

# Insuring Unit Failures in Electricity Markets

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2009



# OUTLINE

- **Introduction**
- **Model**
- **Case study**
- **Conclusions**

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- **Introduction**
- **Model**
- **Case study**
- **Conclusions**



# INTRODUCTION



**Pool market**  
(price volatility)



**Futures market**  
(fixed price)

# INTRODUCTION

Risk neutral	Pool	
	Fut.	
Risk averse	Pool	
	Futures	

# INTRODUCTION



**Pool market**  
(price volatility)



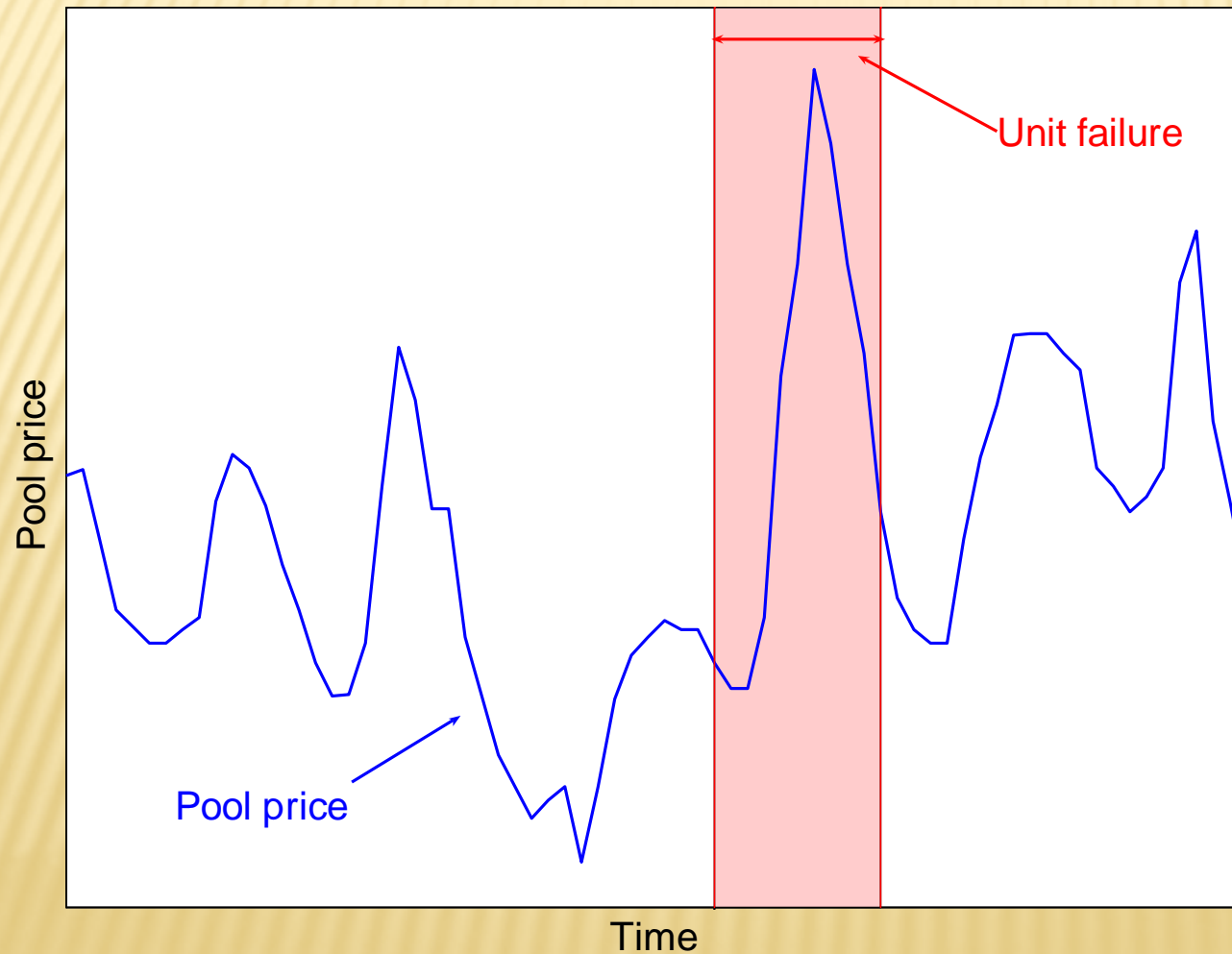
**Futures market**  
(fixed price)



**Production unit**



# INTRODUCTION



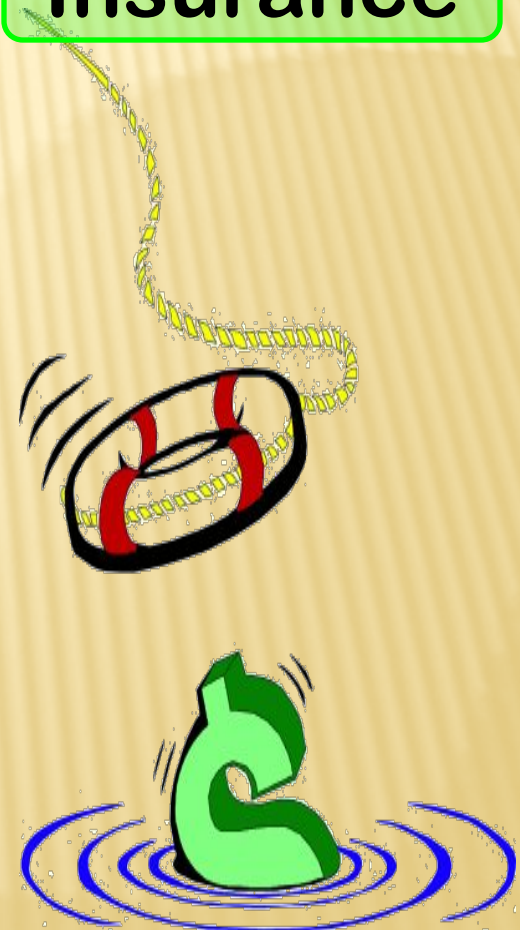
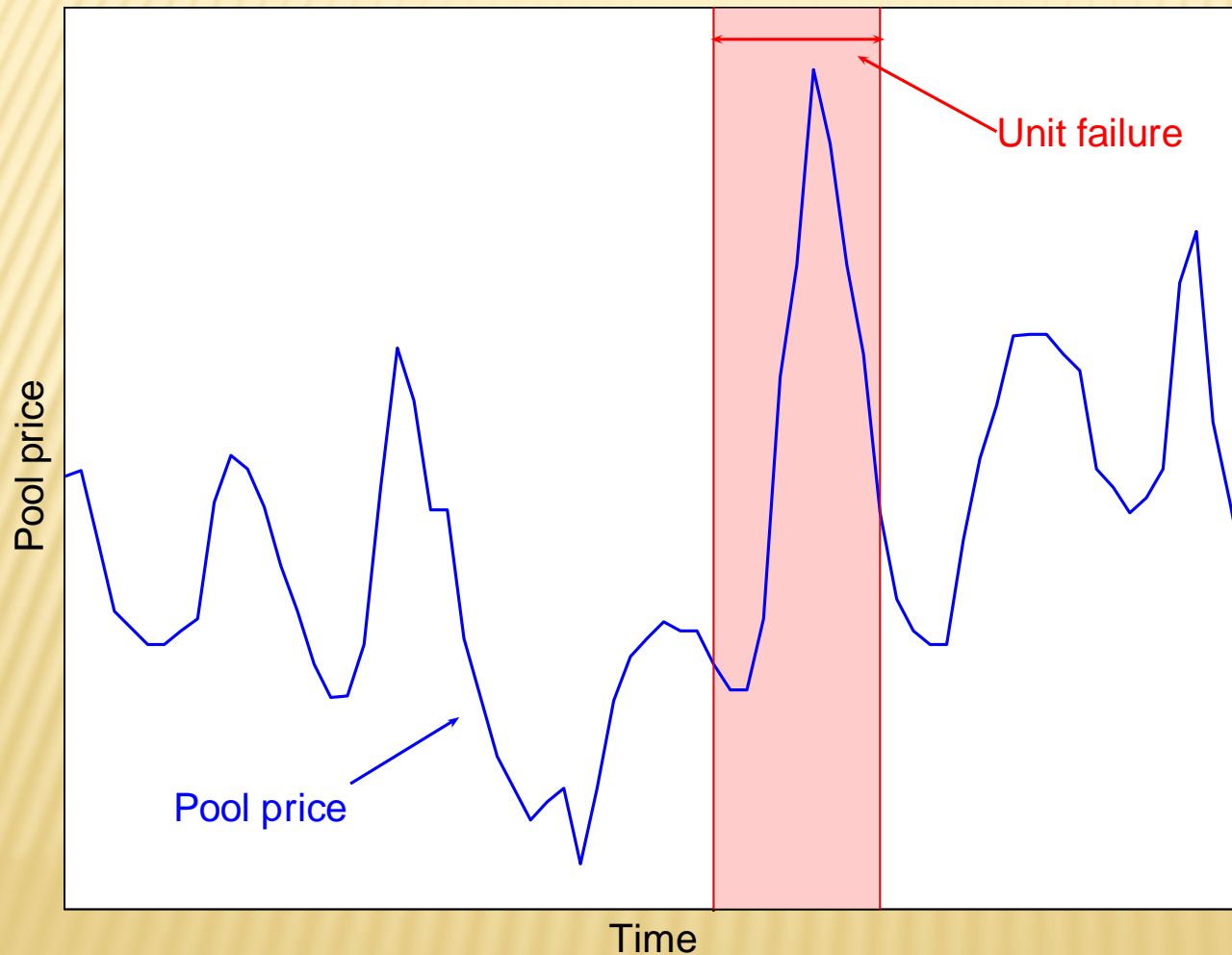


# INTRODUCTION

	Failures neglected		Failures considered	
Risk neutral	Pool		Pool	
	Fut.			
Risk averse	Pool		Pool	
	Futures		Futures	



## Insurance



## Swiss Re New Markets and Mirant Offer Generator Forced Outage Insurance Product.

Swiss Re's Electricity Price and Outage Protection (ELPRO) is a dual-trigger solution which protects against volume and market price by financially firming up generation whenever:

- Generating units suffer unplanned outages, and
- Electricity price exceeds a pre-agreed strike price.

