

Part II: Analysis and Forecast Modelling

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Contents

Defining Weather Elements as Time Series Objects	1
Train and Test Data Exploration	2
Inspect seasonal patterns from weather elements	3
Analyse trend in daily minimum and maximum temperature	9
Building models to predict maximum temperature	10
1. Linear model with a Fourier term to capture seasonality	10
2. Dynamic Regression with ARIMA(2,0,2) error	13
3. Dynamic Regression with ARIMA(5,1,0) error	17
4. Dynamic Regression with ARIMA(2,0,2) error and lag predictors	20
Use the best model (No.4) to build full temperature forecast	24
Building models to predict the number of extreme heat days	35

```
library(fpp)
library(fpp2)
library(forecast)
library(GGally)
library(knitr)
```

```
# Load cleaned data
full = read.csv("full.csv")
train = read.csv("train.csv")
test = read.csv("test.csv")
```

Defining Weather Elements as Time Series Objects

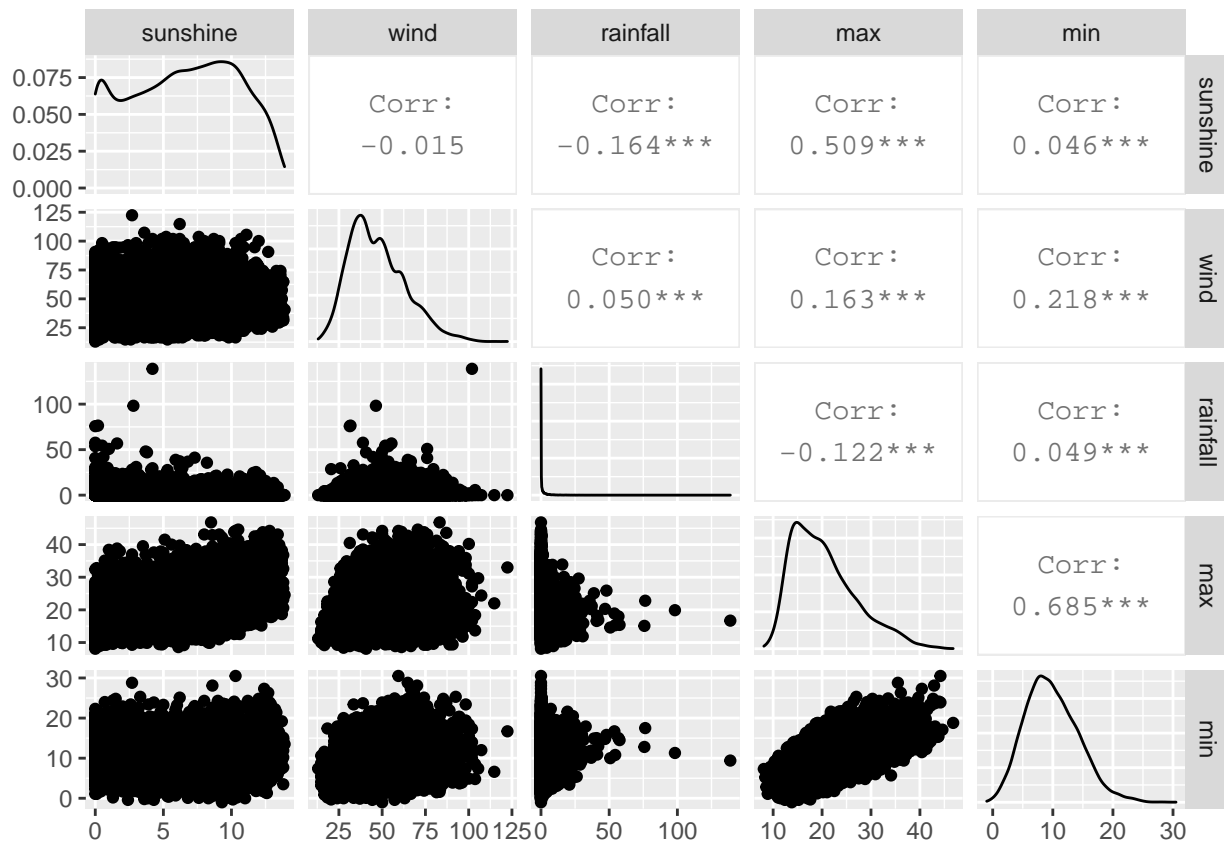
```
ts_full = ts(full, frequency = 365.25, start = c(1999, 230))
ts_train = ts(train, frequency = 365.25, start = c(1999, 230))
ts_test = ts(test, frequency = 365.25, start = c(2016, 55))

ts_max = ts_train[, "max"]
```

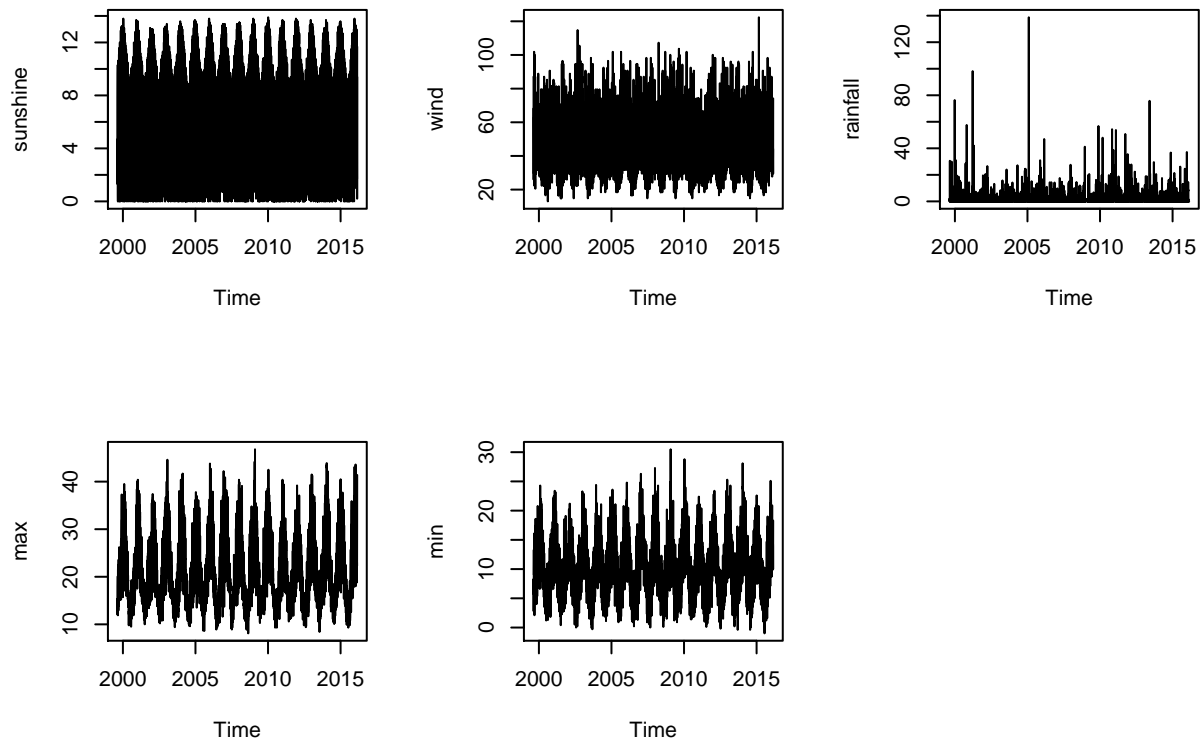
```
ts_min = ts_train[, "min"]
ts_sunshine = ts_train[, "sunshine"]
ts_wind = ts_train[, "wind"]
ts_rainfall = ts_train[, "rainfall"]
```

Train and Test Data Exploration

```
# Check variables correlations
GGally::ggpairs(train[, 1:5])
```

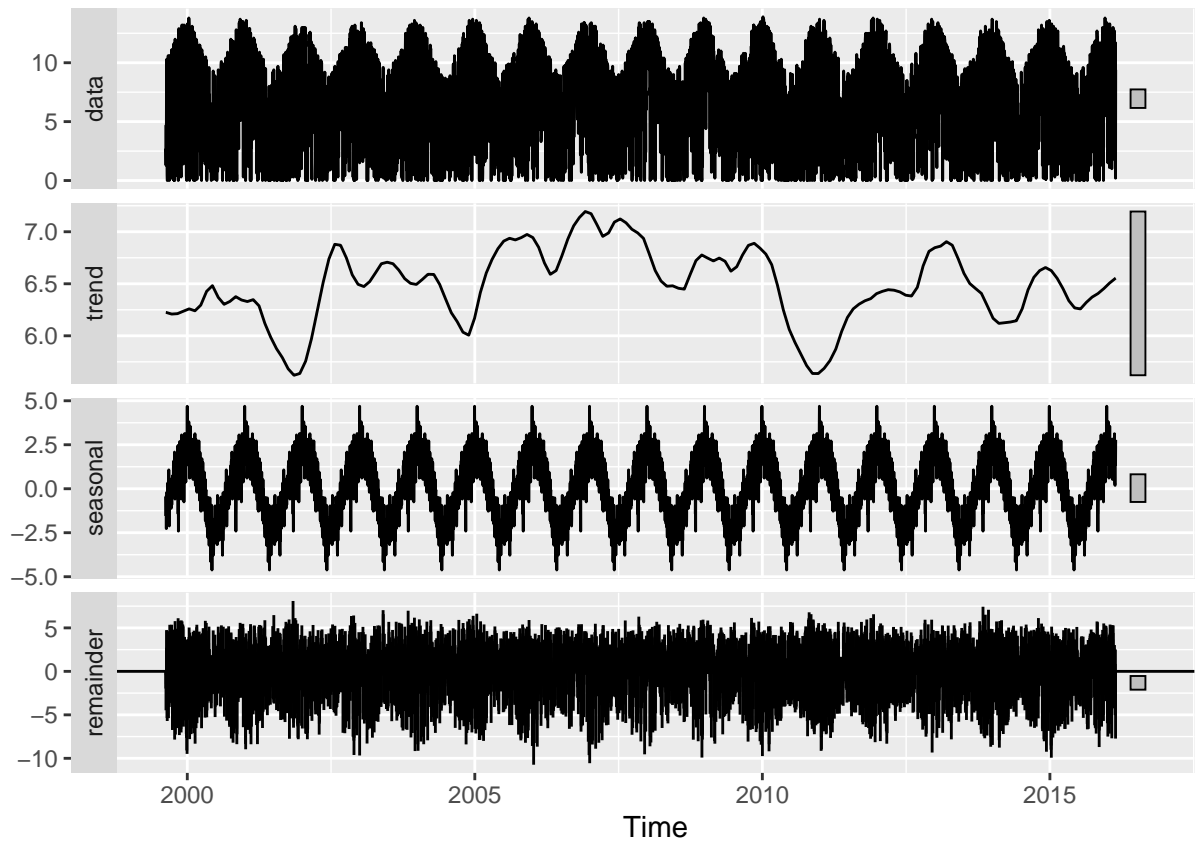


```
## Time series plots for weather elements
elements = colnames(ts_train)
par(mfrow = c(2, 3))
for (i in 1:5) {
  ts.plot(ts_train[, i], type = "l", ylab = elements[i])
}
```



