Assignment 8 - Time series

June 29, 2019

0.1 Assignment 8

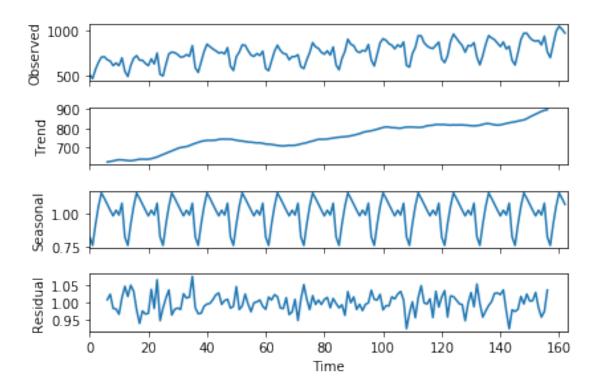
0.1.1 Problem

Using a suitable Python library, extrapolate the time series of the Paladini example over the next 6 months.

0.1.2 Resolution

We can extrapolate the decomposition through the python library *statsmodels*. In particoular we can use the function *seasonal_decompose()* in order to extract and print the 4 variables.

```
In [1]: from random import randrange
        import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        from statsmodels.tsa.seasonal import seasonal_decompose
        %matplotlib inline
In [2]: file = "Paladini Associates example.csv"
        data = open(file, "r")
        data = data.read()
        data = data.split(",")
        data = [float(d) for d in data]
        data = np.array(data)
In [3]: m = data.shape[0]
In [4]: pal = seasonal_decompose(data, model='multiplicative', freq=12)
        pal.plot()
        plt.show()
```



```
In [5]: M = 12
        T = data.shape[0]
        qvt = np.zeros(data.shape[0])
        for i in range(int(M/2),T-int(M/2)):
            tmp = 0
            tmp = data[i-6]/2
            tmp += data[i+6]/2
            for j in range(i-5,i+6):
                tmp += data[j]
            qvt[i] = tmp/M
In [6]: x = np.arange(qvt.shape[0])
        plt.figure(figsize=(15,7))
        plt.plot(x[int(M/2):T-int(M/2)], qvt[int(M/2):T-int(M/2)])
        plt.show()
```

```
900

850

750

700

0 20 40 60 80 100 120 140 160
```

In [7]: z = np.polyfit(x[int(M/2):T-int(M/2)], qvt[int(M/2):T-int(M/2)], 1)

```
In [8]: q = np.zeros(data.shape[0])
        q[int(M/2):T-int(M/2)] = z[0] * x[int(M/2):T-int(M/2)] + z[1]
In [9]: v = np.zeros(data.shape[0])
        v[int(M/2):T-int(M/2)] = qvt[int(M/2):T-int(M/2)] / q[int(M/2):T-int(M/2)]
In [10]: srt = np.zeros(data.shape[0])
         srt[int(M/2):T-int(M/2)] = data[int(M/2):T-int(M/2)]/qvt[int(M/2):T-int(M/2)]
In [11]: s = np.zeros(12)
         for i in range(12):
             count = 0
             for j in range(i+12,T-int(M/2)-1,12):
                 s[i] += srt[j]
                 count += 1
             s[i] = s[i]/count
In [12]: xx = v[149:157]
         yy=np.arange(xx.shape[0])
         zz = np.polyfit(yy, xx, 2)
In [13]: t = np.arange(xx.shape[0],xx.shape[0]+7)
         a = zz[0] * (t**2) + zz[1]*t + zz[2]
In [14]: t = np.arange(157,163)
         qt = z[0]*t+z[1]
In [15]: p = a[:6] * qt * s[1:7]
```

In [16]: print(pal.trend)

[nan		nan	nan	nan	nan
	nan	627.695	83333	630.23333333	632.94583333	636.50416667
639	.0125	638.137	5	636.32916667	634.9875	633.90833333
635	.80416667	638.516	66667	641.55	642.36666667	641.22916667
642	.075	644.7		648.375	653.45	659.51666667
665	.02916667	672.		678.06666667	683.55	690.43333333
696	.79166667	701.370	83333	704.1125	706.35833333	711.1125
717	.5	722.837	5	728.35	732.95833333	735.72916667
737	.8875	738.062	5	737.85833333	739.4625	742.72916667
744	.8	744.158	33333	744.45	744.30416667	741.53333333
738	.03333333	735.904	16667	734.5625	732.2	729.63333333
728	.58333333	726.570	83333	725.08333333	725.34583333	722.8375
719	.1625	718.345	83333	717.26666667	714.2625	712.36666667
710	.26666667	709.362	5	711.05416667	712.425	712.22083333
712	.80416667	715.662	5	719.62916667	722.72083333	726.075
731	.325	734.679	16667	738.9375	743.34166667	743.60416667
743	.72083333	744.916	66667	747.01666667	749.7875	752.2375
754	.075	755.387	5	756.29166667	758.21666667	761.075
764	.4	768.366	66667	772.04166667	777.90416667	782.075
784	.11666667	786.858	33333	790.475	794.90833333	799.225
803	.74583333	806.866	66667	805.64166667	802.725	802.4625
800	.59583333	799.837	5	803.25	805.7	805.81666667
805	.99166667	804.766	66667	803.89166667	804.65	807.5375
812	.55416667	813.662	5	815.4125	818.88333333	818.65
817	.97916667	818.416	66667	816.52083333	815.90833333	816.92916667
816	.2875	816.9		816.725	815.7625	814.625
812	7	812.029	16667	813.16666667	815.4125	819.11666667
823	.2875	823.579	16667	820.60416667	817.45416667	815.90833333
817	.22083333	820.837	5	824.1625	827.4	830.55
832	.85416667	836.675		839.825	842.30416667	848.77916667
857	.325	864.645	83333	871.73333333	879.05416667	885.90833333
890	.95416667	894.862	5	nan	nan	nan
	nan		nan	nan]	

