

## \* Communication

- \* It is transmission of information from one place to another.
- \* Voice  $\rightarrow$  300Hz to 3.5kHz eg. Telephone
- Audio  $\rightarrow$  20Hz to 20kHz eg. Radio.
- Video  $\rightarrow$  0 to 4.5MHz TV.

\* Modulator converts low frequency signal into high frequency signal as freq<sup>n</sup>  $\propto$   $\lambda$  &  $\lambda \propto$  length of antenna  $\propto$   $c/f$ .

$$\therefore \lambda = \frac{c}{f}$$

\* modulator used to

① To Reduce size of antenna

② Multiplexing

③ To reduce effect of noise ( $\because S/N > 1$  is cond<sup>n</sup> to have good transmission)

\* Bandwidth of signal should as low as possible. & B.W. of channel should be high for multiplexing.

\* To reduce the BW of signal insignificant frequencies should be eliminated  $\therefore$  max energy (i.e. 99%) is concentrated in first three lobe of the spectrum.

$\therefore$  we use LPF to have low frequencies having main lobe. B.W. =  $(\pm) f_Hz$ .

practical bandwidth of rectangular pulse is inversely proportional to pulse width.

$\therefore$  B.W.  $\propto$  Pulse width decreases.

Modulation property is nothing but frequency shifting property of signal.

$$g(t) \cos 2\pi f_c t \rightarrow g(t-f_c) + g(t+f_c)$$

↓                      ↑  
Carrier signal      Carrier frequency

Carrier is very high frequency signal FM  $\rightarrow$  88MHz - 108MHz  
Radio - GHz

- \* If a signal is multiplied by ~~west~~ carrier the signal is shifted to the left side & right side by  $f_c$  & the amplitude become half.
- \* hence modulat<sup>n</sup> is nothing but frequency translation ! Signal with low frequency range is translated to high freq range.

$$1 \cdot \cos(2\pi f_c t) \longleftrightarrow \frac{\delta(f-f_c) + \delta(f+f_c)}{2}$$

~~+1~~ ~~-1~~

### \* Concept of modulation & demodulation

\* At transmitter side

$$\text{(original signal)} m(t) \longleftrightarrow \text{Tx spectrum } \left[ -w, w \right] \text{ done freq. } \therefore \text{problem with antenna while transmitting } m(t).$$

$\downarrow \times \cos(2\pi f_c t)$  Tx modulation to remediate Antenna problem.

$$s(t) = m(t) \cos(2\pi f_c t) \longleftrightarrow \text{Tx spectrum } \left[ -f_c, f_c \right]$$

$m(t)$   $\boxed{\text{mod}}$   $s(t)$   $\therefore$  Now we can transmit.

$\oplus c(t) = \cos(2\pi f_c t)$

\* At receiver side.

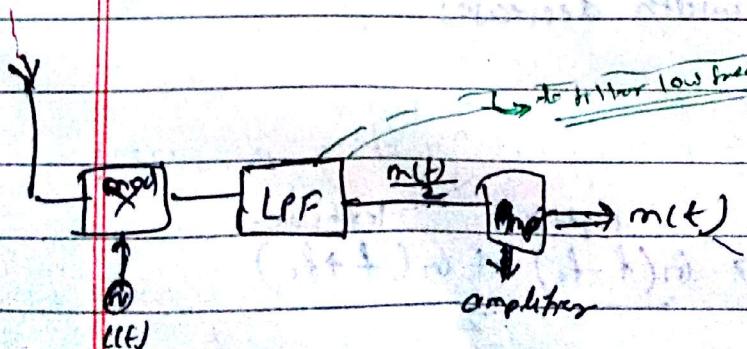
$$s(t) = m(t) \cos 2\pi f_c t \longleftrightarrow \text{Rx spectrum } \left[ -f_c, f_c \right]$$

$\downarrow \times \cos 2\pi f_c t$  Rx modulation (We have spectrum to, will do again shifting of spectrum in bottom stage)  $\therefore$  original eliminate

$$m(t) \cos^2 2\pi f_c t$$

$$= \frac{m(t)}{2} + \frac{m(t)}{2} \cos 4\pi f_c t$$

$\therefore$  eliminate  $\frac{m(t)}{2} \cos 4\pi f_c t$  through L.P.F.  $\therefore$  get  $\frac{m(t)}{2}$  back.





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\* ∵ In modulation characteristic parameters of a carrier is varied according to msg signal.

3 parameter can vary (1) amplitude (2) freqn. (3) phase.

- 1) Amplitude modulation      2) Frequency modulation      3) Phase modulation
- ↓
- ① AM                                  ① N.B.F.M.                                  ① N.B.P.M.
- ② DSB                                  ② W.B.P.M.                                          ② W.B.P.M.
- ③ SSB
- ④ VSB

Carrier Signal.  $\rightarrow C(t) = A_c \cos(2\pi f_c t + \phi_m)$

↓                                          ↓                                          ↓  
Am                                          FM                                          P.M.

## \* Amplitude Modulation

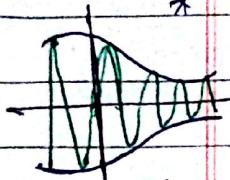
\* Peak amplitude of the carrier is varied according to msg signal.

↑  
amplitude sensitivity.

\* time domain eqn of AM  $s(t) = A_c \cos(2\pi f_c t) + A_c K_a m(t) \cos(2\pi f_c t)$

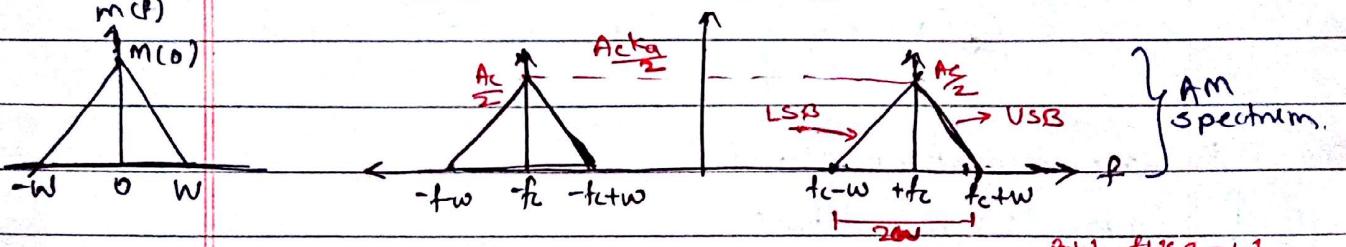
$$\text{standard form} \Rightarrow s(t) = [A_c [1 + K_a m(t)]] \cos(2\pi f_c t)$$

Peak amplitude before of carrier Peak amplitude after modulation



\* Modulated signal in frequency domain

$$S(f) = \frac{A_c}{2} [\delta(f-f_c) + \delta(f+f_c)] + \frac{A_c}{2} K_a [M(f-f_c) + M(f+f_c)]$$



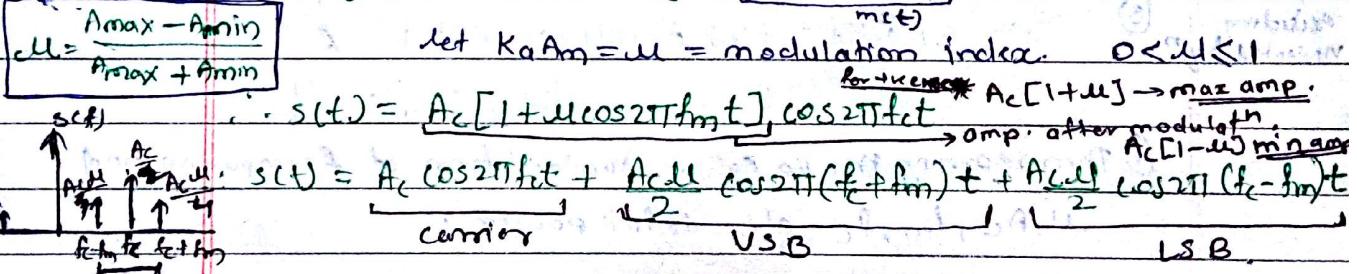
$$\text{B.W.} = 2w \text{ or } 2 \times \text{highest frequency of } m(t) \quad \text{B.W. of LSB} = w.$$

\* AM consists of carrier freq (c), USB frequency & LSB freq (freq.)

\* Singletone Modulation of AM. (i.e.  $m(t)$  has only one frequency)

~~AM~~  $\rightarrow$  the msg signal is sinusoidal signal : only one (single) frequency

$$\therefore s(t) = A_c \cos 2\pi f_c t + A_c K_a A_m \cos 2\pi f_m t \cos 2\pi f_c t$$



\* Power Calculations  $P = I^2 R$  or  $V^2 / R$ .

$$\text{if } R \text{ not given, take } R=1 \quad \therefore V_{rms} = \frac{A_c}{\sqrt{2}} \quad \therefore P_c = \frac{A_c^2}{2R} \quad P_{USB} = \frac{A_c^2 u^2}{8R}, \quad P_{LSB} = \frac{A_c^2 (1-u)^2}{8R}$$

$$P_t = P_c + P_{USB} + P_{LSB} = P_c \left[ 1 + \frac{u^2}{2} \right] \Rightarrow \frac{P_c u^2}{2} \text{ is SB power}$$

$$\eta = \frac{P_{SB}}{P_t} = \frac{\text{sideband power}}{\text{total power}} = \frac{u^2}{2+u^2}$$

$$V_{max} = A_c [1+u] \quad u = \frac{V_{max}-V_{min}}{V_{max}+V_{min}} \quad \frac{V_{max}}{V_{min}} = \frac{1+u}{1-u}$$

$$\text{antenna current after modulation} \quad I_t = I_c \sqrt{1 + \frac{u^2}{2}}$$

$\therefore u$  is not given in problem take  $u = \frac{A_m}{A_c}$

\* carrier is not modulated means  $u=0$   $P_c = P_t$  antenna current after modulation

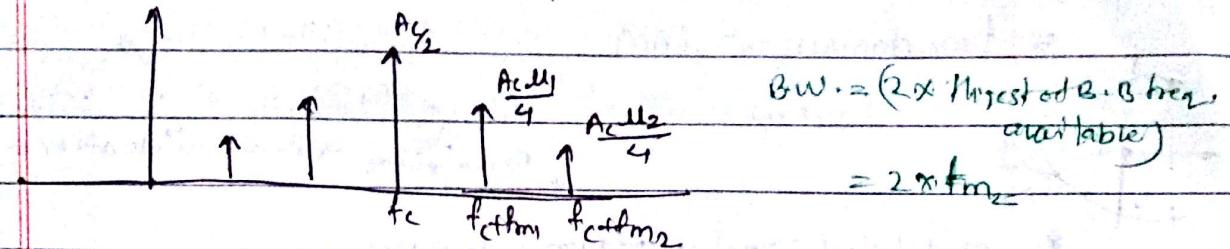
\* when  $u$  changes from 0 to 1 power increased by 50% of  $P_c$

\* Multitone modulation: (m(t) contains more than one frequency)

$$m(t) = A_m_1 \cos 2\pi f_{m_1} t + A_m_2 \cos f_{m_2} t.$$

$$s(t) = A_c [1 + u_1 \cos 2\pi f_{m_1} t + u_2 \cos 2\pi f_{m_2} t] \cos 2\pi f_c t$$

$$K_a A_m_1 = u_1, \quad K_a A_m_2 = u_2.$$



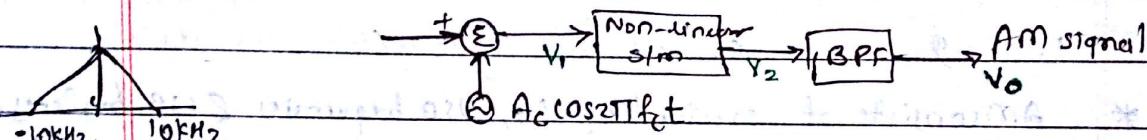
$$u_t = \sqrt{u_1^2 + u_2^2}$$

$$\therefore P_t = P_c \left[ 1 + \frac{u_t^2}{2} \right]$$

$$P_t = P_c + P_{u_1 u_2} + P_{s.s.b.}$$

\* Generation of AM signal.

