

# Integrating Automatic and Manual Reserves in Optimal Power Flow via Chance Constraints

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JULY 10, 2023



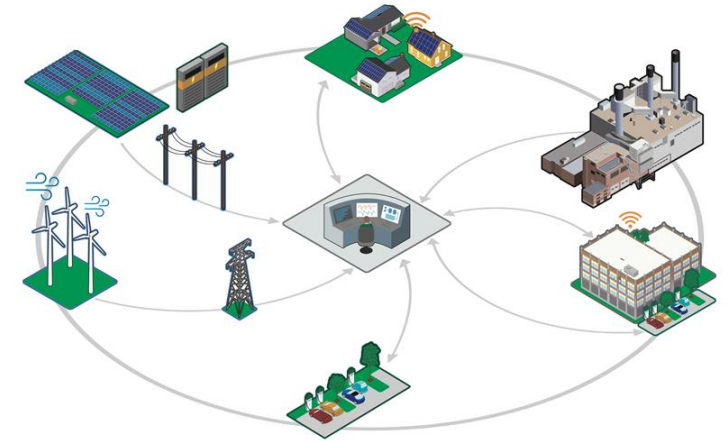
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# OPTIMAL POWER FLOW

- Least-costly dispatch
- Supply electricity net demand
- Technical limits:
  - Production
  - Network equipment

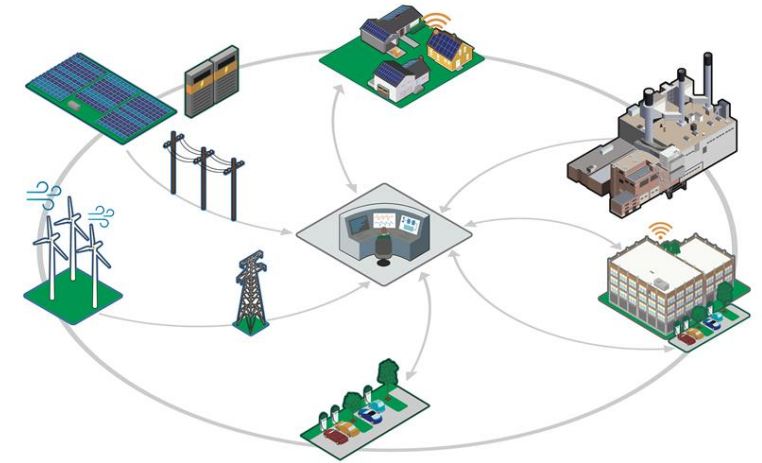
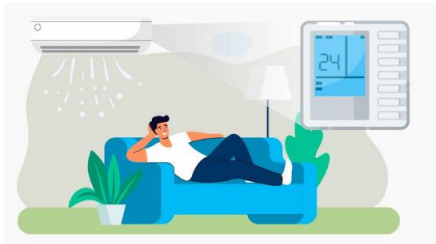


$$\begin{aligned} \min_{p_g} \quad & \sum_{g \in \mathcal{G}} c_g p_g \\ \text{s.t.} \quad & \sum_{g \in \mathcal{G}} p_g = \sum_{n \in \mathcal{N}} d_n \\ & \underline{p}_g \leq p_g \leq \bar{p}_g, \quad \forall g \in \mathcal{G} \\ & -\bar{f}_l \leq \sum_{n \in \mathcal{N}} B_{ln} \left( \sum_{g \in \mathcal{G}} p_g - d_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L} \end{aligned}$$

- Operating cost
- System's balance
- Power output dispatch limits
- Line-flow capacity

# OPTIMAL POWER FLOW under UNCERTAINTY

Uncertainty in   
**electricity demand** and **renewable energy generation**



- Uncertain net demand:  $d_n + \omega_n$
- Reserve deployment:  $p_g + r_g(\omega)$
- To counterbalance error:  $\sum_{g \in \mathcal{G}} r_g(\omega) = \sum_{n \in \mathcal{N}} \omega_n = \Omega$
- To anticipate downward and upward reserve capacity:  $-r_g^d \leq r_g(\omega) \leq r_g^u$

# Two-stage Framework (TS)



$$\min_{p_g, r_g^u, r_g^d, r_g(\omega)} \sum_{g \in \mathcal{G}} c_g p_g + c_g^u r_g^u + c_g^d r_g^d$$

$$\text{s.t.} \quad \sum_{g \in \mathcal{G}} p_g = \sum_{n \in \mathcal{N}} d_n$$

$$\underline{p}_g + r_g^d \leq p_g \leq \bar{p}_g - r_g^u, \quad \forall g \in \mathcal{G}$$

$$r_g^d, r_g^u \geq 0, \quad \forall g \in \mathcal{G}$$

$$\sum_{g \in \mathcal{G}} r_g(\omega) = \sum_{n \in \mathcal{N}} \omega_n = \Omega$$

$$-r_g^d \leq r_g(\omega) \leq r_g^u, \quad \forall g \in \mathcal{G}$$

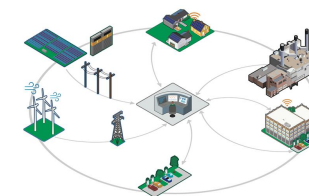
$$-\bar{f}_l \leq \sum_{n \in \mathcal{N}} B_{ln} \left( \sum_{g \in \mathcal{G}} (p_g + r_g(\omega)) - d_n - \omega_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L}$$

