

1. Supervised Learning with scikit-learn

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①

- ML = Giving Computers the ability to learn to make decisions from data
① without being explicitly programmed

- Supervised learning = uses labeled data

- Unsupervised learning = uses unlabeled data

① uncovering hidden patterns from unlabeled data

eg grouping customers in to distinct categories based on purchasing behavior

(clustering)

- Reinforcement learning = ① interacts with an environment
② learn how to optimize their behavior
③ Given a system of rewards and punishment
④ Draws inspiration from behavioral psychology

Supervised Learning

① predictor variables (x) = Features = independent variable

② Target variable (y) = dependent variable = response variable

↳ Classification: categorical variable

↳ Regression: continuous variable or float

2 Exploratory Data Analysis

Iris dataset

```
from sklearn import datasets  
import pandas as pd
```

```
" numpy " np
```

```
" matplotlib.pyplot as plt
```

```
plt.style.use('ggplot')
```

```
iris = datasets.load_iris()
```

type(iris) → Bunch → similar to dictionary

```
type(iris.data), type(iris.target)
```

```
iris.data.shape
```

```
iris.target_names
```

EDA

```
X = iris.data
```

```
Y = iris.target
```

```
df = pd.DataFrame(X, columns=iris.feature_names)
```

```
print(df.head())
```

knn = KNeighborsClassifier(n_neighbors=8)

knn.fit(X_train, y_train)

y_pred = knn.predict(X_test)

print("\n Test set predictions: \n { } ".format(y_pred))

Accuracy

knn.score(X_test, y_test)

Introduction to regression

- Target is continuous variable

boston = pd.read_csv('boston.csv')

boston.head()

Creating feature and target arrays

X = boston.drop('MEDV', axis=1).values

y = boston['MEDV'].values

Predicting house prices from a single feature

X_rooms = X[:, 5] # no. of room column

type(X_rooms), type(y)

Reshaping

y = y.reshape(-1, 1)

X_rooms = X_rooms.reshape(-1, 1) # size 1

keep first dimension ~~and~~ ^{but}
add another dimension of

Plotting house values v/s no. of rooms

plt.scatter(X_rooms, y)

plt.ylabel('Value of house / 1000 (\$)')

plt.xlabel('Number of rooms')

plt.show()

Linear Regression on all features

```
from sklearn.model_selection import train_test_split
```

```
" " .linear_model " LinearRegression
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3,
                                                    random_state=42)
```

```
reg_all = LinearRegression()
```

```
reg_all.fit(X_train, y_train)
```

```
y_pred = reg_all.predict(X_test)
```

```
reg_all.score(X_test, y_test)
```

Cross Validation - 5 folds = 5-fold CV
k folds = k-fold CV

Motivation

- Model performance is dependent on the way data is split
- Not representative of the model's ability to generalize

Split 1	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	Metric 1
.
.
.
.
.

Split 5						Metric 5
.
.
.
.
.

- Divide data in to 5 Fold \rightarrow Step 1 \rightarrow fit data on rest of data and use Fold 1 as test \rightarrow repeat for every fold.

```
from sklearn.model_selection import cross_val_score
" " linear_model " LinearRegression
```

```
reg = LinearRegression()
```

```
cv_results = cross_val_score(reg, X, y, cv=5)
```

```
print(cv_results)
```

```
np.mean(cv_results)
```

Lasso for feature selection in scikit-learn

```
from sklearn.linear_model import Lasso
names = boston.drop('MEDV', axis=1).columns
lasso = Lasso(alpha=0.1)
lasso_coeff = lasso.fit(X, y).coef_
- = plt.plot(range(len(names)), lasso_coeff)
- = plt.xticks(range(len(names)), names, rotation=60)
- = plt.ylabel('Coefficients')
plt.show()
```

Fine tune your Model

How good is your model

Classification metrics

- Accuracy is not always a useful metric

Case imbalance examples: Emails

- Spam classification

- 99% of emails are real
- 1% of emails are spam

- Building a model that predicts All emails are real will be 99% accurate but horrible at actually classifying spam

Diagnosing classification predictions

① Confusion Matrix

	Predicted spam	Actual Predicted real
Actual spam	TP	FN
Actual real	FP	TN

① F1 score: $2 \cdot \frac{\text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$
↓
harmonic mean of precision and recall

↓
class of interest is +ve class

$$\text{Accuracy} = \frac{tp + tn}{tp + tn + fp + fn}$$

$$\text{Precision} = \frac{tp}{tp + fp} = \text{PPV}$$

↓
positive predicted value

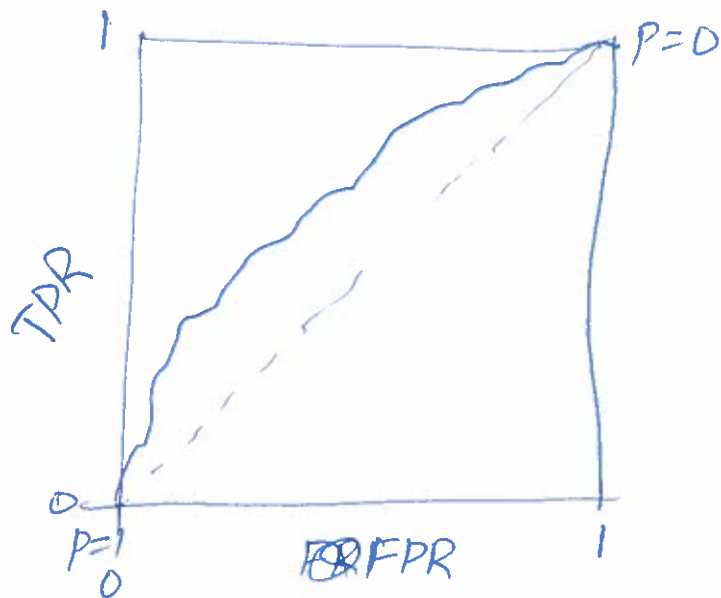
$$\text{Recall} = \frac{tp}{tp + fn}$$

→ sensitivity
Hit rate
TPR → true positive rate

Probability threshold

- By default, logistic Regression threshold = 0.5
- ~~At class~~ Not specific to logreg
 - o k-NN also has a threshold
 - o What happens if we vary this threshold

The ROC-curve (Receiver Operating Characteristic Curve)



$\rightarrow = \frac{TP}{P} = 1 - FNR$
 TDR = sensitivity = recall
 \rightarrow probability of detection

FPR = probability of false alarm
 \rightarrow fall-out

$$FPR = \frac{FP}{N} = \frac{FP}{FP+TN} \quad (\text{1-TNR})$$

Plotting ROC-curve

from sklearn.metrics import roc_curve

y_pred_prob = logreg.predict_proba(X_test)[:,-1]

fpr, tpr, thresholds = roc_curve(y_test, y_pred_prob)

plt.plot([0,1], [0,1], 'k--')

plt.plot(fpr, tpr, label='Logistic Regression')

plt.xlabel('False Positive Rate')

plt.ylabel('True Positive Rate')

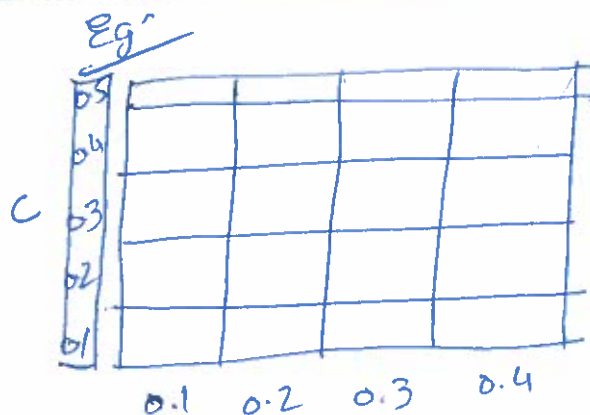
plt.title('Logistic Regression ROC Curve')

plt.show()

Choosing Correct Hyperparameter

- ① Try bunch of different hyperparameters values
- ① Fit all of them separately
- ① See how well each performs
- ① Choose the best performing one
- ① It is essential to use cross-validation

Grid Search cross-validation



pick best set of
alpha and C

from sklearn.model_selection import GridSearchCV

param_grid = {'n_neighbors': np.arange(1, 50)}

knn = KNeighborsClassifier()

knn_cv = GridSearchCV(knn, param_grid, cv=5)

knn_cv.fit(X, y)

knn_cv.best_param_

knn_cv.best_score_

Hold-out set for final evaluation

- ① How well can the model perform on never before seen data?
- ① using ALL data for cross-validation is not ideal.
- ① Split data into training and hold-out set at the beginning.
- ① Perform grid search cross-validation on training set.

