

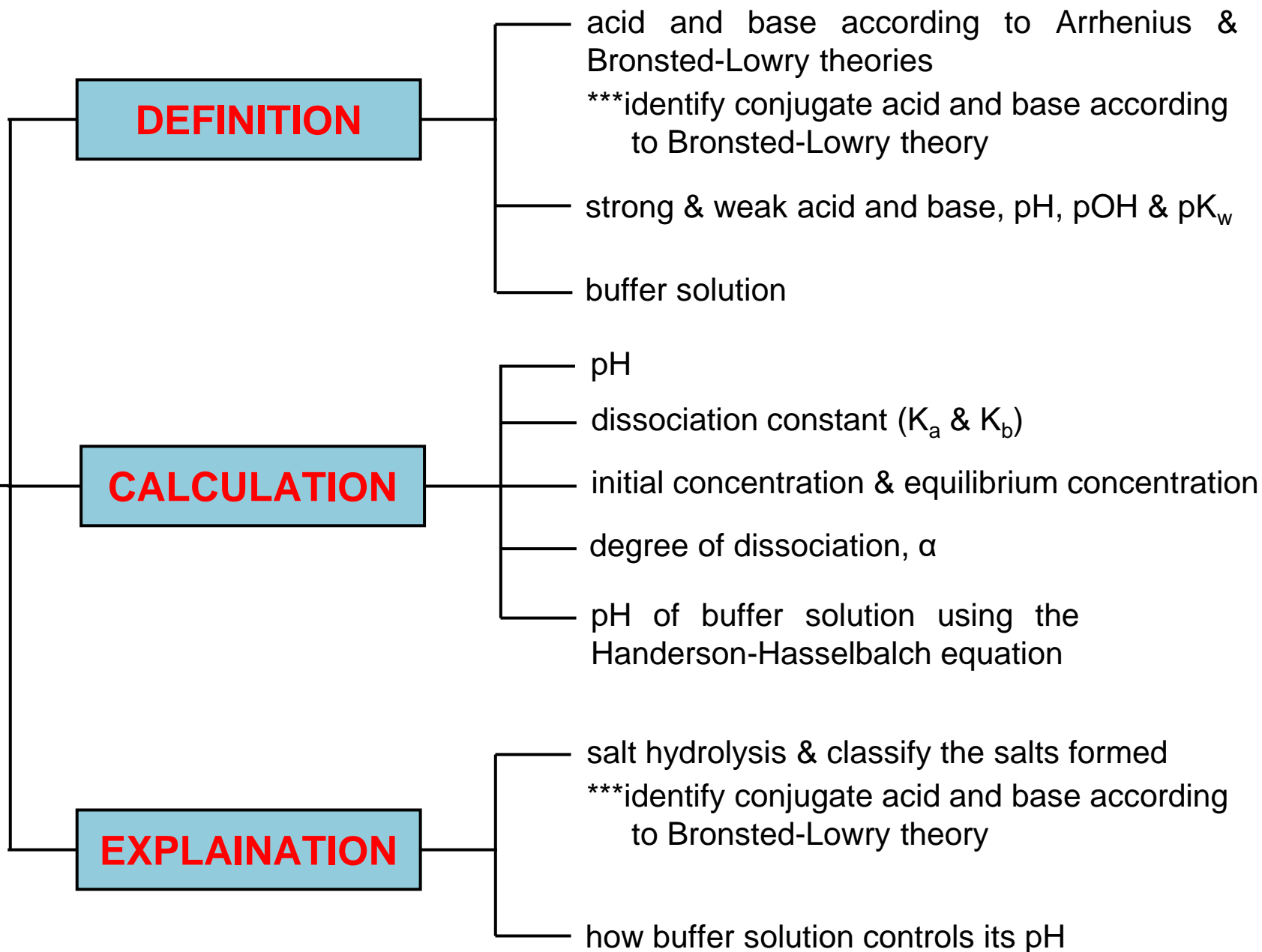
CHAPTER 7

IONIC EQUILIBRIUM

- 7.1 Acids and Bases
- 7.2 Acid-base Titration
- 7.3 Solubility Equilibrium



7.1 ACIDS AND BASES



7.1 a) Definition of Acids and Bases

There are 2 main definitions for acids and bases:

* Arrhenius

* Brönsted-Lowry



Arrhenius Theory

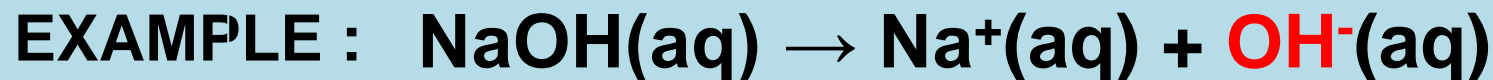
Acid

Substance that dissociate in water to **produce** **H₃O⁺** ion.



Base

Substance that dissociate in water to **produce** **OH⁻** ion.

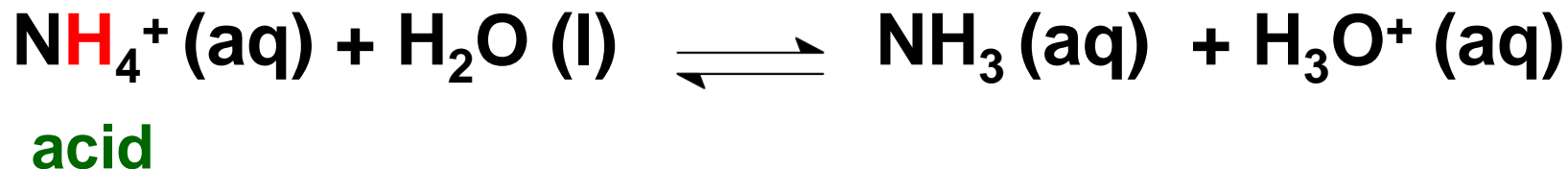
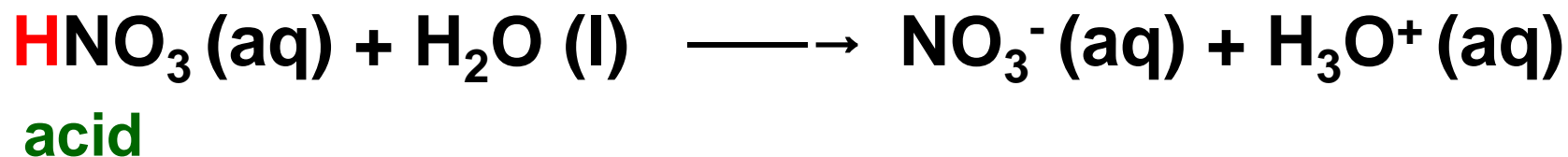


Bronsted-Lowry Theory

Acid

Any substance that **can donate a proton, (H⁺)** to other substance.

EXAMPLE:

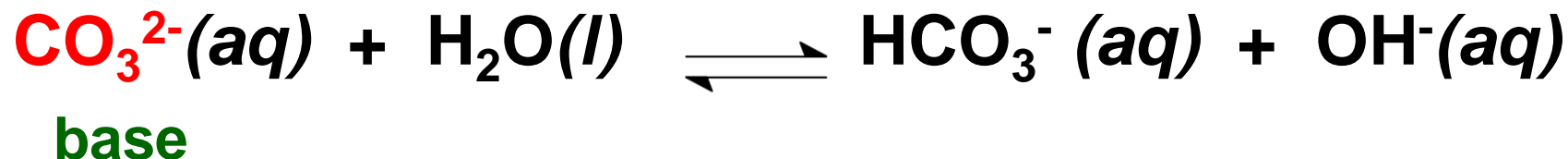
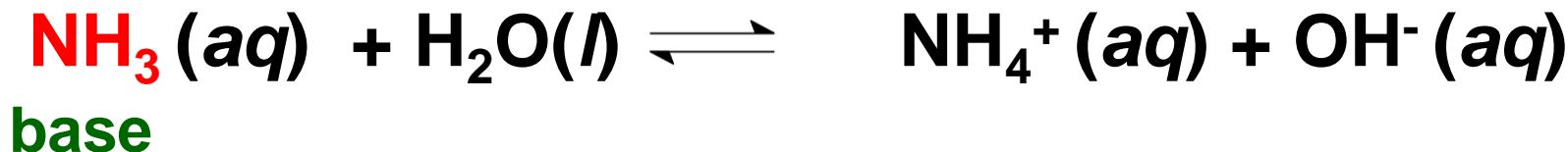


Bronsted-Lowry Theory

Base

Any substance that **can accept a proton, (H⁺)** from other substance.

EXAMPLE:





- An **acid** can exist as “+” charge, “-” charge or **neutral**.

Example: H_3O^+ , H_2SO_4 , HCO_3^- , NH_4^+

- A **base** can only exist as “-” charge or **neutral**.

Example: OH^- , CN^- , NH_3 , NH_2^-

- H_2O is **amphoteric** : able to act as an acid or a base

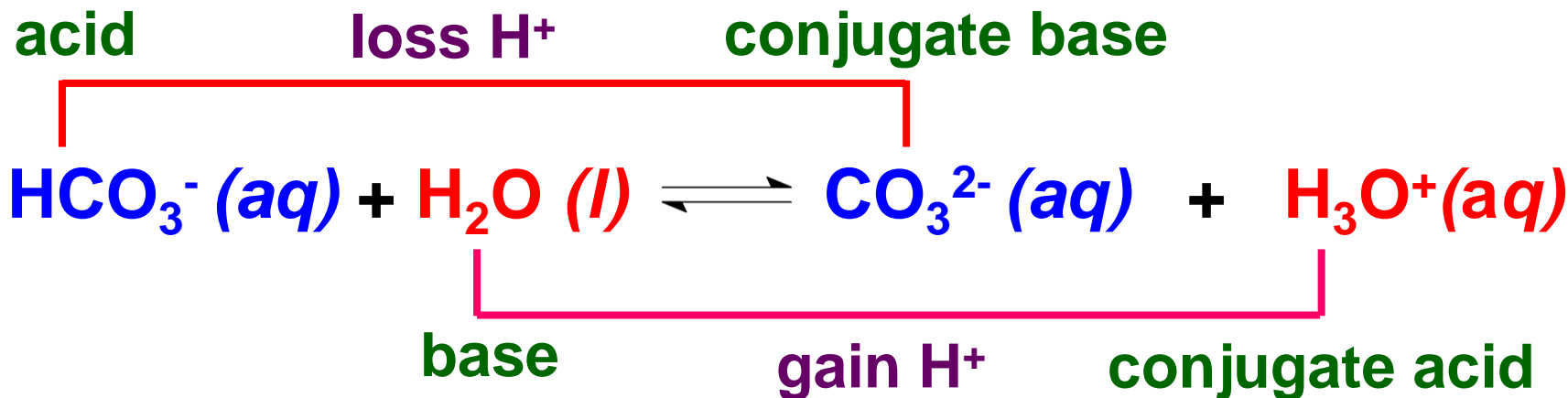
7.1 b) Conjugate Acid-Base Pairs

Conjugate Acid

A species that remains when **one proton, (H⁺)** has been **added** to the **base**.

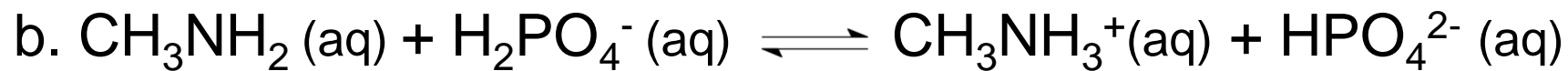
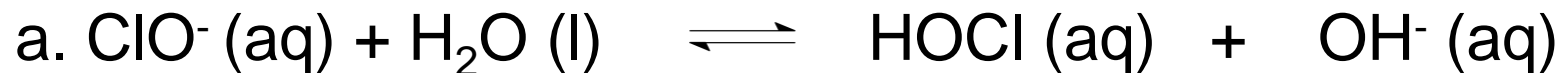
Conjugate Base

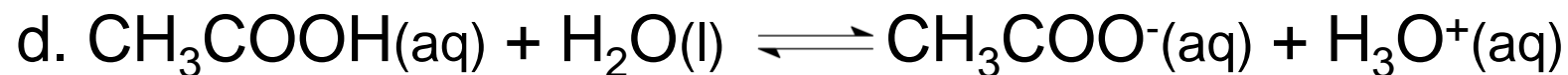
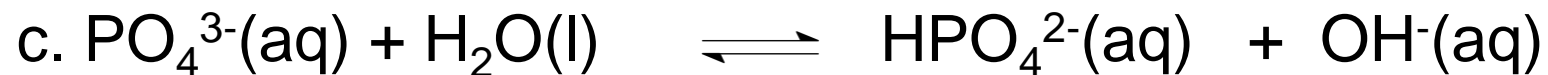
A species that remains when **one proton, (H⁺)** has been **removed** from the **acid**.



EXERCISE 1

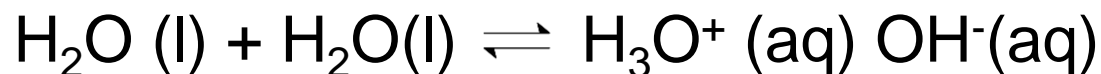
In the following reactions, identify the acid-base conjugate pairs.





7.1 c) The water Ionization Constant, K_w

Water ionizes to a small degree to form very small amount of H_3O^+ and OH^- .



$$K_w = [H_3O^+][OH^-] = 1 \times 10^{-14}$$

**ionic product of water at 25°C*

Negative log of both sides of the expression

$$-\log(K_w) = -\log([H_3O^+][OH^-])$$

$$-\log(1.0 \times 10^{-14}) = (-\log[H_3O^+]) + (-\log[OH^-])$$

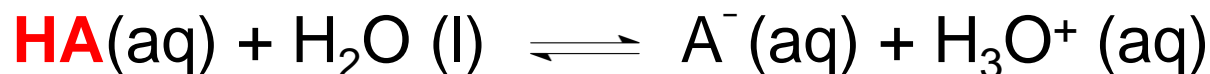
$$14 = pH + pOH$$

The value of K_w increases with temperature because the dissociation of water is an endothermic process. For aqueous solution at 25°C,

ACIDIC SOLUTION	NEUTRAL SOLUTION	BASIC SOLUTION
$[H_3O^+] > [OH^-]$ $[H_3O^+] > 1.0 \times 10^{-7} \text{ M}$ @ $[OH^-] < 1.0 \times 10^{-7} \text{ M}$	$[H_3O^+] = [OH^-]$ $= 1.0 \times 10^{-7} \text{ M}$	$[OH^-] > [H_3O^+]$ $[OH^-] > 1.0 \times 10^{-7} \text{ M}$ @ $[H_3O^+] < 1.0 \times 10^{-7} \text{ M}$

7.1 d) Strong and Weak Acids

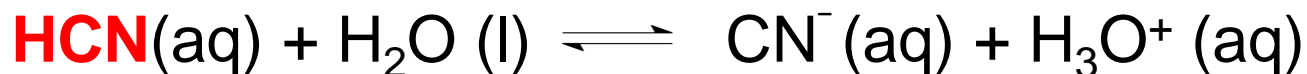
- When an acid **HA** dissolves in water, equilibrium is established



- The stronger the acid, the further the position of the equilibrium lies to right, the higher degree of dissociation.



