

# Chronological Time-Period Clustering for Optimal Capacity Expansion Planning With Storage

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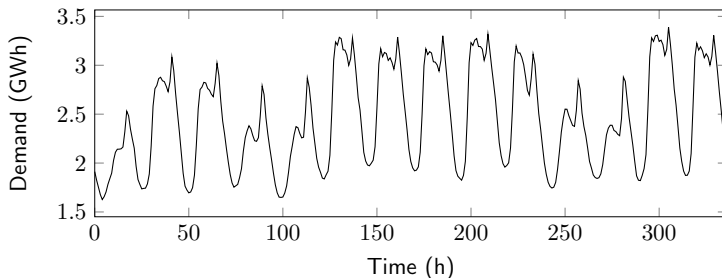
July 10, 2018

# Which are the main problems in power systems?

	<b>OPERATION</b>	<b>PLANNING</b>
<b>Horizon</b>	1 second - 1 week	1 year - 20 years
<b>Decisions</b>	Generation dispatch Power flows	Generation investments Line investments
<b>Objective</b>	Min production cost	Min prod. + inv. cost
<b>Constraints</b>	Generation = Demand Unit technical limits Line technical limits	Generation = Demand Unit technical limits Line technical limits
<b>Comput. burden</b>	Medium	Very high

# How are planning problems usually solved?

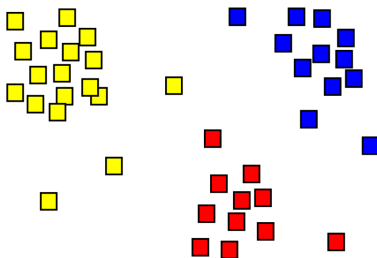
- Taking advantage of the fact that the electrical demand shows strong daily, weekly and annual patterns.



- Using statistical learning techniques such as clustering to group time periods and reduce the computational cost of the planning problem.

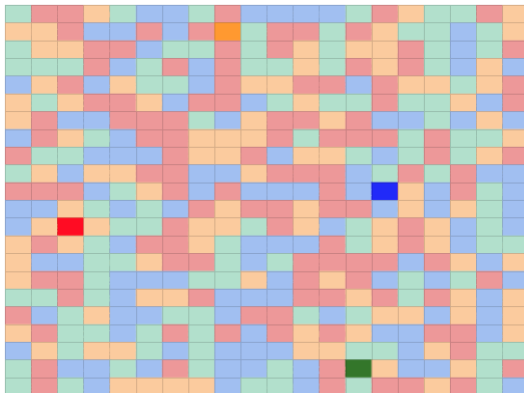
# what is clustering?

- The clustering consists in the task of grouping a set of objects in such a way that the members of the same group (called cluster) are more similar, in one way or another.



# How is clustering used in planning problems?

- The most common approach is to group the days of the time horizon into a small number of clusters and solve the optimization problem considering only the representative days.



# How do I know if two days are similar or not?

- Each day is characterized by normalized demand, wind and solar

$$x_1 = [\underbrace{0.4, 0.6, \dots, 0.5}_{24 \text{ demand values}}, \underbrace{0.1, 0.2, \dots, 0.4}_{24 \text{ wind values}}, \underbrace{0.1, 0.2, \dots, 0.1}_{24 \text{ solar values}}]$$

$$x_2 = [\underbrace{0.6, 0.1, \dots, 0.3}_{24 \text{ demand values}}, \underbrace{0.4, 0.5, \dots, 0.2}_{24 \text{ wind values}}, \underbrace{0.3, 0.4, \dots, 0.2}_{24 \text{ solar values}}]$$

