Examining nonlinear methods to improve prediction of toxicity of carboxylic acids

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The findings of *Improved QSAR Analysis* of the *Toxicity* of *Aliphatic Carboxylic Acids* found improvements in predicting aquatic toxicity of carboxylic acids by using a particular set of molecular and topological parameters. The statistical methods employed were linear, and polynomial in nature which relied upon removing predictors. We attempt to establish a stronger predictive relationship using purely nonlinear methods and all predictors.

The dataset can be found at: Toxicity of Carboxylic Acids Data

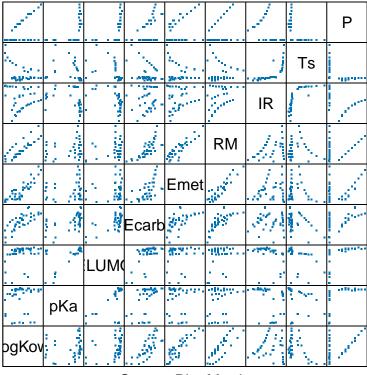
Firstly, we take a peak at the dataset:

head(toxicity)

```
##
     toxicity logKow pKa ELUMO
                                  Ecarb
                                                  RM
                                                         IR
                                                              Ts
                                                                     P
                                          Emet
## 1
        -0.15
                1.68 1.00 4.81 17.8635 1.4838 31.36 1.425 31.3 12.43
## 2
        -0.33
                0.94 0.98
                           4.68 16.9491 0.0000 22.10 1.408 30.4 8.76
        -0.34
                           4.86 17.1806 0.2778 26.73 1.418 30.9 10.59
## 3
                1.16 0.96
                           4.83 18.4794 3.5836 40.63 1.435 31.8 16.10
## 4
         0.03
                2.75 1.00
## 5
        -0.57
                0.79 0.97
                           4.80 16.8022 1.0232 22.14 1.411 32.5 8.77
                2.64 1.01 4.90 18.3937 3.7145 40.63 1.435 31.8 16.10
```

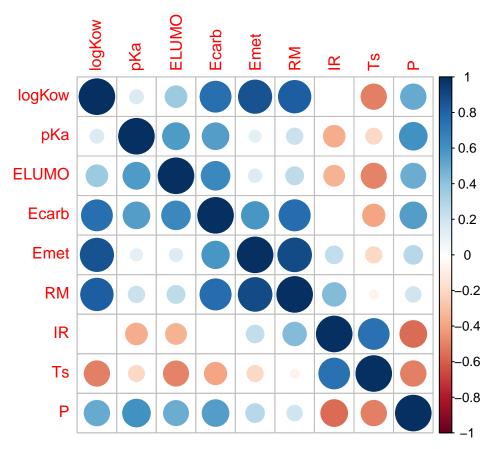
We want to examine the pairwise relationships of features, so we pre-process via centering, scaling, followed by plotting the scatter-plot matrix, and correlation matrix

```
# Centering & Scaling
scaledToxicity <- preProcess(toxicity[, -1], method = c("center", "scale"))
csData <- predict(scaledToxicity, newdata = toxicity[,-1])
# Scatterplot Matrix
splom(~csData, pch = 15, cex = .25, pscales = 0)</pre>
```



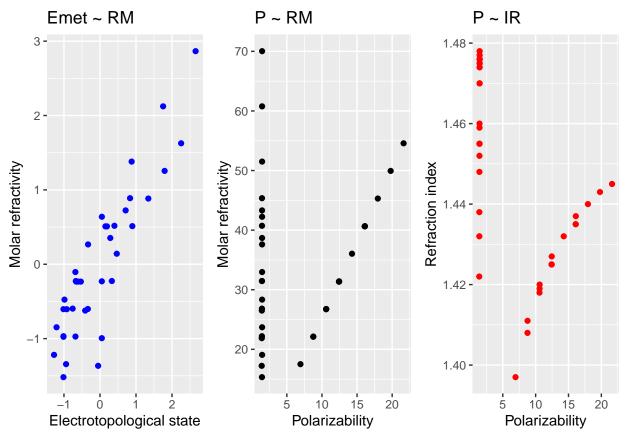
Scatter Plot Matrix

Correlation Matrix
corrplot(cor(csData))



