pre>
          if(i*j>s) Hi[j] = Hi[j] - (Lo[N/(i*j)] - Lo[i-1]
              );
          else Hi[j] = Hi[j] - ( Hi[i*j] - Lo[i-1] );
       }
       // j >= i*i
       for( j=s ; j>=isq ; j-- )
          Lo[j] = Lo[j] - (Lo[j/i] - Lo[i-1]);
       }
   }
   return ;
```

```
int main()
{
   i64 i , j , k , l , m , n ;
   scanf("%lld",&n);
   primeCount(n);
   i64 \text{ ans} = OLL;
   for(i=2 ; (i*i*i)<=n ; i++)</pre>
       if( Lo[i]!=Lo[i-1] ) ans++;
   }
   for(i=2 ; i*i <=n ; i++)</pre>
       if( Lo[i] == Lo[i-1] ) continue ;
       ans += (Hi[i] - Lo[i]);
   printf("%lld\n",ans );
   return 0 ;
```

10 HLD

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
```

```
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define IN freopen("transposition-115.txt","r",stdin)
#define OUT freopen("dichromatic.out", "w", stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 200000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define sq(x) ((x)*(x))
using namespace __gnu_pbds;
using namespace std;
#define maxn (1<<18)+5
#define mod 100000007LL
typedef pair<i64,i64> pii ;
typedef long long int T;
struct edge{
   int u , v , c , id ;
   bool operator<(const edge other)const{ return c < other.c ; }</pre>
};
namespace MST{
   int par[maxn] ;
   int findPar(int u)
```

```
if( par[u] != u ) return par[u] = findPar( par[u] );
       return u ;
   }
   void findMST( int n , vector < edge > &e )
       //after this function , e[0] to e[n-2] will contain the
           treeEdges
       //and other would be non-tree Edges
       sort( e.begin() , e.end() ) ;
       for(int i=1 ; i<=n ; i++) par[i] = i ;</pre>
       vector <edge> treeEdge , otherEdge ;
       for(int i=0 ; i < e.size() ; i++ )</pre>
           int u = e[i].u , v = e[i].v ;
           int pu = findPar(u) , pv = findPar(v) ;
           if( pu==pv ) otherEdge.pb(e[i]) ;
           else{
              par[pu] = pv ;
              treeEdge.pb(e[i]);
           }
       e.clear();
       for(int i=0 ; i<treeEdge.size() ; i++) e.pb( treeEdge[i]</pre>
           ) :
       for(int i=0 ; i<otherEdge.size() ; i++) e.pb(</pre>
           otherEdge[i] );
   }
int tr[2*maxn] , lazy[2*maxn] , ara[maxn] ;
```

```
void relax(int cn, int b, int e)
{
   tr[cn] = min( tr[cn] , lazy[cn] );
   if( b!=e )
   {
       int lc = cn<<1 , rc = lc+1 , m = (b+e)>>1 ;
       lazy[lc] = min( lazy[cn] , lazy[lc] );
       lazy[rc] = min( lazy[cn] , lazy[rc] );
   lazy[cn] = INF ;
void update(int cn, int b , int e, int l, int r,int val)
{
   if( lazy[cn] != INF ) relax(cn,b,e) ;
   if( e < 1 || b > r ) return ;
   if( 1<=b && e<=r )</pre>
       lazy[cn] = val;
       relax(cn,b,e);
       return :
   }
   int lc = cn << 1, rc = lc + 1, m = (b + e) >> 1;
   update(lc,b,m,l,r,val) ; update(rc,m+1,e,l,r,val) ;
   tr[cn] = max(tr[lc],tr[rc]) ;
}
int query(int cn, int b, int e, int l, int r)
{
   if(lazy[cn]!= INF ) relax(cn,b,e);
   if( e < 1 || b > r ) return -INF;
   if( l<=b && e<=r ) return tr[cn] ;</pre>
   int lc = cn<<1 , rc = lc+1 , m = (b+e)>>1 ;
   return max( query(lc,b,m,l,r) , query(rc,m+1,e,l,r) );
```

```
void build(int cn, int b, int e)
   lazy[cn] = INF;
   if( b==e )
       tr[cn] = ara[b] ;
       return :
   int lc = cn << 1, rc = lc + 1, m = (b + e) >> 1;
   build(lc,b,m); build(rc,m+1,e);
   tr[cn] = max(tr[lc], tr[rc]);
namespace hld{
   int in[maxn] , out[maxn] , sub[maxn] , t = 1 , nxt[maxn] ,
       depth[maxn], par[maxn], n;
   vector <int> g[maxn] ;
   void init(int _n)
       n = _n ;
       for(int i=0; i<=n; i++) g[i].clear();</pre>
   void addEdge(int u, int v)
       g[u].pb(v);
       g[v].pb(u);
   void dfsSZ(int u)
       sub[u] = 1;
       for(int i=0 ; i<g[u].size() ; i++)</pre>
```

```
{
       int v = g[u][i] ;
       for(int j=0 ; j<g[v].size() ; j++)</pre>
           if( g[v][j] == u )
               g[v].erase( g[v].begin() + j );
              break :
       }
       dfsSZ(v) ;
       sub[u] += sub[v];
       if( sub[v] > sub[ g[u][0] ] ) swap( g[u][0] , g[u][i]
          );
   }
}
void dfsHLD(int u)
   in[u] = ++t;
   for(int i=0 ; i<g[u].size() ; i++)</pre>
   {
       int v = g[u][i] ;
       par[v] = u;
       depth[v] = depth[u] + 1;
       if( i==0 ) nxt[v] = nxt[u] ;
       else nxt[v] = v ;
       dfsHLD(v) ;
   }
   out[u] = t;
}
void preprocess(int root)
```

```
dfsSZ(root) ;
   t = 0 ; nxt[root] = root ;
   depth[root] = 1 ;
   dfsHLD(root) ;
}
int hldQuery( int u , int v )
{
   int ans = -INF ;
   while( nxt[u] != nxt[v] )
       if( depth[ nxt[u] ] < depth[ nxt[v] ] )</pre>
          ans = max(ans, query(1,1,n, in[nxt[v]], in[v]
              ));
          // do you thing here ( from in[v] to in[ nxt[v] ] )
          v = par[nxt[v]];
       }
       else{
           ans = max(ans, query(1,1,n, in[nxt[u]], in[u]
              ));
          // do your thing here ( from in[u] to in[ nxt[u] ]
              )
          u = par[ nxt[u] ] ;
       }
   int lc ;
   if( depth[u] > depth[v] ) swap(u,v) ;
   1c = u;
   //here lc is the lca
   //if you are working on node , not on edge, then
       update/query upto u also
   //otherwise update/query from in[u]+1 to in[v]
```

```
ans = \max( ans , query(1,1,n,in[u]+1,in[v]) );
   return ans ;
}
void hldUpdate( int u , int v , int val )
{
   while( nxt[u] != nxt[v] )
       if( depth[ nxt[u] ] < depth[ nxt[v] ] )</pre>
           update(1,1,n,in[ nxt[v] ] , in[v] , val );
           // do you thing here ( from in[v] to in[ nxt[v] ] )
           v = par[ nxt[v] ] ;
       else{
           update(1,1,n,in[ nxt[u] ] , in[u] , val );
           // do your thing here ( from in[u] to in[ nxt[u] ]
           u = par[ nxt[u] ] ;
   }
   int lc ;
   if( depth[u] > depth[v] ) swap(u,v);
   1c = u;
   //here lc is the lca
   //if you are working on node , not on edge, then
       update/query upto u also
   //otherwise update/query from in[u]+1 to in[v]
   update(1,1,n,in[u]+1,in[v],val);
   return ;
}
```

```
}
int ans[maxn] ;
int main()
₹
    int n , m ;
   vector < edge > e ;
   scanf("%d %d",&n,&m);
   for( int i=1 ; i<=m ; i++ )</pre>
   {
       int u ,v , c ;
       scanf("%d %d %d",&u,&v,&c);
       e.pb( {u,v,c,i} );
   }
   MST::findMST( n , e ) ;
   hld::init(n);
   for(int i=0 ; i<n-1 ; i++)</pre>
       hld::addEdge( e[i].u , e[i].v );
   }
   hld::preprocess(1);
   for(int i=0 ; i<n-1 ; i++)</pre>
       int u = e[i].u , v = e[i].v , c= e[i].c ;
```

```
if( hld::depth[u] > hld::depth[v] ) swap(u,v) ;
   ara[ hld::in[v] ] = e[i].c ;
}
ara[ hld::in[1] ] = INF ;
build(1,1,n);
for(int i=n-1; i<m; i++)</pre>
   int u = e[i].u , v = e[i].v , c= e[i].c ;
   ans[e[i].id] = hld::hldQuery(u,v) - 1;
}
for(int i=1; i<=n; i++) ara[i] = INF;</pre>
build(1,1,n);
for(int i=n-1 ; i<m ; i++)</pre>
{
   int u = e[i].u , v = e[i].v , c= e[i].c ;
   hld::hldUpdate(u,v,c);
}
for(int i=0 ; i<n-1 ; i++)</pre>
   int u = e[i].u , v = e[i].v , c= e[i].c ;
   int res = hld::hldQuery(u,v);
   if(res==INF) ans [e[i].id] = -1;
   else ans[ e[i].id ] = res-1 ;
}
for(int i=1; i<=m; i++) printf("%d ",ans[i]);</pre>
printf("\n") ;
```

```
return 0 ;
}
```