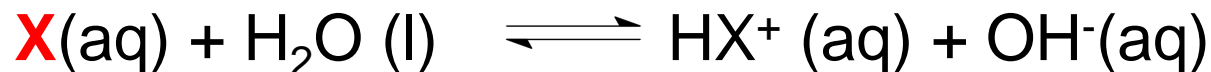
- Strong acids** *completely* dissociated in aqueous solution



- Weak acids** *partially* dissociate in aqueous solution.

Strong and Weak Bases

- When a base **X** dissolves in water, equilibrium is established



- The stronger the base, the further the position of the equilibrium lies to right, the higher degree of dissociation.



- Strong base** *completely* dissociated in aqueous solution



- Weak base** *partially* dissociate in aqueous solution.

Example:

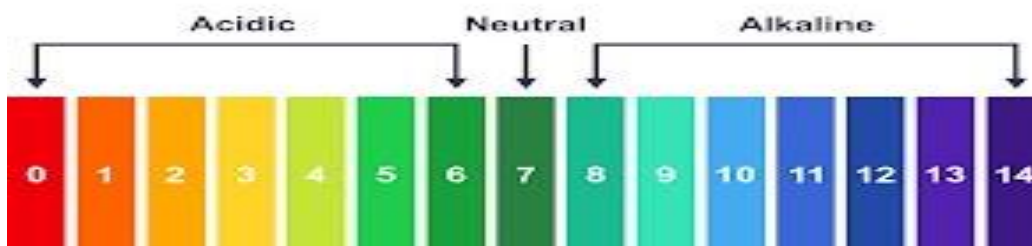
STRONG ACIDS	STRONG BASES
<p>The hydrohalic acids e.g: HCl, HBr and HI</p>	<p>M_2O or MOH, where M is group 1 element : Li, Na, K, Rb, Cs</p>
<p>Oxoacids : the number of O atoms exceeds the number of ionizable protons by two or more. e.g: HNO₃ and HClO₄</p>	<p>RO or $R(OH)_2$, where R is Ca, Sr, Ba</p>

Example:

WEAK ACIDS	WEAK BASES
Hydrohalic acids: HF	Ammonia : NH_3
Acids in which H not bonded to O or halogen: HCN and H₂S	Amine : R-NH_2 , $\text{R}_2\text{-NH}$ & $\text{R}_3\text{-N}$ such as $\text{CH}_3\text{CH}_2\text{-NH}_2$ & etc
Oxoacids: HClO , HNO₂ and H₃PO₄	Hydrazine : N_2H_4
Organic acids (general formula = R-COOH): CH₃COOH and C₆H₅COOH	

pH	pOH	pK _w
pH is a measure of the concentration of H ⁺ /H ₃ O ⁺ ions in a solution	pOH is a measure of the concentration of OH ⁻ ions a solution	pK _w is a measure of negative logarithm (-log) of the dissociation or ionisation constant of water.
pH = -log [H ⁺]	pOH = -log [OH ⁻]	pK _w = -log (K _w)

pH scale: Scale to express acidity/basicity



Neutral solution : pH =7 ; [H₃O⁺] = [OH⁻]
 Acidic solution: pH < 7 ; [H₃O⁺] > [OH⁻]
 Basic solution: pH > 7 ; [H₃O⁺] < [OH⁻]

7.1 e) pH Calculation for Strong Acid & Strong Base

Example :

- 1. Calculate the pH of 0.15 mol dm^{-3} of HCl solution.**
- 2. Calculate the pH of 0.20 M of NaOH solution.**

Answer :

Question 1

$\text{HCl(aq)} \longrightarrow \text{H}^{\text{+}}(\text{aq}) + \text{Cl}^{-}(\text{aq})$			
Initial (M)	0.15	0	0
Final (M)	0	0.15	0.15

$$\text{pH} = -\log [\text{H}^{\text{+}}]$$

$$= -\log (0.15)$$

$$= 0.82$$

Answer :

Question 2

$\text{NaOH(aq)} \longrightarrow \text{OH}^{\cdot}\text{(aq)} + \text{Na}^{\cdot}\text{(aq)}$			
Initial (M)	0.20	0	0
Final (M)	0	0.20	0.20

$$\begin{aligned}\text{pOH} &= -\log [\text{OH}^{\cdot}] \\ &= -\log (0.20) \\ &= 0.6989\end{aligned}$$

$$\begin{aligned}\text{pH} &= 14 - \text{pOH} \\ &= 14 - 0.6989 \\ &= 13.30\end{aligned}$$



$$\text{pH} = -\log [\text{H}^+]$$

$$\text{pOH} = -\log [\text{OH}^-]$$

$$\text{pH} + \text{pOH} = 14$$

scale

pH

0

7

14

acidic

$[\text{H}^+] > [\text{OH}^-]$

neutral

$[\text{H}^+] = [\text{OH}^-]$

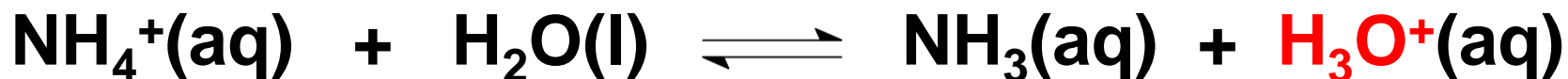
basic

$[\text{H}^+] < [\text{OH}^-]$

7.1 f) Relationship Between K_a and K_b for Acid-Base Conjugate Pairs

Consider the acid-base conjugate pair of ammonium ion, NH_4^+ and ammonia, NH_3 .

The dissociation of both species in water is given by,



For ammonium ion, NH_4^+ the expression corresponding to K_a is :

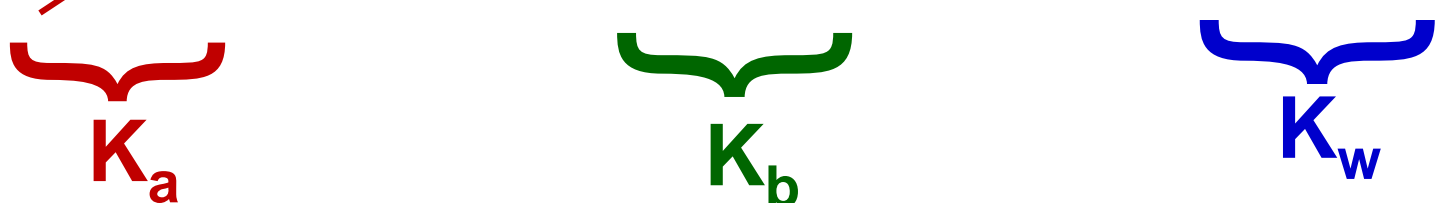
$$K_a = \frac{[\text{NH}_3] [\text{H}_3\text{O}^+]}{[\text{NH}_4^+]}$$

For ammonia, NH_3 the expression corresponding to K_b is :

$$K_b = \frac{[\text{NH}_4^+] [\text{OH}^-]}{[\text{NH}_3]}$$

Therefore, the product of $K_a \times K_b$ is:

$$\frac{[\cancel{\text{NH}_3}] [\text{H}_3\text{O}^+]}{[\cancel{\text{NH}_4^+}]} \times \frac{[\cancel{\text{NH}_4^+}] [\text{OH}^-]}{[\cancel{\text{NH}_3}]} = [\text{H}_3\text{O}^+] [\text{OH}^-]$$



$$K_a \times K_b = K_w$$

$$-\log K_a + (-\log K_b) = -\log K_w$$

The equation above can be written as,

$$\text{p}K_a + \text{p}K_b = \text{p}K_w = 14$$

The Strengths of Acids And Bases

The strengths of acids and bases can be compared in terms of:

- i. the degree of dissociation (α)**
- ii. the dissociation constant (K)**



7.1 g) Degree of dissociation (α)

Ability of acids or bases to ionize or dissociate in aqueous solution

$$\alpha = \frac{\text{Concentration of acid or base dissociation}}{\text{Initial concentration}}$$

$$\alpha = \frac{x}{[\text{initial}]}$$

Example 1 :

Calculate the percent dissociation if amount of H^+ dissociated in a solution of 0.10 M acetic acid is 1.3×10^{-3} M.

ANSWER:

$$\begin{aligned}\text{Percent dissociation} &= \frac{1.3 \times 10^{-3}}{0.10} \times 100\% \\ &= 1.3 \%\end{aligned}$$

K_a or K_b value can be used to distinguish the relative acidity strength of weak acid and weak base.

☞ $K_a \uparrow$ ($pK_a \downarrow$), $[H^+] \uparrow$, thus pH \downarrow (more acidic)

☞ $K_b \uparrow$ ($pK_b \downarrow$), $[OH^-] \uparrow$, thus pH \uparrow (more basic)

Acid	pK_a		Base	pK_b
CH_3COOH	4.74		$C_6H_5NH_2$	9.37
$HCOOH$	3.76		NH_3	4.74

Conclusion :

- **Relative acidity, $HCOOH > CH_3COOH$**
- **Relative basicity, $NH_3 > C_6H_5NH_2$**

EXERCISE 1:

Find the values of $[H^+]$ that correspond to each of the following values of pH.

- a) 2.90 (the approximate pH of lemon juice)**
- b) 11.61 (the pH of dilute, household ammonia)**

Answer:

- a. $1.26 \times 10^{-3} M$**
- b. $2.455 \times 10^{-12} M$**

Solving Problems Involving Weak Acid & Weak Base Equilibria

Two general types of problems:

1. Equilibrium concentrations

✚ find K_a (or K_b)

2. K_a (or K_b) and some concentrations information are given.

✚ find the other equilibrium concentrations.

USE ***ICE*** TABLE

ASSUMPTIONS:

1. If the formation of H_3O^+ is very small,
⇒ therefore $[\text{H}_3\text{O}^+]$ is negligible
2. A weak acid has a small K_a , ($K_a \leq 1.0 \times 10^{-5}$),
⇒ x is very small
⇒ $[\text{HA}]_{\text{initial}} - x = [\text{HA}]_{\text{initial}}$

apply 5% test to check the assumption is justified



Example 1:

Degree of dissociation of 1.0 M solution of hydrazine, N_2H_4 at 25°C is 3.5%. What is its base dissociation constant, K_b ?

Answer :

$$\begin{array}{l} \text{\% ionization} \\ \text{of } \text{N}_2\text{H}_4 \end{array} = \frac{\text{concentration dissociated } (x)}{\text{initial concentration } (c)} \times 100$$

$$3.5 \% = \frac{x \text{ M}}{1.0 \text{ M}} \times 100$$

$$x = 0.035 \text{ M}$$

	$\text{N}_2\text{H}_4 (\text{aq}) + \text{H}_2\text{O} (\text{l}) \rightleftharpoons \text{OH}^- (\text{aq}) + \text{N}_2\text{H}_5^+ (\text{aq})$			
Initial (M)	1.0	-	0	0
Change (M)	- 0.035	-	+ 0.035	+ 0.035
Equilibrium (M)	1.0 - 0.035 = 0.965	-	0.035	0.035

At equilibrium, $K_b = \frac{[\text{N}_2\text{H}_5^+][\text{OH}^-]}{[\text{N}_2\text{H}_4]}$

$$= \frac{(0.035)(0.035)}{(0.965)} = 1.27 \times 10^{-3}$$

Example 2:

Calculate the pH of a 0.20 M solution of HCN.
[K_a for HCN is 4.90×10^{-10} .]

Answer :

	$\text{HCN}_{(\text{aq})} + \text{H}_2\text{O}_{(\text{l})} \rightleftharpoons \text{H}_3\text{O}^+_{(\text{aq})} + \text{CN}^-_{(\text{aq})}$			
Initial (M)	0.2	-	0	0
Change (M)	- x	-	+ x	+ x
Equilibrium (M)	0.2 - x	-	x	x

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{CN}^-]}{[\text{HCN}]} = 4.90 \times 10^{-10}$$

$$K_a \ll 1$$

\therefore Assume x very small, therefore:

$$0.20 - x \approx 0.20$$

$$4.90 \times 10^{-10} = \frac{(x)(x)}{(0.2)}$$

$$x^2 = (4.9 \times 10^{-10} \text{ M})(0.20 \text{ M})$$

$$x = 9.9 \times 10^{-6} \text{ M}$$

Therefore,

$$[\text{H}^+] = 9.9 \times 10^{-6} \text{ M}$$

$$\text{pH} = -\log [\text{H}^+]$$

$$= 5.00$$

Example 3:

The K_a for formic acid (HCOOH) is 1.8×10^{-4} . What is the pH of a 0.010 M solution of formic acid?

Answer :

	$\text{HCOOH}_{(\text{aq})} + \text{H}_2\text{O}_{(\text{l})} \rightleftharpoons \text{H}_3\text{O}^+_{(\text{aq})} + \text{HCOO}^-_{(\text{aq})}$			
Initial (M)	0.01	-	0	0
Change (M)	- x	-	+ x	+ x
Equilibrium (M)	0.01 - x	-	x	x

At equilibrium,

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{HCOO}^-]}{[\text{HCOOH}]} = 1.8 \times 10^{-4}$$

$$K_a \gg 1.0 \times 10^{-5}$$

solve the calculation with quadratic equation. 39

$$1.8 \times 10^{-4} = \frac{(x)(x)}{(0.01 - x)}$$

$$x^2 = (1.8 \times 10^{-4})(0.01 - x)$$

$$x^2 + 1.8 \times 10^{-4}x - 1.8 \times 10^{-6} = 0$$

$$x_1 = 1.255 \times 10^{-3} \quad x_2 = -1.435 \times 10^{-3} \text{ (neglected)}$$

$$[\text{H}^+] = 1.255 \times 10^{-3} \text{ M}$$

$$\text{Therefore, pH} = -\log [\text{H}^+]$$

$$= -\log (1.255 \times 10^{-3})$$

$$= \mathbf{2.90}$$

Example 4:

The base-dissociation constant for ammonia, $\text{NH}_{3(\text{aq})}$ is 1.8×10^{-5} M. Calculate the concentration of OH^- ion, pH and % dissociation at equilibrium if the initial concentration of NH_3 is 0.15 M.