■ First-stage constraints

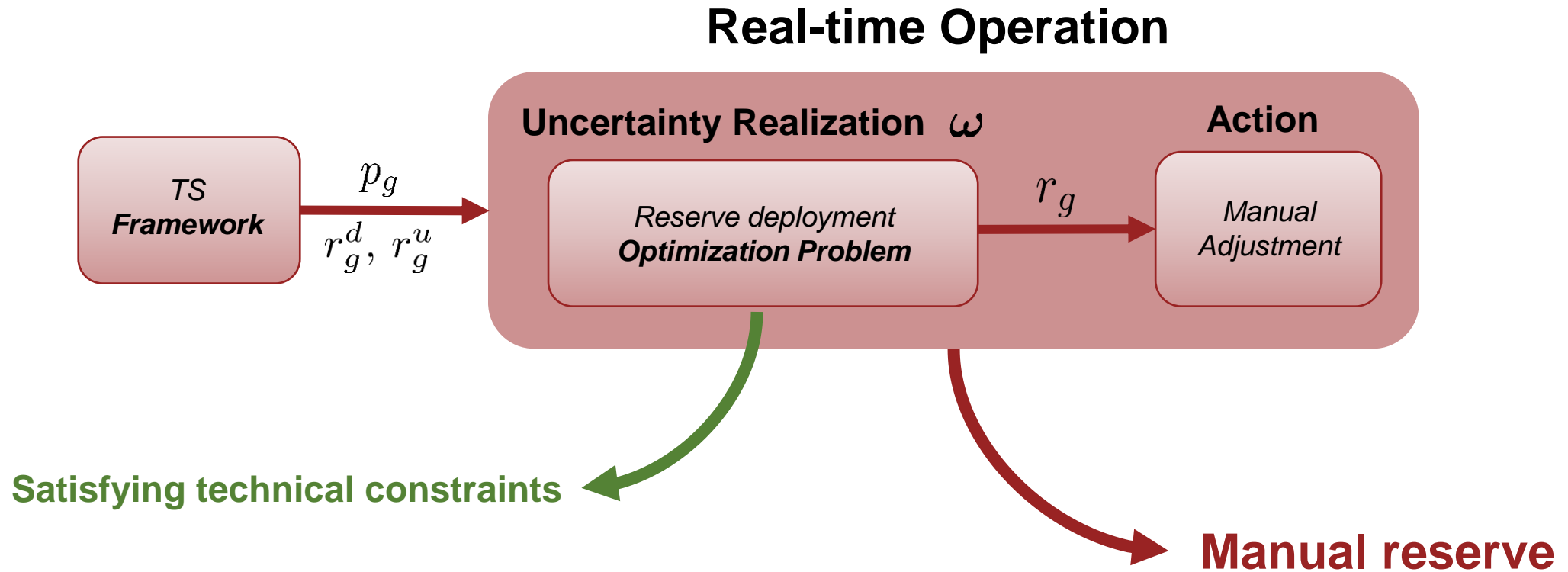
■ Second-stage constraints

$p_g, r_g^u, r_g^d \rightarrow$  first-stage variables

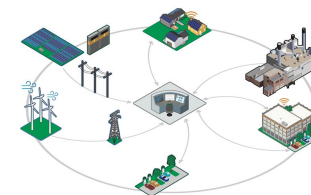
$r_g(\omega) \rightarrow$  second-stage variables



# How does it work?



**Computationally demanding!!!  
Unrealistic**



# Real-time Operation

## Spectrum of Uncertainty Realizations

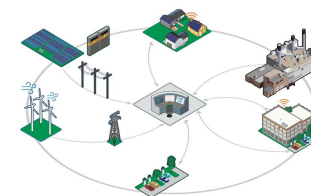
unrealistic

Manual

Automatic



***Automatic Generation Control - AGC***



# Affine Control Policy (AGC)

$$\min_{p_g, \beta_g, r_g^u, r_g^d} \sum_{g \in \mathcal{G}} c_g p_g + c_g^u r_g^u + c_g^d r_g^d$$

$$\text{s.t.} \quad \sum_{g \in \mathcal{G}} p_g = \sum_{n \in \mathcal{N}} d_n$$

$$\underline{p}_g + r_g^d \leq p_g \leq \bar{p}_g - r_g^u, \quad \forall g \in \mathcal{G}$$

$$r_g^d, r_g^u \geq 0, \quad \forall g \in \mathcal{G}$$

$$\sum_{g \in \mathcal{G}} \beta_g = 1$$

$$-r_g^d \leq \beta_g \Omega \leq r_g^u, \quad \forall g \in \mathcal{G}$$

$$-\bar{f}_l \leq \sum_{n \in \mathcal{N}} B_{ln} \left( \sum_{g \in \mathcal{G}} (p_g + \beta_g \Omega) - d_n - \omega_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L}$$