We observe a few select heavily-correlated non-linear features, such as $\mathbf{RM} \sim \mathbf{Emet}$, some with a mix of both linear and uncorrelated points, like $\mathbf{P} \sim \mathbf{RM}$, and some with non-linear and uncorrelated points, like $\mathbf{P} \sim \mathbf{IR}$

```
csData <- as.data.frame(csData)
plt1 <- ggplot(csData, aes(x=Emet, y = RM)) + geom_point(color = "blue") + labs(
    title = "Emet ~ RM",
    x = "Electrotopological state", y = "Molar refractivity",
)
plt2 <- ggplot(toxicity, aes(x=P, y = RM)) + geom_point() + labs(
    title = "P ~ RM",
    x = "Polarizability", y = "Molar refractivity",
)
plt3 <- ggplot(toxicity, aes(x=P, y = IR)) + geom_point(color = "red") + labs(
    title = "P ~ IR",
    x = "Polarizability", y = "Refraction index",
)
ggarrange(plt1, plt2, plt3, ncol = 3)</pre>
```

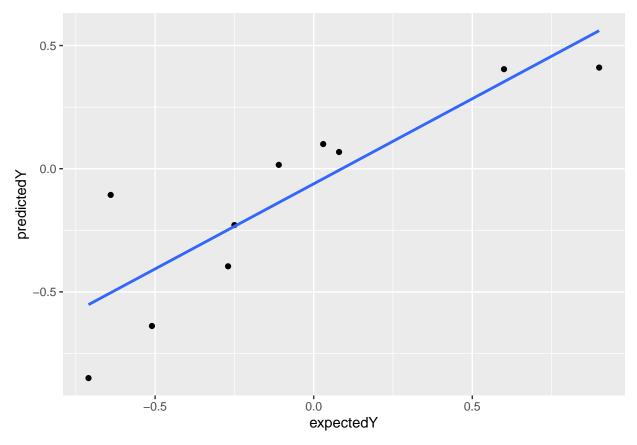


We see that some feature-feature relationships occur only after a certain threshold. For example, as polarizability increases after \sim 6.5, molar refractivity increases with it linearly. A model that captures these sudden pattern changes is MARS.

Multivariate Adaptive Regression Splines (MARS)

```
set.seed(1)
# Make training and test sets
trainingRows <- createDataPartition(toxicity[,1], p = 0.7, list = FALSE)
# Training set
trainSet <- toxicity[trainingRows,]</pre>
# Testing set
testSet <- toxicity[-trainingRows,]</pre>
# 1-3 degree interactions
hyper_grid <- expand.grid(
  degree = 1:3,
  nprune = seq(2, 100, length.out = 10) %>% floor()
# MARS with 5-fold CV
marsModel <- train(</pre>
  toxicity ~ .,
  data = trainSet,
  method = "earth",
  metric = "RMSE",
  preProcess = c("BoxCox", "center", "scale"),
```

`geom_smooth()` using formula = 'y ~ x'



```
# R2 value
caret::R2(predictedValuesMars, testSet[,1])
```

```
## y
## [1,] 0.7462671
```

Unfortunately, MARS didn't perform particularly well with an \mathbb{R}^2 of 0.7463.

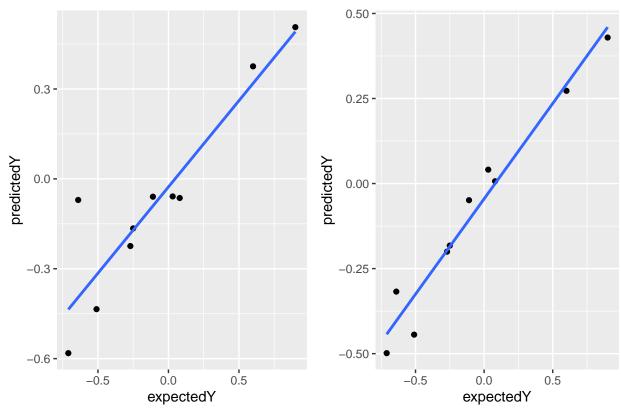
We follow with SVM; in particular, we try a radial basis, and linear kernel.

```
set.seed(1)
# Radial Basis kernel
svmRadialModel <- train(
  toxicity ~ .,
  data = trainSet,</pre>
```

```
method = "svmRadial",
 preProc = c("BoxCox", "center", "scale"),
 tuneLength = 14,
 trControl = trainControl(method = "cv"))
# Linear kernel
svmLinearModel <- train(</pre>
 toxicity ~ .,
 data = trainSet,
 method = "svmLinear",
 preProc = c("BoxCox", "center", "scale"),
 tuneLength = 14,
 trControl = trainControl(method = "cv"))
# Plotting results
predictedValuesRadial <- predict(svmRadialModel, testSet)</pre>
predictedDataRadial <- cbind(testSet[,1], predictedValuesRadial)</pre>
colnames(predictedDataRadial) <- c("expectedY", "predictedY")</pre>
pltSVMRadial <- ggplot(predictedDataRadial, aes(x = expectedY, y = predictedY)) +</pre>
     geom_point() +
     geom_smooth(method = "lm", se = FALSE) +
     labs(title = "SVM with radial basis kernel")
predictedValuesLinear <- predict(svmLinearModel, testSet)</pre>
predictedDataLinear <- cbind(testSet[,1], predictedValuesLinear)</pre>
colnames(predictedDataLinear) <- c("expectedY", "predictedY")</pre>
pltSVMLinear <- ggplot(predictedDataLinear, aes(x = expectedY, y = predictedY)) +</pre>
     geom_point() +
     geom_smooth(method = "lm", se = FALSE) +
     labs(title = "SVM with linear kernel")
ggarrange(pltSVMRadial, pltSVMLinear, ncol = 2)
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
```



