Multiple linear regression

Grading the professor

Many college courses conclude by giving students the opportunity to evaluate the course and the instructor anonymously. However, the use of these student evaluations as an indicator of course quality and teaching effectiveness is often criticized because these measures may reflect the influence of non-teaching related characteristics, such as the physical appearance of the instructor. The article titled, "Beauty in the classroom: instructors' pulchritude and putative pedagogical productivity" (Hamermesh and Parker, 2005) found that instructors who are viewed to be better looking receive higher instructional ratings. (Daniel S. Hamermesh, Amy Parker, Beauty in the classroom: instructors pulchritude and putative pedagogical productivity, *Economics of Education Review*, Volume 24, Issue 4, August 2005, Pages 369-376, ISSN 0272-7757, 10.1016/j.econedurev.2004.07.013. http://www.sciencedirect.com/science/article/pii/S0272775704001165.)

In this lab we will analyze the data from this study in order to learn what goes into a positive professor evaluation.

The data

The data were gathered from end of semester student evaluations for a large sample of professors from the University of Texas at Austin. In addition, six students rated the professors' physical appearance. (This is aslightly modified version of the original data set that was released as part of the replication data for Data Analysis Using Regression and Multilevel/Hierarchical Models (Gelman and Hill, 2007).) The result is a data frame where each row contains a different course and columns represent variables about the courses and professors.

load("more/evals.RData")

variable	description
score	average professor evaluation score: (1) very unsatisfactory - (5) excellent.
rank	rank of professor: teaching, tenure track, tenured.
ethnicity	ethnicity of professor: not minority, minority.
gender	gender of professor: female, male.
language	language of school where professor
	received education: english or
	non-english.
age	age of professor.
cls_perc_eval	percent of students in class who
	completed evaluation.
cls_did_eval	number of students in class who
	completed evaluation.
cls_students	total number of students in class.
cls_level	class level: lower, upper.
cls_profs	number of professors teaching sections in
	course in sample: single, multiple.
cls_credits	number of credits of class: one credit
	(lab, PE, etc.), multi credit.

variable	description
bty_f1lower	beauty rating of professor from lower
	level female: (1) lowest - (10) highest.
bty_f1upper	beauty rating of professor from upper
	level female: (1) lowest - (10) highest.
bty_f2upper	beauty rating of professor from second
	upper level female: (1) lowest - (10)
	highest.
bty_m1lower	beauty rating of professor from lower
	level male: (1) lowest - (10) highest.
bty_m1upper	beauty rating of professor from upper
	level male: (1) lowest - (10) highest.
bty_m2upper	beauty rating of professor from second
	upper level male: (1) lowest - (10)
	highest.
bty_avg	average beauty rating of professor.
pic_outfit	outfit of professor in picture: not formal,
	formal.
pic_color	color of professor's picture: color, black
	& white.

Exploring the data

1. Is this an observational study or an experiment? The original research question posed in the paper is whether beauty leads directly to the differences in course evaluations. Given the study design, is it possible to answer this question as it is phrased? If not, rephrase the question.

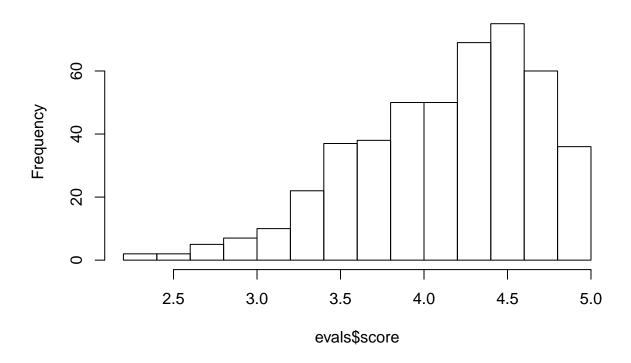
This is an observational study. We can rephrase the question as: Is there an association between beauty and course evaluation score?

