

Solve problem by simplex method.

$$\text{Max. } Z = 120x + 100y$$

$$\begin{aligned} \text{Subj. to } 2x + 2.5y &\leq 1000 \\ 3x + 1.5y &\leq 1200 \\ 1.5x + 4y &\leq 1200 \\ x, y &\geq 0 \end{aligned}$$

Solⁿ:

Converting canonical form to standard form.

$$\text{Max. } Z = 120x + 100y + 0.s_1 + 0.s_2 + 0.s_3$$

Subj to

$$\begin{aligned} 2x + 2.5y + s_1 &= 1000 \\ 3x + 1.5y + s_2 &= 1200 \\ 1.5x + 4y + s_3 &= 1200 \end{aligned}$$

$$x, y, s_1, s_2, s_3 \geq 0$$

1st selection

e _i	C _j	120 100 0 0 0					b	Θ = b _i /a _{ik}	
		x	y	s ₁	s ₂	s ₃			
0	s ₁	2	2.5	1	0	0	1000	1000/2 = 500	
0	s ₂	3	1.5	0	1	0	1200	1200/3 = 400 ←	K.R (Outgoing)
0	s ₃	1.5	4	0	0	1	1200	1200/1.5 = 800	
E _j = Σ e _i a _{ij}		0	0	0	0	0			
C _j - E _j		120	100	0	0	0			

↑
K_c
(Incoming Variable)

New Pivot element

e _i	C _j	120 100 0 0 0					b	Θ = b _i /a _{ik}	
		x	y	s ₁	s ₂	s ₃			
0	s ₁	0	1.5	1	-0.66	0	200	200/1.5 = 133.33 ←	K.R out
120	x	1	0.5	0	-0.33	0	400	400/0.5 = 800	
0	s ₃	0	3.25	0	-0.495	1	600	600/3.25 = 184.6	
E _j = Σ e _i a _{ij}		120	60	0	39.6	0			
C _j - E _j		0	40	0	-39.6	0			

↑
K_c
Incoming variable.

New Row Element = Element of the Row to be replaced - [(Intersection of old row & key column) × (Corresponding element in new pivot row)]

e_j		120	100	0	0	0		
e_i	crs	x	y	s_1	s_2	s_3	b	θ
100	y	0	1	0.66	-0.44	0	133.33	
120	x	1	0	-0.33	0.55	0	333.33	
0	s_3	0	0	-2.145	0.935	1	166.67	
$E_j = \sum e_i a_{ij}$		120	100	26.4	22	0		
$C_j - E_j$		0	0	-26.4	-22	0		

As $C_j - E_j$ row contains 0 and -ve value solution is the optimal solution

$$y = 133.33 \text{ units}$$

$$x = 333.33 \text{ units}$$

$$\therefore Z = 120x + 100y$$

$$= 120 \times 333.33 + 100 \times 133.33$$

$$Z = 53,332.1$$

$$1 - 1.5 \times 0.1$$

$$6.5 - 1.5 \times 1$$

$$0.5 - 1.5$$

$$= -1$$