- ## Scaling in sklearn

$\text{np.mean}(x)$, $\text{np.std}(x)$

Scaling in a pipeline

```
Steps = [('scale', StandardScaler()),  
         ('knn', KNeighborsClassifier())]
```

~~pipeline.~~
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=21)

```
y_pred = pipeline.predict(x_test)
```

accuracy_score(y_test, y_pred)

$$km_unscaled = k \cdot km_scaled$$

$$km_unscaled \cdot score(x_test, y_test)$$

2-1 (2) Unsupervised Learning

k-means Clustering Clustering for dataset Exploration

- ① Finds clusters of samples
- ① Number of clusters must be specified
- ① Implemented in sklearn ("scikit-learn")

```
from sklearn.cluster import KMeans
```

```
model = KMeans(n_clusters=3)
```

```
model.fit(samples)
```

```
labels = model.predict(samples)
```

```
labels.
```

Cluster labels for new samples

- ① New samples can be assigned to existing clusters.
- ① k-means remembers the mean of each cluster (the centroids)
- ① Finds the nearest centroid to each new sample.

```
new_samples
```

```
new_labels = model.predict(new_samples)
```

Scatter plots

```
import matplotlib.pyplot as plt
```

```
xs = samples[:, 0]
```

```
ys = samples[:, 2]
```

```
plt.scatter(xs, ys, c=labels)
```

```
plt.show()
```

Evaluating Cluster

- ① Measure quality of clustering.
- ① Informs choice of how many clusters to look for

Clustering the wines

```
model = KMeans(n_clusters = 3)
```

labels = model.~~fit~~ ~~(samples)~~ ~~fit~~-predict(samples)

```
df = pd.DataFrame({'labels': labels,
                   'varieties': varieties})
```

```
ct = pd.crosstab(df['labels'], df['varieties'])
```

Feature variances

- Feature Variances
- ① The wine features have very different variances.
 - ② Variance of a feature measure spread of its values.

- In kmeans: feature variance = feature influence
- Standard Scalar transforms each feature to have mean 0 and variance 1

- In kmeans: feature variance = feature influence
- Standard Scalar transforms each feature to have mean 0 and variance 1 (called the "standardized")

and variance 1
- Features are said to be "standardized"
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()

scalar · fit (samples)

StandardScaler (copy=True, with_mean=True, with_std=True)

`samples_scaled = scaler.transform(samples)`

Similar Methods
- StandardScaler and KMeans have similar methods

- StandardScaler and KMeans have same
- Use fit()/transform() with StandardScaler
- Use fit()/predict() " KMeans

2-2 Visualizing Hierarchies

⊖ t-SNE: creates a 2D map of a dataset → based on proximity. ①

⊖ Hierarchical clustering

A hierarchy of groups

- Eurovision dataset

- ⊙ ~~Countries~~ tree-like diagram = dendrogram
- ⊙ Group countries into larger and larger clusters.

Steps

- ⊙ Every country is in a separate cluster.
- ⊙ At each step two closer clusters are merged.
- ⊙ Continue until all countries in a single cluster.
- ⊙ This is "agglomerative" hierarchical clustering.
- ⊙ There is also "divisive clustering" which works the other way around.

Dendrogram

- ⊙ Read from bottom up
- ⊙ Vertical lines represent clusters.

Hierarchical Clustering with SciPy

⊙ Given samples (the array of scores), and country-names

```
import matplotlib.pyplot as plt
from scipy.cluster.hierarchy import linkage, dendrogram
mergings = linkage(samples, method='complete')
dendrogram(mergings, labels=country_names,
            leaf_rotation=90, leaf_font_size=6)
plt.show()
```

Aligning cluster labels with country-names

```
import pandas as pd
```

```
pairs = pd.DataFrame({'labels': labels, 'countries': country_name})
```

```
print(pairs.sort_values('labels'))
```

t-SNE for 2-dimensional maps

- t-SNE = "t-distributed stochastic neighbor embedding"

- Maps samples to 2D space (or 3D)

t-SNE on Iris dataset

- Iris data set is 4D

- t-SNE maps samples to 2D space

- t-SNE didn't know that there were different species

- ... yet kept the species mostly separate.

Interpreting t-SNE scatter plots

- 'versicolor' and 'virginica' harder to distinguish from one another.

- Consistent with k-means inertia plot: could argue for 2 clusters, or for 3.

t-SNE in sklearn

Samples → 2D Numpy array

species → list

```
import matplotlib as plt
```

```
from sklearn.manifold import TSNE
```

```
model = TSNE(learning_rate=100)
```

```
transformed = model.fit_transform(samples)
```

```
xs = transformed[:, 0]
```

```
ys = transformed[:, 1]
```

```
plt.scatter(xs, ys, c=species)
```

```
plt.show()
```

2-3 Visualizing PCA transformation

1

Dimension Reduction

- More efficient storage and computation
- Remove less-informative "noise" features
- ... which cause problems for prediction tasks e.g: classification, regress.

PCA

- Fundamental dimension reduction technique
- First step "decorrelation"
- Second step reduces dimension

PCA aligns data with axes

- Rotates data samples to be aligned with axes
- Shift data samples so they have mean 0

PCA follows the fit/transform pattern

- like KMeans or StandardScaler.
- `fit()` learns the transformation from given data
- `transform()` applies learned transformation
- `transform()` can be applied to new unseen samples.
- Samples \rightarrow array of two features (total-phenols & od280)

from sklearn.decomposition import PCA

model = PCA()

model.fit(samples)

transformed = model.transform(samples)

transformed

- Rows of transformed corresponds to samples
- Columns of transformed are "PCA features".
- Row gives PCA feature values of corresponding sample.

Versicolor dataset

- "versicolor", one of iris species.
- Only 3 features: sepal-length, sepal width, and petal width
- Samples are points in 3D space.
- Versicolor has intrinsic dimension 2
 - ① samples lie close to flat 2-D sheet
 - ② so can be approximated using 2 features

PCA identifies intrinsic dimensions

- Scatter plots work only if samples have 2 or 3 features.
- PCA identifies intrinsic dimensions when samples have any number of features.
- Intrinsic dimension = number of PCA features with significant variance.
- PCA features are ordered by variance (descending)
- Intrinsic dimension is number of PCA features with significant variance.

Plotting the variance of PCA features

samples = array of versicolor samples
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA

pca = PCA()

pca.fit(samples)

features = range(pca.n_components_)

plt.bar(features, pca.explained_variance_)

plt.xticks(features)

plt.ylabel('variance'); plt.xlabel('PCA feature')

plt.show()

- PCA has reduced the dimension to 2
- Retained the 2 PCA features with highest variance
- Important info. preserved: species remain distinct.
- Discards low variance PCA features.
- Assumes the high variance features are informative
- Assumption typically holds in practice (e.g. of iris)

Word frequency arrays

- rows represent documents, columns represent words
- Entries measure presence of each word in each document.
- ... measure using "tf-idf"

Sparse arrays and csr-matrix

- "Sparse": most entries are zero.
- can use `scipy.sparse.csr-matrix` instead on NumPy array
- `csr-matrix` remembers only the non-zero entries (saves space)

Truncated SVD and csr-matrix

* `scikit-learn` PCA does not support `csr-matrix`

- use `scikit-learn` TruncatedSVD instead
- performs same transformation

from `sklearn.decomposition` import `TruncatedSVD`

`model = TruncatedSVD(n_components=3)`

`model.fit(documents)` # no. of documents is `csr-matrix`

`transformed = model.transform(documents)`

(2-4) Non-Negative Matrix Factorization (NMF)

- like PCA is a dimension reduction technique
- NMF models are interpretable (unlike PCA)
- Easy to interpret means easy to explain
- (*) - However, all sample features must be non-negative (≥ 0)

Interpretable parts

- NMF expresses documents as combinations of topics (or "themes")
- NMF expresses images as combinations of patterns.

Using sklearn NMF

- Follows `fit()` / `transform()` pattern
- Must specify number of components e.g.
NMF(`n_components=2`)
- works with Numpy arrays and with `csc_matrix`

Example word-frequency array

- word frequency array has 4 words, many documents
- Measure presence of words in each document using "tf-idf"
 - ① tf = frequency of word in document
 - ② idf = reduces influence of frequent words.