$p_g, \beta_g, r_g^u, r_g^d \rightarrow$  first-stage variables

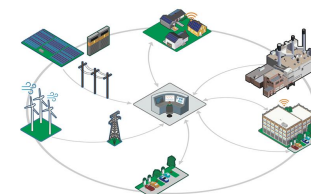


- Reserve deployment follows an affine control policy (AGC):

$$r_g(\omega) = \beta_g \sum_{n \in \mathcal{N}} \omega_n = \beta_g \Omega$$

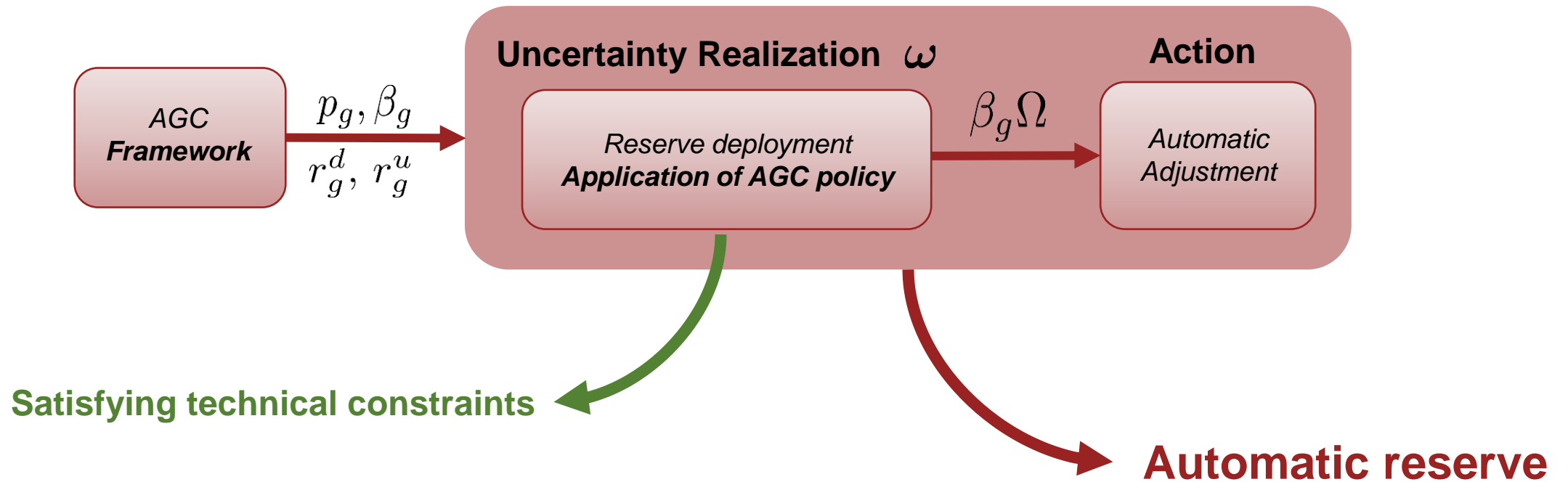
- AGC counterbalances forecast errors:

$$\sum_{g \in \mathcal{G}} \beta_g = 1$$



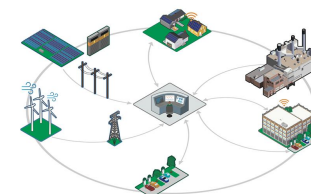
# How does it work?

