Analysis I Chapter 5 Exercises

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5.1 Cauchy Sequences

- 5.1.1 Let a_n be a cauchy sequence. By definintion a_n is 1-steady, hence $\exists \mathbb{N}$ such that $\forall i,j \geq \mathbb{N} \ | a_i a_j | \leq 1$. If we fix j then from the reverse triangle inequality we obtain $|a_i| |a_j| \leq 1$ which implies $|a_i| \leq 1 + |a_j|$, which shows a_i is bounded by $1 + |a_j| \ \forall i \geq N$. Consider all the terms before the index N of a_n , these make up a up a finite sequence which is bounded by $x = \max(\{a_k | k < N\})$. Let $M = \max(x, 1 + a_j)$ then $a_n \leq M \ \forall n$.
- 5.2 Equivalent Cauchy Sequences

5.2.1

5.3 The Construction of The Real Numbers

5.3.1

5.4 Ordering The Real Numbers

5.4.1

5.5 The Least Upper Bound Property

5.5.1

5.6 Real Exponentiation Part I

5.6.1