① Square law modulator:-



$$\text{mod o/p } ① \quad v_1 = [m(t) + A_c \cos 2\pi f_c t]$$

$$\text{Non lin. o/p } ② \quad v_2 = a v_1 + b v_1^2 \quad \rightarrow \text{This contain All the term but we have terms of } m(t) \text{ only to BPF is used to attenuate high freq. range (problem) excluding unwanted by n.}$$

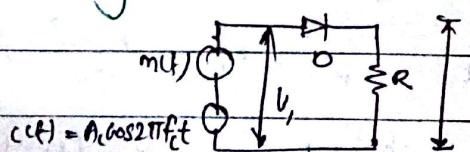
$$\therefore v_2 = a A_c \cos 2\pi f_c t + 2b A_c m(t) \cos 2\pi f_c t$$

$$\text{* amp. sensitivity (Samp)} = \frac{2b}{a}$$

③ Then rearrang the v\_o eqn in standard form & comparing find

$A_c, f_m, f_c$  etc. to find power.

② Switching modulator:-



$$v_1 = m(t) + A_c \cos 2\pi f_c t$$

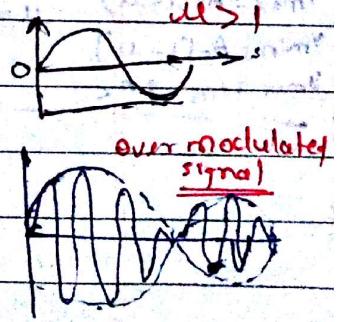
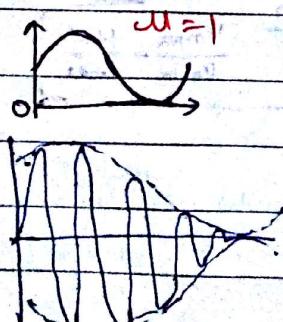
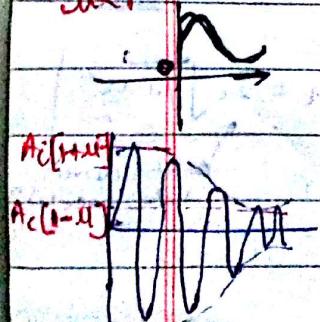
$$v_2(t) = v_1(t) \quad \text{for } c(t) > 0.$$

$$= 0 \quad \text{for } c(t) < 0.$$

$$\text{(Passing } v_2(t) \text{ through BPF)} \Rightarrow v_2(t) = \frac{A_c}{2} \cos(2\pi f_c t) + \frac{2}{\pi} m(t) \cos 2\pi f_c t$$

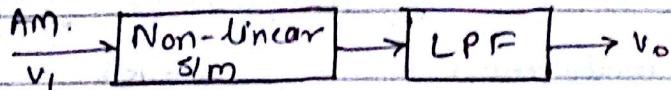
center freq.  $f_c$   
B.W.  $2\omega_b$

$M < 1$



## \* Demodulation of AM Signal.

(1) Square law modulator:- (used for  $M \leq 1$ ) (can not detect over modulated signal)



$$V_1 = A_c \cos 2\pi f_c t + A_s k_m(t) \cos 2\pi f_m t$$

$$V_2 = aV_1 + bV_1^2 \quad \text{then } V_2 \text{ passed through LPF to select desired frequency}$$

$$\therefore \text{Now } V_0 = \underbrace{b A_c^2 k_m(t)}_{\text{Signal component}} + \underbrace{\frac{b A_s^2 k_m^2(t)}{2} m^2(t)}_{\text{noise component}} \quad \because \text{output LPF consists of } m(t) \text{ & } m^2(t) \text{ components}$$

$m^2(t)$  causes interference with  $m(t)$ .

$$\frac{\text{Signal component}}{\text{Noise component}} = \frac{S}{N} = \frac{2}{k_m(t)}$$

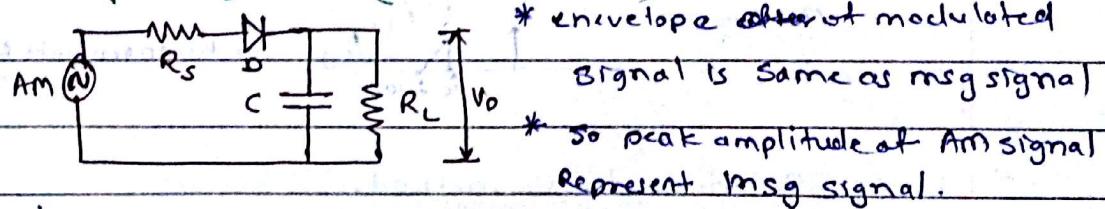
$$\text{if } \frac{S}{N} = \frac{2}{k_m(t)} < 1 \quad \text{demodulation not possible}$$

$$\therefore \frac{S}{N} > 1 \Rightarrow \frac{2}{k_m(t) A_m \cos 2\pi f_m t} > 1$$

$$\therefore \left(\frac{S}{N}\right)_{\min} = \frac{2}{k_m(t) A_m} = \frac{2}{M} \quad \text{if } M=10 \quad \frac{S}{N}=0.2 \\ \text{if } M=0.1 \quad \frac{S}{N}=20$$

$\therefore M$  should be  $<$  than 1 so that  $S/N$  is high.

(2) Envelope detector (used for  $M \leq 1$ ) (can not detect over modulated sig)



$$\text{i/p: } 10 \cos 2\pi f_c t \quad \text{o/p: } V_0 = 10$$

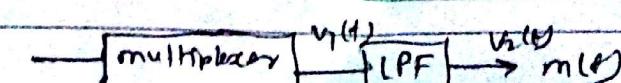
$$A_c \cos 2\pi f_m t \quad V_0 = A_c$$

$$e^t \cos 2\pi f_m t \quad V_0 = e^t$$

$$A_c \cos 2\pi f_c t + B_s \sin 2\pi f_m t \quad V_0 = \sqrt{A_c^2 + B_s^2}$$

$$\therefore A_c [1 + k_m(t)] \cos 2\pi f_m t \quad \boxed{V_0 = A_c [1 + k_m(t)]} \quad \begin{array}{l} \text{as demodulator} \\ \text{not consider DC component} \end{array} \\ \therefore V_0 = A_c k_m(t)$$

(3) Synchronous Detector



(For synchronous detector modulation oscillator  $m(t) = A_c^2 [k_m(t)]^2$ )  
efficiency is 100% but complexity is very high)

## → Single side band (SSB)

\* Only USB or LSB is transmitted.

\* for single tone modulation  $m(t) = A_m \cos 2\pi f_m t$ .

$$\text{time domain eqn} \Rightarrow \frac{A_c A_m}{2} \cos 2\pi (f_c + f_m)t \xrightarrow{\text{+ } \rightarrow \text{USB}} \quad \xrightarrow{- } \text{LSB}.$$

\* for multitone modulation

$$\text{time domain eqn} \Rightarrow \frac{A_c}{2} m(t) \cos 2\pi f_c t + \frac{A_c}{2} \hat{m}(t) \cos 2\pi f_c t$$

$\hat{m}(t)$  is hilbert transform of  $m(t)$  which gives  $90^\circ$  phase shift

### Power

$$\begin{array}{c} \text{LSB power} \\ \frac{A_c^2 A_m^2}{8R} \end{array} \quad \begin{array}{c} \text{USB power} \\ \frac{A_c^2 A_m^2}{8R} \end{array}$$

$$\text{Total power in DSB} = \frac{A_c^2 A_m^2}{8R} + \frac{A_c^2 A_m^2}{8R}$$

Total power in SSB = LSB power or USB power.

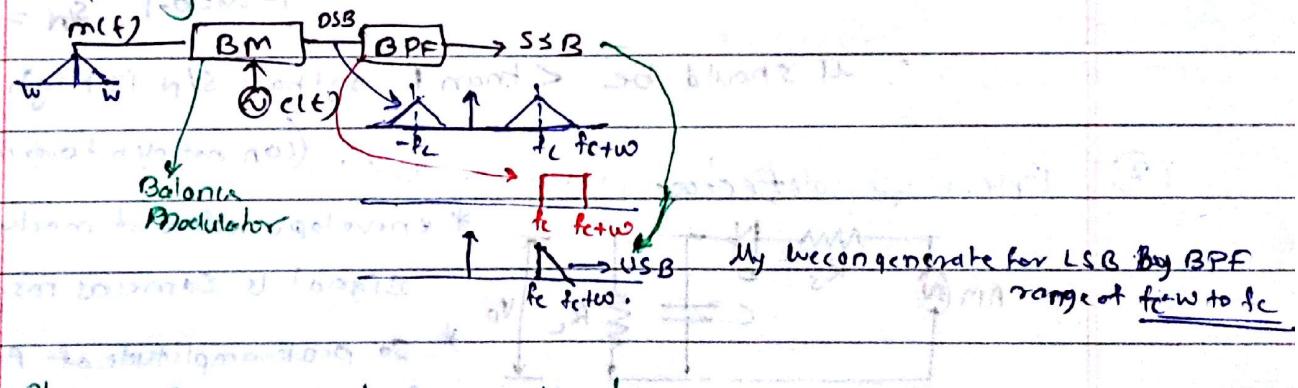
In SSB BW & PW is reduced by 50% compared to DSB

$$\% \text{ power saving in DSB} = \frac{2}{2+\mu^2} \times 100 = \frac{\text{Power saved in DSB}}{P_t} \quad \text{around 50\%}$$

$$\text{--- " ---} \quad \text{SSB} = \frac{1 + \mu^2/4}{1 + \mu^2/2} \times 100 = \frac{\text{Power saved in SSB}}{P_t} \quad \text{around 90\%}$$

## \* Generation of SSB signal.

### ① Frequency Discrimination method:-



### ② Phase Discrimination method.

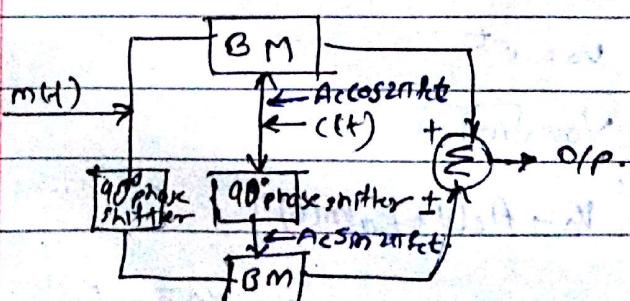
We know time domain  $\xrightarrow{\text{eqn of SSB}} \frac{A_c A_m(t) \cos 2\pi f_c t + \frac{A_c}{2} \hat{m}(t) \sin 2\pi f_c t}$

it's multiplication at carrier

(msg signal) by [BM] back

it is multiplication at carrier

signal and msg signal) with one shifted by  $90^\circ$  phase shift.



