The package Tikz-MultInets

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Abstract

We describe here the use of the package Tikz-MultInets, an extended version of a package written by Marc De Falco to represent interaction nets. His package was meant to represent simple interaction nets, i.e. with one principal port and simple wires as well as boxes and exponential boxes for linear logic. We added the possibility of defining cells with multiple principal ports, cells with only one port at all as well as many different ways of defining new paths for wires.

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1 Introduction

The package uses Tikz to create graphical representations of the most general case of interaction nets, i.e. interaction nets with multiport cells and multiwires.

The package is meant to be retro-compatible with v0.1 tikz interaction nets library by Marc de Falco which was aimed at representing interaction nets as intended by Laffont. All original commands are maintained and new commands were created in the same spirit, thus the sporadic use of french names for some of the objects.

2 Main extensions from original package

Evolutions from v0.1 tikz interaction nets library by Marc de Falco:

- apex angle of simple cells (from 60 to 100)
- added multiport cells and 1-port cells
- added multiwires
- added invisible node with port-like anchors for better building of wires
- added external auxiliary and principal ports to bypass cells
- added commands for : cellheight, size of principal port in multicells, port size, free wire size, bypass distance

3 Macro usage

3.1 Global rules

Some generic rules apply for all commands.

Arguments between square brackets $- \lceil \langle options \rangle \rceil$ – are optional and may or may not have a default value. They will be usually marked in blue. For instance, $\langle direction \rangle$ is always optional and has default value D, for down. This default value can be globally modified (see section 5).

The optional arguments in square brackets right after the command name are usually $\langle tikz\text{-}options \rangle$ that change or overwrite graphical options for the given entity, cell or wire. See the Tikz package for more details. Some package specific options to the given object are also available through pgf/tikz key options.

Arguments between braces $-\{\langle options \rangle\}$ - are mandatory. In general, the red colour will be used to emphasize the fact that a value is **mandatory**.

Sometimes, in some contexts, some arguments don't make much sense. Then, an otherwise mandatory option can be skipped and the default value is used.

In that case, it will be shown in orange $-\{\langle position \rangle\}$. This is mainly true of the position of a cell in the case it is the unique cell in the picture. Its value is then equivalent to $\{0,0\}^1$. Note that if it is ommitted, in order for the parser to understand the omission, the command needs to have an explicit $[\langle direction \rangle]$ or end with a semicolon ';'.

Finally, the elements' naming mechanism – normal parenthesis, ($\langle name \rangle$) – follows Tikz' rules and is mandatory except if $\langle label \rangle$ is simple, in which case the cell is implemented with the name $\langle label \rangle$ (again, see Tikz package for details).

3.2 Positioning

An important aspect of building nets is the positioning of cells and wires. The usual way of positioning objects in tikz is by corrdinates – cartesian or polar – but many other ways are available (using tikzlibraries positioning and calc included in Tikz-MultInets.

There are options to do calculations on positions: take some known position and add a vector, again cartesian of polar:

```
\node[draw] (a) at (0,0) {a};
\node[draw] (b) at ($(a)+(2,0.5)$) {b};
b
```

Or you can calculate a position in between two given positions at a proportion of the path:

```
\node[draw] (a) at (0,0) {a};
\node[draw] (b) at (4,0) {b};
\node[draw] (c) at ($(a)!.3!(b)$) {c};

a c b
```

Those are composable

¹To say the truth, in such a case any position value would give the same result since images are cropped.

```
\node[draw] (a) at (0,0) {a};
\node[draw] (b) at (4,2) {b};
\node[draw, color=red] (c) at ($(a)!.5!(b)+(1,0)$]) {c};
```

Another most interesting way is to use two elements and at the crossing of their positions: at the vertical of one of them and one the same line as the other.

```
\node[draw] (a) at (0,0) {a};
\node[draw] (b) at (4,2) {b};
\node[draw, color=red] (c) at (a -| b) {c};
\node[draw, color=green] (d) at (a |- b) {d};

d

b
```

Cells can be positioned using these techniques. Better, there positions can then be used for calculations: at the crossing of multicell A and multicell B. Actually, for more precision, even ports of cells can be used as positions.

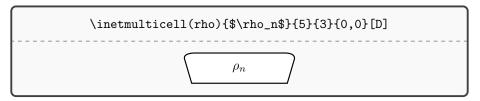
This package adds even more position capabilities connected to the specifics of cells. More on that in section 4.