- The similarity between two days is computed using a norm

$$d(x_1, x_2) = \|x_1 - x_2\|_2$$

# How does the clustering algorithm work?

- 1) Set the initial number of clusters  $n$  to the number of days  $N$ .
- 2) Determine the centroid  $\bar{\mathbf{x}}_I$  of each cluster  $I$  as

$$\bar{\mathbf{x}}_I = \frac{1}{|I|} \sum_{i \in I} \mathbf{x}_i$$

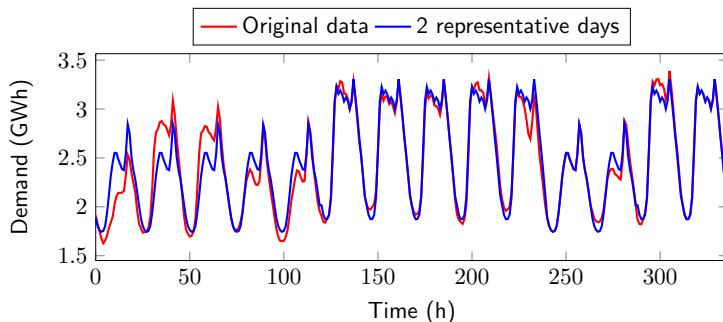
- 3) Compute the dissimilarity between each pair of clusters  $I, J$  according to Ward's method as follows

$$D(I, J) = \frac{2|I||J|}{|I| + |J|} \|\bar{\mathbf{x}}_I - \bar{\mathbf{x}}_J\|^2$$

- 4) Merge the two closest clusters  $(I', J')$  according to the dissimilarity matrix, i.e.,  $(I', J') \in \operatorname{argmin} D(I, J)$  s.t.  $I \neq J$ .
- 5) Update  $n \leftarrow n - 1$ .
- 6) If  $n = N'$  go to step 7). Otherwise go to step 2).
- 7) Determine the representative days as the elements with minimum dissimilarity to the rest of elements in each cluster (medoid).
- 8) The number of days belonging to each cluster determines the weight factor of each representative day.

# How do the representative days approach work?

- As the figure below shows, using representative days works quite well



- Instead of 14 days (336 hours), we use 2 representative days (48 hours) to reduce the computational burden.



# And what about current power systems?

- Current power systems have new actors



Generators



Lines



Demand



Renewables

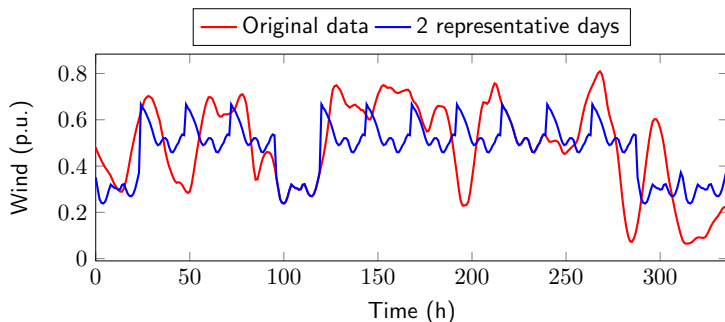


Storage

- Renewable generation is free and reduce CO2 emissions
- Renewable generation may happen at the wrong time
- Storage energy systems are the perfect partner of renewables:
  - If the wind blows and the demand is low, the battery stores energy
  - If the wind does not blow and the demand is high, we use the energy of the battery

# Can we still use representative days?

- Some renewables do not present a strong daily pattern



- The energy stored by some storage energy systems can be used several days later.

# What do we propose?

- Instead of using representative days, we propose a new clustering methodology to group **consecutive hours** and maintain chronology.
- By doing so we can capture the **longer dynamics** of power generation from renewable sources such as wind
- In addition, we can model the operation of the batteries more accurately since we maintain the **chronology** of the data

# How do I know if two consecutive hours are similar or not?

- Each hour is characterized by normalized demand, wind and solar

$$x_1 = \left[ \underbrace{0.4}_{\text{demand}}, \underbrace{0.1}_{\text{wind}}, \underbrace{0.2}_{\text{solar}} \right]$$

$$x_2 = \left[ \underbrace{0.6}_{\text{demand}}, \underbrace{0.4}_{\text{wind}}, \underbrace{0.3}_{\text{solar}} \right]$$