This method is complex

as compared to first method.

## \* Demodulation of SSB

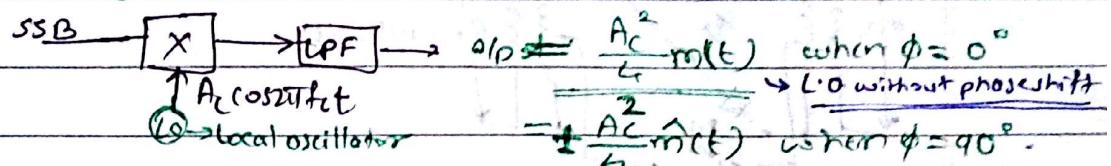
\* Envelope detector ~~(X)~~  $\xrightarrow{\text{SSB}} \boxed{\text{ED}} \rightarrow \text{O/P}$

$$\text{O/P of envelope D.} = \sqrt{\left[\frac{A_c}{2} m(t)\right]^2 + \left[\frac{A_c}{2} \hat{m}(t)\right]^2}$$

$$\text{If } m(t) = \cos 2\pi f_m t \Rightarrow \text{O/P} = \frac{A_c}{2} \sqrt{\cos^2 2\pi f_m t + \sin^2 2\pi f_m t} = \frac{A_c}{2}$$

$\Rightarrow$  O/P is constant  $\therefore$  Envelope detector cannot used to demodulate of DSB & SSB signal  $\therefore$  only Synchronous modulator is the option

### ① Synchronous Modulation



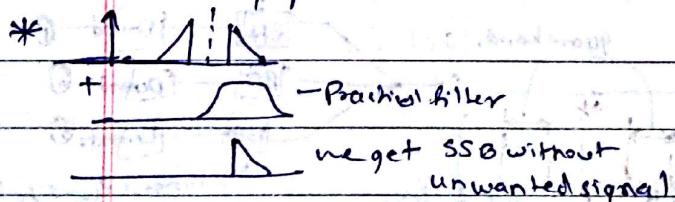
$$\text{O/P} = \frac{A_c^2}{4} m(t) \cos \phi \pm \frac{A_c^2}{4} \hat{m}(t) \sin \phi \Rightarrow \text{if } \phi \text{ is not } 0^\circ \text{ or } 90^\circ \\ \text{i.e. L.O. has some phase shift}$$

Advantages of SSB - BW  $\downarrow$  by 50% ; power  $\downarrow$  by 50% compared to DSB.  
No quadrature Null effect.

Dis-adv. of SSB - since filters are used (No practical filter has sharp cut-off. Cicular filter not possible)  $\therefore$  Not possible to suppress side band which is not required.

\*  $\therefore$  SSB modulat<sup>n</sup> is suitable only for the transmission of voice only.

\* there is gap of 600Hz bet<sup>n</sup> USB & LSB in voice signal spectrum



## \* Double Sideband (DSB)

\* both sidebands are transmitted (SB & VSB).

single tone modulat<sup>n</sup> DSB-SC.

$$s(t) = \frac{A_c A_m}{2} [\cos 2\pi(f_c - f_m)t + \cos 2\pi(f_c + f_m)t]$$

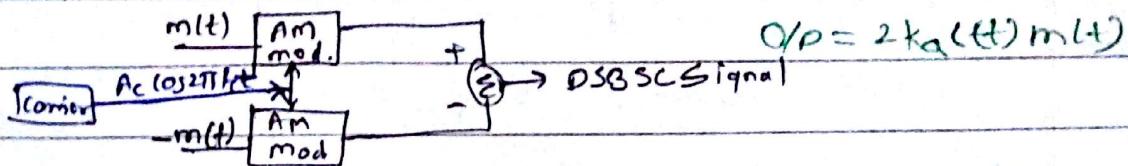
$$\begin{aligned} s(t) &= \frac{A_c A_m}{4} [\delta(t - f_c + f_m) + \delta(t + f_c - f_m)] + \frac{A_c A_m}{4} [\delta(t - f_c - f_m) + \delta(t + f_c + f_m)] \end{aligned}$$

$$\text{BW} = 2f_m$$

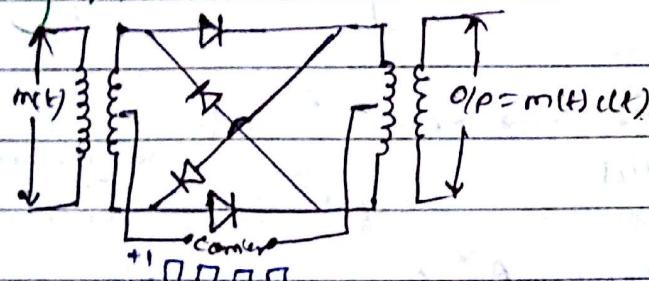
$$\text{Power} = \frac{A_c^2 A_m^2}{4} \quad P_{\text{DSB}} = P_{\text{LSB}}$$

## \* Generation of DSB-SC signal

### (1) Balance modulator

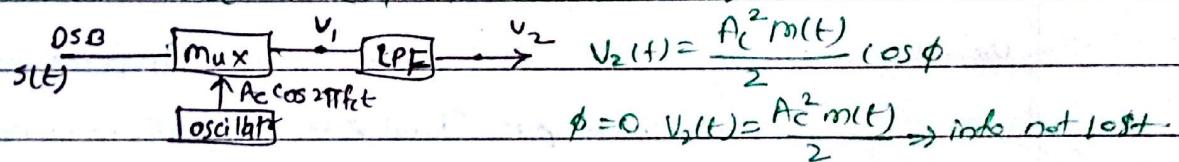


### (2) Ring modulator.



## \* Demodulation of DSB-SC signal

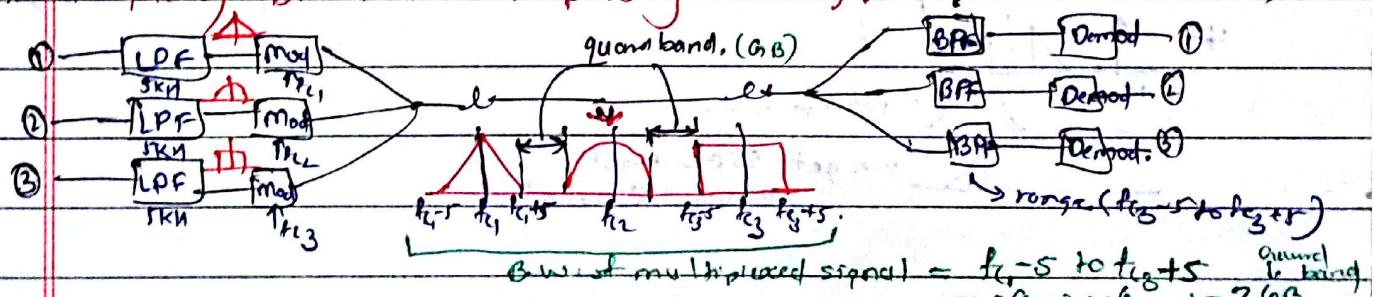
coherent detection : (synchronous detection)



$$\phi = 90^\circ \quad V_2(t) = 0 \Rightarrow \text{info totally lost}$$

\* Quadrature null effect.

## \* Frequency Division Multiplexing (FDM)



\* Carrier freq'nies carefully selected to avoid interference of signals.

\* For multiplexing B\_w. of the channel should be as high as possible.

\* B\_w. of the signal is as low as possible to have multiplexing.

\* here 3 signal passed through one channel.

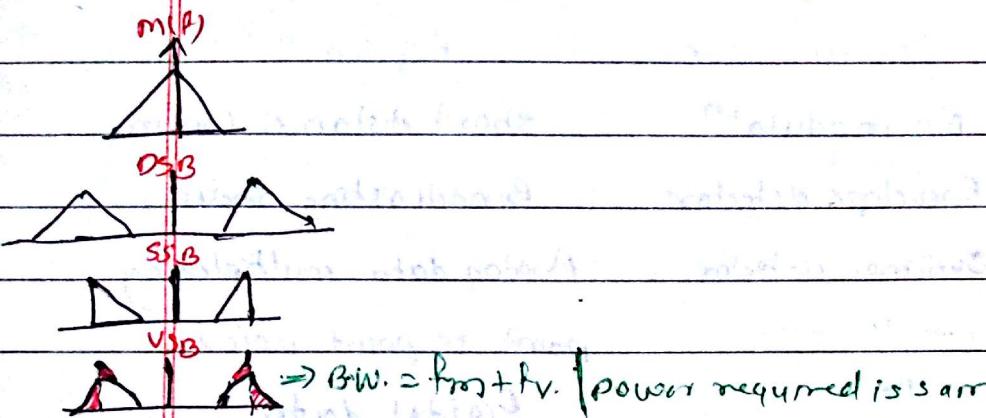
twisted pair cable.  $\rightarrow 500\text{kHz} \rightarrow$  telephone comm.

coaxial cable.  $\rightarrow 500\text{MHz} \rightarrow$  TV transmission (require 4.5MHz)

fiber optical cables  $\rightarrow$  in range of GHz  $\rightarrow$

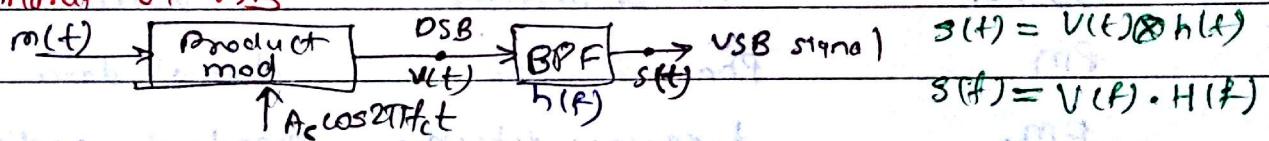
## \* Vestigial Sideband (VSB) modulation

- Used in transmission of video signal. (∴ significant range is up to  $4-5 \text{ MHz}$ )
- AM & DSB not used ∵ BW is  $9 \text{ MHz}$ . ∴ multiplexing is not possible
- SSB used only for voice.
- ∴ VSB is used for video trans.



