Project- CCPS 844 Data Mining

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This project aims to tackle a challenging regression problem focused on predicting life expectancy. Life expectancy is a critical indicator of the overall health and well-being of a population, and accurately predicting it can have far-reaching implications for public health, social policies, and resource allocation.\ \ The key steps of the project involve data cleaing, visualizations, Clustering, feature selection and PCA, model training and evaluation. Several regression learing algorithms will be explored and compared to find the best-performing model.

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Data summary

```
In [ ]:
          import pandas as pd
          df=pd.read csv("world-data-2023.csv")
Out[ ]:
                                                                                  Armed
                                                                                          Birth Calling Capi
                                                          Agricultural
                                                                            Land
                 Country Density\n(P/Km2) Abbreviation
                                                                                   Forces
                                                             Land(%) Area(Km2)
                                                                                           Rate
                                                                                                  Code
                                                                                     size
            0 Afghanistan
                                        60
                                                      ΑF
                                                              58.10%
                                                                                 323,000
                                                                                          32.49
                                                                                                   93.0
                                                                         652,230
            1
                  Albania
                                        105
                                                      AL
                                                              43.10%
                                                                          28,748
                                                                                    9,000
                                                                                          11.78
                                                                                                  355.0
           2
                   Algeria
                                                      DΖ
                                                              17.40%
                                                                        2,381,741 317,000
                                                                                          24.28
                                                                                                  213.0
                                        18
           3
                  Andorra
                                                     AD
                                                              40.00%
                                                                             468
                                                                                           7.20
                                        164
                                                                                    NaN
                                                                                                  376.0
                   Angola
                                        26
                                                     AO
                                                              47.50%
                                                                        1,246,700
                                                                                 117,000
                                                                                          40.73
                                                                                                  244.0
                                                                                 343,000
          190
                Venezuela
                                        32
                                                      VE
                                                              24.50%
                                                                         912,050
                                                                                         17.88
                                                                                                   58.0
          191
                  Vietnam
                                                                                 522,000
                                        314
                                                     VN
                                                              39.30%
                                                                         331,210
                                                                                          16.75
                                                                                                   84.0
          192
                   Yemen
                                        56
                                                      YΕ
                                                              44.60%
                                                                         527,968
                                                                                   40,000
                                                                                          30.45
                                                                                                  967.0
          193
                  Zambia
                                        25
                                                     ZM
                                                              32.10%
                                                                         752,618
                                                                                   16,000
                                                                                          36.19
                                                                                                  260.0
          194
                Zimbabwe
                                        38
                                                     ZW
                                                              41.90%
                                                                         390,757
                                                                                   51,000 30.68
                                                                                                  263.0
         195 rows × 35 columns
In [ ]:
          df.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 195 entries, 0 to 194
         Data columns (total 35 columns):
          #
               Column
                                                               Non-Null Count
                                                                                 Dtype
          0
               Country
                                                               195 non-null
                                                                                 object
          1
               Density
          (P/Km2)
                                                 195 non-null
                                                                  object
          2
               Abbreviation
                                                               188 non-null
                                                                                 object
          3
               Agricultural Land(%)
                                                               188 non-null
                                                                                 object
          4
               Land Area(Km2)
                                                               194 non-null
                                                                                 object
          5
               Armed Forces size
                                                               171 non-null
                                                                                 object
          6
               Birth Rate
                                                               189 non-null
                                                                                 float64
          7
               Calling Code
                                                               194 non-null
                                                                                 float64
          8
               Capital/Major City
                                                               192 non-null
                                                                                 object
          9
               Co2-Emissions
                                                               188 non-null
                                                                                 object
          10
               CPI
                                                               178 non-null
                                                                                 object
          11
               CPI Change (%)
                                                               179 non-null
                                                                                 object
```

180 non-null

188 non-null

object float64

12

13

Currency-Code

Fertility Rate

```
14 Forested Area (%)
                                               188 non-null
                                                               object
15 Gasoline Price
                                               175 non-null
                                                               object
16 GDP
                                               193 non-null
                                                               object
17
   Gross primary education enrollment (%)
                                               188 non-null
                                                               object
18 Gross tertiary education enrollment (%)
                                               183 non-null
                                                               object
19 Infant mortality
                                               189 non-null
                                                               float64
20 Largest city
                                               189 non-null
                                                               object
21 Life expectancy
                                               187 non-null
                                                               float64
22 Maternal mortality ratio
                                               181 non-null
                                                               float64
23 Minimum wage
                                               150 non-null
                                                               object
24 Official language
                                               194 non-null
                                                               object
25 Out of pocket health expenditure
                                               188 non-null
                                                               object
                                                               float64
26 Physicians per thousand
                                               188 non-null
27 Population
                                               194 non-null
                                                               object
28 Population: Labor force participation (%)
                                               176 non-null
                                                               object
29 Tax revenue (%)
                                               169 non-null
                                                               object
30 Total tax rate
                                               183 non-null
                                                               object
31 Unemployment rate
                                               176 non-null
                                                               object
32 Urban population
                                               190 non-null
                                                               object
                                                               float64
33 Latitude
                                               194 non-null
34 Longitude
                                               194 non-null
                                                               float64
```

dtypes: float64(9), object(26)

memory usage: 53.4+ KB

In []: | df.describe()

Out[]:

| | Birth Rate | Calling Code | Fertility Rate | Infant mortality | Life expectancy | Maternal mortality ratio | Physicians per thousand | Latitude |
|-------|------------|-----------------|-------------------|---------------------|-----------------|--------------------------------|-------------------------------|------------|
| count | 189.000000 | 194.000000 | 188.000000 | 189.000000 | 187.000000 | 181.000000 | 188.000000 | 194.000000 |
| mean | 20.214974 | 360.546392 | 2.698138 | 21.332804 | 72.279679 | 160.392265 | 1.839840 | 19.092351 |
| std | 9.945774 | 323.236419 | 1.282267 | 19.548058 | 7.483661 | 233.502024 | 1.684261 | 23.961779 |
| min | 5.900000 | 1.000000 | 0.980000 | 1.400000 | 52.800000 | 2.000000 | 0.010000 | -40.900557 |
| 25% | 11.300000 | 82.500000 | 1.705000 | 6.000000 | 67.000000 | 13.000000 | 0.332500 | 4.544175 |
| 50% | 17.950000 | 255.500000 | 2.245000 | 14.000000 | 73.200000 | 53.000000 | 1.460000 | 17.273849 |
| 75% | 28.750000 | 506.750000 | 3.597500 | 32.700000 | 77.500000 | 186.000000 | 2.935000 | 40.124603 |
| max | 46.080000 | 1876.000000 | 6.910000 | 84.500000 | 85.400000 | 1150.000000 | 8.420000 | 64.963051 |

Droping columns that do not add value to the df

```
cols_to_drop= ['Abbreviation','Calling Code','Capital/Major City','Currency-Code','Larg
    df = df.drop(columns=cols_to_drop)
    df
```

Out[]:

| | Country | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Forces size | Birth Rate | Co2- Emissions | СРІ | Chang (% |
|---|-------------|------------------|--------------------------|-------------------|----------------|---------------|-------------------|-------|-------------|
| 0 | Afghanistan | 60 | 58.10% | 652,230 | 323,000 | 32.49 | 8,672 | 149.9 | 2.309 |

Armod

CE

| | Country | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | Co2- Emissions | СРІ | CF Chang (% |
|-----|-----------|------------------|--------------------------|-------------------|-------------------------|---------------|-------------------|----------|-------------------|
| 1 | Albania | 105 | 43.10% | 28,748 | 9,000 | 11.78 | 4,536 | 119.05 | 1.409 |
| 2 | Algeria | 18 | 17.40% | 2,381,741 | 317,000 | 24.28 | 150,006 | 151.36 | 2.009 |
| 3 | Andorra | 164 | 40.00% | 468 | NaN | 7.20 | 469 | NaN | Nal |
| 4 | Angola | 26 | 47.50% | 1,246,700 | 117,000 | 40.73 | 34,693 | 261.73 | 17.109 |
| ••• | | | | | | | | | |
| 190 | Venezuela | 32 | 24.50% | 912,050 | 343,000 | 17.88 | 164,175 | 2,740.27 | 254.909 |
| 191 | Vietnam | 314 | 39.30% | 331,210 | 522,000 | 16.75 | 192,668 | 163.52 | 2.809 |
| 192 | Yemen | 56 | 44.60% | 527,968 | 40,000 | 30.45 | 10,609 | 157.58 | 8.109 |
| 193 | Zambia | 25 | 32.10% | 752,618 | 16,000 | 36.19 | 5,141 | 212.31 | 9.209 |
| 194 | Zimbabwe | 38 | 41.90% | 390,757 | 51,000 | 30.68 | 10,983 | 105.51 | 0.909 |
| | | | | | | | | | |

195 rows × 24 columns

```
In []: df.shape
Out[]: (195, 24)
```

Visualizing NA's

```
import seaborn as sns
import matplotlib.pyplot as plt

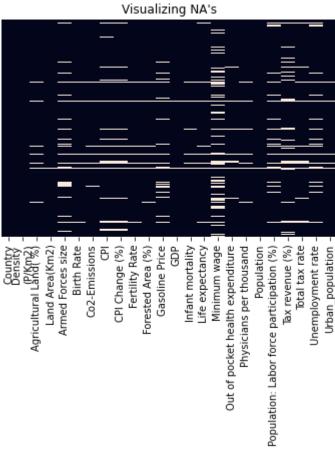
na_counts = df.isna().sum()
print("The Number of NA's in",na_counts)

sns.heatmap(df.isnull(),yticklabels=False,cbar=False)
plt.title("Visualizing NA's")
```

```
The Number of NA's in Country
                                                                       0
Density\n(P/Km2)
                                                0
                                                7
Agricultural Land( %)
Land Area(Km2)
                                                1
Armed Forces size
                                               24
Birth Rate
                                                6
Co2-Emissions
                                                7
CPI
                                               17
CPI Change (%)
                                               16
Fertility Rate
                                                7
                                                7
Forested Area (%)
Gasoline Price
                                               20
GDP
                                                2
Infant mortality
                                                6
Life expectancy
                                                8
Minimum wage
                                               45
```

```
8/5/23, 9:13 PM
                                                             project2
              Out of pocket health expenditure
                                                                7
              Physicians per thousand
                                                                7
              Population
                                                                1
              Population: Labor force participation (%)
                                                              19
              Tax revenue (%)
                                                               26
              Total tax rate
                                                               12
              Unemployment rate
                                                               19
              Urban_population
                                                                5
              dtype: int64
              Text(0.5, 1.0, "Visualizing NA's")
     Out[ ]:
```