# INTRODUCTION

**Sources of uncertainty**

**Pool prices**

**Unit availability**

**Forward  
contracts**

**Insurance  
policy**

# INTRODUCTION

Sources of uncertainty

Pool prices

Unit availability

Forward  
contracts

Insurance  
policy



Pool  
market

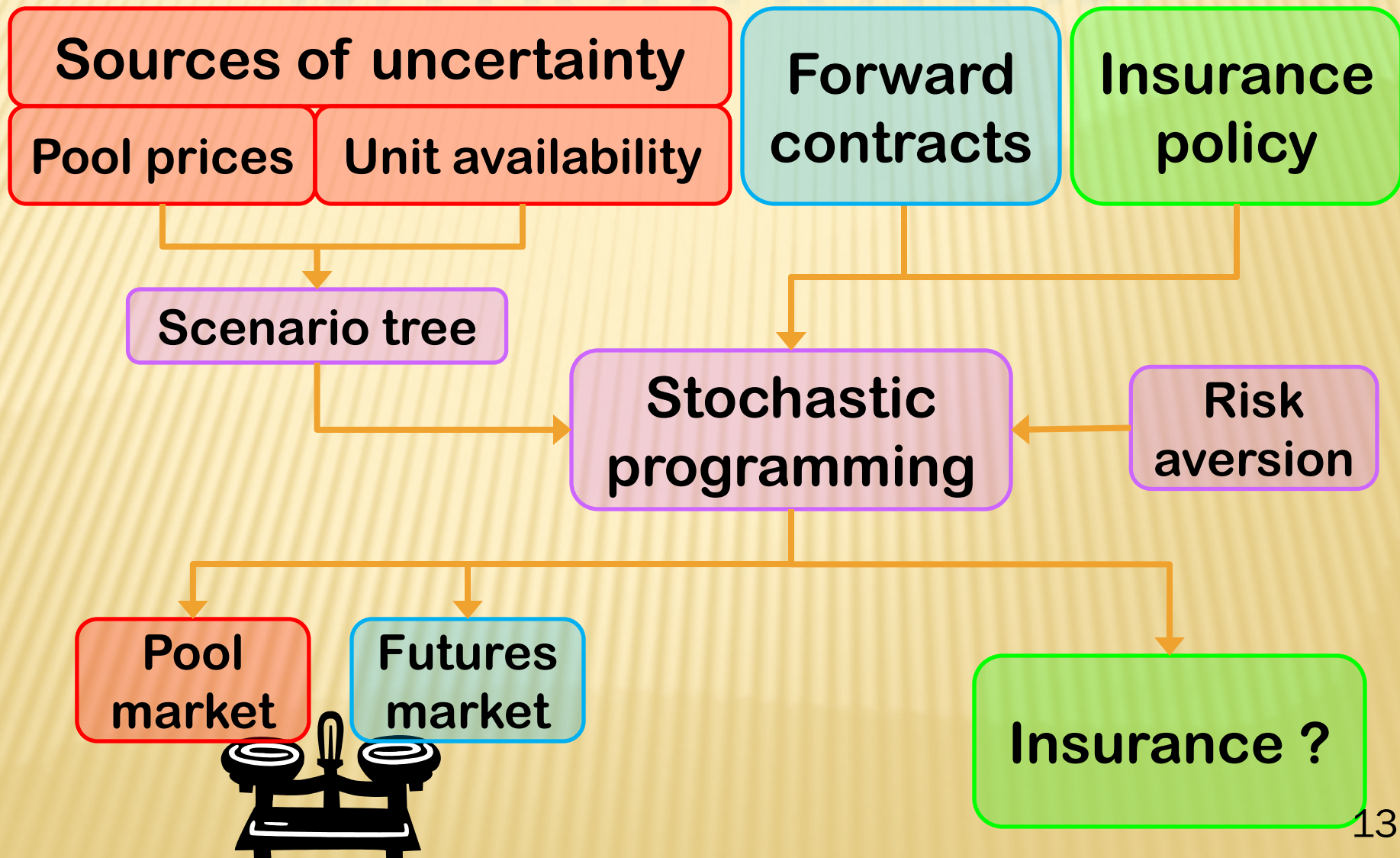
Futures  
market



Insurance ?