3.3 Cells

3.3.1 Defining cells

 $\label{locality} $$\left(\frac{options}{(aname)}, \frac{\langle label \rangle}{\langle coarity \rangle}, \frac{\langle arity \rangle}{\langle arity \rangle}, \frac{\langle coarity \rangle}{\langle options \rangle} \right] $$ (anamely options)$ can be a tikz-style, predefined style or any options for tikz lines.$

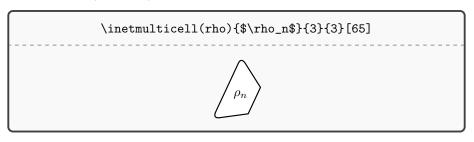
 $\langle name \rangle$ is a name to reference the object when building wires and ports. $\langle label \rangle$ is the label of the cell. It appears inside. $\langle coarity \rangle$ is the number of $principal\ ports$ of the cell. $\langle arity \rangle$ is the number of $auxiliary\ ports$ of the cell. $\langle position \rangle$ is a position in tikz-style cartesian or polar coordinates. $\langle direction \rangle$ is either D (default),L,U,R or any angle where '0' is down.

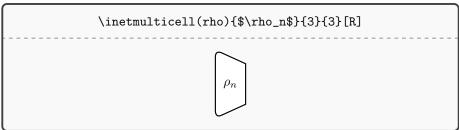


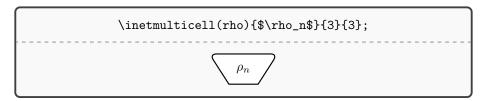
The length of a cell depends on the value of $\langle coarity \rangle$: it is defined as $\langle coarity \rangle \times \text{portsize}$.

If $\langle coarity \rangle = 1$, then the constructed multicell will be an \inetcell (see below). If $\langle coarity \rangle = 1$ and $\langle arity \rangle = 0$, then the constructed multicell will be an \inetzerocell.

A special writing is allowed for cases where positioning is not done by coordinates (e.g. in matrix environments). In such a case the $\langle position \rangle$ can be omitted (equivalent to $\{0,0\}$ or $\{0:0\}$) but then the command should finish with a ';' or a $\langle direction \rangle$.







\inetcell $[\langle options \rangle] (\langle name \rangle) \{\langle label \rangle\} \{\langle position \rangle\} [\langle direction \rangle]$

 $\langle options \rangle$ can be a tikz-style, predefined style or any options for tikz lines, or arity=k to create a cell with k auxiliary ports.

 $\langle name \rangle$ is a name to reference the object when building wires and ports.

 $\langle label \rangle$ is the label of the cell. It appears inside.

 $\langle position \rangle$ is a position in tikz-style Cartesian or polar coordinates.

(direction) is either D (default), L, U, R or any angle where '0' is down.

\inetcell(A){A}{0,0}[U];



For retro-compatibility with De Falco's tikz-inet, the arity of a simple cell is defined as a tikz-option: defaults to arity=4. It is equivalent to define a simple cell of arity k or a multicell with coarity 1 and arity k. The package actually replaces the former by the latter.

\inetcell[arity=5]{A}{0,0}; \inetmulticell(B){B}{1}{5}{0,-1.5};





A special kind of cell is a cell with only principal ports (originally only the particular case of a cell with 1 principal port and 0 auxiliary ones was considered). Such a cell is represented by a circle.

\inetzerocell

$[\langle options \rangle] (\langle name \rangle) \{\langle label \rangle\} \{\langle position \rangle\}$

 $\langle options \rangle$ can be a tikz-style, predefined style or any options for tikz lines. $\langle name \rangle$ is a name to reference the object when building wires and ports. $\langle label \rangle$ is the label of the cell. It appears inside.

 $\langle position \rangle$ is a position in tikz-style Cartesian or polar coordinates.

\inetzerocell(Z){Z}{0,0};



Of course, the zerocell is a convention. A cell with only one pricipal port could just be as well a triangle with no ports in the back.

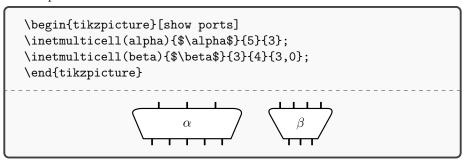


3.3.2 Then drawing its ports

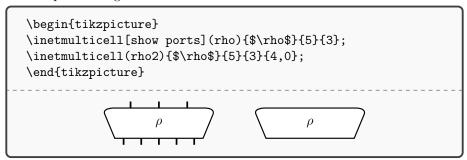
Ports are not drawn by default, because they usually should not be *free* (disconnected) but rather connected through a (multi)wire to another port, and are thus drawn when the wire is created.