Visualizing NA



Web Scraping

Fill in Agricultural Land(%) values

```
In []:
    from lxml import html
    from bs4 import BeautifulSoup
    import requests

In []:
    #Find Out which countries have missing Agricultural Land(%) values
    rows_with_na = df[df["Agricultural Land(%)"].isna()]

# Display the result
    print(rows_with_na)
    print("Eswatini, Monaco, Nauru, North Macedonia, Palestinian National Authority, South
```

```
Country Density\n(P/Km2) Agricultural Land( %)
56
                             Eswatini
                                                      67
                                                                             NaN
                                                  2,003
73
                        Vatican City
                                                                            NaN
113
                               Monaco
                                                 26,337
                                                                            NaN
120
                                Nauru
                                                     541
                                                                            NaN
                     North Macedonia
128
                                                      83
                                                                            NaN
133
     Palestinian National Authority
                                                     847
                                                                            NaN
163
                         South Sudan
                                                      18
                                                                            NaN
    Land Area(Km2) Armed Forces size
                                         Birth Rate Co2-Emissions
                                                                          CPI \
56
             17,364
                                                NaN
                                                                NaN
                                   NaN
                                                                          NaN
73
                  0
                                   NaN
                                                NaN
                                                                NaN
                                                                          NaN
                  2
113
                                               5.90
                                   NaN
                                                               NaN
                                                                          NaN
120
                 21
                                   NaN
                                                NaN
                                                               NaN
                                                                          NaN
             25,713
128
                                   NaN
                                                NaN
                                                               NaN
                                                                          NaN
133
                                   NaN
                                                               NaN
                NaN
                                                NaN
                                                                          NaN
163
           644,329
                               185,000
                                              35.01
                                                             1,727
                                                                     4,583.71
    CPI Change (%)
                     Fertility Rate
                                       ... Life expectancy Minimum wage
56
                NaN
                                                        NaN
                                 NaN
73
                NaN
                                 NaN
                                                        NaN
                                                                      NaN
113
                NaN
                                                        NaN
                                                                  $11.72
                                 NaN
120
                NaN
                                 NaN
                                                        NaN
                                                                      NaN
128
                NaN
                                                        NaN
                                                                      NaN
                                 NaN
133
                NaN
                                                        NaN
                                                                      NaN
                                 NaN
163
           187.90%
                                 4.7
                                                       57.6
                                                                      NaN
    Out of pocket health expenditure Physicians per thousand
                                                                    Population
56
                                11.30%
                                                              NaN
                                                                     1,093,238
73
                                   NaN
                                                              NaN
                                                                           836
113
                                 6.10%
                                                             6.56
                                                                        38,964
120
                                                                        10,084
                                   NaN
                                                              NaN
128
                                35.60%
                                                              NaN
                                                                     1,836,713
133
                                                              NaN
                                   NaN
                                                                           NaN
163
                                61.30%
                                                              NaN
                                                                    11,062,113
    Population: Labor force participation (%) Tax revenue (%)
                                                                    Total tax rate
56
                                             NaN
                                                           28.60%
                                                                                NaN
73
                                             NaN
                                                              NaN
                                                                                NaN
113
                                             NaN
                                                              NaN
                                                                                NaN
120
                                             NaN
                                                              NaN
                                                                                NaN
128
                                             NaN
                                                              NaN
                                                                                NaN
133
                                             NaN
                                                              NaN
                                                                                NaN
163
                                          72.40%
                                                              NaN
                                                                            31.40%
    Unemployment rate Urban population
56
                   NaN
                                     NaN
73
                   NaN
                                     NaN
113
                   NaN
                                  38,964
120
                   NaN
                                     NaN
128
                   NaN
                                     NaN
133
                   NaN
                                     NaN
163
                12.24%
                               2,201,250
[7 rows x 24 columns]
Eswatini, Monaco, Nauru, North Macedonia, Palestinian National Authority, South Sudan
```

```
In [ ]: #get agricultral land data
import requests
```

from bs4 import BeautifulSoup

```
In [ ]:
         url = 'https://wdi.worldbank.org/table/3.2'
         # end a GET request to the URL
         response = requests.get(url)
         html content = response.text
         # create a Beautiful Soup object
         soup = BeautifulSoup(html content, 'html.parser')
         country_elements = soup.find_all(class_="country")
         #Eswatini %
         for country_element in country_elements:
             country_content = country_element.get_text()
             if "Eswatini" in country_content:
                 row element = country element.find parent("tr")
                 if row element:
                     eswatini row = row element.get text()
                     #print("Row:", eswatini_row)
         #Monaco %
         for country_element in country_elements:
             country_content = country_element.get_text()
             if "Monaco" in country content:
                 row_element = country_element.find_parent("tr")
                 if row element:
                     monaco_row = row_element.get_text()
                     #print("Row:", monaco_row)
         #Nauru %
         for country element in country elements:
             country_content = country_element.get_text()
             if "North Macedonia" in country_content:
                 row_element = country_element.find_parent("tr")
                 if row element:
                     nm_row = row_element.get_text()
                     #print("Row:", nm row)
         #South Sudan %
         for country element in country elements:
             country_content = country_element.get_text()
             if "South Sudan" in country content:
                 row_element = country_element.find_parent("tr")
                 if row element:
                     ss row = row element.get text()
                     #print("Row:", ss row)
         print("Nauru, Vatican City, and Moanco, could not be found\nPalestinian National Author
         # helper function to format extaracted data
         def get_first_number(words):
             for word in words:
```

```
if word.replace('.', '', 1).isdigit(): # formating
                     return float(word)
         # split the rows by whitespaces
         nm words = nm row.split()
         ss words = ss row.split()
         eswatini_words = eswatini_row.split()
         # create dictionary
         data dict = {
             'North Macedonia': get_first_number(nm_words),
             'South Sudan': get_first_number(ss_words),
             'Eswatini': get_first_number(eswatini_words)
         }
         print(data_dict)
        Nauru, Vatican City, and Moanco, could not be found
        Palestinian National Authority(will be dropped due to lack of data)
        {'North Macedonia': 50.0, 'South Sudan': 45.0, 'Eswatini': 71.0}
In [ ]:
         #input values to df
         df.loc[df['Country'] == 'North Macedonia', 'Agricultural Land( %)'] = get_first_number(
         df.loc[df['Country'] == 'South Sudan', 'Agricultural Land( %)'] = get first number(ss w
```

df.loc[df['Country'] == 'Eswatini', 'Agricultural Land(%)'] = get_first_number(eswatin

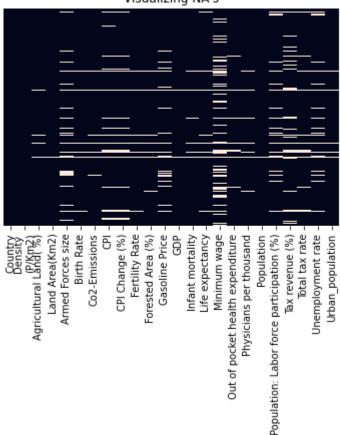
Data Preprocessing

Replace '0' in all rows with NA

```
In [ ]:
         import numpy as np
         df = df.replace(0, np.nan)
In [ ]:
         sns.heatmap(df.isnull(),yticklabels=False,cbar=False)
         plt.title("Visualizing NA's")
         na counts = df.isna().sum()
         print("The Number of NA's in",na_counts)
        The Number of NA's in Country
                                                                               0
        Density\n(P/Km2)
                                                        0
        Agricultural Land( %)
                                                        4
        Land Area(Km2)
                                                        1
        Armed Forces size
                                                       24
        Birth Rate
                                                        6
        Co2-Emissions
                                                        7
        CPI
                                                       17
        CPI Change (%)
                                                       16
        Fertility Rate
                                                        7
        Forested Area (%)
                                                        7
        Gasoline Price
                                                       20
        GDP
                                                        2
        Infant mortality
                                                        6
        Life expectancy
                                                        8
        Minimum wage
                                                       45
```

| Out of pocket health expenditure | 7 |
|---|----|
| Physicians per thousand | 7 |
| Population | 1 |
| Population: Labor force participation (%) | 19 |
| Tax revenue (%) | 26 |
| Total tax rate | 12 |
| Unemployment rate | 19 |
| Urban_population | 5 |
| dtype: int64 | |





Drop Minumum Wage column due to lack of data

```
In [ ]: df.drop(columns='Minimum wage', inplace=True)
```

0 0

0

Birth Rate

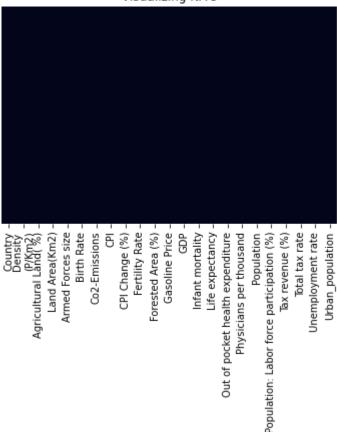
CPI

Co2-Emissions

CPI Change (%)

```
8/5/23, 9:13 PM
                                                              project2
              Fertility Rate
                                                               0
               Forested Area (%)
                                                               0
              Gasoline Price
                                                               0
              GDP
                                                               0
                                                               0
               Infant mortality
              Life expectancy
                                                               0
              Out of pocket health expenditure
                                                               0
              Physicians per thousand
                                                               0
              Population
                                                               0
              Population: Labor force participation (%)
                                                               0
              Tax revenue (%)
                                                               0
               Total tax rate
                                                               0
                                                               0
              Unemployment rate
              Urban_population
                                                               0
              dtype: int64
     In [ ]:
               df.shape
               (146, 23)
     Out[]:
     In [ ]:
               \verb|sns.heatmap(df.isnull(),yticklabels=False,cbar=False)|\\
               plt.title("Visualizing NA's")
              Text(0.5, 1.0, "Visualizing NA's")
     Out[]:
```





change data types 'object' to 'float64' so we can fit the dataframe into machine learning algorithms

```
In [ ]:
         df.dtypes
        Country
                                                       object
Out[ ]:
        Density\n(P/Km2)
                                                       object
        Agricultural Land( %)
                                                       object
        Land Area(Km2)
                                                       object
        Armed Forces size
                                                       object
        Birth Rate
                                                      float64
                                                       object
        Co2-Emissions
        CPI
                                                       object
        CPI Change (%)
                                                       object
        Fertility Rate
                                                      float64
        Forested Area (%)
                                                       object
        Gasoline Price
                                                       object
        GDP
                                                       object
                                                      float64
        Infant mortality
        Life expectancy
                                                      float64
        Out of pocket health expenditure
                                                       object
        Physicians per thousand
                                                      float64
        Population
                                                       object
        Population: Labor force participation (%)
                                                       object
        Tax revenue (%)
                                                       object
        Total tax rate
                                                       object
        Unemployment rate
                                                       object
        Urban population
                                                       object
        dtype: object
In [ ]:
         #Changing columns data types
         #remove commas from Density column
         df['Density\n(P/Km2)'] = df['Density\n(P/Km2)'].str.replace(',', '')
         df['Density\n(P/Km2)'] = df['Density\n(P/Km2)'].astype(float)
         #remove (%) from Agricultural Land(%) column
         df['Agricultural Land( %)'] = df['Agricultural Land( %)'].str.replace('%', '')
         df['Agricultural Land( %)'] = df['Agricultural Land( %)'].astype(float)
         #remove commas from Land Area(Km2) column
         df['Land Area(Km2)'] = df['Land Area(Km2)'].str.replace(',', '')
         df['Land Area(Km2)'] = df['Land Area(Km2)'].astype(float)
         #remove commas from Armed Forces size column
         df['Armed Forces size'] = df['Armed Forces size'].str.replace(',', '')
         df['Armed Forces size'] = df['Armed Forces size'].astype(float)
         #remove commas from Co2-Emissions column
         df['Co2-Emissions'] = df['Co2-Emissions'].str.replace(',', '')
         df['Co2-Emissions'] = df['Co2-Emissions'].astype(float)
         #remove commas from CPI column
         df['CPI'] = df['CPI'].str.replace(',', '')
         df['CPI'] = df['CPI'].astype(float)
         #remove "%" from CPI Change column
         df['CPI Change (%)'] = df['CPI Change (%)'].str.replace('%', '')
         df['CPI Change (%)'] = df['CPI Change (%)'].astype(float)
```

```
#remove "%" from Forested Area (%) column
df['Forested Area (%)'] = df['Forested Area (%)'].str.replace('%', '')
df['Forested Area (%)'] = df['Forested Area (%)'].astype(float)
#remove "$" from Gasoline Price column
df['Gasoline Price'] = df['Gasoline Price'].str.replace('$', '')
df['Gasoline Price'] = df['Gasoline Price'].astype(float)
#remove "$" from GDP Change column
df['GDP'] = df['GDP'].str.replace('$', '')
#remove commas from GDP Change column
df['GDP'] = df['GDP'].str.replace(',', '')
df['GDP'] = df['GDP'].astype(float)
#Pandas formats large number to scinetifc notation, therfore this converts back
pd.set option('display.float format', '{:.2f}'.format)
#remove "%" from Out of pocket health expenditure column
df['Out of pocket health expenditure'] = df['Out of pocket health expenditure'].str.rep
df['Out of pocket health expenditure'] = df['Out of pocket health expenditure'].astype(
#remove commas from Population column
df['Population'] = df['Population'].str.replace(',', '')
df['Population'] = df['Population'].astype(float)
#remove "%" from Population: Labor force participation (%) column
df['Population: Labor force participation (%)'] = df['Population: Labor force participa
df['Population: Labor force participation (%)'] = df['Population: Labor force participa
#remove "%" from Tax revenue (%) column
df['Tax revenue (%)'] = df['Tax revenue (%)'].str.replace('%', '')
df['Tax revenue (%)'] = df['Tax revenue (%)'].astype(float)
#remove "%" from Total tax rate column
df['Total tax rate'] = df['Total tax rate'].str.replace('%', '')
df['Total tax rate'] = df['Total tax rate'].astype(float)
#remove "%" from Unemployment rate column
df['Unemployment rate'] = df['Unemployment rate'].str.replace('%', '')
df['Unemployment rate'] = df['Unemployment rate'].astype(float)
#remove commas from Urban population column
df['Urban population'] = df['Urban population'].str.replace(',', '')
df['Urban population'] = df['Urban population'].astype(float)
#turn life expenctancy into into so it can be used as a TARGET variable
df['Life expectancy'] = df['Life expectancy'].astype(int)
```