11 Matching(kuhn)+VertexCover

```
#include <bits/stdc++.h>
#define pf printf
#define sf scanf
#define INF 100000000000000001LL
#define PI (acos(-1.0))
#define DBG printf("Hi\n")
#define loop(i,n) for(i =1; i<=n; i++)</pre>
#define mp make_pair
#define pb push_back
#define mod 100000007
#define maxn 100005
#define ff first
#define ss second
#define sq(x) ((x)*(x))
#define eps 0.000000001
#define i64 long long int
#define ui64 unsigned long long int
using namespace std;
int pairs[2005] ;
bool vis[2005] ;
vector <int> g[2005] , g1[2005] ;
bool dfs1(int u)
   if(vis[u]) return false;
   vis[u] = true ;
```

```
for(int i = 0 ; i<g[u].size() ; i++)</pre>
       int v = g[u][i] ;
       if( pairs[v] == -1 || dfs1(pairs[v]) ){
           pairs[v] = u ;
          pairs[u] = v ;
            printf("printing from dfs %d %d\n",u,v);
           return true ;
       }
   }
   return false;
}
int kuhn(int r, int c)
{
   memset(pairs,-1,sizeof(pairs));
   int ret = 0 ;
   for(int i=1 ; i<=r ; i++)</pre>
       memset( vis , 0 , sizeof(vis) );
       if(dfs1(i)) ret++ ;
   return ret ;
}
void dfs2(int u)
   if(vis[u]) return ;
   vis[u] = 1;
   for(int i=0; i<g1[u].size(); i++) dfs2(g1[u][i]);</pre>
   return ;
```

```
int main()
{
   int i , j , k , l , m , n , r , c , u , v , ans ;
   while( sf("%d %d %d",&r,&c,&n) )
       if(r==0 &&c==0 && n==0) break ;
       for(i=1 ; i<=n ; i++)</pre>
          sf("%d %d",&u,&v);
          g[u].pb(v+r);
          g[v+r].pb(u);
       ans = kuhn(r,c);
   // for(i=1; i<=r; i++) pf("%d %d\n",i,pairs[i]-r);
    // for(i=r+1; i<=r+c; i++) pf("%d %d\n",i-r,pairs[i]);
       for(i=1 ; i<=r ; i++)</pre>
          for(j=0; j<g[i].size(); j++)</pre>
              if( pairs[i] == g[i][j] ) g1[ g[i][j] ].pb(i) ;
              else g1[i].pb( g[i][j] );
          }
       memset(vis,0,sizeof(vis));
       for( i=1 ; i<=r ; i++ )</pre>
```

```
if( pairs[i] == -1 ) dfs2(i) ;
   }
   pf("%d",ans);
   for(i=1 ; i<=r+c ; i++)</pre>
   {
       if( pairs[i]!=-1 )
           if( i<=r && !vis[i] ) pf(" r%d",i) ;</pre>
           else if( i>r && vis[i] ) pf(" c%d",i-r) ;
   }
   pf("\n");
   for(i=1 ; i<=r+c ; i++){</pre>
       g[i].clear();
       g1[i].clear();
   }
}
return 0 ;
```

12 PointsInRectangle

```
/*
Add a point , and add a rectangle .
After each addition answer how many (rectangle,point) pair
   exists such that point is in rectangle.
*/
#include <bits/stdc++.h>
```

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 100000007LL
#define IN freopen("C.in", "r", stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
using namespace __gnu_pbds;
using namespace std;
typedef pair<int, int> pii ;
typedef tree< pii, null_type, less<pii>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
#define maxn 300005
/*
    *os.find_by_order(k) -> returns the k'th smallest element
        (indexing starts from 0)
```

```
os.order_of_key(v) -> returns how many elements are
         strictly smaller than v
*/
ordered_set os[maxn] ;
struct DataStructure
public:
   ordered_set os[maxn] ;
   int mxX , cur = 0 ;
   void init( int _mxX )
       mxX = _mxX;
       for(int i=1; i<=mxX; i++) os[i].clear();</pre>
       cur = 0:
   }
   void add(int x ,int y)
   {
       cur++ :
       pii element = mp( y, cur ) ;
       while( x<= mxX )</pre>
           os[x].insert( element ) ;
          x += (x&(-x)) ;
       }
   }
   int query( int x ,int y )
       int sum = 0;
       pii element = mp( y, cur+1 ) ;
       while( x>0 )
           sum += os[x].order_of_key(element) ;
           x = (x&(-x));
       }
       return sum ;
```

```
}
};
struct Rectangle{
   int x1 , y1 , x2, y2 ;
}rect[maxn]:
struct Point
    int x, y;
}point[maxn];
set<int> xSet , ySet ;
map<int,int> xMap, yMap ;
int qType[maxn] ;
int main()
{
   int i , j , k , l , m , n , t ;
   scanf("%d",&n);
   int cntPoint = 0 , cntRect = 0 ;
   for(i=1 ; i<=n ; i++)</pre>
       scanf("%d",&t);
       qType[i] = t;
       if(t==1)
           cntPoint++ ;
           scanf("%d %d",&point[cntPoint].x,&point[cntPoint].y);
           xSet.insert( point[cntPoint].x );
           ySet.insert( point[cntPoint].y );
       else{
           cntRect++ ;
```