- The similarity between two consecutive hours is computed using a norm

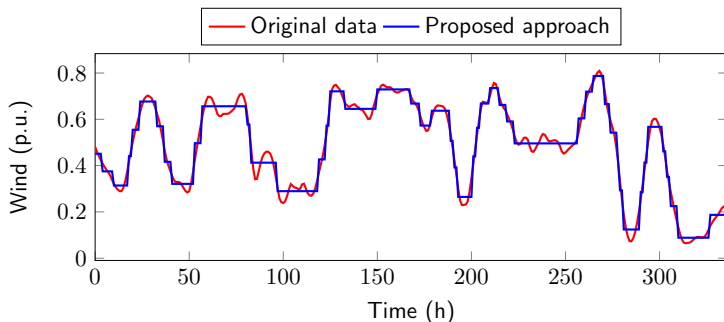
$$d(x_1, x_2) = \|x_1 - x_2\|_2$$

# How does the proposed clustering algorithm work?

- 1) Set the initial number of clusters  $n$  to the total number of hours  $N$ .
- 2) Determine the centroid of each cluster as  $\bar{\mathbf{x}}_I = \frac{1}{|I|} \sum_{i \in I} \mathbf{x}_i$
- 3) Compute the dissimilarity between each pair of adjacent clusters  $I, J$  according to Ward's method as  $D(I, J) = \frac{2|I||J|}{|I|+|J|} \|\bar{\mathbf{x}}_I - \bar{\mathbf{x}}_J\|^2$
- 4) Merge the two closest *adjacent* clusters  $(I', J')$  according to the dissimilarity matrix, i.e.,  $(I', J') \in \operatorname{argmin} D(I, J)$  s.t.  $J \in \mathcal{A}(I)$ , where  $\mathcal{A}(I)$  is the set of clusters adjacent to cluster  $I$ . Two clusters  $I$  and  $J$  are said to be adjacent if  $I$  contains an hour that is consecutive to an hour in  $J$ , or vice versa, according to the original time series.
- 5) Update  $n \leftarrow n - 1$ .
- 6) If  $n = N'$  go to step 7). Otherwise go to step 2).
- 7) Determine the representative periods as the clusters' centroids  $\bar{\mathbf{x}}_I$ .
- 8) The number of hours belonging to each cluster corresponds to the value of the time-period duration.

# Does the proposed clustering work?

- With only 48 time periods (2 days) we managed to represent the wind much better



# How does the aggregation affect the optimization model?

$$\min \sum_{gnt} \tau_t w_t c_g p_{gnt} + \sum_{nt} \tau_t w_t s c_n (\bar{d}_{nt} - d_{nt}) + \sum_{gn} \frac{i_g^G}{y_g^G} \bar{p}_{gn} + \sum_n \frac{i^H}{y^H} \bar{h}_n + \sum_{sn} \frac{i_s^S}{y_s^S} \bar{b}_{sn} + \sum_{nm} \frac{i^F l_{nm}}{y^F} \bar{f}_{nm}$$

s.t.

$$\sum_{g \in \mathcal{G}^{rnt}} \tau_t w_t p_{gnt} \geq \kappa \sum_{gnt} \tau_t w_t p_{gnt} \quad 0 \leq \bar{p}_{gn} \leq \hat{p}_{gn}, \quad \forall g \in \mathcal{G}^r, n$$

$$0 \leq \bar{h}_n \leq \hat{h}_n, \quad \forall n \quad 0 \leq \bar{f}_{nm} \leq \hat{f}_{nm}, \quad \forall n, m$$

$$\sum_g p_{gnt} + \sum_s (b_{snt}^- - b_{snt}^+) + h_{nt} = d_{nt} + \sum_m f_{nmt}, \quad \forall n, t$$

$$0 \leq p_{gnt} \leq \rho_{gnt} (\bar{p}_{gn}^0 + \bar{p}_{gn}), \quad \forall g, n, t$$

$$-r_g^- (\bar{p}_{gn}^0 + \bar{p}_{gn}) \leq p_{gnt} - p_{gnt-1} \leq r_g^+ (\bar{p}_{gn}^0 + \bar{p}_{gn}), \quad \forall g, n, t \notin T_1$$

$$0 \leq h_{nt} \leq \bar{h}_n^0 + \bar{h}_n, \quad \forall n, t$$

$$\sum_t \tau_t w_t h_{nt} \leq a_n \sum_t \tau_t w_t (\bar{h}_n^0 + \bar{h}_n), \quad \forall n$$