C:\Users\almas\AppData\Local\Temp/ipykernel_8696/1912219860.py:37: FutureWarning: The de fault value of regex will change from True to False in a future version. In addition, si ngle character regular expressions will *not* be treated as literal strings when regex=T rue.

df['Gasoline Price'] = df['Gasoline Price'].str.replace('\$', '')
C:\Users\almas\AppData\Local\Temp/ipykernel_8696/1912219860.py:41: FutureWarning: The de
fault value of regex will change from True to False in a future version. In addition, si
ngle character regular expressions will *not* be treated as literal strings when regex=T
rue.

df['GDP'] = df['GDP'].str.replace('\$', '')

All NUMERIC columns that were data type 'object' are now changed to 'float64'. Target Varible 'Life Expectancy' is changed into 'int32'

```
In [ ]:
         df.dtypes
        Country
                                                        object
Out[]:
        Density\n(P/Km2)
                                                       float64
        Agricultural Land( %)
                                                       float64
        Land Area(Km2)
                                                       float64
        Armed Forces size
                                                       float64
                                                       float64
        Birth Rate
        Co2-Emissions
                                                       float64
        CPI
                                                       float64
        CPI Change (%)
                                                       float64
        Fertility Rate
                                                       float64
        Forested Area (%)
                                                       float64
        Gasoline Price
                                                       float64
        GDP
                                                       float64
        Infant mortality
                                                       float64
        Life expectancy
                                                         int32
        Out of pocket health expenditure
                                                       float64
        Physicians per thousand
                                                       float64
        Population
                                                       float64
        Population: Labor force participation (%)
                                                       float64
        Tax revenue (%)
                                                       float64
        Total tax rate
                                                       float64
        Unemployment rate
                                                       float64
        Urban population
                                                       float64
        dtype: object
In [ ]:
         df
```

Out[]:

| | Country | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | Co2- Emissions | СРІ | Cha |
|-----|------------------|------------------|--------------------------|-------------------|----------------------|---------------|-------------------|--------|-----|
| 0 | Afghanistan | 60.00 | 58.10 | 652230.00 | 323000.00 | 32.49 | 8672.00 | 149.90 | |
| 1 | Albania | 105.00 | 43.10 | 28748.00 | 9000.00 | 11.78 | 4536.00 | 119.05 | |
| 2 | Algeria | 18.00 | 17.40 | 2381741.00 | 317000.00 | 24.28 | 150006.00 | 151.36 | |
| 4 | Angola | 26.00 | 47.50 | 1246700.00 | 117000.00 | 40.73 | 34693.00 | 261.73 | 1 |
| 6 | Argentina | 17.00 | 54.30 | 2780400.00 | 105000.00 | 17.02 | 201348.00 | 232.75 | 5 |
| ••• | | | | | | | | | |
| 186 | United States | 36.00 | 44.40 | 9833517.00 | 1359000.00 | 11.60 | 5006302.00 | 117.24 | |
| 187 | Uruguay | 20.00 | 82.60 | 176215.00 | 22000.00 | 13.86 | 6766.00 | 202.92 | |
| 191 | Vietnam | 314.00 | 39.30 | 331210.00 | 522000.00 | 16.75 | 192668.00 | 163.52 | |
| 193 | Zambia | 25.00 | 32.10 | 752618.00 | 16000.00 | 36.19 | 5141.00 | 212.31 | |
| 194 | Zimbabwe | 38.00 | 41.90 | 390757.00 | 51000.00 | 30.68 | 10983.00 | 105.51 | (|
| | ows × 23 col | umns | | | | | | | |
| 4 | | | | | | | | | • |

Visualizations

Correlation matrix in text and heatmap (to idenitfy relationships and to help with feature selection)

Rate Forested Area (%) Gasoline Price GDP Infant mortality Life expectancy Out of

Area(Km2) Armed Forces size Birth Rate Co2-Emissions

Correlation Heatmap (Text Representation):

Density\n(P/Km2) Agricultural Land(%) Land

CPI CPI Change (%) Fertility

| | | ysicians per tho | | | | |
|----------------|-------------|------------------|----------|-------|-------------|------------|
| | | e (%) Total tax | rate | | rate Urban_ | population |
| Density\n(P/Km | • | | | 1.00 | | -0.14 |
| -0.09 | -0.01 | -0.15 | -0.02 | -0.06 | -0.08 | -0.1 |
| 5 | -0.12 | 0.10 -0.01 | | -0.12 | 0.18 | 1 |
| 0.03 | 0.03 | 0.00 | | | | 0.07 |
| -0.05 | -0.16 | -0.12 | | -0.01 | | |
| Agricultural L | and(%) | | | -0.14 | | 1.00 |
| -0.05 | 0.05 | 0.16 | 0.06 | 0.04 | 0.05 | 0.1 |
| 5 | -0.40 | -0.05 0.05 | | 0.14 | -0.22 | |
| 0.10 | -0.04 | 0.12 | | | | -0.11 |
| 0.04 | 0.10 | 0.13 | | 0.10 | | |
| Land Area(Km2) | | | | -0.09 | | -0.05 |
| 1.00 | 0.58 | -0.08 | 0.59 | 0.06 | 0.08 | -0.07 |
| 0.04 | -0.20 0.54 | -0.08 | | 0.05 | | |
| -0.04 | 0.0 | 8 0.44 | | | | -0.00 |
| -0.16 | 0.17 | 0.06 | | 0.54 | | |
| Armed Forces s | ize | | | -0.01 | | 0.05 |
| 0.58 | 1.00 | -0.13 | 0.77 | 0.05 | 0.08 | -0.13 |
| -0.02 | -0.17 0.63 | -0.06 | | 0.07 | | |
| 0.18 | -0.03 | | | | | -0.15 |
| -0.20 | 0.17 | 0.01 | | 0.89 | | |
| Birth Rate | 0.1 | 0.02 | | -0.15 | | 0.16 |
| -0.08 | -0.13 | 1.00 | -0 16 | 0.25 | 0.21 | 0.9 |
| 8 | -0.05 | -0.24 -0.20 | 0.10 | 0.88 | -0.88 | |
| 0.26 | -0.75 | | | 0.00 | 0.00 | 0.23 |
| -0.39 | 0.17 | -0.03 | | -0.11 | | 0.23 |
| Co2-Emissions | 0.17 | -0.03 | | -0.02 | | 0.06 |
| 0.59 | 0.77 | -0.16 | 1 00 | -0.02 | 0.01 | -0.14 |
| -0.01 | -0.08 0.92 | -0.10 | | 0.12 | 0.01 | -0.14 |
| | | | <u>-</u> | 0.12 | | 0 02 |
| -0.04 | 0.0 | | | 0.03 | | -0.02 |
| -0.15 | 0.12 | 0.02 | | 0.93 | | 0.04 |
| CPI | 0.05 | 0.25 | 0 02 | -0.06 | 0.60 | 0.04 |
| 0.06 | 0.05 | | -0.02 | | 0.68 | 0.23 |
| -0.09 | -0.13 -0.06 | 0.24 | | -0.24 | | 0.13 |
| 0.18 | -0.22 | | | 0.01 | | -0.12 |
| | | 0.18 | | | | 0.05 |
| CPI Change (%) | | 0 21 | 0 01 | -0.08 | | 0.05 |
| 0.08 | | 0.21 | | | | 0.19 |
| | -0.07 -0.02 | 0.25 | • | -0.24 | | 0.14 |
| 0.13 | -0.15 | 0.05 | | 0.04 | | -0.14 |
| | | 0.16 | | | | 0.45 |
| Fertility Rate | | 0.98 | | -0.15 | 0.40 | 0.15 |
| | | | | | | |
| | -0.05 | -0.18 -0.17 | | 0.86 | -0.85 | |
| 0.22 | -0.69 | -0.05 | | | | 0.22 |
| | | -0.06 | | | | |
| Forested Area | | | | -0.12 | | -0.40 |
| | | -0.05 | | | -0.08 | -0.05 |
| | | 0.01 | | -0.01 | | |
| -0.19 | -0.0 | 5 -0.03 | | | | 0.13 |
| 0.02 | 0.09 | -0.11 | | -0.01 | | |
| Gasoline Price | | | | 0.10 | | -0.05 |
| -0.20 | | -0.24 | | -0.13 | -0.07 | -0.1 |
| 8 | | 1.00 -0.02 | | -0.20 | 0.29 |) |
| -0.30 | 0.3 | 3 -0.08 | | | | -0.02 |
| 0.46 | 0.06 | -0.02 | | -0.08 | | |
| GDP | | | | -0.01 | | 0.05 |
| 0.54 | 0.63 | -0.20 | 0.92 | -0.06 | -0.02 | -0.17 |
| 0.02 | -0.02 1.00 | -0.16 | | 0.18 | | |
| | | | | | | |