$\Rightarrow \text{BW} = f_m + f_v$  (power required is same as SSB (ideal))

## \* Generation of VSB

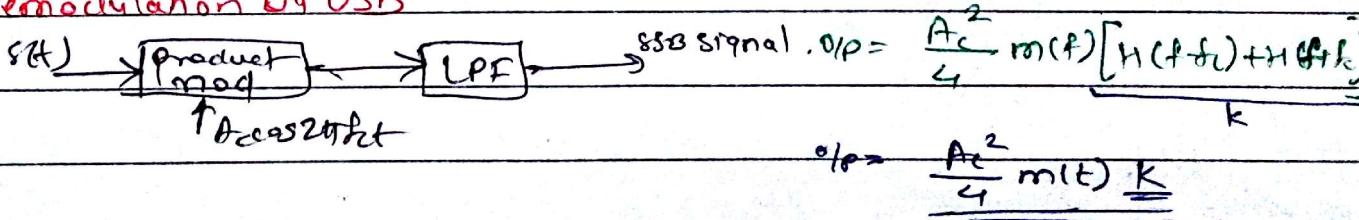


Time domain eqn of VSB  $s(t) = \frac{A_c}{2} [m(t) \cos 2\pi f_c t - m_s(t) \sin 2\pi f_c t]$

$m_s(t) \Rightarrow 0$  if filter width is  $\ll m(t)$

Filter has  $H_S(f) = \frac{1}{2} [H(f-f_c) + H(f+f_c)]$

## \* Demodulation of VSB



\* figure of merit of DSB signal = 1

\*  $\rightarrow$  FOM SSB signal = 1

\*  $\rightarrow$  FOM Noise in AM =  $\frac{4I^2}{2fRL^2} = N$  [modulation efficiency]

Name	Detection process	Applicat'n.
Baseband	No modulat'n	short distance comm.
AM	Envelope detector	Broadcasting radio.
DSB-SC	Synchr. Detector	Analog data, multiplexing
SSB-SC	— " —	point to point voice
VSB-SC	— " —	Digital data.
SSB-PC.	Envelope Detector	T.V. video.
PM	Phase detector	Digital data.
FM.	Frequency detector	Broadcasting radio, Microwave relay satellite system.

## \* Angle modulation

Angle of ~~carrier signal~~ (eighth frequency or phase) is varied according msg signal.

1) Frequency Modulation (FM)

2) Phase modulation (PM)

$$* \theta = \omega t = 2\pi f t \Rightarrow \frac{d\theta}{dt} = 2\pi f \Rightarrow f = \frac{1}{2\pi} \frac{d\theta}{dt} \Rightarrow \theta(t) = \frac{1}{2\pi} \int P_i d\theta.$$

$$\theta(t) = 2\pi f_c t + 2\pi k_f \int m(t) dt$$

$$* s(t) = A_c \cos [2\pi f_c t + 2\pi k_f \int m(t) dt] \Rightarrow \text{FM signal}$$

$\hookrightarrow$  frequency sensitivity. carrier swing =  $2\Delta f$   
 $\Delta f = k_f A_m = \text{freq deviation}$

$$* s(t) = A_c \cos [2\pi f_c t + k_p m(t)] \Rightarrow \text{PM signal}$$

$\hookrightarrow$  phase sensitivity.

[for single tone  $m(t) = A_m \cos 2\pi f_m t$ ]  $k_p A_m \rightarrow$  phase deviation]

\* FM in case of single tone modulation  $m(t) = A_m \cos 2\pi f_m t$

$$s(t) = A_c \cos \left[ 2\pi f_c t + \frac{k_f A_m}{f_m} \sin 2\pi f_m t \right].$$

$\therefore \beta = \frac{k_f A_m}{f_m} \rightarrow$  modulation index.

$\beta = \frac{\Delta f}{f_m} \rightarrow$  frequency deviation =  $\pm$  change in msg frequency.

①  $\beta \ll 1$ , Nano Band FM (NBFM)

②  $\beta \gg 1$ , Wide Band FM (WBFM).

$$f_i = f_c + k_f m(t) \quad f_i - \text{instantaneous frequency.}$$

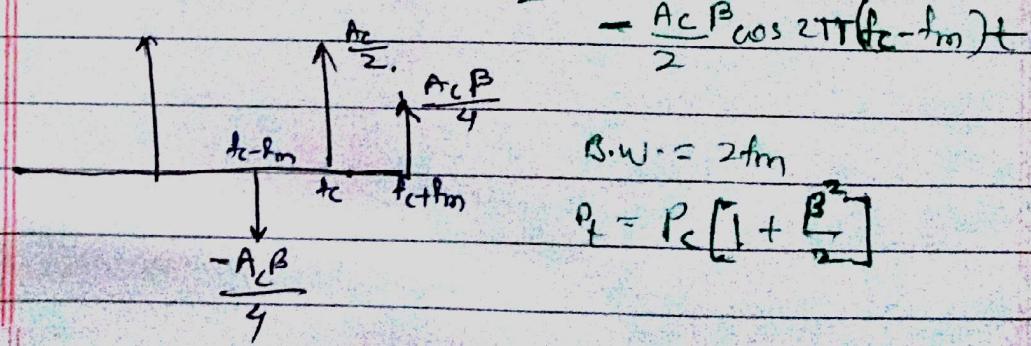
$k_f$  → indicates change in carrier frequency per volt

FM ~~actually~~ can be considered as voltage to freq. converter i.e. voltage variation to freq. variation. as value  $m(t)$  varies  $f$  at carrier  $f_c$  for max voltage  $f_{\max}$  i.e.  $t_{\max}$  & for minimum  $f_{\min}$ .

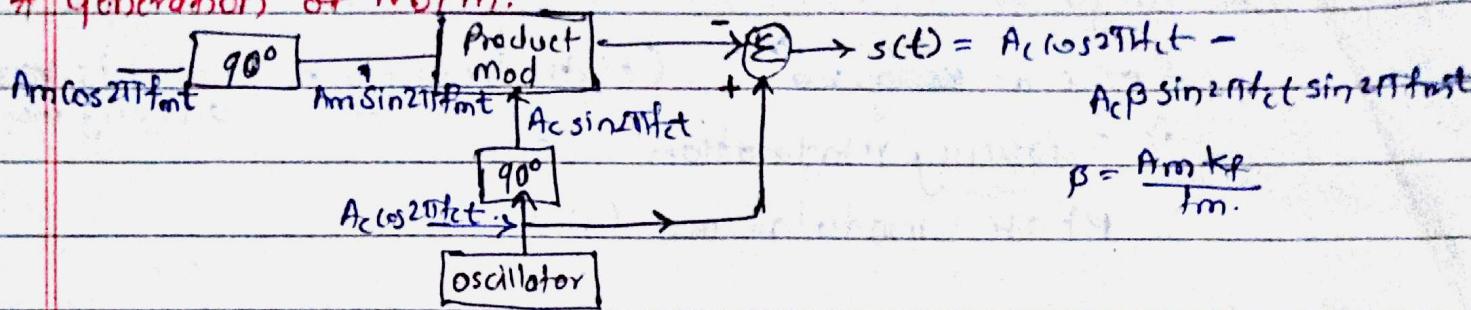
$$f_{\max} = f_c + \Delta f \quad f_{\min} = f_c - \Delta f$$

\* NBFM ( $\beta \ll 1$ )  $\therefore s(t) = A_c \cos 2\pi f_c t - A_c \beta \sin 2\pi f_c t \sin 2\pi f_m t.$

$$s(t) = A_c \cos 2\pi f_c t + A_c \beta \cos 2\pi (f_c + f_m) t - \frac{A_c \beta}{2} \cos 2\pi (f_c - f_m) t$$

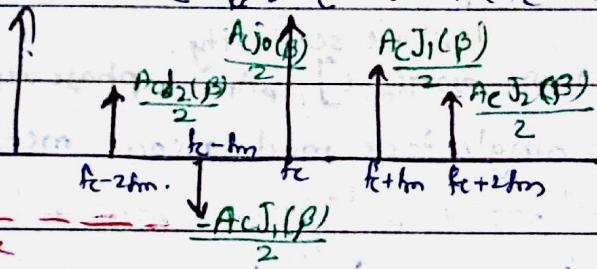


## \* generation of NBFM.



\* WideBand FM (WBFM).  $s(t) = A_c \operatorname{Re} \sum_{n=-\infty}^{\infty} J_n(\beta) \cos [2\pi(f_c + n f_m) t]$

$$\therefore s(t) = A_c J_0(\beta) \cos 2\pi f_c t + A_c J_1(\beta) [\cos 2\pi(f_c + f_m) t - \cos 2\pi(f_c - f_m) t] \\ + A_c J_2(\beta) [\cos 2\pi(f_c + 2f_m) t + \cos 2\pi(f_c - 2f_m) t]$$



Theoretical BW =  $\infty$

Practical by Carson's rule

$$BW = 2(\beta + 1)f_m \quad \beta = \frac{\Delta f}{f_m}$$

$$= 2\Delta f + 2f_m$$

\* (only consider up to  $\beta = 2$ )  $\therefore BW \approx 6f_m$

Properties:-

- WB FM spectrum consist of carrier & infinite number of sidebands separated by  $f_m$ .
- amplitude of the sideband depend on Bessel  $J^n$  coefficient  $J_n(\beta)$  which decreases as  $n \rightarrow \infty$ .