$$0 \leq b_{snt}^+ \leq \bar{b}_{sn}^0 + \bar{b}_{sn}, \quad \forall s, n, t \quad 0 \leq b_{snt}^- \leq \bar{b}_{sn}^0 + \bar{b}_{sn}, \quad \forall s, n, t$$

$$b_{snt} = b_{snt-1} - \tau_t b_{snt}^- + \tau_t \xi_s b_{snt}^+, \quad \forall s, n, t \notin T_1$$

$$0 \leq b_{snt} \leq \eta_s (\bar{b}_{sn}^0 + \bar{b}_{sn}), \quad \forall s, n, t$$

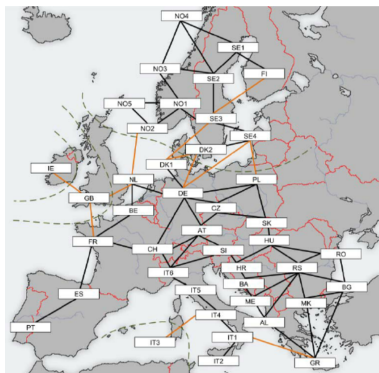
$$b_{snt} = b_{snt'}, \quad \forall s, n, (t, t') \in T_2$$

$$0 \leq d_{nt} \leq \bar{d}_{nt}, \quad \forall n, t$$

$$-\bar{f}_{nm}^0 - \bar{f}_{nm} \leq f_{nmt} \leq \bar{f}_{nm}^0 + \bar{f}_{nm}, \quad \forall n, m, t$$

# Have you tried in a realistic case study?

- Electric power system (28 countries) for 2030 (single target year)
- Investments in conventional and renewable generation, transmission lines and two storage technologies (intraday and interday).
- Greenfield approach (no initial capacities)
- Given renewable penetration target





# Have you tried in a realistic case study?

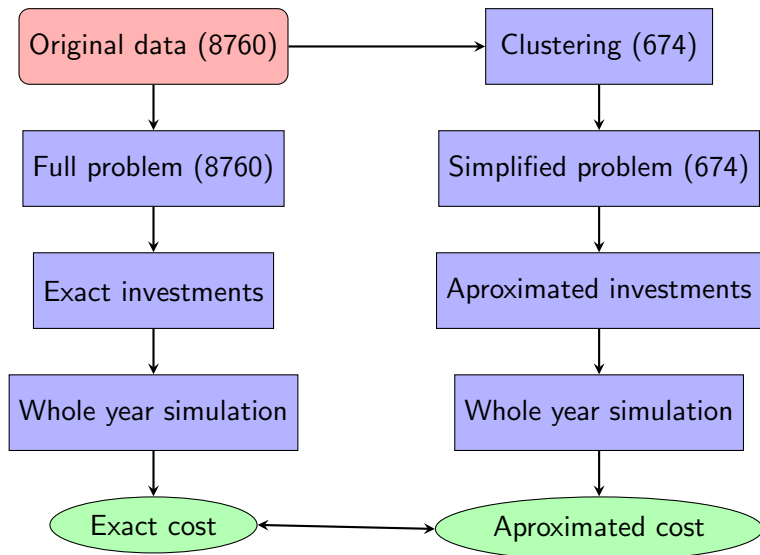
Table: Generation technology data

Technology	$i_g^G$ (€/MW)	$y_g^G$ (years)	$c_g$ (€/MWh)	$r_g^+/r_g^-$ (p.u.)
Base	$4 \cdot 10^6$	60	10	0.1
Peak	$1.5 \cdot 10^6$	40	40	1.0
Wind	$1.5 \cdot 10^6$	25	-	-
Solar	$1 \cdot 10^6$	25	-	-

Table: Storage technology data

Storage	$\eta_s$ (h)	$\xi_s$ (p.u.)	$i_s^S$ (€/MW)	$y_s$ (years)
intraday	6	0.8	$1.5 \cdot 10^6$	80
interday	48	0.7	$2 \cdot 10^6$	60