2. Describe the distribution of **score**. Is the distribution skewed? What does that tell you about how students rate courses? Is this what you expected to see? Why, or why not?

summary(evals\$score)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 2.300 3.800 4.300 4.175 4.600 5.000
```

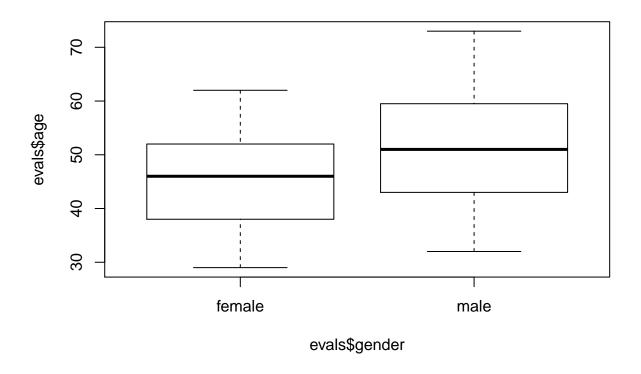
Histogram of evals\$score



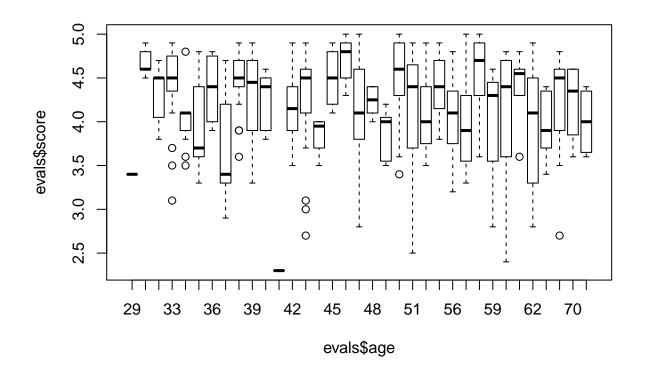
Score is left skewed. The distribution of score is between 2.3 and 5 with a median score of 4.3 and an IQR of less than 1.

3. Excluding score, select two other variables and describe their relationship using an appropriate visualization (scatterplot, side-by-side boxplots, or mosaic plot).

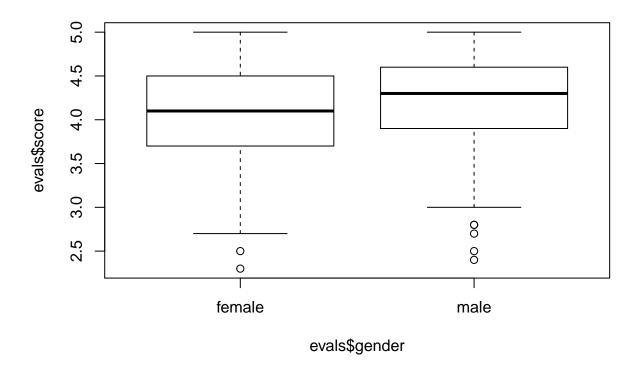
boxplot(evals\$age~evals\$gender)



boxplot(evals\$score~evals\$age)



boxplot(evals\$score~evals\$gender)



The two variable that i choose are age and gender. We can see here younger instructors are having higher scores.

Simple linear regression

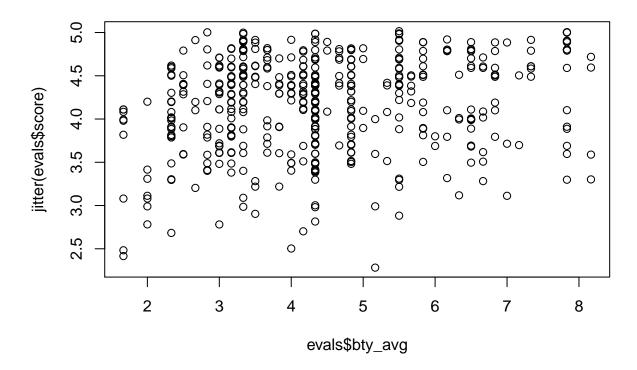
The fundamental phenomenon suggested by the study is that better looking teachers are evaluated more favorably. Let's create a scatterplot to see if this appears to be the case:

```
plot(evals$score ~ evals$bty_avg)
```

Before we draw conclusions about the trend, compare the number of observations in the data frame with the approximate number of points on the scatterplot. Is anything awry?

4. Replot the scatterplot, but this time use the function jitter() on the y- or the x-coordinate. (Use ?jitter to learn more.) What was misleading about the initial scatterplot?

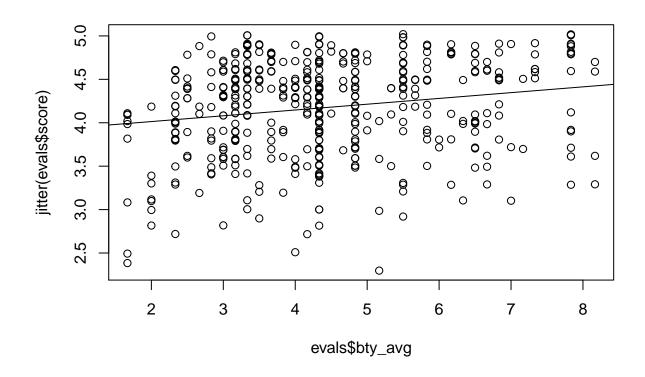
```
plot(jitter(evals$score)~evals$bty_avg)
```



In the Initial scatterplot ne dot represents many observations and this is fixed by atting jitter.

5. Let's see if the apparent trend in the plot is something more than natural variation. Fit a linear model called m_bty to predict average professor score by average beauty rating and add the line to your plot using abline(m_bty). Write out the equation for the linear model and interpret the slope. Is average beauty score a statistically significant predictor? Does it appear to be a practically significant predictor?

```
m_bty = lm(evals$score~ evals$bty_avg)
plot(jitter(evals$score)~evals$bty_avg)
abline(m_bty)
```



summary(m_bty)

```
##
## Call:
## lm(formula = evals$score ~ evals$bty_avg)
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
  -1.9246 -0.3690 0.1420 0.3977
                                  0.9309
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                                      50.96 < 2e-16 ***
## (Intercept)
                 3.88034
                            0.07614
                            0.01629
                                       4.09 5.08e-05 ***
## evals$bty_avg 0.06664
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5348 on 461 degrees of freedom
## Multiple R-squared: 0.03502,
                                Adjusted R-squared: 0.03293
## F-statistic: 16.73 on 1 and 461 DF, p-value: 5.083e-05
correlation = cor(evals$bty_avg, evals$score)
correlation
```

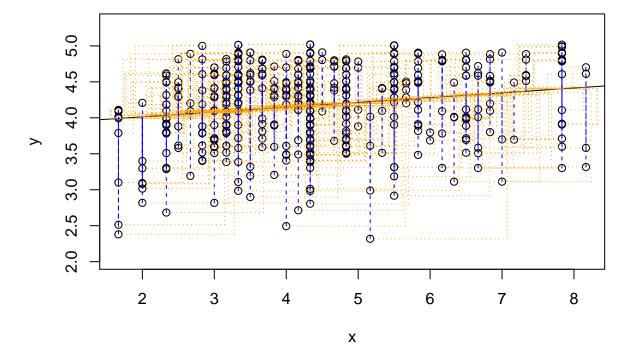
[1] 0.1871424

```
y(hat) = 3.88 + 0.06xbty avg
```

bty_avg is a statistically significant predictor of evaluation score with p-value close of 0.

6. Use residual plots to evaluate whether the conditions of least squares regression are reasonable. Provide plots and comments for each one (see the Simple Regression Lab for a reminder of how to make these).

```
DATA606::plot_ss(x= evals$bty_avg, y= jitter(evals$score), showSquares = TRUE)
```



```
## Click two points to make a line.
## Call:
## lm(formula = y ~ x, data = pts)
##
## Coefficients:
## (Intercept) x
## 3.87956 0.06685
##
## Sum of Squares: 131.454
```

Multiple linear regression

The data set contains several variables on the beauty score of the professor: individual ratings from each of the six students who were asked to score the physical appearance of the professors and the average of these six scores. Let's take a look at the relationship between one of these scores and the average beauty score.

```
plot(evals$bty_avg ~ evals$bty_f1lower)
cor(evals$bty_avg, evals$bty_f1lower)
```

As expected the relationship is quite strong - after all, the average score is calculated using the individual scores. We can actually take a look at the relationships between all beauty variables (columns 13 through 19) using the following command:

```
plot(evals[,13:19])
```

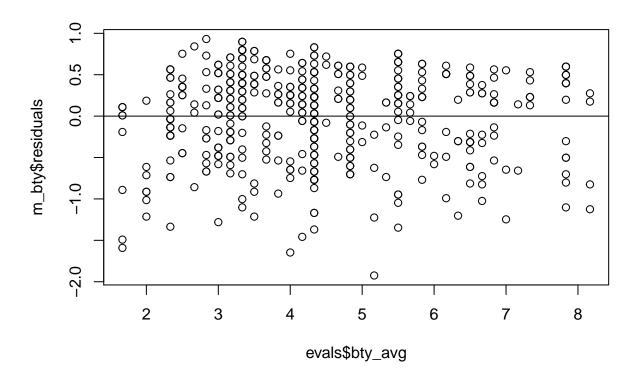
These variables are collinear (correlated), and adding more than one of these variables to the model would not add much value to the model. In this application and with these highly-correlated predictors, it is reasonable to use the average beauty score as the single representative of these variables.

In order to see if beauty is still a significant predictor of professor score after we've accounted for the gender of the professor, we can add the gender term into the model.

```
m_bty_gen <- lm(score ~ bty_avg + gender, data = evals)
summary(m_bty_gen)</pre>
```

7. P-values and parameter estimates should only be trusted if the conditions for the regression are reasonable. Verify that the conditions for this model are reasonable using diagnostic plots.

```
plot(m_bty$residuals~evals$bty_avg)
abline(h = 0)
```



Variability is constant so conditions for regression are pretty reasonable.

8. Is bty_avg still a significant predictor of score? Has the addition of gender to the model changed the parameter estimate for bty_avg?

```
lm(formula = score ~ bty_avg + gender, data = evals, y = TRUE)
```

```
##
## Call:
## lm(formula = score ~ bty_avg + gender, data = evals, y = TRUE)
##
## Coefficients:
## (Intercept) bty_avg gendermale
## 3.74734 0.07416 0.17239
```

bty_avg is still significant and the addition of gender has changed the estimate from 0.066 to 0.074.

Note that the estimate for gender is now called gendermale. You'll see this name change whenever you introduce a categorical variable. The reason is that R recodes gender from having the values of female and male to being an indicator variable called gendermale that takes a value of 0 for females and a value of 1 for males. (Such variables are often referred to as "dummy" variables.)

As a result, for females, the parameter estimate is multiplied by zero, leaving the intercept and slope form familiar from simple regression.

$$\widehat{score} = \hat{\beta}_0 + \hat{\beta}_1 \times bty_avg + \hat{\beta}_2 \times (0)$$
$$= \hat{\beta}_0 + \hat{\beta}_1 \times bty_avg$$

We can plot this line and the line corresponding to males with the following custom function.

```
multiLines(m_bty_gen)
```

9. What is the equation of the line corresponding to males? (*Hint:* For males, the parameter estimate is multiplied by 1.) For two professors who received the same beauty rating, which gender tends to have the higher course evaluation score?

```
# summary(m_bty_gen)
```

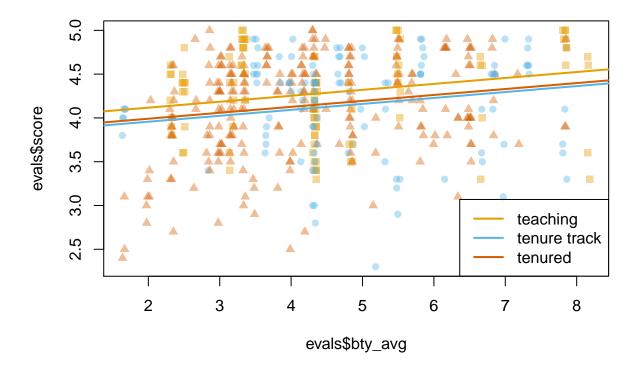
Score can be calculated as:

```
score(hat) = (3.75 + 0.1724) + 0.074 \times bty avg
```

Male professors would score 0.1724 higher than a female with the same beauty rating.

The decision to call the indicator variable gendermale instead ofgenderfemale has no deeper meaning. R simply codes the category that comes first alphabetically as a 0. (You can change the reference level of a categorical variable, which is the level that is coded as a 0, using therelevel function. Use ?relevel to learn more.)

10. Create a new model called m_bty_rank with gender removed and rank added in. How does R appear to handle categorical variables that have more than two levels? Note that the rank variable has three levels: teaching, tenure track, tenured.



The interpretation of the coefficients in multiple regression is slightly different from that of simple regression. The estimate for bty_avg reflects how much higher a group of professors is expected to score if they have a beauty rating that is one point higher while holding all other variables constant. In this case, that translates into considering only professors of the same rank with bty_avg scores that are one point apart.

The search for the best model

We will start with a full model that predicts professor score based on rank, ethnicity, gender, language of the university where they got their degree, age, proportion of students that filled out evaluations, class size, course level, number of professors, number of credits, average beauty rating, outfit, and picture color.

11. Which variable would you expect to have the highest p-value in this model? Why? *Hint:* Think about which variable would you expect to not have any association with the professor score.

I picked the cls profs

Let's run the model...

12. Check your suspicions from the previous exercise. Include the model output in your response.

It was correct, The cls_profs

13. Interpret the coefficient associated with the ethnicity variable.

When ethnicity is not minority the score tends to increase by 0.1234929.

14. Drop the variable with the highest p-value and re-fit the model. Did the coefficients and significance of the other explanatory variables change? (One of the things that makes multiple regression interesting is that coefficient estimates depend on the other variables that are included in the model.) If not, what does this say about whether or not the dropped variable was collinear with the other explanatory variables?

m_without_cls_profs = lm(score ~ rank + ethnicity + gender + language + age + cls_perc_eval

```
+ cls_students + cls_level + cls_credits + bty_avg
             + pic_outfit + pic_color, data = evals)
summary(m_without_cls_profs)
##
## Call:
  lm(formula = score ~ rank + ethnicity + gender + language + age +
##
       cls_perc_eval + cls_students + cls_level + cls_credits +
##
       bty_avg + pic_outfit + pic_color, data = evals)
##
## Residuals:
                1Q
                    Median
##
       Min
                                 3Q
                                        Max
## -1.7836 -0.3257
                    0.0859
                            0.3513
                                    0.9551
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          4.0872523
                                      0.2888562
                                                14.150 < 2e-16 ***
## ranktenure track
                         -0.1476746
                                      0.0819824
                                                 -1.801 0.072327
## ranktenured
                         -0.0973829
                                      0.0662614
                                                 -1.470 0.142349
## ethnicitynot minority
                          0.1274458
                                      0.0772887
                                                  1.649 0.099856 .
## gendermale
                           0.2101231
                                      0.0516873
                                                  4.065 5.66e-05 ***
## languagenon-english
                         -0.2282894
                                     0.1111305
                                                 -2.054 0.040530 *
                         -0.0089992
                                     0.0031326
                                                 -2.873 0.004262 **
## cls_perc_eval
                           0.0052888
                                     0.0015317
                                                  3.453 0.000607 ***
## cls_students
                           0.0004687
                                      0.0003737
                                                  1.254 0.210384
## cls_levelupper
                                                  1.055 0.292200
                           0.0606374
                                      0.0575010
## cls creditsone credit
                          0.5061196
                                      0.1149163
                                                  4.404 1.33e-05 ***
## bty_avg
                           0.0398629
                                      0.0174780
                                                  2.281 0.023032 *
## pic outfitnot formal
                                                 -1.501 0.134080
                         -0.1083227
                                      0.0721711
                                                 -3.079 0.002205 **
## pic_colorcolor
                         -0.2190527
                                     0.0711469
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.4974 on 449 degrees of freedom
Multiple R-squared: 0.187, Adjusted R-squared: 0.1634
F-statistic: 7.943 on 13 and 449 DF, p-value: 2.336e-14

The coefficients and p-values have changed slightly. The dropped variable had only minimal collinearity with the other explanatory variables.

15. Using backward-selection and p-value as the selection criterion, determine the best model. You do not need to show all steps in your answer, just the output for the final model. Also, write out the linear model for predicting score based on the final model you settle on.