```
scanf("%d %d %d %d",&rect[cntRect].x1,
           &rect[cntRect].y1, &rect[cntRect].x2,
           &rect[cntRect].y2);
       xSet.insert(rect[cntRect].x1 );
           xSet.insert(rect[cntRect].x2);
       ySet.insert(rect[cntRect].y1 );
          ySet.insert(rect[cntRect].y2);
   }
}
set<int> :: iterator it ;
it = xSet.begin();
int mxX = 0:
while( it!=xSet.end() )
   xMap[*it] = ++mxX;
   it++ ;
it = ySet.begin();
int mxY = 0;
while( it!=ySet.end() )
   yMap[*it] = ++mxY;
   it++ ;
}
for(i=1 ; i<=cntPoint ; i++)</pre>
{
   point[i].x = xMap[point[i].x]; point[i].y =
       yMap[point[i].y] ;
for(i=1 ; i<=cntRect ; i++)</pre>
   rect[i].x1 = xMap[rect[i].x1] ; rect[i].x2 =
       xMap[rect[i].x2] ;
```

```
rect[i].y1 = yMap[rect[i].y1] ; rect[i].y2 =
       yMap[rect[i].y2] ;
}
DataStructure pt , r1, r2 ;
pt.init(mxX+2); r1.init(mxX+2); r2.init(mxX+2);
cntRect = 0 ; cntPoint = 0 ;
i64 \text{ ans} = OLL;
for(i=1 ; i<=n ; i++)</pre>
{
   t = qType[i] ;
   if( t==1 )
       cntPoint++ ;
       int x = point[cntPoint].x , y = point[cntPoint].y ;
   // printf("%d %d\n",x,y);
       ans += r1.query(x, y) - r2.query(x, y);
       pt.add( x, y );
   }
   else{
       cntRect++ ;
       int x1 = rect[cntRect].x1 , x2=rect[cntRect].x2 ,
          y1=rect[cntRect].y1 , y2=rect[cntRect].y2 ;
 // printf("%d %d %d \n",x1,y1,x2,y2);
       ans += pt.query(x2,y2)-pt.query(x1-1,y2) -
          pt.query(x2,y1-1)+pt.query(x1-1,y1-1);
       r1.add( x1,y1 ); r1.add( x2+1,y2+1 );
       r2.add(x1,y2+1); r2.add(x2+1,y1);
   printf("%lld\n",ans);
```

```
return 0;

/*

7
1 5 5
1 5 5
1 5 5
2 2 2 9 9
2 1 1 5 5
2 1 1 2 2
1 2 2
*/
```

13 SOS(on the fly)

```
public class TestProctoring {
   public double expectedTime(int[] p, int[] q) {
       int n = p.length;
       double[] prob = new double[n];
       for (int i = 0; i < n; i++) {</pre>
           prob[i] = p[i] * 1.0 / q[i];
       }
       double[][] t = new double[n+1][1<<n];</pre>
       double[] dp = new double[1<<n];</pre>
      /* t[i][mask] is sum of all submask of mask where
      difference of mask and submask is before i'th bit( 0 based
          ) , that means
      difference can be in 0 to i-1 th bit
      t[0] [mask] contains nothing other than just value of this
          mask
      t[n][mask] contains result of all submask of this mask
```

```
*/
for (int mask = 1; mask < 1 << n; mask++) {</pre>
   double fail = 1;
   double mult = 1;
   double am = 1;
   for (int j = 0; j < n; j++) { t[j+1][mask] =
       t[j][mask]; if (((mask>>j)&1) == 1) {
           t[j+1][mask] += t[j][mask^(1<<j)];
           fail *= (1 - prob[j]);
           mult *= prob[j];
           am *= (1 - prob[j]) / prob[j];
       }
   }
   dp[mask] = (1 + mult * t[n][mask]) / (1 - fail);
   for (int j = 0; j <= n; j++) {</pre>
       t[j][mask] += dp[mask] * am;
   }
return dp[(1<<n)-1];</pre>
```

14 SmallToLarge(nlogn)

```
#include <bits/stdc++.h>
// #include <ext/pb_ds/assoc_container.hpp>/
// #include <ext/pb_ds/tree_policy.hpp>
#define pb push_back
#define mp make_pair
#define mod 998244353LL
```

```
#define IN freopen("input.txt","r",stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG printf("Hi\n")
#define INF 1000000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
#define SZ(z) ((int)z.size())
#define sq(x) ((x)*(x))
#define FastIO ios_base::sync_with_stdio(false); cin.tie(NULL)
#define EPS 1e-7
// using namespace __gnu_pbds;
using namespace std;
// typedef tree< i64, null_type, less<i64>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
typedef pair<i64, i64> pii;
#define maxn 500005
#define alpha 22
int ans[maxn] ;
int lenOff[maxn] , mask[maxn] ;
int len[(1<<alpha)+2] ;</pre>
int sub[maxn] ;
vector <int> g[maxn] , e[maxn] ;
```

```
void Add(int u , int root , int curMask, int 1)
   len[ (curMask^mask[root]) ] = max( len[ (curMask^mask[root])
       ] , l-lenOff[root] );
   for(int i=0 ; i<g[u].size() ; i++)</pre>
   {
       int v = g[u][i];
       Add( v , root , (curMask^(1<<e[u][i])) , l+1 ) ;
}
void Remove(int u , int root , int curMask, int 1)
₹
   len[ (curMask^mask[root]) ] = -INF ;
   for(int i=0 ; i<g[u].size() ; i++)</pre>
       int v = g[u][i];
       Remove( v , root , (curMask^(1<<e[u][i])) , l+1 );</pre>
}
void addAnswer(int u , int root , int curMask, int 1)
   ans[root] = max( ans[root] , len[ (curMask^mask[root]) ] +
       lenOff[root] + 1 ) :
   for(int i=0 ; i<alpha ; i++)</pre>
       int m = (curMask^(1 << i)) :
       ans[root] = max( ans[root] , len[ m^mask[root] ] +
           lenOff[root] + 1 );
   }
```

```
for(int i=0 ; i<g[u].size() ; i++)</pre>
   {
       int v = g[u][i];
       addAnswer( v , root , (curMask^(1<<e[u][i])) , l+1 );
   }
}
void dfs(int u, bool keep)
{
   bool hasChild = ( (int)g[u].size() > 0 );
   for(int i=1; i<g[u].size(); i++)</pre>
   {
       dfs(g[u][i],0);
   }
   if( hasChild )
       int bigChild = g[u][0] ;
       dfs( bigChild , 1) ;
      mask[u] = (mask[bigChild]^( 1<<e[u][0] ));
      lenOff[u] = lenOff[ bigChild ] + 1;
   }
   len[ mask[u] ] = max( len[ mask[u] ] , -lenOff[u] ) ;
   for(int i=1; i<g[u].size(); i++)</pre>
   {
       addAnswer( g[u][i] , u , (1<<e[u][i]) , 1 );
       Add(g[u][i], u, (1<<e[u][i]), 1);
   }
   ans[u] = max(ans[u], 0);
   ans[u] = max(ans[u], len[mask[u]] + lenOff[u]);
```

```
for(int i=0 ; i<alpha ; i++)</pre>
       ans[u] = max(ans[u], len[(mask[u]^(1<<i))] +
           lenOff[u] );
   }
   for(auto v:g[u]) ans[u] = max( ans[u] , ans[v] );
   if ( keep == 0 ) Remove(u,u,0,0);
void dfsSize(int u )
{
    sub[u] = 1;
   for( int i=0 ; i<g[u].size() ; i++ )</pre>
       int v = g[u][i] ;
       dfsSize(v) ;
       sub[u] += sub[v];
       if( sub[v] > sub[ g[u][0] ] )
           swap( g[u][0] , g[u][i] );
           swap( e[u][0] , e[u][i] );
}
int main()
{
   int n;
   scanf("%d",&n);
   for(int i=2 ; i<=n ; i++)</pre>
       int p ;
```