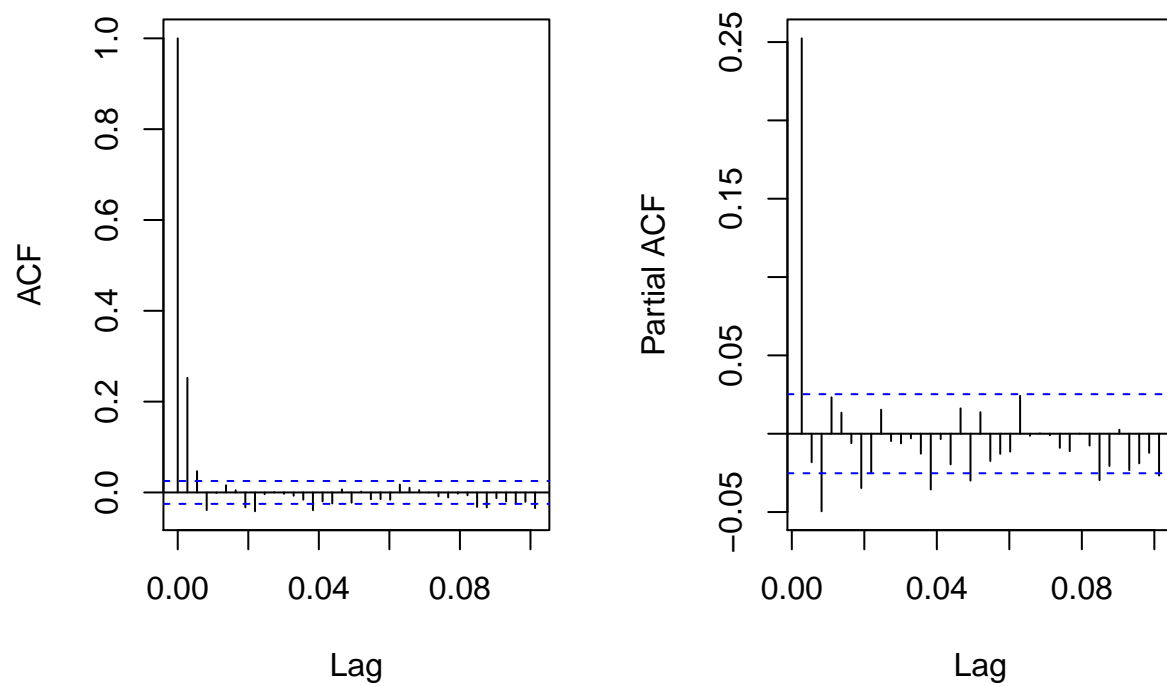
Inspect seasonal patterns from weather elements

```
# Sunshine -> seasonality, no trend
fitstl_sunshine = stl(ts_sunshine, t.window = 365.25, s.window = 365.25)
autoplot(fitstl_sunshine)
```

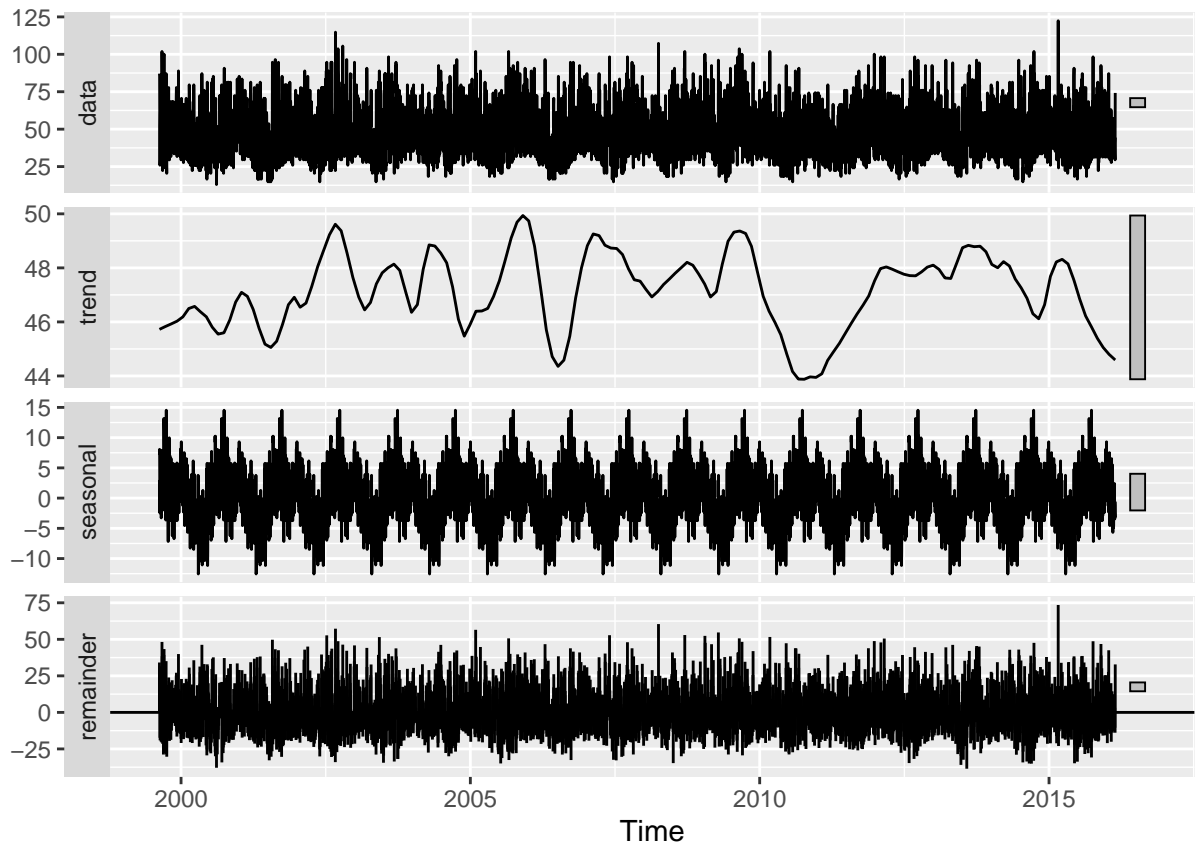


```
par(mfrow = c(1, 2))
acf(remainder(fitstl_sunshine), main = "ACF of residual from seasonal decomposition")
pacf(remainder(fitstl_sunshine), main = "PACF of residual from seasonal decomposition")
```

F of residual from seasonal decomposition

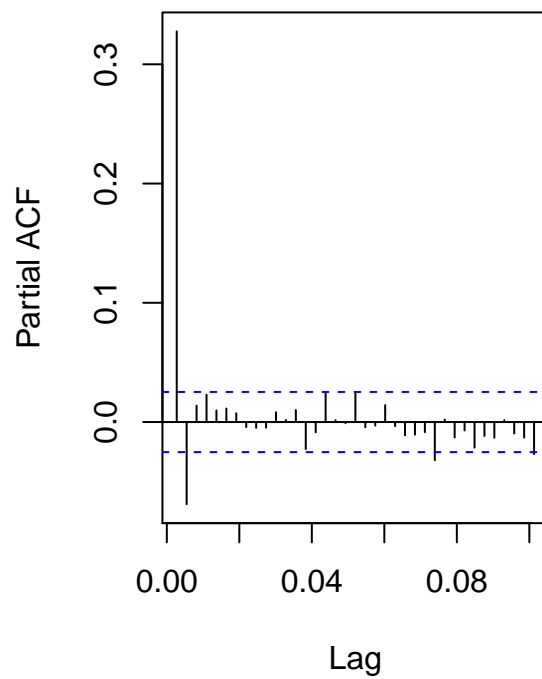
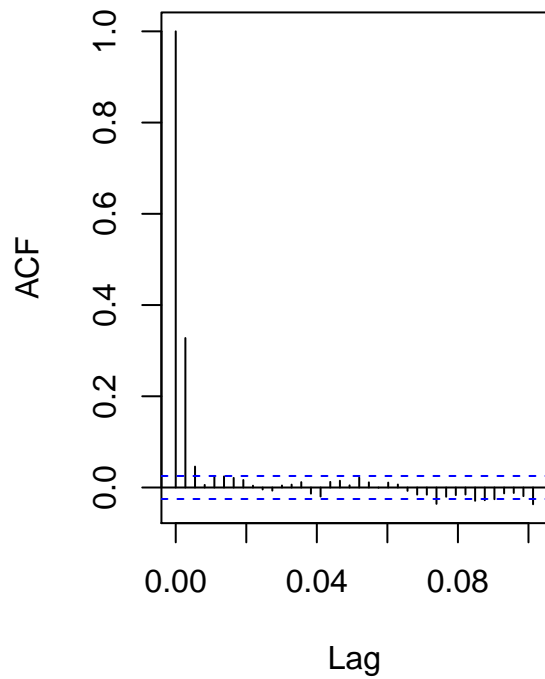


```
# wind -> seasonality, no trend
fitstl_wind = stl(ts_wind, t.window = 365.25, s.window = 365.25)
autoplot(fitstl_wind)
```

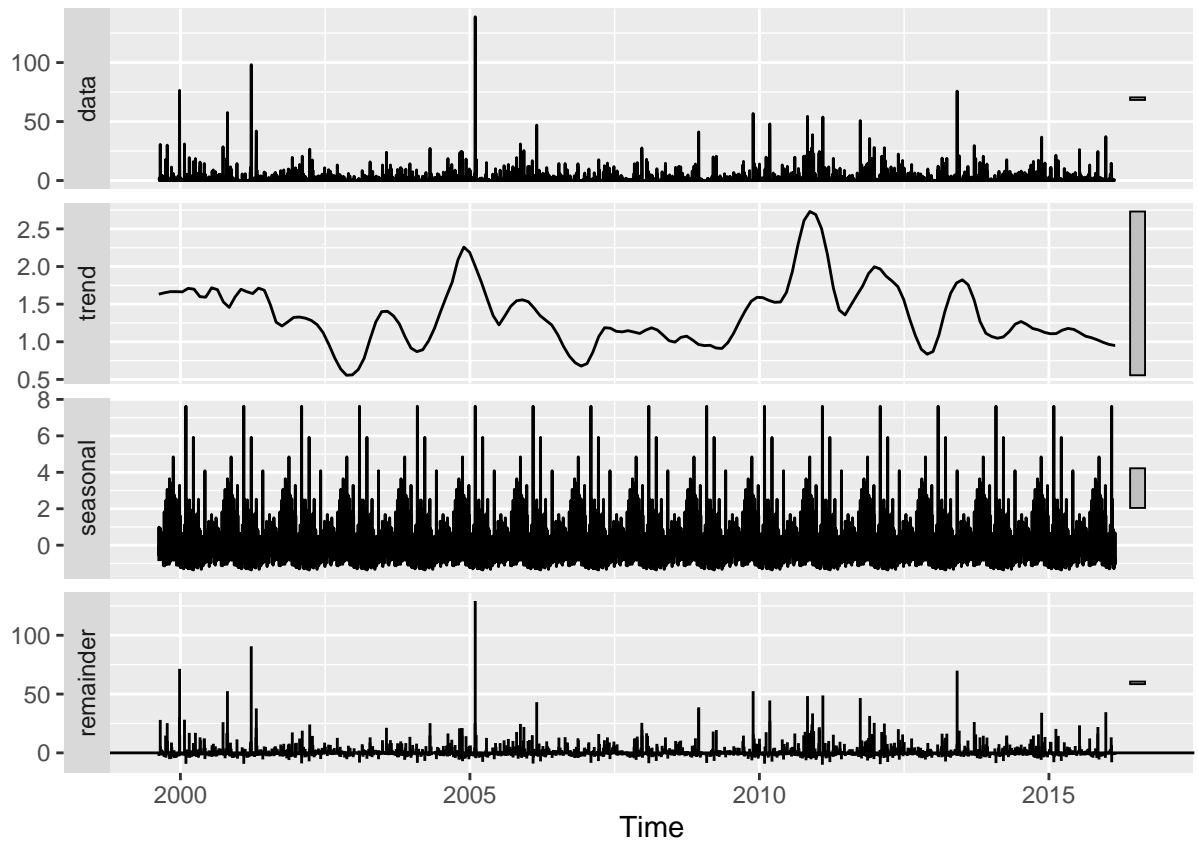


```
par(mfrow = c(1, 2))
acf(remainder(fitstl_wind), main = "ACF of residual from seasonal decomposition")
pacf(remainder(fitstl_wind), main = "PACF of residual from seasonal decomposition")
```