# INTRODUCTION

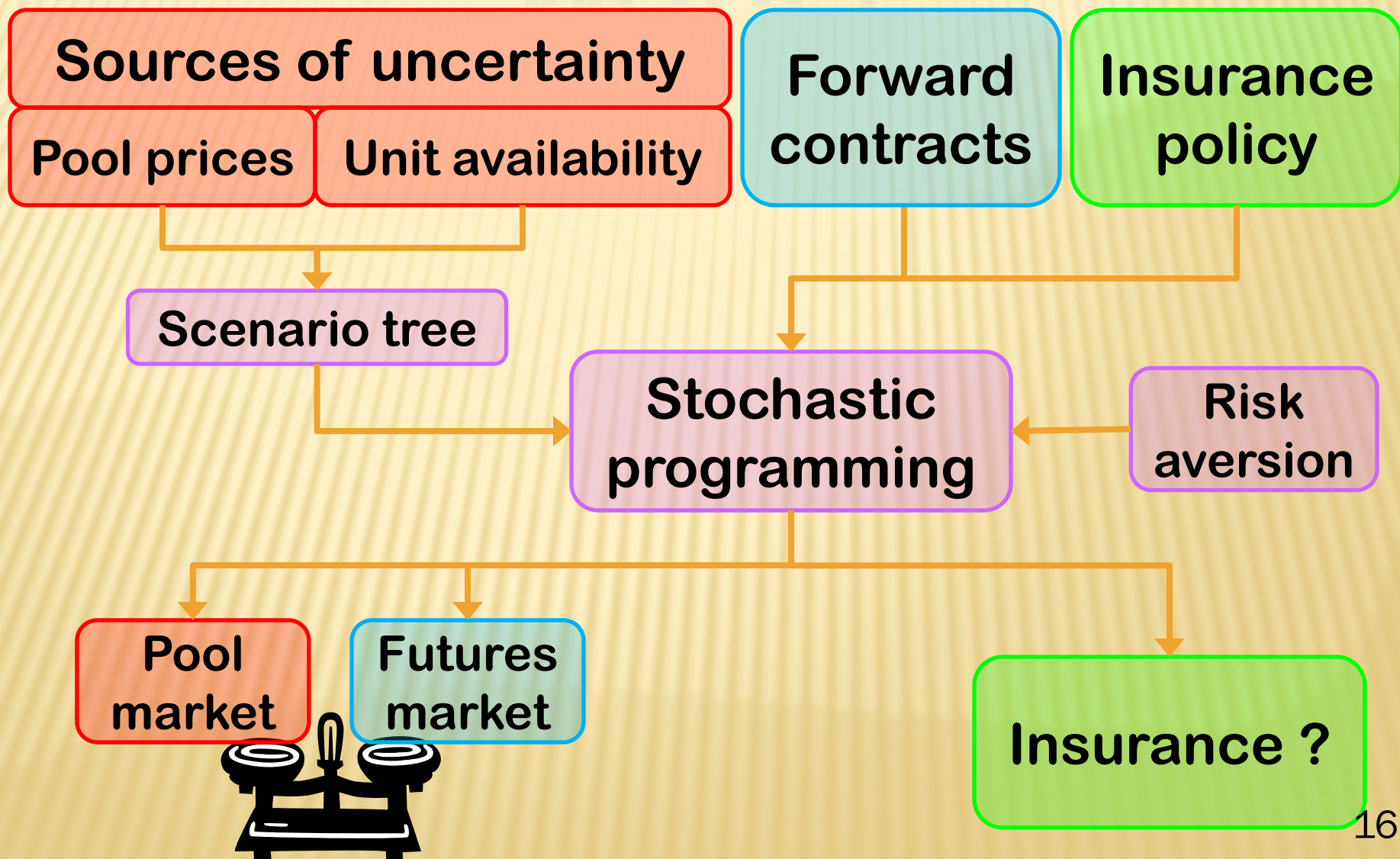


**Analyze the effect of an  
insurance contract on the  
decisions of a power producer**

# OUTLINE

- Introduction
- **Model**
- Case study
- Conclusions

# MODEL





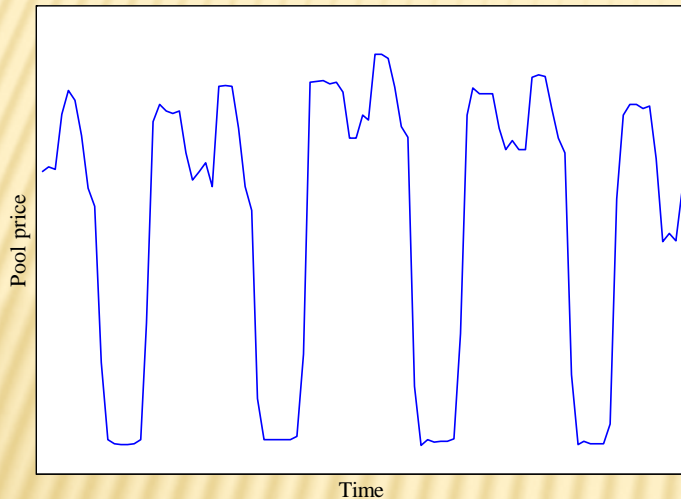
# MODEL

**Pool prices**

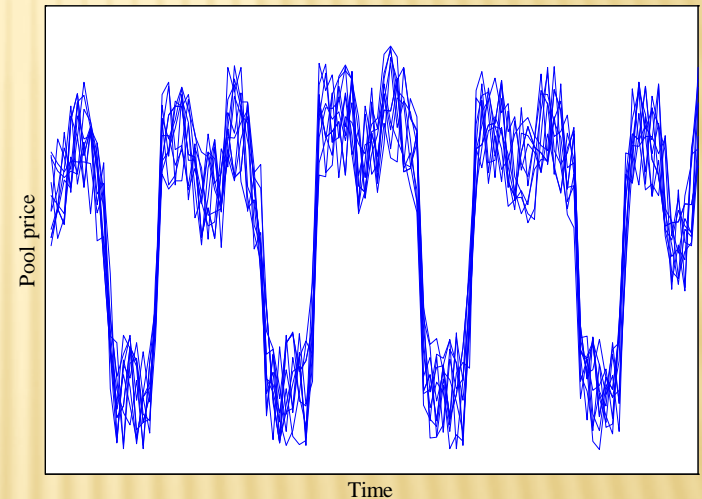
# MODEL

## Pool prices

Historical data

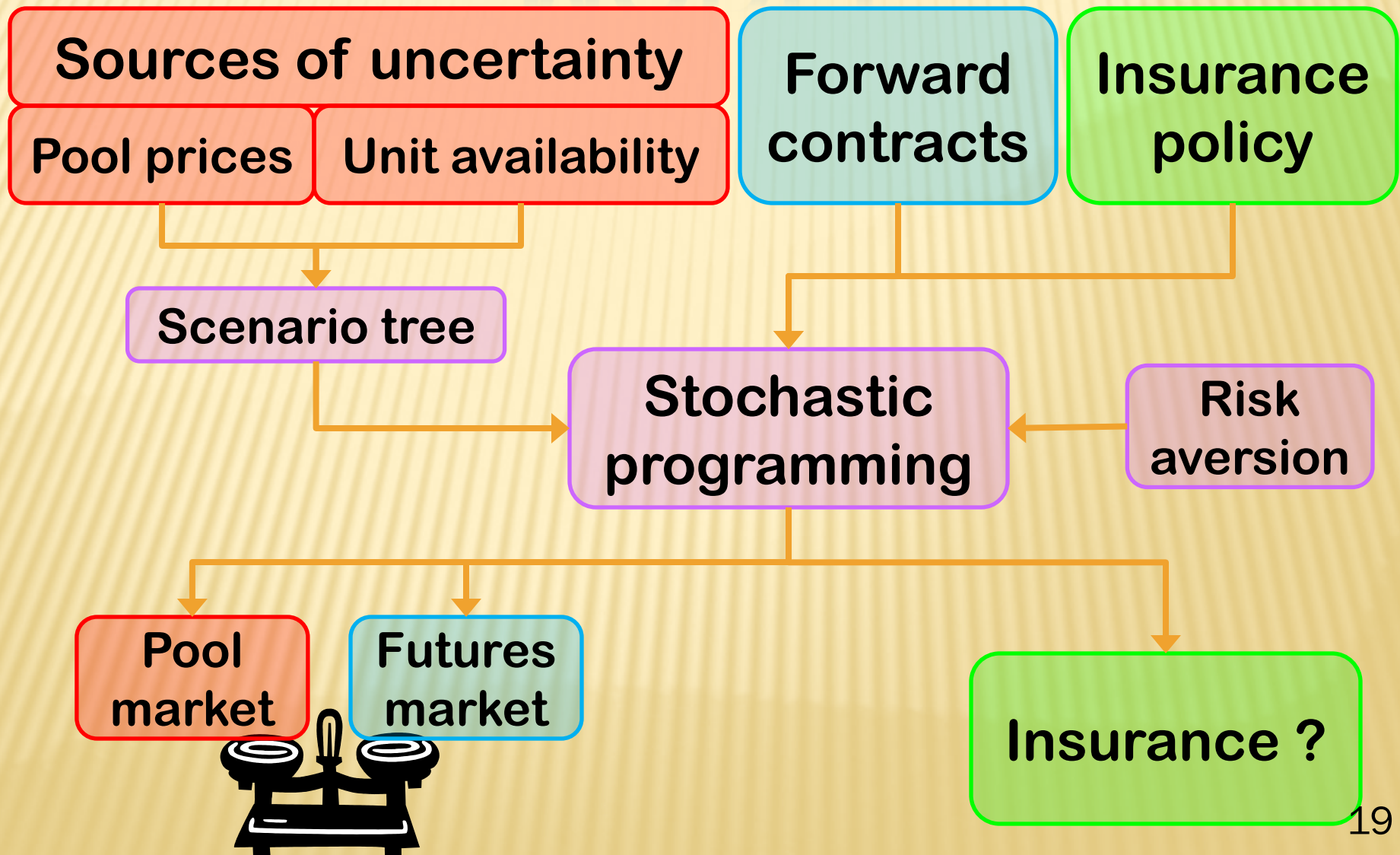


Pool price scenarios



ARIMA model

# MODEL



# MODEL

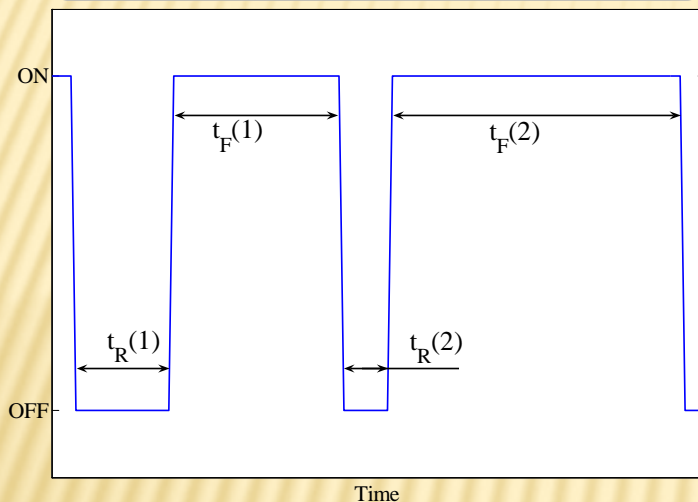
**Unit availability**



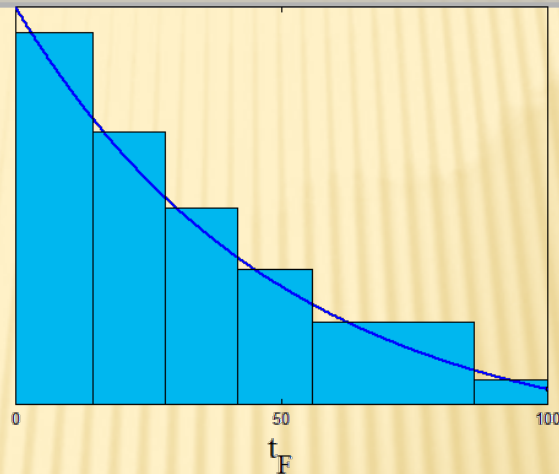
# MODEL

## Unit availability

### Historical data

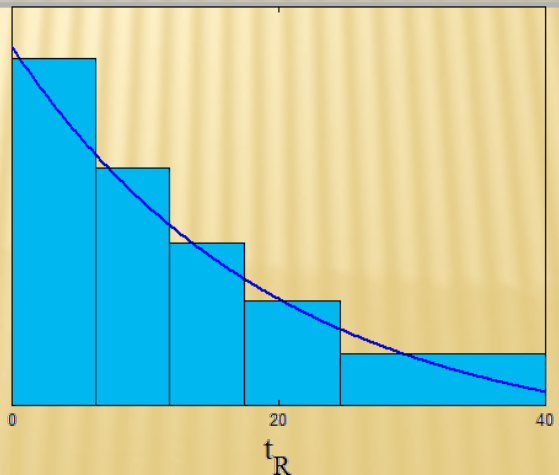


Failure time series = 20, 35, ....



$\sim \exp(\text{MTTF})$

Repair time series = 12, 8, ....

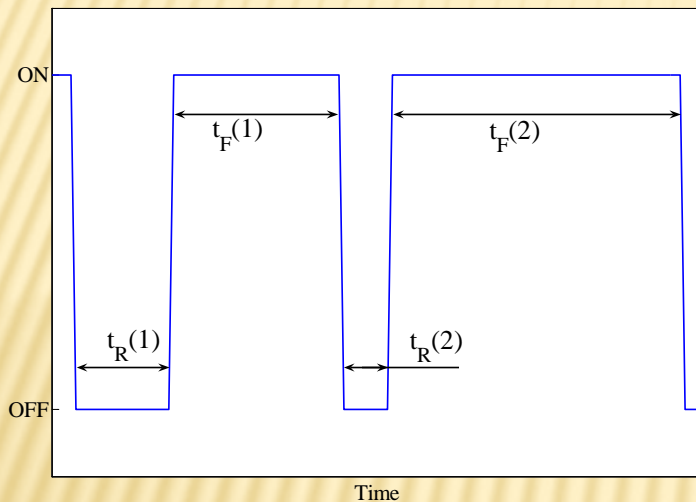


$\sim \exp(\text{MTTR})$

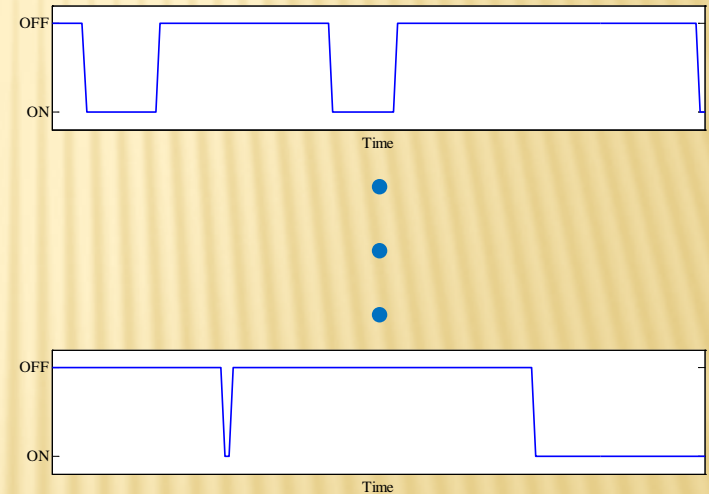
$$\text{FOR}(\%) = \frac{\text{MTTR}}{\text{MTTF} + \text{MTTR}}$$