```
char s[4];
    scanf("%d %s",&p,s);
    g[p].pb(i); e[p].pb( s[0]-'a');
}

for(int i=0; i<(1<<alpha); i++) len[i] = -INF;

dfsSize(1);
dfs(1,1);

for(int i=1; i<=n; i++)
{
    printf("%d ",ans[i]);
}
printf("\n");

return 0;</pre>
```

15 SuffixAutomata(short)

```
/*
https://www.spoj.com/problems/STRSOCU/
given two strings s,t and an integer k, how many distinct
    substrings of s occurs exactly k times in t ?
O(n) solution
*/
#include <bits/stdc++.h>

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
```

```
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 100000007LL
#define IN freopen("C.in","r",stdin)
#define OUT freopen("output.txt","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
using namespace __gnu_pbds;
using namespace std;
typedef pair<int, int> pi ;
typedef tree< pi, null_type, less<pi>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
#define maxn 100005
/*
    *os.find_by_order(k) -> returns the k'th smallest element
        (indexing starts from 0)
     os.order_of_key(v) -> returns how many elements are
         strictly smaller than v
class SuffixAutomaton{
public:
    struct state{
```

```
int edge[27] , len , link , cnt ;
};
state *st;
int sz , last , alpha = 26 ;
SuffixAutomaton( string &s )
   int l = s.length();
   int i , j ;
   st = new state[1*2];
   st[0].link = -1 ; st[0].len = 0 ; st[0].cnt = 0 ; sz = 1
       : last = 0 :
   for(i=0 ; i<alpha ; i++) st[0].edge[i] = -1 ;</pre>
   for(i=0 ; i<l ; i++)</pre>
       int cur = sz++ ;
       for(j=0; j<alpha; j++) st[cur].edge[j] = -1;</pre>
       st[cur].len = st[last].len+1; st[cur].cnt = 1;
       int p = last, c = s[i] - a';
       while( p!=-1 && st[p].edge[c] == -1 )
           st[p].edge[c] = cur;
           p = st[p].link;
       }
       if(p == -1)
           st[cur].link = 0;
```

```
else
        {
            int q = st[p].edge[c] ;
            if( st[p].len+1 == st[ q ].len ) st[cur].link = q ;
            else{
               int clone = sz++ ;
               for(j=0; j<alpha; j++) st[clone].edge[j] =</pre>
                   st[a].edge[i];
               st[clone].len = st[p].len+1;
               st[clone].link = st[q].link;
               st[clone].cnt = 0;
               while( p!=-1 && st[p].edge[c] == q )
               ₹
                   st[p].edge[c] = clone;
                   p = st[p].link ;
               st[q].link = st[cur].link = clone;
           }
        }
        last = cur ;
    vector <pi> vp ;
    for(i=0; i<sz; i++) vp.pb( mp( st[i].len , i ) );</pre>
    sort(vp.begin(), vp.end());
    for( i=sz-1 ; i>0 ; i-- )
        int state = vp[i].yy ;
        st[st[ state].link].cnt += st[ state].cnt ;
//
         printf("%d %d\n",st[state].cnt[0],st[state].cnt[1])
 }
```

```
int f( string t )
       int len = (int)t.size();
       t = t+t;
       t.pop_back() ;
       int cur = 0 , myLen = 0 ;
       vector <int> vis ;
       for(int i=0 ; i<t.size() ; i++)</pre>
           int ch = t[i] - 'a';
           while( st[ cur ].edge[ch] == -1 && st[cur].link!=-1 )
              cur = st[cur].link ;
              myLen = st[cur].len ;
           if( st[cur].edge[ch]!=-1 ) cur = st[cur].edge[ch] ,
              myLen++ ;
           while( cur!=0 && st[ st[cur].link ].len >= len )
           ₹
              cur = st[cur].link ;
              myLen = st[cur].len ;
           if( cur !=0 && myLen >= len ) vis.pb( cur );
            if( myLen >= len && st[cur].len >= len ) cout<<i<<"</pre>
//
   "<<st[cur].cnt<<endl :
       sort( vis.begin() , vis.end() );
       int ans = 0;
```

```
for( int i=0 ; i<vis.size() ; i++ )</pre>
           int cur = vis[i] ;
           if( i > 0 && vis[i]==vis[i-1] ) continue ;
           if( st[cur].len >= len && st[ st[cur].link ].len <</pre>
               len ) ans += st[cur].cnt ;
        return ans ;
    ~SuffixAutomaton()
       delete []st ;
   }
};
int main()
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    string s , t ;
    cin>>s ;
    int m;
    cin>>m ;
    SuffixAutomaton sa(s);
   for(int i=1 ; i<=m ; i++)</pre>
        cin>>t ;
       cout << sa.f(t) << "\n";
```

```
return 0;
}
```

16 Weighted Blossoms

```
//from facelessman&vfleaking
 #include<bits/stdc++.h>
 #define cin kin
#define DIST(e) (lab[e.u]+lab[e.v]-g[e.u][e.v].w*2)
using namespace std;
typedef long long 11;
 const int N=1023, INF=1e9;
 struct Edge
 {
                                             int u, v, w;
} g[N][N];
 int
                      \texttt{n,m,n_x,lab[N],match[N],slack[N],st[N],pa[N],flower\_from[N][N],S[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{vis}[N],\check{v
vector<int> flower[N];
deque<int> q;
void update_slack(int u,int x)
{
                                           if(!slack[x]||DIST(g[u][x])<DIST(g[slack[x]][x]))slack[x]=u;</pre>
void set_slack(int x)
                                            slack[x]=0;
                                           for(int u=1; u<=n; ++u)</pre>
                                                                                        if(g[u][x].w>0\&\&st[u]!=x\&\&S[st[u]]==0)update_slack(u,x);
}
void q_push(int x)
```

```
{
        if(x<=n)return q.push_back(x);</pre>
       for(int i=0; i<flower[x].size(); i++)q_push(flower[x][i]);</pre>
void set_st(int x,int b)
{
       st[x]=b;
        if(x<=n)return;</pre>
       for(int i=0; i<flower[x].size();</pre>
           ++i)set_st(flower[x][i],b);
int get_pr(int b,int xr)
{
        int
           pr=find(flower[b].begin(),flower[b].end(),xr)-flower[b].begi
        if(pr%2==1) //
               reverse(flower[b].begin()+1,flower[b].end());
               return (int)flower[b].size()-pr;
        else return pr;
       match[u]=g[u][v].v;
        if(u<=n)return;</pre>
        Edge e=g[u][v];
        int xr=flower_from[u][e.u],pr=get_pr(u,xr);
       for(int i=0; i<pr;</pre>
           ++i)set_match(flower[u][i],flower[u][i^1]);
        set_match(xr,v);
        rotate(flower[u].begin(),flower[u].begin()+pr,flower[u].end());
void augment(int u,int v)
```

