

Exercice :

$$\text{info}(\bar{T}) = -\sum \frac{\text{freq}(\bar{T}, c_j)}{|\bar{T}|} \cdot \log_2 \frac{\text{freq}(\bar{T}, c_j)}{|\bar{T}|}$$

$$= -\frac{5}{10} \cdot \log_2 \frac{5}{10} - \frac{5}{10} \log_2 \frac{5}{10}$$

$$= 1$$

info Age (T)?

$$\text{info}(\bar{T}_{\text{Age}}) = -\frac{3}{3} \log_2 \left(\frac{3}{3}\right) = 0$$

$$\text{info}(\bar{T}_{\text{moyen}}) = -\frac{2}{4} \log_2 \left(\frac{2}{4}\right) - \frac{2}{4} \log_2 \left(\frac{2}{4}\right) = 1$$

$$\text{info}(\bar{T}_{\text{recent}}) = -\frac{3}{3} \log_2 \left(\frac{3}{3}\right) = 0$$

$$\text{info Age}(\bar{T}) = \frac{3}{10} \text{info}(\bar{T}_{\text{Age}}) + \frac{4}{10} \text{info}(\bar{T}_{\text{moyen}}) + \frac{3}{10} \text{info}(\bar{T}_{\text{recent}})$$

$$= 0.4$$

Gain ratio (Age)?

$$\text{Gain}(\bar{T}, \text{Age}) = \text{info}(\bar{T}) - \text{info Age}(\bar{T}) = 1 - 0.4 = 0.6$$

$$\text{Split Info}(\bar{T}, \text{Age}) = -\frac{3}{10} \log_2 \frac{3}{10} - \frac{4}{10} \log_2 \frac{4}{10} - \frac{3}{10} \log_2 \frac{3}{10}$$

$$\text{Gain Ratio}(\bar{T}, \text{Age}) = \frac{\text{Gain}(\bar{T}, \text{Age})}{\text{Split info}(\bar{T}, \text{Age})} = \frac{0.6}{1.57} = 0.382$$

info concurrence (T)?

$$\text{info}(\bar{T}_{\text{men}}) = -\frac{2}{6} \log_2 \frac{2}{6} - \frac{4}{6} \log_2 \frac{4}{6} = 0.91$$

$$\text{info}(\bar{T}_{\text{oui}}) = -\frac{3}{4} \log_2 \frac{3}{4} - \frac{1}{4} \log_2 \frac{1}{4} = 0.81127$$

$$\text{info conc}(\bar{T}) = \frac{6}{10} \text{info}(\bar{T}_{\text{men}}) + \frac{4}{10} \text{info}(\bar{T}_{\text{oui}}) = 0.87$$

Gain ratio (concurrence)?

$$\text{Gain}(\bar{T}, \text{concurrence}) = \text{info}(\bar{T}) - \text{info conc}(\bar{T}) = 1 - 0.87 = 0.13$$

$$\text{Split info}(\bar{T}, \text{concurrence}) = -\frac{6}{10} \log_2 \frac{6}{10} - \frac{4}{10} \log_2 \frac{4}{10} = 0.97$$

$$\text{Gain Ratio}(\bar{T}, \text{concurrence}) = \frac{0.13}{0.97} = 0.134$$

info type (T)?

$$\text{info}(\bar{T}_{\text{software}}) = -\frac{3}{6} \log_2 \left(\frac{3}{6}\right) - \frac{3}{6} \log_2 \left(\frac{3}{6}\right) = 1$$

$$\text{info}(T_{\text{hardware}}) = -\frac{2}{4} \log_2\left(\frac{2}{4}\right) - \frac{2}{4} \log_2\left(\frac{2}{4}\right) = 1$$

$$\text{info}_{\text{type}}(T) = \frac{6}{10} \text{info}(T_{\text{software}}) + \frac{4}{10} \text{info}(T_{\text{hardware}}) = 1$$

Gain ratio (type)

$$\text{Gain}(T, \text{type}) = \text{info}(T) - \text{info}_{\text{type}}(T) = 0$$

$$\text{Split info}(T, \text{type}) = -\frac{6}{10} \log_2\frac{6}{10} - \frac{4}{10} \log_2\frac{4}{10} = 0,97$$

$$\text{Gain ratio}(T, \text{type}) = \frac{0}{0,97} = 0$$

$$\text{Gain ratio}(T, \text{age}) = 0,38$$

$$\text{Gain ratio}(T, \text{age}) = 0,38$$

$$\text{Gain ratio}(T, \text{concurrency}) = 0,134$$

Diagram showing splits on Age and Recent:

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    graph TD
      Root(( )) -- Age --> Baisse1[Baisse]
      Root -- Recent --> Hausse1[Hausse]
      Root -- Age --> Moyen1[Moyen]
      Root -- Recent --> Hausse2[Hausse]
      Root -- Age --> Moyen2[Moyen]
      Root -- Recent --> Hausse3[Hausse]
      Root -- Age --> Moyen3[Moyen]
      Root -- Recent --> Hausse4[Hausse]
  
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Age	Concurrence	Type	Profit
Moyen	oui	soft	Baisse
Moyen	Non	Hard	Hausse
Moyen	Non	Soft	Hausse
Moyen	oui	hard	Baisse

Concurrence

$$\text{info}(T_{\text{oui}}) = -\frac{2}{2} \log_2\frac{2}{2} = 0$$

$$\text{info}(T_{\text{non}}) = -\frac{2}{2} \log_2\frac{2}{2} = 0$$

$$\text{info}_{\text{conc}}(T) = \frac{2}{4} \text{info}(T_{\text{oui}}) + \frac{2}{4} \text{info}(T_{\text{non}}) = 0$$

$$\text{Gain}(T, \text{concurrency}) = \text{info}(T) - \text{info}_{\text{conc}}(T) = 1$$

$$\text{Split info}(T, \text{concurrency}) = -\frac{2}{4} \log_2\frac{2}{4} - \frac{2}{4} \log_2\frac{2}{4} = 1$$

$$\text{Gain ratio}(T, \text{concurrency}) = \frac{1}{1} = 1$$

Type

$$info(T_{soft}) = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1$$

$$info(T_{hard}) = -\frac{1}{2} \log_2 \frac{1}{2} - \frac{1}{2} \log_2 \frac{1}{2} = 1$$

$$info_{Type}(T) = \frac{2}{4} info(T_{soft}) + \frac{2}{4} info(T_{hard}) = 1$$

$$Gain(T, type) = info(T) - info_{type}(T) = 0$$

$$split\ info = -\frac{2}{4} \log_2 \frac{2}{4} - \frac{2}{4} \log_2 \frac{2}{4} = 1$$

$$Gain\ ratio(T, type) = \frac{0}{1} = 0$$

$$Gain\ ratio(T, concurrence) = 1$$

$$Gain\ ratio(T, type) = 0$$

Arbre :