## Unit availability

### Historical data



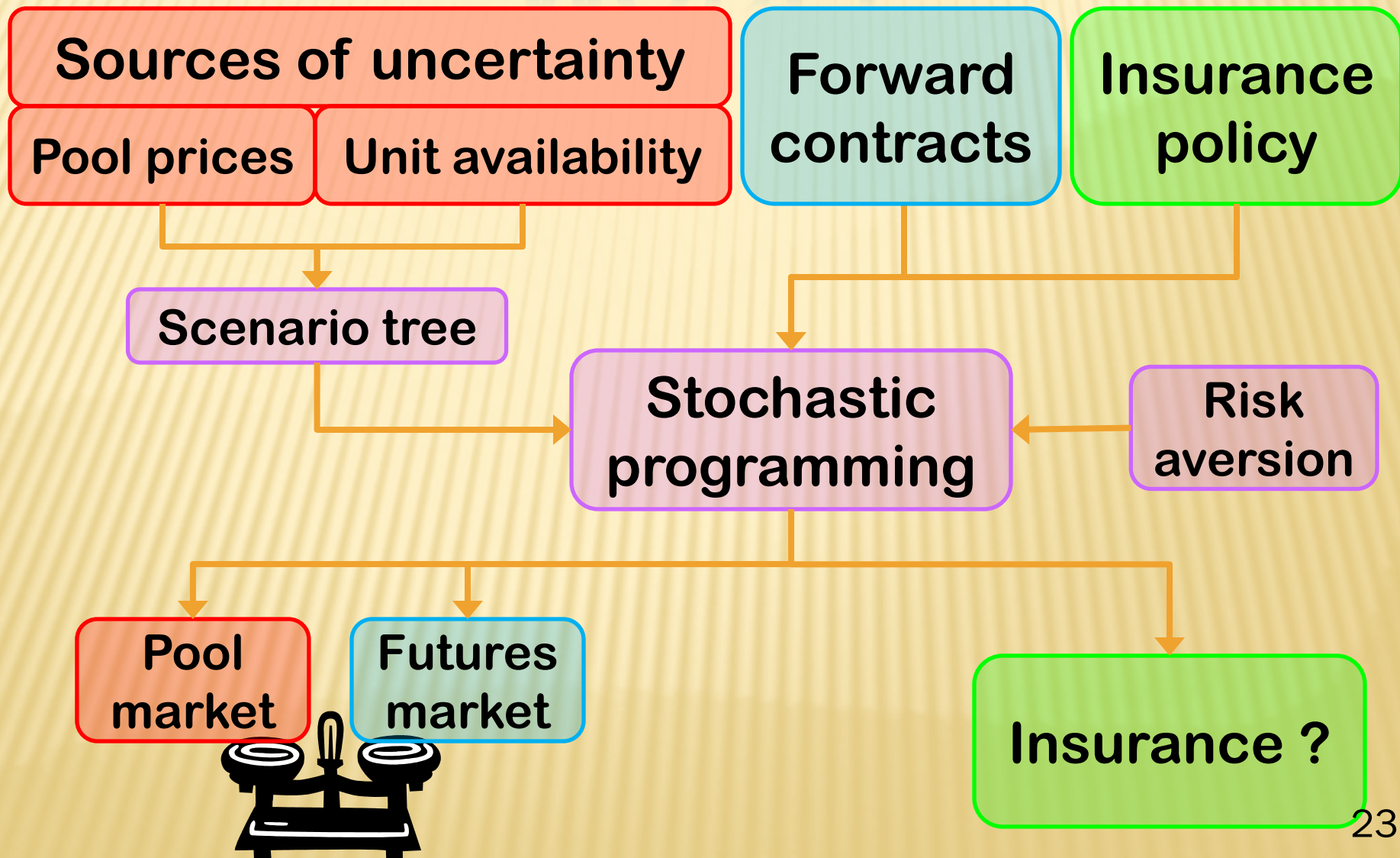
### Availability scenarios



$$t_F \sim \exp(\text{MTTF})$$

$$t_R \sim \exp(\text{MTTR})$$

# MODEL



# MODEL

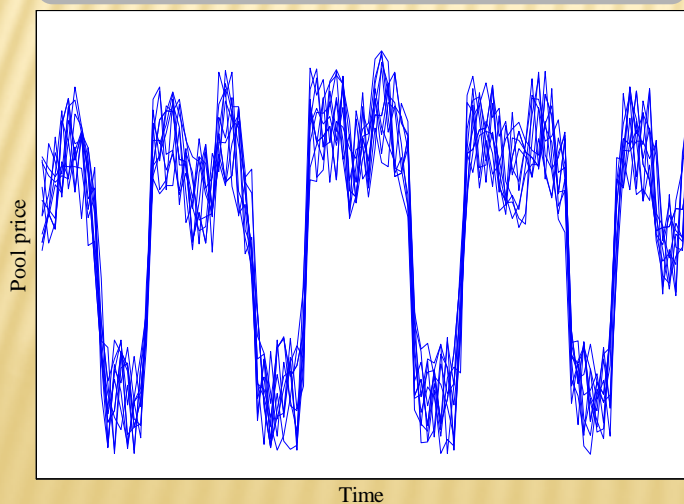
Sources of uncertainty

Pool prices

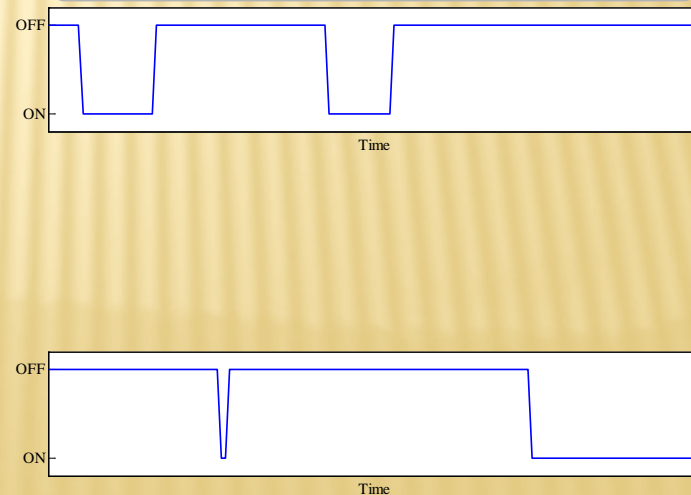
Unit availability

Scenario tree

Pool price scenarios

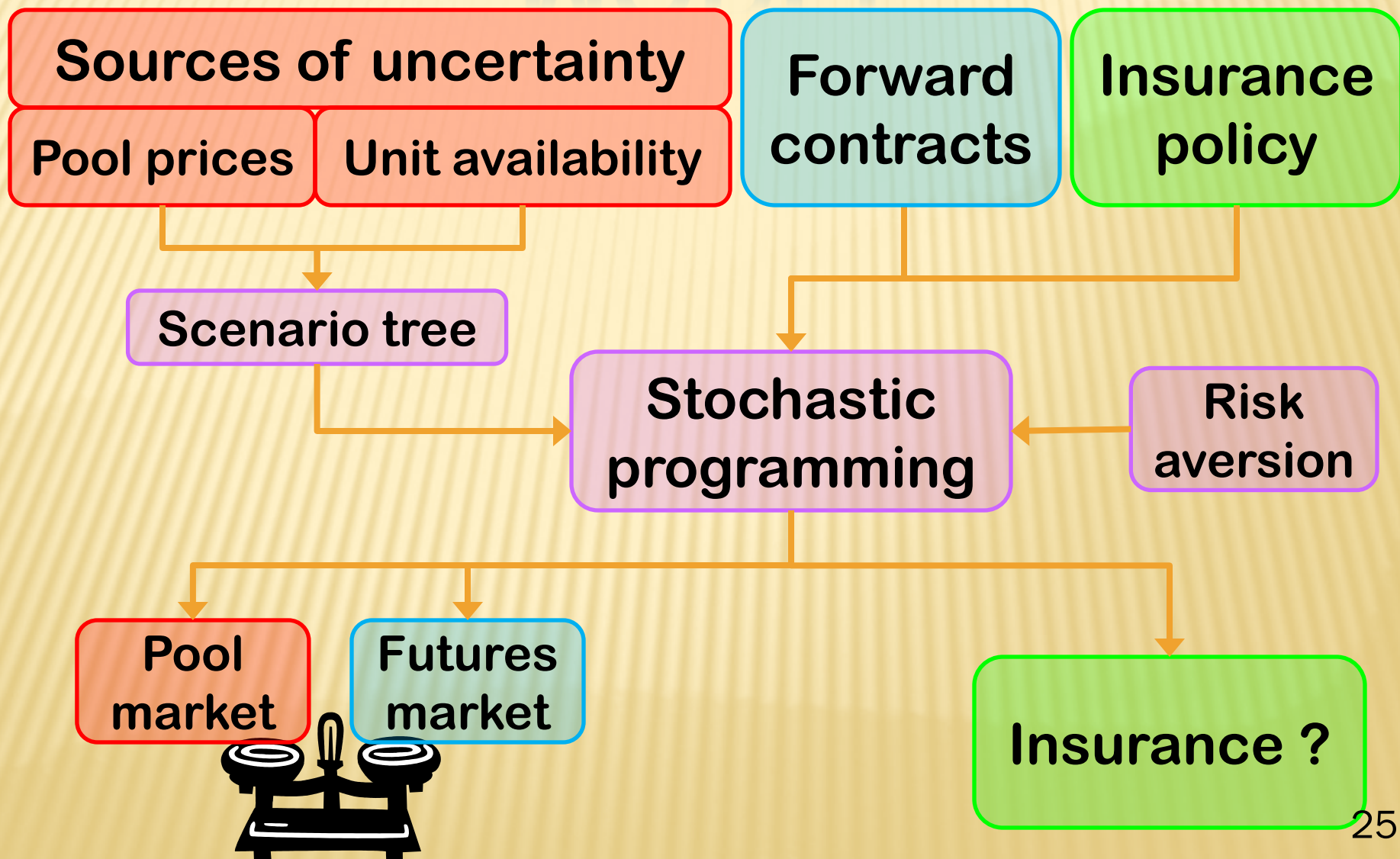


Availability scenarios





# MODEL



# MODEL

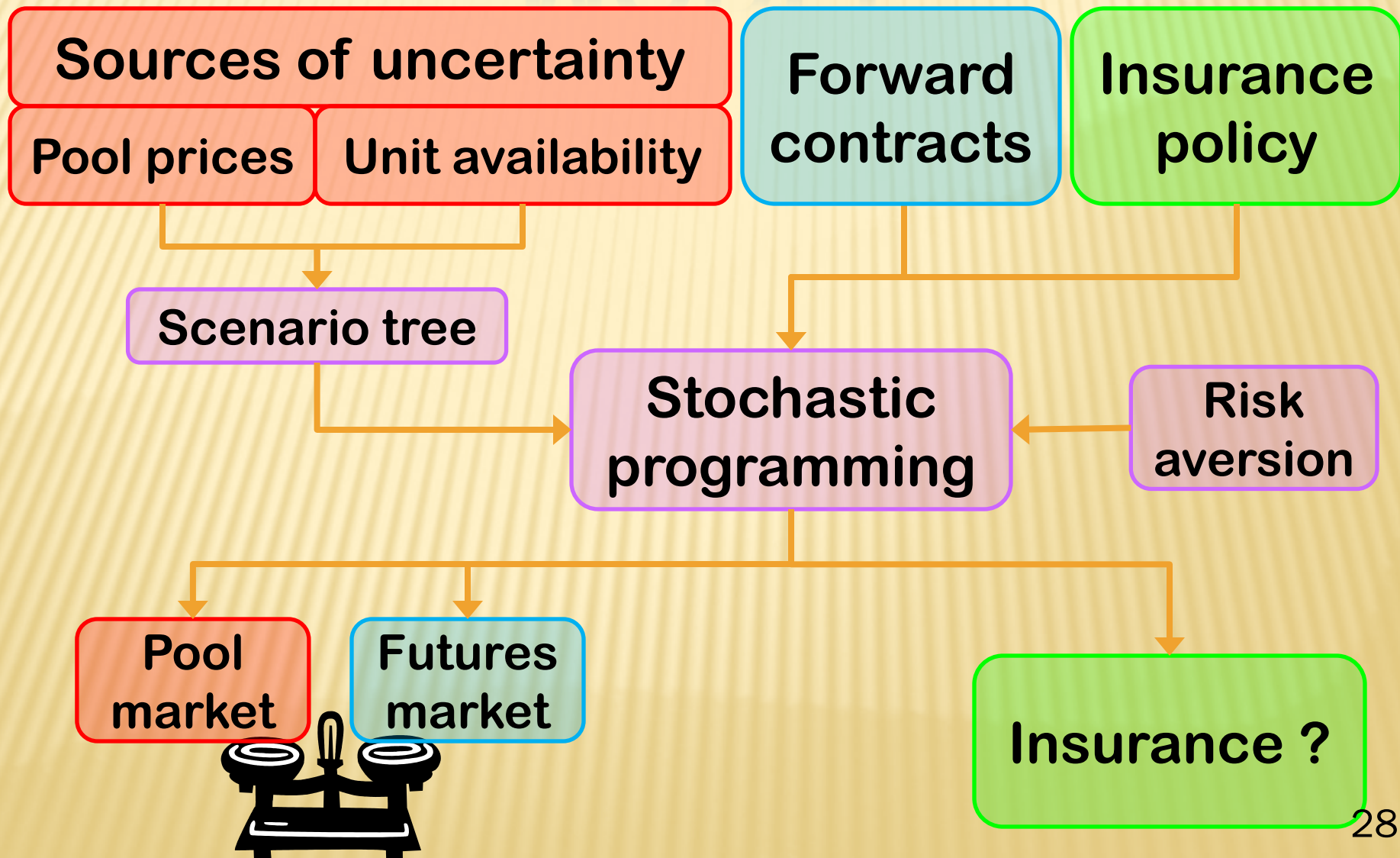
**Forward  
contracts**

# MODEL

## Forward contracts

- Specified quantity (MWh)
- Fixed price
- Future delivery period

# MODEL





# MODEL

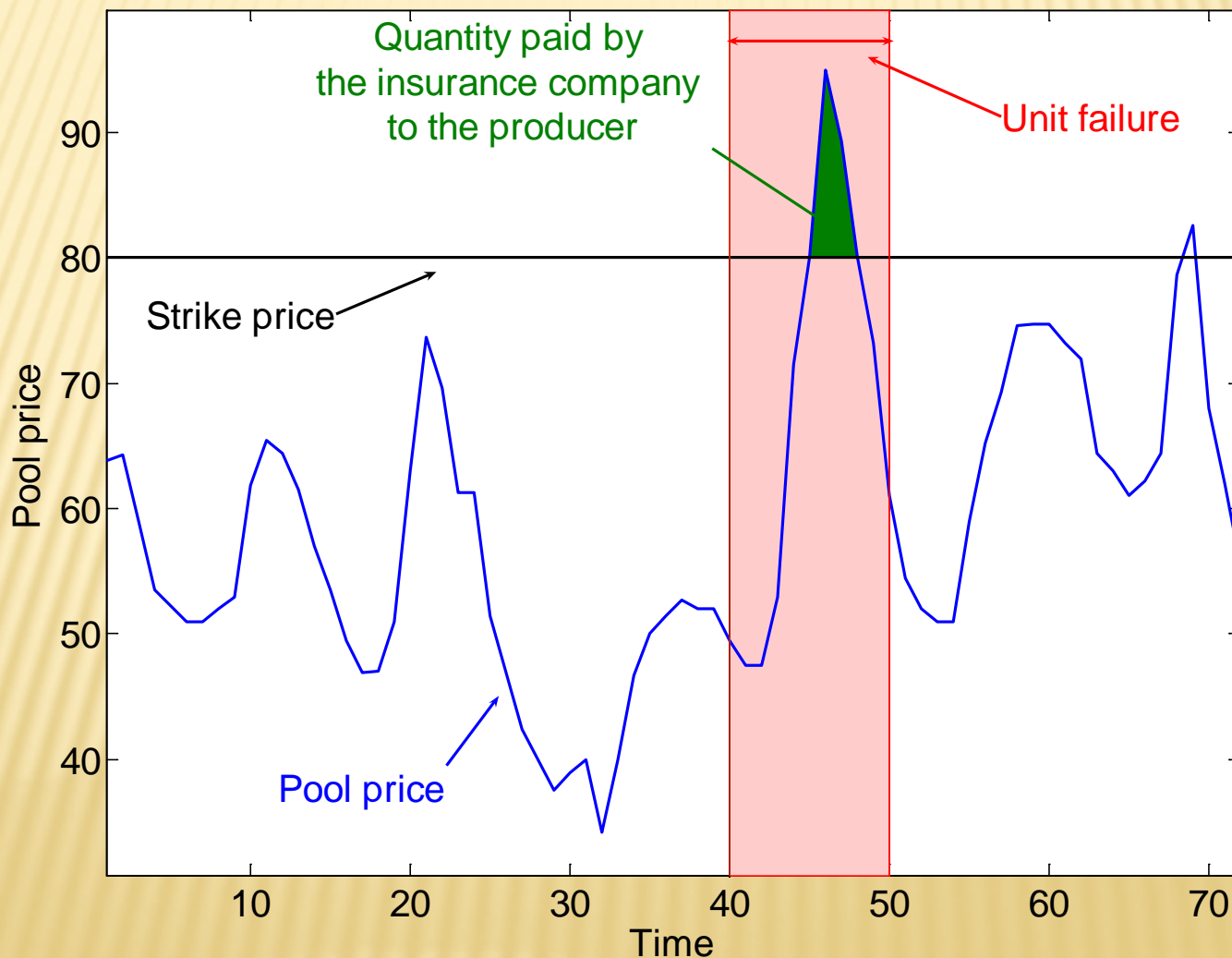
**Insurance  
policy**

# MODEL

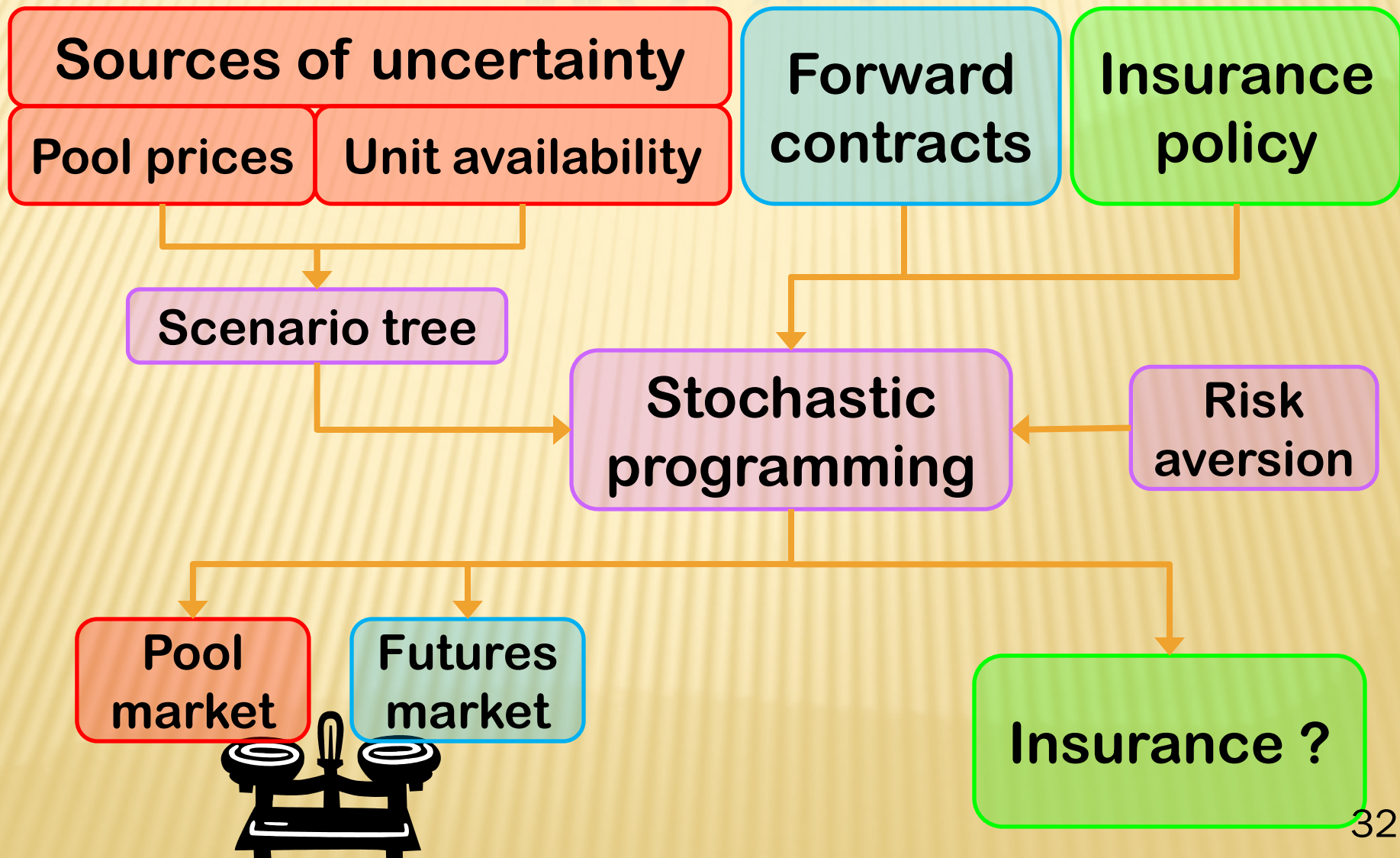
## Insurance policy

- Initial premium
- Insured power
- Time period covered
- Conditions:
  - Pool price > Strike price
  - Unit unavailable

## Insurance policy



# MODEL





# MODEL

**Stochastic  
programming**

**Risk  
aversion**