Example Usage of NMF

```
samples = is the word-frequency array
from sklearn.decomposition import NMF
model = NMF(n_components=2)
model.fit(samples)
nmf_features = model.transform(samples)
model.components_
nmf_features
```

NMF learns

NMF learns interpretable Parts

ex

- Word frequency article (tf-idf)
- 20,000 scientific articles (rows)
- 800 words (columns)

Applying NMF to the articles

articles.shape

from sklearn.decomposition import NMF

nmf = NMF(n_components=10)

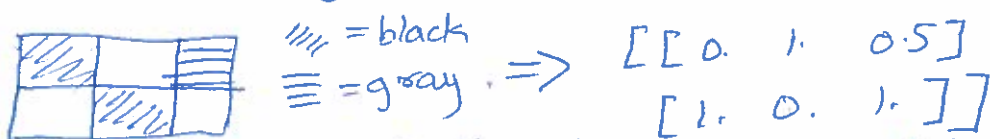
nmf.fit(articles)

nmf.components_.shape

- NMF components are topics
- For documents
 - o NMF components represents topics
 - o NMF features combine topics into documents
- for images, NMF components are parts of images

Grayscale images

- "Grayscale" image = no colors, only shades of grey
- Measure pixel brightness.
- Represent with value b/w 0 & 1 (0 is black)
- Convert to 2D array.



- These 2D-arrays can be flattened by enumerating the entries.

Apply NMF to the word-frequency array

articles is a word frequency array.

from sklearn.decomposition import NMF

nmf = NMF(n_components = 6)

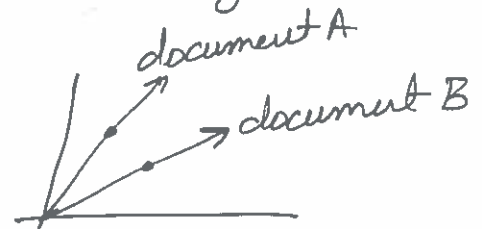
nmf_features = nmf.fit_transform(articles)

Versions of articles

- Different versions of the same document have same topic proportions.
- ... exact feature values may be different
- eg: one version uses many meaningless words.
- But all versions lie on the same line through the origin.

Cosine similarity

- Uses angle b/w lines
- higher values means more similarity



Calculating cosine similarity

from sklearn.preprocessing import normalize

norm_features = normalize(nmf_features)

it has index 23

current_article = norm_features[23:]

similarities = norm_features.dot(current_article)

similarities

DataFrames and labels

- label similarities with article titles, using a DataFrame
- Titles given as list: titles

import pandas as pd

norm_features = normalize(nmf_features)

df = pd.DataFrame(norm_features, index=titles)

current_article = df.loc['Dog bites man']

similarities = df.dot(current_article)

3-1 Linear Classifiers

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①

Applying Logistic Regression and SVM

Sklearn Refresher

Fitting and predicting

```
import sklearn.datasets
newsgroups = sklearn.datasets.fetch_20newsgroups_vectorized()
X, y = newsgroups.data, newsgroups.target
X.shape
y.shape
from sklearn.neighbors import KNearestNe KNeighborsClassifier
knn = KNeighborsClassifier(n_neighbors=1)
knn.fit(X, y)
knn y_pred = knn.predict(X)
```

Model Evaluation

```
knn.score(X, y)
from sklearn.model_selection import train_test_split
X_train, X_test, y_train, y_test = train_test_split(X, y)
knn.fit(X_train, y_train)
knn.score(X_test, y_test)
```

Using Logistic Regression

```
from sklearn.linear_model import LogisticRegression
```

```
lr = LogisticRegression()
```

```
lr.fit(X_train, y_train)
```

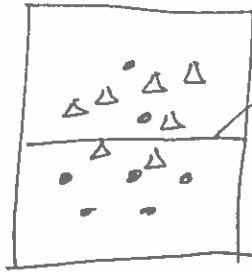
```
lr.predict(X_test)
```

```
lr.score(X_test, y_test)
```

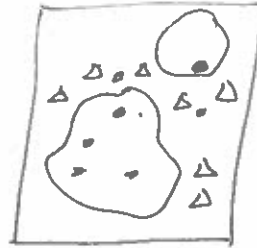
: Model Complexity review:

- underfitting: model is too simple, low training accuracy.
- overfitting: model is too complex, low test accuracy.

Linear decision boundaries



linear boundary



Non-linear boundary.

Definitions

- Classification: learning to predict categories
- decision boundary: the surface separating different predicted classes
- Linear classifier: a classifier that learns linear decision boundaries
e.g.: Logistic Regression, Linear SVM
- Linearly separable: a dataset can be perfectly explained by a linear classifier.

3-2 Linear Classifiers: the coefficients

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Predicting Equations

● Dot Product

```
x = np.arange(3)
```

```
x      # array([0, 1, 2])
```

```
y = np.arange(3, 6)
```

```
y      # array([3, 4, 5])
```

```
x * y    # element wise multiplication.
```

```
array([0, 4, 10])
```

```
np.sum(x * y) == x @ y
```

- $x @ y$ is called the dot product of x and y , and is written $x \cdot y$

Linear Classifier Prediction

● - raw model output = coefficients \cdot features + intercept

- compute raw model output, check the sign

① If +ve, predict one class

② If -ve, " other class

- This is same for logistic regression and linear SVM

③ fit is different but predict is the same

- Difference in fit relates to loss function (In next chapters)

How Logistic Regression makes predictions

raw model output = coefficients \cdot features + intercepts

```
lr = LogisticRegression()
```

```
lr.fit(X, y)
```

```
lr.predict(X)[10]
```

```
lr.predict(X)[20]
```

```
lr.coef_ @ X[10] + lr.intercept_ # raw model output
```

→ `array([-33.78...])` → It is -ve so we ~~call~~ predict -ve class.

minimizing loss

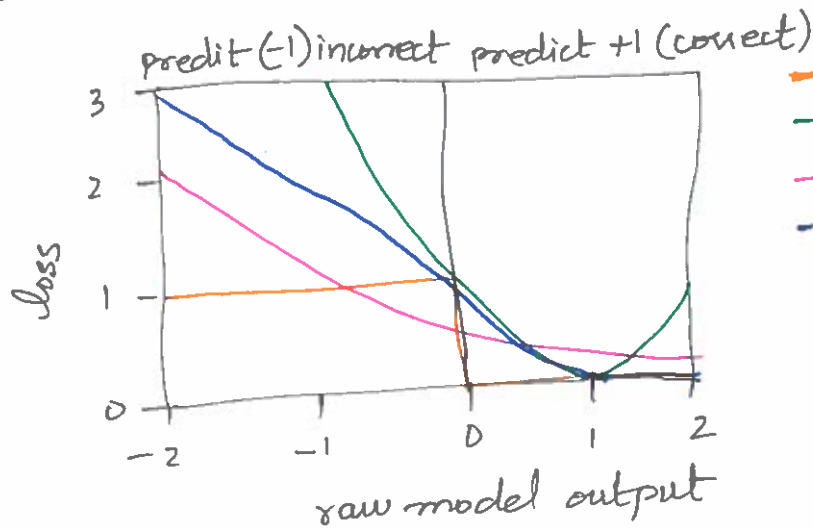
from scipy.optimize import minimize

`minimize(np.square, 0).x`

`minimize(np.square, 2).x`

Loss functions Diagrams

The raw model output



- 0-1 loss function
- least squares
- logistic (smooth version of 0-1)
- hinge loss

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8-3 Logistic Regression and Regularization

(1)

How does regularization affect training accuracy

lr_weak_reg = LogisticRegression(C=100)

lr_strong_reg = LogisticRegression(C=0.01)

lr_weak_reg.fit(X_train, y_train)

lr_strong_reg.fit(X_train, y_train)

lr_weak_reg.score(X_train, y_train)

lr_strong_reg.score(X_train, y_train)

(*) lower C \rightarrow smaller coefficients.

(*) bigger C \rightarrow bigger coefficients.

regularized loss = original loss + large coefficient penalty

⑥ more regularization: lower training accuracy.

How does regularization affect test accuracy

lr_weak_reg.score(X_test, y_test) \rightarrow 0.86

lr_strong_reg.score(X_test, y_test) \rightarrow 0.88

~~regularized loss = xi~~

⑥ more regularization: (almost always) higher test accuracy.

L1 vs L2 regularization:

① Lasso = linear regression with L1 regularization

② Ridge = linear " " L2 "

③ For other models like logistic regression we just say L1, L2 etc

lr_l1 = LogisticRegression(penalty='L1')

lr_l2 = " " () # penalty='L2' by default

lr_l1.fit(X_train, y_train)

lr_l2.fit(X_train, y_train)

plt.plot(lr_l1.coef_.flatten())

\rightarrow can also doing feature selection

plt.plot(lr_l2.coef_.flatten())

\rightarrow shrinks coef to smaller.