## Real-time Operation



**Conservative approach!!!**

Linear decision rule replacing second-stage variables





# Real-time Operation

## Spectrum of Uncertainty Realizations

**unrealistic**

**Manual**

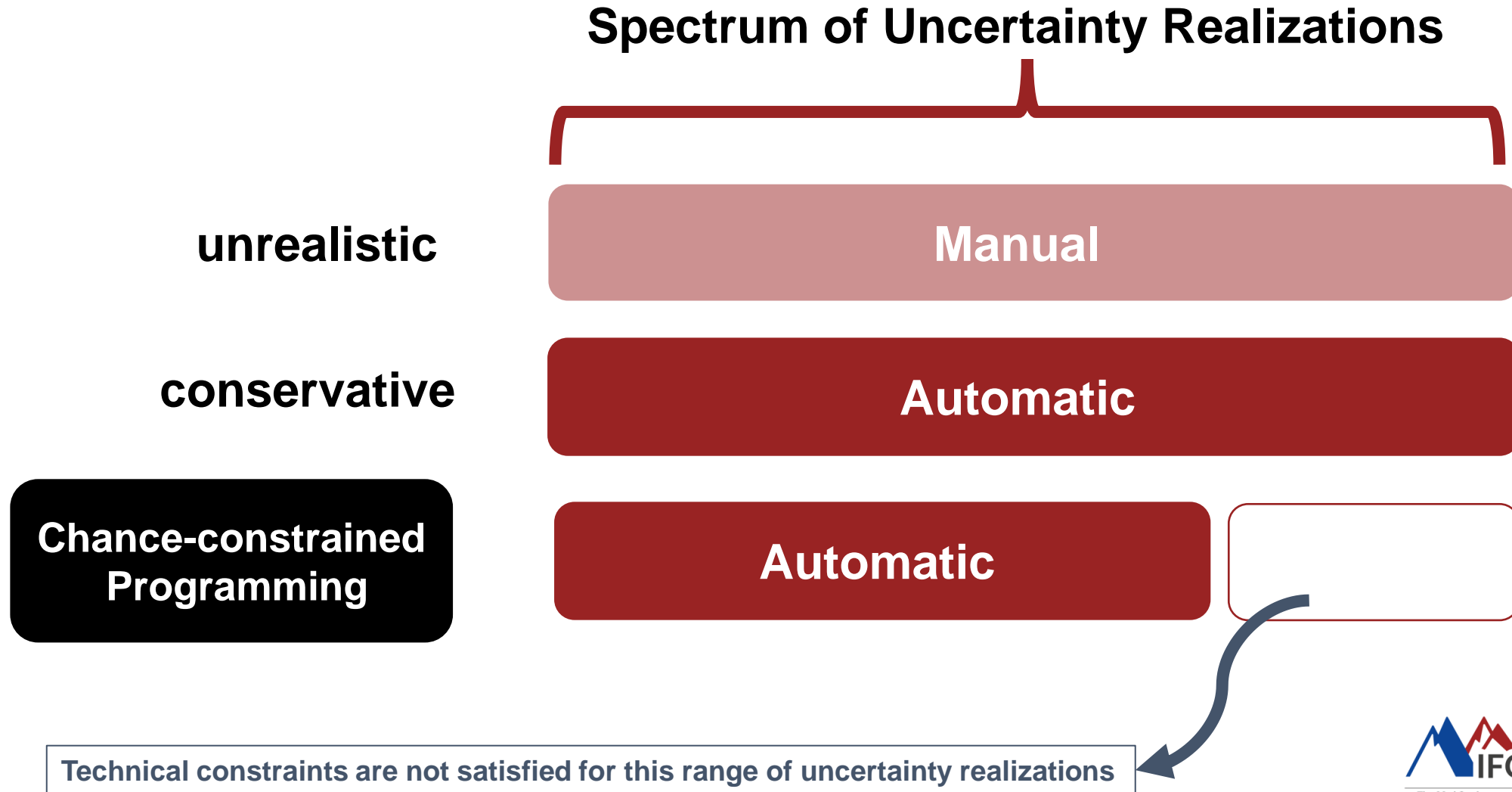
**conservative**

**Automatic**

**Why does SO have to meet technical constraints  
in low-probability and high-impact events?**



# Real-time Operation



# Chance-constrained Program (AGC+CC)



$$\min_{p_g, r_g^u, r_g^d, r_g(\omega)} \sum_{g \in \mathcal{G}} c_g p_g + c_g^u r_g^u + c_g^d r_g^d$$

$$\text{s.t.} \quad \sum_{g \in \mathcal{G}} p_g = \sum_{n \in \mathcal{N}} d_n$$

$$\underline{p}_g + r_g^d \leq p_g \leq \bar{p}_g - r_g^u, \quad \forall g \in \mathcal{G}$$

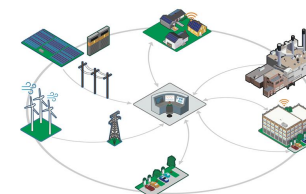
$$r_g^d, r_g^u \geq 0, \quad \forall g \in \mathcal{G}$$

$$\sum_{g \in \mathcal{G}} \beta_g = 1$$

$$\mathbb{P} \left( \begin{array}{l} -r_g^d \leq \beta_g \Omega \leq r_g^u, \quad \forall g \in \mathcal{G} \\ -\bar{f}_l \leq \sum_n B_{ln} \left( \sum_{g \in \mathcal{G}} (p_g + \beta_g \Omega) - d_n - \omega_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L} \end{array} \right) \geq 1 - \epsilon$$