# MODEL

## Stochastic programming

**Objective function**

**Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$**

**Constraints**

**Production unit limits**

**Energy balance**

**Forward characteristics**

# MODEL

## Stochastic programming

Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

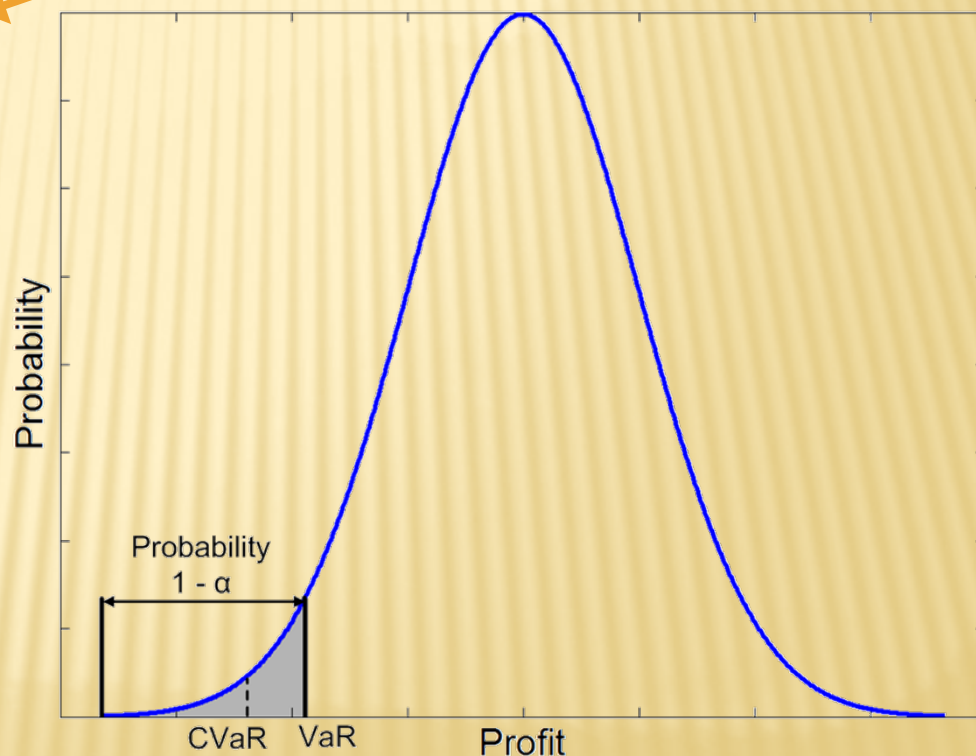
Risk aversion

Constraints

Production unit limits

Energy balance

Forward characteristics





## Stochastic programming

### Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

$$CVaR_{\alpha} = \zeta - \frac{1}{1-\alpha} \sum_{\omega=1}^{N_W} \pi_{\omega} \eta_{\omega}$$

$$- \text{profit}_{\omega} + \zeta - \eta_{\omega} \leq 0$$

$$\eta_{\omega} \geq 0$$

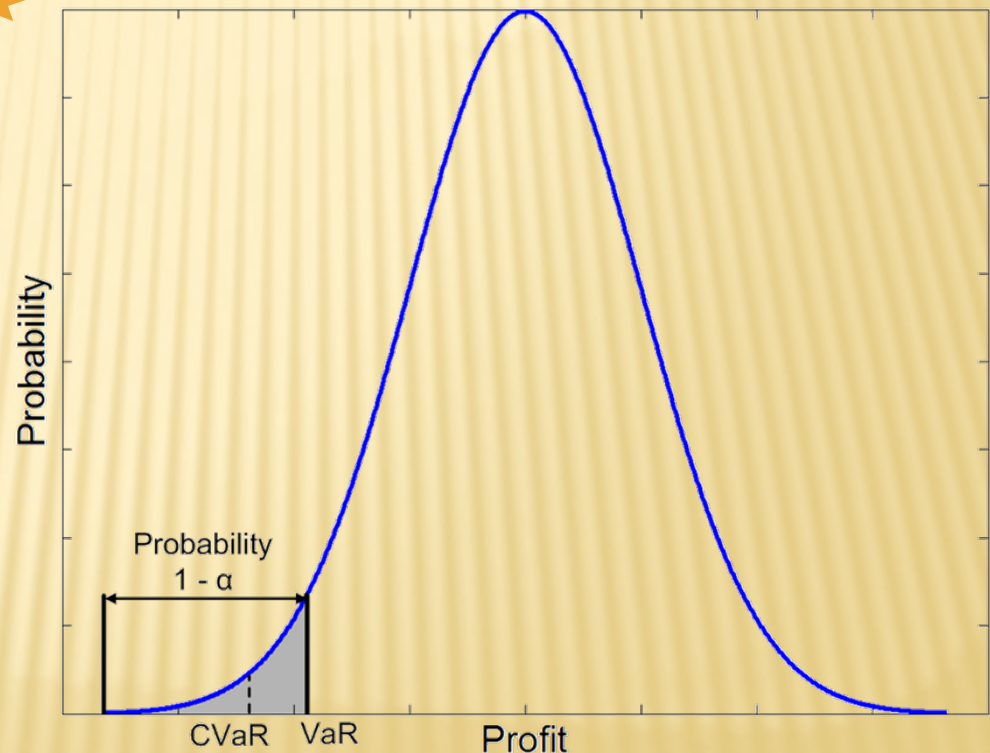
### Constraints

Production unit limits

Energy balance

Forward characteristics

### Risk aversion





# MODEL

## Stochastic programming

### Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

$$\text{profit}_{\omega} = \sum_{t=1}^{N_T} \pi_{\omega} \left( \lambda_{t\omega}^P P_{t\omega}^P T_t - C(P_{t\omega}^G) \right) + \sum_{c=1}^{N_C} \lambda_c P_c T_c + s_I \left( -M_I + P_I \sum_{t \in G_{\omega}} (\lambda_{t\omega}^P - \lambda_I) T_t \right)$$