Answer :

	$\text{NH}_3 (\text{aq}) + \text{H}_2\text{O} (\text{l}) \rightleftharpoons \text{OH}^- (\text{aq}) + \text{NH}_4^+ (\text{aq})$			
Initial (M)	0.15	-	0	0
Change (M)	- x	-	+ x	+ x
Equilibrium (M)	0.15 - x	-	x	x

At equilibrium,

$$\begin{aligned} K_b &= \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} \\ &= \frac{(x)(x)}{(0.15 - x)} = 1.80 \times 10^{-5} \end{aligned}$$

$$K_b \lll 1$$

\therefore Assume x very small, therefore:

$$0.15 - x \approx 0.15$$

$$1.80 \times 10^{-5} = \frac{(x)(x)}{(0.15)}$$

$$x^2 = (1.8 \times 10^{-5} \text{ M})(0.15 \text{ M})$$

$$x = 1.64 \times 10^{-3} \text{ M}$$

Therefore,

$$[\text{OH}^-] = 1.64 \times 10^{-3} \text{ M}$$

$$\text{pOH} = -\log [\text{OH}^-]$$

$$= 2.79$$

$$\text{pH} + \text{pOH} = 14$$

$$\begin{aligned}\text{pH} &= 14 - 2.79 \\ &= 11.21\end{aligned}$$

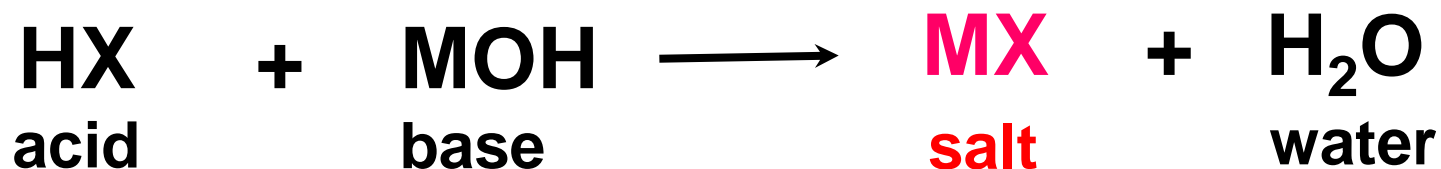
$$\begin{aligned}\% \text{ dissociation} &= \frac{1.64 \times 10^{-3}}{0.15} \times 100\% \\ &= 1.09 \% \\ &\approx 1.1 \%\end{aligned}$$

$$\text{Degree of dissociation, } \alpha = 0.011$$

7.1 h) Salt Hydrolysis

Salt is an ionic compound that is formed by the reaction of an acid with a base.

General equation of neutralization:

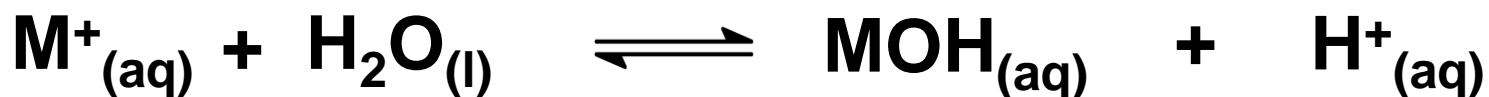


Hydrolysis is the reaction of cations/anions (or both) from salts with water molecules to produce H^+ or OH^-

MX salt dissociation equation:

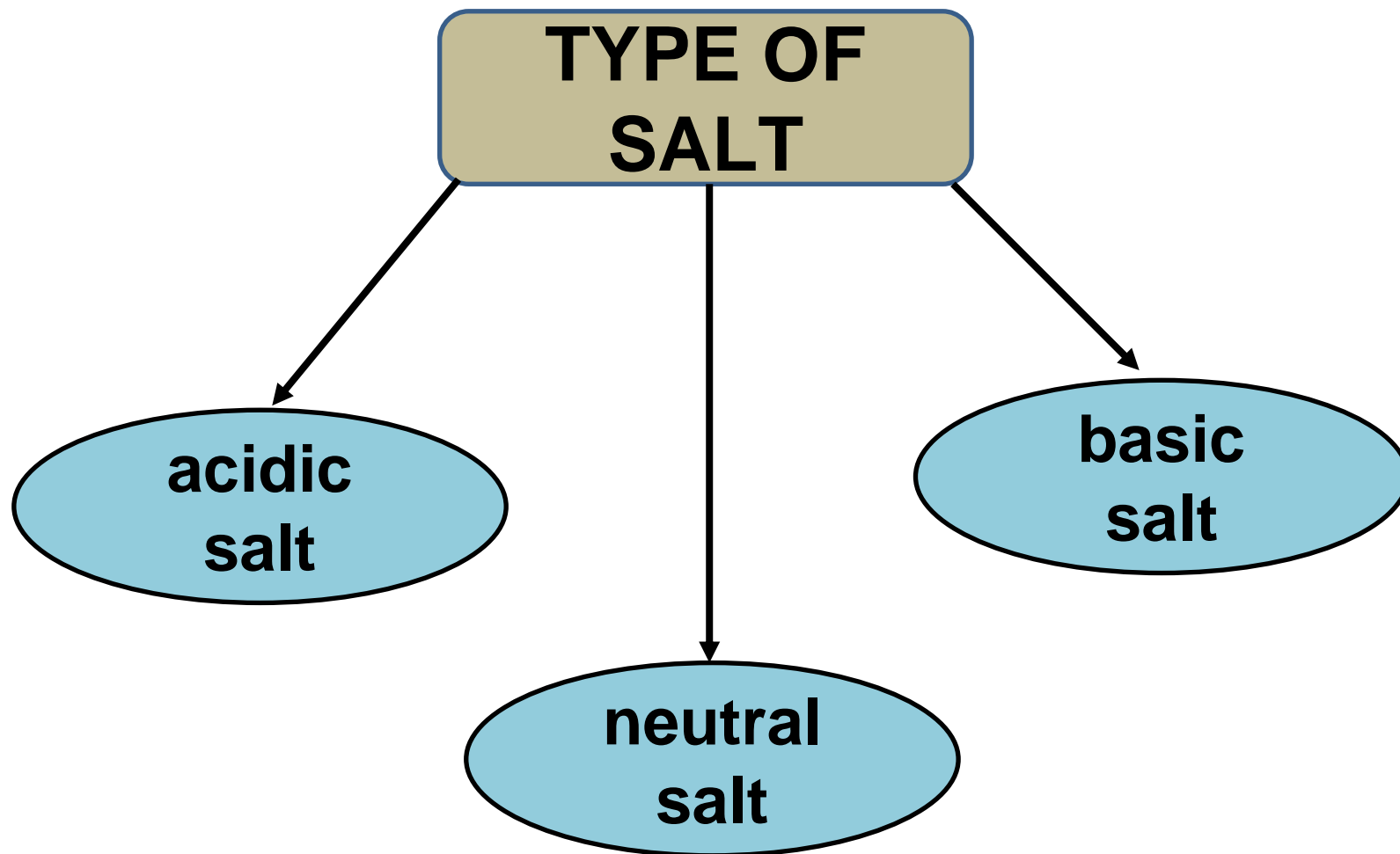


Cation Hydrolysis :



Anion Hydrolysis :

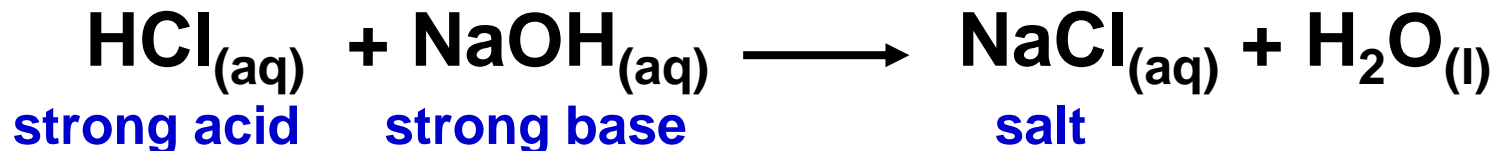




Neutral Salt

- * Produced when a **strong acid** reacts with a **strong base**.

- * Example: Sodium chloride, NaCl



- * Dissociation of salt :



Neutral Salt

- * Na^+ is **cation** of **strong base**, NaOH
 - ☞ Na^+ **does not hydrolyzed** in water
- * Cl^- is **anion** comes from **strong acid**, HCl
 - ☞ Cl^- **does not hydrolyzed** in water

Neutral Salt

So, **pH** of a **solution** depends on the **autoionization** of water



$$\begin{aligned} K_w &= [\text{H}_3\text{O}^+] [\text{OH}^-] \\ &= 1 \times 10^{-14} \end{aligned}$$

$$[\text{H}^+] = [\text{OH}^-] = 1.0 \times 10^{-7} \text{ M}$$

$$\text{pH} = 7$$

Basic Salt

* Produced from the reaction of **weak acid** and **strong base**.

* Example : Sodium ethanoate, CH_3COONa



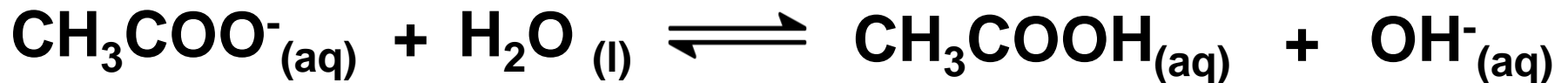
Basic Salt

- * Na^+ is cation of strong base, NaOH

- ☞ Na^+ does not hydrolyzed in water

- * CH_3COO^- is conjugate base of weak acid, CH_3COOH

- ☞ CH_3COO^- is hydrolyzed in water to produce OH^-



- ☞ The solution is **basic** because **OH^-** formed

- ☞ **$\text{pH} > 7.0$**

Acidic Salt

- * Produced from the reaction of **strong acid** and **weak base**.

- * Example : Ammonium chloride, NH_4Cl



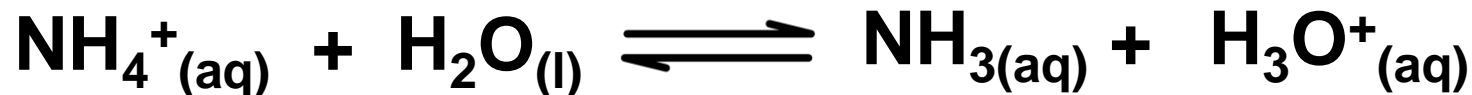
Acidic Salt

* Cl^- is anion of strong acid, HCl

☞ Cl^- does not hydrolyzed in water

* NH_4^+ is conjugate acid of weak base, NH_3

☞ NH_4^+ is hydrolyzed in water to produce H_3O^+



☞ The solution is **acidic** because H_3O^+ formed

☞ $\text{pH} < 7.0$

Example 1:

Sodium cyanide, NaCN is a salt formed when a strong base, NaOH is reacted with a weak acid, HCN.

Write a balanced equation to show the reaction between NaOH and HCN. Classify the salt formed.

What would be expected pH of the NaCN solution? Explain the answer using equation(s).

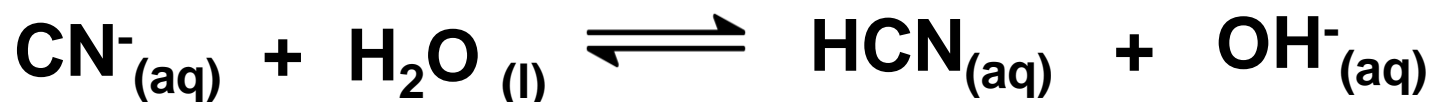
Answer :

* Na^+ is cation of strong base, NaOH

☞ Na^+ does not hydrolyzed in water

* CN^- is conjugate base of weak acid, HCN

☞ CN^- is hydrolyzed in water to produce OH^-



☞ The solution is **basic** because **OH^-** formed

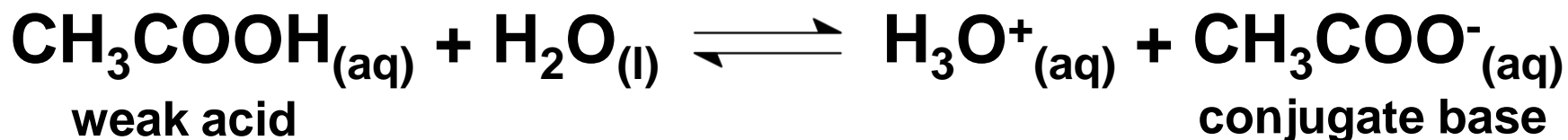
☞ **$\text{pH} > 7.0$**

7.1 j) Buffer Solutions

- A solution which has the **ability to maintain its pH** when a small amount of **strong acid or strong base** is added to the solution.
- Two types of buffer solutions :
 - i. acidic buffer solution ($\text{pH} < 7$)
 - ☞ a solution that contains a weak acid and its salt (or its conjugate base)
 - ii. basic buffer solution ($\text{pH} > 7$)
 - ☞ a solution that contains a weak base and its salt (or its conjugate acid)

Acidic Buffer Solution

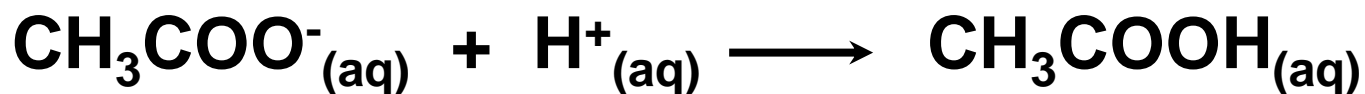
- ☞ A solution that contains a mixing of weak acid and its salt (or its conjugate base).
- ☞ Example : CH_3COOH and CH_3COONa .



7.1 k) How the Acidic Buffer Solution Works?

When a small amount of strong acid is added,

- ✚ The H^+ ions will react with ethanoate ion, CH_3COO^- to form CH_3COOH .

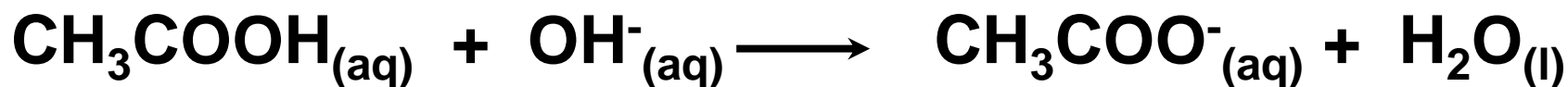


- ✚ As a result, $[\text{CH}_3\text{COOH}]$ increases and $[\text{CH}_3\text{COO}^-]$ decreases.
- ✚ $[\text{H}^+]$ & $[\text{OH}^-]$ remains constant.
- ✚ Therefore, pH not much affected.

How the Acidic Buffer Solution Works?

When a small amount of strong base is added,

- ➡ The OH^- ions will be neutralized by the acid, CH_3COOH to form CH_3COO^- and H_2O .



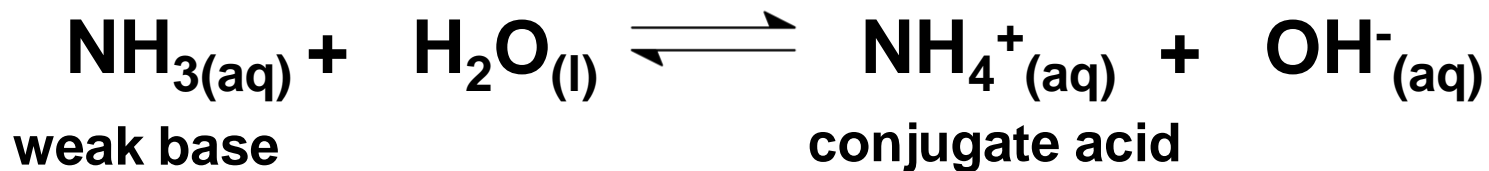
- ➡ As a result, $[\text{CH}_3\text{COO}^-]$ increases and $[\text{CH}_3\text{COOH}]$ decreases.