```
int xnv=st[match[u]]:
                                                                                   for(int x=1; x<=n; ++x)flower_from[b][x]=0;</pre>
       set_match(u,v);
                                                                                   for(int i=0; i<flower[b].size(); ++i)</pre>
       if(!xnv)return;
       set_match(xnv,st[pa[xnv]]);
                                                                                           int xs=flower[b][i];
                                                                                          for(int x=1; x<=n_x; ++x)</pre>
       augment(st[pa[xnv]],xnv);
}
                                                                                                  if(g[b][x].w==0||DIST(g[xs][x])<DIST(g[b][x]))</pre>
                                                                                                          g[b][x]=g[xs][x],g[x][b]=g[x][xs];
int get_lca(int u,int v)
                                                                                          for(int x=1; x<=n; ++x)</pre>
{
       static int t=0;
                                                                                                  if(flower_from[xs][x])flower_from[b][x]=xs;
       for(++t; u||v; swap(u,v))
                                                                                   set_slack(b);
               if (u==0) continue;
               if(vis[u]==t)return u:
                                                                           void expand_blossom(int b) // S[b] == 1
               vis[u]=t://
                                                                            {
                                           V
                                                                                   for(int i=0; i<flower[b].size(); ++i)</pre>
               u=st[match[u]]:
                                                                                          set_st(flower[b][i],flower[b][i]);
               if(u)u=st[pa[u]];
                                                                                   int xr=flower_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
       }
                                                                                   for(int i=0; i<pr; i+=2)</pre>
       return 0;
}
                                                                                          int xs=flower[b][i],xns=flower[b][i+1];
void add_blossom(int u,int lca,int v)
{
                                                                                          pa[xs]=g[xns][xs].u;
       int b=n+1;
                                                                                          S[xs]=1,S[xns]=0;
       while(b<=n_x&&st[b])++b;</pre>
                                                                                          slack[xs]=0,set_slack(xns);
       if(b>n_x)++n_x;
                                                                                          q_push(xns);
       lab[b]=0,S[b]=0;
       match[b]=match[lca];
                                                                                   S[xr]=1,pa[xr]=pa[b];
       flower[b].clear();
                                                                                   for(int i=pr+1; i<flower[b].size(); ++i)</pre>
       flower[b].push_back(lca);
       for(int x=u,y; x!=lca; x=st[pa[y]])
                                                                                          int xs=flower[b][i];
               flower[b].push_back(x),flower[b].push_back(y=st[match[k]]),q_push(y); S[xs]=-1,set_slack(xs);
       reverse(flower[b].begin()+1,flower[b].end());
       for(int x=v,y; x!=lca; x=st[pa[y]])
                                                                                   st[b]=0:
               flower[b].push_back(x),flower[b].push_back(y=st[match[k]]),q_push(y);
       set_st(b,b);
                                                                           bool on_found_Edge(const Edge &e)
       for(int x=1; x<=n_x; ++x)g[b][x].w=g[x][b].w=0;</pre>
                                                                            {
```

```
int u=st[e.u],v=st[e.v];
       if(S[v]==-1)
       {
               pa[v]=e.u,S[v]=1;
               int nu=st[match[v]];
               slack[v]=slack[nu]=0;
               S[nu]=0,q_push(nu);
       }
       else if(S[v]==0)
               int lca=get_lca(u,v);
               if(!lca)return augment(u,v),augment(v,u),1;
               else add_blossom(u,lca,v);
       }
       return 0;
bool matching()
       fill(S,S+n_x+1,-1),fill(slack,slack+n_x+1,0);
       q.clear();
       for(int x=1; x<=n_x; ++x)</pre>
               if (st[x]==x\&\&!match[x])pa[x]=0,S[x]=0,q_push(x);
       if(q.empty())return 0;
       for(;;)
       {
               while(q.size())
                      int u=q.front();
                      q.pop_front();
                      if(S[st[u]]==1)continue;
                      for(int v=1; v<=n; ++v)</pre>
                              if(g[u][v].w>0&&st[u]!=st[v])
                                     if(DIST(g[u][v])==0)
```

```
if(on_found_Edge(g[u][v]))r
                                   1;
                       else update_slack(u,st[v]);
               }
}
int d=INF;
for(int b=n+1; b<=n_x; ++b)</pre>
       if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
for(int x=1; x<=n_x; ++x)</pre>
       if(st[x]==x\&\&slack[x])
               if(S[x]==-1)d=min(d,DIST(g[slack[x]][x]));
                else
                   if(S[x]==0)d=min(d,DIST(g[slack[x]][x]
for(int u=1; u<=n; ++u)</pre>
       if(S[st[u]]==0)
               if(lab[u]<=d)return 0;</pre>
               lab[u]-=d;
       else if(S[st[u]]==1)lab[u]+=d;
for(int b=n+1; b<=n_x; ++b)</pre>
       if(st[b]==b)
        {
               if(S[st[b]]==0)lab[b]+=d*2;
               else if(S[st[b]]==1)lab[b]-=d*2;
q.clear();
for(int x=1; x<=n_x; ++x)</pre>
       if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&DIST(g[sl
```

```
if(on_found_Edge(g[slack[x]][x]))return
                                   1:
                for(int b=n+1; b<=n_x; ++b)</pre>
                        if(st[b] == b&&S[b] == 1&&lab[b] == 0) expand_blossom(b);
       }
        return 0;
}
pair<ll,int> weight_blossom()
{
       fill(match, match+n+1,0);
        n_x=n;
        int n_matches=0;
       11 tot_weight=0;
       for(int u=0; u<=n; ++u)st[u]=u,flower[u].clear();</pre>
        int w_max=0;
       for(int u=1; u<=n; ++u)</pre>
               for(int v=1; v<=n; ++v)</pre>
                       flower_from[u][v]=(u==v?u:0);
                       w_max=max(w_max,g[u][v].w);
       for(int u=1; u<=n; ++u)lab[u]=w_max;</pre>
       while(matching())++n_matches;
       for(int u=1; u<=n; ++u)</pre>
                if (match[u] &&match[u] < u)</pre>
                       tot_weight+=g[u][match[u]].w;
       return make_pair(tot_weight,n_matches);
struct Istream
{
        char b[20<<20],*i,*e;</pre>
        Istream(FILE*
           in):i(b),e(b+fread(b,sizeof(*b),sizeof(b)-1,in)) {}
       Istream& operator>>(int &val)
```

```
while(*i<'0')++i:
               for(val=0; *i>='0';
                   ++i)val=(val<<3)+(val<<1)+*i-'0';
                return *this;
} kin(stdin);
int main()
{
        cin>>n>>m;
        for(int u=1; u<=n; ++u)</pre>
               for(int v=1; v<=n; ++v)</pre>
                        g[u][v]=Edge \{u,v,0\};
        for(int i=0,u,v,w; i<m; ++i)</pre>
                cin>>u>>v>>w;
               g[u][v].w=g[v][u].w=w;
        cout<<weight_blossom().first<<'\n';</pre>
        for(int u=1; u<=n; ++u)cout<<match[u]<<' ';</pre>
```

17 basisFinding

```
#include <bits/stdc++.h>

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
```

```
#define IN freopen("dichromatic.in", "r", stdin)
#define OUT freopen("dichromatic.out","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define sq(x) ((x)*(x))
using namespace __gnu_pbds;
using namespace std;
#define maxn 200005
int bit[(1<<18)+5] ;</pre>
vector <int> Generate( int x )
   vector <int> vec ;
   vector <int> res ;
   vec.pb(0);
   vec.pb(1) ;
   for(int i=1 ; i<x ; i++)</pre>
   {
       int j = (1 << i) - 1;
       for( ; j>=0 ; j--)
           vec.pb( (vec[j]|(1<<i)) );</pre>
       }
   }
   for( int i=1 ; i<(1<<x) ; i++ )</pre>
```