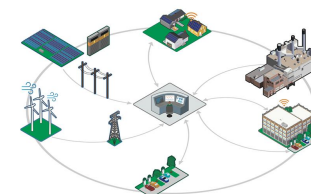
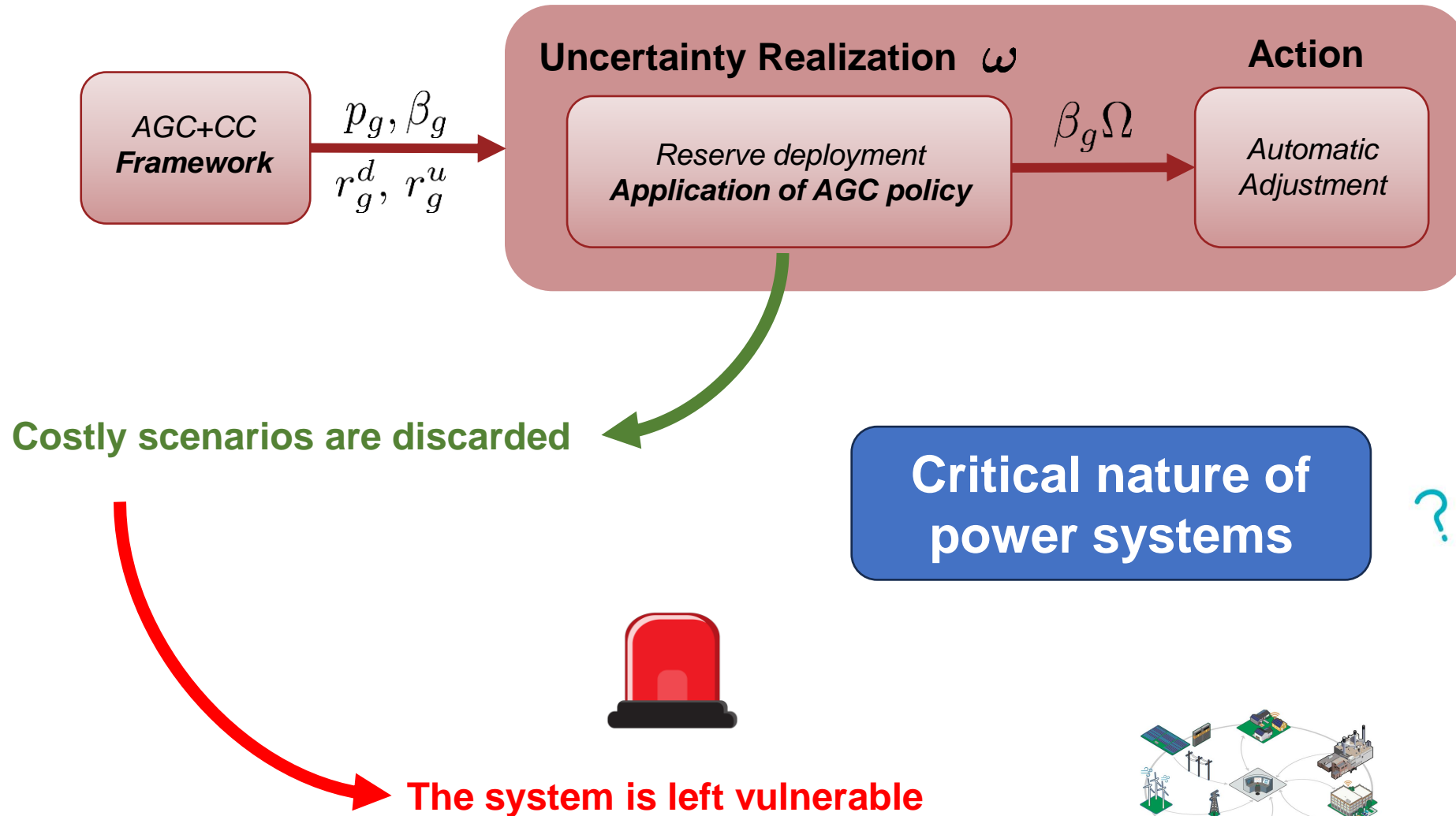
$p_g, \beta_g, r_g^u, r_g^d \rightarrow$  first-stage variables

- Technical constraints are satisfied with a given (high) probability.
- Solutions more economical, since extreme events are discarded.