Model Coefficients for multiclass

one-vs-rest by default.

```
lr_ovr = LogisticRegression()
```

```
lr_ovr.fit(X, y)
```

```
lr_ovr.coef_.shape
```

```
lr_ovr.intercept_.shape
```

```
lr_mn = LogisticRegression(  
    multi_class = "multinomial",  
    solver = "lbfgs")
```

```
lr_mn.fit(X, y)
```

```
lr_mn.coef_.shape
```

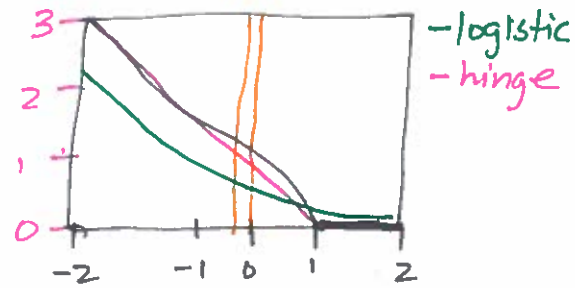
```
lr_mn.coef_.shape  
lr_mn.intercept_.shape
```

What is an SVM?

① Linear ~~SVM~~ classifiers

① Trained using the hinge loss and L2 Regularization

① A key difference b/w hinge + logistic is in "flat" part of hinge loss, which occurs when the raw model output is greater than 1 \rightarrow meaning you predicted an example correctly beyond some margin of error.



① If training example fall in this "zero loss" region, it doesn't contribute to the fit.

① If we remove that example, nothing would change.

① This the key property of SVMs

① Support vectors: a training example not in the flat part of the loss diagram.

① Support vector: an example that is incorrectly classified or close to the boundary.

① How close is considered close enough this is controlled by regularization strength.

① Support vectors are the examples that matter to your fit.

① Logistic regression doesn't has flat part so non-support vectors are also crucial in a way as for LR logReg all examples are crucial.

① Kernel SVM are fast to fit and predict.

① speed is determined by no-of support vectors rather than the whole training dataset.

SGDClassifier (Stochastic Gradient Descent)

• scales well to larger datasets.

from sklearn.linear_model import SGDClassifier

logreg = SGDClassifier(loss='log')

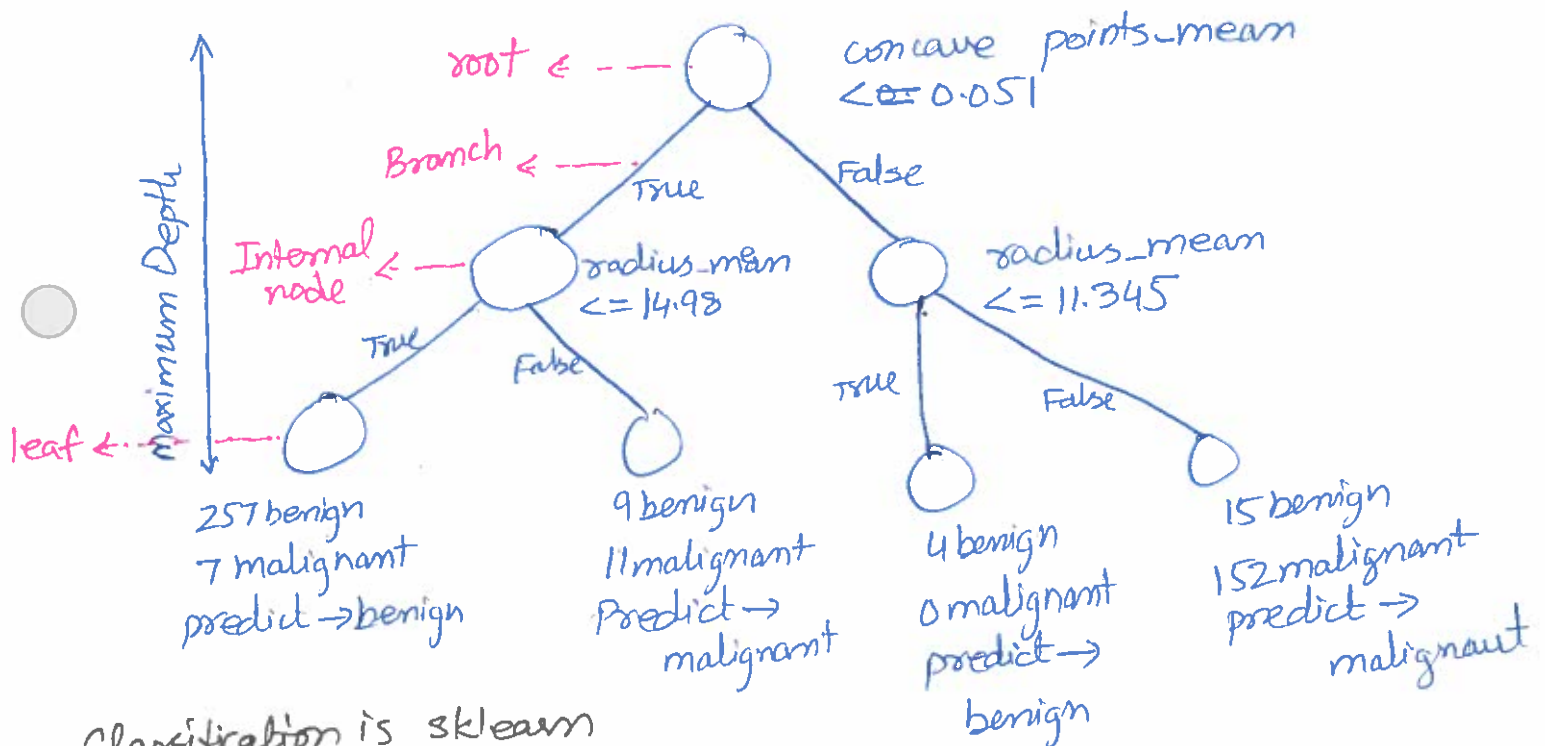
linsvm = SGDClassifier(loss='hinge')

• SGDClassifier hyperparameter alpha is like $1/C$

Classification-tree

Classification and Regression Trees (CART)

- Sequence of if-else questions about individual features
- Objective: infer class labels
- Able to capture non-linear relationships b/w features and labels.
- Don't require features scaling (eg: Standardization, ...)

Breast Cancer Dataset in 2DDecision-tree diagramClassification is sklearn

Import decision tree DecisionTreeClassifier

from sklearn.tree import DecisionTreeClassifier

Import train-test-split

from sklearn.model_selection import train_test_split

Import accuracy score

from sklearn.metrics import accuracy_score

split data into 80% train, 20% test

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,

Instantiate dt

dt = DecisionTreeClassifier(max_depth=2, random_state=1)

Classification - Tree Learning

- Nodes are grown recursively
- At each ~~split~~ node, split the data based on:
 - feature t and split-point s to maximize $IG(\text{node})$.
- If $IG(\text{node}) = 0$, declare the node a leaf...

```
from sklearn.tree import DecisionTreeClassifier
```

```
" " .model_selection import train_test_split
```

```
" " .metrics import accuracy_score
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,
```

```
                                stratify=y,  
                                random_state=0,  
                                random_state=1)  
dt = DecisionTreeClassifier(criterion='gini',  
df.fit(X_train, y_train)
```

```
dt.y_pred = dt.predict(X_test)
```

```
accuracy_score(y_test, y_pred)
```

Decision-Tree for Regression

Auto-mpg Dataset → UCI ML Repo

Regression-Tree in sklearn

```
from sklearn.tree import DecisionTreeClassifier DecisionTreeRegressor
```

```
" " .model_selection import train_test_split
```

```
" " .metrics import mean_squared_error as MSE
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,
```

```
                                random_state=3)  
dt = RegressorDecisionTreeClassifier(max_depth=4, min_samples_leaf=0.1,  
                                random_state=3)
```

```
dt.fit(X_train, y_train)
```

```
y_pred = dt.predict(X_test)
```

```
mse_dt = MSE(y_test, y_pred)
```

```
rmse_dt = mse_dt**(1/2)
```

```
rmse_dt
```


Difficulties

- Overfitting \rightarrow fitting to noise in training set
- Underfitting \rightarrow not fitting enough.

Generalization Error

① does \hat{f} generalize well on unseen data?