**Pool**

$\lambda_{t\omega}^P \rightarrow$  Pool price

$P_{t\omega}^P \rightarrow$  Power sold in the pool

$T_t \rightarrow$  Duration of time period

### Constraints

Production unit limits

Energy balance

Forward characteristics

# MODEL

## Stochastic programming

### Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

$$\text{profit}_{\omega} = \sum_{t=1}^{N_T} \pi_{\omega} \left( \lambda_{t\omega}^P P_{t\omega}^P T_t - C(P_{t\omega}^G) \right) + \sum_{c=1}^{N_C} \lambda_c P_c T_c + s_I \left( -M_I + P_I \sum_{t \in G_{\omega}} (\lambda_{t\omega}^P - \lambda_I) T_t \right)$$

Pool
Cost

$C(\cdot) \rightarrow$  Cost function

$P_{t\omega}^G \rightarrow$  Generated power

### Constraints

Production unit limits

Energy balance

Forward characteristics

# MODEL

## Stochastic programming

### Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

$$\text{profit}_{\omega} = \sum_{t=1}^{N_T} \pi_{\omega} \left( \underbrace{\lambda_{t\omega}^P P_{t\omega}^P T_t}_{\text{Pool}} - \underbrace{C(P_{t\omega}^G)}_{\text{Cost}} \right) + \underbrace{\sum_{c=1}^{N_C} \lambda_c P_c T_c}_{\text{Forward}} + s_I \left( -M_I + P_I \sum_{t \in G_{\omega}} (\lambda_{t\omega}^P - \lambda_I) T_t \right)$$

$\lambda_c \rightarrow$  Forward price

$P_c \rightarrow$  Power sold through forward contract

$T_c \rightarrow$  Forward contract duration

### Constraints

Production unit limits

Energy balance

Forward characteristics



# MODEL

## Stochastic programming

### Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

$$\text{profit}_{\omega} = \sum_{t=1}^{N_T} \pi_{\omega} \left( \underbrace{\lambda_{t\omega}^P P_{t\omega}^P T_t}_{\text{Pool}} - \underbrace{C(P_{t\omega}^G)}_{\text{Cost}} \right) + \underbrace{\sum_{c=1}^{N_C} \lambda_c P_c T_c}_{\text{Forward}} + s_I \left( -M_I + P_I \sum_{t \in G_{\omega}} (\lambda_{t\omega}^P - \lambda_I) T_t \right) \quad \text{Insurance}$$

$s_I \rightarrow$  Binary variable

$M_I \rightarrow$  Initial premium

$P_I \rightarrow$  Insured power

$t \in G_{\omega} \Leftrightarrow k_{t\omega} = 0$  and  $\lambda_{t\omega}^P \geq \lambda_I$

$\lambda_I \rightarrow$  Strike price

### Constraints

Production unit limits

Energy balance

Forward characteristics



## Stochastic programming

Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

Constraints

Production unit limits

$$P_{\max} \geq u_{t\omega} k_{t\omega} P_{t\omega}^G \geq P_{\min}$$

Input data (availability scenarios)

Binary variable (on/off)

Balance energy

Forward characteristics

## Stochastic programming

Objective function

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

Constraints

Production unit limits

Energy balance

$$P_{t\omega}^G = \sum_{c \in F_t} P_c + P_{t\omega}^P$$

$$\quad \quad \quad \hookrightarrow P_{t\omega}^P \geq (k_{tw} - 1) \sum_{c \in F_t} P_c$$

Forward characteristics

# MODEL

## Stochastic programming

**Objective function**

Maximize  $CVaR_{\alpha}(\text{profit}_{\omega})$

**Constraints**

Production unit limits

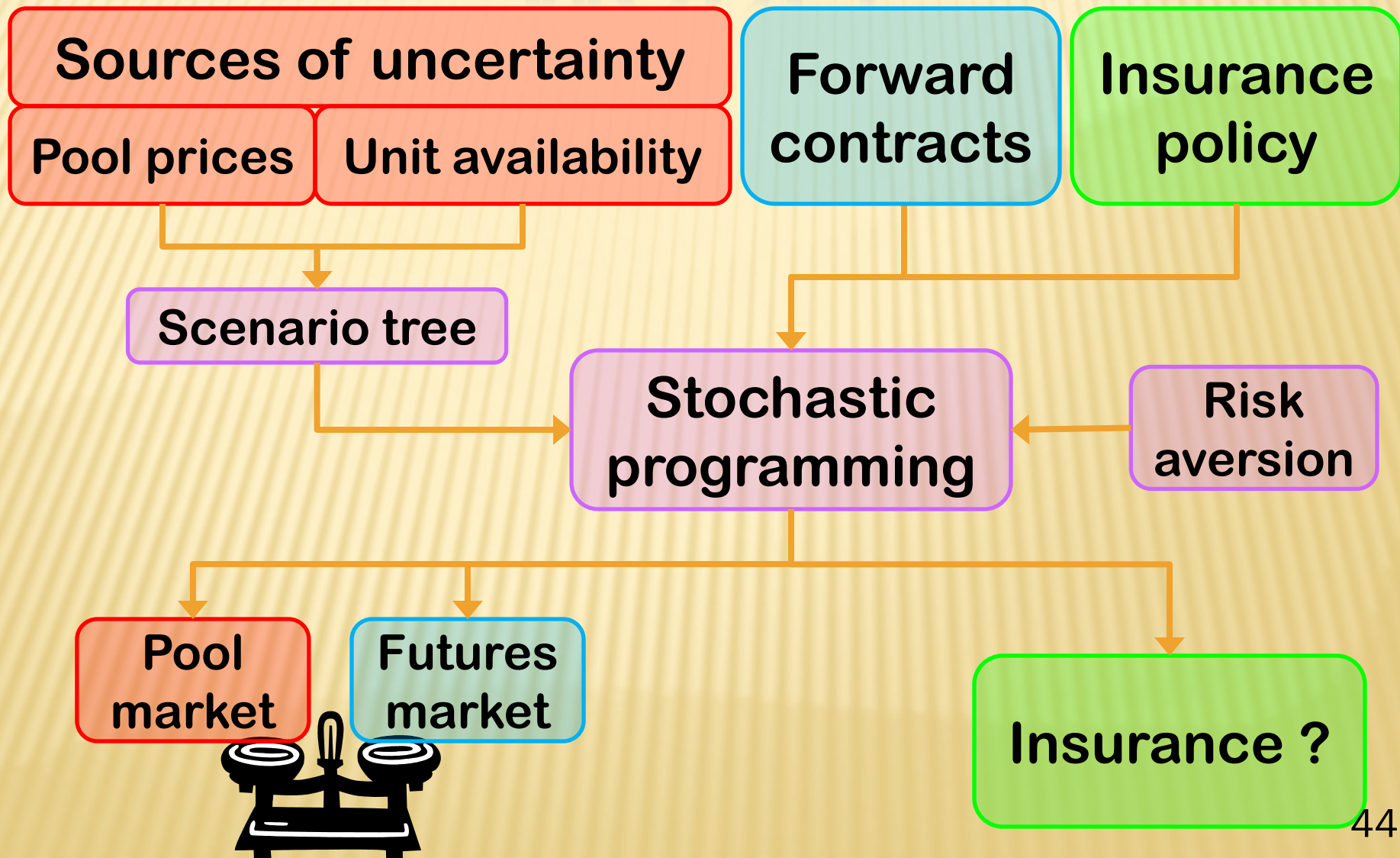
Energy balance

Forward characteristics

$$P_c \leq P_c^{\max}$$



# MODEL



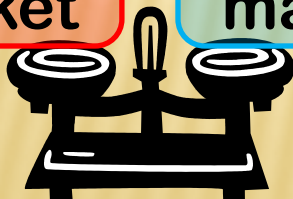


# MODEL

MODEL

Pool  
market

Futures  
market



Insurance ?

# OUTLINE

- Introduction
- Model
- Case study
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# CASE STUDY

- 3 months
- 4 forward contracts (3 monthly and 1 quarterly)
- 1 Insurance contract
  - Premium: 100,000 €
  - Insured power: 75 MW
  - Strike price: 10 €/MWh
- 300 pool price scenarios reduced to 50
- 10,000 availability scenarios reduced to 200
- Generating unit
  - $P_{\max} = 500 \text{ MW}$  &  $P_{\min} = 50 \text{ MW}$
  - Three FOR values: 0, 4 and 8%
  - Piecewise lineal cost function

# CASE STUDY

## Without insurance

FOR	$\alpha^P$	Average $P_c$ (MW)	CVaR (/10 <sup>6</sup> €)
0%	0	0	11.7
	0.95	150	8.5
4%	0	0	11.2
	0.95	150	7.9
8%	0	0	10.7
	0.95	125	7.0

## With insurance

FOR	$\alpha^P$	Average $P_c$ (MW)	CVaR (/10 <sup>6</sup> €)	$s_i$
0%	0	0	11.7	0
	0.95	150	8.5	0
4%	0	0	11.2	0
	0.95	150	8.0	1
8%	0	0	10.7	1
	0.95	150	7.4	1



# CASE STUDY

## Without insurance

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# CASE STUDY

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# CASE STUDY

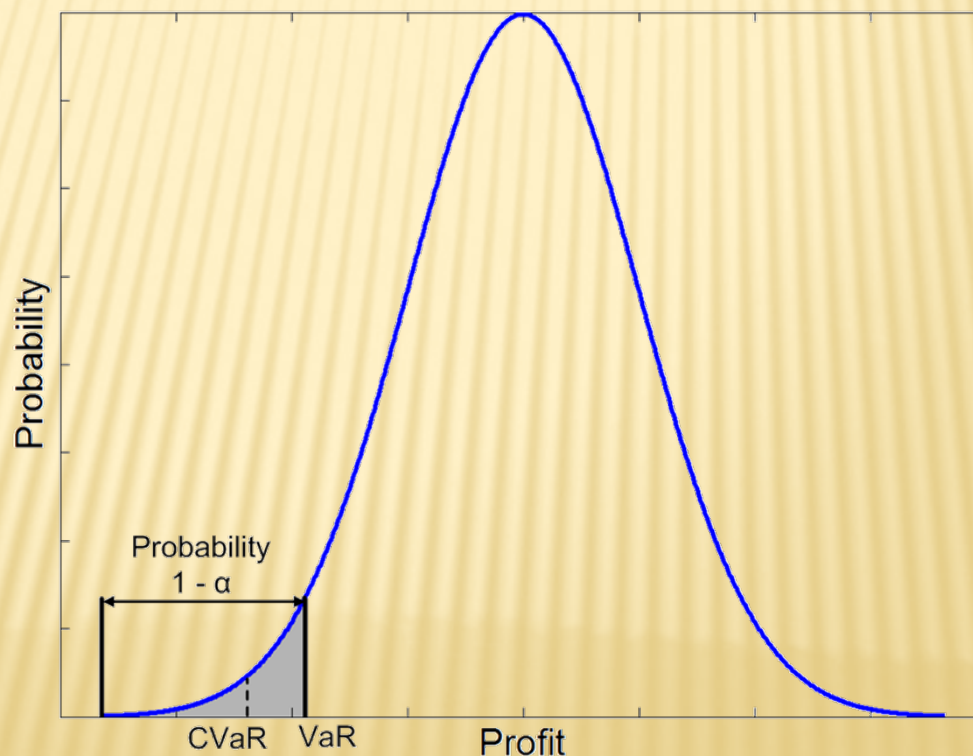
- **Critical premium:** the maximum amount that a producer is willing to pay in exchange for a given insurance contract.