- ➡ $[\text{H}^+]$ & $[\text{OH}^-]$ remains constant.

- ➡ Therefore, pH not much affected.

Basic Buffer Solution

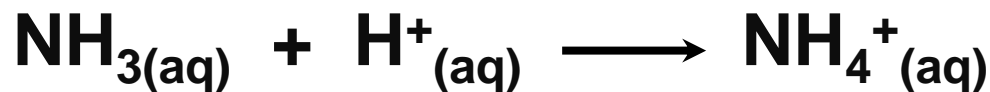
- A solution that contains a mixing of weak base and its salt (or its conjugate acid).
- Example : NH_3 and NH_4Cl



How the Basic Buffer Solution Works?

When a small amount of strong acid is added,

- The H^+ ions will be consumed by the ammonia, NH_3 to form NH_4^+ ion.



- As a result, $[\text{NH}_4^+]$ increases and $[\text{NH}_3]$ decreases.
- $[\text{H}^+]$ & $[\text{OH}^-]$ remains constant.
- Therefore, pH not much affected.

How the Basic Buffer Solution Works?

When a small amount of strong base is added,

➡ The OH^- ions will be neutralised by **the ammonium ions**, NH_4^+ to form NH_3 and H_2O .



➡ As a result, $[\text{NH}_3]$ increases and $[\text{NH}_4^+]$ decreases.

➡ $[\text{H}^+]$ & $[\text{OH}^-]$ remains constant.

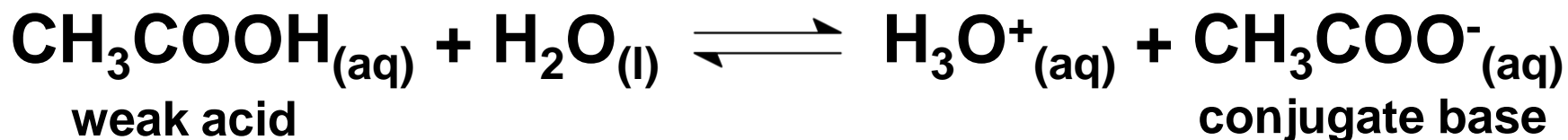
➡ Therefore, pH not much affected.

7.1 I) Henderson-Hasselbalch Equation & Its Application

Acidic Buffer Solution

☞ Example : CH_3COOH and CH_3COONa .

☞ Equations :



☞ Henderson-Hasselbalch equation : salt


$$\text{pH} = \text{pK}_a + \log \frac{[\text{conjugate base}]}{[\text{weak acid}]}$$

Acidic Buffer Solution

From the equations :
$$K_a = \frac{[\text{CH}_3\text{COO}^-] [\text{H}_3\text{O}^+]}{[\text{CH}_3\text{COOH}]}$$

∴ Henderson-Hasselbalch equation for acidic buffer solution:

$$\text{pH} = \text{p}K_a + \log \frac{[\text{CH}_3\text{COO}^-]}{[\text{CH}_3\text{COOH}]}$$

$$\text{p}K_a = -\log K_a$$

Example 1:

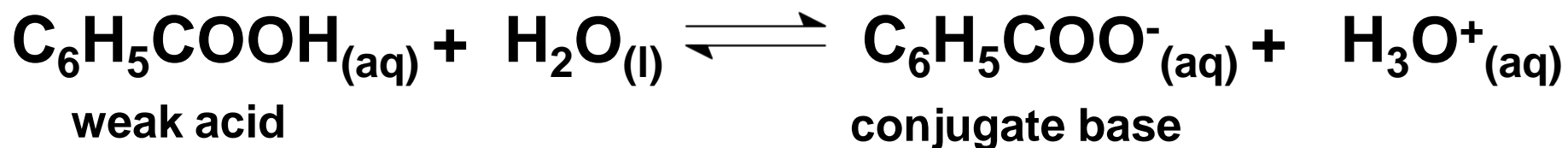
A buffer solution is prepared by adding 2.00 g of benzoic acid, $\text{C}_6\text{H}_5\text{COOH}$ & 2.00 g sodium benzoate, $\text{C}_6\text{H}_5\text{COONa}$ in enough water to make 1.00 L solution.

$(K_a(\text{C}_6\text{H}_5\text{COOH}) = 6.3 \times 10^{-5} \text{ M})$

(i) Write its Henderson-Hasselbalch equation.

(ii) Calculate the pH of a solution.

Answer :



∴ Henderson-Hasselbalch equation :

$$\text{pH} = \text{pK}_a + \log \frac{[\text{C}_6\text{H}_5\text{COO}^-]}{[\text{C}_6\text{H}_5\text{COOH}]}$$

$$\text{Mol C}_6\text{H}_5\text{COOH} = \frac{2.00 \text{ g}}{122.1 \text{ g mol}^{-1}} = 1.64 \times 10^{-2} \text{ mol}$$

$$[\text{C}_6\text{H}_5\text{COOH}] = \frac{1.64 \times 10^{-2} \text{ mol}}{1.00 \text{ L}} = 1.64 \times 10^{-2} \text{ M}$$

$$\text{Mol C}_6\text{H}_5\text{COO}^- = \frac{2.00 \text{ g}}{144 \text{ g mol}^{-1}} = 1.39 \times 10^{-2} \text{ mol}$$

$$[\text{C}_6\text{H}_5\text{COO}^-] = \frac{1.39 \times 10^{-2} \text{ mol}}{1.00 \text{ L}} = 1.39 \times 10^{-2} \text{ M}$$

$$\text{pH} = \text{pK}_a + \log \frac{[\text{C}_6\text{H}_5\text{COO}^-]}{[\text{C}_6\text{H}_5\text{COOH}]}$$

$$\begin{aligned}\text{pH} &= -\log 6.3 \times 10^{-5} + \log \frac{1.39 \times 10^{-2}}{1.64 \times 10^{-2}} \\ &= 4.13\end{aligned}$$

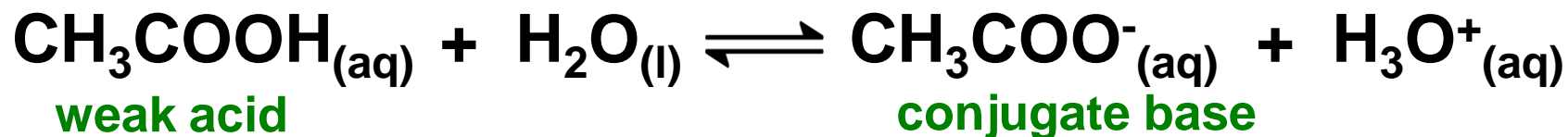
Example 2:

A buffer solution is prepared by dissolving 0.025 mol CH_3COONa in 250 cm^3 aqueous solution of CH_3COOH (0.10 mol dm^{-3}). Calculate the pH of the buffer solution.

$$\text{K}_a (\text{CH}_3\text{COOH}) = 1.74 \times 10^{-5} \text{ mol dm}^{-3}$$

(Assume addition of CH_3COONa does not change the volume of solution)

Answer :



$$[\text{CH}_3\text{COO}^{-}] = \frac{0.025 \text{ mol}}{0.250 \text{ dm}^3} = 0.10 \text{ mol dm}^{-3}$$

$$\text{pH} = \text{pK}_a + \log \frac{[\text{CH}_3\text{COO}^{-}]}{[\text{CH}_3\text{COOH}]}$$

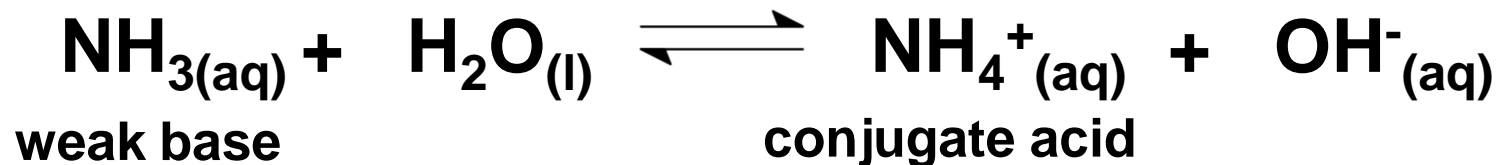
$$= -\log (1.74 \times 10^{-5}) + \log \frac{0.10}{0.10}$$

$$= 4.76$$

Basic Buffer Solution

👉 **Example : NH_3 and NH_4Cl**

Equations :



Henderson-Hasselbalch equation : **salt**

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{conjugate acid}]}{[\text{weak base}]}$$

Basic Buffer Solution

From the equations : $K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]}$

∴ Henderson-Hasselbalch equation for basic buffer solution:

$$\text{pOH} = \text{p}K_b + \log \frac{[\text{NH}_4^+]}{[\text{NH}_3]}$$

$$\text{p}K_b = -\log K_b$$

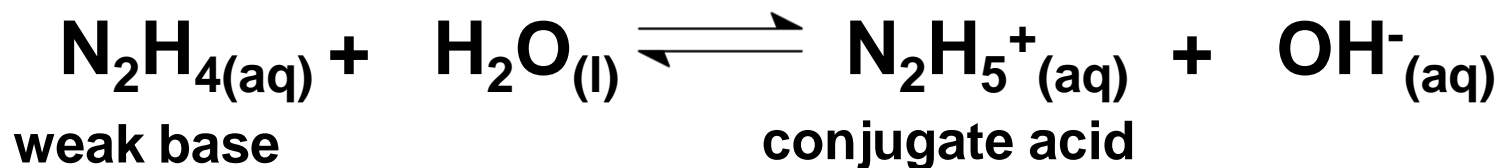
Example 3:

**A buffer solution is prepared by mixing 500 mL 0.1 M hydrazinium chloride, $\text{N}_2\text{H}_5\text{Cl}$ with 500 mL 0.2 M hydrazine, N_2H_4 .
($K_b = 1.7 \times 10^{-7}$)**

- (i) Write its Henderson-Hasselbalch equation.**
- (ii) Calculate the pH of a solution.**

Answer :

Equations :



∴ Henderson-Hasselbalch equation :

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{N}_2\text{H}_5^+]}{[\text{N}_2\text{H}_4]}$$

Answer :

salt

$$\text{No. of moles of } \text{N}_2\text{H}_5^+ = \frac{500 \text{ mL}}{1000} \times 0.1 \text{ M}$$

$$= 0.05 \text{ moles}$$

No. of mole
Volume of solution (L)

$$[\text{N}_2\text{H}_5^+] = \frac{0.05}{(0.50 + 0.50)}$$

500mL $\text{N}_2\text{H}_5\text{Cl}$
+ 500mL N_2H_4

$$= 0.05 \text{ M}$$

$$\text{No. of moles of N}_2\text{H}_4 = \frac{500 \text{ mL} \times 0.2 \text{ M}}{1000} = 0.1 \text{ mol}$$

$$[\text{N}_2\text{H}_4] = \frac{0.1}{(0.50 + 0.50)} = 0.1 \text{ M}$$

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{N}_2\text{H}_5^+]}{[\text{N}_2\text{H}_4]}$$

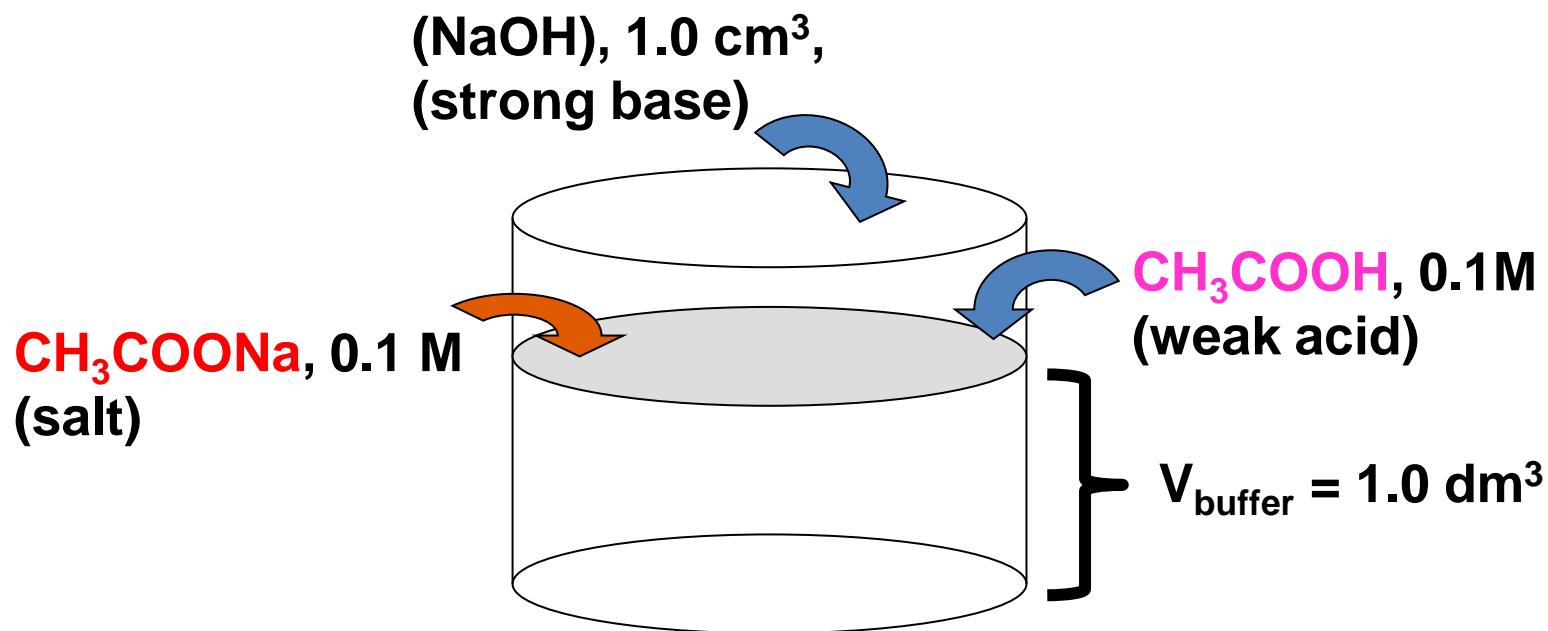
$$\begin{aligned} \text{pOH} &= -\log (1.7 \times 10^{-7}) + \log \frac{0.05}{0.1} \\ &= 6.47 \end{aligned}$$

$$\begin{aligned} \text{pH} &= 14 - \text{pOH} \\ &= 14 - 6.47 \\ &= \mathbf{7.53} \end{aligned}$$

7.1 m) Calculation pH of buffer solution before and after the addition of strong acid or base

Example 4:

Calculate the change in pH when 1.00 cm^3 of 1.00 M NaOH is added to a 1.00 dm^3 buffer solution which contains a mixture of 0.10 M , CH_3COOH and $0.10 \text{ M CH}_3\text{COONa}$ ($\text{p}K_a \text{ CH}_3\text{COOH} = 4.750$)