[show ports]

It is nevertheless possible to tell the package to draw all ports of all cells in the tikzpicture:



or all ports of a given cell:



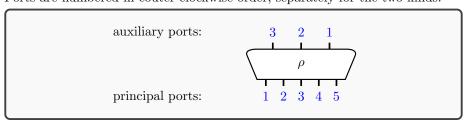
Nevertheless, the "normal" way of doing is to draw only ports that are not connected to any wire, since wires in some way contain the ports they connect. The default name of a port is of the form

$$\langle cell \ name \rangle . \langle type \ of \ port \rangle \quad \langle number \rangle$$

with a space before the number and where $\langle type\ of\ port \rangle$ is

- pal for *principal* ports
- pax for auxiliary ports

Ports are numbered in couter-clockwise order, separately for the two kinds:



To draw a given port, use the following command

\inetport

```
[\langle options \rangle] (\langle port name \rangle)
```

 $\langle options \rangle$ can be a tikz-style, predefined style or any options for tikz lines. $\langle port \ name \rangle$ is the complete name of a port.

```
\inetmulticell(rho){\$\rho\$}{5}{3};
\inetport(rho.pal 1)
\inetport(rho.pal 4)
\inetport(rho.pax 2)
```

\inetportnamed

It is often the case that one needs to give and show a name of a port.

 $[\langle options \rangle] (\langle port \ name \rangle) \{\langle port \ label \rangle\} [\langle label \ options \rangle]$

(options) can be a tikz-style, predefined style or any options for tikz lines.

⟨**port** name⟩ is the identification name of a port.

(port label) is the name you wish to show for this port.

 $\langle label\ options \rangle$ are tikz-options for the label.

The label is in its own tikz-node, so all options that apply to nodes are acceptable in the $\langle label\ options \rangle$.

```
\inetmulticell(rho){$\rho$}{5}{3}[R];
\inetportnamed(rho.pal 1){$a$}
\inetportnamed(rho.pal 4){$b$}[color=red]
\inetportnamed(rho.pax 2){You name it!}[rotate=90]
```

3.3.3 Identifying ports

Ports need to be identified not only to draw them, but also to connect wires to them. Such identification can be done in various ways.

Following the naming of tikz-inet, the usual way of identifying a port of a multicell is by its type and numbering: third principal port or first auxiliary port for instance. As shown in the examples above, this is done by attaching to the *name* of the cell a suffix .pal 3 for the third principal port or .pax 1 for the first auxiliary one.

Some ports nevertheless have special names.

Special names in multicells Multicells have few specially named ports.

pax A survivor from the tikz-inet package: that port is in the middle even if the cell has even arity.

\inetmulticell{a}{5}{4};
\inetport(a.pax)

Special names in simple cells Laffont has shown that in interaction nets, all simple cells can be simulated by a small set of cells with arities 1 or 2. Such cells therefore have therefore been well treated, in particular for there special ports.

pal The principal port is unique, so its easy to identify (pal 1 also works).



pax An auxiliary port in the middle, for the case of arity 1. In the case of odd arity 2k + 1, it's the same as pax k+1. In the case of even arity, it does not correspond to any numbered port: it's just a port in the middle.



left pax The first auxiliary port (remember that ports are numbered counter-clockwise).



right pax The last auxiliary port.



The default simple cell has arity 4. Therefore, the default cell can be used for any arity < 4 as follows:

- arity = $1 \rightarrow pax \text{ or middle } pax$
- $arity = 2 \rightarrow left|right pax$

- $arity = 3 \rightarrow left|middle|right pax$
- arity = $4 \rightarrow pax 1|2|3|4$ and |left|right

3.3.4 The case of zerocells

Zerocells were introduced to represent a cell with a unique (principal) port. To be clear, it was decided to represent them as circles as they do not have deiferentiated sets of ports. Pgf/tikz has an anchor mechanism in which circles have a natural set of positions around them that can be referred to using cardinal directions. We extended these anchors to define ports in the 8 positions of the 8-point compass: north, south, west, east, north west, north east, south west, south east.

We also provided some aliases for these points: the version without spaces and the initials. As a result, the possibilities are:

```
north, n
south, s
west, w
east, e
north west, northwest, nw
north east, northeast, ne
south west, southwest, sw
south east, southeast, se
```

```
\inetzerocell(A){A};
\inetport(A.south east);
```

Note that because of the use of anchors to define the position of the port, it is possible to have zerocells with up to 8 ports if necessary:

```
\inetzerocell(A){A}{0,0};
\inetport(A.n);
\inetport(A.ne);
\inetport(A.e);
\inetport(A.se);
\inetport(A.sw);
\inetport(A.w);
\inetport(A.nw);
```

3.3.5 Free ports

Ports can be *free* in the net and act as an interface of that net to the external world. In such a case, it can be useful to draw them a little longer in order to emphasize this fact.