F of residual from seasonal decomposition

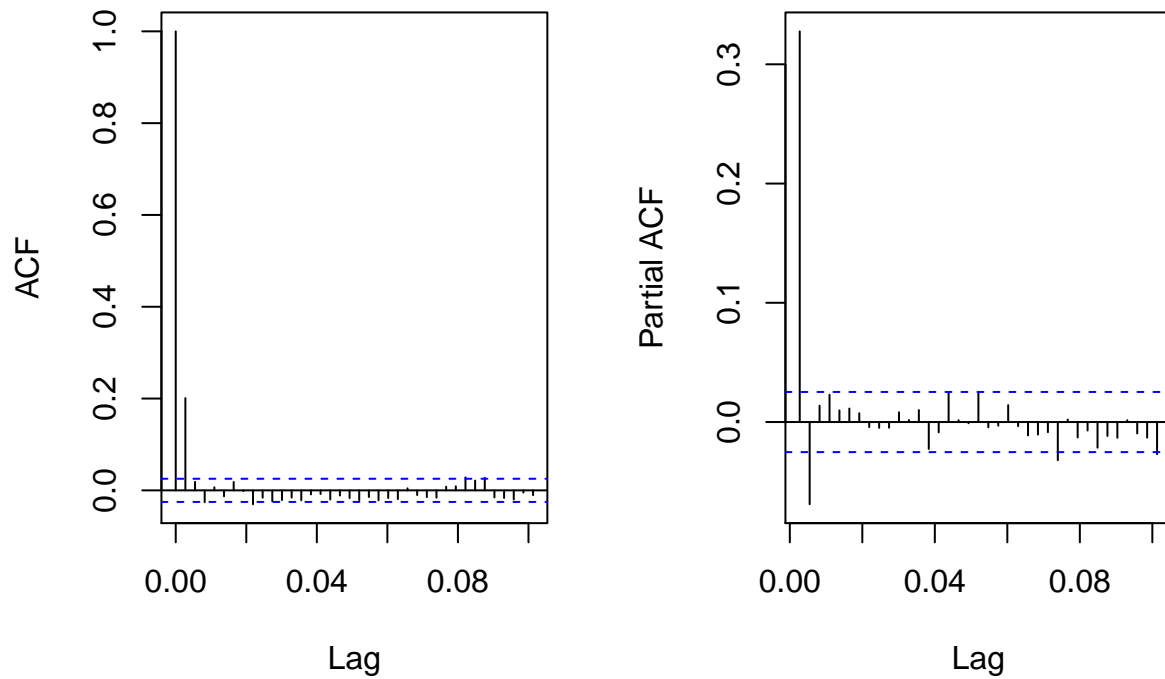


```
# rainfall -> no seasonality, no trend
fitstl_rainfall = stl(ts_rainfall, t.window = 365.25, s.window = 365.25)
autoplot(fitstl_rainfall)
```



```
par(mfrow = c(1, 2))
acf(remainder(fitstl_rainfall), main = "ACF of residual from seasonal decomposition")
pacf(remainder(fitstl_wind), main = "PACF of residual from seasonal decomposition")
```

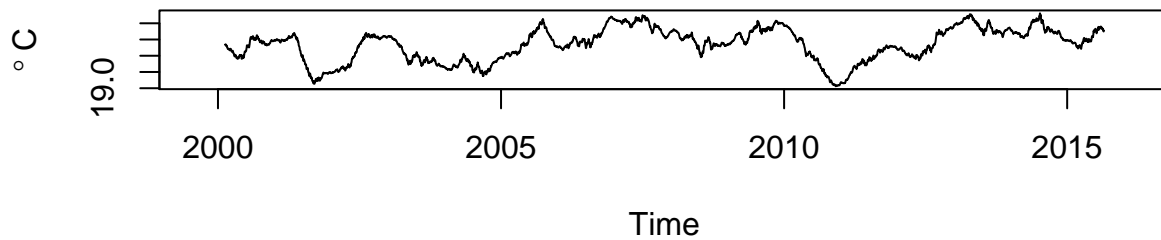

F of residual from seasonal decomposition



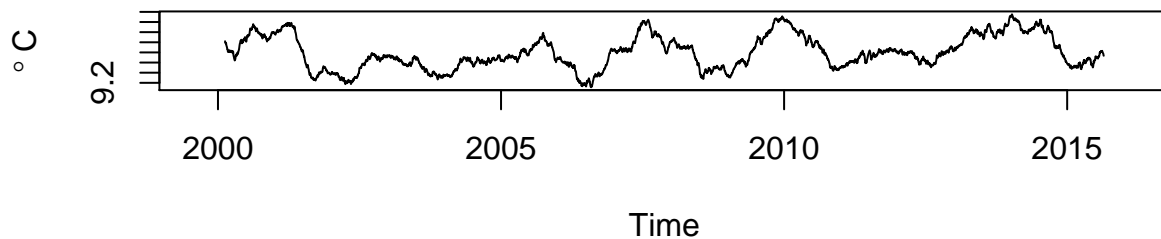
Analyse trend in daily minimum and maximum temperature

```
## use moving average
par(mfrow = c(2, 1))
plot(ma(ts_max, order = 365), main = "Moving Average for Max Temperature", ylab =
  ↳ expression(degree ~
    C))
plot(ma(ts_min, order = 365), main = "Moving Average for Min Temperature", ylab =
  ↳ expression(degree ~
    C))
```

Moving Average for Max Temperature



Moving Average for Min Temperature



Building models to predict maximum temperature

1. Linear model with a Fourier term to capture seasonality

```
# Fit a linear trend with seasonality using tslm()
tslm_max = tslm(ts_max ~ trend + ts_rainfall + ts_sunshine + ts_wind + fourier(ts_max,
  K = 2))
summary(tslm_max)
```

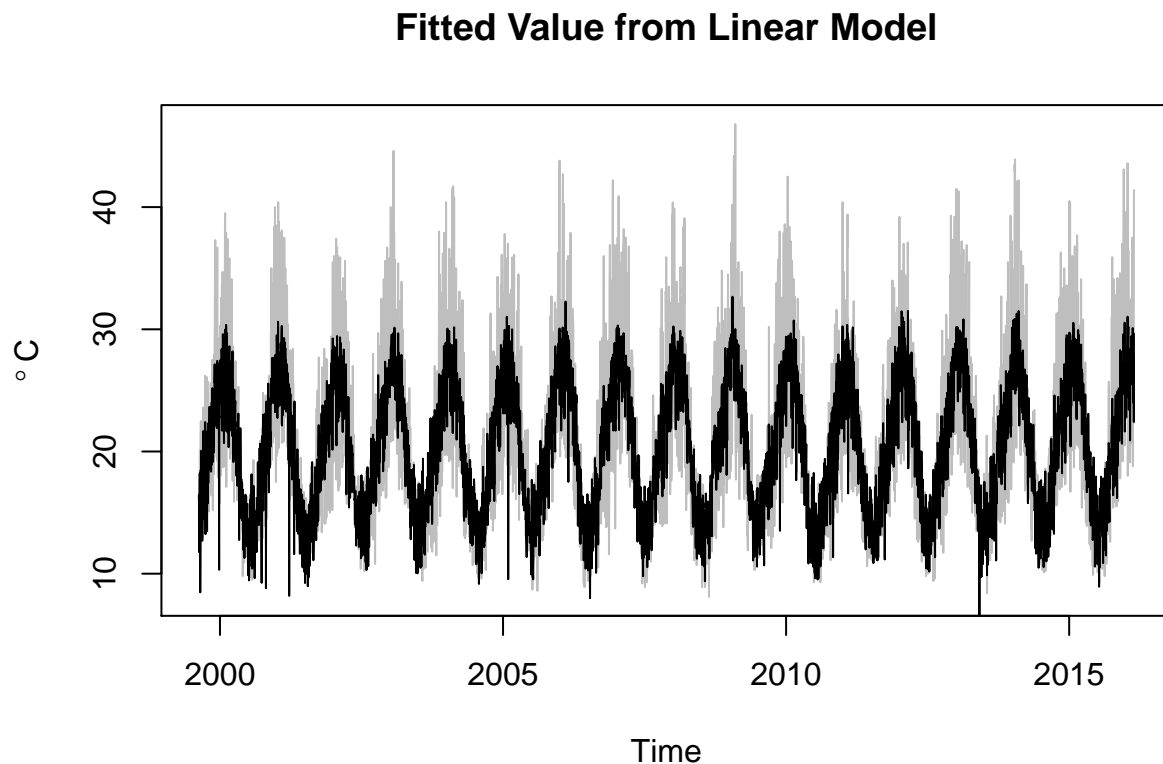
```
##
## Call:
## tslm(formula = ts_max ~ trend + ts_rainfall + ts_sunshine + ts_wind +
##       fourier(ts_max, K = 2))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14.2130  -2.6097  -0.2136   2.1744  16.7789
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.399e+01  2.082e-01  67.215  < 2e-16 ***
## trend        1.051e-04  2.913e-05   3.608  0.000311 ***
```

```
## ts_rainfall          -1.428e-01  1.103e-02 -12.956 < 2e-16 ***
## ts_sunshine          4.364e-01  1.461e-02  29.870 < 2e-16 ***
## ts_wind              7.269e-02  3.192e-03  22.774 < 2e-16 ***
## fourier(ts_max, K = 2)S1-365  2.338e+00  7.663e-02  30.508 < 2e-16 ***
## fourier(ts_max, K = 2)C1-365 -5.446e+00  7.522e-02 -72.401 < 2e-16 ***
## fourier(ts_max, K = 2)S2-365  4.179e-01  7.187e-02   5.815 6.39e-09 ***
## fourier(ts_max, K = 2)C2-365  3.168e-01  7.210e-02   4.394 1.13e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.94 on 6025 degrees of freedom
## Multiple R-squared:  0.6409, Adjusted R-squared:  0.6404
## F-statistic: 1344 on 8 and 6025 DF,  p-value: < 2.2e-16
```

```
AIC(tslm_max) # AIC = 33683.01
```