② It can be decomposed as follows:

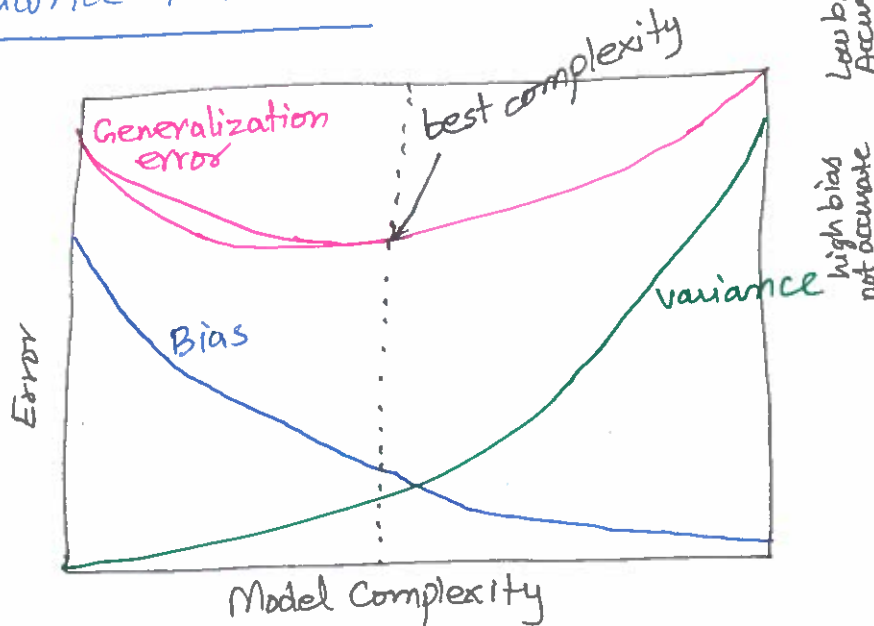
Generalization Error of $\hat{y} = \text{bias}^2 + \text{variance} + \text{irreducible error}$

Bias \rightarrow It tells you on average how much $\hat{f} \neq f$
 \rightarrow high bias models lead to underfitting.

Variance \rightarrow It tells you how much \hat{f} is inconsistent over different training sets.
 \rightarrow high variance models leads to overfitting.

Model Complexity \rightarrow set the flexibility of \hat{f}

\rightarrow example \rightarrow Maximum tree depth, minimum samples-per-le

Bias-Variance Tradeoff

Low Var.
precise
Low bias
Accurate

high Var.
not precise

high bias
not accurate



`print('CV MSE: {:.2f}'.format(MSE_cv.mean()))` → (8)
`" ('Train MSE: {:.2f}'.format(MSE(y_train, y_pred_train)))`
`" ('Test MSE: " " " (MSE(y_test, y_pred_test)))`

Ensemble Learning

Advantages of CART

- Simple to understand
- Simple to interpret
- easy to use.
- Flexibility: ability to describe non-linear dependencies.
- preprocessing: no need to standardize or normalize features.

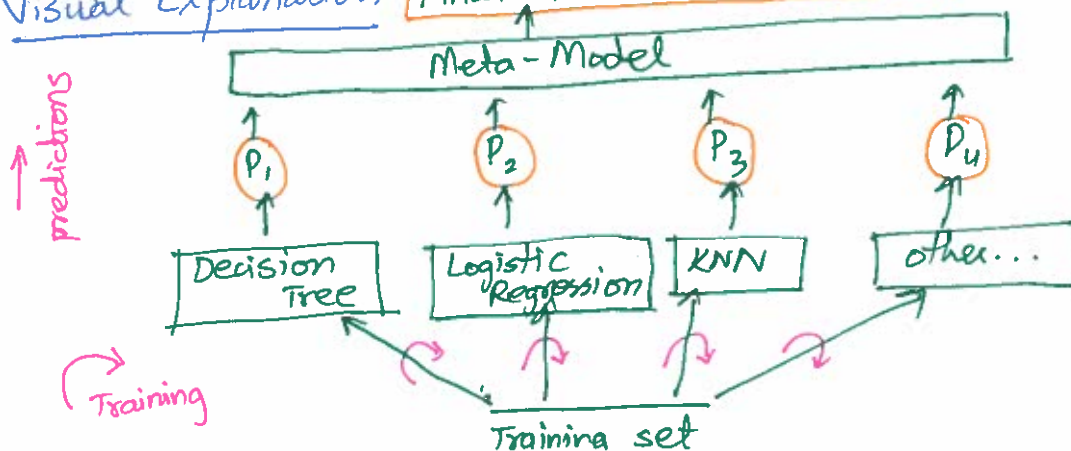
Limitation of CART

- Classification: can only produce orthogonal decision boundaries.
- Sensitive to small variations in the training set.
- High Variance: unconstrained CARTs may overfit the training set.
- Solution: ensemble learning.

Ensemble learning

- Train different models on the same dataset.
- let each model make its predictions.
- Meta-model: aggregates predictions of individual models.
- Final predictions: more robust and less prone to errors.
- Best results: models are skillful in different ways.

Visual Explanation Final Ensemble Predictions



Iterate over the defined list of tuples containing classifiers. ③

for clf_name, clf in classifiers:

fit clf to training set

clf.fit(X_train, y_train)

Predict the labels of test set

y_pred = clf.predict(X_test)

Evaluate accuracy of clf on test set

print('{:s} : {:.3f}'.format(clf_name, accuracy_score(y_test, y_pred)))

Instantiate a VotingClassifier 'vc'

vc = VotingClassifier(estimators = classifiers)

fit 'vc' to training set and predict test set labels

vc.fit(X_train, y_train)

y_pred = vc.predict(X_test)

Evaluate the test accuracy of 'vc'

~~print~~ print('Voting Classifier: {:.3f}'.format(accuracy_score(y_test, y_pred)))

4-3 Bagging

May-8-2022

4.3.1

An ensemble method \rightarrow Bootstrap Aggregating (Bagging)

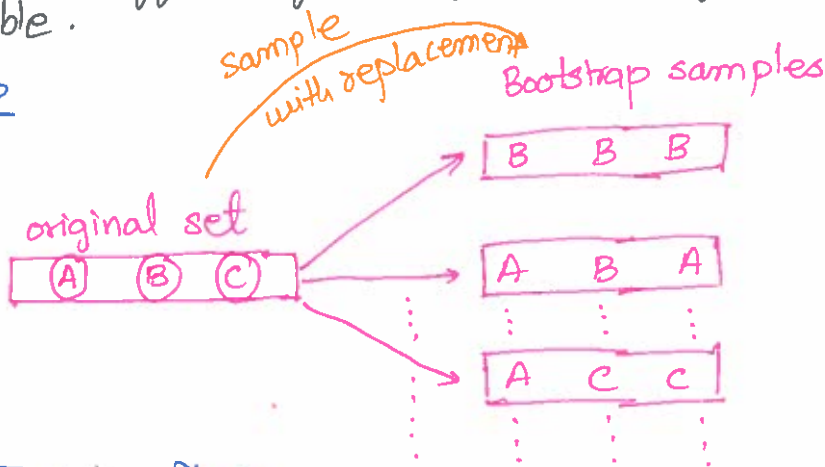
- Voting Classifier

- same training set
 - \neq algorithms.
- } final prediction by majority voting

- Bagging

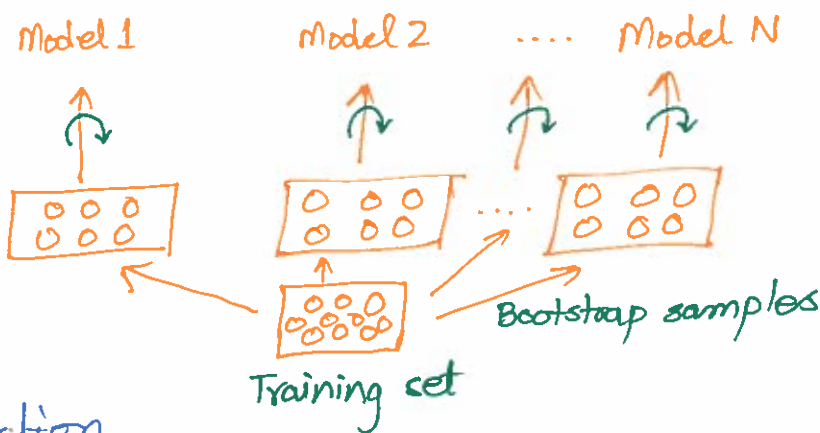
- one algorithm,
 - \neq subsets of the training set
 - uses a technique \equiv Bootstrap
 - It has the effect of reducing variance of individual models in the ensemble.
- } - each model is trained on subset of training data