→ WB FM spectrum amp. depends on  $J_0(\beta)$  hence, modulation index  $\beta$ .

$$P_{\text{total}} = \frac{A_c^2}{2} \left( \sum_{n=-\infty}^{\infty} J_n^2(\beta) \right) = P_c \quad P_{f_c} = P_{\text{carrier}} = \frac{A_c^2}{2} J_0^2(\beta)$$

$$\therefore P_t = \frac{A_c^2}{2} = P_c \quad P_{f_c + f_m} = P_{f_c - f_m} = \frac{A_c^2 J_1^2(\beta)}{2}$$

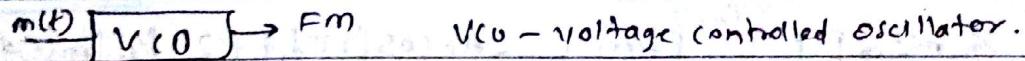
$$\text{Bessel } J^n \quad J_n(\beta) = \frac{1}{2\pi} \int_{-\pi}^{\pi} e^{j(n \sin \theta - n\theta)} d\theta.$$

$$\textcircled{1} \quad J_n(x) = (-1)^n J_{-n}(x)$$

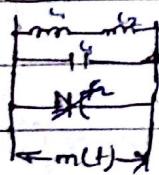
$$\textcircled{2} \quad \sum_{n=0}^{\infty} J_n^2(x) = 1$$

## \* Generation of WBFM.

### ① Direct Method.



VCO - voltage controlled oscillator.



$$\text{freq. of oscillation} = \frac{1}{2\pi\sqrt{L_1 L_2 (C + C_v)}}$$

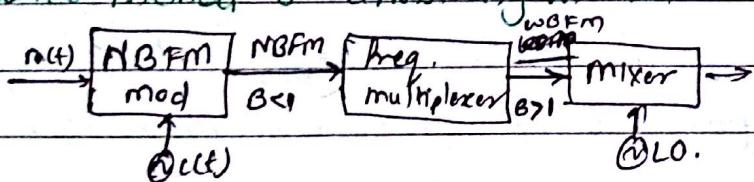
$C_v$  - varactor diode used as voltage variable caps.

When  $m(t)$  is ip, capacitance of  $C_v$  changes & hence o/p signal freq. changes.

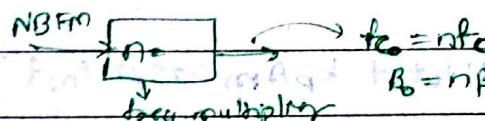
\* This method is used in short distance communicatn.)

$$f_i = f_c + k_f m(t)$$

### ② Indirect method or Armstrong method.

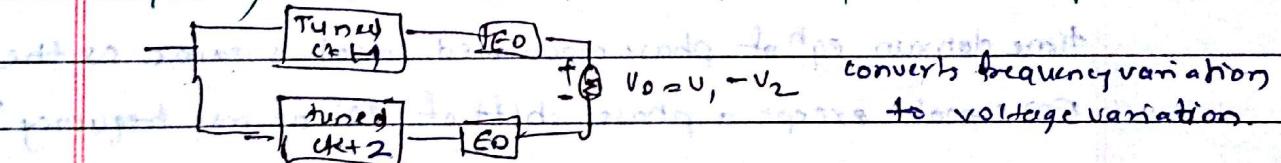


\* square law device multiply frequency by 2



## \* Demodulation of WBFM.

### ① Frequency discrimination method. using balance slope detector



i) when  $f_i = f_c$  as we know  $f_i = f_c + k_f m(t)$

$$\therefore m(t) = 0 \quad \therefore \text{voltage } m(t) = 0.$$

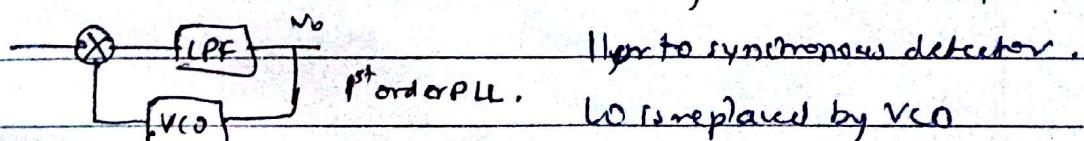
ii) when  $f_i > f_c$   $v_o > 0$   $m(t)$  should greater than 0

iii)  $f_i < f_c$   $v_o < 0$   $m(t)$  should be less than 0.

Resonant frequency of tuned circuit  $CK1 = f_r_1 > f_c + \Delta f$

$$\text{tuned } CK2 = f_r_2 < f_c + \Delta f.$$

### ② Phase Discrimination method using Phase lock loop (PLL)



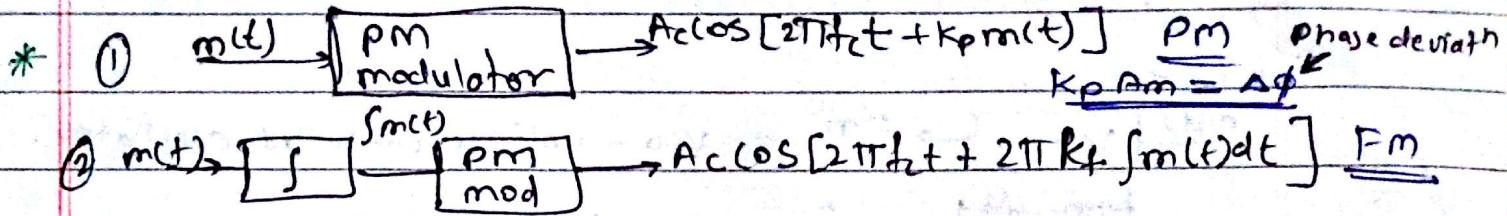
when ip to PLL  $\cos(2\pi f t + \phi)$   $v_o \propto \frac{d}{dt} [\phi]$

when ip to PLL is FM  $A_c \cos(2\pi f t + 2\pi K_p \int m(t) dt)$

$$v_o \propto 2\pi K_p (m(t)) \quad v_o = \frac{K_p}{K_V} m(t) \rightarrow \text{mag. sensitivity at TX}$$

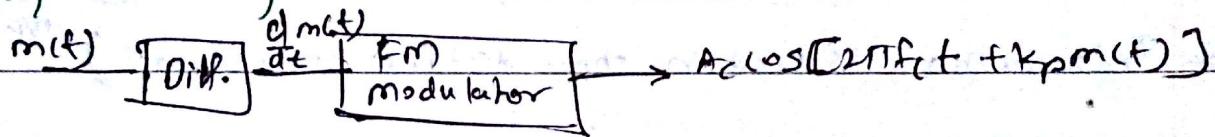
$$K_V \rightarrow \text{freq. sensitivity at RX.}$$

$$\phi = k_p m(t) \text{ rad}$$



∴ FM can be generated using phase modulator by prior  $\int m(t)$

My PM can be generated from FM



\* Bandwidth and power of PM are same as that of FM.

$$BW = 2(\beta_{pm} + 1) \text{ fm} \quad P_{pm} = \frac{A^2}{2}$$

$\beta$  of PM is independent of frequencies.

\* Figure of merit in FM =  $\frac{3}{2} \beta^2$  (for singletone modulator)

$$s(t)_{pm} = A_c \cos[2\pi f_c t + k_p A_m \cos 2\pi f_m t]$$

$$s(t)_{fm} = A_c \cos[2\pi f_c t + \beta \cos 2\pi f_m t]$$

$$\text{modulator index} \rightarrow \Delta\phi = k_p A_m = \beta$$

time domain eqn of phase modulated signal is same as the FM signal except a phase shift of  $90^\circ$  at msg frequency

## \* Radio Receivers.

### ① characteristics

\* Sensitivity: minimum signal strength to get std o/p.

sensitivity depends on overall gain of s/m.

\* Selectivity: ability to select the required frequencies.

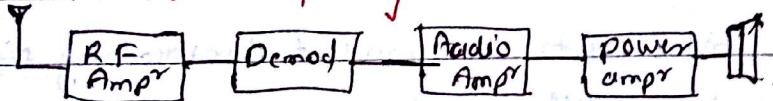
& Reject unwanted. B.W. =  $\frac{f_r}{Q}$  → resonant freq.  
Q → quality factor

tuned ckt tuned to resonant freq. fr & has B.W. 10KHz

then  $f_r - 5 \text{ KHz}$  &  $f_r + 5 \text{ KHz}$  frequencies are selected.

\* Fidelity: ability to reproduce all audio frequencies equally in the range of entire tuning

### \* Tuned Radio Frequency (TRF) Receiver

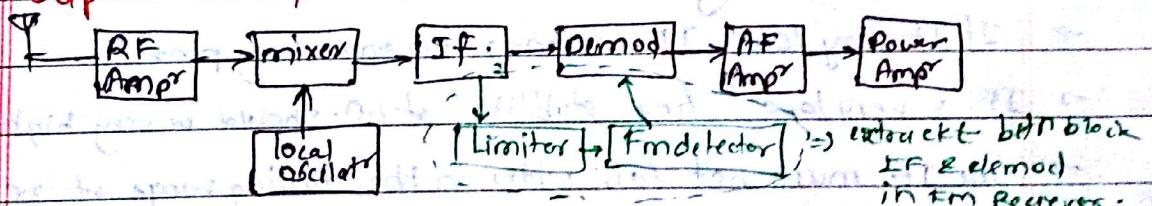


\* carrier frequencies allotted from FM = 88MHz - 108MHz.

from AM = 550KHz - 1650KHz

\* RF amp's are tuned amp's which allots only selected frequencies. value depends on  $f_r$  (resonant frequency)  
 $f_r$  can change by changing the capacitor value by tuning knob.

### \* Super heterodyne Receiver.



AM Range  $\rightarrow 550\text{KHz} - 1650\text{KHz}$  &  $\Delta f = 455\text{KHz}$

FM Range  $\rightarrow 88$  to  $108\text{MHz}$  &  $\Delta f \rightarrow 10.7\text{MHz}$

i) RF converted to IF then to AF

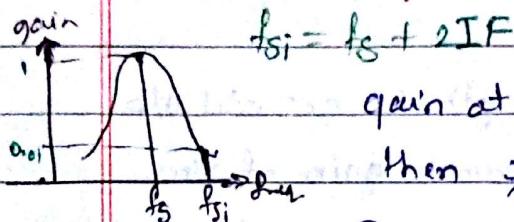
ii) IF freq. is always equal to  $455\text{KHz}$  & LO is tuned such that IF obtained  $= 455\text{KHz}$  called tuning.

iii) IF amp's tuned circuit always tuned to  $455\text{KHz}$ .

IF  $\rightarrow$  intermediate frequency

$f_{si}$   $\rightarrow$  image frequency.

## \* Image frequency (IF & its suppression)



gain at  $f_{si}$ ; should be as minimum as possible.

then  $S_N \gg 1$

To measure suppression factor Image Reject Ratio (IRR)

is used.  $IRR = \alpha = \frac{G_{IS}}{G_{IF}} = \frac{1}{0.01} = 100$ .

$$\alpha = \sqrt{1 + g^2 s^2} \quad s = \frac{f_{si}}{f_s} \quad \frac{f_s}{f_{si}}$$

$s$  should be as high as possible in accordance with  $\alpha$ .

## \* RF amp<sup>r</sup>

④ IRR  $\uparrow$  ses  $\Rightarrow$  overall gain  $\uparrow$  ses  $\Rightarrow$  sensitivity  $\uparrow$  ses  $\Rightarrow$  S/N at o/p neg.

## \* Mixer

→ Purpose of mixer is to downconvert the incoming signal

→ O/p of mixer is = difference of input frequencies.