# How does it work?

## Real-time Operation



# Real-time Operation

## Spectrum of Uncertainty Realizations

unrealistic

Manual

conservative

Automatic

vulnerability

Automatic

Manual

*in-between  
solution*

Integration of automatic and manual



# Integrating Automatic and Manual (AGC+M)

- Reserve deployments are combinations of AGC and manual adjustments:

$$r_g(\omega) = \beta_g \Omega + r_g^M(\omega) \quad \sum_{g \in \mathcal{G}} r_g^M(\omega) = 0$$

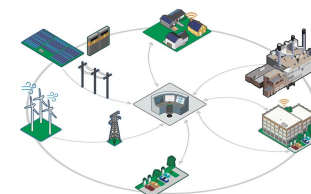
- Guaranteeing robust feasibility.

$$-r_g^d \leq \beta_g \Omega + r_g^M(\omega) \leq r_g^u, \quad \forall g \in \mathcal{G}$$

$$-\bar{f}_l \leq \sum_{n \in \mathcal{N}} B_{ln} \left( \sum_{g \in \mathcal{G}} (p_g + \beta_g \Omega + r_g^M(\omega)) - d_n - \omega_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L}$$

- Most of the time the operation is automatic except in extreme, unlikely events. Manual reserve is computationally expensive. Thus, its probability of occurrence is limited.

$$\mathbb{P}(r_g^M(\omega) = 0, \quad \forall g \in \mathcal{G}) \geq 1 - \epsilon$$



# Integrating Automatic and Manual (AGC+M)

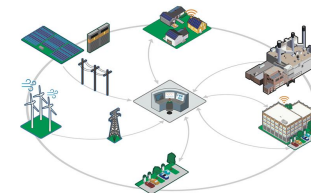


$$\begin{aligned}
 \min_{p_g, r_g^u, r_g^d, r_g(\omega)} \quad & \sum_{g \in \mathcal{G}} c_g p_g + c_g^u r_g^u + c_g^d r_g^d \\
 \text{s.t.} \quad & \sum_{g \in \mathcal{G}} p_g = \sum_{n \in \mathcal{N}} d_n \\
 & \underline{p}_g + r_g^d \leq p_g \leq \bar{p}_g - r_g^u, \quad \forall g \in \mathcal{G} \\
 & r_g^d, r_g^u \geq 0, \quad \forall g \in \mathcal{G}
 \end{aligned}$$

$$\begin{aligned}
 \sum_{g \in \mathcal{G}} \beta_g &= 1, \quad \sum_{g \in \mathcal{G}} r_g^M(\omega) = 0 \\
 -r_g^d &\leq \beta_g \Omega + r_g(\omega) \leq r_g^u, \quad \forall g \in \mathcal{G} \\
 -\bar{f}_l &\leq \sum_{n \in \mathcal{N}} B_{ln} \left( \sum_{g \in \mathcal{G}} (p_g + \beta_g \Omega + r_g(\omega)) - d_n - \omega_n \right) \leq \bar{f}_l, \quad \forall l \in \mathcal{L} \\
 \mathbb{P}(r_g^M(\omega) = 0, \quad \forall g \in \mathcal{G}) &\geq 1 - \epsilon
 \end{aligned}$$

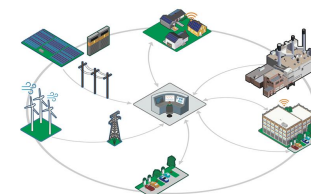
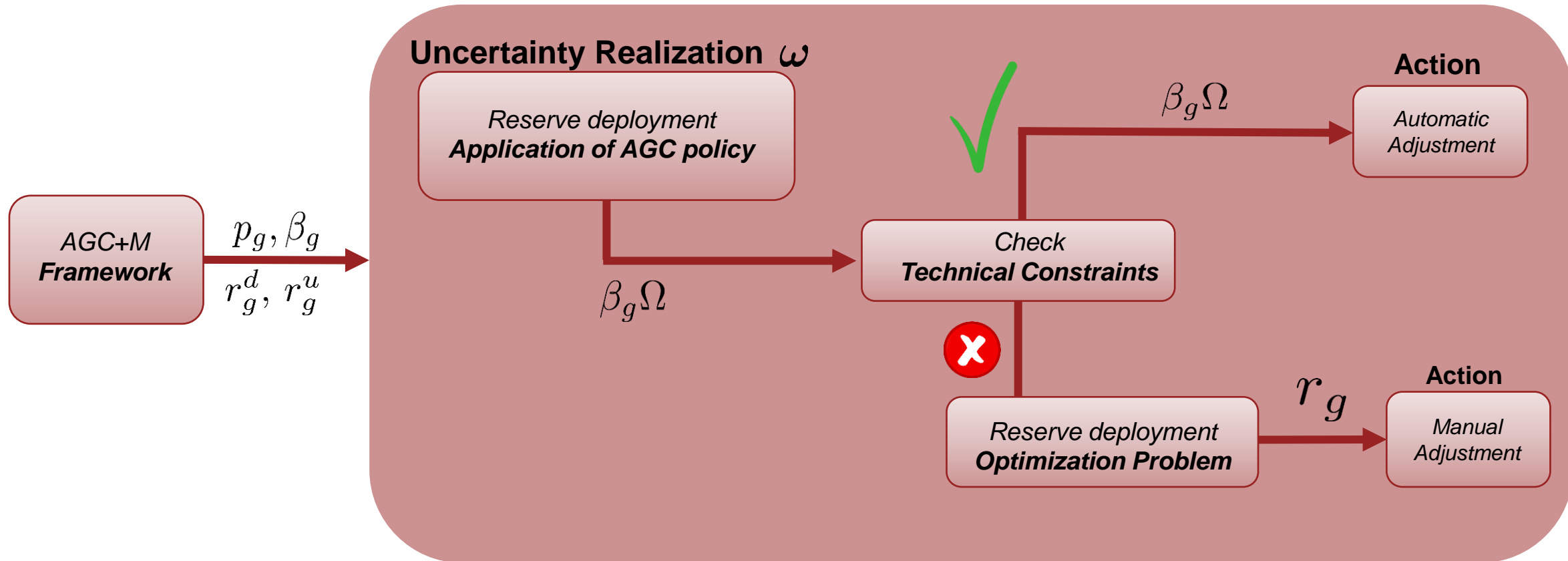
$p_g, \beta_g, r_g^u, r_g^d \rightarrow$  first-stage variables