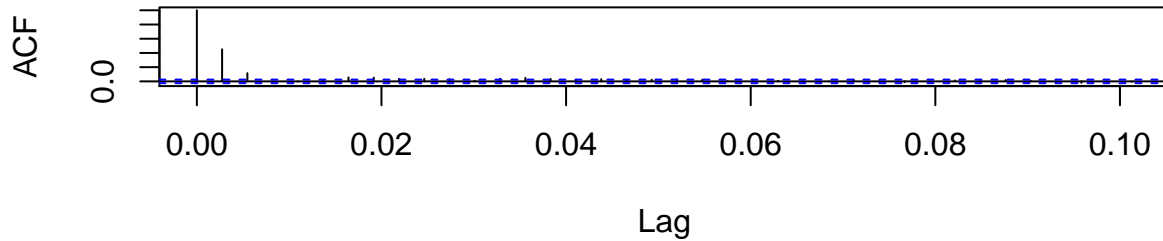
```
## [1] 33683.01
```

```
plot(ts_max, col = "grey", main = "Fitted Value from Linear Model", ylab =
  ↪ expression(degree ~
  C))
lines(tslm_max$fitted.values)
```

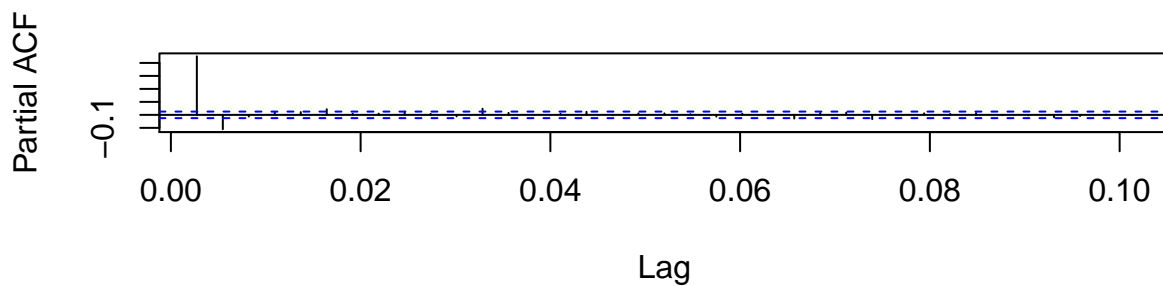


```
## Model diagnosis
par(mfrow = c(2, 1))
acf(tslm_max$residuals, main = "ACF of residual from fitted model") # lag q = 2
pacf(tslm_max$residuals, main = "PACF of residual from fitted model") # lag p = 2
```

ACF of residual from fitted model



PACF of residual from fitted model



```
Box.test(tslm_max$residuals, type = "Ljung") #autocorrelation different from 0
```

```
##
## Box-Ljung test
##
## data: tslm_max$residuals
## X-squared = 1228.3, df = 1, p-value < 2.2e-16
```

```
dwtest(tslm_max, alternative = "two")
```

```
##
## Durbin-Watson test
##
## data: tslm_max
## DW = 1.0964, p-value < 2.2e-16
## alternative hypothesis: true autocorrelation is not 0
```

```
bgtest(tslm_max, 20)
```

```
##
## Breusch-Godfrey test for serial correlation of order up to 20
##
## data:  tslm_max
## LM test = 1365.2, df = 20, p-value < 2.2e-16
```

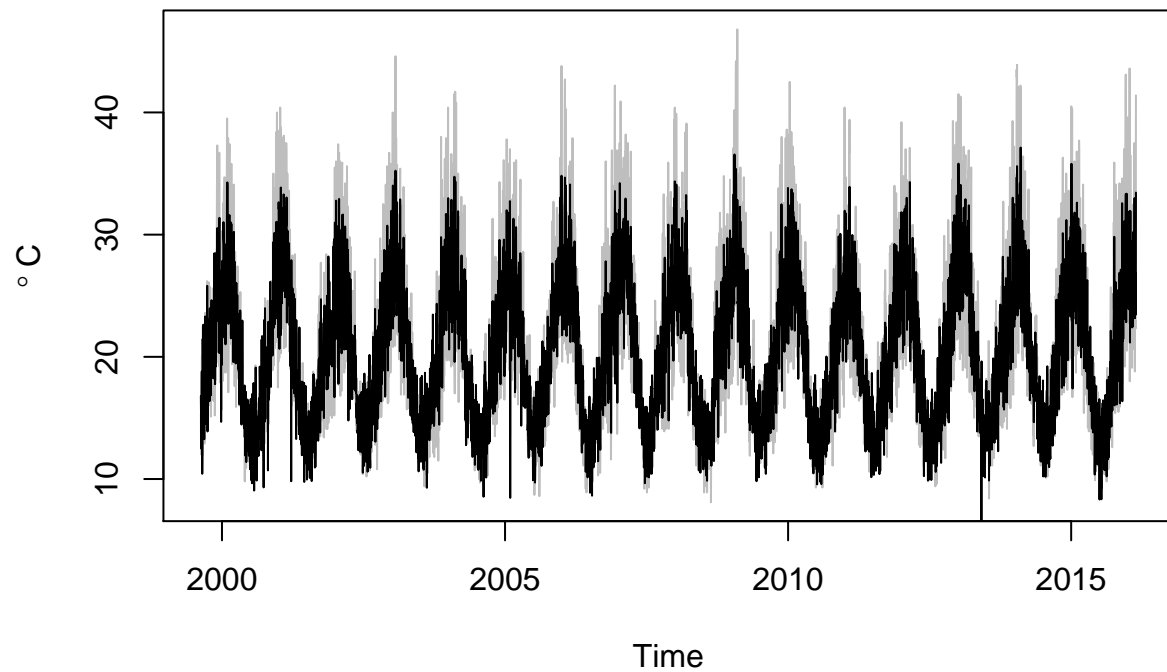
2. Dynamic Regression with ARIMA(2,0,2) error

```
# Fit a dynamic regression to capture the dynamics left in the residuals
dr_max = Arima(ts_max, xreg = cbind(ts_rainfall, ts_sunshine, ts_wind, fourier(ts_max,
  K = 2)), order = c(2, 0, 2))
summary(dr_max) # AIC = 32213.94
```

```
## Series: ts_max
## Regression with ARIMA(2,0,2) errors
##
## Coefficients:
##          ar1          ar2          ma1          ma2  intercept  ts_rainfall  ts_sunshine
##          0.3119 -0.0777  0.2000  0.0720    14.4956      -0.1114      0.3825
## s.e.      0.2973  0.0948  0.2974  0.0658     0.1857       0.0094      0.0129
##          ts_wind  fourier(ts_max, K = 2).S1-365  fourier(ts_max, K = 2).C1-365
##          0.0754                                2.4065                                -5.5318
## s.e.      0.0030                                0.1081                                0.1071
##          fourier(ts_max, K = 2).S2-365  fourier(ts_max, K = 2).C2-365
##          0.4200                                0.3435
## s.e.      0.1055                                0.1055
##
## sigma^2 estimated as 12.16: log likelihood=-16093.97
## AIC=32213.94  AICc=32214  BIC=32301.11
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.001506474 3.484254 2.624239 -2.377646 12.90383 0.5519211
##              ACF1
## Training set 0.0001884346
```

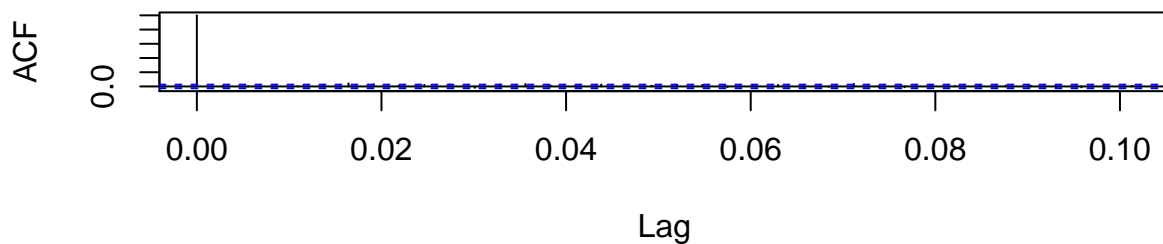
```
plot(ts_max, col = "grey", main = "Fitted Value from Dynamic Regression with ARIMA(2,0,2)
  errors",
  ylab = expression(degree ~ C))
lines(dr_max$fitted)
```

Fitted Value from Dynamic Regression with ARIMA(2,0,2) errors

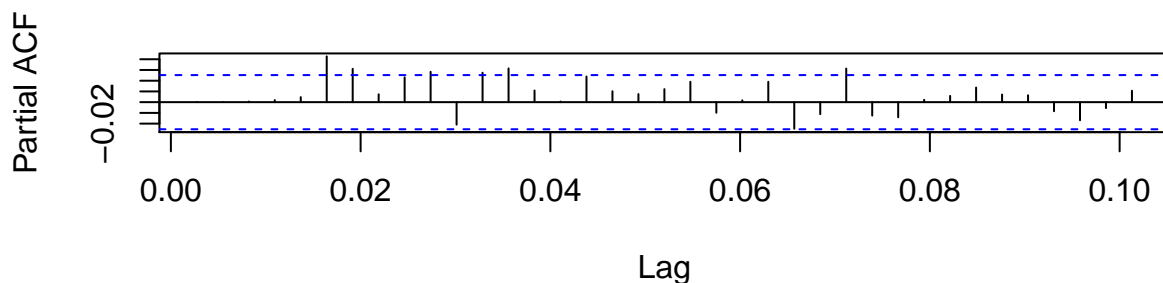


```
par(mfrow = c(2, 1))
acf(dr_max$residuals, main = "ACF of residual from fitted model")
pacf(dr_max$residuals, main = "PACF of residual from fitted model")
```

ACF of residual from fitted model



PACF of residual from fitted model



```
Box.test(dr_max$residuals)
```

```
##
## Box-Pierce test
##
## data: dr_max$residuals
## X-squared = 0.00021425, df = 1, p-value = 0.9883
```

```
## Construct a function to calculate p-value for fitted models
p_value = function(model) {
  t_fit = model$coef/(sqrt(diag(model$var.coef)))
  p_fit = 2 * pnorm(abs(t_fit), mean = 0, sd = 1, lower.tail = FALSE)

  return(p_fit)
}
p_value(dr_max)
```

```
##              ar1              ar2
##      2.941101e-01      4.124677e-01
##              ma1              ma2
##      5.012829e-01      2.741662e-01
##      intercept      ts_rainfall
##      0.000000e+00      2.011271e-32
##      ts_sunshine      ts_wind
```