Answer :

pH before addition of NaOH

$$\text{pH} = \text{pK}_a + \log \frac{[\text{CH}_3\text{COO}^-]}{[\text{CH}_3\text{COOH}]}$$

$$= 4.750 + \log \frac{0.10}{0.10}$$

$$= 4.75$$

pH after addition of NaOH

$$\begin{aligned}\text{No. of moles of OH}^- \text{ ions in } 1.0 \text{ cm}^3 \text{ of } 1.0 \text{ mol dm}^{-3} \text{ NaOH} &= \frac{1.0 \times 1.0}{1000} \\ &= 1 \times 10^{-3} \text{ mol}\end{aligned}$$

$$\text{No. of moles of CH}_3\text{COOH} = 0.1 \times 1.0 = 0.1 \text{ mol}$$

$$\text{No. of moles of CH}_3\text{COO}^- = 0.1 \times 1.0 = 0.1 \text{ mol}$$

$$\text{Final volume of buffer} = 1.001 \text{ dm}^3$$

Buffer action :

	$\text{CH}_3\text{COOH}_{(\text{aq})}$	$+$	$\text{OH}^{-}_{(\text{aq})}$	\longrightarrow	$\text{CH}_3\text{COO}^{-}_{(\text{aq})}$	$+$	$\text{H}_2\text{O}_{(\text{l})}$
$(\text{mol})_{\text{initial}}$	0.100		1×10^{-3}		0.100		-
$(\text{mol})_{\text{change}}$	-1×10^{-3}		-1×10^{-3}		$+1 \times 10^{-3}$		-
$(\text{mol})_{\text{equilibrium}}$	0.099		0		0.101		-

$$[\text{CH}_3\text{COOH}]_{\text{new}} = \frac{0.099}{1.001}$$

$$= 0.0989 \text{ M}$$

$$[\text{CH}_3\text{COO}^{-}]_{\text{new}} = \frac{0.101}{1.001}$$

$$= 0.1009 \text{ M}$$

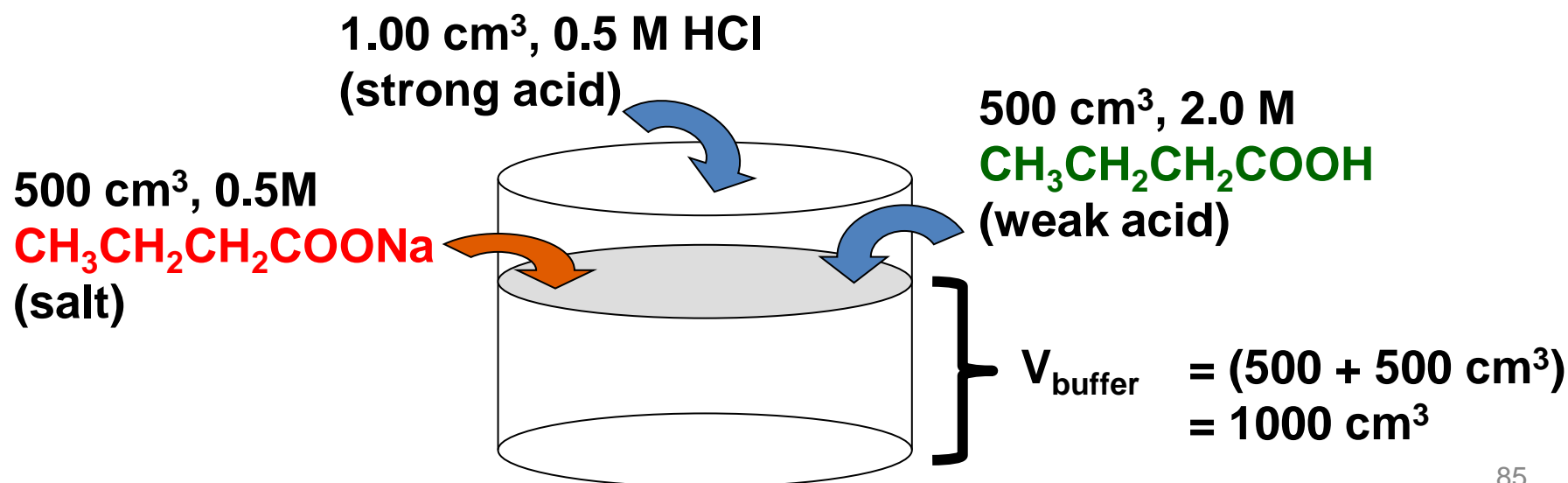
$$\text{pH} = \text{pK}_a + \log \frac{[\text{CH}_3\text{COO}^{-}]}{[\text{CH}_3\text{COOH}]}$$

$$= 4.750 + \log \frac{0.1009}{0.0989} = 4.75$$

Change in pH = 4.76 - 4.75 = 0.01 (small increase in pH)

Example 5:

A solution is made by mixing 500.00 cm³ of 2.00 M butanoic acid with 500.00 cm³ of 0.50 M sodium butanoate. Calculate the change in pH when 1.00 cm³ of 0.50 M HCl is added to 1.00 dm³ of the buffer solution. K_a for butanoic acid is 1.5×10^{-5} .



Answer :

pH before addition of HCl

$$\text{Mol CH}_3\text{CH}_2\text{CH}_2\text{COOH} = \frac{2.0 \times 500}{1000} = 1.00 \text{ mol}$$

$$\text{Mol CH}_3\text{CH}_2\text{CH}_2\text{COO}^- = \frac{0.5 \times 500}{1000} = 0.25 \text{ mol}$$

$$\text{volume of buffer solution} = 500 + 500 = 1000 \text{ cm}^3 = 1 \text{ L}$$

$$[\text{CH}_3\text{CH}_2\text{CH}_2\text{COOH}] = \frac{1.00}{1.00} = 1.00 \text{ M}$$

$$[\text{CH}_3\text{CH}_2\text{CH}_2\text{COO}^-] = \frac{0.25}{1.00} = 0.25 \text{ M}$$

pH before the addition of HCl

$$\text{pH} = \text{pK}_a + \log \frac{[\text{CH}_3\text{CH}_2\text{CH}_2\text{COO}^-]}{[\text{CH}_3\text{CH}_2\text{CH}_2\text{COOH}]}$$

$$= -\log (1.50 \times 10^{-5}) + \log \frac{0.25}{1.00}$$

$$= 4.2218$$

pH after the addition of HCl

$$\begin{aligned}\text{No. of moles of HCl added} &= \frac{0.5 \times 1.00}{1000} \\ &= 5.0 \times 10^{-4} \text{ mol}\end{aligned}$$

$$\begin{aligned}\text{Final volume of buffer} &= 1000 + 1.00 = 1001 \text{ cm}^3 \\ &= 1.001 \text{ L}\end{aligned}$$

Buffer action :

$\text{CH}_3\text{CH}_2\text{CH}_2\text{COO}^-_{(\text{aq})} + \text{H}^+_{(\text{aq})} \longrightarrow \text{CH}_3\text{CH}_2\text{CH}_2\text{COOH}_{(\text{aq})}$			
$(\text{mol})_{\text{initial}}$	0.250	5×10^{-4}	1.000
$(\text{mol})_{\text{change}}$	$- 5 \times 10^{-4}$	$- 5 \times 10^{-4}$	$+ 5 \times 10^{-4}$
$(\text{mol})_{\text{final}}$	0.2495	0	1.0005

$$[\text{CH}_3\text{CH}_2\text{CH}_2\text{COO}^-]_{\text{new}} = \frac{0.2495}{1.001} = 0.2493 \text{ M}$$

$$[\text{CH}_3\text{CH}_2\text{CH}_2\text{COOH}]_{\text{new}} = \frac{1.0005}{1.001} = 0.9995 \text{ M}$$

$$\begin{aligned} \text{pH} &= \text{pK}_a + \log \frac{[\text{CH}_3\text{CH}_2\text{CH}_2\text{COO}^-]}{[\text{CH}_3\text{CH}_2\text{CH}_2\text{COOH}]} \\ &= 4.824 + \log \frac{0.2493}{0.9995} = 4.2209 \end{aligned}$$

Change in pH = 4.2218 - 4.2209 = 0.0009 (small decrease in pH)

Example 6:

A buffer solution is prepared by mixing 400 mL of 1.50 M NH_4Cl solution with 600 mL of 0.10 M NH_3 .

(a) Calculate the pH of the buffer solution.

(b) Calculate the pH of the buffer solution after the addition of

(i) 0.015 mol NaOH

(ii) 0.011 mol HCl

(Assume that the volume of the solution does not change when HCl and NaOH is added)

[K_b for $\text{NH}_3 = 1.8 \times 10^{-5}$]

Answer :

(a) pH of the buffer solution

$$\text{Mol NH}_3 = \frac{0.1 \times 600}{1000} = 0.06 \text{ mol}$$

$$\text{Mol NH}_4^+ = \frac{1.5 \times 400}{1000} = 0.6 \text{ mol}$$

$$\text{volume of buffer solution} = 600 + 400 = 1000 \text{ cm}^3 = 1.00 \text{ L}$$

$$[\text{NH}_3] = \frac{0.06}{1.00} = 0.06 \text{ M}$$

$$[\text{NH}_4^+] = \frac{0.6}{1.00} = 0.6 \text{ M}$$

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{NH}_4^+]}{[\text{NH}_3]}$$

$$= -\log (1.8 \times 10^{-5}) + \log \frac{0.6}{0.06}$$

$$= 5.74$$

$$\text{pH} + \text{pOH} = 14$$

$$\text{pH} = 14 - 5.74$$

$$= 8.26$$

b) (i) pH of the buffer solution after the addition of 0.015 mol NaOH

	$\text{NH}_4^+(\text{aq})$	+	$\text{OH}^-(\text{aq})$	\longrightarrow	$\text{NH}_3(\text{aq})$	+	$\text{H}_2\text{O}(\text{l})$
(mol)_{initial}	0.60		0.015		0.06		-
(mol)_{change}	- 0.015		- 0.015		+ 0.015		-
(mol)_{equilibrium}	0.585		0		0.075		-

$$[\text{NH}_3]_{\text{new}} = \frac{0.075}{1 \text{ L}} = 0.075 \text{ M}$$

$$[\text{NH}_4^+]_{\text{new}} = \frac{0.585}{1 \text{ L}} = 0.585 \text{ M}$$

$$\text{pOH} = \text{pK}_b + \log \frac{[\text{NH}_4^+]}{[\text{NH}_3]}$$

$$= -\log (1.8 \times 10^{-5}) + \log \frac{0.585}{0.075} = 5.64$$

$$\text{pH} + \text{pOH} = 14$$

$$\text{pH} = 14 - 5.64 = 8.36$$

b) (ii) pH of the buffer solution after the addition of 0.011 mol HCl

	$\text{NH}_{3(\text{aq})}$	$+$	$\text{H}^+_{(\text{aq})}$	\longrightarrow	$\text{NH}_4^+_{(\text{aq})}$
(mol)_{initial}	0.06		0.011		0.60
(mol)_{change}	- 0.011		- 0.011		+ 0.011
(mol)_{final}	0.049		0		0.611

$$\begin{aligned} [\text{NH}_3]_{\text{new}} &= \frac{0.049}{1\text{L}} \\ &= 0.049 \text{ M} \end{aligned}$$

$$\begin{aligned} [\text{NH}_4^+]_{\text{new}} &= \frac{0.611}{1\text{L}} \\ &= 0.611 \text{ M} \end{aligned}$$

$$= -\log(1.8 \times 10^{-5}) + \log \frac{0.611}{0.049} = \mathbf{5.84}$$

$$\text{pH} + \text{pOH} = 14$$

$$\text{pH} = 14 - 5.84 = \mathbf{8.16}$$

Exercise:

A solution is prepared by mixing 100 cm³ aqueous NH₃ (0.1M) with 100 cm³ NH₄Cl (1.0 M). Calculate the pH of the solution before and after the addition of 1 cm³ HCl (0.1 M). Comment on the result.

($K_b \text{ NH}_3 = 1.74 \times 10^{-5} \text{ M}$)

Answer:

Before pH = 8.24

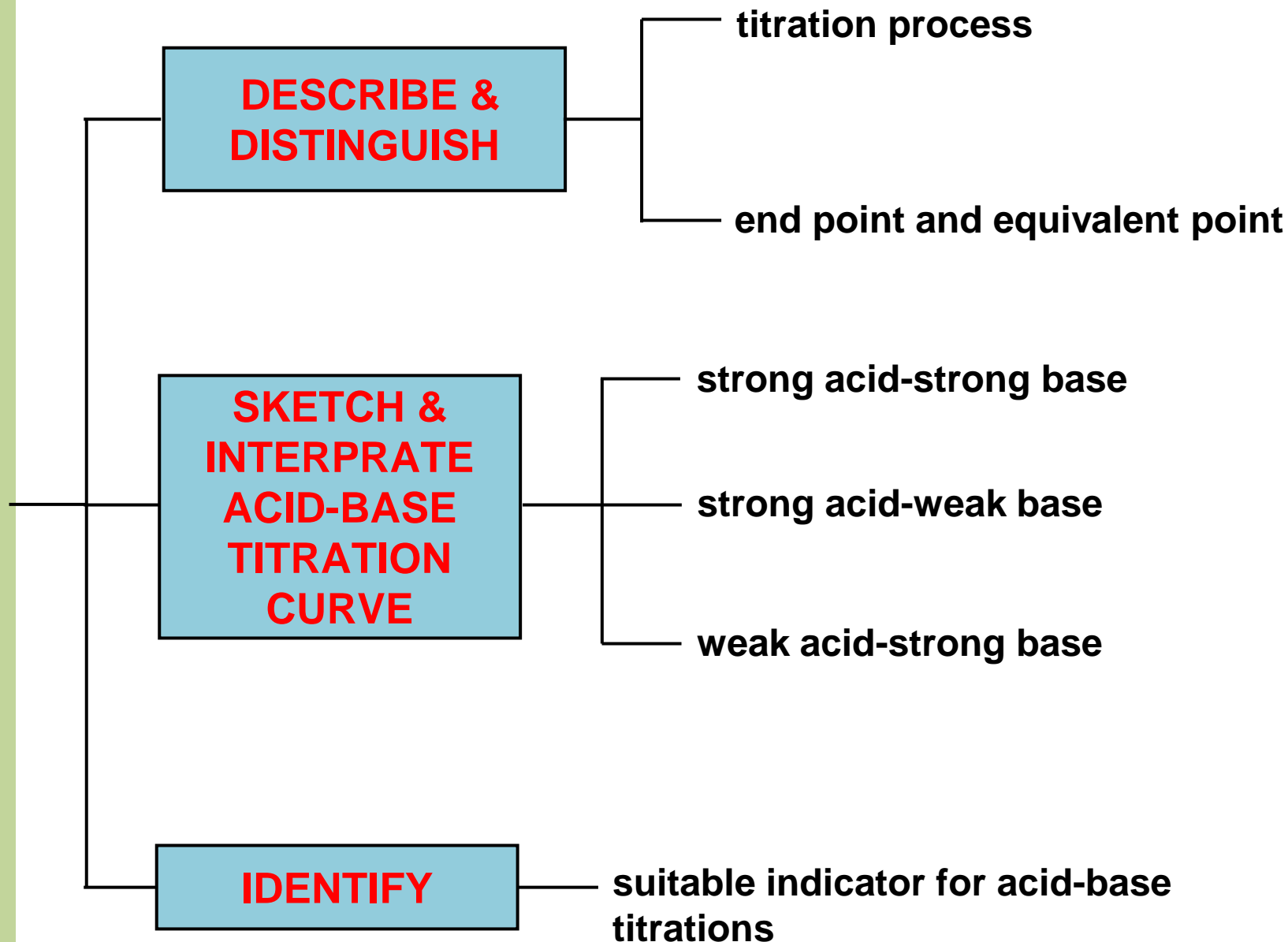
After pH = 8.24

7.2

ACID-BASE TITRATION



7.2 ACIDS – BASES TITRATION



TITRATION

Method for determining the concentration of an unknown solution by using another solution of known concentration (standard solution)

TITRANT

Standard solution is a solution of accurately known concentration

ANALYTE

The solution with unknown concentration

INDICATOR

A **weak organic acid** that has different color than its conjugate base and **color changes** occurring over a specific and relatively **narrow pH range**.