→  $f_s$  - incoming signal freq.  $f_L$  - local oscillator frequency.

then O/p of mixer =  $[f_L - f_s]$   $f_L$  always  $> f_s$ .

→ If receiver tuned at  $f_s$ ,  $f_L$  adjusted so that O/p would be IF  
i.e.  $f_L - f_s = IF$

## \* choice of IF freq.

→ IF IF is too high poor selectivity poor adjustment channel reject<sup>high value</sup>

→ IF tracking difficulties.

→ If IF very low IF rejection becomes very poor.

→ If IF is very low freq. stability of LO should be very high.

→ The IF must not fall within the tuning range of receiver.

## \* Tracking of Receiver.

→ quenched capacitor adjusted for proper operation at highest freq.

→ peaking capacitor in parallel series with tank inductor adjusted

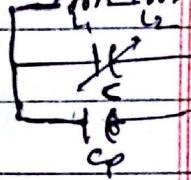
to provide tracking at low frequency.

→ final adjustment made at mid frequencies by slight adjustment of the inductance in each tank.

adjust LO frequency so that mixer o/p = IF  $f_L - f_s = IF$

$f_L - f_s \neq IF \Rightarrow$  tracking error.

tracking error can be minimised using ladder capacitor & trimmer circuit.  $f_t = \frac{1}{2\pi\sqrt{(L_1+L_2)C}}$

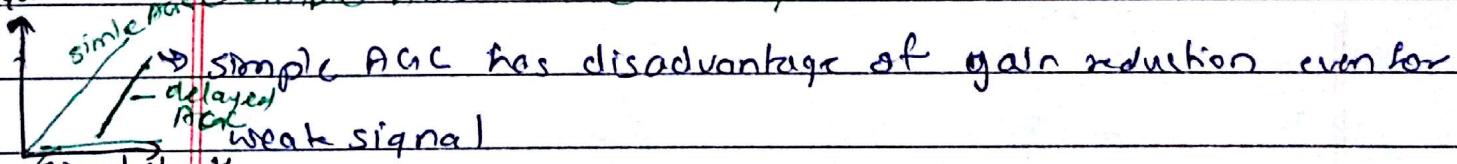
changing C nothing but tuning at receiver adjusting ladder capacitor is called tuning of receiver.  $\therefore f_t = \frac{1}{2\pi\sqrt{(L_1+L_2)(C+C_p)}}$   
  
For fine tuning to reduce tracking error trimmer capacitor is placed in series with C.

$$1. C_{eq} = \frac{C C_p}{C + C_p} + C_p$$

### \* Automatic Gain Control

- to maintain constant o/p. irrespective of variation in i/p signal strength
  - if i/p strength decreases gain increases & vice versa. so that o/p gain is constant
- Fading:- variation in signal strength at the i/p of the Receiver due to atmospheric conditions & multiple path reflections
- Receiver changes gain according to signal strength to have constant o/p.

#### ① Simple AGC      ② Delayed AGC.



Simple AGC has disadvantage of gain reduction even for weak signal  
No AGC → Delayed AGC not provide gain reduction until some arbitrarily signal level is attained.

### \* Squelch circuit

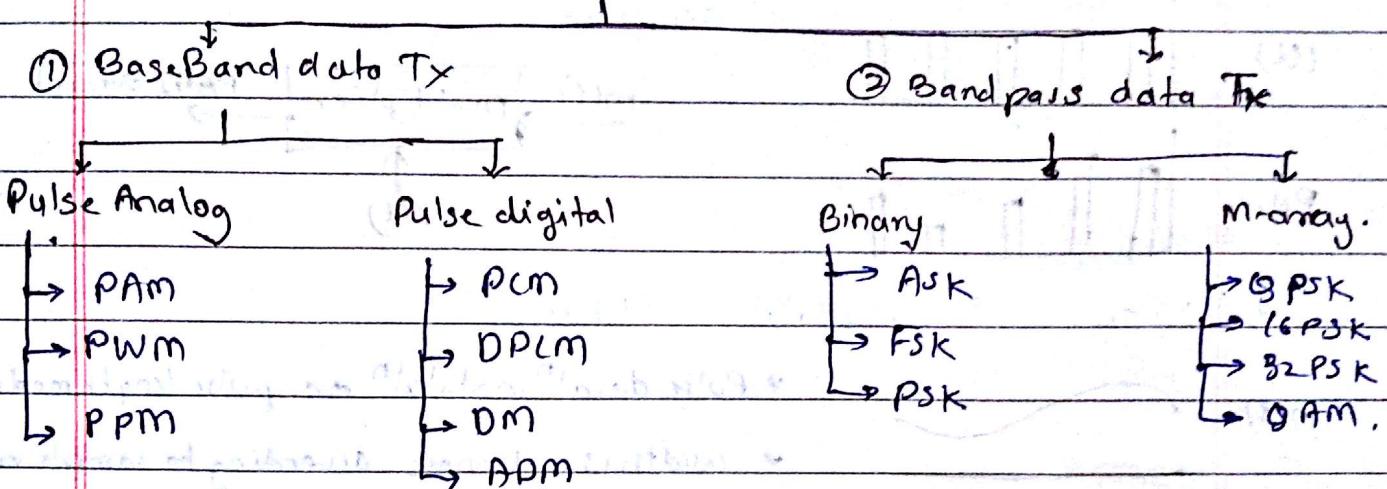
- switch on the receiver when signal is present switch off the receiver when signal is absent.

### \* Double spotting

- 1600 kHz station is selected when L.O. frequency is 1100 kHz as well as 2100 kHz. for an IF 500 kHz. so each station is selected twice.

## \* Digital communications.

- more rugged than analog as it can withstand channel noise & distortion.
- Possibility of introducing regenerative repeaters in the former.
- high fidelity & high privacy.



\* for bandpass channel is freespace & for passband channel is co-axial cable or fiber optic cable or twisted pair

\* we can not Tx digital data (Binary data) in freespace.  
 $\therefore$  its low freq. spectrum height of antenna should be very large  
 so baseband signal is converted to pass band pass signal  
 or digital data converted to analog then modulated & Txed.

\* Sampling :- Analog s/g.  $\xrightarrow{\text{to}}$  digital s/g. (ADC)

$$f_s \geq 2W \Rightarrow T_s \leq \frac{1}{2W}$$

$f_m$

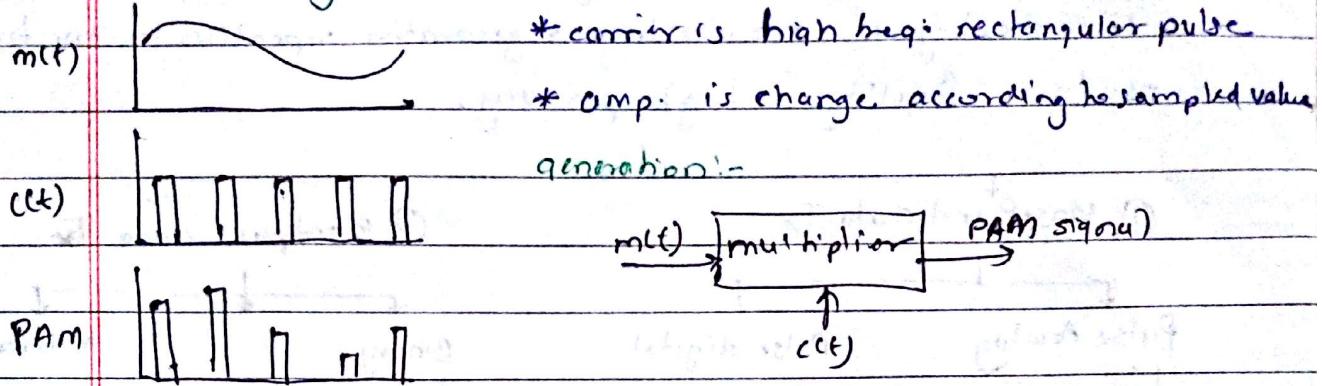
$w$  - highest freq. of s/g.

No. of samples more reconstruction is very close to i/p.

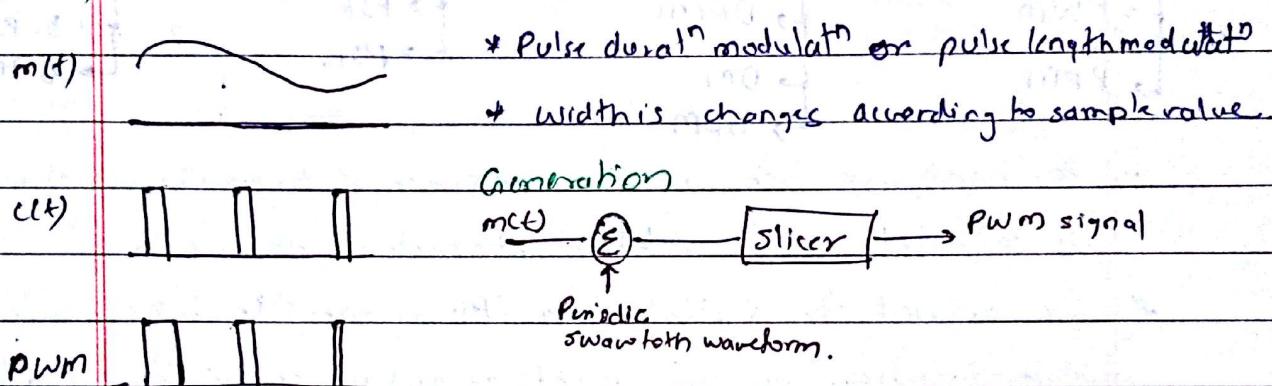
$\therefore f_s = 2w$  is called Nyquist rate

If  $f_s < 2f_m$  aliasing occurs loss of data.