In [17]: print(pal.seasonal)

```
[0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445 1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577 0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445 1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577 0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445 1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577 0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445 1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577 0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445 1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577 0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
```

```
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
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0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315 1.02505042 0.98307259 1.02505984 0.98940811 1.07755577
0.82382161 0.76156155 0.92124624 1.05494351 1.15456277 1.11418445
1.06953315]
```

In [18]: print(pal.resid)

```
Γ
       nan
                 nan
                            nan
                                       nan
                                                 nan
1.00827969 1.02396061 0.98323503 0.98167711 0.96655699 1.01391922
1.04688528 1.01761425 1.05002576 1.03214748 0.97896444 0.94011649
0.976082
           0.96699759 0.96925517 1.0380475 0.98315299 1.06571409
0.94823701 0.98408436 1.01312037 1.03631647 0.96413921 0.98092987
0.98437851 0.98047061 1.02543552 1.01317632 1.0158042 1.07560501
0.98507252 0.96793962 0.96929201 0.98936716 0.99584777 0.9976436
1.00853568 1.02231393 1.02772462 0.99480713 1.00587241 1.00961573
0.98406022 0.98915703 1.04602013 0.98011519 0.99045097 1.02450846
0.99568532 0.9738434 0.99961938 1.0020803 1.00757591 0.98947523
0.98065426 1.01596783 1.00744693 1.02281787 1.01705586 0.98449764
0.98261903 1.01417767 0.96549589 0.97319572 1.00942324 0.94856329
1.00953695 1.0517874 1.00987621 0.97990093 1.0200025 0.99476181
1.00725942 0.99457939 1.00912071 1.01481937 0.98497594 1.01195903
0.99740281 0.98489481 0.99382396 0.96334503 1.03151815 0.99967225
1.01632786 0.98030182 0.99516057 0.97705247 0.9951003 0.99913669
1.03558779 1.00931009 1.00750189 1.02367678 0.97912118 0.99121434
0.99029726 1.01660895 1.01067479 1.02442107 1.03226611 1.00768685
0.92489215 0.96956228 1.00213222 0.95643805 1.01439067 1.04860022
0.99931906 0.99590713 1.01076487 0.95723305 1.03244862 0.98714374
0.99667893 0.9941658 0.94793496 0.99839604 1.02898677 0.98799242
1.05328482 0.99760573 0.95824568 0.97602616 0.99161419 1.00294825
1.0264278 1.02780283 1.02291871 1.03659635 0.97604579 0.92488568
0.97906386 0.97450657 0.98081991 1.01764406 0.99620251 1.02443009
```

1.00464862 1.00540945 1.02919898 0.98503676 0.95832989 0.97484221 1.0359369 nan nan nan nan nan

In [19]: print(pal.observed)

[511.7 468.3 571.9 648.2 705.6 709.1 676.9 661.5 611.8 640.5 611.1 697.2 548.8 492.1 613.2 692.3 721.7 672. 670.6 635.6 611.8 686. 630.7 750.4 515.2 498.4 627.2 741.3 760.9 754.6 733.6 704.9 709.8 733.6 714.7 831.6 586.6 536.9 654.5 767.9 848.4 820.4 795.9 774.9 750.4 759.5 740.6 809.9 603.4 558.6 711.2 760.9 840. 835.8 777. 727.3 714. 744.8 723.1 770.7 581. 555.8 665.7 770.7 836.5 779.1 745.5 739.2 676.2 710.5 711.9 731.5 598.5 578.9 675.5 756. 865.2 819. 800.8 758.1 737.8 774.9 728. 817.6 618.1 565.6 691.6 768.6 903. 847.7 830.9 772.1 755.3 779.1 770. 844.2 671.3 607.6 737.8 863.1 908.6 891.1 853.3 836.5 797.3 840.7 816.9 872.2 613.9 595. 744.1 812. 941.5 940.1 863.1 829.5 808.5 800.1 836.5 870.8 684.6 644.7 721. 877.1 959.7 916.3 870.8 832.3 760.2 833.7 827.4 864.5 705.6 619.5 723.1 847.7 942.9 917. 897.4 859.6 821.8 872.2 795.9 824.6 669.9 618.1 756. 901.6 968.8 968.8 935.9 763.7 700. 921.2 891.1 882. 887.6 840. 844.2 989.1 1045.8 1012.9 970.9]