EQUIVALENT POINT

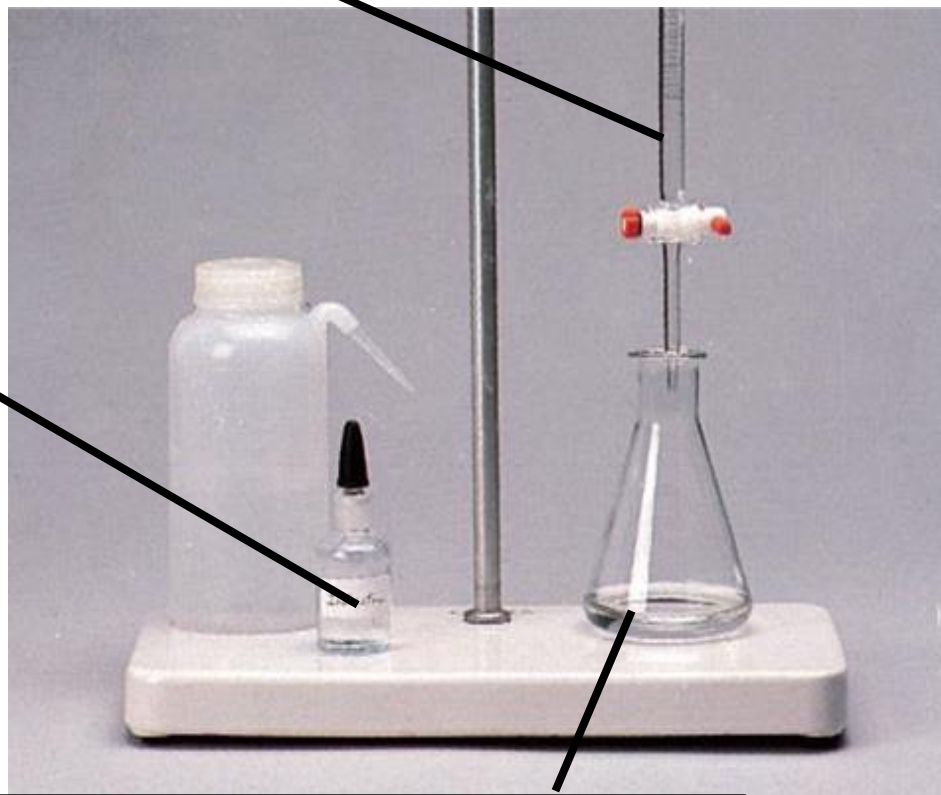
The point where the mole of acid and base is stoichiometrically equivalent @
mole of H^+ equals to mole of OH^-
(no more acid or base left in the solution)

END POINT

The point where an indicator **changes color**

Burette: (contains titrant)
Concentration of solution inside:
known Example: $\text{NaOH}(aq)$

Indicator:
(Example:
phenolphthalein)



Conical flask: (contains **analyte)**
Concentration of solution inside:
unknown Example: $\text{CH}_3\text{COOH}(aq)$

Acid-Base Titration Curve

A plot of the **pH** of a solution of acid (or base) versus the **volume** of base (or acid) **added** to the solution

TYPES OF TITRATION CURVE

✓ **Strong Acid-Strong Base**

✓ **Weak Acid-Strong Base**

✓ **Strong Acid-Weak Base**

**weak acid-weak base titration not normally done
because the equivalence point cannot be
accurately observed.**

How to Sketch a Titration Curve

- 1. Calculate the initial pH of an analyte (solution in the conical flask).**
- 2. Determine the equivalence point : the volume and its pH.**
- 3. Identify type of pH jump (steep portion)**
- 4. Identify the final pH.**
 - * depends on the [titrant] (solution in the burette).**

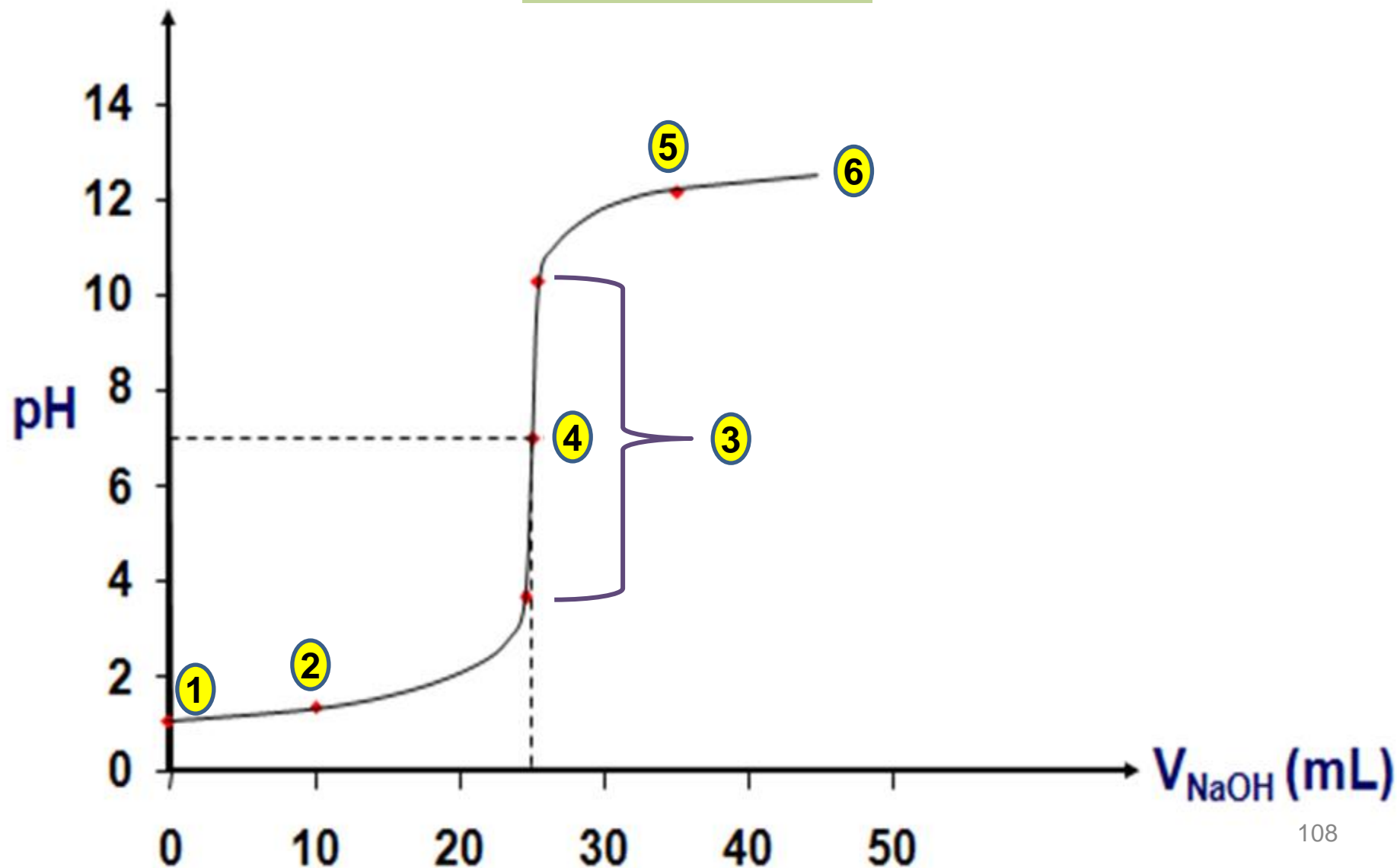
pH Jump (Steep Portion / Sharp Portion)

*** depends on the type of the titration**

Type	pH jump
strong acid – strong base	3 – 11
strong acid – weak base	3 – 7
weak acid – strong base	7 – 11

Strong Acid-Strong Base Titration Curve

Example :

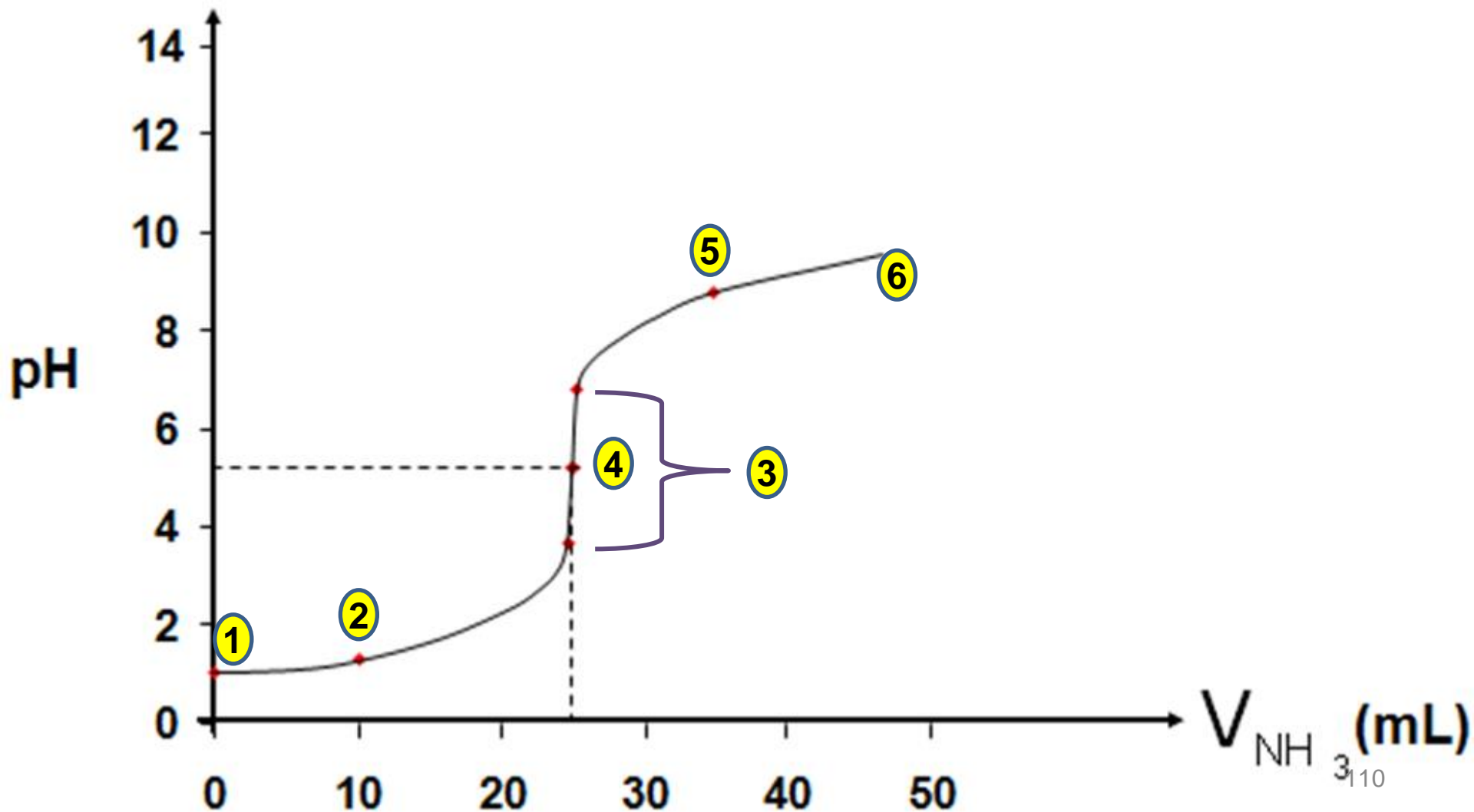


Description :

- ① HCl as a strong acid. $\text{pH} = -\log [\text{H}_3\text{O}^+]$
- ② NaOH is added. It makes $[\text{H}_3\text{O}^+]$ decreases. pH increases.
- ③ pH jump is 3-11
- ④ Equivalent point. Mole of H^+ equals to mole of OH^- . Neutral salt formed. $\text{pH} = 7$
- ⑤ Beyond equivalent point. pH increases slowly as excess OH^- added.
- ⑥ pH approaching 13.