```
res.pb( bit[ vec[i]^vec[i-1] ] );
   return res ;
int a[maxn] ;
given some numbers in range [0 to 2^x), this function will
   return you with a set of basis
vectors from this numbers
vector <int> findBasis( vector <int> b , int x )
   vector <int> idx , num ;
   for(int i=0; i < b.size(); i++) idx.pb(i), num.pb(b[i]);</pre>
   for(int i=x-1 , j=0 ; i>=0 ; i--,j++)
       for(int k= j+1 ; k<idx.size() ; k++)</pre>
           if(b[k] > b[j])
              swap(b[k],b[j]);
              swap(idx[k],idx[j]);
           }
       }
       for(int k=j+1 ; k<idx.size() ; k++)</pre>
           if( (b[k]^b[j]) < b[k] ) b[k] ^= b[j] ;</pre>
   int i = (int)idx.size() - 1;
   while( i > 0 && b[i] == 0 )
```

```
{
       b.pop_back();
       idx.pop_back();
       i-- ;
   vector <int> basis ;
   for(int i=0; i<idx.size(); i++) basis.pb( num[idx[i]] );</pre>
   return basis ;
}
//
const int ln = 18 ;
int main()
   for(int i=0 ; i<=ln ; i++) bit[(1<<i)] = i ;</pre>
   int n;
   scanf("%d",&n);
   for(int i=0; i<n; i++)</pre>
   {
       scanf("%d",&a[i]);
   }
   vector <int> ans ;
   ans.pb(0);
   for(int i=ln ; i>=1 ; i-- )
   {
       vector <int> b :
       for(int j=0; j<n; j++) if(a[j] < (1<<i)) b.pb(a[j]);</pre>
       vector <int> basis = findBasis(b,i) ;
       if( (int)basis.size() == i )
       {
```

```
vector <int> res = Generate(i) ;
    for(int j=0 ; j<res.size() ; j++) ans.pb(
        ans.back()^basis[ res[j] ] ) ;
    break ;
}

printf("%d\n",bit[(int)ans.size()]) ;
for(int i=0 ; i<ans.size() ; i++)
{
    printf("%d ",ans[i]) ;
}

return 0 ;
}</pre>
```

18 fft(anymod)

```
//fft with any mod
//be careful in choosing MAXN , it should be double of next
  power of 2 of your needed n
//example, here n is 131072 = 2^17 , so MAXN is 2^19 ( double of 2^18 )
// if n was 10, then MAXN = 32 suffices

#include <bits/stdc++.h>

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

#define sf scanf
#define pf printf
```

```
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define IN freopen("dichromatic.in", "r", stdin)
#define OUT freopen("dichromatic.out", "w", stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
#define sq(x) ((x)*(x))
using namespace __gnu_pbds;
using namespace std;
typedef tree< i64, null_type, less<i64>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
typedef pair<i64, i64> pii;
#define MAX 131073
#define MAXN 524288
#define MOD 258280327
#define clr(ar) memset(ar, 0, sizeof(ar))
#define read() freopen("lol.txt", "r", stdin)
#define dbg(x) cout << #x << " = " << x << endl
#define ran(a, b) ((((rand() << 15) ^ rand()) % ((b) - (a) + 1))
   + (a))
using namespace std;
namespace fft{
```

```
int len, last = -1, step = 0, rev[MAXN];
   struct complx{
   double real, img;
   inline complx(){
       real = img = 0.0;
   inline complx conjugate(){
       return complx(real, -img);
   inline complx(double x){
       real = x, img = 0.0;
   inline complx(double x, double y){
       real = x, img = y;
   inline complx operator + (complx other){
       return complx(real + other.real, img + other.img);
   }
   inline complx operator - (complx other){
       return complx(real - other.real, img - other.img);
   inline complx operator * (complx other){
       return complx((real * other.real) - (img *
          other.img), (real * other.img) + (img *
          other.real));
} u[MAXN], v[MAXN], f[MAXN], g[MAXN], dp[MAXN];
```

```
void build(int& a, int *A, int& b, int* B){
   while (a > 1 \&\& A[a - 1] == 0) a--;
   while (b > 1 \&\& B[b - 1] == 0) b--;
       len = 1 \ll (32 - \_builtin\_clz(a + b) -
           (__builtin_popcount(a + b) == 1));
   for (int i = a; i < len; i++) A[i] = 0;</pre>
   for (int i = b; i < len; i++) B[i] = 0;
           if (!step++){
       dp[1] = complx(1);
       for (int i = 1; (1 << i) < MAXN; i++){
           double theta = (2.0 * acos(0.0)) / (1 << i);
           complx mul = complx(cos(theta), sin(theta));
           int lim = 1 << i;</pre>
           for (int j = lim >> 1; j < lim; j++){</pre>
               dp[2 * j] = dp[j];
              dp[2 * j + 1] = dp[j] * mul;
   }
   if (last != len){
       last = len;
       int bit = (32 - __builtin_clz(len) -
           (__builtin_popcount(len) == 1));
       for (int i = 0; i < len; i++) rev[i] = (rev[i >> 1]
           >> 1) + ((i & 1) << (bit - 1));
   }
   }
   void transform_unrolled(complx *in, complx *out, complx*
       ar){
```

```
for (int i = 0; i < len; i++) out[i] = in[rev[i]];</pre>
   for (int k = 1; k < len; k <<= 1){
   for (int i = 0; i < len; i += (k << 1)){
       complx z, *a = out + i, *b = out + i + k, *c = ar
           + k;
       if (k == 1){
           z = (*b) * (*c):
           *b = *a - z, *a = *a + z;
       }
       for (int j = 0; j < k && k > 1; j += 2, a++, b++,
           c++){
           z = (*b) * (*c):
           *b = *a - z, *a = *a + z;
           a++, b++, c++;
           z = (*b) * (*c);
           *b = *a - z, *a = *a + z;
       }
   }
bool equals(int a, int * A, int b, int * B){
if (a != b) return false;
for (a = 0; a < b \&\& A[a] == B[a]; a++){}
return (a == b);
}
int mod_multiply(int a, int* A, int b, int* B, int mod){
   build(a, A, b, B);
   int flag = equals(a, A, b, B);
   for (int i = 0; i < len; i++) A[i] %= mod, B[i] %=
   for (int i = 0; i < len; i++) u[i] = complx(A[i] &</pre>
       32767, A[i] >> 15);
```

```
32767, B[i] >> 15);
               transform_unrolled(u, f, dp);
               for (int i = 0; i < len; i++) g[i] = f[i];</pre>
               if (!flag) transform_unrolled(v, g, dp);
               for (int i = 0; i < len; i++){</pre>
           int j = (len - 1) & (len - i);
           complx c1 = f[j].conjugate(), c2 = g[j].conjugate();
           complx a1 = (f[i] + c1) * complx(0.5, 0);
                      complx a2 = (f[i] - c1) * complx(0, -0.5);
                      complx b1 = (g[i] + c2) * complx(0.5 /
                          len, 0);
                      complx b2 = (g[i] - c2) * complx(0, -0.5 /
                          len);
                      v[j] = a1 * b2 + a2 * b1;
                      u[j] = a1 * b1 + a2 * b2 * complx(0, 1);
               }
               transform_unrolled(u, f, dp);
               transform_unrolled(v, g, dp);
       long long x, y, z;
               for (int i = 0; i < len; i++){</pre>
           x = f[i].real + 0.5, y = g[i].real + 0.5, z =
               f[i].img + 0.5;
           A[i] = (x + ((y \% mod) << 15) + ((z \% mod) << 30)) %
               mod;
               return a + b - 1;
       }
}
int black[17][MAXN] , red[17][MAXN] , ans[MAXN] ;
```

for (int i = 0; i < len; i++) v[i] = complx(B[i] &</pre>