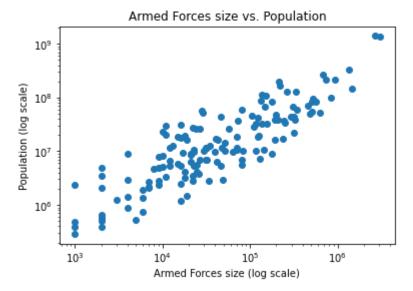
| | | pr | roject2 | |
|------------------|----------------------------|---------------------|----------------------------|-------------|
| -0.12 | | 0.63 | | -0.01 |
| -0.12 | 0.10 | 0.05 | 0.78 | |
| Infant mortalit | . y | 0.88 -0.20 -0.16 | -0.12 | 0.14 |
| -0.08 | -0.06 | 0.88 | -0.12 0.24 | 0.25 0.8 |
| 6 | 0.01 | -0.20 -0.16 | 1.00 | -0.93 |
| 0.32 | -0.72 | | | 0.19 |
| | 0 18 | -0.02 | -0.05 | 3.25 |
| life expectancy | , | 0.02 | 0.03 0.18 | -0.22 |
| 0 05 | , a a7 | -0 88 | 0.18 0.12 -0.24 1.00 | -0.24 -0.85 |
| -0.05 | 0.07 | -0.00 | 1.00 | 0.03 |
| -0.31 | | 2 -0.00 | 1.00 | -0.20 |
| 0.36 | | -0.04 | 0 06 | -0.20 |
| | | | | 0.10 |
| Out of pocket h | o 10 | ure a ac | 0.03 -0.04 0.18 | 0.10 |
| | | | | |
| | | -0.30 -0.12 | | -0.31 |
| 1.00 | -0.24 | 0.15 | 0.07 | -0.19 |
| | | | | |
| Physicians per | | | 0.03 | -0.04 |
| | | | 0.05 -0.22 | -0.15 -0.69 |
| | | | 0.72 | |
| -0.24 | | 0 -0.07 | | -0.20 |
| 0.38 | -0.07 | 0.08 | -0.02 | |
| Population | | | 0.00 | 0.12 |
| | | | 0.81 0.03 | 0.05 -0.05 |
| -0.03 | | | -0.00 | |
| 0.15 | -0.07 | 1.00 | | -0.07 |
| -0.19 | 0.15 | -0.03 | 0.95 | |
| Population: Lab | or force parti | cipation (%) | 0.07 | -0.11 |
| -0.00 | -0.15 | 0.23 | 0.07 -0.02 -0.12 | -0.14 0.2 |
| 2 | 0.13 | -0.02 -0.01 | 0.19 | -0.20 |
| | -0.2 | 0 -0.07 | | 1.00 |
| -0.19 -0.17 | -0.17 | -0.46 | -0.06 | |
| Tax revenue (%) |) | | -0.05 | 0.04 |
| -0.16 | -0.20 | -0.39 | -0.15 -0.20 | -0.24 -0.3 |
| 9 | | 0.46 -0.12 | -0.37 | 0.36 |
| -0.29 | | 8 -0.19 | 0.57 | -0.17 |
| 1.00 | | 0.26 | -0.18 | 0.17 |
| Total tax rate | | 0.20 | -0.16 | 0.10 |
| 0.17 | 0 17 | 0 17 | | 0.31 0.18 |
| 0.17 | 0.17 | 0.17 | 0.12 0.10 | 0.31 |
| 0.09 | 0.00 0.10 | 0.18 | -0.10 | 0 17 |
| 0.14 | 0.06 0.10 -0.07 1.00 | 0.15 | 0.10 | -0.17 |
| -0.09 | 1.00 | 0.03 | 0.18 | 0.42 |
| Unemployment ra | | | -0.12 | 0.13 |
| 0.06 | 0.01 | -0.03 | 0.02 0.18 | 0.16 -0.06 |
| | | | -0.04 | |
| 0.01 | | -0.03 | | -0.46 |
| 0.26 | | 1.00 | 0.00 | |
| Urban_population | | | -0.01 | 0.10 |
| 0.54 | 0.89 | -0.11 | 0.93 0.01 | 0.04 -0.10 |
| -0.01 | -0.08 0.78 | -0.05 | 0.06 | |
| 0.07 | -0.02 | 0.95 | | -0.06 |
| -0.18 | 0.18 | 0.00 | 1.00 | |
| | | | | |

```
Correlation Heatmap
                                                                                                                                                                    - 1 00
                                                <mark>-1.00</mark>0.140.090.0<u>1</u>0.150.020.060.080.150.1<mark>20.10</mark>0.010.12<mark>0.180</mark>.030.030.00<mark>0.07</mark>0.050.160.120.01
                      Agricultural Land( %) -0.141000.050.050.160.060.040.050.150.400.050.050.140.220.100.040.120.110.040.100.130.10
                            Land Area(Km2) -0.090.091000.580.080.590.060.080.070.040.200.540.080.050.040.080.440.000.160.170.060.9
                                                                                                                                                                    - 0.75
                         Armed Forces size -0.010.050.581.000.130.770.050.080.130.020.170.630.060.070.180.030.910.150.200.170.010.89
                                   Birth Rate -0.150.160.080.131.000.160.250.210.960.050.240.200.880.860.260.750.050.230.390.170.030.11
                              Co2-Emissions -0.020.060.590.770.161.000.020.010.140.010.080.920.120.120.040.050.810.020.150.120.020.93
                                                                                                                                                                    -0.50
                                           CPI -0.060.040.060.050.250.021.000.680.230.090.130.060.240.240.180.220.030.120.260.100.180.01
                            CPI Change (%) -0.080.050.080.080.210.010.681.000.190.080.070.020.250.240.130.150.050.140.240.310.160.04
                                Fertility Rate -0.150.150.070.130.980.140.230.191.000.050.180.170.860.850.220.650.050.220.390.180.060.10
                                                                                                                                                                    -0.25
                          Forested Area (%) -0.120.400.040.020.050.010.090.080.010000.220.020.010.010.190.050.030.130.020.090.110.01
                              Gasoline Price -0.100.050.200.170.240.080.130.070.180.221.000.020.200.290.300.330.080.020.4c0.060.020.08
                                          GDP -0.010.050.540.630.200.920.060.020.170.020.021.000.160.180.120.100.630.010.120.100.050.78
                                                                                                                                                                   -0.00
                            Infant mortality -0.120.140.080.060.8860.120.240.250.860.010.200.161.000.950.320.770.020.190.370.180.020.05
                            Life expectancy -0.180.220.050.070.880.120.240.240.840.010.290.180.931.000.310.720.000.200.360.100.040.06
                                                                                                                                                                    -0.25
        Out of pocket health expenditure -0.030.100.040.180.260.040.180.130.220.190.300.120.320.331.000.0.240.150.190.290.140.010.07
                  Physicians per thousand -0.030.040.080.050.750.050.220.150.650.050.330.100.720.720.24L000.070.200.380.070.080.02
                                  Population -0.000.12<mark>0.44</mark>0.910.050.810.030.050.050.030.050.060.030.020.000.150.071.000.070.190.150.050.95
                                                                                                                                                                      -0.50
Population: Labor force participation (%) -0.070.110.000.150.230.020.120.140.220.130.020.010.190.200.190.200.071.000.170.170.460.06
                            Tax revenue (%) -0.050.040.160.290.390.150.290.240.390.020.460.120.370.360.290.380.190.171.000.090.260.18
                                Total tax rate -0.160.100.170.170.170.120.10<mark>0.31</mark>0.180.090.060.10<mark>0.18</mark>0.100.140.07<mark>0.15</mark>0.170.09<mark>1.00</mark>0.03<mark>0.18</mark>
                                                                                                                                                                    -0.75
                       Unemployment rate -0.120.130.060.010.030.020.180.160.060.110.020.050.020.040.010.080.030.460.260.031.000.00
                          Urban population -0.010.100.540.890.110.930.010.040.100.010.060.780.050.060.070.010.950.060.180.180.001.00
                                                                  Birth Rate
                                                                            굡
                                                                                CPI Change (%)
                                                              Armed Forces size
                                                                       Co2-Emissions
                                                                                      Fertility Rate
                                                                                          Forested Area (%)
                                                                                               Gasoline Price
                                                                                                    gb
                                                                                                        Infant mortality
                                                                                                                  Out of pocket health expenditure
                                                                                                                       Physicians per thousand
                                                                                                                                Population: Labor force participation (%)
                                                                                                                                    Tax revenue (%)
                                                                                                                                                   Urban_population
                                                    Agricultural Land(%)
                                                         Land Area(Km2)
                                                                                                             Life expectancy
                                                                                                                                              Unemployment rate
                                                                                                                                         Total tax rate
```

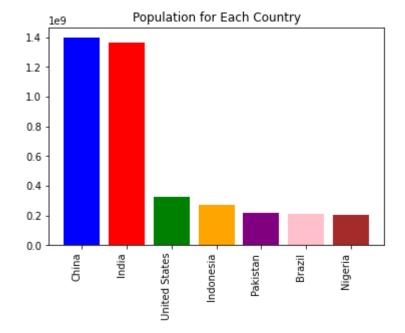
```
In []: #scatter plot with a logarithmic scale
   plt.scatter(x=df['Armed Forces size'], y=df['Population'])
   plt.xscale('log')
   plt.yscale('log')

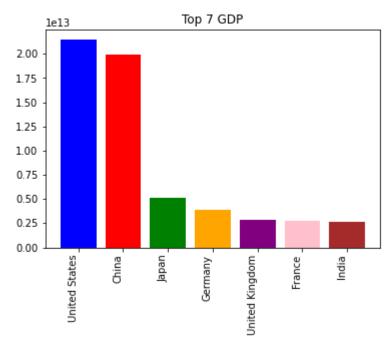
# labels
   plt.xlabel('Armed Forces size (log scale)')
   plt.ylabel('Population (log scale)')

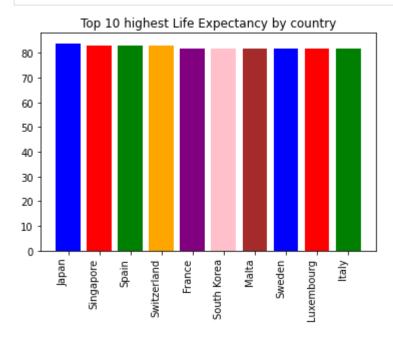
   plt.title('Armed Forces size vs. Population')
Out[]: Text(0.5, 1.0, 'Armed Forces size vs. Population')
```

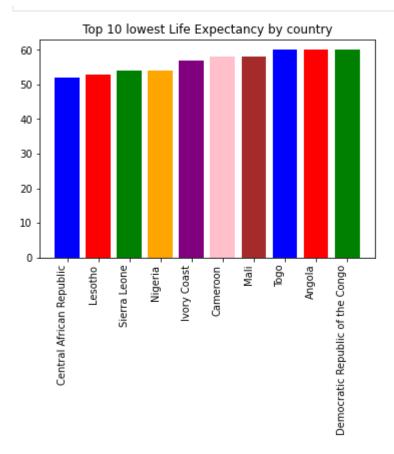


Bar graph of top 7 most populated countries







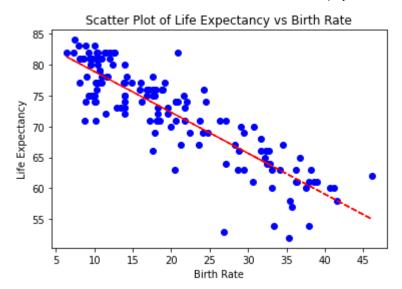


```
In []:
    birth_rate = df['Birth Rate']
    life_expectancy = df['Life expectancy']

plt.scatter(birth_rate, life_expectancy, color='blue')
    plt.xlabel('Birth Rate')
    plt.ylabel('Life Expectancy')
    plt.title('Scatter Plot of Life Expectancy vs Birth Rate')

# Add best fit line

#get coefficients for best fit
    coefficients = np.polyfit(birth_rate, life_expectancy, 1)
    #equation of best fit line
    polynomial = np.polyId(coefficients)
    plt.plot(birth_rate, polynomial(birth_rate), color='red', linestyle='--', label='Line o
    plt.show()
```



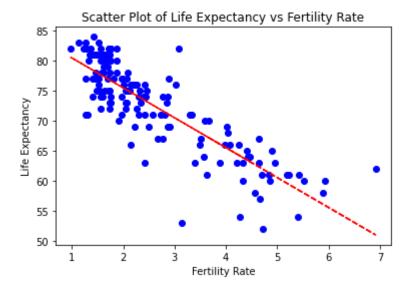
```
In []:
    fertility_rate = df['Fertility Rate']
    life_expectancy = df['Life expectancy']

    plt.scatter(fertility_rate, life_expectancy, color='blue')
    plt.xlabel('Fertility Rate')
    plt.ylabel('Life Expectancy')
    plt.title('Scatter Plot of Life Expectancy vs Fertility Rate')

# Add a line of best fit

    coefficients = np.polyfit(fertility_rate, life_expectancy, 1)
    polynomial = np.polyd(coefficients)
    plt.plot(fertility_rate, polynomial(fertility_rate), color='red', linestyle='--', label

    plt.show()
```

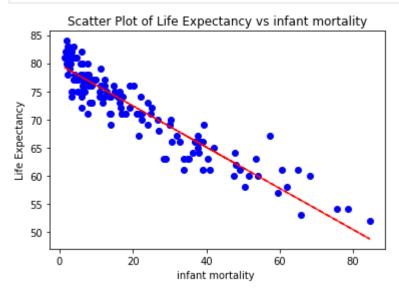


```
infant_mortality = df['Infant mortality']
life_expectancy = df['Life expectancy']

plt.scatter(infant_mortality, life_expectancy, color='blue')
plt.xlabel('infant mortality ')
```

```
plt.ylabel('Life Expectancy')
plt.title('Scatter Plot of Life Expectancy vs infant mortality')

# Add best fit line
coefficients = np.polyfit(infant_mortality, life_expectancy, 1)
polynomial = np.poly1d(coefficients)
plt.plot(infant_mortality, polynomial(infant_mortality), color='red', linestyle='--')
plt.show()
```

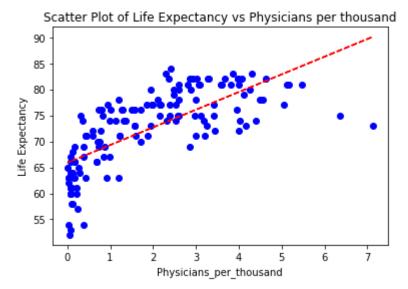


```
In []:
    Physicians_per_thousand = df['Physicians per thousand']
    life_expectancy = df['Life expectancy']

# Create a scatter plot
    plt.scatter(Physicians_per_thousand, life_expectancy, color='blue')
    plt.xlabel('Physicians_per_thousand')
    plt.ylabel('Life Expectancy')
    plt.title('Scatter Plot of Life Expectancy vs Physicians per thousand')

# Add a line of best fit
    coefficients = np.polyfit(Physicians_per_thousand, life_expectancy, 1)
    polynomial = np.polyld(coefficients)
    plt.plot(Physicians_per_thousand, polynomial(Physicians_per_thousand), color='red', lin
```