Strong Acid-Weak Base Titration Curve

Example :

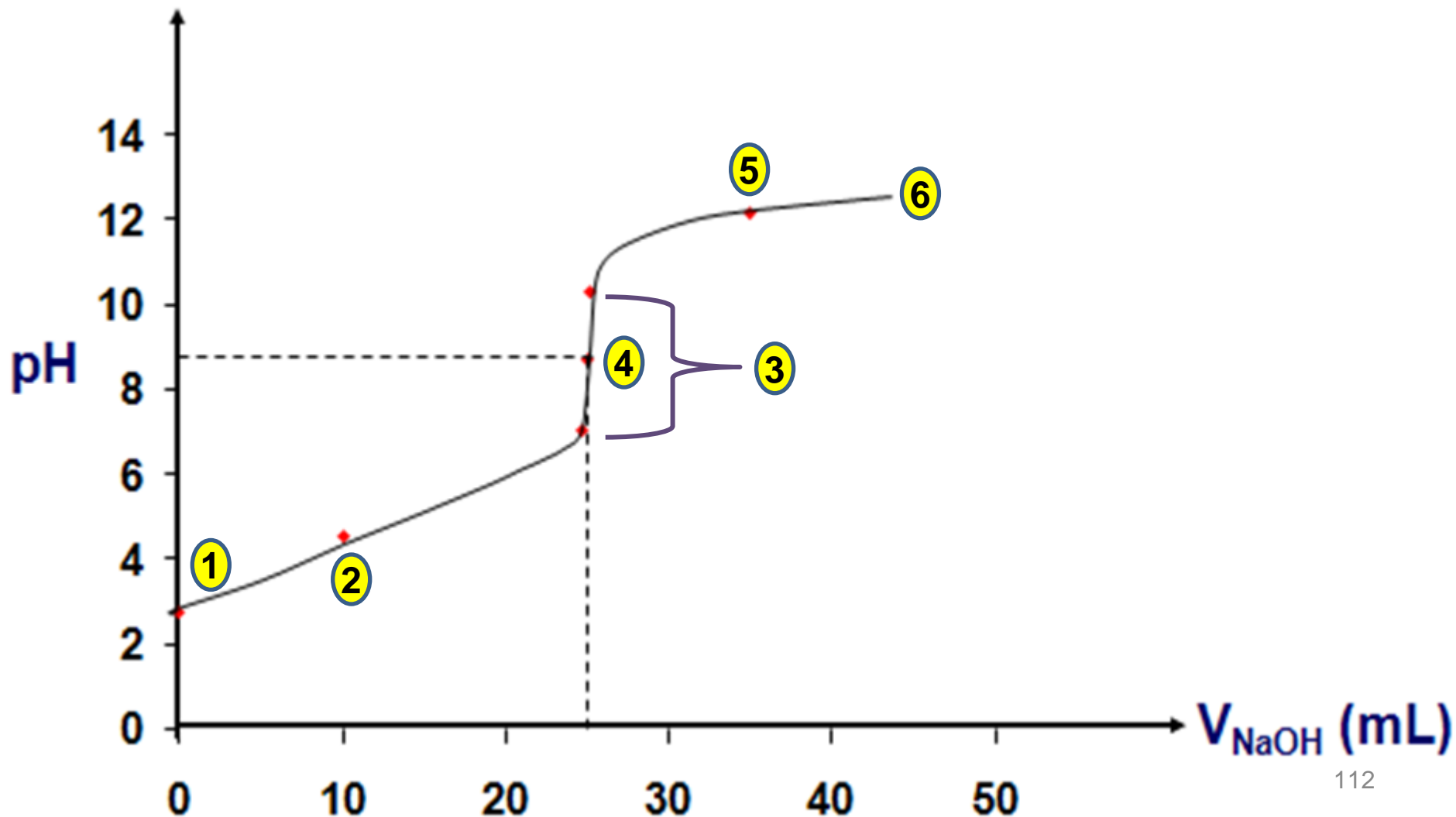


Description :

- ① HCl as a strong acid. $\text{pH} = -\log [\text{H}_3\text{O}^+]$
- ② NH_3 is added. It makes $[\text{H}_3\text{O}^+]$ decreases. pH increases.
- ③ pH jump is 3-7
- ④ Equivalent point. Mole of H^+ equals to mole of OH^- . Acidic salt formed. $\text{pH} < 7$
- ⑤ Beyond equivalent point. pH increases slowly as excess OH^- added.
- ⑥ pH approaching 11.

Strong Base-Weak Acid Titration Curve

Example :



Description :

- ① CH_3COOH as a weak acid partially dissociate. The pH is about 2.8.
- ② NaOH is added. It makes $[\text{H}_3\text{O}^+]$ decreases. pH increases.
- ③ pH jump is 7-11
- ④ Equivalent point. Mole of H^+ equals to mole of OH^- . Basic salt formed. $\text{pH} > 7$
- ⑤ Beyond equivalent point. pH increases slowly as excess OH^- added.
- ⑥ pH approaching 13.

Keep in mind!

- At the **midpoint** of the buffer region, **[base] = [acid]**, so the pH equals the pK_a

$$\text{pH} = pK_a + \log \left(\frac{[\text{base}]}{[\text{acid}]} \right)$$

$$\begin{aligned} \text{pH} &= pK_a + \log 1 = pK_a + 0 \\ &= pK_a \end{aligned}$$



In fact, observing the **pH** at the **midpoint** of the buffer region is a common experimental method for **estimating the pK_a** of an unknown acid

pH Calculation for Acid Base Titrations

Example 1 :

Sketch the titration curve of 25.0 mL 0.10 M HCl with 0.10 M NaOH.

Step 1 :

Analyte is a strong acid,

HCl – dissociates completely



$$[\text{H}^{\text{+}}] = [\text{HCl}] = 0.10 \text{ M}$$

$$\text{pH} = -\log [\text{H}^{\text{+}}]$$

$$= 1.0$$

Step 2 : At equivalence point



pH at equivalence:

- the solution is NaCl (aq)
- both Na^+ and Cl^- do not hydrolyse
- therefore pH = 7.0

Volume equivalence:

$$n_{\text{HCl}} = n_{\text{NaOH}}$$

$$M_{\text{HCl}} V_{\text{HCl}} = M_{\text{NaOH}} V_{\text{NaOH}}$$

$$V_{\text{NaOH}} = \frac{0.10 \times 25}{0.10} = 25 \text{ mL}$$

Step 3 :

pH jump : 3 – 11 (strong acid-strong base)

Step 4 :

Titrant is a strong base, NaOH.



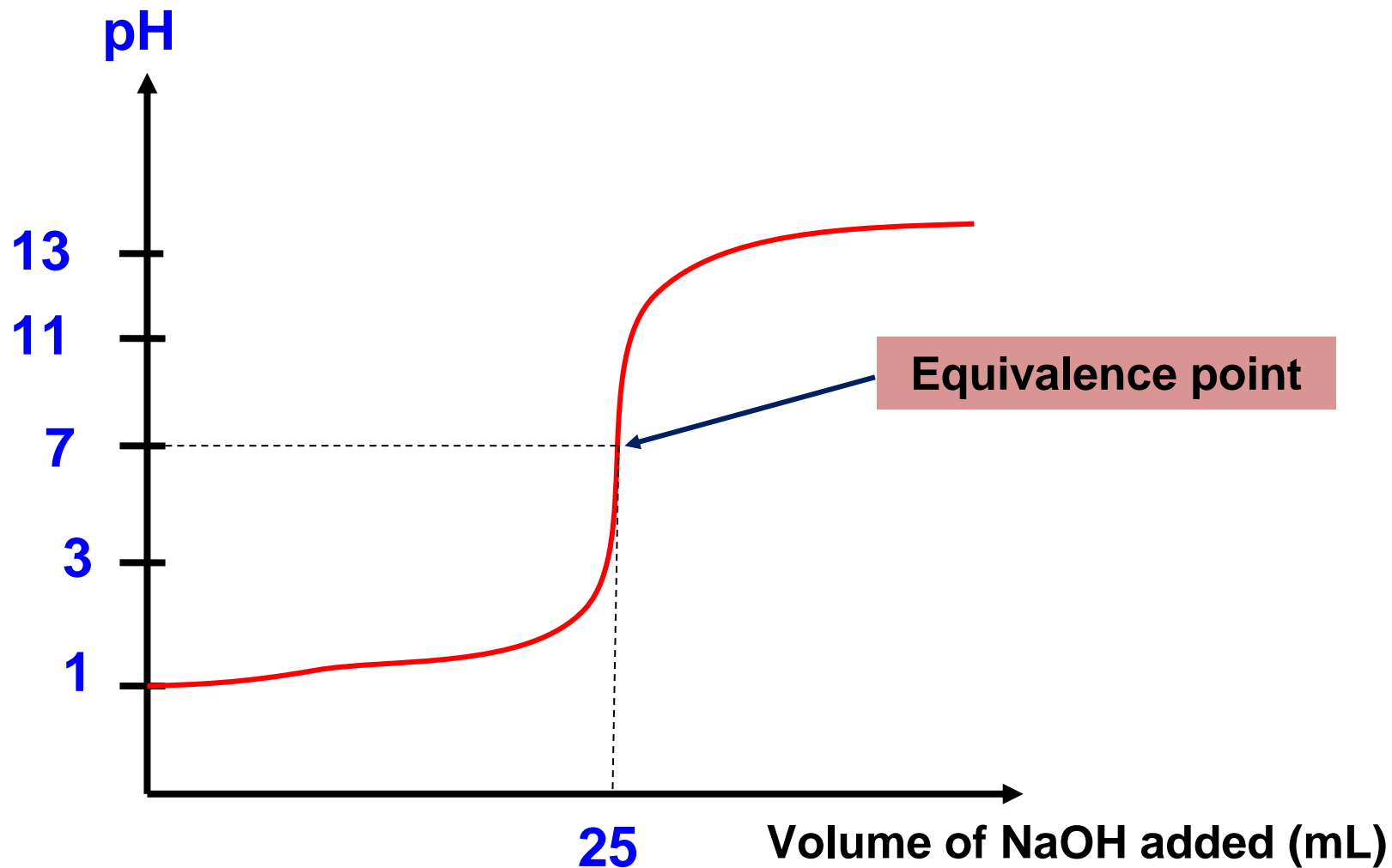
$$[\text{OH}^-] = [\text{NaOH}] = 0.10 \text{ M}$$

$$\text{pOH} = -\log 0.10 = 1$$

$$\begin{aligned} \text{pH} &= 14 - 1 \\ &= 13 \end{aligned}$$

Final point approaching pH < 13.

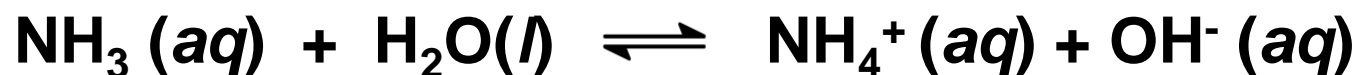
Sketch a titration curve



Example 2 :

Sketch the titration curve of 25.0 mL 0.10 M NH_3 and 0.10 M HCl.

Step 1 : Analyte is a weak base, NH_3



$$[\text{OH}^-] = [\text{x}] = \quad ?$$

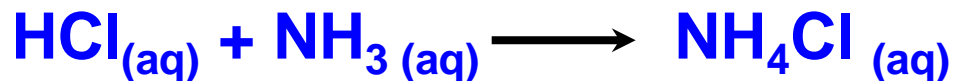
$$1.8 \times 10^{-5} = \frac{x^2}{0.10 - x}$$

$$[\text{x}] = [\text{OH}^-] = 1.3 \times 10^{-3} \text{ M}$$

$$\begin{aligned} \text{pOH} &= -\log(1.3 \times 10^{-3}) \\ &= 2.90 \end{aligned}$$

$$\begin{aligned} \text{pH} &= 14 - 2.90 \\ &= 11.10 \end{aligned}$$

Step 2 : At equivalence point



pH at equivalence

- the solution is $\text{NH}_4\text{Cl}_{(\text{aq})}$
- only NH_4^+ hydrolyses to form H_3O^+
- therefore $\text{pH} < 7.0$

Volume at equivalence

$$n \text{ NH}_3 = n \text{ HCl} \quad M_{\text{NH}_3} V_{\text{NH}_3} = M_{\text{HCl}} V_{\text{HCl}}$$

$$\frac{M_{\text{NH}_3} V_{\text{NH}_3}}{M_{\text{HCl}} V_{\text{HCl}}} = \frac{1}{1}$$

$$V_{\text{HCl}} = \frac{0.10 \times 25.0}{0.10} = 25 \text{ mL}$$

Step 3 :

Type of titration : strong acid-weak base

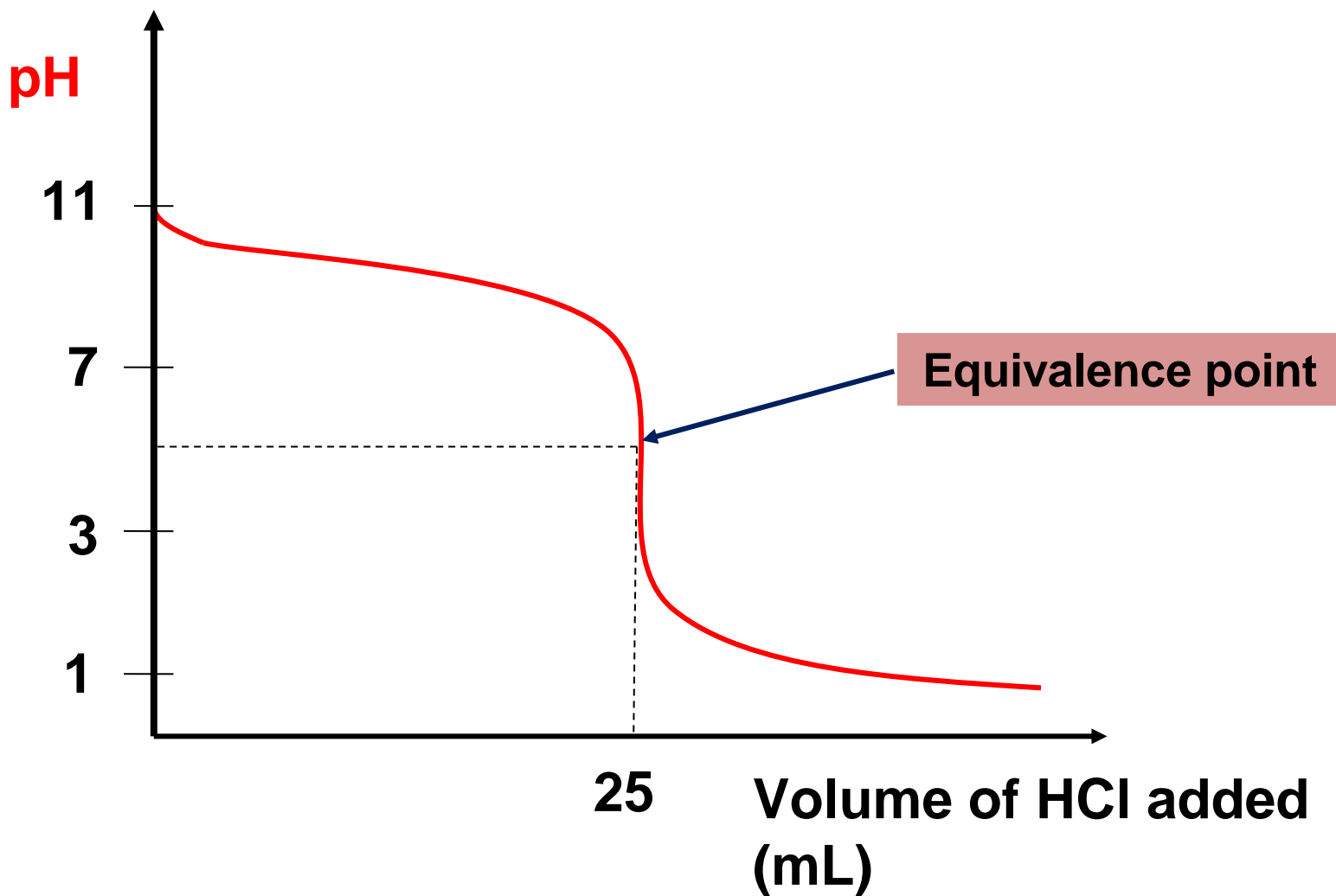
pH jump : 3 – 7

Step 4 :

Titrant is a strong acid, HCl.

Final point approaching pH < 2

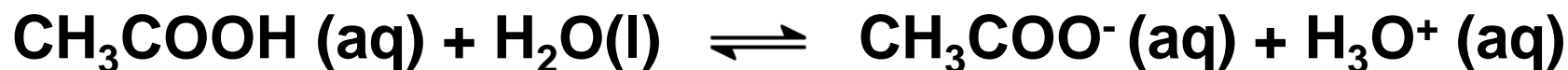
Sketch a titration curve



Example 3 :

Sketch the titration curve of 25.0 mL 0.10 M CH₃COOH and 0.10 M NaOH.