$r_g^M(\omega) \rightarrow$  second-stage variables



# How does it work?

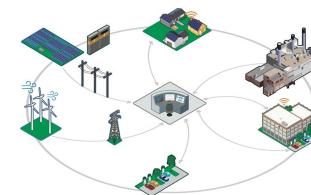
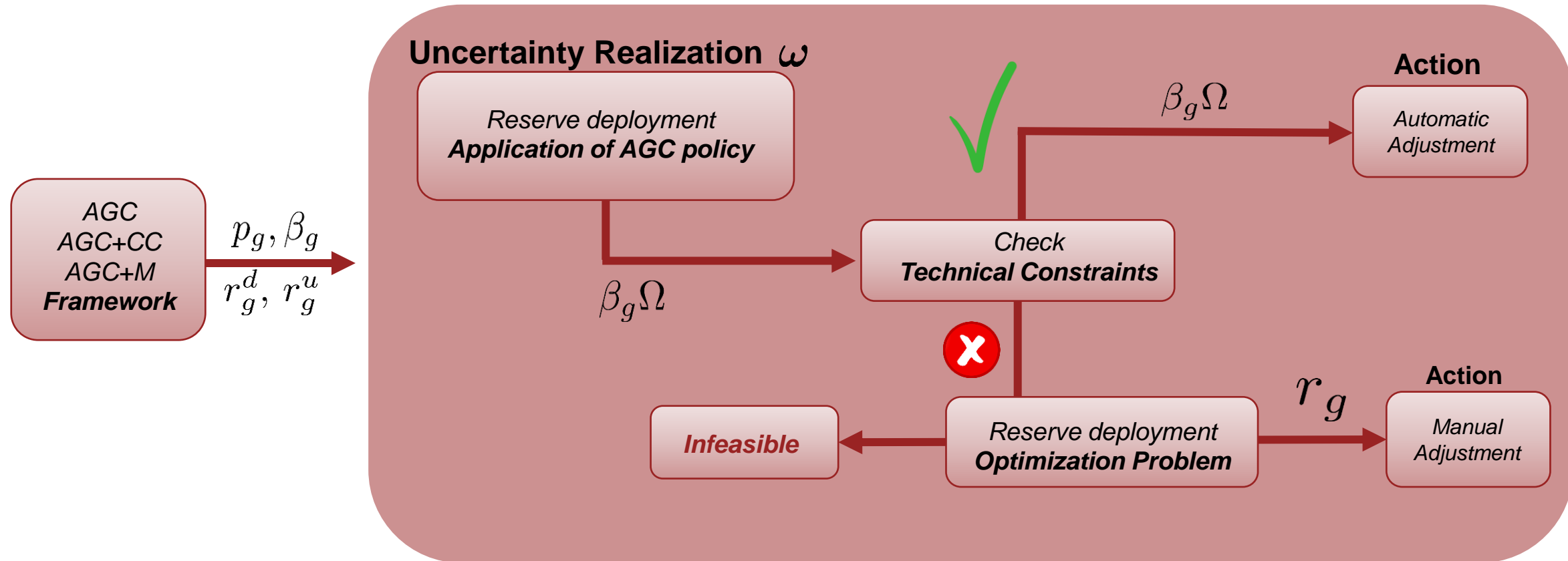
## Real-time Operation