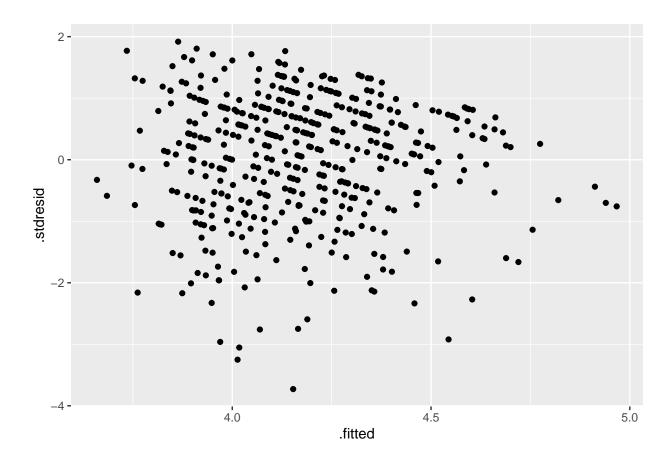
```
m_back <- lm(score ~ ethnicity + gender + language + age + cls_perc_eval + cls_credits + bty_avg + pic_
summary(m_back)
```

```
##
## Call:
## lm(formula = score ~ ethnicity + gender + language + age + cls_perc_eval +
##
       cls_credits + bty_avg + pic_color, data = evals)
##
## Residuals:
       Min
                 1Q
                      Median
                                            Max
  -1.85320 -0.32394 0.09984 0.37930
##
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         3.771922
                                    0.232053 16.255 < 2e-16 ***
## ethnicitynot minority 0.167872
                                    0.075275
                                               2.230 0.02623 *
## gendermale
                         0.207112
                                    0.050135
                                                4.131 4.30e-05 ***
## languagenon-english
                         -0.206178
                                    0.103639 -1.989
                                                     0.04726 *
## age
                         -0.006046
                                    0.002612 - 2.315
                                                      0.02108 *
## cls_perc_eval
                                    0.001435
                         0.004656
                                               3.244 0.00127 **
## cls creditsone credit 0.505306
                                     0.104119
                                                4.853 1.67e-06 ***
## bty_avg
                                     0.016934
                                                3.016 0.00271 **
                         0.051069
## pic_colorcolor
                         -0.190579
                                     0.067351 -2.830 0.00487 **
## ---
## Signif. codes:
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.4992 on 454 degrees of freedom
## Multiple R-squared: 0.1722, Adjusted R-squared: 0.1576
## F-statistic: 11.8 on 8 and 454 DF, p-value: 2.58e-15
```

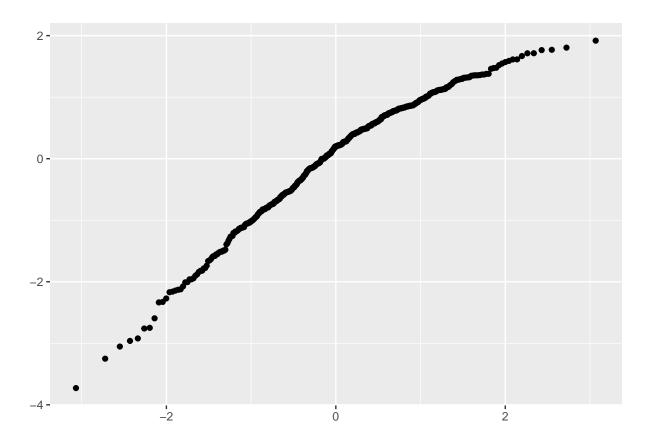
 $score(hat) = 3.77 + 0.17 \\ xethnicity_not_minority + 0.21 \\ xgendermale - 0.206 \\ xlanguage_non_english - 0.006 \\ xage + 0.004 \\ xcls_percondense \\ xcls_percondens$

16. Verify that the conditions for this model are reasonable using diagnostic plots.

```
ggplot2::qplot(x = .fitted, y = .stdresid, data = m_back, position = "jitter")
## Warning: `position` is deprecated
```



ggplot2::qplot(sample = .stdresid, data = m_back)



+ geom_abline()

Nearly normal residuals so data appears to satisfy the conditions for regression.

17. The original paper describes how these data were gathered by taking a sample of professors from the University of Texas at Austin and including all courses that they have taught. Considering that each row represents a course, could this new information have an impact on any of the conditions of linear regression?

I thinks if the same student takes two or more classes with the same instructor this will affect the outcome since independence will not be satisfied.

18. Based on your final model, describe the characteristics of a professor and course at University of Texas at Austin that would be associated with a high evaluation score.

Male instructors with english speaking, teach one credit class, not a minority and has a black and white picture will have high evaluation score.

19. Would you be comfortable generalizing your conclusions to apply to professors generally (at any university)? Why or why not?

I will be comfortable generalizing my conclusions on similar kind/ size of universities and not all.