```
int dp[MAXN] ;
int main()
{
   IN;
   OUT ;
   black[0][0] = 1; red[0][0] = 1; red[0][1] = 1;
   black[1][1] = 1; black[1][2] = 2; black[1][3] = 1;
   red[1][3] = 1; red[1][4] = 4; red[1][5] = 6; red[1][6] =
       4 ; red[1][7] = 1 ;
   for(int i=2; i<=16 ; i++)</pre>
   {
    // printf("%d\n",i);
       for(int j=0 ; j<MAX ; j++) dp[j] =</pre>
          (red[i-1][j]+black[i-1][j])%MOD;
       fft::mod_multiply(MAX,dp,MAX,dp,MOD);
       for(int j=1; j<MAX; j++) black[i][j] = dp[j-1];</pre>
       for(int j=0; j<MAX; j++) dp[j] = black[i][j];</pre>
       fft::mod_multiply(MAX,dp,MAX,dp,MOD);
       for(int j=0; j<MAX; j++) red[i][j] = dp[j-1];</pre>
        for(int j=0; j<10; j++) printf("%d: %d
    %d\n",j,black[i][j],red[i][j]);
   }
   int t , h ;
   scanf("%d %d",&t,&h);
   for(int i=0 ; i<MAX ; i++)</pre>
       for(int j=0 ; j<=h ; j++) ans[i] = (ans[i] +</pre>
          black[j][i]+red[j][i])%MOD;
       ans[i] = (ans[i] %MOD + MOD) %MOD ;
   }
```

```
for(int i=0; i<t; i++)
{
    int n;
    scanf("%d",&n);
    printf("%d\n",ans[n]);
}

return 0;
}</pre>
```

19 lca

```
#include <bits/stdc++.h>
#define i64 long long int
using namespace std;
//starts O(1) lca
//preprocessing nlogn
#define MAX 100010
#define LOG 18
namespace LCA{
   i64 sum[MAX];
   int st[MAX] , en[MAX] , lg[MAX] , par[MAX] , a[MAX] ,
      id[MAX] , dp[LOG][MAX] ;
   vector <int> weight[MAX] , g[MAX] ;
   int n , r , Time , cur ;
   void init(int nodes, int root){
       n = nodes, r = root, lg[0] = lg[1] = 0;
      for (int i = 2; i \le n; i++) lg[i] = lg[i >> 1] + 1;
```

```
for (int i = 0; i <= n; i++) g[i].clear(),</pre>
       weight[i].clear();
}
void addEdge(int u, int v, int w){
    g[u].push_back(v), weight[u].push_back(w);
   g[v].push_back(u), weight[v].push_back(w);
int lca(int u, int v)
   if(en[u] > en[v])swap(u,v);
   if( st[v] <= st[u] && en[u] <= en[v] ) return v ;</pre>
   int l = lg[id[v] - id[u] + 1] ;
   int p1 = id[u] , p2 = id[v] - (1<<1) + 1 ;</pre>
   if( sum[ dp[1][p1] ] < sum[ dp[1][p2] ] ) return par[</pre>
       dp[1][p1] ];
    else return par[ dp[1][p2] ] ;
}
i64 dis( int u ,int v )
    int 1 = lca(u,v);
   return (sum[u] + sum[v] - ( sum[l] << 1LL ));</pre>
void dfs(int u, int p , i64 curSum){
    st[u] = ++Time ; par[u] = p ; sum[u] = curSum ;
   for(int i=0 ; i<g[u].size() ; i++)</pre>
   {
       if( g[u][i]==p ) continue ;
       dfs( g[u][i] ,u,curSum+weight[u][i]);
    en[u] = ++Time;
    a[++cur] = u;
```

20 moSet

```
/*
CF-375D
A undirected tree is given, each node having a colour , we'll
   have some queries of form (v,k).
We've to answer how many color occurs at least k'times in the
   subtree rooted at v.
*/
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
```

```
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 1000000007LL
#define IN freopen("nocross.in","r",stdin)
#define OUT freopen("nocross.out","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 100000001
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
#define sq(x) ((x)*(x))
using namespace __gnu_pbds;
using namespace std;
typedef pair< i64,i64 > pii ;
typedef tree< i64, null_type, less<i64>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
/* Special functions:
       find_by_order(k) --> returns iterator to the kth largest
           element counting from 0
       order_of_key(val) --> returns the number of items in a
           set that are strictly smaller than our item
*/
```

```
#define maxn 100005
class moSet{
   /*
   intution
   say, now I have my cnt array like this cnt[] = { 0 , 4 , 1 ,
      2,3,4,0,2}
   and each time cnt changes by only one, so if a element
       occurred 2 times before, now it's
   occurrence can be either 1 or 3. And each time we want to
       know, how many element occurred
   at least k times. Then we can keep our cnt[] array in
       another form by sorting the occurrence.
   occ[] = \{0,0,1,2,2,3,4,4\}. So when an increase an elements
       occurrence, say previously an element
   occurred 2 times, now it is occurring 3 times, then there
       will be only a slight change in occ array,
   one 2 will be just turned into 3.
    Description of the data structure
    this is a data-structure mainly for keeping track of
       occurrences
    lets say currently we have n=6 and our sortedArray[] =
       {0,0,1,2,2,3,4,4}
    if we increase(2), then sortedArray[] = \{0,0,1,2,3,3,4,4\}
       }, so one 2 will be turned into 3
    if we decrease(3) now ,then sortedArray[] = {
       0,0,1,2,2,3,4,4 }, so one 3 will be turned into 2
    along with this we've start, and en array and exist array,
       start[1] = 2, en[2] = 4, exist[1] = true,
    exist[5] = false, also remember here we can only handle
       elements from 0 to n (inclusive)
   */
public:
```

```
bool *exist ;
int *sortedArray, *Start , *End , n ;
moSet(int _n)
   n = _n ;
    exist = new bool[n+2] ;
   sortedArray = new int[n+2] ;
    Start = new int[n+2] ;
   End = new int[n+2];
    for(int i=0 ; i<=n ; i++) exist[i] = false ;</pre>
}
moSet( int _n , int initVal )
   n = _n ;
    exist = new bool[n+2] ;
   sortedArray = new int[n+2] ;
    Start = new int[n+2] ;
   End = new int[n+2];
   for(int i=0 ; i<=n ; i++) exist[i] = false ;</pre>
    exist[initVal] = true ;
   for(int i=0; i<=n; i++) sortedArray[i] = initVal;</pre>
   Start[initVal] = 0 ; End[initVal] = n ;
void increase(int v)
₹
    if(!exist[v] || v<0 || v>=n ) return : // 0 to n-1
    sortedArray[ End[v] ] = v+1 ;
   if( !exist[v+1] )
       exist[v+1] = true ;
       Start[v+1] = End[v+1] = End[v];
```

```
}
   else Start[v+1]-- ;
   End[v]-- ;
   if(Start[v]>End[v]) exist[v] = false ;
   return ;
}
void decrease(int v)
   if( !exist[v] || v<=0 || v>n ) return ; // 1 to n
   sortedArray[ Start[v] ] = v-1 ;
   if(!exist[v-1])
   {
       exist[v-1] = true ;
       Start[v-1] = End[v-1] = Start[v];
   }
   else End[v-1]++ ;
   Start[v]++ ;
   if(Start[v]>End[v]) exist[v] = false ;
   return ;
}
int howMany(int x)
   if( sortedArray[n] <x ) return 0 ;</pre>
   int lo = 0 , hi = n ;
   while(lo<hi)</pre>
       int mid = (lo+hi)/2;
       if( sortedArray[mid]>=x ) hi = mid ;
       else lo = mid+1 ;
   }
   return n-lo+1 ;
}
```

};