# Evaluation Procedure

## Real-time Operation

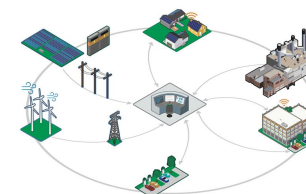
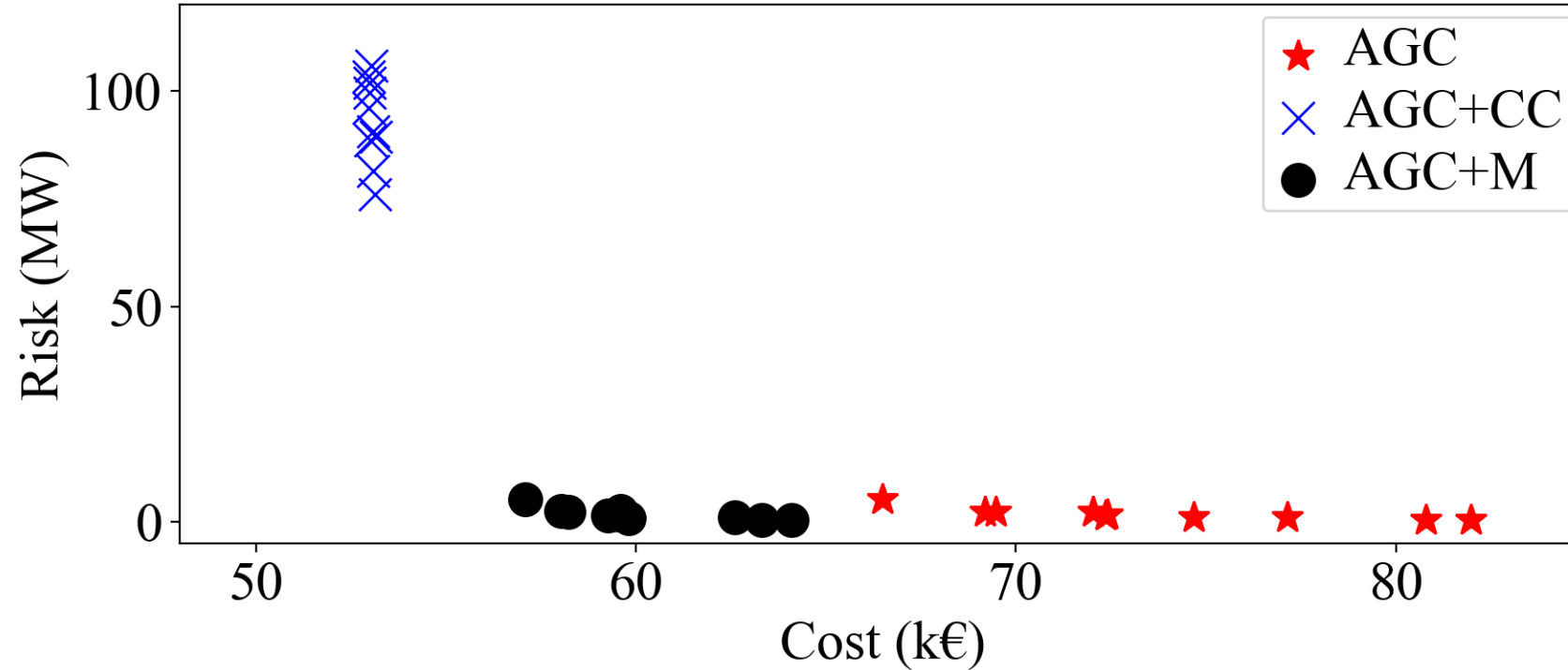


# Numerical Experiments

- IEEE-118 bus system.
- Real-time operation over 100.000 scenarios.  $\epsilon = 5\%$
- Different metrics are evaluated.:
  - The number of scenarios where AGC is sufficient to handle the forecast errors satisfying technical constraints.  $|\mathcal{S}_A|$
  - The number of scenarios where manual adjustments are required to meet technical constraints.  $|\mathcal{S}_M|$
  - The number of scenarios where AGC and manual reserve are not enough to offset the power imbalances whilst satisfying technical constraints.  $|\mathcal{S}_I|$
- Expected operating cost  $\mathbb{E}[C]$  (k€)

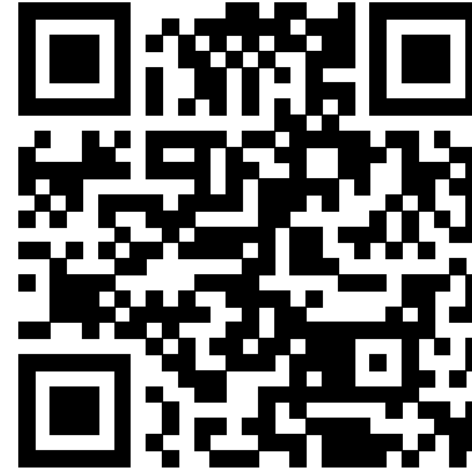
	$ \mathcal{S}_A $	$ \mathcal{S}_M $	$ \mathcal{S}_I $	$\mathbb{E}[C]$ (k€)
<b>AGC</b>	99.56%	0.16%	0.28%	73.65
<b>AGC+CC</b>	94.12%	0.17%	5.71%	53.04
<b>AGC+M</b>	94.30%	5.41%	0.29%	60.15

# Numerical Experiments



# Thanks! Any question?

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