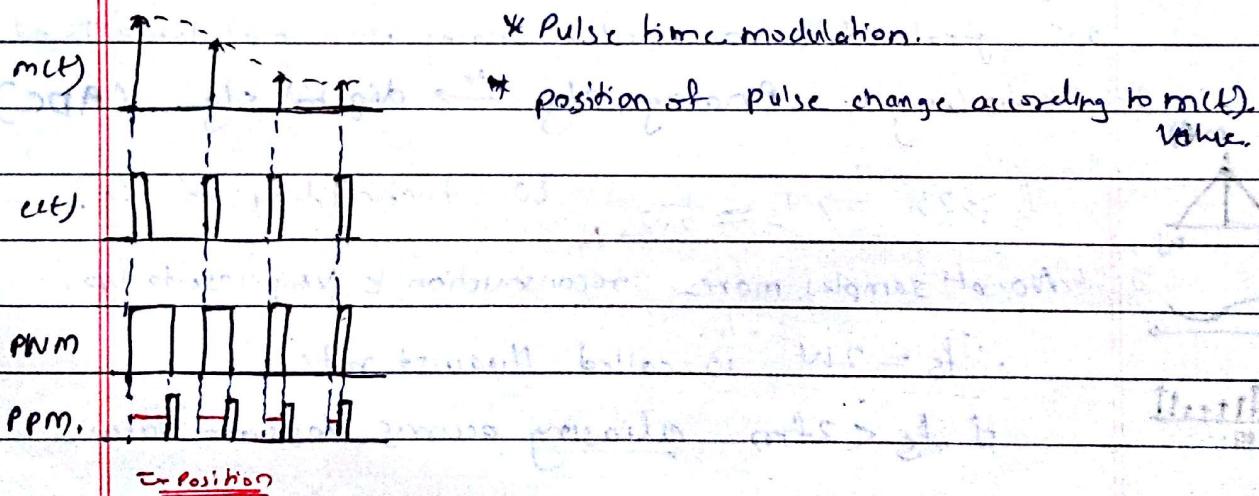
\* Baseband data Tx  
 Pulse Analog  
 ①\*) Pulse Analog modulation (PAM)



\*2) Pulse width Modulation (PWM)

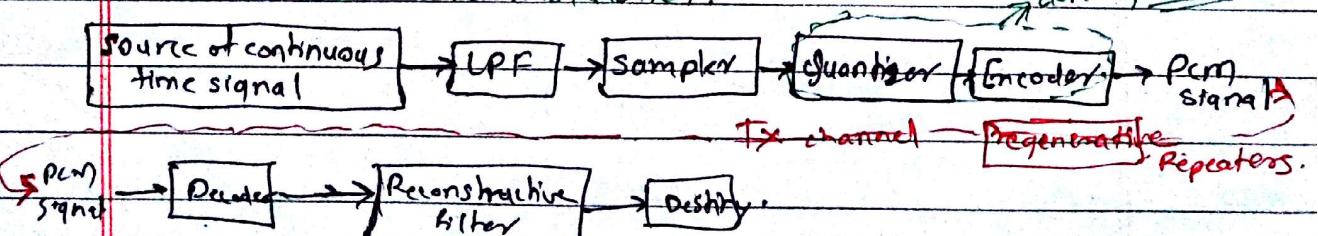


\*3) Pulse position Modulation (PPM)



②\*) Pulse Digital.

\*4) PCM (Pulse code modulation.)



- \* Quantiser converts continuously varying amp. signal to discrete amp. sig.
- \* encoding use to translate discrete set of sample in 1's & 0's.

\* For  $n$  bit PCM No. of quantisation levels =  $2^n$

$$\text{Step size, } \Delta = V_{\max} - V_{\min}$$

$$\text{Bit rate, } R_b = \text{sampling Rate} \times n = \frac{1}{T_s} \times n = \frac{n}{T_s}$$

$$\text{Bit duration, } T_b = \frac{T_s}{n} = \frac{1}{R_b} \quad \text{Max. B.W.} = \frac{n}{T_s} = \frac{1}{T_b}$$

$$\text{Min. B.W.} = \frac{1}{2T_b}$$

\* Regenerative Repeaters reproduce original sig free from noise.

\* In quantizer each sample is rounded off to the nearest quantization levels present in quantizer dependent on encoder.

Let samples from 0 to 8V. If encoder is 2-bit ADC.

$\therefore$  levels =  $2^2 = 4$ . divide 0 to 8V in ~~4~~ equal intervals.

$$\text{or step size} = 2V.$$

$$\begin{array}{l} 8V \\ 6V \\ 4V \\ 2V \\ 0V \end{array} \xrightarrow{\text{1}} \begin{array}{l} 7V \\ 5V \\ 3V \\ 1V \end{array}$$

\* 8V sample between 0-2 is rounded off to 00.

here 4 levels at receiver. 00 value is used so original value can not be recovered. The diff betw. that original value & quantized value is called Quantizer error. & distortion due to this is quantizer noise.

Quantized error,  $(\Delta e) = \text{sampled value} - \text{quantized value}$

$$(\Delta e)_{\max} = \frac{\Delta}{2} (\log_{10} \text{range from } -\frac{\Delta}{2} \text{ to } +\frac{\Delta}{2})$$

\* To reduce quantization error reduce step size ( $\Delta$ ) or No. levels (L)

\* ~~companding~~  $\Rightarrow$  level increases by using  $n$  (bits)

Passing the baseband sig through compressor then compressed sig sent to uniform quantizer. At the receiver this is compensated by expander this process is called companding.

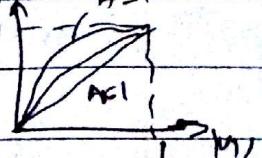
Two methods are used ① M-law ② A-law.

$$\textcircled{1} \text{ M law} \rightarrow |U_2| = \frac{\log(1+u/U_1)}{\log(1+u)}$$

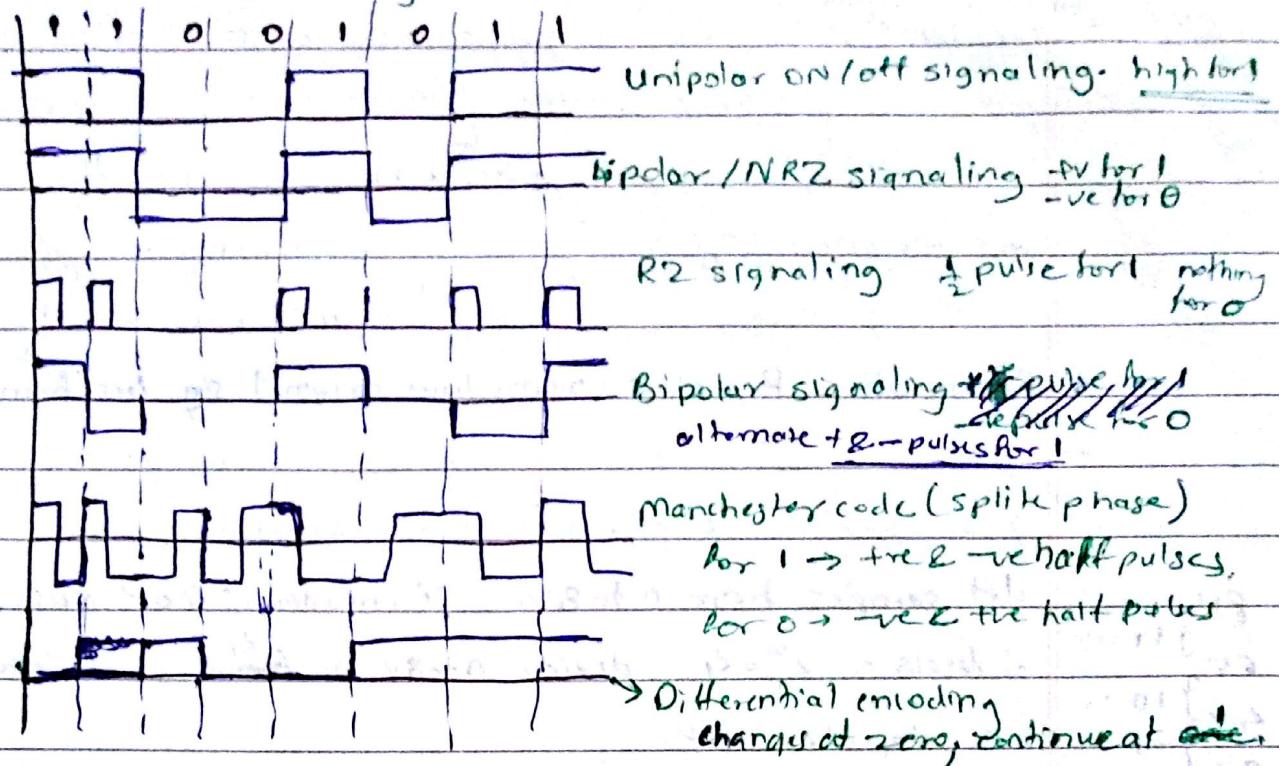


$$\textcircled{2} \text{ A law} \rightarrow |U_2| = A |U_1|$$

$$\frac{1 + \log(A|U_1|)}{1 + \log A} \quad 0 \leq |U_1| \leq \frac{1}{A} \quad |U_2| \quad A=100$$



\* Uncodes (electrically represented at 1's & 0's)



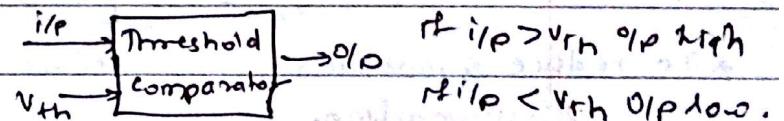
\* most widely used NRZ & bipolar signalling : effect of noise is less . used in PCM, DPCM, DM, FSK, PSK.

\* OFF set signalling (unipolar) used in ASK.

\* Differential encoding is used in DPSK.

\* RZ (Return to Zero) used in Fibre optics cable.

\* Regenerative Repeaters.



→ noise voltage eliminated.

for NRZ threshold voltage is 0.

\* Signal to quantisation Noise Ratio :

Quantisation Noise power = mean square value of the noise

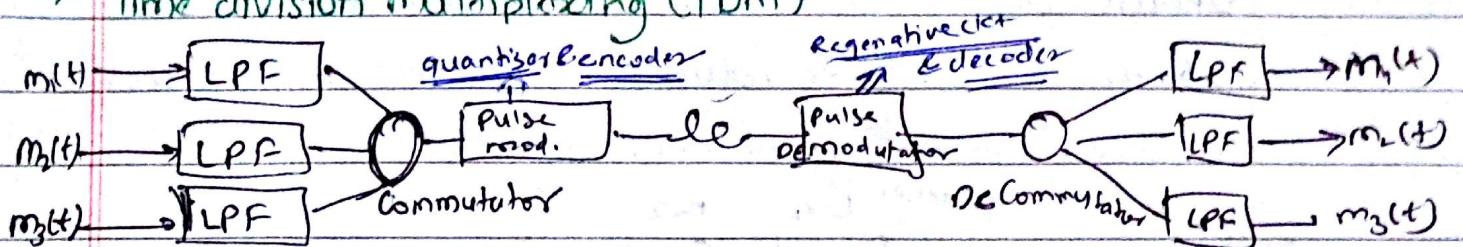
$$= \int_{-\infty}^{\infty} x^2 f(x) dx.$$

$$= \frac{\Delta^2}{12}$$

∴ Signal to quantisation Noise Ratio (SQNR) =  $\frac{A_m^2/2}{\Delta^2/12}$  but  $\Delta = \frac{2A_m}{2^n}$

$$\therefore SQNR = 1.8 + 6n \text{ dB}$$

## \* Time division multiplexing (TDM)



\* time taken by commutator or decommutator for one full revolution is  $T_s$

Total no. of channels =  $N$ , max freq. of every channel =  $f_m$ .