SVM with linear kernel



```
# R2 value of SVM Radial
caret::R2(predictedValuesRadial, testSet[,1])
```

```
## [1] 0.8377675
```

```
# R2 value of SVM Linear
caret::R2(predictedValuesLinear, testSet[,1])
```

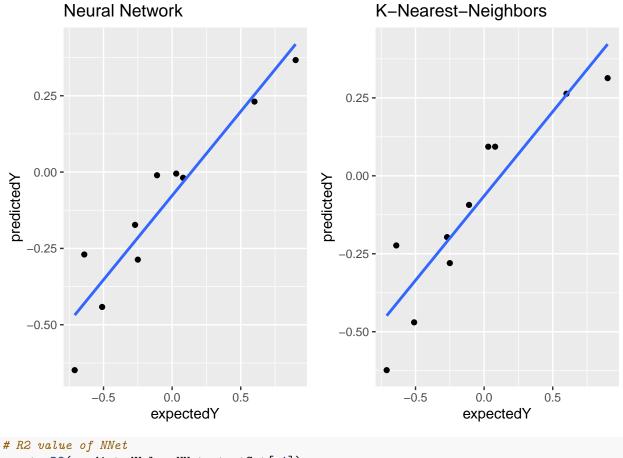
[1] 0.9586954

The radial basis kernel performed mediocre at $R^2 = 0.8377675$, while the linear kernel performed fairly well at $R^2 = 0.9586954$ which beats all but two polynomial models in the original study.

Finally, we attempt a neural network, and K-Nearest-neighbours.

For NN, we can't have our correlated features crippling the model, so we apply PCA for pre-processing.

```
trace = FALSE,
    MaxNWts = 10 * (ncol(toxicity[,-1]) + 1) + 10 + 1,
    maxit = 500)
#K-Nearest-Neighbors
knnModel <- train(toxicity ~ .,</pre>
   data = trainSet,
    method = "knn",
    preProc = c("center", "scale"),
    tuneGrid = data.frame(.k = 1:20),
    trControl = trainControl(method = "cv"))
# Generating predictions - NN
predictedValuesNNet <- predict(nnetModel, testSet)</pre>
predictedDataNNet <- cbind(testSet[,1], predictedValuesNNet)</pre>
colnames(predictedDataNNet) <- c("expectedY", "predictedY")</pre>
pltNNet <- ggplot(predictedDataNNet, aes(x = expectedY, y = predictedY)) +</pre>
     geom_point() +
     geom_smooth(method = "lm", se = FALSE) +
     labs(title = "Neural Network")
# Generating predictions - KNN
predictedValuesKNN <- predict(knnModel, testSet)</pre>
predictedDataKNN <- cbind(testSet[,1], predictedValuesKNN)</pre>
colnames(predictedDataKNN) <- c("expectedY", "predictedY")</pre>
pltKNN <- ggplot(predictedDataKNN, aes(x = expectedY, y = predictedY)) +</pre>
     geom_point() +
     geom_smooth(method = "lm", se = FALSE) +
     labs(title = "K-Nearest-Neighbors")
# Plotting results
ggarrange(pltNNet, pltKNN, ncol = 2)
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
```



```
caret::R2(predictedValuesNNet, testSet[,1])
```

```
## [1] 0.8847985
# R2 value of KNN
caret::R2(predictedValuesKNN, testSet[,1])
```

[1] 0.8399075

We observe that both NNet, and KNN perform fairly medicore with \mathbb{R}^2 values of 0.8848 and 0.8399.

We conclude that the traditional nonlinear methods examined in this analysis do not perform well enough to compete with the simpler, and better-performing linear methods described in the original study.