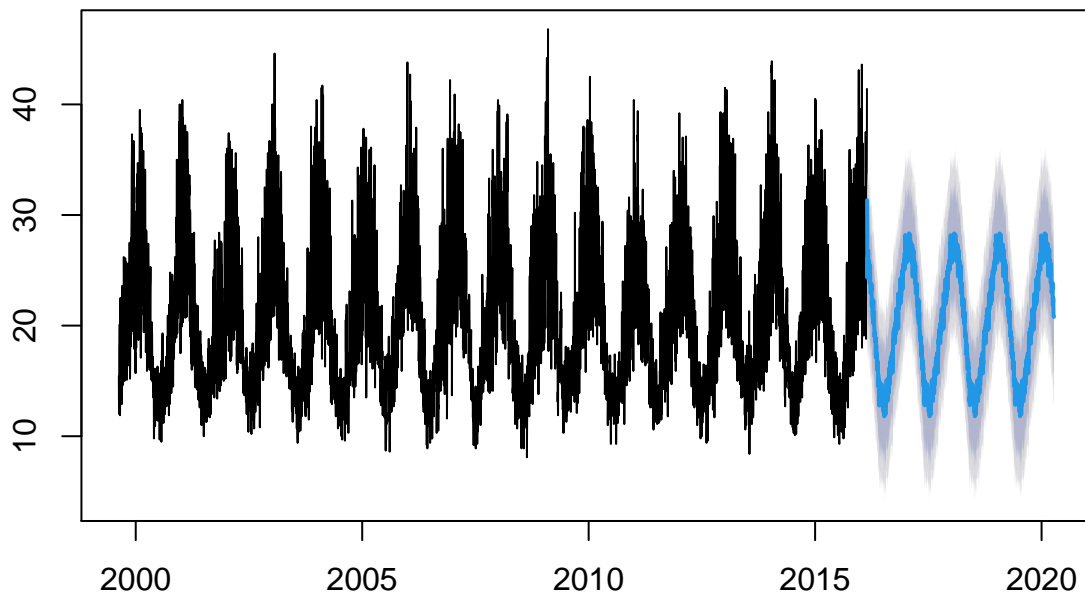
```
##          1.178194e-193          2.610144e-141
## fourier(ts_max, K = 2).S1-365 fourier(ts_max, K = 2).C1-365
##          1.079688e-109          0.000000e+00
## fourier(ts_max, K = 2).S2-365 fourier(ts_max, K = 2).C2-365
##          6.823194e-05          1.131803e-03
```

```
# Forecast using fitted model
fcast_rainfall = forecast(ts_rainfall, method = "ets", h = 1508)
fcast_sunshine = forecast(ts_sunshine, method = "ets", h = 1508)
fcast_wind = forecast(ts_wind, method = "ets", h = 1508)

fcast_xreg = cbind(fcast_rainfall$mean, fcast_sunshine$mean, fcast_wind$mean,
  ↪  fourier(ts_max,
    K = 2, h = 1508))
colnames(fcast_xreg) = names(dr_max$coef)[-c(1:5)]

fcast1 = forecast(dr_max, xreg = fcast_xreg, h = 1508)
par(mfrow = c(1, 1))
plot(fcast1)
```

Forecasts from Regression with ARIMA(2,0,2) errors



```
accuracy(fcast1, ts_test[, "max"])
```

```
##          ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.001506474 3.484254 2.624239 -2.3776465 12.90383 0.5519211
```



```
## Test set      0.630405671 4.546492 3.455661 -0.8162259 16.01995 0.7267829
##              ACF1 Theil's U
## Training set 0.0001884346      NA
## Test set     0.4054704347 0.9815607
```

3. Dynamic Regression with ARIMA(5,1,0) error

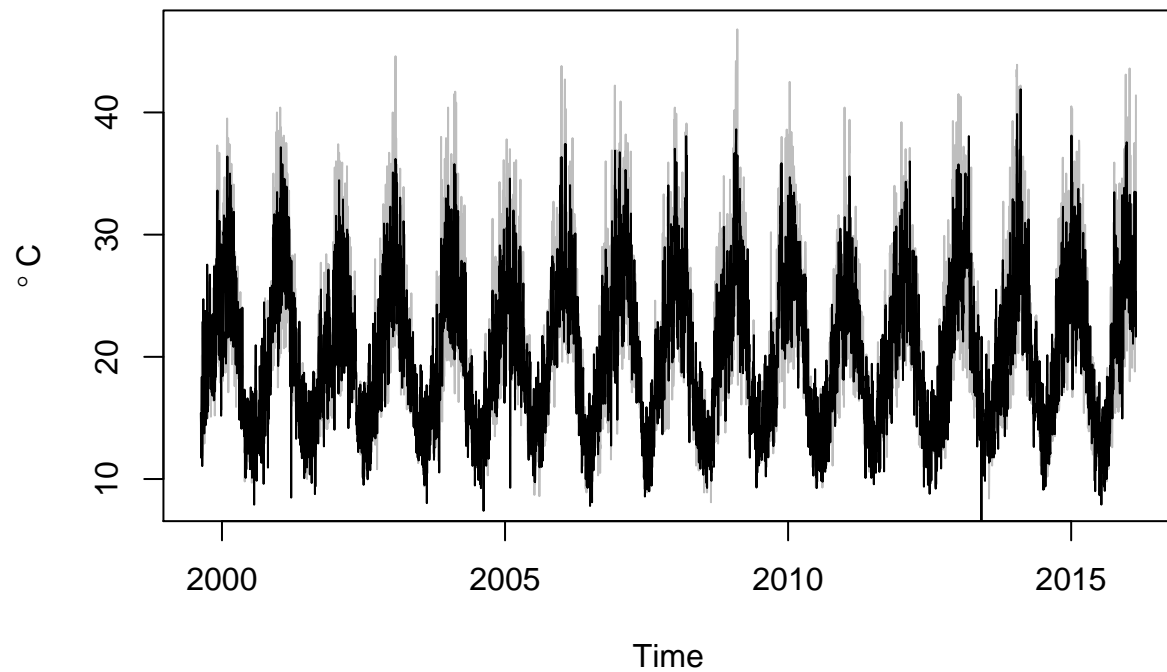
```
# Fit another dynamic regression using auto arima
dr2_max = auto.arima(ts_max, xreg = cbind(ts_rainfall, ts_sunshine, ts_wind,
  ↪  fourier(ts_max,
    K = 2)))

summary(dr2_max) # ARIMA(5,1,0), AIC = 32894.15

## Series: ts_max
## Regression with ARIMA(5,1,0) errors
##
## Coefficients:
##      ar1      ar2      ar3      ar4      ar5 ts_rainfall ts_sunshine
##      -0.3593 -0.4016 -0.3344 -0.2413 -0.1734      -0.1073      0.3773
## s.e.   0.0128  0.0132  0.0135  0.0132  0.0127      0.0093      0.0127
##      ts_wind fourier(ts_max, K = 2).S1-365 fourier(ts_max, K = 2).C1-365
##      0.0768                                2.3077                                -5.5230
## s.e.   0.0030                                1.5564                                1.5568
##      fourier(ts_max, K = 2).S2-365 fourier(ts_max, K = 2).C2-365
##      0.4726                                0.3174
## s.e.   0.7789                                0.7795
##
## sigma^2 estimated as 13.63: log likelihood=-16434.07
## AIC=32894.15 AICc=32894.21 BIC=32981.31
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.002838698 3.687538 2.751103 -2.09439 13.55714 0.5786026
##              ACF1
## Training set -0.02089691
```

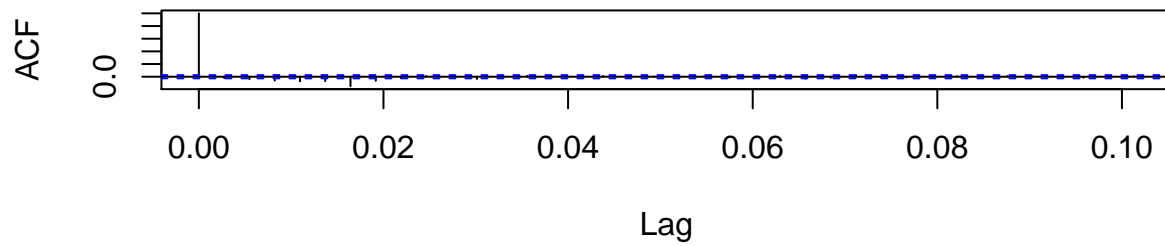
```
plot(ts_max, col = "grey", main = "Fitted Value from Dynamic Regression with ARIMA(5,1,0)
  ↪  errors",
  ylab = expression(degree ~ C))
lines(dr2_max$fitted)
```

Fitted Value from Dynamic Regression with ARIMA(5,1,0) errors

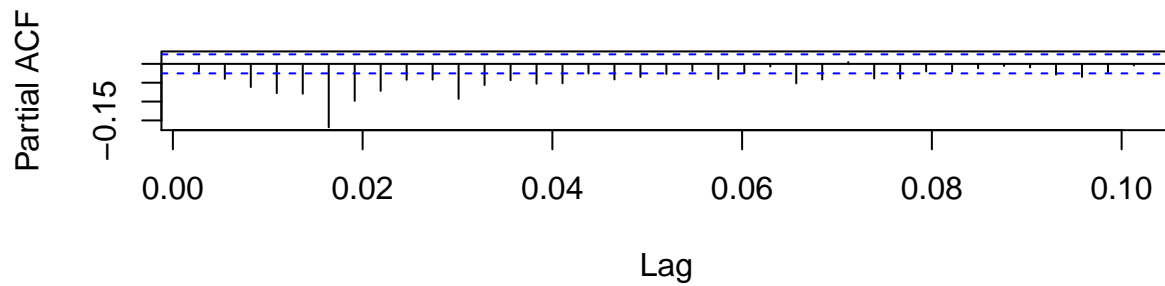


```
par(mfrow = c(2, 1))
acf(dr2_max$residuals, main = "ACF of residual from fitted model")
pacf(dr2_max$residuals, main = "PACF of residual from fitted model")
```

ACF of residual from fitted model



PACF of residual from fitted model

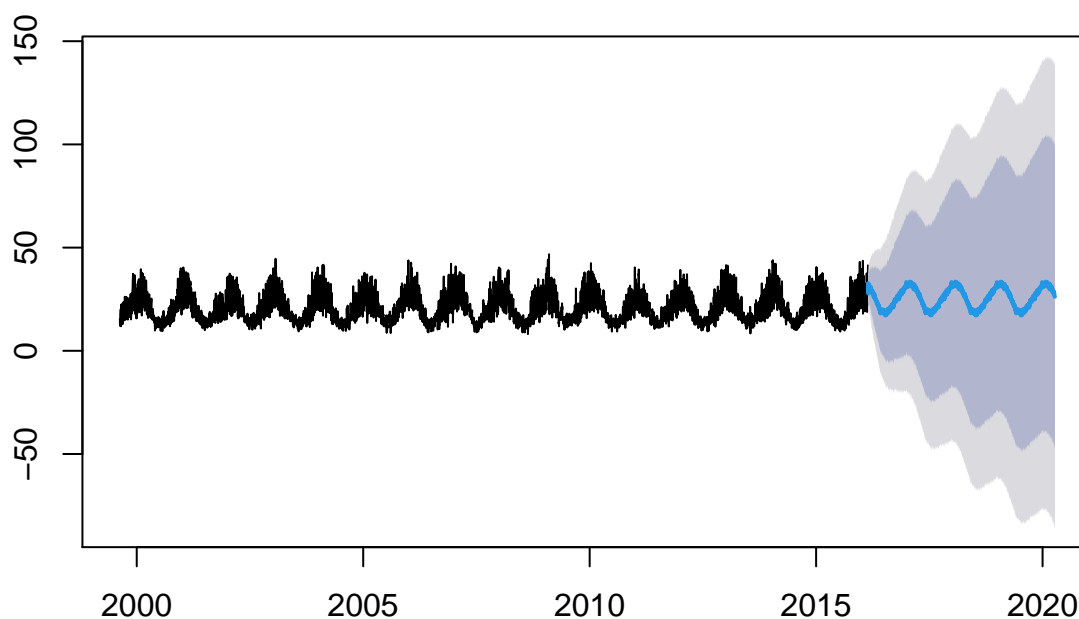


```
Box.test(dr2_max$residuals)
```

```
##  
## Box-Pierce test  
##  
## data: dr2_max$residuals  
## X-squared = 2.6349, df = 1, p-value = 0.1045
```

```
# Forecast using fitted model  
fcast2 = forecast(dr2_max, xreg = fcast_xreg, h = 1508)  
par(mfrow = c(1, 1))  
plot(fcast2)
```

