

## Homework 12

1] We are assuming that no clause contains both variable as well as its complement.

We create a graph  $G(V, E)$  which has 1-1 correspondence with ~~the~~<sup>an</sup> instance of minsat where there are  $C_i$  clauses set  $X$  variables.

For every node  $v_i \in V$  there's also

1-1 correspondence with  $C_i$ . For any nodes  $v_i$  and  $v_j$  there is an edge ~~if~~  $(v_i, v_j) \in E$  if and only if there

are ~~a~~ corresponding clauses  $C_i$  and  $C_j$  where in the variable  $x \in X$  has its uncomplemented form in

$C_i$  and complemented form in  $C_j$  or vice versa. We then ~~to~~ construct a

truth assignment using a vertex cover  $V'$  where  $|V'|$  is ~~the~~<sup>half</sup> the ~~map~~<sup>map</sup>.

vertex cover of  $G$ . We then construct a truth assignment that causes all  $V_i - V'$  clauses to be False.

2] Variables would be  $v_i$  for vertex  $G$  and  $e_{ij}$  for the edges.  
 $v_i = 1$  if it is on the s-side of the cut 0 otherwise



$e_{ij} = 1$  if it is part of the cut 0 otherwise.

Objective fun<sup>n</sup>:  $\min \sum_{(i,j) \in E} d_{ij} c_{ij}$

Constraints:-  $d_{ij} \geq v_i - v_j \quad \forall (i,j) \in E$   
 $v_i - v_j = 1$   
 $v_i, d_{ij} \in \{0,1\} \quad \forall i \in V, (i,j) \in E$

3] Our variables would be  $S_i$   
 Objective function:  $\max \sum_{i=1}^{16} \alpha_i (D_i - S_i)$

Constraints:-  $S_i \geq 0 \quad 0 < i \leq 16$   
 $D_i - S_i \geq 0 \quad 0 < i \leq 16$   
 $\sum_{i=1}^{16} S_i = 720 \quad 0 < i \leq 16$

4] (a)  $x_i$  the power of the  $i^{\text{th}}$  transmitter would be our variable.  $i = 1, \dots, n$ .

(b)  $\min \sum x_i \quad i = 1, \dots, n$

(c)  $d_{ij} \leq x_i + x_j$

(distance between  $i^{\text{th}}$  &  $j^{\text{th}}$  stations)

$\sum_{i=1}^{n-1} i = \frac{n(n-1)}{2}$  constraints