```
int posInArray[maxn] , endPos[maxn] , Time , s ;
int c[maxn] , col[maxn] , cnt[maxn] , ans[maxn] ;
vector <int> g[maxn] ;
void dfs(int u , int par)
{
   posInArray[u] = ++Time ;
   col[Time] = c[u] ;
   for(int i=0 ; i<g[u].size() ; i++ )</pre>
       int v = g[u][i] ;
       if(v==par) continue ;
       dfs(v,u);
    endPos[u] = Time ;
struct Query{
   int l ,r ,id , k ;
}query[maxn];
bool moComp( Query q1 , Query q2 )
   if( q1.1/s == q2.1/s ) return q1.r<q2.r ;</pre>
   return q1.1<q2.1 ;</pre>
}
int main()
   int i , j , k , m , n , l , r ;
    scanf("%d %d",&n,&m);
```

```
moSet mySet(n,0);
/*
   while(1)
       scanf("%d %d",&k,&l);
       if( k==1 ) mySet.increase(1) ;
       else mySet.decrease(1) ;
       for(i=0; i<=10; i++) printf("%d ",mySet.sortedArray[i])</pre>
       printf("\n") ;
*/
   for(i=1; i<=n; i++) scanf("%d",&c[i]);</pre>
   for(i=1 ; i<n ; i++)</pre>
   {
       int u , v ;
       scanf("%d %d",&u,&v);
       g[u].pb(v); g[v].pb(u);
   }
   Time = 0;
   dfs(1,-1);
   for(i=1 ; i<=m ; i++)</pre>
       int v;
       scanf("%d %d",&v,&k);
       query[i].l = posInArray[v] ; query[i].r = endPos[v] ;
           query[i].k = k;
       query[i].id = i ;
   }
   s = sqrt(n+0.0) + 1;
   sort(query+1, query+m+1,moComp) ;
```

```
memset(cnt,0,sizeof(cnt));
1 = 1 ; r = 0 ;
for(i=1 ; i<=m ; i++)</pre>
₹
 // printf("%d %d")
   while(r<query[i].r)</pre>
       r++ ;
       j = r;
       mySet.increase( cnt[ col[j] ] );
       cnt[ col[j] ]++ ;
   while(l>query[i].1)
   {
       1-- ;
       j = 1;
       mySet.increase( cnt[ col[j] ] );
       cnt[ col[j] ]++ ;
   while(r>query[i].r)
       j = r;
       mySet.decrease(cnt[col[j]]);
       cnt[ col[j] ]-- ;
       r-- ;
   while(l<query[i].1)</pre>
   {
       j = 1;
       mySet.decrease(cnt[col[j]]);
       cnt[ col[j] ]-- ;
       1++;
```

```
}
       ans[ query[i].id ] = mySet.howMany(query[i].k) ;
  /* printf("%d\n",query[i].id);
       for(j=0; j<=n; j++) printf("%d ",mySet.sortedArray[j]);</pre>
       printf("\n") ; */
   }
   for(i=1; i<=m; i++) printf("%d\n", ans[i]);</pre>
   return 0;
/*
10 10
82 48 59 48 32 83 34 46 47 79
2 1
3 1
4 3
5 4
6 1
7 2
8 3
9 2
10 2
1 2
1 1
1 3
1 5
2 1
2 2
3 1
3 3
6 1
9 2
*/
```

21 non negative soln extended euclid

```
#include <bits/stdc++.h>
// #include <ext/pb_ds/assoc_container.hpp>/
// #include <ext/pb_ds/tree_policy.hpp>
#define sf scanf
#define pf printf
#define pb push_back
#define mp make_pair
#define PI ( acos(-1.0) )
#define mod 100000007
#define IN freopen("nocross.in","r",stdin)
#define OUT freopen("nocross.out","w",stdout)
#define FOR(i,a,b) for(i=a ; i<=b ; i++)</pre>
#define DBG pf("Hi\n")
#define INF 200000000
#define i64 long long int
#define eps (1e-8)
#define xx first
#define yy second
#define ln 17
#define off 2
#define SZ(z) ((int)z.size())
// using namespace __gnu_pbds;
using namespace std;
// typedef tree< i64, null_type, less<i64>, rb_tree_tag,
   tree_order_statistics_node_update> ordered_set;
#define maxn 50005
typedef pair<i64, i64> pii;
```

```
// f(a,b,c) returns how many non_negative (x,y) are there such
   that a*x+b*y = c
//tested for (a,b,c) > 0
// for negative (a,b) equation changes
pii extendedEuclid(i64 a, i64 b) { // returns x, y | ax + by =
   gcd(a,b)
   if(b == 0) return pii( a >= 0 ? 1 : -1 , OLL);
   else {
       pii d = extendedEuclid(b, a % b);
       return pii(d.yy, d.xx - d.yy * (a / b));
   }
}
i64 gcd(i64 a, i64 b)
{
   if(b==0) return a ;
   return gcd(b,a%b) ;
}
i64 Floor(i64 a, i64 b)
   if(b<0) b *= (-1) , a *= (-1) ;
   i64 c = a/b;
   if( a<0 && b*c!=a ) c-- ;</pre>
   return c ;
}
i64 Ceil(i64 a, i64 b)
{
   if(b<0) b *= (-1) , a *= (-1) ;
   i64 c = a/b ;
   if( a>0 && b*c!=a ) c++ ;
   return c ;
}
i64 f( i64 a, i64 b, i64 c )
```

```
if( a==0 && b==0 ) return (c==0) ;
   if(a==0) return (c%b == 0) ;
   if(b==0) return (c%a == 0) ;
   i64 g = gcd(a,b);
   if(c%g!=0) return 0 ;
   c /= g;
   a /= g ; b/= g ;
   pii soln = extendedEuclid(a,b) ;
   soln.xx*= c ; soln.yy *= c ;
   i64 lo = Ceil(-soln.xx,b) , hi = Floor(soln.yy,a) ;
   return max( OLL , hi-lo+1 ) ;
}
int main()
   i64 i , j , k , l , m , n ;
   i64 t = 1 , tc ;
   i64 a , b , c , p ;
    scanf("%11d",&tc);
   while(t<=tc)</pre>
       scanf("%11d %11d %11d %11d",&a,&b,&c,&p);
       printf("Case %lld: ",t++);
```

```
i64 g = gcd( a , gcd(b,c) ) ;

if(p%g!=0)
{
    printf("0\n") ;
    continue ;
}

a /= g ; b /= g ; c/=g ; p/=g ;

i64 ans = OLL ;

while( p>=0 )
{
    ans += f(a,b,p) ;
    p -= c ;
}

printf("%lld\n",ans) ;
}
```

}

$22 \quad \text{sum of } (p*i+r) \quad q$

```
/*
i64 res = 0 ;
for(int i=0 ; i<n ; i++) res += ( p*i+r )/q ;
return res ;
*/
//this function does the above thing in logarithmic time
i64 findSum(i64 n, i64 p, i64 r, i64 q) {
   if (p == 0) {
      return (r / q) * n;
   }
   if (p >= q || r >= q) {
      return ((p / q) * (n - 1) + 2 * (r / q)) * n / 2 +
         findSum(n, p % q, r % q, q);
   }
   return findSum((p * n + r) / q, q, (p * n + r) % q, p);
}
```