- Bootstrap

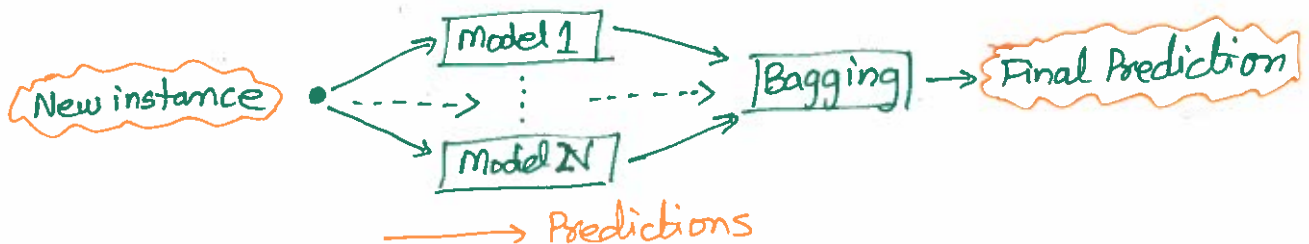


- Bagging: Training Phase

Training



Bagging: Prediction



4.3.2

Out of Bag Evaluation

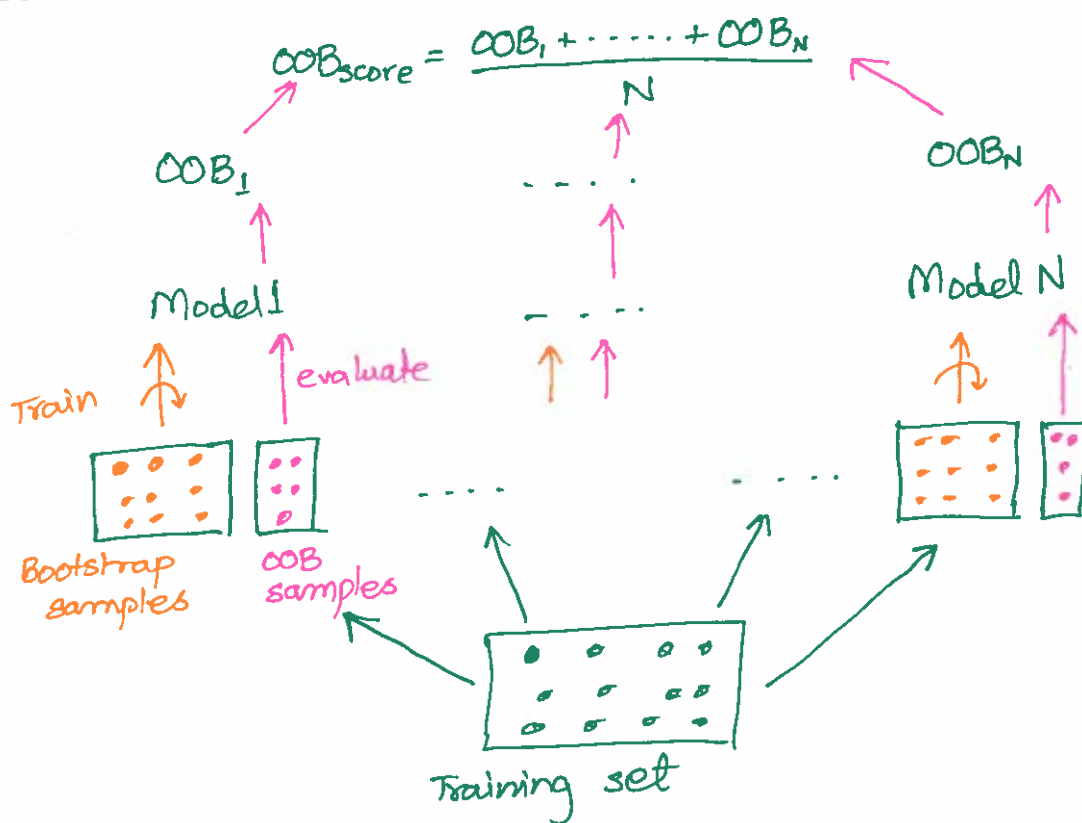
- Bagging

- Some instances may be sampled several times for one model
- other instances may not be sampled at all.

- Out of Bag (OOB) instances

- On average, ~~53%~~ for each model, 63% of ^{training} instances are sampled.
- The remaining 37% constitute the OOB instances.
- Since OOB instances are not seen by the model during training, these can be used to estimate the performance of the ensemble without the need for crossvalidation.
- This technique is called OOB-evaluation.

- OOB-Evaluation



4.3.3 Random Forests (ensemble learning method)

Bagging

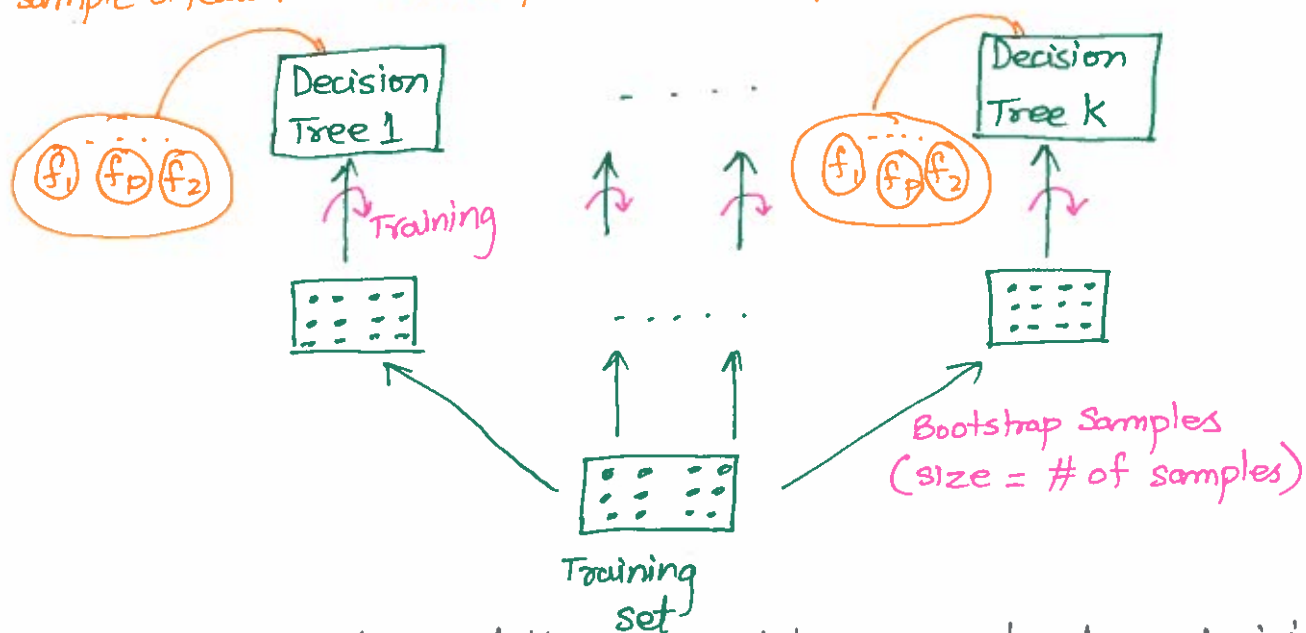
- each estimator can be any model: DecisionTree, Logistic Regression, Neural Net, ...
- Each estimator is trained on a distinct bootstrap samples of training set
- estimators use all available features for training and prediction.

Random Forest

- Base estimator: Decision Tree
- Each estimator is trained on a different bootstrap sample having the same size as training set.
- RF introduces further randomization in the training of individual trees.
- d features are sampled at each node without replacement.
($d < \text{total number of features}$)

Random Forest: Training

sample d features at each split without replacement



- Each tree is trained on different bootstrap sample from training set
- In addition, when a tree is trained, at each node, only d features are sampled from all features without replacement
- The node is then split using the sampled feature that minimizes info gain
- In sklearn default value of d is $\sqrt{\# \text{ of features}}$

Feature Importance

- Tree based methods: enable measuring the importance of each feature in prediction.

- In sklearn:

- ⊙ how much the tree model use a particular feature (weighted avg.) to reduce impurity.
- ⊙ can be accessed using the attribute `feature_importance_`.

Feature Importance in sklearn

- To visualize the importance of features as assessed by rf. we can create a pandas series of feature importances as shown below and then sort this series and make a horizontal barplot.