Out[]: [<matplotlib.lines.Line2D at 0x2120e4a3970>]



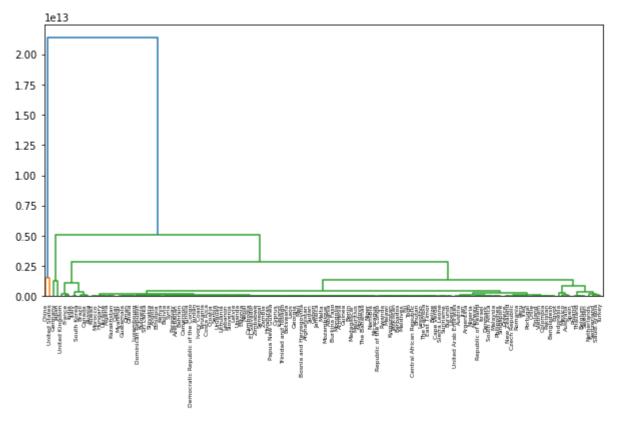
EDA, Clustering

Hierarchical Clustering

```
from scipy.cluster.hierarchy import linkage, dendrogram
import matplotlib.pyplot as plt
from sklearn.preprocessing import normalize
```

We need to seperate Country col from the rest of the df

```
In [ ]: # remove the 'Country' column from the DataFrame before clustering
    numerical_features_df = df.drop(columns=['Country'])
    country=df.Country.values
```



Feature Elimination

Recursive Feature Elimination Cross Validation to reduce features to find out the most important ones

```
In [ ]:
         import matplotlib.pyplot as plt
         from sklearn.svm import SVC
         from sklearn.model selection import StratifiedKFold
         from sklearn.feature_selection import RFECV
         from sklearn.datasets import make_classification
         %matplotlib inline
In [ ]:
         from sklearn.linear_model import LogisticRegression
         #max iter to make sure algorithm reaches convergence
         logit=LogisticRegression(multi_class='ovr',solver='lbfgs',max_iter=200000)
        Set X and y to features and target
In [ ]:
         from sklearn.preprocessing import StandardScaler
         scaler = StandardScaler()
         X=df.drop(columns=['Country','Life expectancy'])
         y=df['Life expectancy']
         Χ
```

Out[]:

| | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | Co2- Emissions | СРІ | CPI Change (%) | Fertility Rate |
|-----|------------------|--------------------------|-------------------|----------------------|---------------|-------------------|--------|----------------------|-------------------|
| 0 | 60.00 | 58.10 | 652230.00 | 323000.00 | 32.49 | 8672.00 | 149.90 | 2.30 | 4.47 |
| 1 | 105.00 | 43.10 | 28748.00 | 9000.00 | 11.78 | 4536.00 | 119.05 | 1.40 | 1.62 |
| 2 | 18.00 | 17.40 | 2381741.00 | 317000.00 | 24.28 | 150006.00 | 151.36 | 2.00 | 3.02 |
| 4 | 26.00 | 47.50 | 1246700.00 | 117000.00 | 40.73 | 34693.00 | 261.73 | 17.10 | 5.52 |
| 6 | 17.00 | 54.30 | 2780400.00 | 105000.00 | 17.02 | 201348.00 | 232.75 | 53.50 | 2.26 |
| ••• | | | | | | | | | |
| 186 | 36.00 | 44.40 | 9833517.00 | 1359000.00 | 11.60 | 5006302.00 | 117.24 | 7.50 | 1.73 |
| 187 | 20.00 | 82.60 | 176215.00 | 22000.00 | 13.86 | 6766.00 | 202.92 | 7.90 | 1.97 |
| 191 | 314.00 | 39.30 | 331210.00 | 522000.00 | 16.75 | 192668.00 | 163.52 | 2.80 | 2.05 |
| 193 | 25.00 | 32.10 | 752618.00 | 16000.00 | 36.19 | 5141.00 | 212.31 | 9.20 | 4.63 |
| 194 | 38.00 | 41.90 | 390757.00 | 51000.00 | 30.68 | 10983.00 | 105.51 | 0.90 | 3.62 |

146 rows × 21 columns

1

RFECV without scaling X (we get a warning if we dont scale the data, beacuse the algorthim is having difficulty reaching *convergance*)

```
# Reduced number of splits and 'roc_auc' scoring
rfecv = RFECV(estimator=logit, step=1, cv=StratifiedKFold(10), scoring='accuracy')
rfecv.fit(X, y)
```

```
In [ ]: print(f"Optimal number of features : {rfecv.n_features_}")
```

Optimal number of features : 3

3 features yields the highest cross validation score

```
plt.figure()
   plt.xlabel("Number of features selected")
   plt.ylabel("Cross validation score (nb of correct classifications)")
   plt.plot(range(1, len(rfecv.grid_scores_) + 1), rfecv.grid_scores_)
   plt.show()
```

```
Cross validation score (nb of correct classifications)
    0.12
    0.10
    0.08
    0.06
    0.04
    0.02
                       2.5
                                  5.0
                                               7.5
                                                          10.0
                                                                     12.5
                                                                                             17.5
                                                                                                         20.0
           0.0
                                                                                 15.0
                                            Number of features selected
```

```
In [ ]:
         print(rfecv.support )
         print("Selected Features: ",X.columns[rfecv.support_])
        [False False False True False False False True False False False
         False False True False False False False False]
        Selected Features: Index(['Birth Rate', 'Fertility Rate', 'Physicians per thousand'], d
        type='object')
        Ranking = 1 means that RFECV has chosen the feature
In [ ]:
         rfecv.ranking
        array([12, 9, 15, 14, 1, 13, 11, 4, 1, 10, 18, 19, 2, 8,
                                                                       1, 17,
Out[]:
                   7, 3, 16])
        RFECV with sacling X, to make sure the algorithm reaches convergence
In [ ]:
         from sklearn.preprocessing import StandardScaler
         scaler = StandardScaler()
         X scaled = scaler.fit transform(X)
         rfecv = RFECV(estimator=logit, step=1, cv=StratifiedKFold(10), scoring='accuracy')
         rfecv.fit(X scaled, y)
        c:\Users\almas\anaconda3\lib\site-packages\sklearn\model selection\ split.py:666: UserWa
        rning: The least populated class in y has only 1 members, which is less than n_splits=1
          warnings.warn(("The least populated class in y has only %d"
        RFECV(cv=StratifiedKFold(n_splits=10, random_state=None, shuffle=False),
Out[ ]:
              estimator=LogisticRegression(max iter=200000, multi class='ovr'),
              scoring='accuracy')
In [ ]:
         print(f"Optimal number of features : {rfecv.n features }")
         selected features= X.columns[rfecv.support ]
         print("Selected Features: ",selected_features)
         #create a df using the selected features
         selected_features_df = X[selected_features]
         selected features df
```

Out[]:

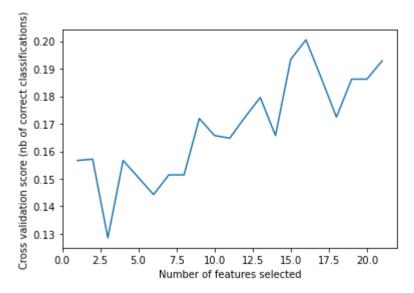
| | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | СРІ | CPI Change (%) | Fertility Rate | Forested Area (%) | Gasoline Price | Infant mortality |
|-----|--------------------------|-------------------|----------------------|---------------|--------|----------------------|-------------------|-------------------------|-------------------|---------------------|
| 0 | 58.10 | 652230.00 | 323000.00 | 32.49 | 149.90 | 2.30 | 4.47 | 2.10 | 0.70 | 47.90 |
| 1 | 43.10 | 28748.00 | 9000.00 | 11.78 | 119.05 | 1.40 | 1.62 | 28.10 | 1.36 | 7.80 |
| 2 | 17.40 | 2381741.00 | 317000.00 | 24.28 | 151.36 | 2.00 | 3.02 | 0.80 | 0.28 | 20.10 |
| 4 | 47.50 | 1246700.00 | 117000.00 | 40.73 | 261.73 | 17.10 | 5.52 | 46.30 | 0.97 | 51.60 |
| 6 | 54.30 | 2780400.00 | 105000.00 | 17.02 | 232.75 | 53.50 | 2.26 | 9.80 | 1.10 | 8.80 |
| ••• | | | | | | | | | | |
| 186 | 44.40 | 9833517.00 | 1359000.00 | 11.60 | 117.24 | 7.50 | 1.73 | 33.90 | 0.71 | 5.60 |
| 187 | 82.60 | 176215.00 | 22000.00 | 13.86 | 202.92 | 7.90 | 1.97 | 10.70 | 1.50 | 6.40 |
| 191 | 39.30 | 331210.00 | 522000.00 | 16.75 | 163.52 | 2.80 | 2.05 | 48.10 | 0.80 | 16.50 |
| 193 | 32.10 | 752618.00 | 16000.00 | 36.19 | 212.31 | 9.20 | 4.63 | 65.20 | 1.40 | 40.40 |
| 194 | 41.90 | 390757.00 | 51000.00 | 30.68 | 105.51 | 0.90 | 3.62 | 35.50 | 1.34 | 33.90 |

146 rows × 16 columns

→

16 features yields the highest cross validation score

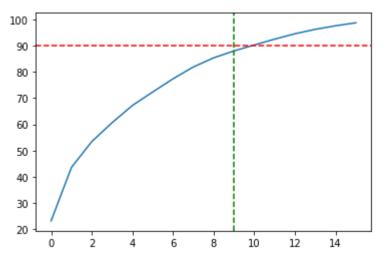
```
#plot CV score with number of features selected
plt.figure()
plt.xlabel("Number of features selected")
plt.ylabel("Cross validation score (nb of correct classifications)")
plt.plot(range(1, len(rfecv.grid_scores_) + 1), rfecv.grid_scores_)
plt.show()
```



PCA

Dimensionality reduction algorithm on **selcted_features_df**, to reduce the dimensions of the dataframe

```
In [ ]:
         from sklearn.decomposition import PCA
         pca_Object = PCA(n_components=16)
         pca Object.fit(X scaled)
         pca_X = pca_Object.transform(X)
In [ ]:
         #The amount of variance that each PC explains
         var Data= pca Object.explained variance ratio
         #Cumulative Variance explains
         var1_Data=np.cumsum(np.round(pca_Object.explained_variance_ratio_, decimals=4)*100)
         var1 Data
        array([23.18, 43.54, 53.4, 60.61, 67.18, 72.32, 77.35, 81.87, 85.34,
Out[]:
               87.98, 90.24, 92.47, 94.52, 96.21, 97.57, 98.71])
In [ ]:
         plt.plot(var1 Data)
         plt.axhline(y=90, color='red', linestyle='--')
         plt.axvline(x=9, color='green', linestyle='--')
         plt.show()
```



