

## Congestion Maps

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## Project

**Congestion Maps** is a [web-based](#) inference engine for visualizing and analyzing congestion and travel times in traffic networks. Its main objective is to inform urban planners, policy makers, fellow researchers, and the public at large about the increase in traffic conditions (congestion and travel times) in the Eastern Massachusetts network.

These maps are part of the project [A Dynamic Optimization Framework for Connected Automated Vehicles in Urban Environment](#) carried out at the [CODES](#) and [NOC](#) Labs and the [Center for Information and Systems Engineering](#) at [Boston University](#).

## Data description

The dataset contains millions of observed vehicle speeds on more than 11,000 road segments in eastern Massachusetts including collector roadways, arterial roadways, and expressways. The data was gathered by the private firm [INRIX](#) and made available to us by the Central Transportation Planning Staff ([CTPS](#)) of the Boston Metropolitan Planning Organization ([MPO](#)). We have obtained both 2012 (50 GB) and 2015 (130 GB) datasets. This collection of data contains average vehicle speeds on a minute-by-minute basis for the entire year. The data was collected in real-time from mobile phones, connected cars, trucks, and other fleet vehicles equipped with GPS sensors (vehicle-probe technology).

We also use the [MassDot](#) 2016 Road Inventory database which contains engineering characteristics (number of lanes) and typical traffic patterns of each road segment. The database covers more than 500,000 road segments in eastern MA.

## Processing

We analyze data for the three-month period between April and June, for both 2012 and 2015. We are interested in calculating three key metrics: average speed time, travel time and congestion. All of these metrics are obtained for each road segment and for each time period (later defined as time instances). We begin by defining the relevant notation to explain how each metric was evaluated.

## Notation

- Let  $i \in \mathcal{I}$  denote an instance in the set of time instances  $\{AM, MD, PM, NT, All\}$ .  
Where  $AM$  points to the time-window (7 am - 9 am),  $MD$  (11 am - 1 pm),  $PM$  (5 pm - 7 pm),  $NT$  (9 pm - 11 pm) and  $All$  (12:00 am - 11:59 pm)
- Let  $t \in T$  denote an observation in an instance  $i$ .
- Let  $a \in \mathcal{A}$  denote a road segment.

## Data

Our data consists of three main variables:

$v_{ait}$  which is the average speed on a road segment  $a$  in time instance  $i$  at time  $t$ .

$l_a$  which is the length of road segment  $a$ .

$m_a$  which is the capacity of the road segment  $a$ .

## Calculations

### Step 1: Calculate average speed by instance

$$v_{ai} = \frac{1}{|T|} \sum_{t=1}^T v_{ait} \quad \forall a \in \mathcal{A}, \forall i \in \mathcal{I} \quad (1)$$

where  $T$  is the set of indices pointing to each speed observation of road segment  $a$  and time period  $i$ .

### Step 2: Calculate travel time

$$c_{ai} = \frac{v_{ai}}{l_a} \quad \forall a \in \mathcal{A}, \forall i \in \mathcal{I} \quad (2)$$

where  $c_{ai}$  is the travel time or cost of utilizing road segment  $a$ .

### Step 3: Calculate density

Using the Greenshield model [2], it follows that density is a linear function of speed. Then:

$$d_{ait} = \left( \frac{v_{ait} - v_a^{min}}{v_a^{max} - v_a^{min}} - 1 \right) * -d^{max} \quad (3)$$

where we fixed  $v_a^{min}$  to be equal to 1 mph and  $v_a^{max}$  is the road segment's free-flow speed estimated as the 85% percentile of the road segment speeds. In order to find this percentile we build a histogram by randomly sampling more than 5,000 observations for each road segment. Finally  $d^{max}$  is the *jam density* value which is estimated as twice the value of the capacity

### Step 4: Calculate congestion

$$C_{ai} = \frac{1}{|T|} \sum_{t=1}^T I\{d_{ait} \geq m_{ai}\} \quad \forall a \in \mathcal{A}, \forall i \in \mathcal{I} \quad (4)$$

These expression is estimating the fraction of time in a specific time period (e.g. AM) when the road segment  $a$  is above its capacity. This corresponds to the common notion of "traffic jam". In this expression  $I$  is the *indicator function* resulting in ones when the condition is satisfied and zeros otherwise.

### Step 5: Group data by Zip Code

To group the statistics by Zip Code, we calculate a weighted-sum for each statistic.

### Avg. Speed

$$v_{zip} = \frac{\sum_{a \in zip} l_a v_{ai}}{\sum_{a \in zip} l_a} \quad \forall i \in \mathcal{I} \quad (5)$$

## Zip Congestion

$$C_{zip} = \frac{\sum_{a \in zip} l_a C_{ai}}{\sum_{a \in zip} l_a} \quad \forall i \in \mathcal{I} \quad (6)$$

## References

- [1] Zhang, J., Pourazarm, S., Cassandras, C. G., Paschalidis, I. C. (2018) *The Price of Anarchy in Transportation Networks: Data-Driven Evaluation and Reduction Strategies*. Proceedings of the IEEE, 106(4). <https://doi.org/10.1109/JPROC.2018.2790405>
- [2] Adolf D. May (1990) *Fundamentals of Traffic Flow*. Prentice - Hall, Inc. Englewood Cliff New Jersey 07632, second edition