Forecasts from Regression with ARIMA(5,1,0) errors



```
accuracy(fcast2, ts_test[, "max"])
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set  0.002838698 3.687538 2.751103 -2.09439 13.55714 0.5786026
## Test set     -4.654307073 6.478497 5.638558 -28.67872 31.51016 1.1858823
##               ACF1 Theil's U
## Training set -0.02089691      NA
## Test set     0.40549696  1.760783
```

4. Dynamic Regression with ARIMA(2,0,2) error and lag predictors

```
# Fit a dynamic regression with lag values
len_train = length(ts_train[, "max"])
lag1_sunshine = c(NA, ts_sunshine[1:(len_train - 1)])
lag2_sunshine = c(rep(NA, 2), ts_sunshine[1:(len_train - 2)])
lag1_rainfall = c(NA, ts_rainfall[1:(len_train - 1)])
lag2_rainfall = c(rep(NA, 2), ts_rainfall[1:(len_train - 2)])
lag1_wind = c(NA, ts_wind[1:(len_train - 1)])
lag2_wind = c(rep(NA, 2), ts_wind[1:(len_train - 2)])

drlag_max = Arima(ts_max, xreg = cbind(ts_rainfall, lag1_rainfall, lag2_rainfall,
  ts_sunshine, lag1_sunshine, lag2_sunshine, ts_wind, lag1_wind, lag2_wind,
  ↪  fourier(ts_max,
```

```

      K = 2)), order = c(2, 0, 2))
summary(drlag_max) #AIC = 31560.4

```

```

## Series: ts_max
## Regression with ARIMA(2,0,2) errors
##
## Coefficients:
##          ar1          ar2          ma1          ma2  intercept  ts_rainfall  lag1_rainfall
##          0.4347 -0.0893  0.0498  0.0541    15.4300    -0.0644    -0.0229
## s.e.      0.2797  0.1024  0.2797  0.0464     0.3204     0.0097     0.0102
##          lag2_rainfall ts_sunshine lag1_sunshine lag2_sunshine ts_wind
##          -0.0258      0.4175      0.2432      0.1182  0.0595
## s.e.      0.0094      0.0127      0.0136      0.0132  0.0029
##          lag1_wind lag2_wind  fourier(ts_max, K = 2).S1-365
##          -0.0502  -0.0083      2.0346
## s.e.      0.0029  0.0029      0.1118
##          fourier(ts_max, K = 2).C1-365  fourier(ts_max, K = 2).S2-365
##          -4.7925      0.3369
## s.e.      0.1099      0.1015
##          fourier(ts_max, K = 2).C2-365
##          0.3365
## s.e.      0.1021
##
## sigma^2 estimated as 10.92:  log likelihood=-15761.2
## AIC=31560.4  AICc=31560.52  BIC=31687.79
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.0001517959 3.300164 2.508675 -2.084281 12.45151 0.5276159
##              ACF1
## Training set 0.0001495279

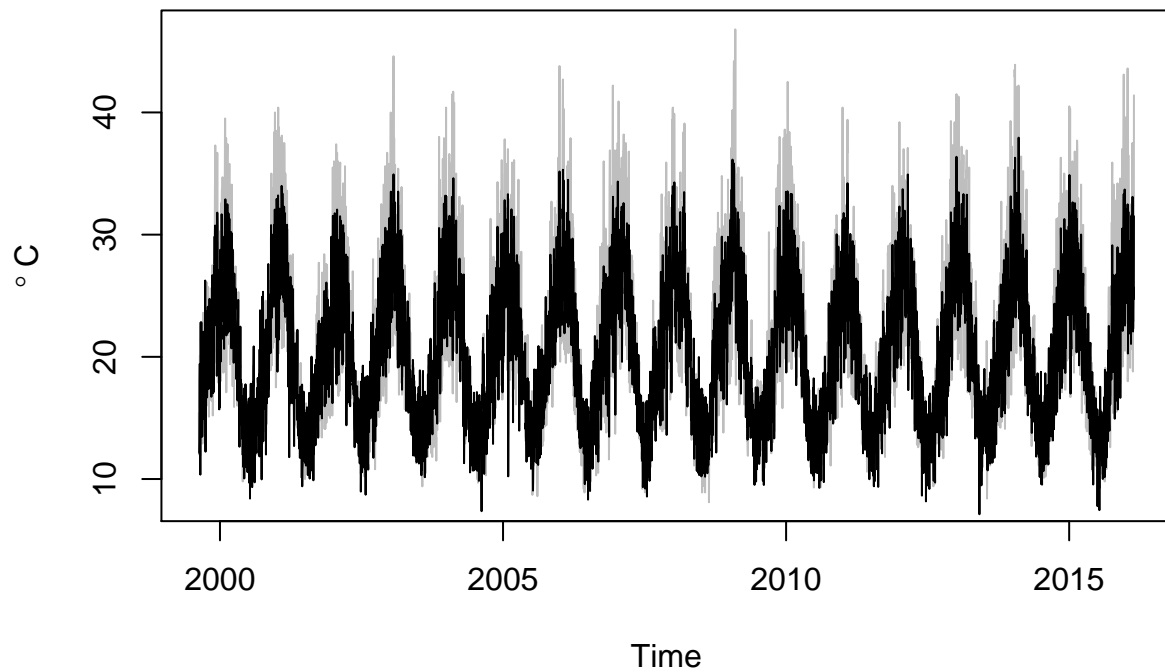
```

```

plot(ts_max, col = "grey", main = "Fitted value from Dynamic Regression with ARIMA(2,0,2)
  ↪ errors",
      ylab = expression(degree ~ C))
lines(drlag_max$fitted)

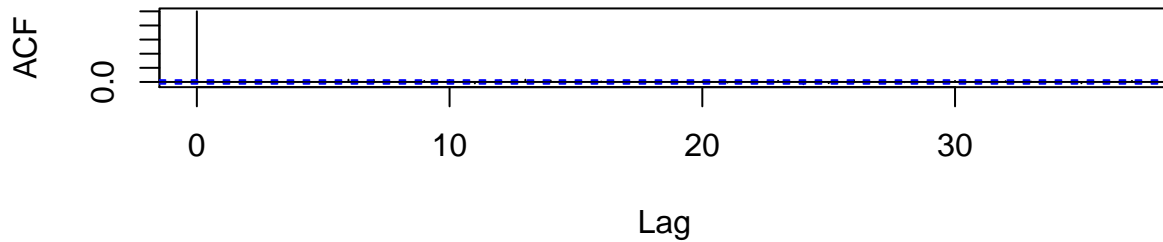
```

Fitted value from Dynamic Regression with ARIMA(2,0,2) errors

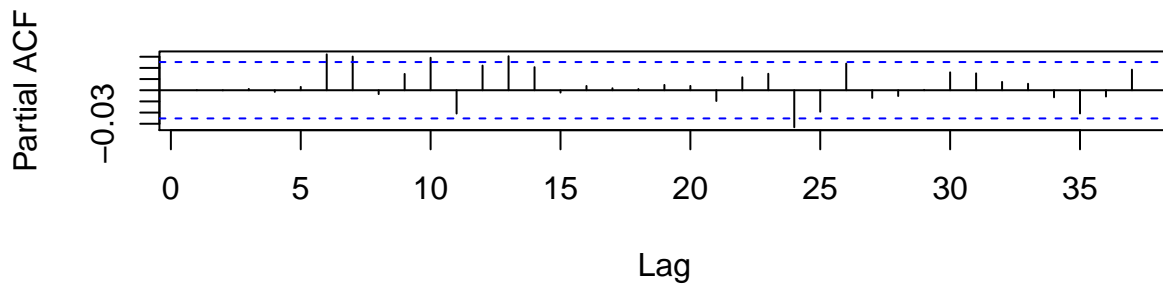


```
par(mfrow = c(2, 1))
acf(drlag_max$residuals[3:len_train], main = "ACF of residual from fitted model")
pacf(drlag_max$residuals[3:len_train], main = "PACF of residual from fitted model")
```

ACF of residual from fitted model



PACF of residual from fitted model



```
Box.test(drlag_max$residuals)
```

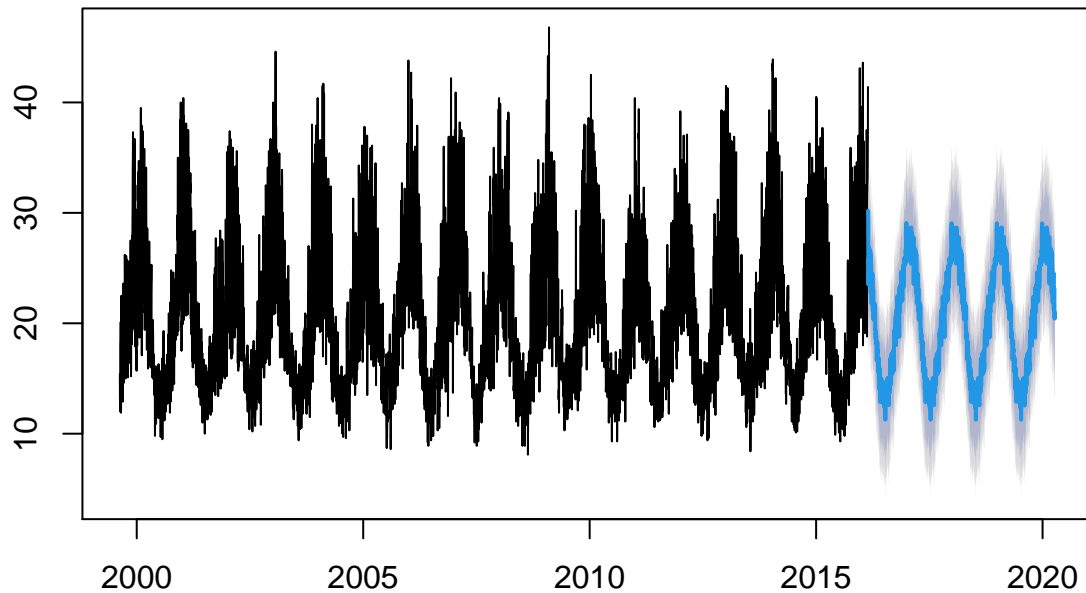
```
##
## Box-Pierce test
##
## data: drlag_max$residuals
## X-squared = 0.00013487, df = 1, p-value = 0.9907
```

```
# Forecast using fitted model
fcast_lag1_rainfall = c(ts_sunshine[6034], fcast_rainfall$mean[1:1507])
fcast_lag2_rainfall = c(ts_sunshine[6033:6034], fcast_rainfall$mean[1:1506])
fcast_lag1_sunshine = c(ts_sunshine[6034], fcast_sunshine$mean[1:1507])
fcast_lag2_sunshine = c(ts_sunshine[6033:6034], fcast_sunshine$mean[1:1506])
fcast_lag1_wind = c(ts_wind[6034], fcast_wind$mean[1:1507])
fcast_lag2_wind = c(ts_wind[6033:6034], fcast_wind$mean[1:1506])

fcast_lag_xreg = cbind(fcast_rainfall$mean, fcast_lag1_rainfall, fcast_lag2_rainfall,
  fcast_sunshine$mean, fcast_lag1_sunshine, fcast_lag2_sunshine, fcast_wind$mean,
  fcast_lag1_wind, fcast_lag2_wind, fourier(ts_max, K = 2, h = 1508))
colnames(fcast_lag_xreg) = names(drlag_max$coef)[-c(1:5)]

fcast3 = forecast(drlag_max, xreg = fcast_lag_xreg, h = 1508)
par(mfrow = c(1, 1))
plot(fcast3)
```