`import pandas as pd`

`import matplotlib.pyplot as plt`

`importances_rf = pd.Series(rf.feature_importances_, index=X.columns)`

`sorted_importances_rf = importances_rf.sort_values()`

`sorted_ " " .plot(kind="barh", color='lightgreen')`

`plt.show()`

44.1 Ada Boosting

Boosting

- Refers to ensemble method in which many predictors are trained and each predictor learns from the errors of its predecessor.
- Ensemble method combining several weak learners to form a strong learner.
- Weak learner: Model doing slightly better than guessing.
- ~~Eg~~ Eg: Decision stump (CART whose maximum depth is 1)

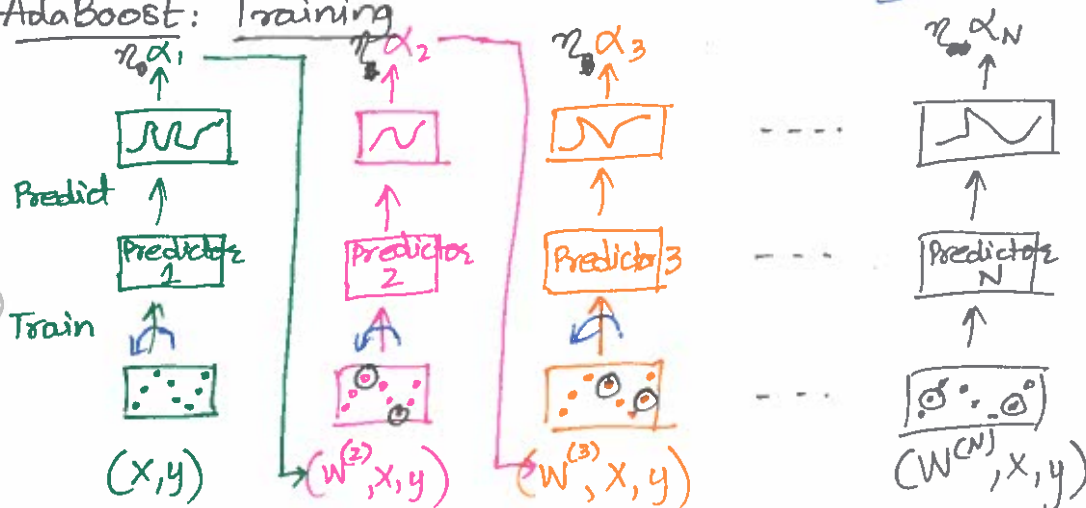
Boosting

- Train an ensemble of predictors sequentially.
- Each predictor tries to correct its predecessor.
- Most popular boosting methods:
 - ① Ada Boost.
 - ② Gradient Boosting.

Ada Boost

- Stands for adaptive boosting
- Each predictor pays more attention to the instances wrongly predicted by its predecessor.
- Achieved by changing the weights of training instances.
- Each predictor is assigned a coefficient α .
- α depends on the predictor's training error.

Ada Boost: Training

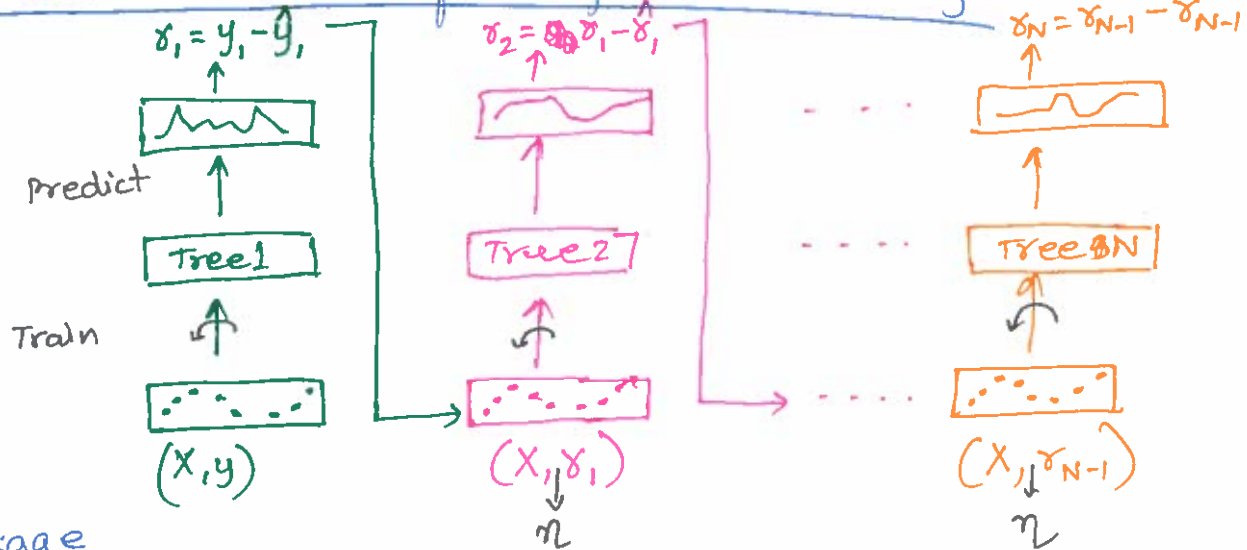


$\eta = \text{learning rate}$
(0-1)

4.4.2 Gradient Boosting (GB)

- Sequential correction of predecessor's errors.
- Does not tweak the weights of training instances like AdaBoost
- Fit each predictor is trained using its predecessor's residual errors as labels.
- Gradient Boosted trees: a CART is used as a base learner.

Gradient Boosted trees for Regression: Training.



Shrinkage

- learning rate (η) (0-1)
- prediction of each tree in the ensemble is shrunk after it is multiplied by learning rate (η)
- Just like AdaBoost there is a trade off b/w η and no. of estimators
- $\downarrow \eta \rightarrow \uparrow$ no. of estimators.

Gradient Boosted Trees: Prediction

Regression:

- $y_{\text{pred}} = y_1 + \eta g_1 + \eta g_2 + \dots + \eta g_N$
- In sklearn: Gradient Boosting Regressor.

Classification

- In sklearn: Gradient Boosting Classifier.

4.4.3 Stochastic Gradient Boosting (SGB)

①⑥

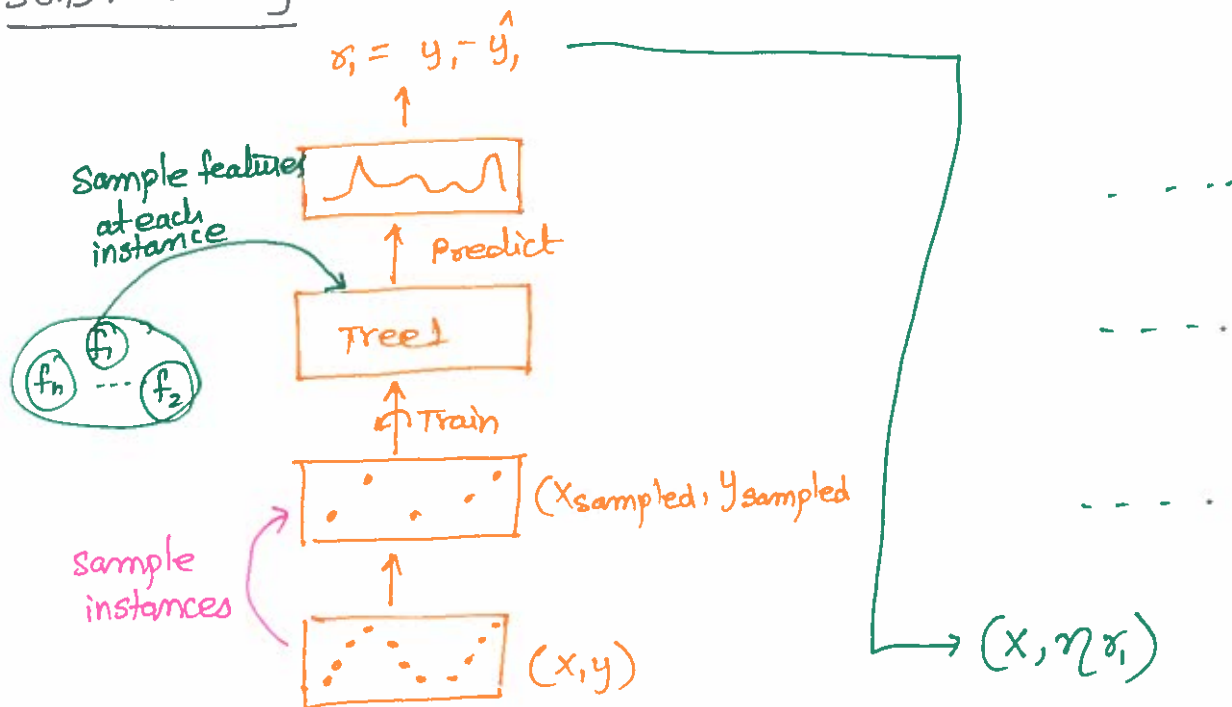
Cons of GB:

- GB involves exhaustive search procedure
- Each CART is trained to find the best split points and features.
- May lead to CARTs using the same split points and maybe the same features.

Stochastic GB:

- Each tree is trained on a random subset of rows of the training data.
- The sampled instances (40%-80% of training set) are sampled without replacement.
- Features are sampled (without replacement) when choosing split points.
- Result: further ensemble diversity.
- Effect: adding further variance to the ensemble of trees.

SGB: Training



4.5.1 Tuning a CART's Hyperparameters

- To obtain better performance hyperparameters of ML model should be tuned.
- ML models are characterized by parameters and hyperparameters.
 - parameters: learn from data
 - CART example: split-point of a node, split-feature of a node, ...
 - hyperparameter: not learned from data, set prior to training.
 - CART example: max-depth, min-samples-leaf, splitting criterion,etc.