# CASE STUDY

## ➤ Critical premium.

**CVaR is a coherent risk measure:**  $\text{CVaR}_\alpha(Y + c) = \text{CVaR}_\alpha(Y) + c$



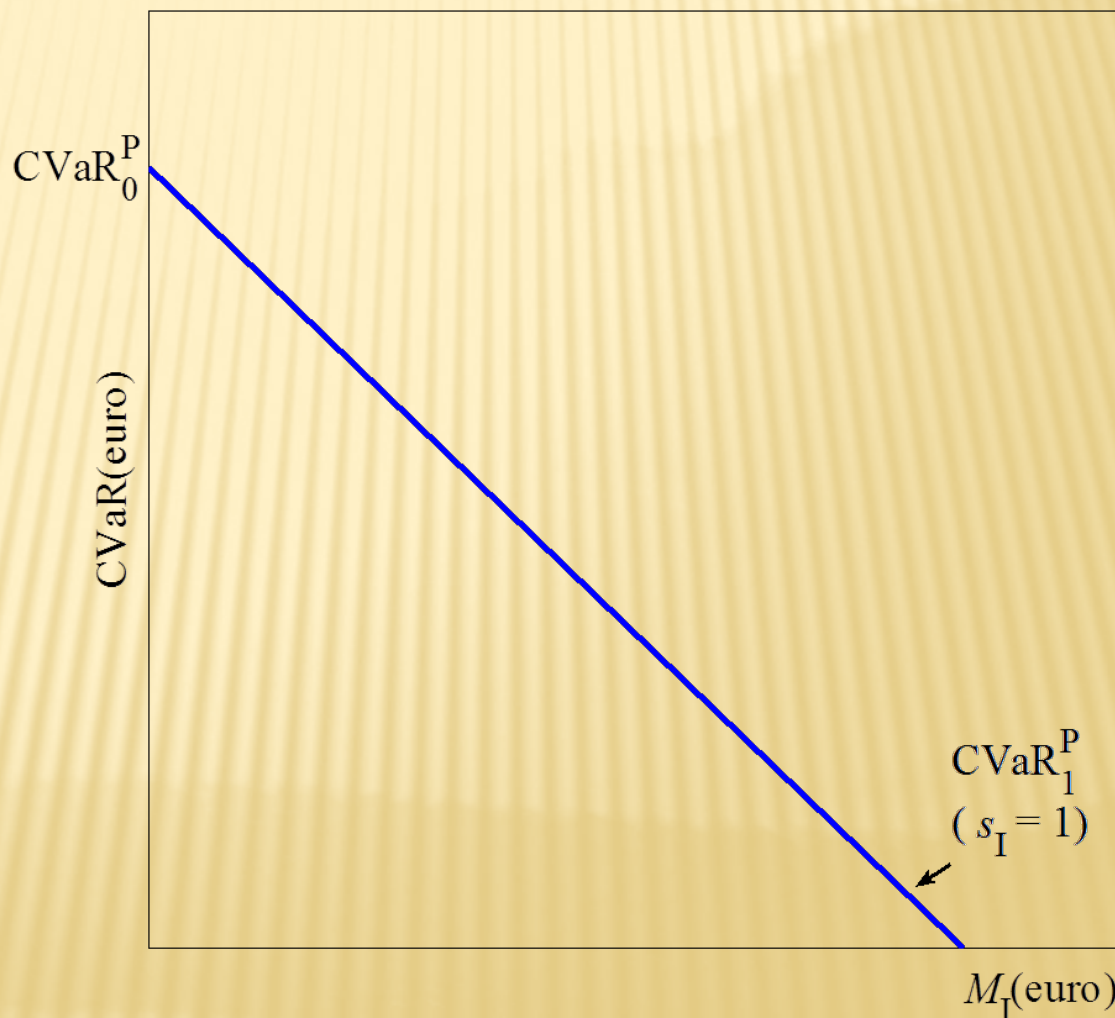
# CASE STUDY

## ➤ Critical premium.

$$\text{CVaR}_{\alpha}(Y + c) = \text{CVaR}_{\alpha}(Y) + c$$

**Case 1** ( $s_I = 1$ ):

$$\text{CVaR}_1^P = \text{CVaR}_0^P - M_I$$



# CASE STUDY

$$\text{CVaR}_{\alpha}(Y + c) = \text{CVaR}_{\alpha}(Y) + c$$

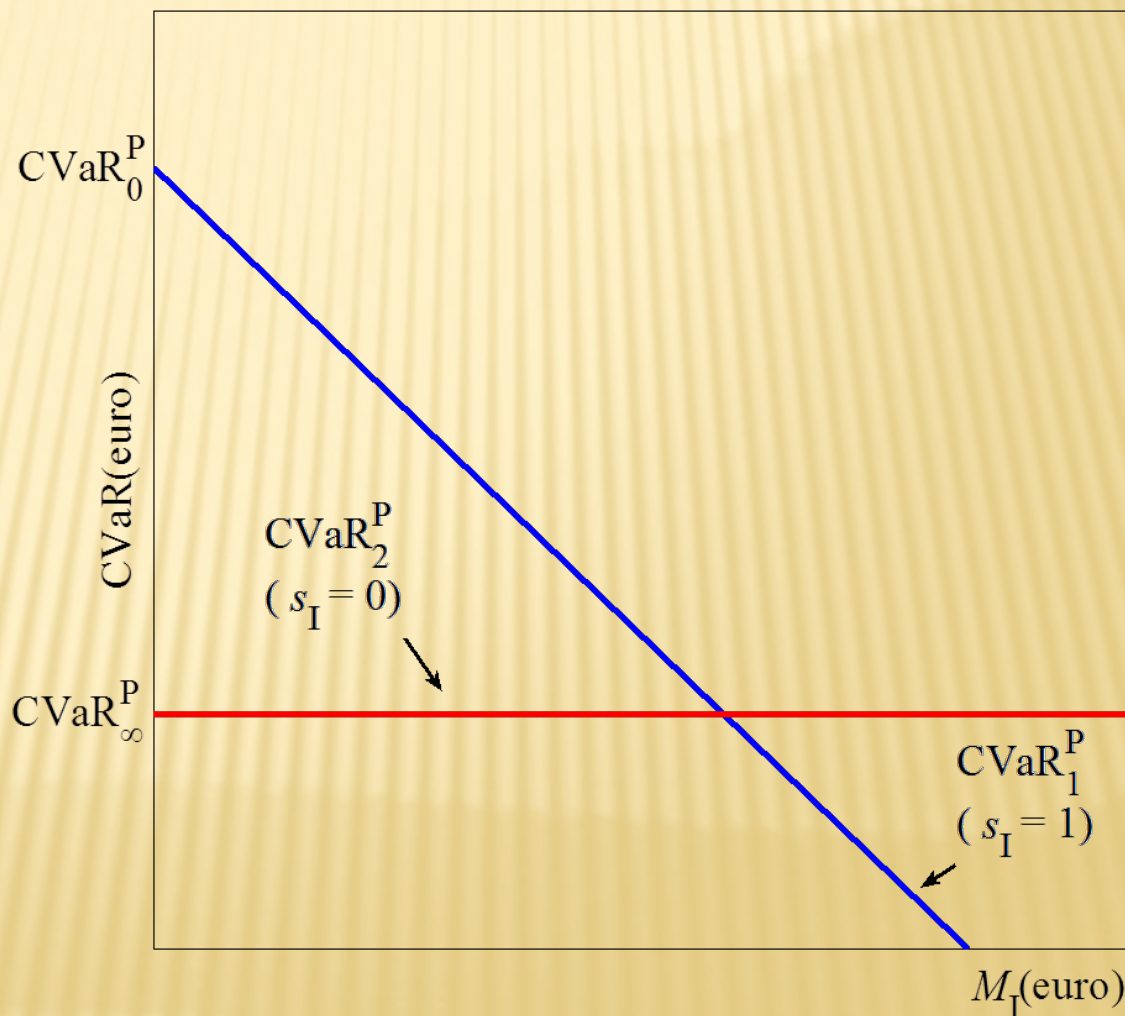
## ➤ Critical premium.

**Case 1** ( $s_I = 1$ ):

$$\text{CVaR}_1^P = \text{CVaR}_0^P - M_I$$

**Case 2** ( $s_I = 0$ ):

$$\text{CVaR}_2^P = \text{CVaR}_{\infty}^P$$





# CASE STUDY

$$\text{CVaR}_{\alpha}(Y + c) = \text{CVaR}_{\alpha}(Y) + c$$

## ➤ Critical premium.

**Case 1** ( $s_I = 1$ ):

$$\text{CVaR}_1^P = \text{CVaR}_0^P - M_I$$

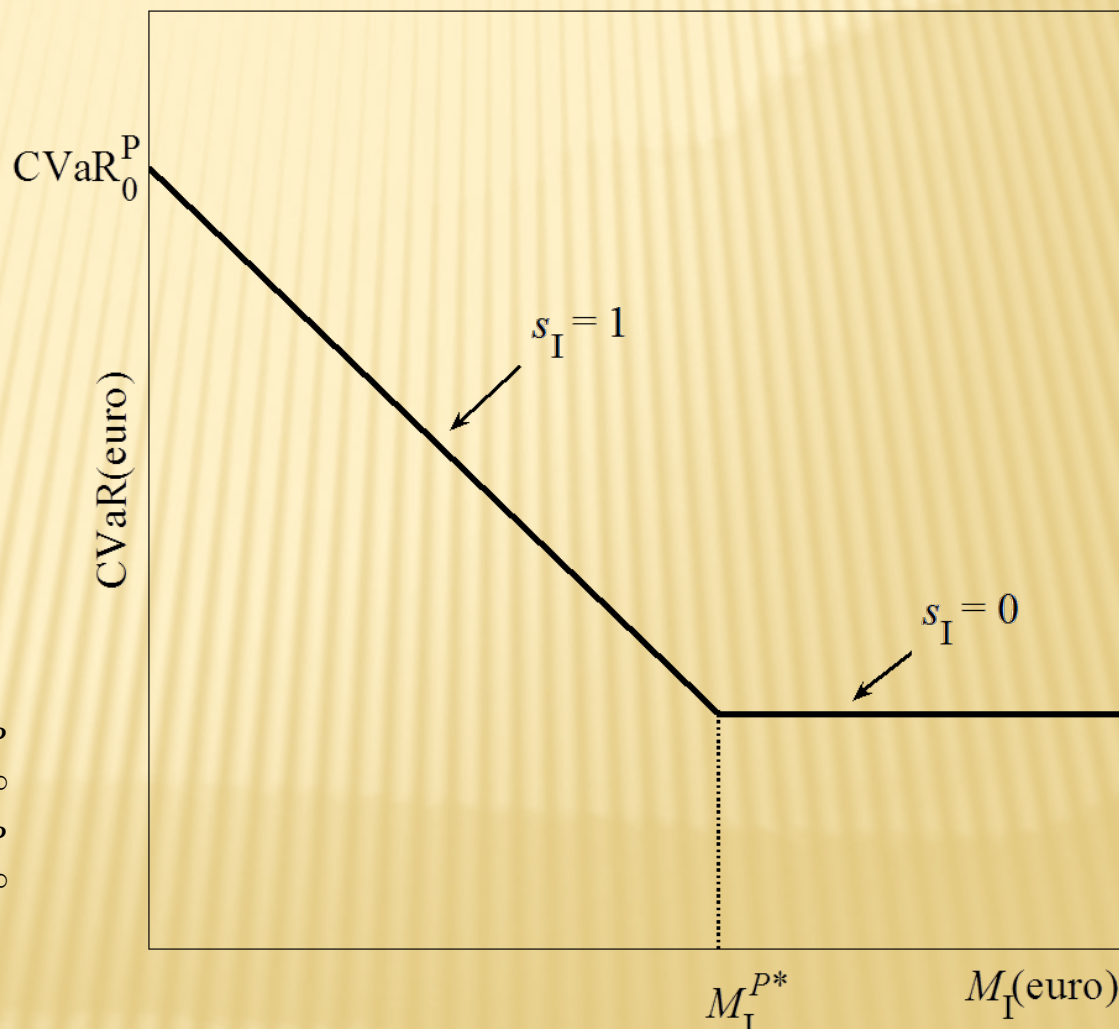
**Case 2** ( $s_I = 0$ ):