Forecasts from Regression with ARIMA(2,0,2) errors



```
accuracy(fcast3, ts_test[, "max"])
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.0001517959 3.300164 2.508675 -2.084281 12.45151 0.5276159
## Test set      0.5938947740 4.569709 3.483299 -0.980496 16.21407 0.7325955
##               ACF1 Theil's U
## Training set 0.0001495279      NA
## Test set      0.4080117323 0.9925416
```

Use the best model (No.4) to build full temperature forecast

```
full_len = length(ts_full[, "max"])
full_max = ts_full[, "max"]
full_sunshine = ts_full[, "sunshine"]
full_rainfall = ts_full[, "rainfall"]
full_wind = ts_full[, "wind"]

full_lag1_sunshine = c(NA, full_sunshine[1:(full_len - 1)])
full_lag2_sunshine = c(rep(NA, 2), full_sunshine[1:(full_len - 2)])
full_lag1_rainfall = c(NA, full_rainfall[1:(full_len - 1)])
full_lag2_rainfall = c(rep(NA, 2), full_rainfall[1:(full_len - 2)])
full_lag1_wind = c(NA, full_wind[1:(full_len - 1)])
full_lag2_wind = c(rep(NA, 2), full_wind[1:(full_len - 2)])
```

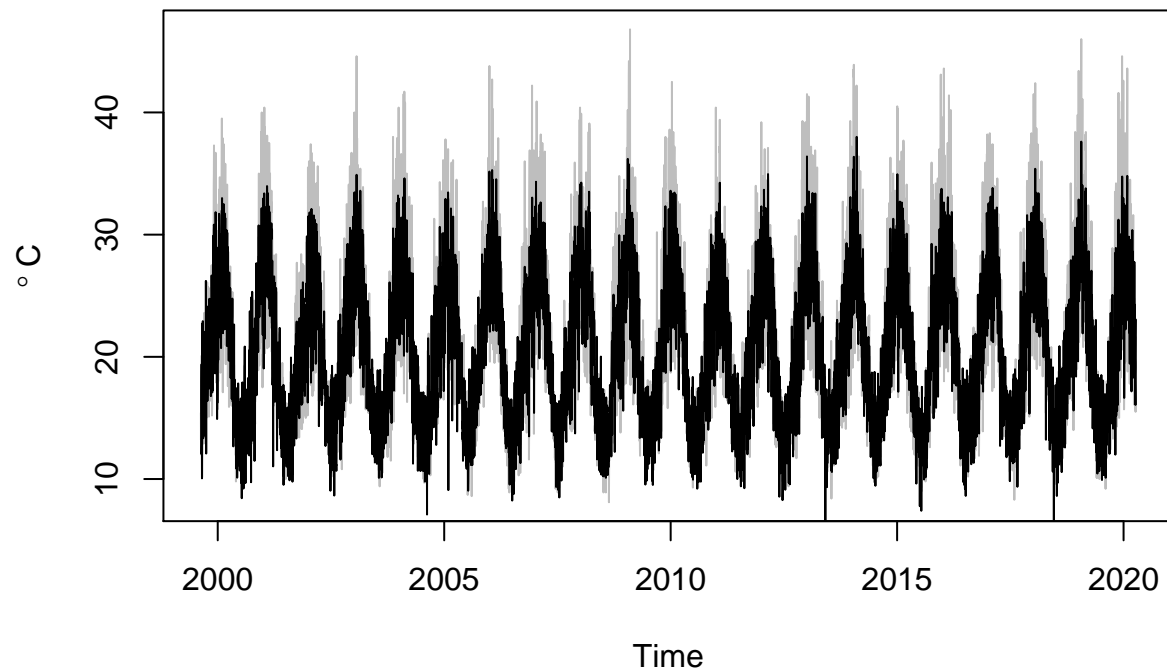


```
finaldr_max = Arima(full_max, xreg = cbind(full_sunshine, full_lag1_sunshine,
↪ full_lag2_sunshine,
    full_rainfall, full_lag1_rainfall, full_lag2_rainfall, full_wind, full_lag1_wind,
    full_lag2_wind, fourier(full_max, K = 2)), order = c(2, 0, 2))
summary(finaldr_max)
```

```
## Series: full_max
## Regression with ARIMA(2,0,2) errors
##
## Coefficients:
##          ar1      ar2      ma1      ma2  intercept  full_sunshine
##          0.2189  0.0077  0.2545  0.0523   15.4908         0.4090
## s.e.      1.1741  0.4071  1.1740  0.1503    0.2885         0.0114
##          full_lag1_sunshine  full_lag2_sunshine  full_rainfall  full_lag1_rainfall
##                               0.2382              0.1203          -0.0749          -0.0305
## s.e.                        0.0122              0.0119          0.0087          0.0091
##          full_lag2_rainfall  full_wind  full_lag1_wind  full_lag2_wind
##                               -0.0253      0.0620          -0.0495          -0.0091
## s.e.                        0.0084      0.0026          0.0026          0.0026
##          fourier(full_max, K = 2).S1-365  fourier(full_max, K = 2).C1-365
##                               2.0328              -4.9460
## s.e.                        0.1004              0.0989
##          fourier(full_max, K = 2).S2-365  fourier(full_max, K = 2).C2-365
##                               0.3476              0.3008
## s.e.                        0.0914              0.0923
##
## sigma^2 estimated as 11.07:  log likelihood=-19754.23
## AIC=39546.45  AICc=39546.55  BIC=39678.08
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.0001978426  3.323339  2.533286 -2.096745  12.53738  0.5317751
##              ACF1
## Training set 1.017968e-05
```

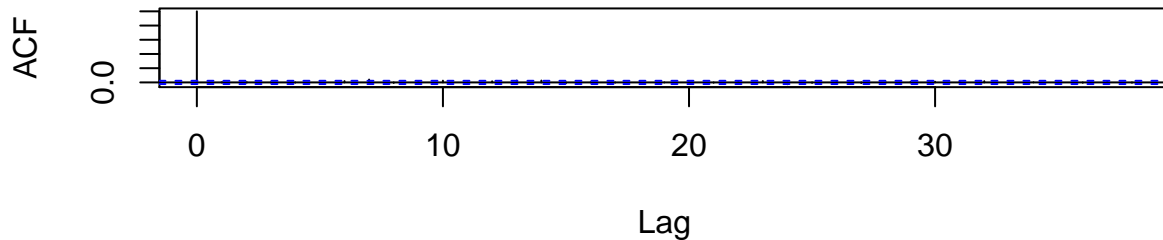
```
plot(full_max, col = "grey", main = "Fitted value from predictive model for max
↪ temperature",
    ylab = expression(degree ~ C))
lines(finaldr_max$fitted)
```

Fitted value from predictive model for max temperature

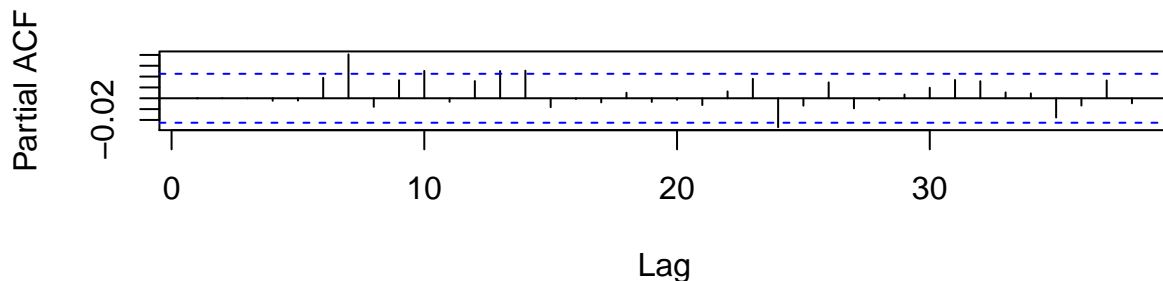


```
par(mfrow = c(2, 1))
acf(finaldr_max$residuals[3:full_len], main = "ACF of residual from fitted model")
pacf(finaldr_max$residuals[3:full_len], main = "PACF of residual from fitted model")
```

ACF of residual from fitted model



PACF of residual from fitted model



```
Box.test(finaldr_max$residuals)
```

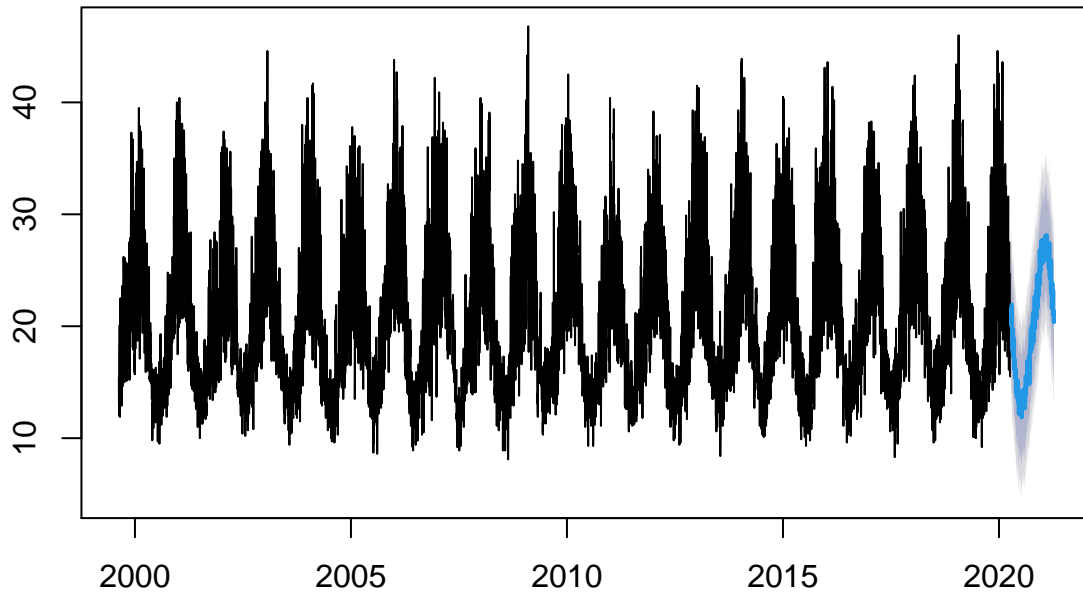
```
##
## Box-Pierce test
##
## data: finaldr_max$residuals
## X-squared = 7.8134e-07, df = 1, p-value = 0.9993
```

```
## build forecast
fcast_full_sunshine = forecast(full_sunshine, method = "ets", h = 365)
fcast_full_rainfall = forecast(full_rainfall, method = "ets", h = 365)
fcast_full_wind = forecast(full_wind, method = "ets", h = 365)
fcast_full_lag1_sunshine = c(full_sunshine[7542], fcast_full_sunshine$mean[1:364])
fcast_full_lag2_sunshine = c(full_sunshine[7541:7542], fcast_full_sunshine$mean[1:363])
fcast_full_lag1_rainfall = c(full_rainfall[7542], fcast_full_rainfall$mean[1:364])
fcast_full_lag2_rainfall = c(full_rainfall[7541:7542], fcast_full_rainfall$mean[1:363])
fcast_full_lag1_wind = c(full_wind[7542], fcast_full_wind$mean[1:364])
fcast_full_lag2_wind = c(full_wind[7541:7542], fcast_full_wind$mean[1:363])

fcast_full_xreg = cbind(fcast_full_sunshine$mean, fcast_full_lag1_sunshine,
  ↪ fcast_full_lag2_sunshine,
  fcast_full_rainfall$mean, fcast_full_lag1_rainfall, fcast_full_lag2_rainfall,
  fcast_full_wind$mean, fcast_full_lag1_wind, fcast_full_lag2_wind, fourier(full_max,
    K = 2, h = 365))
colnames(fcast_full_xreg) = names(finaldr_max$coef)[-c(1:5)]
```

```
fcast_full_max = forecast(finaldr_max, xreg = fcast_full_xreg, h = 365)
par(mfrow = c(1, 1))
plot(fcast_full_max)
```