Selecting features that have > 90% of the variance (9 features in this case)

```
In [ ]:
         from sklearn.decomposition import PCA
         from sklearn import decomposition
         pcaOBJ = decomposition.PCA(n components=9)
         pcaOBJ.fit(pca_X)
         obj = pcaOBJ.transform(pca_X)
         print("obj shape: ",obj.shape)
         obj
        obj shape: (146, 9)
        array([[-4.87493786e+11, 7.29694423e+06, -9.48837518e+04, ...,
Out[ ]:
                 -1.97292447e+02, -1.57562916e+01, -4.40227242e+01],
               [-4.90576478e+11, -1.92718691e+07, -5.03016090e+05, ...,
                -1.34243206e+02, -2.79482985e+01, -9.88525772e+00],
               [-3.65685046e+11, 1.47602551e+07, 1.98171091e+06, ...,
                -1.47821908e+02, -2.85436096e+01, -1.51489105e+01],
               [-2.91477272e+11, 4.78513204e+07, -6.13503980e+05, ...,
                 1.94506550e+01, -8.08257122e+00, 1.49074173e+01],
               [-4.84291735e+11, -7.01658472e+06, 1.50381783e+05, ...,
                -1.82729399e+02, 5.22851105e+01, 3.78757973e+01],
               [-4.85602729e+11, -1.04848006e+07, -2.28985431e+05, ...,
                -1.91586820e+02, -5.09214783e+01, 6.35052490e+00]])
In [ ]:
         import pandas as pd
         # Convert the 'obj' array into a DataFrame
         pca df = pd.DataFrame(obj)
         # Print the DataFrame containing the chosen principal components with updated column na
         print(pca_df)
                                           1
                                                       2
                                                                  3
                                                                            4
             -487493786286.97
                                 7296944.23
                                               -94883.75
                                                          293155.97
        0
                                                                     25075.00
        1
             -490576478144.36
                                            -503016.09
                                                         -38965.69
                              -19271869.06
                                                                     -7349.40
        2
             -365685046327.28
                                14760255.08 1981710.91 -134068.24
                                                                     19735.61
        3
             -426515000792.43
                                 5499636.44
                                              765716.05 -118533.82
                                                                      -446.08
        4
             -139910852947.05
                                 9360349.40 2375281.85 -338646.30 -10305.89
        141 16794992860626.67 -536659176.46 -1665092.48 3011280.81 40423.10
```

```
142 -457665749541.99 -19774800.46 -351530.98
                                                -51741.36 -5544.30
143 -291477272304.45
                                                224789.70 40564.44
                       47851320.39
                                    -613503.98
144 -484291734611.70
                       -7016584.72
                                     150381.78
                                                 67663.12 -13902.30
145 -485602729205.39 -10484800.58
                                    -228985.43
                                                 83918.12
                                                          -7096.85
           5
                          7
                   6
    -10631.59 -197.29 -15.76 -44.02
1
     -2708.75 -134.24 -27.95 -9.89
     -391.50 -147.82 -28.54 -15.15
3
     6531.91 -170.07 89.28 11.03
4
    16199.47 -105.59 57.68 -30.45
                        . . .
          . . .
                  . . .
141 20006.63 -177.45 58.16
                             -8.67
142 -1615.29 -215.07 44.31 -36.88
143 -15125.34
               19.45
                      -8.08 14.91
144
     2864.06 -182.73 52.29 37.88
145 -2157.83 -191.59 -50.92
                              6.35
[146 rows x 9 columns]
```

Split data into train and test (for both orginal dataframe and PCA dataframe)

Split data

```
In [ ]:
    #set X and Y
    df.columns
    df_X = df.drop(columns=['Life expectancy','Country'])
    df_y=df['Life expectancy']
    df_X
```

Out[]:

| | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | Co2- Emissions | СРІ | CPI Change (%) | Fertility Rate |
|-----|------------------|--------------------------|-------------------|----------------------|---------------|-------------------|--------|----------------------|-------------------|
| 0 | 60.00 | 58.10 | 652230.00 | 323000.00 | 32.49 | 8672.00 | 149.90 | 2.30 | 4.47 |
| 1 | 105.00 | 43.10 | 28748.00 | 9000.00 | 11.78 | 4536.00 | 119.05 | 1.40 | 1.62 |
| 2 | 18.00 | 17.40 | 2381741.00 | 317000.00 | 24.28 | 150006.00 | 151.36 | 2.00 | 3.02 |
| 4 | 26.00 | 47.50 | 1246700.00 | 117000.00 | 40.73 | 34693.00 | 261.73 | 17.10 | 5.52 |
| 6 | 17.00 | 54.30 | 2780400.00 | 105000.00 | 17.02 | 201348.00 | 232.75 | 53.50 | 2.26 |
| ••• | | | | | | | | | |
| 186 | 36.00 | 44.40 | 9833517.00 | 1359000.00 | 11.60 | 5006302.00 | 117.24 | 7.50 | 1.73 |
| 187 | 20.00 | 82.60 | 176215.00 | 22000.00 | 13.86 | 6766.00 | 202.92 | 7.90 | 1.97 |
| 191 | 314.00 | 39.30 | 331210.00 | 522000.00 | 16.75 | 192668.00 | 163.52 | 2.80 | 2.05 |
| 193 | 25.00 | 32.10 | 752618.00 | 16000.00 | 36.19 | 5141.00 | 212.31 | 9.20 | 4.63 |
| 194 | 38.00 | 41.90 | 390757.00 | 51000.00 | 30.68 | 10983.00 | 105.51 | 0.90 | 3.62 |

146 rows × 21 columns

```
In [ ]: from sklearn.model_selection import train_test_split
    #orginal df
    df_X_train, df_X_test, df_y_train, df_y_test = train_test_split(df_X, df_y, test_size=0)
#PCA df
    pca_X_train, pca_X_test, pca_y_train, pca_y_test = train_test_split(pca_df, df_y, test_size=0)
In [ ]: df_X_train
```

Out[]:

| | Density\n(P/Km2) | Agricultural Land(%) | Land Area(Km2) | Armed Forces size | Birth Rate | Co2- Emissions | СРІ | CPI Change (%) | Fertility Rate |
|-----|------------------|--------------------------|-------------------|-------------------------|---------------|-------------------|--------|----------------------|-------------------|
| 119 | 3.00 | 47.10 | 824292.00 | 16000.00 | 28.64 | 4228.00 | 157.97 | 3.70 | 3.40 |
| 82 | 400.00 | 24.60 | 20770.00 | 178000.00 | 20.80 | 65166.00 | 108.15 | 0.80 | 3.09 |
| 2 | 463.00 | 79.20 | 27830.00 | 31000.00 | 39.01 | 495.00 | 182.11 | -0.70 | 5.41 |
| (| 17.00 | 54.30 | 2780400.00 | 105000.00 | 17.02 | 201348.00 | 232.75 | 53.50 | 2.26 |
| 69 | 53.00 | 59.00 | 245857.00 | 13000.00 | 36.36 | 2996.00 | 262.95 | 9.50 | 4.70 |
| • | • | | | | | | | | |
| 8 | 72.00 | 64.50 | 70273.00 | 9000.00 | 12.50 | 37711.00 | 106.58 | 0.90 | 1.75 |
| 88 | 94.00 | 48.50 | 580367.00 | 29000.00 | 28.75 | 17910.00 | 180.51 | 4.70 | 3.49 |
| 102 | 203.00 | 61.40 | 118484.00 | 15000.00 | 34.12 | 1298.00 | 418.34 | 9.40 | 4.21 |
| 13 | 1265.00 | 70.60 | 148460.00 | 221000.00 | 18.18 | 84246.00 | 179.68 | 5.60 | 2.04 |
| 122 | 508.00 | 53.30 | 41543.00 | 41000.00 | 9.70 | 170780.00 | 115.91 | 2.60 | 1.59 |

102 rows × 21 columns

| In []: | рс | pca_X_train | | | | | | | | | | | |
|---------|-----|------------------|--------------|------------|------------|-----------|----------|---------|--------|--------|--|--|--|
| Out[]: | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | | | |
| | 93 | -492926879761.13 | -19717685.69 | 256225.54 | 98781.60 | -11653.80 | -1115.61 | -201.53 | -0.06 | -14.45 | | | |
| | 64 | -183959199408.05 | -27185565.61 | -623347.54 | -68353.35 | 18859.10 | -6318.34 | 134.32 | -43.21 | -5.67 | | | |
| | 23 | -500479450191.16 | -13257115.23 | -613016.44 | 93768.01 | -8092.75 | -3646.17 | 215.76 | 25.75 | -31.44 | | | |
| | 4 | -139910852947.05 | 9360349.40 | 2375281.85 | -338646.30 | -10305.89 | 16199.47 | -105.59 | 57.68 | -30.45 | | | |
| | 55 | -491939923727.14 | -11411869.72 | -347960.33 | 30812.81 | -10788.27 | -372.50 | -177.48 | 97.91 | -16.82 | | | |
| | ••• | | | | | | | | | | | | |

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|----|------------------|--------------|-------------|-----------|-----------|----------|---------|--------|--------|
| 63 | -189125853565.30 | -32173212.42 | -695049.22 | 66042.76 | -7560.54 | 225.08 | -172.24 | -39.09 | -25.86 |
| 70 | -425818347608.60 | 15742854.47 | -348130.07 | 326042.23 | -22711.15 | 5840.07 | -126.89 | 23.52 | -17.46 |
| 81 | -496722856174.43 | -8073093.00 | -583445.79 | 150327.81 | -13331.71 | -1680.22 | -34.93 | 243.66 | 4.09 |
| 11 | -258667874182.18 | 104258888.57 | -1150506.61 | 265280.72 | -14807.03 | 22589.15 | 995.19 | 37.40 | -34.07 |
| 95 | 230953991129.07 | -38835968.31 | -872017.13 | -73547.49 | -3141.47 | 3172.27 | 254.38 | -28.03 | -19.89 |

102 rows × 9 columns

Regression learning algorithms

Linear Regression (Original DF)

```
In [ ]:
         # import model
         from sklearn.linear_model import LinearRegression
         # instantiate
         linreg = LinearRegression()
         # fit the model to the training data (learn the coefficients)
         linreg.fit(df_X_train, df_y_train)
        LinearRegression()
Out[]:
In [ ]:
         # print the intercept and coefficients
         print(linreg.intercept )
         print(linreg.coef )
        85.4435090872766
        [ 1.84055701e-04 -4.35098883e-02 3.47239592e-07 4.20157735e-06
          3.33298458e-02 -1.22994058e-05 -3.98249478e-03 -2.72815435e-02
         -1.26333909e+00 -4.05463409e-02 1.37548973e+00 2.60968148e-12
         -2.71481873e-01 -1.62726276e-02 3.41912389e-01 1.41881517e-08
         -5.08852319e-02 -2.35309539e-02 2.38153255e-02 -9.73249186e-02
         -2.19851545e-08]
In [ ]:
         # make predictions on the testing set
         df_y_pred = linreg.predict(df_X_test)
In [ ]:
         from sklearn import metrics
         df lr mae=metrics.mean absolute error(df y test, df y pred)
         df lr mse=metrics.mean squared error(df y test, df y pred)
         df lr rmse=np.sqrt(metrics.mean squared error(df y test, df y pred))
         print('Mean Absoulute Error',df lr mae)
         print('Mean Squared Error:',df lr mse)
         print('Root Mean Squared Error: ',df_lr_rmse)
```

Mean Absoulute Error 3.2640263593722225 Mean Squared Error: 73.34989071379162 Root Mean Squared Error: 8.564455073954887