Hyperparameter tuning

- * Problem: search for a set of optimal hyperparameters for a learning algorithm.
- * Solution: find a set of optimal hyperparameters that results in an optimal model.
- * Optimal Model: yields and optimal score.
- * Score: in sklearn defaults to accuracy (classification) and R^2 (regression)
- * Cross-Validation: is used to estimate the generalization performance

Why tune Hyperparameters?

- In sklearn - a model's default hyperparameters are not optimal for all problems.
- Hyperparameters should be tuned to obtain the best model performance.

Approaches to hyperparameter tuning

- Grid Search
- Randomized Search
- Bayesian Optimization
- Genetic Algorithms.
- - - - - -

→ (

Extract best hyperparameters from 'grid-dt'

best-~~param~~hyperparams = grid-dt.best-params

print('Best hyperparameters: \n', best-hyperparams)

Extract best CV score from 'grid-dt'

best-CV-score = grid-dt.best-score-

print('Best CV accuracy:'.format(best-CV-score))

Extract best model from grid-dt

best-model = grid-dt.best-estimator -

Evaluate test set accuracy

test-acc = best-model.score(X-test, y-test)

print('Test set accuracy of best model: {:.3f}'.format(test-~~acc~~^{acc}))

4.5.2 Tuning an RF's Hyperparameters

Random Forest hyperparameters

- ~~CART~~ CART hyperparameters
- no. of estimators
- bootstrap
-

Tuning is expensive:

- computationally expensive
- sometimes leads to very slight improvement

(*) For above reasons it is desired to weight the impact of tuning on the pipeline of your data analysis project as a whole in order to understand if it is worth pursuing.

Inspecting RF hyperparameters in sklearn

```
from sklearn.ensemble import RandomForestRegressor
```

```
SEED = 1
```

```
rf = RandomForestRegressor(random_state = SEED)
```

inspect rf's hyperparameters.

```
rf.get_params()
```

Autodataset

```
from sklearn.metrics import mean_squared_error as MSE
```

```
from sklearn.model_selection import GridSearchCV
```

```
params_rf = { 'n_estimators': [300, 400, 500],  
              'max_depth': [4, 6, 8],  
              'min_samples_leaf': [0.1, 0.2],  
              'max_features': ['log2', 'sqrt'] }
```

```
grid_rf = GridSearchCV(estimator = rf, param_grid = param_rf  $\uparrow$  cv=3, scoring="neg_mean_squared_err",  
                      verbose=1, n_jobs=-1)
```

```
grid_rf.fit(X_train, y_train)
```

```
best_hyperparams = grid_rf.best_params_
```

```
print('Best hyperparameters: \n', best_hyperparams)
```



Python For Data Science Scikit-Learn Cheat Sheet

Learn Scikit-Learn online at www.DataCamp.com

Scikit-learn

Scikit-learn is an open source Python library that implements a range of machine learning, preprocessing, cross-validation and visualization algorithms using a unified interface.

A Basic Example

```
from sklearn import neighbors, datasets, preprocessing
from sklearn.model_selection import train_test_split
iris = datasets.load_iris()
X, y = iris.data[:, 2:4], iris.target
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=33)
scaler = preprocessing.StandardScaler() fit(X_train)
X_test = scaler.transform(X_test)
neighbors = neighbors.KNeighborsClassifier(n_neighbors=5)
y_pred = neighbors.predict(X_test)
accuracy_score(y_test, y_pred)
```

Loading The Data

Your data needs to be numeric and stored as NumPy arrays or SciPy sparse matrices. Other types that are convertible to numeric arrays, such as Pandas DataFrames, are also acceptable.

```
import numpy as np
X = np.random.randn(10, 5)
y = np.array(['H', 'M', 'F', 'F', 'M', 'F', 'M', 'F', 'F', 'F'])
X[X < 0] = 0
```

Training And Test Data

```
from sklearn.model_selection import train_test_split
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)
```

Model Fitting

Supervised learning

```
lr = LinearRegression()
lr.fit(X_train, y_train)
y_pred = lr.predict(X_test)
```

Unsupervised Learning

```
from sklearn.cluster import KMeans
kmeans = KMeans(n_clusters=3, random_state=0)
kmeans.fit(X_train)
```

Prediction

Supervised Estimators

```
from sklearn.linear_model import LinearRegression
lr = LinearRegression()
lr.fit(X_train, y_train)
y_pred = lr.predict(X_test)
```

Unsupervised Estimators

```
from sklearn.cluster import KMeans
kmeans = KMeans(n_clusters=3, random_state=0)
kmeans.fit(X_train)
```

Preprocessing The Data

Standardization

```
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
scaler.fit(X_train)
X_train = scaler.transform(X_train)
```

Normalization

```
from sklearn.preprocessing import Normalizer
normalizer = Normalizer()
normalizer.fit(X_train)
X_train = normalizer.transform(X_train)
```

Binarization

```
from sklearn.preprocessing import Binarizer
binarizer = Binarizer(threshold=0.0)
binarizer.fit(X_train)
X_train = binarizer.transform(X_train)
```

Encoding Categorical Features

```
from sklearn.preprocessing import LabelEncoder
encoder = LabelEncoder()
encoder.fit(X_train)
X_train = encoder.transform(X_train)
```

Imputing Missing Values

```
from sklearn.preprocessing import Imputer
imputer = Imputer(missing_values='NaN', strategy='mean', axis=0)
imputer.fit(X_train)
X_train = imputer.transform(X_train)
```

Generating Polynomial Features

```
from sklearn.preprocessing import PolynomialFeatures
poly = PolynomialFeatures(degree=2)
poly.fit(X_train)
```

Create Your Model

Supervised Learning Estimators

```
from sklearn.linear_model import LinearRegression
lr = LinearRegression()
lr.fit(X_train, y_train)

from sklearn.svm import SVC
svm = SVC(kernel='linear')
svm.fit(X_train, y_train)
```

Naive Bayes

```
from sklearn.naive_bayes import GaussianNB
gnb = GaussianNB()
gnb.fit(X_train, y_train)
```

KNN

```
from sklearn.neighbors import KNeighborsClassifier
knn = KNeighborsClassifier(n_neighbors=5)
knn.fit(X_train, y_train)
```

Unsupervised Learning Estimators

Principal Component Analysis (PCA)

```
from sklearn.decomposition import PCA
pca = PCA(n_components=2)
pca.fit(X_train)
```

K-Means

```
from sklearn.cluster import KMeans
kmeans = KMeans(n_clusters=3, random_state=0)
kmeans.fit(X_train)
```

Evaluate Your Model's Performance

Classification Metrics

Accuracy Score

```
from sklearn.metrics import accuracy_score
accuracy_score(y_test, y_pred)
```

Classification Report

```
from sklearn.metrics import classification_report
classification_report(y_test, y_pred)
```

Cross-Validation

```
from sklearn.cross_validation import cross_val_score
cross_val_score(estimator, X_train, y_train, cv=5)
```

Regression Metrics

Mean Absolute Error

```
from sklearn.metrics import mean_absolute_error
mean_absolute_error(y_test, y_pred)
```

Mean Squared Error

```
from sklearn.metrics import mean_squared_error
mean_squared_error(y_test, y_pred)
```

R² Score

```
from sklearn.metrics import r2_score
r2_score(y_test, y_pred)
```

Clustering Metrics

Adjusted Rand Index

```
from sklearn.metrics import adjusted_rand_score
adjusted_rand_score(y_test, y_pred)
```

Homogeneity

```
from sklearn.metrics import homogeneity_score
homogeneity_score(y_test, y_pred)
```

V-measure

```
from sklearn.metrics import v_measure_score
v_measure_score(y_test, y_pred)
```

Cross-Validation

```
from sklearn.cross_validation import cross_val_score
print(cross_val_score(estimator, X_train, y_train, cv=5))
```

Tune Your Model

Grid Search

```
from sklearn.grid_search import GridSearchCV
param_grid = {'C': [0.1, 1, 10, 100, 1000],
              'gamma': [0.001, 0.01, 0.1, 1, 10]}
grid_search = GridSearchCV(estimator=svm, param_grid=param_grid,
                           cv=5, n_jobs=-1)
grid_search.fit(X_train, y_train)
print(grid_search.best_estimator_.C)
```

Randomized Parameter Optimization

```
from sklearn.grid_search import RandomizedSearchCV
param_grid = {'C': [0.1, 1, 10, 100, 1000], 'gamma': [0.001, 0.01, 0.1, 1, 10]}
random_search = RandomizedSearchCV(estimator=svm, param_grid=param_grid,
                                    n_iter=10, cv=5, n_jobs=-1)
random_search.fit(X_train, y_train)
print(random_search.best_estimator_.C)
```