Forecasts from Regression with ARIMA(2,0,2) errors



```
max_temperature_result = data.frame(seq(as.Date("2020-04-11"), by = "days", length.out =
  ↪ 365),
  round(fcast_full_max$mean, 2))
colnames(max_temperature_result) = c("Date", "Forecasted Max Temperature")

kable(max_temperature_result)
```

Date	Forecasted Max Temperature
2020-04-11	20.33
2020-04-12	21.22
2020-04-13	21.65
2020-04-14	20.05
2020-04-15	20.47
2020-04-16	20.50
2020-04-17	20.35
2020-04-18	21.30

Date	Forecasted Max Temperature
2020-04-19	21.94
2020-04-20	19.57
2020-04-21	18.00
2020-04-22	18.88
2020-04-23	19.09
2020-04-24	18.97
2020-04-25	19.80
2020-04-26	18.57
2020-04-27	17.66
2020-04-28	17.97
2020-04-29	19.40
2020-04-30	18.79
2020-05-01	18.05
2020-05-02	18.22
2020-05-03	17.20
2020-05-04	18.19
2020-05-05	18.26
2020-05-06	18.94
2020-05-07	17.82
2020-05-08	17.30
2020-05-09	16.55
2020-05-10	16.24
2020-05-11	16.10
2020-05-12	16.97
2020-05-13	17.05
2020-05-14	16.72
2020-05-15	16.88
2020-05-16	16.20
2020-05-17	15.97
2020-05-18	16.00
2020-05-19	16.12
2020-05-20	15.30
2020-05-21	16.15
2020-05-22	15.57
2020-05-23	15.64
2020-05-24	14.92
2020-05-25	14.76
2020-05-26	15.04
2020-05-27	13.98
2020-05-28	15.00
2020-05-29	15.30
2020-05-30	14.43
2020-05-31	13.66
2020-06-01	14.15
2020-06-02	14.08
2020-06-03	13.59
2020-06-04	13.63
2020-06-05	14.47
2020-06-06	14.27
2020-06-07	14.32
2020-06-08	14.11
2020-06-09	15.11

Date	Forecasted Max Temperature
2020-06-10	15.13
2020-06-11	14.36
2020-06-12	13.26
2020-06-13	14.39
2020-06-14	13.57
2020-06-15	12.88
2020-06-16	12.77
2020-06-17	12.16
2020-06-18	12.66
2020-06-19	13.24
2020-06-20	13.85
2020-06-21	13.53
2020-06-22	14.04
2020-06-23	12.88
2020-06-24	13.28
2020-06-25	13.91
2020-06-26	13.41
2020-06-27	12.77
2020-06-28	13.45
2020-06-29	12.19
2020-06-30	13.05
2020-07-01	14.11
2020-07-02	13.55
2020-07-03	12.88
2020-07-04	12.15
2020-07-05	13.09
2020-07-06	13.47
2020-07-07	12.66
2020-07-08	12.55
2020-07-09	13.38
2020-07-10	12.08
2020-07-11	11.85
2020-07-12	13.27
2020-07-13	12.54
2020-07-14	13.18
2020-07-15	13.76
2020-07-16	13.82
2020-07-17	12.98
2020-07-18	12.76
2020-07-19	13.97
2020-07-20	13.28
2020-07-21	14.01
2020-07-22	13.18
2020-07-23	12.80
2020-07-24	13.65
2020-07-25	13.25
2020-07-26	13.35
2020-07-27	13.02
2020-07-28	14.38
2020-07-29	13.80
2020-07-30	14.21
2020-07-31	13.60

Date	Forecasted Max Temperature
2020-08-01	14.24
2020-08-02	12.98
2020-08-03	13.21
2020-08-04	13.99
2020-08-05	12.88
2020-08-06	12.65
2020-08-07	13.29
2020-08-08	13.85
2020-08-09	14.28
2020-08-10	13.22
2020-08-11	13.95
2020-08-12	13.82
2020-08-13	14.88
2020-08-14	15.51
2020-08-15	14.67
2020-08-16	14.06
2020-08-17	14.76
2020-08-18	14.59
2020-08-19	14.53
2020-08-20	14.61
2020-08-21	15.21
2020-08-22	15.56
2020-08-23	15.13
2020-08-24	15.11
2020-08-25	16.23
2020-08-26	16.87
2020-08-27	15.17
2020-08-28	15.47
2020-08-29	15.93
2020-08-30	16.61
2020-08-31	15.55
2020-09-01	15.01
2020-09-02	15.94
2020-09-03	16.29
2020-09-04	16.57
2020-09-05	16.69
2020-09-06	16.60
2020-09-07	16.73
2020-09-08	15.71
2020-09-09	15.25
2020-09-10	17.35
2020-09-11	16.64
2020-09-12	16.20
2020-09-13	16.94
2020-09-14	15.73
2020-09-15	14.84
2020-09-16	17.05
2020-09-17	16.95
2020-09-18	17.47
2020-09-19	18.09
2020-09-20	17.73
2020-09-21	18.07

Date	Forecasted Max Temperature
2020-09-22	17.92
2020-09-23	18.15
2020-09-24	17.67
2020-09-25	18.98
2020-09-26	19.69
2020-09-27	17.74
2020-09-28	17.85
2020-09-29	17.90
2020-09-30	18.72
2020-10-01	19.36
2020-10-02	19.95
2020-10-03	19.13
2020-10-04	18.77
2020-10-05	18.48
2020-10-06	17.97
2020-10-07	20.13
2020-10-08	18.70
2020-10-09	18.22
2020-10-10	19.01
2020-10-11	19.47
2020-10-12	20.21
2020-10-13	20.79
2020-10-14	19.97
2020-10-15	19.87
2020-10-16	19.96
2020-10-17	21.22
2020-10-18	20.33
2020-10-19	20.04
2020-10-20	18.58
2020-10-21	18.82
2020-10-22	19.83
2020-10-23	20.66
2020-10-24	20.64
2020-10-25	20.21
2020-10-26	20.48
2020-10-27	21.17
2020-10-28	22.63
2020-10-29	22.62
2020-10-30	21.42
2020-10-31	19.80
2020-11-01	19.96
2020-11-02	21.45
2020-11-03	21.89
2020-11-04	21.41
2020-11-05	21.43
2020-11-06	21.26
2020-11-07	21.75
2020-11-08	21.22
2020-11-09	21.66
2020-11-10	23.13
2020-11-11	22.90
2020-11-12	21.50

Date	Forecasted Max Temperature
2020-11-13	20.70
2020-11-14	21.53
2020-11-15	22.17
2020-11-16	23.28
2020-11-17	24.51
2020-11-18	23.34
2020-11-19	24.56
2020-11-20	23.74
2020-11-21	22.37
2020-11-22	23.04
2020-11-23	21.93
2020-11-24	21.64
2020-11-25	22.01
2020-11-26	22.03
2020-11-27	23.83
2020-11-28	24.71
2020-11-29	24.70
2020-11-30	24.12
2020-12-01	23.34
2020-12-02	23.57
2020-12-03	22.73
2020-12-04	22.87
2020-12-05	23.39
2020-12-06	24.88
2020-12-07	23.95
2020-12-08	23.91
2020-12-09	24.67
2020-12-10	25.43
2020-12-11	26.81
2020-12-12	25.36
2020-12-13	23.74
2020-12-14	24.91
2020-12-15	25.10
2020-12-16	25.92
2020-12-17	25.53
2020-12-18	26.10
2020-12-19	25.00
2020-12-20	25.06
2020-12-21	25.19
2020-12-22	26.65
2020-12-23	27.46
2020-12-24	27.19
2020-12-25	27.02
2020-12-26	27.68
2020-12-27	26.81
2020-12-28	25.81
2020-12-29	25.62
2020-12-30	26.13
2020-12-31	26.67
2021-01-01	27.03
2021-01-02	26.45
2021-01-03	27.68

Date	Forecasted Max Temperature
2021-01-04	26.70
2021-01-05	27.10
2021-01-06	25.67
2021-01-07	25.92
2021-01-08	26.06
2021-01-09	27.00
2021-01-10	26.44
2021-01-11	26.97
2021-01-12	26.03
2021-01-13	26.10
2021-01-14	27.03
2021-01-15	27.34
2021-01-16	26.94
2021-01-17	26.52
2021-01-18	27.35
2021-01-19	25.89
2021-01-20	26.30
2021-01-21	27.59
2021-01-22	26.74
2021-01-23	27.57
2021-01-24	27.73
2021-01-25	27.81
2021-01-26	28.06
2021-01-27	27.99
2021-01-28	27.97
2021-01-29	27.20
2021-01-30	26.56
2021-01-31	26.00
2021-02-01	27.30
2021-02-02	27.41
2021-02-03	27.58
2021-02-04	28.13
2021-02-05	27.59
2021-02-06	26.98
2021-02-07	28.11
2021-02-08	27.42
2021-02-09	26.32
2021-02-10	26.33
2021-02-11	26.60
2021-02-12	26.41
2021-02-13	27.41
2021-02-14	26.08
2021-02-15	25.96
2021-02-16	26.90
2021-02-17	26.24
2021-02-18	26.39
2021-02-19	26.17
2021-02-20	25.86
2021-02-21	26.50
2021-02-22	26.79
2021-02-23	26.52
2021-02-24	25.59

Date	Forecasted Max Temperature
2021-02-25	25.19
2021-02-26	26.69
2021-02-27	25.93
2021-02-28	26.04
2021-03-01	26.93
2021-03-02	27.46
2021-03-03	27.23
2021-03-04	25.11
2021-03-05	24.49
2021-03-06	24.28
2021-03-07	25.69
2021-03-08	25.36
2021-03-09	25.04
2021-03-10	25.43
2021-03-11	25.33
2021-03-12	25.04
2021-03-13	24.52
2021-03-14	24.60
2021-03-15	23.14
2021-03-16	24.41
2021-03-17	25.90
2021-03-18	24.60
2021-03-19	23.59
2021-03-20	23.00
2021-03-21	22.82
2021-03-22	22.99
2021-03-23	21.59
2021-03-24	23.56
2021-03-25	22.06
2021-03-26	22.43
2021-03-27	23.88
2021-03-28	23.84
2021-03-29	23.43
2021-03-30	22.39
2021-03-31	22.70
2021-04-01	22.21
2021-04-02	21.87
2021-04-03	22.36
2021-04-04	23.18
2021-04-05	21.67
2021-04-06	20.92
2021-04-07	21.39
2021-04-08	20.71
2021-04-09	20.36
2021-04-10	20.62

Building models to predict the number of extreme heat days