Linear Regression (PCA DF)

```
In [ ]:
         # instantiate
         linreg = LinearRegression()
         # fit the model to the training data (learn the coefficients)
         linreg.fit(pca_X_train, pca_y_train)
        LinearRegression()
Out[ ]:
In [ ]:
         # print the intercept and coefficients
         print(linreg.intercept )
         print(linreg.coef )
        71.60813416620944
        [ 3.70777203e-13 -1.36824062e-08 -2.05564542e-07 -1.79670327e-09
          5.01305770e-05 2.22923475e-05 1.81176697e-03 -6.89317500e-02
          1.81977457e-02]
In [ ]:
         # make predictions on the testing set
         pca_y_pred = linreg.predict(pca_X_test)
In [ ]:
         from sklearn import metrics
         pca lr mae=metrics.mean absolute error(pca y test, pca y pred)
         pca_lr_mse=metrics.mean_squared_error(pca_y_test, pca_y_pred)
         pca_lr_rmse=np.sqrt(metrics.mean_squared_error(pca_y_test, pca_y_pred))
         print('Mean Absoulute Error',pca lr mae)
         print('Mean Squared Error:',pca_lr_mse)
         print('Root Mean Squared Error: ',pca_lr_rmse)
        Mean Absoulute Error 7.031591494863505
        Mean Squared Error: 169.2208982835762
        Root Mean Squared Error: 13.008493313354018
       SVM (Original DF)
       Without scaling
In [ ]:
         # Fitting SVR to the dataset
         from sklearn.svm import SVR
         regressor = SVR(kernel = 'rbf',gamma='auto')
         regressor.fit(df_X_train, df_y_train)
        SVR(gamma='auto')
Out[]:
In [ ]:
         df_y_pred_no_scaling = regressor.predict(df_X_test)
```

```
In [ ]:
         predictions = [[206,43.2,301340,347000,7.3,320411,110.62,0.6,1.29,31.8,1.61,20012443920]
         # Scale the prediction data
         scaler X = StandardScaler()
         scaler X.fit(predictions)
         scaled_prediction = scaler_X.transform(predictions)
         # Predict using the scaled input
         predicted value = regressor.predict(scaled prediction)
         # Print the predicted value
         print("Predicted Life expectancy:", predicted_value)
         print('Actual Life expectancy: ',)
        Predicted Life expectancy: [74.04545455]
        Actual Life expectancy: 82
         [74.04545455]
        Actual Life expectancy: 82
In [ ]:
         print('Mean Absoulute Error',metrics.mean_absolute_error(df_y_test, df_y_pred_no_scalin
         print('Mean Squared Error:',metrics.mean_squared_error(df_y_test, df_y_pred_no_scaling)
         print('Root Mean Squared Error: ',np.sqrt(metrics.mean_squared_error(df_y_test, df_y_pr
        Mean Absoulute Error 5.890495867768595
        Mean Squared Error: 55.81611570247933
        Root Mean Squared Error: 7.471018384563067
       SVM with Scaling
In [ ]:
         #scaling
         from sklearn.preprocessing import StandardScaler
         scaler X = StandardScaler()
         df X scaled = scaler X.fit transform(df X train)
In [ ]:
         #create and fit SVR using scaled values
         regressor = SVR(kernel='rbf', gamma='auto')
         regressor.fit(X scaled, y)
        SVR(gamma='auto')
Out[ ]:
In [ ]:
         predictions = [[206,43.2,301340,347000,7.3,320411,110.62,0.6,1.29,31.8,1.61,20012443920]
         # Scale the prediction data
         scaled prediction = scaler X.transform(predictions)
         # Predict using scaled input
         predicted value = regressor.predict(scaled prediction)
         # Print the predicted value
         print("Predicted Life expectancy:", predicted_value)
         print('Actual Life expectancy: 82')
        Predicted Life expectancy: [80.88365092]
        Actual Life expectancy: 82
```

```
In [ ]:
         print('Mean Absoulute Error',metrics.mean_absolute_error(df_y_test, df_y_pred))
         print('Mean Squared Error:',metrics.mean_squared_error(df_y_test, df_y_pred))
         print('Root Mean Squared Error: ',np.sqrt(metrics.mean_squared_error(df_y_test, df_y_pr
        Mean Absoulute Error 3.2640263593722225
        Mean Squared Error: 73.34989071379162
        Root Mean Squared Error: 8.564455073954887
       SVM (PCA df)
       Without scaling
In [ ]:
         regressor = SVR(kernel = 'rbf',gamma='auto')
         regressor.fit(pca X train, pca y train)
        SVR(gamma='auto')
Out[ ]:
In [ ]:
         pca y pred no scaling = regressor.predict(pca X test)
In [ ]:
         pca predictions = [[-258667874182.18,104258888.57,-1150506.61,265280.72,-14807.03,22589
         # Scale the prediction data
         scaler X = StandardScaler()
         scaler X.fit(pca X train)
         pca_scaled_prediction = scaler_X.transform(pca_predictions)
         # Predict using the scaled input
         pca predicted value = regressor.predict(pca scaled prediction)
         # Print the predicted value
         print("Predicted Life expectancy:", pca_predicted_value)
         print('Actual Life expectancy: 82')
        Predicted Life expectancy: [74.04545455]
        Actual Life expectancy: 82
In [ ]:
         pca svm mae=metrics.mean absolute error(pca y test, pca y pred)
         pca_svm_mse=metrics.mean_squared_error(pca_y_test, pca_y_pred)
         pca svm rmse=np.sqrt(metrics.mean squared error(pca y test, pca y pred))
         print('Mean Absoulute Error',pca_svm_mae)
         print('Mean Squared Error:',pca_svm_mse)
         print('Root Mean Squared Error: ',pca svm rmse)
        Mean Absoulute Error 7.031591494863505
        Mean Squared Error: 169.2208982835762
        Root Mean Squared Error: 13.008493313354018
       With scaling
In [ ]:
         #scaling
         from sklearn.preprocessing import StandardScaler
         scaler X = StandardScaler()
         pca X scaled = scaler X.fit transform(pca X train)
```

```
In [ ]:
         #create and fit SVR using scaled values
         regressor = SVR(kernel='rbf', gamma='auto')
         regressor.fit(pca X scaled, pca y train)
        SVR(gamma='auto')
Out[]:
In [ ]:
         pca predictions = [[-258667874182.18,104258888.57,-1150506.61,265280.72,-14807.03,22589]
         # Scale the prediction data
         scaler X = StandardScaler()
         scaler X.fit(pca X train)
         pca scaled prediction = scaler X.transform(pca predictions)
         # Predict using the scaled input
         pca predicted value = regressor.predict(pca scaled prediction)
         # Print the predicted value
         print("Predicted Life expectancy:", pca_predicted_value)
         print('Actual Life expectancy: 80')
        Predicted Life expectancy: [71.62540858]
        Actual Life expectancy: 80
In [ ]:
         pca svmS mae=metrics.mean absolute error(pca y test, pca y pred)
         pca svmS mse=metrics.mean squared error(pca y test, pca y pred)
         pca_svmS_rmse=np.sqrt(metrics.mean_squared_error(pca_y_test, pca_y_pred))
         print('Mean Absoulute Error',pca_svmS_mae)
         print('Mean Squared Error:',pca_svmS_mse)
         print('Root Mean Squared Error: ',pca_svmS_rmse)
        Mean Absoulute Error 7.031591494863505
        Mean Squared Error: 169.2208982835762
        Root Mean Squared Error: 13.008493313354018
        KNN Regression (Original DF)
In [ ]:
         from sklearn.neighbors import KNeighborsRegressor
         from sklearn.model selection import cross val score
         knn_regressor = KNeighborsRegressor(n_neighbors=5)
         #Use scaled X
         knn regressor.fit(df X train, df y train)
        KNeighborsRegressor()
Out[]:
In [ ]:
         from sklearn.model selection import cross val score
         from sklearn.neighbors import KNeighborsRegressor
         k_range = list(range(1, 31))
         k scores MAE = []
         k scores MSE = []
         k_scores_RMSE = []
         min_k_MAE = k_range[0]
         min k MSE = k range[0]
         min k RMSE = k range[0]
```

for k in k range:

```
knn = KNeighborsRegressor(n neighbors=k)
             # Use 'neg mean absolute error' as the scoring metric
             scores_MAE = cross_val_score(knn, df_X_train, df_y_train, cv=10, scoring='neg_mean_
             k scores MAE.append(-scores MAE.mean())
         for k in k range:
             knn = KNeighborsRegressor(n_neighbors=k)
             # Use 'neg_mean_squared_error' as the scoring metric
             scores MSE = cross val score(knn, df X train, df y train, cv=10, scoring='neg mean
             k scores MSE.append(-scores MSE.mean())
         for k in k range:
             knn = KNeighborsRegressor(n_neighbors=k)
             # Use 'neg_root_mean_squared_error' as the scoring metric
             scores_RMSE = cross_val_score(knn, df_X_train, df_y_train, cv=10, scoring='neg_root
             k_scores_RMSE.append(-scores_RMSE.mean())
         k scores MAE.sort()
         k scores MSE.sort()
         k_scores_RMSE.sort()
         print('Minimum MAE:', k_scores_MAE[0], 'at k =', min_k_MAE)
         print('Minimum MSE:', k_scores_MSE[0], 'at k =', min_k_MSE)
         print('Minimum RMSE:', k_scores_RMSE[0], 'at k =', min_k_RMSE)
        Minimum MAE: 5.559870129870131 at k = 1
        Minimum MSE: 46.58687899402185 at k = 1
        Minimum RMSE: 6.604713443110066 at k = 1
       KNN Regression (PCA df)
In [ ]:
         from sklearn.neighbors import KNeighborsRegressor
         from sklearn.model selection import cross val score
         knn_regressor = KNeighborsRegressor(n_neighbors=5)
         knn regressor.fit(pca X train, pca y train)
        KNeighborsRegressor()
Out[ ]:
In [ ]:
         from sklearn.model selection import cross val score
         from sklearn.neighbors import KNeighborsRegressor
         k range = list(range(1, 31))
         pca_k_scores_MAE = []
         pca k scores MSE = []
         pca k scores RMSE = []
         min_k_MAE = k_range[0]
         min_k_MSE = k_range[0]
         min k RMSE = k range[0]
         for k in k range:
             knn = KNeighborsRegressor(n neighbors=k)
             # Use 'neg_mean_absolute_error' as the scoring metric
             scores_MAE = cross_val_score(knn, pca_X_train, pca_y_train, cv=10, scoring='neg_mea'
             pca k scores MAE.append(-scores MAE.mean())
```

```
for k in k range:
     knn = KNeighborsRegressor(n neighbors=k)
     # Use 'neg mean squared error' as the scoring metric
     scores_MSE = cross_val_score(knn, pca_X_train, pca_y_train, cv=10, scoring='neg_mea'
     pca k scores MSE.append(-scores MSE.mean())
for k in k range:
     knn = KNeighborsRegressor(n neighbors=k)
     # Use 'neg_root_mean_squared_error' as the scoring metric
     scores RMSE = cross val score(knn, pca X train, pca y train, cv=10, scoring='neg ro
     pca k scores RMSE.append(-scores RMSE.mean())
pca k scores MAE.sort()
pca_k_scores_MSE.sort()
pca_k_scores_RMSE.sort()
print("MAE scores:")
for k, score in zip(k range, k scores MAE):
     print("k =", k, "MAE =", score)
print("\nMSE scores:")
for k, score in zip(k range, k scores MSE):
     print("k =", k, "MSE =", score)
print("\nRMSE scores:")
for k, score in zip(k_range, k_scores_RMSE):
     print("k =", k, "RMSE =", score)
MAE scores:
k = 1 MAE = 5.559870129870131
k = 2 MAE = 5.577090909090909
k = 3 MAE = 5.58603305785124
k = 4 MAE = 5.5901010101010105
k = 5 MAE = 5.60267942583732
k = 6 MAE = 5.618636363636363
k = 7 MAE = 5.630121212121212
k = 8 MAE = 5.634743083003952
k = 9 MAE = 5.646420454545455
k = 10 MAE = 5.6551636363636355
k = 11 MAE = 5.65979020979021
k = 12 MAE = 5.661643356643357
k = 13 MAE = 5.661711229946524
k = 14 \text{ MAE} = 5.671598746081505
k = 15 \text{ MAE} = 5.685422077922078
k = 16 \text{ MAE} = 5.687077922077922
k = 17 \text{ MAE} = 5.688212121212121
k = 18 \text{ MAE} = 5.690033670033669
k = 19 \text{ MAE} = 5.752499999999999
k = 20 MAE = 5.7841414141414145
k = 21 \text{ MAE} = 5.797909090909091
k = 22 MAE = 5.828512396694215
k = 23 MAE = 5.880795454545455
k = 24 MAE = 5.945454545454545
k = 25 \text{ MAE} = 5.991363636363635
k = 26 \text{ MAE} = 6.083090909090909
k = 27 \text{ MAE} = 6.287954545454546
k = 28 MAE = 6.824545454545455
k = 29 \text{ MAE} = 7.129545454545455
```

k = 30 MAE = 7.4227272727272

MSE scores:

- k = 1 MSE = 46.58687899402185
- k = 2 MSE = 46.69948181818183
- k = 3 MSE = 46.777253787878784
- k = 4 MSE = 46.85133358377159
- k = 5 MSE = 46.86868446654417
- k = 6 MSE = 47.07009548144164
- k = 7 MSE = 47.08132799999999
- k = 8 MSE = 47.1026393939394
- k = 9 MSE = 47.14599345253086
- k = 10 MSE = 47.21397379406308
- k = 11 MSE = 47.361157251527615
- k = 12 MSE = 47.44026936026937
- k = 13 MSE = 47.47800481182334
- k = 14 MSE = 47.91210443535704
- k = 15 MSE = 48.136615767045456
- k = 16 MSE = 48.20710707070707
- k = 17 MSE = 48.71043033889187
- k = 18 MSE = 49.41036641929499
- k = 19 MSE = 49.82027146464647
- k = 20 MSE = 50.300681818181815
- k = 21 MSE = 50.63913580246914
- k = 22 MSE = 51.09359128474831 k = 23 MSE = 51.74509943181819
- k = 24 MSE = 52.9969573283859
- k = 25 MSE = 54.05542929292928
- k = 26 MSE = 57.44425454545454
- k = 27 MSE = 61.12335227272727
- k = 28 MSE = 69.9249494949495 k = 29 MSE = 76.77386363636363
- k = 30 MSE = 90.9009090909091