\inetwirefree

```
[\langle options \rangle] (\langle port name \rangle)
```

 $\langle options \rangle$ can be a tikz-style, predefined style or any options for tikz lines. $\langle port\ name \rangle$ is the complete name of a port.

```
\inetmulticell[show ports]{A}{2}{3}{0,0}
\inetwirefree(A.pal 1)
\inetzerocell{B}{0,-1.5};
\inetwirefree(B.south east)
\inetport(B.s)
```

The length of such free ports can be set globally (see section 5).

We will see later that such free ports can also be attached to other objects, like wires and invisible nodes. The definition stays the same since these objects also define a set of ports.

3.3.6 Grouping ports under braces

One can wish to annotate ports to comment on their value or use. The package provides a useful *curly brace* possibility to group nodes:

\inetbrace

```
(\langle first\ port \rangle) (\langle last\ port \rangle) \{\langle description \rangle\}
\langle first\ port \rangle is the complete name of a port.
\langle last\ port \rangle is the complete name of a port.
\langle description \rangle is the text over the brace.
```

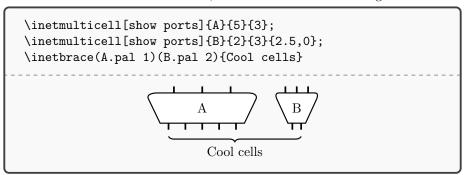
```
\inetmulticell[show ports]{A}{5}{3};
\inetbrace(A.pal 1)(A.pal 4){First group}
\inetbrace(A.pax 1)(A.pax 3){Other group}

First group
```

Be careful not to invert the order of the start and end ports:

```
\inetmulticell[show ports]{A}{5}{3};
\inetbrace(A.pal 4)(A.pal 1){First group}
```

This command can be hacked to annotate a group of cells instead, with rather random results. As a rule of thumb, it works of cells are well aligned.



3.4 Defining useful cells

This is a macro that enables to predefine a cell with particular label, coarity, arity and possibly direction.

\inetmulticelltype

```
[\langle options \rangle ] \{\langle abel \rangle} \{\langle coarity \rangle} \{\langle arity \rangle} \} \{\langle arity \rangle} \{\langle arity \rangle} \} \{\langle arity \rangle} \rangle arity \rangle arity \rangle is the number of principal ports of the cell.
$\langle arity \rangle$ is the number of auxiliary ports of the cell.
$\langle arity \rangle$ is the number of auxiliary ports of the cell.
$\langle arity \rangle$ is either D (default), L, U, R or any angle where '0' is down.

It is used inside a \newcommand as follows:
```

It is then possible to define such a predefined cell by just giving its name and its position:

Notice that $\langle new\ options \rangle$ add up with options from the definition of the special command, and overwrite them in case of conflict.

For example:

 $\label{lem:likelitype[very thick]{}} $$ \operatorname{likelitype[very thick]{}} {alphacell[thin,minimum width=2ex](cellA){3,-1}} $$$

3.5 Wires

The simplest wire is between two ports:

Or between any two nodes:

```
\inetwire [\langle options \rangle] (\langle port\ name \rangle) *<\langle cross\ node \rangle> (\langle port\ name \rangle) < \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines. \langle cross\ node \rangle is optional nodes the wire should cross (see Section ) \langle port\ name \rangle are complete names of ports.
```

```
\inetwirecoords
                                [\langle options \rangle] (\langle node\ name \rangle) (\langle node\ name \rangle)
                                   (options) can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle node \ name \rangle are any node name.
                                  For some uses, when cells are really close, it might come in handy to use more
                               flexible wires.
                                [\langle options \rangle] (\langle port \ name \rangle) (\langle port \ name \rangle)
        \inetshortwire
                                   (options) can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle port \ name \rangle are complete names of ports.
  \inetveryshortwire
                                [\langle options \rangle] (\langle port name \rangle) (\langle port name \rangle)
                                   \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle port \ name \rangle are complete names of ports.
                                  Now the serious connectors:
                                [\langle options \rangle] (\langle name \rangle) \{\langle position \rangle\}
        \inetmultiwire
                                          \langle cross\ node \rangle \rangle \langle port\ 1 \rangle
                                          \langle cross\ node \rangle > (\langle port\ n \rangle) [\langle free\ port\ angle \rangle]
                                   \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle name \rangle is a name for the wire. If not provided, no future use of it.
                                   \langle position \rangle is a position in (cartesian or polar) coordinates for the wire.
                                   \langle cross \ node \rangle is optional nodes the wire should cross (see Section )
                                   \langle port \ i \rangle is a complete name of a port.
                                   (free port angle) give the angle for the freeport if provided.
                                  At the center of a multiwire, there is a visible \inetnode:
                                [\langle option \rangle] (\langle name \rangle) \{\langle position \rangle\}
               \inetnode
                                   ⟨option⟩ can be 'wire' or any options for tikz circle nodes.
                                   \langle name \rangle is a name for the wire.
                                   \langle position \rangle is a position in (cartesian or polar) coordinates.
                                [\langle options \rangle] \{\langle position \rangle\}
               \inetloop
                                   \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle position \rangle is a position for the center of the loop.
                                [\langle options \rangle] (\langle pal \rangle) (\langle pax \rangle)
 \inetwirearoundleft
                                   \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle pal \rangle is the complete name of a principal port of a cell.
                                   \langle pax \rangle is the complete name of an auxiliary port of a (usually the same) cell.
\inetwirearoundright
                                [\langle options \rangle] (\langle pal \rangle) (\langle pax \rangle)
                                   (options) can be a tikz-style, predefined style or any options for tikz lines.
                                   \langle pal \rangle is the complete name of a principal port of a cell.
                                   \langle pax \rangle is the complete name of an auxiliary port of a (usually the same) cell.
```

3.5.1 Fake ports of cells to better draw wires

Simili-ports of multicells and simple cells

- leftext pax
- rightext pax
- leftext pal
- rightext pal

rightext pax

A fake port after the last port of a cell.



External anchors

- westwest
- easteast

3.6 Boxes

First a box around some nodes, then the promotion box of linear logic.

```
\inetbox [\langle options \rangle] \{\langle fit \rangle\} (\langle name \rangle) \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines. \langle fit \rangle is a space-separated list of cell names (a) (b) .... \langle name \rangle is a name for further reference of the box. [\langle options \rangle] \{\langle fit \rangle\} (\langle name \rangle) \langle options \rangle can be a tikz-style, predefined style or any options for tikz lines. \langle fit \rangle is a space-separated list of cell names (a) (b) .... \langle name \rangle is a name for the !-cell. The name of the box is b\langle name \rangle.
```

4 Relative positionning

There are three main features of relative positionning.

Above a port

Add a coordinate, cartesian or polar

Crossings

5 Global values and defaults

```
\inetsetportlength
                     \renewcommand{\abovedistance}{#1}
                       \renewcommand{\aboveabovedistance}{(#1+.35cm)}
    \inetsetportsize
                       \inetportsize
                       \inetcellheight
  \inetsetcellheight
                       \abovedistance
\inetsetabovedistance
\inetsetaboveabovedistanc\aboveabovedistance
                       \bypassdistance
\inetsetbypassdistance
\inetsetwirefreelength
                       \inetwirefreelength
\inetsetportnamedistance \inetportnamedistance
\inetsetbracedistance
                       \inetbracedistance
\inetsetbracetextdistance\inetbracetextdistance
```

6 Miscellaneous

6.1 Unspecific number of ports

\inetdotsbetween

```
Use three dots to show repetitive ports, behaviors or connections: [\langle direction \rangle] (\langle position \rangle) (\langle position \rangle) \langle direction \rangle can be h or v.
```

 $\langle position \rangle$ is any positioning tikz can understand, including cells, ports or any anchor defined by them, calculations on positions.

```
\inetmulticell{A}{5}{3};
\inetport(A.pax 1)
\inetport(A.pax 2)
\inetport(A.pax 3)
\inetport(A.pal 1)
\inetport(A.pal 3)
\inetport(A.pal 4)
\inetport(A.pal 5)
\inetdotsbetween(A.above pal 1)(A.above pal 3)
\inetbrace(A.pal 1)(A.pal 3){First group}
```

The three dots can be used between any two positions and can thus be used to signify an unsepcified number of cells for instance.

7 Known issues

Simple cells of arity 1 In the case of a simple cell with defined arity 1, the port .pax 1 returns a divide by θ error. It is well defined if the multicell has coarity at least 2. This problem can arise in the case of automation of tikz-multinet creation. Otherwise:

Temporary solution: just use .pax instead.