$$\text{CVaR}_2^P = \text{CVaR}_{\infty}^P$$

$$\text{CVaR}_1^P = \text{CVaR}_2^P$$

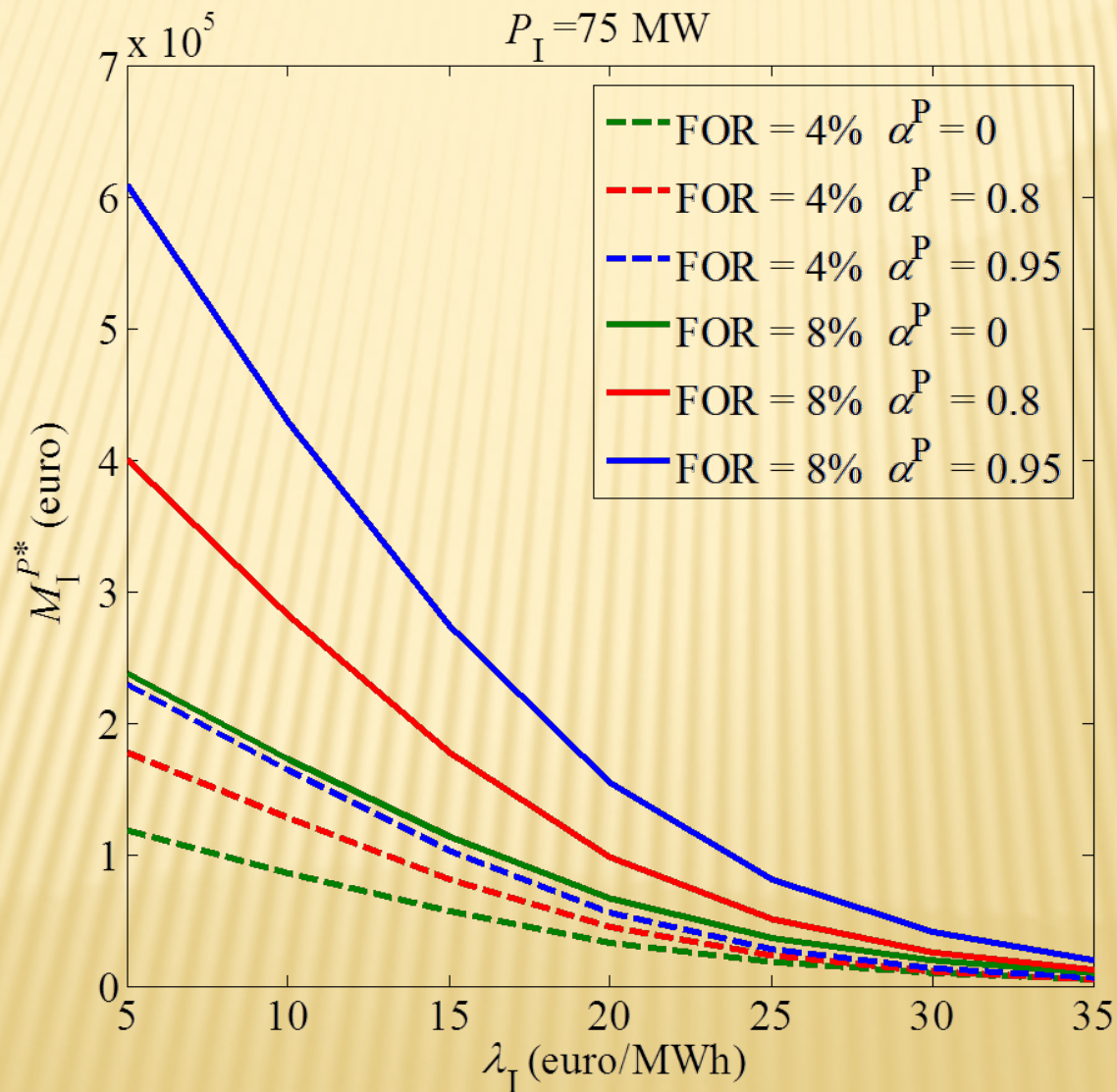
$$\text{CVaR}_0^P - M_I^{P*} = \text{CVaR}_{\infty}^P$$

$$M_I^{P*} = \text{CVaR}_0^P - \text{CVaR}_{\infty}^P$$





# CASE STUDY



# CASE STUDY

## Producer

$\alpha^P$	$M_I^{P*}(\text{€})$
0	173.275
0.3	196.166
0.5	214.615
0.9	358.210

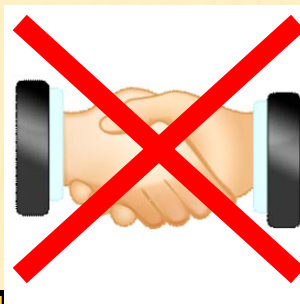
## Insurance company

$\alpha^S$	$M_I^{S*}(\text{€})$
0	173.275
0.3	242.071
0.5	302.974
0.9	563.779

$$P_I = 75MW \quad \lambda_I = 10\text{€}/MWh \quad \text{FOR} = 8\%$$

# CASE STUDY

Producer



Insurance  
company

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# CASE STUDY

Producer



Insurance  
company

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$$P_I = 75MW \quad \lambda_I = 10\text{€}/MWh \quad \text{FOR} = 8\%$$



# OUTLINE

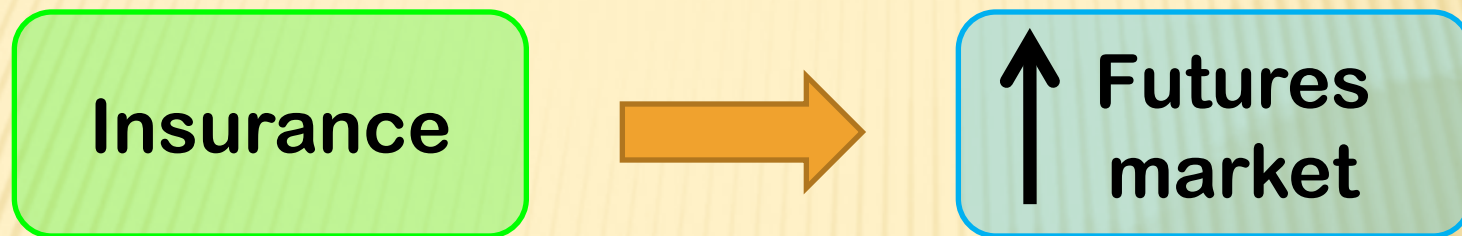
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# CONCLUSIONS

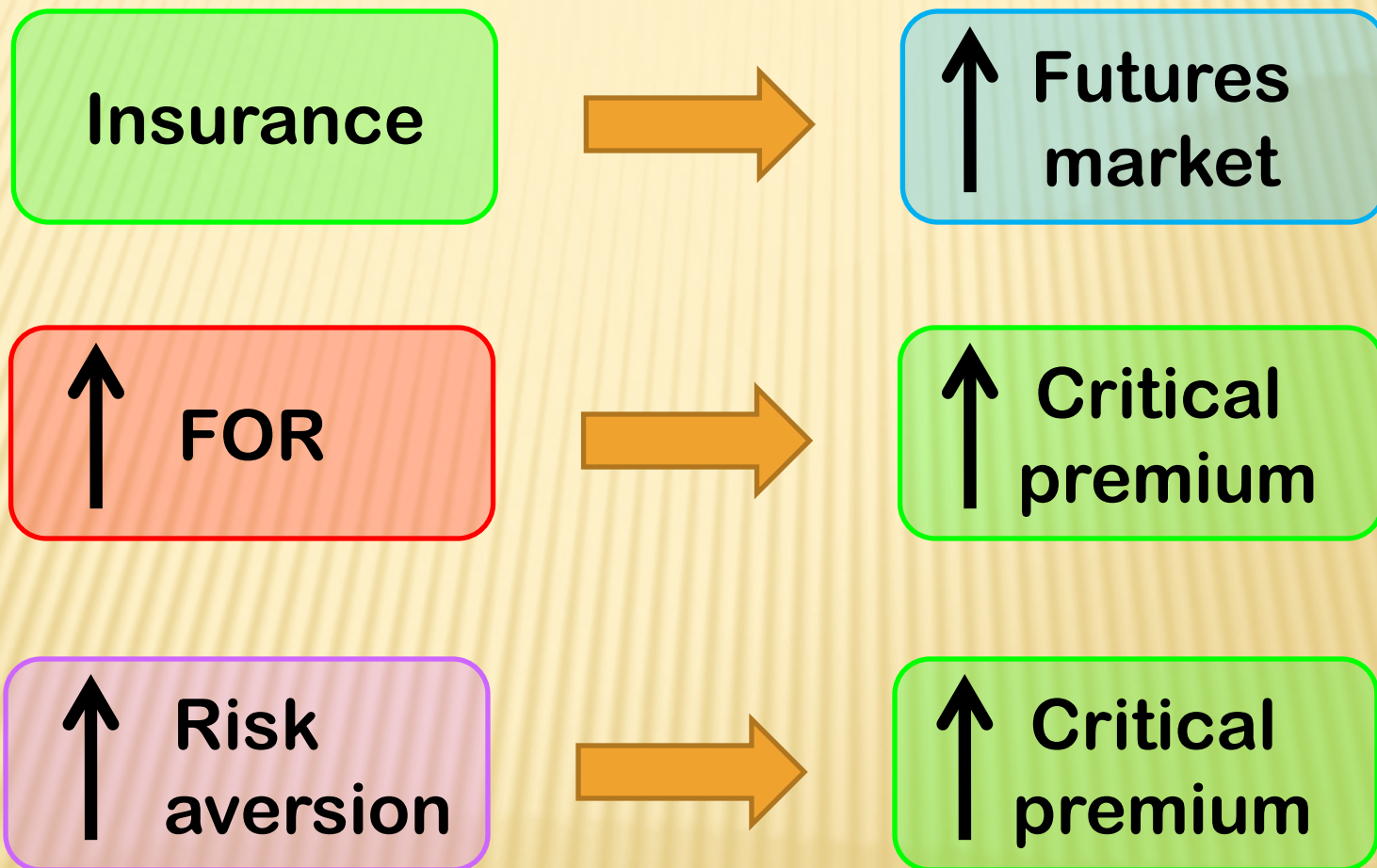
**Stochastic  
programming**



# CONCLUSIONS



# CONCLUSIONS





# CONCLUSIONS



# CONCLUSIONS

Thank you!

Questions?

[www.uclm.es/area/gsee](http://www.uclm.es/area/gsee)