No. of quantisat<sup>n</sup> levels =  $L = 2^n$ , sampling freq. =  $2f_m$

$$\text{Sampling period} = T_s = \frac{1}{2f_m}$$

One bit is used to separate every channel & one bit is used for synchronisation for one period.

~~Total no. of bits per sampling period =  $Nn + N + 1$~~

$$\text{bit rate} = R_b = \frac{1}{T_b} = \frac{Nn + N + 1}{T_s} \rightarrow (\text{No. of signals per sample})$$

$$\text{bit duration} = T_b = \frac{\text{Sampling Period}}{\text{total no. of bits}} = \frac{1}{2f_m(Nn + N + 1)}$$

$$\text{minimum B.W.} = \frac{1}{T_b} = 2f_m(Nn + N + 1)$$

### FDM

\* carrier freq. are allotted

\* All signals Tx at same rate

\* synchronisation not required

### TDM

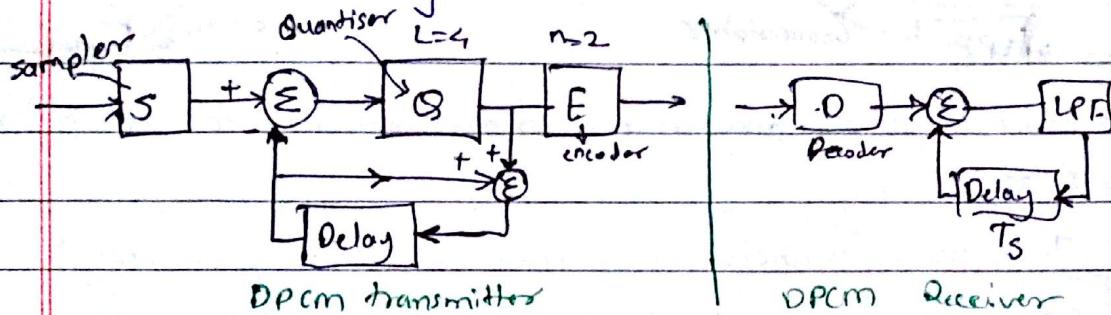
\* time slots are allotted

\* signals Tx in allotted time rate

\* synchronisation required

## \* DPCM Differential pulse code modulation

→ DPCM is used to reduce the quantisation error without increasing number of bits.



\* In PCM samples are applied directly to quantiser so dynamic range is high.

\* In DPCM difference betn two successive samples is applied as i/p to quantiser so dynamic range is reduced.

& hence dynamic range varies with sampling rate.

\* bit Rate of DPCM is same as PCM signal.  $= \frac{1}{T_s} = B.W.$

## \* Delta Modulation

Block diagram same as DPCM. but the encoder is 1 bit encoder.

$\delta$  Decoder.

\* It is used to decrease B.W. i.e. to reduce bit rate

to characteristics of input

\* When i/p to  $\square$  is +ve o/p is  $+\Delta$  if -ve. o/p is  $-\Delta$

In DM as  $n=1$  bit rate is same as sampling rate

$$R_b = \frac{1}{T_s} \quad T_b = T_s \quad B.W. \propto \frac{1}{\text{pulse width}}$$

at receiver end 1 is decoded as  $\Delta$  & 0 as  $-\Delta$

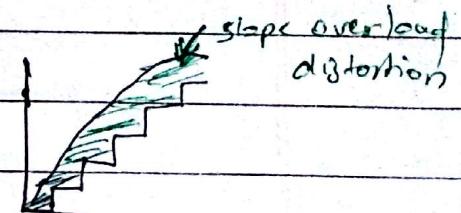
The signal reconstruction depends on  $\Delta$ .

## \* Quantisat'n errors in DM:-

### ① Slope overload distortion

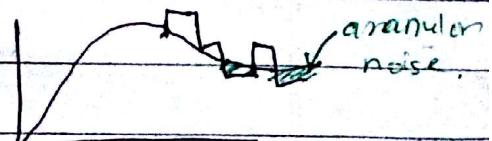
when step size  $\Delta$  is too small for

the staircase approximation.



### ② Granular noise

step size  $\Delta$  is large.



Condition for no slope overload distortion for single tone modul'tn

$$\Rightarrow \text{is } \frac{\Delta}{T_s} = A_m 2\pi f_m$$

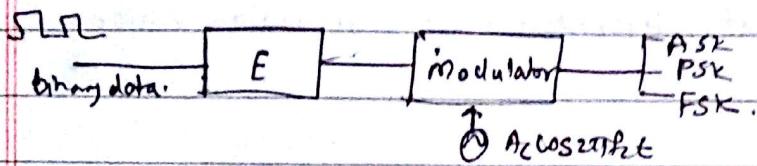
## \* Adaptive delta modulation (ADM)

→ In ADM additional hardware is designed to provide variable step size thereby reducing slope overload effects without increasing the granular noise.

-eas

## \* Bandpass communication system.

msg signal is in form of binary data but having significant low frequencies. so to Tx antenna problem occurs so msg signal is multiplied by analog carrier through modulator.

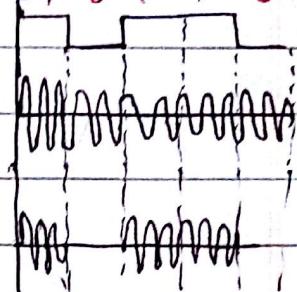


## \* Digital carrier modulation

### ① Amplitude shift keying (ASK):

Amplitude is modulated according to msg, carrier.

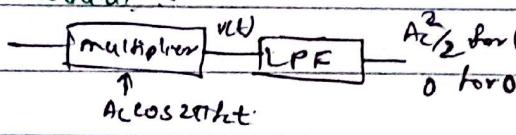
$$s(t) = A_c \cos 2\pi f_c t \text{ if } m(t) = 1 \\ = 0 \quad \text{if } m(t) = 0$$



$B.W. = 2 \times \frac{1}{T_b} = 2 \times \text{bit rate.}$

$s(t) = A_c \cos 2\pi f_c t$  for 1  
 $s(t) = 0$  for 0

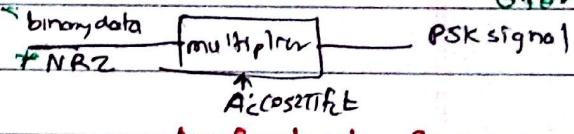
Demodulation:



$$\text{energy per bit } E_b = \int_0^{T_b} s_b(t) dt = PXT_b \\ = \frac{A_c^2}{2} T_b \text{ for } 1 \\ \text{for } 0$$

### ② Phase shift keying (PSK)

$$s(t) = A_c \cos 2\pi f_c t \text{ if } m(t) = 1 \\ = -A_c \cos 2\pi f_c t \text{ if } m(t) = 0.$$



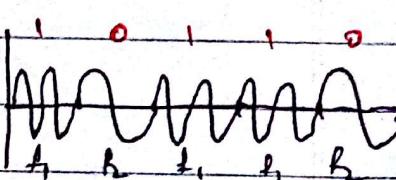
$T_b = \frac{n}{f_c} \Rightarrow f_c = \frac{n}{T_b} = n f_b$

Demodulation: B.D. same as ASK.  $E_b = A_c^2 / 2 \text{ for } 1$   
 $B.W. = 2 \times \text{bitrate} = 2 \times f_b. \quad = -A_c^2 / 2 \text{ for } 0.$

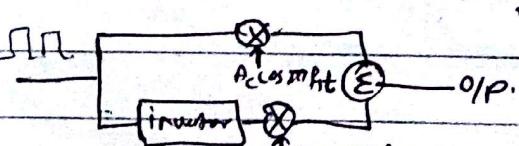
③

### Frequency shift keying (FSK):

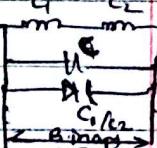
$$s(t) = A_c \cos 2\pi f_1 t \text{ if } m(t) = 1 \\ = A_c \cos 2\pi f_2 t \text{ if } m(t) = 0.$$



generation:-



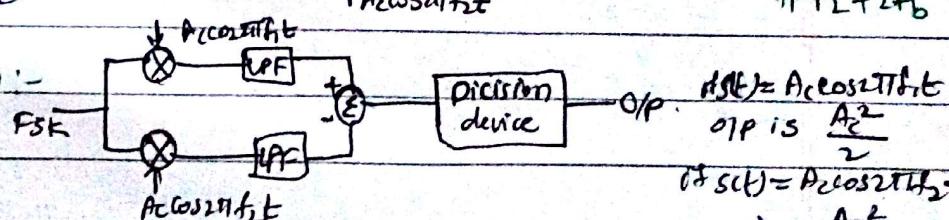
$$B.W. = 2\Delta f + 2f_b \\ = f_1 - f_2 + 2f_b$$



$f_1 = f_c + k_f v \Rightarrow$  Mark freq.

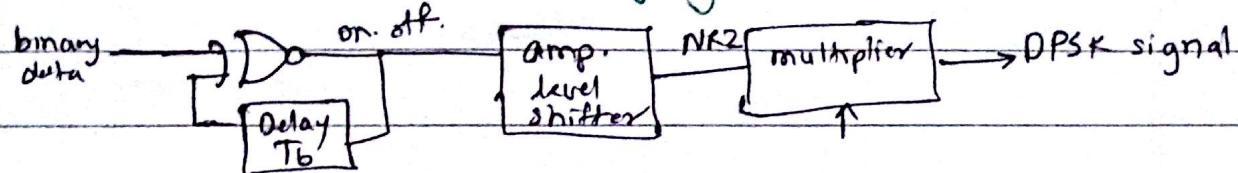
$f_2 = f_c + k_f u \Rightarrow$  space freq.

$$f_1 = \frac{1}{2\pi(f_c + k_f v)} \text{ for } v \text{ (mark freq.)} \\ f_2 = \frac{1}{2\pi(f_c + k_f u)} \text{ for } u \text{ (space freq.)}$$



Cut off frequency of LPF should be less than  $(f_1 - f_2)$  so that  $f_1 - f_2$  terms is also suppressed.

## Differential Phase shift keying (DPSK).



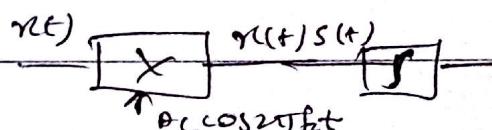
- amplitude level shifter use to change on off signaling to NR2 by adding negative dc level
- DPSK not require a coherent carrier for modulation.

## Matched filter.

- Optimum filter is an integrator that gives min. probability of error.
- Matched filter is the optimum filter with white noise as i/p.  
 $H(f) = k g(t-t)$        $g(t)$  is i/p signed.

### Correlation Receiver

$$y(t) = \int_0^{T_p} r(\tau) s(\tau) d\tau$$



In general correlation receiver & match filter are same.

$$P_e = Q \left[ \sqrt{\frac{E_b}{2N_0}} \right]$$