RMSE scores:

- k = 1 RMSE = 6.604713443110066
- k = 2 RMSE = 6.6177688685869995
- k = 3 RMSE = 6.621117640262172
- k = 4 RMSE = 6.626885443241572
- k = 5 RMSE = 6.649646223739947
- k = 6 RMSE = 6.649748701978079
- k = 7 RMSE = 6.653014433461443
- k = 8 RMSE = 6.6591523090502465
- k = 9 RMSE = 6.668777816434617
- k = 10 RMSE = 6.670497428290341
- k = 11 RMSE = 6.676416612257256
- k = 12 RMSE = 6.678124672699113
- k = 13 RMSE = 6.685631333103286
- k = 14 RMSE = 6.720406837360675
- k = 15 RMSE = 6.748622374986992
- k = 16 RMSE = 6.760062472606554
- k = 17 RMSE = 6.787917913681817
- k = 18 RMSE = 6.83219262360767
- k = 19 RMSE = 6.869665695377165
- k = 20 RMSE = 6.887678949578192 k = 21 RMSE = 6.888104366033588
- k = 21 RMSE = 6.888104366033588 k = 22 RMSE = 6.951764087690283
- k = 23 RMSE = 6.952990742983587
- k = 24 RMSE = 7.053922891738419
- k = 25 RMSE = 7.111311505688965
- k = 26 RMSE = 7.320246818563701

```
k = 27 RMSE = 7.5610146161599605
k = 28 RMSE = 8.098451858996993
k = 29 RMSE = 8.405167919718448
k = 30 RMSE = 9.098034490730683
```

Decision Tree (Original DF)

```
In [ ]:
         from sklearn.tree import DecisionTreeClassifier
In [ ]:
         dtree = DecisionTreeClassifier()
In [ ]:
         dtree.fit(df X train,df y train)
        DecisionTreeClassifier()
Out[ ]:
In [ ]:
         df y pred dt = dtree.predict(df X test)
In [ ]:
         from sklearn.metrics import mean absolute error, mean squared error, r2 score, explaine
         df_dt_mae = mean_absolute_error(df_y_test, df_y_pred_dt)
         df_dt_mse = mean_squared_error(df_y_test, df_y_pred_dt)
         df dt rmse = np.sqrt(df dt mse)
         df_dt_r2 = r2_score(df_y_test, df_y_pred_dt)
         df_dt_ev = explained_variance_score(df_y_test, df_y_pred_dt)
         print("Mean Absolute Error:", df_dt_mae)
         print("Mean Squared Error:", df dt mse)
         print("Root Mean Squared Error:", df_dt_rmse)
         print("R-squared:", df_dt_r2)
         print("Explained Variance Score:", df_dt_ev)
        Mean Absolute Error: 3.0
        Mean Squared Error: 16.045454545454547
        Root Mean Squared Error: 4.005677788521506
        R-squared: 0.7042509639643928
        Explained Variance Score: 0.7088589517779789
       Decision Tree (PCA DF)
In [ ]:
         from sklearn.tree import DecisionTreeClassifier
In [ ]:
         dtree = DecisionTreeClassifier()
In [ ]:
         dtree.fit(pca_X_train,pca_y_train)
        DecisionTreeClassifier()
Out[]:
```

pca_y_pred_dt = dtree.predict(pca_X_test)

In []:

In []:

```
from sklearn.metrics import mean absolute error, mean squared error, r2 score, explaine
         pca dt mae = mean absolute error(pca y test, pca y pred dt)
         pca_dt_mse = mean_squared_error(pca_y_test, pca_y_pred_dt)
         pca dt rmse = np.sqrt(pca dt mse)
         pca_dt_r2 = r2_score(pca_y_test, pca_y_pred_dt)
         pca_dt_ev = explained_variance_score(pca_y_test, pca_y_pred_dt)
         print("Mean Absolute Error:", pca_dt_mae)
         print("Mean Squared Error:", pca_dt_mse)
         print("Root Mean Squared Error:", pca_dt_rmse)
         print("R-squared:", pca dt r2)
         print("Explained Variance Score:", pca dt ev)
        Mean Absolute Error: 4.5
        Mean Squared Error: 37.09090909090909
        Root Mean Squared Error: 6.0902306270706275
        R-squared: 0.3163421716570667
        Explained Variance Score: 0.3578140619793402
       Random Forest (orgainal DF)
In [ ]:
         from sklearn.ensemble import RandomForestClassifier
In [ ]:
         rfc = RandomForestClassifier(n estimators=600)
In [ ]:
         rfc.fit(df X train,df y train)
        RandomForestClassifier(n_estimators=600)
Out[ ]:
In [ ]:
         predictions rf = rfc.predict(df X test)
In [ ]:
         from sklearn.metrics import classification report,confusion matrix
In [ ]:
         from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score, explaine
         mae = mean absolute error(df y test, predictions rf)
         mse = mean_squared_error(df_y_test, predictions_rf)
         rmse = np.sqrt(mse)
         r2 = r2 score(df y test, predictions rf)
         ev = explained variance score(df y test, predictions rf)
         print("Mean Absolute Error:", mae)
         print("Mean Squared Error:", mse)
         print("Root Mean Squared Error:", rmse)
         print("R-squared:", r2)
         print("Explained Variance Score:", ev)
        Mean Absolute Error: 2.0454545454545454
        Mean Squared Error: 7.8636363636363
        Root Mean Squared Error: 2.8042176027613057
        R-squared: 0.8550578378635693
        Explained Variance Score: 0.8564288094444709
```

Random Forest (PCA DF)

```
In [ ]:
         from sklearn.ensemble import RandomForestClassifier
In [ ]:
         rfc = RandomForestClassifier(n estimators=600)
In [ ]:
         rfc.fit(pca X train,pca y train)
        RandomForestClassifier(n estimators=600)
Out[ ]:
In [ ]:
         predictions rf = rfc.predict(pca X test)
In [ ]:
         from sklearn.metrics import classification_report,confusion_matrix
         from sklearn.metrics import mean absolute error, mean squared error, r2 score, explaine
         mae = mean_absolute_error(pca_y_test, predictions_rf)
         mse = mean_squared_error(pca_y_test, predictions_rf)
         rmse = np.sqrt(mse)
         r2 = r2_score(pca_y_test, predictions_rf)
         ev = explained_variance_score(pca_y_test, predictions_rf)
         print("Mean Absolute Error:", mae)
         print("Mean Squared Error:", mse)
         print("Root Mean Squared Error:", rmse)
         print("R-squared:", r2)
         print("Explained Variance Score:", ev)
        Mean Absolute Error: 3.70454545454546
        Mean Squared Error: 25.1136363636363
        Root Mean Squared Error: 5.011350752405619
        R-squared: 0.5371066787261389
```

Explained Variance Score: 0.543057076212691

Regression learning algorithms Summary

```
In [ ]:
         import pandas as pd
         summary = {
             'Model': ['Linear Regression (ODF)', 'Linear Regression (PCA DF)', 'SVM (ODF NO SCA
                        'SVM (PCA DF With SCALING)', 'KNN (ODF)', 'KNN (PCA DF)', 'DT (ODF)', 'DT
             'MAE': [3.26, 7.03, 5.89, 3.26, 7.03, 7.03, 5.56, 5.56, 3.00, 4.50, 2.05, 3.70],
             'MSE': [73.35, 169.22, 55.82, 73.35, 169.22, 169.22, 46.59, 46.78, 16.05, 37.09, 7.
             'RMSE': [8.56, 13.01, 7.47, 8.56, 13.01, 13.01, 6.60, 6.62, 4.01, 6.09, 2.80, 5.01]
         }
         df = pd.DataFrame(summary)
         df
```

```
Out[]:
                                Model MAE
                                               MSE RMSE
                  Linear Regression (ODF)
                                        3.26
                                              73.35
                                                      8.56
```

| 1 | Linear Regression (P Model | M'9E | 1 64.5E | RM:SE |
|----|-----------------------------------|------|----------------|-------|
| 2 | SVM (ODF NO SCALING) | 5.89 | 55.82 | 7.47 |
| 3 | SVM (ODF With SCALING) | 3.26 | 73.35 | 8.56 |
| 4 | SVM (PCA DF NO SCALING) | 7.03 | 169.22 | 13.01 |
| 5 | SVM (PCA DF With SCALING) | 7.03 | 169.22 | 13.01 |
| 6 | KNN (ODF) | 5.56 | 46.59 | 6.60 |
| 7 | KNN (PCA DF) | 5.56 | 46.78 | 6.62 |
| 8 | DT (ODF) | 3.00 | 16.05 | 4.01 |
| 9 | DT (PCA DF) | 4.50 | 37.09 | 6.09 |
| 10 | Random Forest (ODF) | 2.05 | 7.86 | 2.80 |
| 11 | Random Forest (PCA DF) | 3.70 | 25.11 | 5.01 |

Report

Top 2 algorithms

Random Forest (Original DF):

The Random Forest algorithm applied to the original DataFrame demonstrates outstanding performance in predicting life expectancy. With a Mean Absolute Error (MAE) of 2.05 and a Root Mean Squared Error (RMSE) of 2.80, the model provides highly accurate predictions. The low MAE and RMSE scores indicate that the model's predictions are, on average, very close to the actual life expectancy values. The strength of Random Forest lies in its ability to handle complex relationships within the data, making it robust against overfitting. By combining multiple decision trees and averaging their outputs, Random Forest reduces the risk of individual tree biases and increases overall prediction accuracy. This makes it a powerful and reliable choice for life expectancy prediction.

Decision Tree (Original DF):

The Decision Tree algorithm, when applied to the original DataFrame, also exhibits commendable performance in predicting life expectancy. With a Mean Absolute Error (MAE) of 3.0 and a Root Mean Squared Error (RMSE) of 4.01, the model delivers relatively accurate predictions. Decision Trees are easy to understand and interpret, making them valuable for gaining insights into feature importance and the decision-making process. However, compared to Random Forest, Decision Trees might be more prone to overfitting, especially on complex datasets. Nonetheless, the model's performance is still satisfactory, and its simplicity and interpretability make it an attractive option for scenarios where model interpretability is of extreme importance or when dealing with smaller datasets.

The rest of the algorithms

The remaining algorithms, including Linear Regression and SVM, show varying levels of performance in predicting life expectancy. While SVM demonstrates good performance with proper scaling, Linear Regression performs reasonably well. However, both PCA-based models (Linear Regression and SVM) show lower accuracy compared to the original DataFrame. KNN models provide moderate performance but are sensitive to the choice of the number of

neighbors (k). In summary, SVM and Linear Regression models can provide useful insights, but Random Forest and Decision Tree models offer superior accuracy for life expectancy prediction.

In conclusion, both the Random Forest and Decision Tree models applied to the original DataFrame show promise in predicting life expectancy. The Random Forest stands out as the top performer, providing superior accuracy and robustness to complex data relationships. On the other hand, the Decision Tree offers simplicity and interpretability, making it suitable for scenarios where model transparency and explainability are essential. The choice between these models would depend on the specific requirements of the project and the trade-offs between accuracy and interpretability.

Correlation analysis

Birth Rate (-0.88 correlation):The strong negative correlation between life expectancy and birth rate indicates that countries with higher birth rates tend to have lower life expectancies. High birth rates can put a strain on healthcare systems and resources, impacting overall public health and access to medical care.

Fertility Rate (-0.85 correlation): The negative correlation between life expectancy and fertility rate suggests that countries with higher fertility rates also tend to have lower life expectancies. High fertility rates can lead to challenges in providing adequate healthcare and social services, which can impact population health and life expectancy.

Infant Mortality (-0.93 correlation):The significant negative correlation between life expectancy and infant mortality underscores the critical link between early-life health and overall life expectancy. Lower infant mortality rates indicate better access to healthcare and improved maternal and child health.

Physicians per Thousand (0.72 correlation): The positive correlation between life expectancy and the number of physicians per thousand reflects the importance of healthcare access and medical resources in improving life expectancy. Countries with more physicians per thousand are better equipped to provide medical care and preventive services, positively impacting life expectancy.

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