# What about the results?



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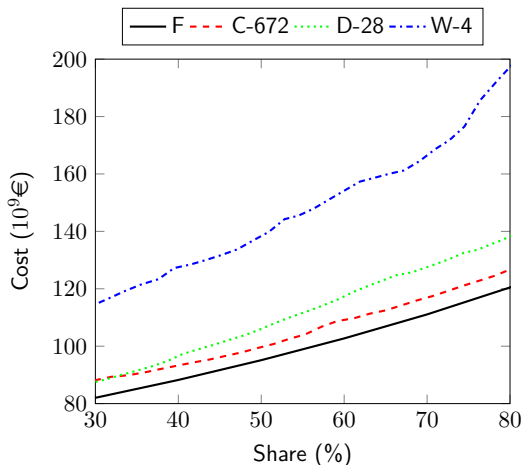
These are the investment results for a 50% renewable target

	F	C-672	D-28	W-4
Base (GW)	208	206	235	207
Peak (GW)	20	16	41	0
Wind (GW)	772	747	692	790
Solar (GW)	217	255	276	155
Hydro (GW)	160	160	160	160
Intraday (GW)	48	31	135	100
Interday (GW)	144	151	0	69
Network (GW)	23	18	34	19
Cost (10 <sup>9</sup> €)	95.13	99.31	102.17	133.72
Share (%)	50	49.5	46.1	47.1
Shed (%)	0	0.1	0.2	1.1
Spil (%)	2	3.3	3.4	3.3

- W-4 underinvest in peak, highest cost because of load shedding
- D-28 underinvest in wind+interday and overinvest in solar+intraday
- C-672 closest to full model, balance between intraday and interday storage

# What about the results?

We plot now the cost of the 4 approaches for different renewable targets



# What about the results?

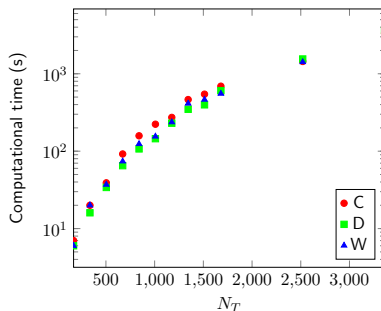
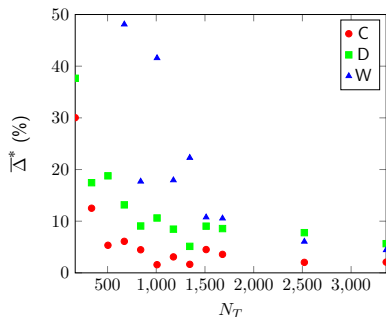
- Below we provide the average cost increase over all renewable penetration levels.

Approach	Number periods	Av. cost increase	Time
F	8760	0 %	~ 10 h
D-28	$28 \times 24 = 672$	13.1 %	~ 100 s
W-4	$4 \times 168 = 672$	48.1 %	~ 100 s
C-672	672	6.1 %	~ 100 s

- The proposed approach has the same computational burden as existing methodologies but reduces significantly the cost increase with respect to the benchmark model.

# What about the results?

We also compare the proposed approach with existing ones for different number of time periods



# What about the results?

Finally, we evaluate the proposed method in different scenarios

Scenario	C-672	D-28	W-4
Base	6.1%	13.1%	48.1%
No_solar	8.6%	18.3%	31.5%
No_wind	9.0%	7.2%	32.8%
No_hydro	2.3%	13.2%	60.3%
No_storage	11.1%	7.2%	6.3%

- If wind or storage investments are not possible, the performance of the proposed method is worse than the representative days

# Conclusions

- Existing models to reduce the computational burden of planning problems do not properly capture the mid-term dynamics of renewable generation and fail to model storage operation.
- We propose a new time-period clustering technique that retains the chronology of the time-dependent parameters throughout the whole planning horizon.
- The proposed method determines capacity expansion plans that take into account the economic value of using interday storage to handle prolonged periods of high or low renewable power generation.
- Numerical results show the superior performance of our method, which determines more efficient capacity expansion plans without increasing the computational burden.



# Thanks for the attention!

## Questions?



More info: [oasys.uma.es](http://oasys.uma.es)