Step 1 : Analyte is a weak acid, CH₃COOH



$$[\text{H}_3\text{O}^+] = [\text{x}] = \quad ?$$

$$1.8 \times 10^{-5} = \frac{x^2}{0.10 - x}$$

$$[\text{x}] = [\text{H}_3\text{O}^+] = 1.3 \times 10^{-3} \text{ M}$$

$$\text{pH} = -\log(1.3 \times 10^{-3}) = 2.90$$

Step 2 : At equivalence point



- pH equivalence

- the solution is $\text{CH}_3\text{COONa}(\text{aq})$
- CH_3COO^- hydrolyses to form OH^-
- therefore $\text{pH} > 7.0$

- Volume equivalence

$$n \text{ CH}_3\text{COOH} = n \text{ NaOH}$$

$$M_{\text{CH}_3\text{COOH}} V_{\text{CH}_3\text{COOH}} = M_{\text{NaOH}} V_{\text{NaOH}}$$

$$V_{\text{NaOH}} = \frac{0.10 \times 25.0}{0.10} = 25 \text{ mL}$$

Step 3 :

Type of titration : **weak acid-strong base**

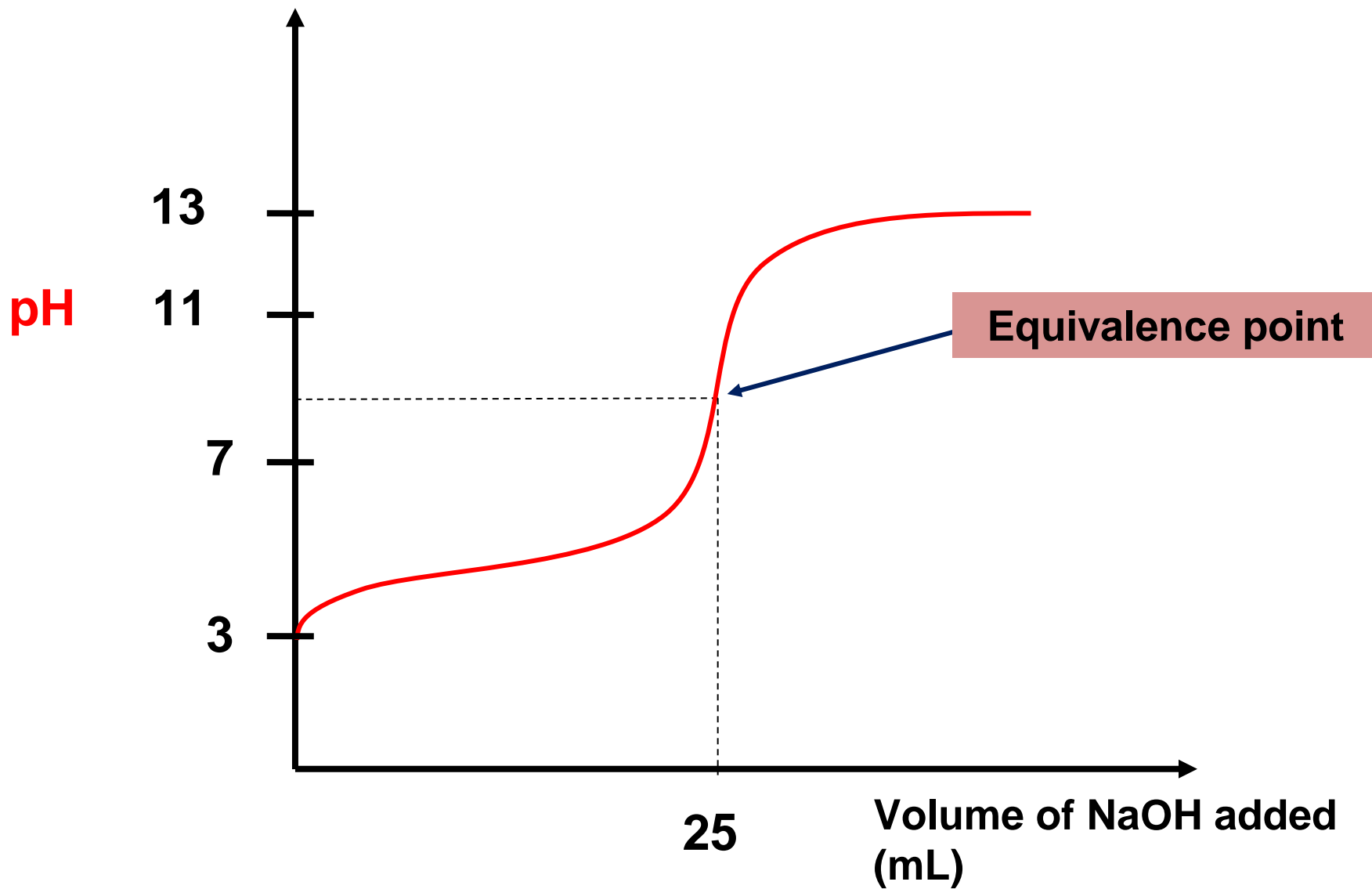
pH jump : 7 - 11

Step 4 :

Titrant is a strong base, NaOH.

Final point approaching $\text{pH} < 13$

Sketch a titration curve



7.2 e) Acid-base Titration Indicator

- Acid–base **indicator** is a weak organic acid that changes colour according to the concentration of hydrogen ions in the solution to which the indicator is added.
- The indicators can change colour because their ions have colours that are different from the undissociated molecule.

Some Common Acid–Base Indicators

Indicator	C o l o r		pH Range*
	In Acid	In Base	
Thymol blue	Red	Yellow	1.2–2.8
Bromophenol blue	Yellow	Bluish purple	3.0–4.6
Methyl orange	Orange	Yellow	3.1–4.4
Methyl red	Red	Yellow	4.2–6.3
Chlorophenol blue	Yellow	Red	4.8–6.4
Bromothymol blue	Yellow	Blue	6.0–7.6
Cresol red	Yellow	Red	7.2–8.8
Phenolphthalein	Colorless	Reddish pink	8.3–10.0

* The pH range is defined as the range over which the indicator changes from the acid color to the base color.

pH Ranges for Different Type of Titrations

Type of titrations	End point of pH Range	Suitable Indicators
strong acid-strong base	3 -11	any indicator (except thymol blue)
weak acid-strong base	7 - 11	phenolphthalein, cresol red
strong acid-weak base	3 - 7	methyl orange, methyl red, bromophenol blue, chlorophenol blue

EXAMPLE

What indicator would be suitable for the titration of each of these:

- (a) NaOH with HClO_4**
- (b) CH_3COOH with KOH**
- (c) NH_3 solution with HBr**

Explain your choices.

ANSWER

(a) NaOH (strong base) with HClO_4 (strong acid)

Suitable indicator : **bromothymol blue**

(b) CH_3COOH (weak acid) with KOH (strong base)

Suitable indicator : **phenolphthalein**

(c) NH_3 (weak base) solution with HBr (strong acid)

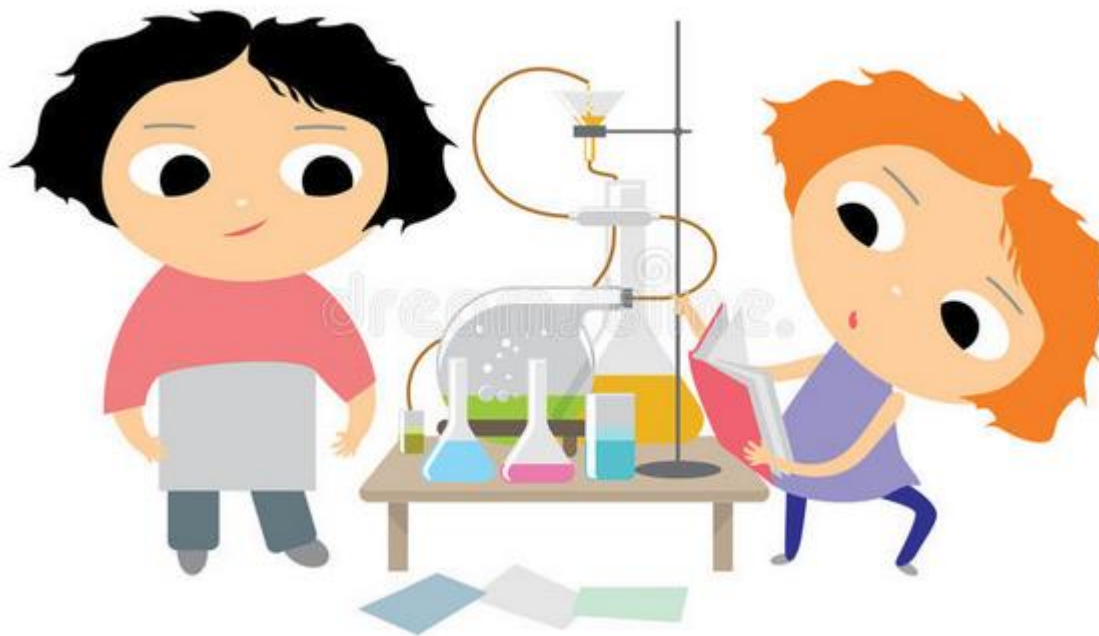
Suitable indicator : **methyl red**

Reason:

All indicators are chosen because the equivalence points are within the range of the pH color changes.

7.3

SOLUBILITY EQUILIBRIA



7.3 a) SALT SOLUBILITY

- Some salts are soluble but many are insoluble or slightly soluble in water.
- * The solubility of a salt is the **amount of solid that dissolved** in a **known value of saturated solution**.
- * The unit of solubility used may be **gL^{-1} or molL^{-1}**

Solubility (**s**)

- Mass of solute (g) dissolved in 1 L of a saturated solution.
- Unit : *g/L*

Molar solubility (**s**)

- Moles of solute dissolved in L of a saturated solution.
- Unit : *mol/L*

Solubility product (K_{sp})

- Is the product of the molar concentrations of the constituent ions, each raised to the power of its stoichiometric coefficient in the equilibrium equation.

EXAMPLE 1 :

Write the ion–product (K_{sp}) expression for each of the following:

(a) Silver carbonate

(a) Barium fluoride

(a) Copper(II) sulfide

(d) Iron(III) hydroxide

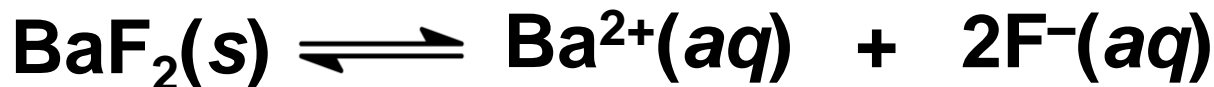
ANSWER

(a) Silver carbonate



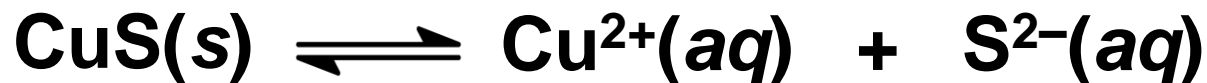
$$K_{\text{sp}} = [\text{Ag}^+]^2 [\text{CO}_3^{2-}]$$

(b) Barium fluoride



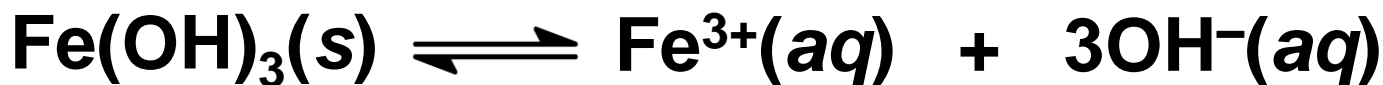
$$K_{\text{sp}} = [\text{Ba}^{2+}] [\text{F}^-]^2$$

(c) Copper(II) sulfide



$$K_{\text{sp}} = [\text{Cu}^{2+}] [\text{S}^{2-}]$$

(d) Iron(III) hydroxide



$$K_{\text{sp}} = [\text{Fe}^{3+}] [\text{OH}^{-}]^3$$

EXAMPLE 2 :

Write solubility equilibrium equations that are described by the following K_{sp} expressions.

For example, $K_{sp} = [Ag^+][Cl^-]$ represent as



ANSWER

$$(a) \quad K_{\text{sp}} = [\text{Ag}^+]^2 [\text{SO}_4^{2-}]$$



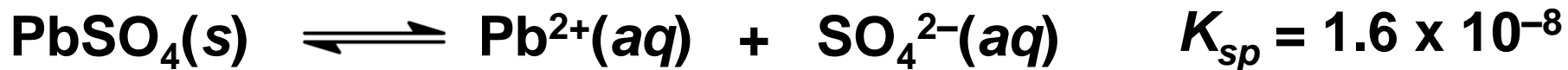
$$(b) \quad K_{\text{sp}} = [\text{Ni}^{2+}]^3 [\text{PO}_4^{3-}]^2$$



K_{sp} AND SOLUBILITY

- The **higher** the K_{sp} , the **greater** the solubility.
- The **higher** the temperature, the **greater** the K_{sp}

EXAMPLE:



MgCO_3 is more soluble than PbSO_4

7.3 b) SOLVING PROBLEMS INVOLVING K_{sp}

Two general types of problems:

- Determining K_{sp} from solubility (g/L) or molar solubility (mol/L)
- Determining solubility or molar solubility from K_{sp}

USE ***ICE*** TABLE

EXAMPLE 3 :

A particular saturated solution of PbI_2 has $[\text{Pb}^{2+}] = 5.0 \times 10^{-3} \text{ M}$ and $[\text{I}^-] = 1.3 \times 10^{-3} \text{ M}$.

- (a) What is the value of K_{sp} for PbI_2 ?**
- (b) What is $[\text{I}^-]$ in a saturated solution of PbI_2 that has $[\text{Pb}^{2+}] = 2.5 \times 10^{-4} \text{ M}$?**
- (c) What is $[\text{Pb}^{2+}]$ in a saturated solution has $[\text{I}^-] = 2.5 \times 10^{-4} \text{ M}$?**

ANSWER

(a) $[\text{Pb}^{2+}] = 5.0 \times 10^{-3} \text{ M}$ $[\text{I}^-] = 1.3 \times 10^{-3} \text{ M}$

K_{sp} of $\text{PbI}_2 = ?$

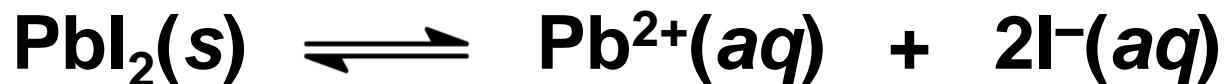


$$K_{\text{sp}} = [\text{Pb}^{2+}] [\text{I}^-]^2$$

$$= (5.0 \times 10^{-3}) \times (1.3 \times 10^{-3})^2$$

$$= 8.5 \times 10^{-9}$$

(b) $[\text{Pb}^{2+}] = 2.5 \times 10^{-4} \text{ M}$ $[\text{I}^-] = ?$



$$K_{\text{sp}} = [\text{Pb}^{2+}] [\text{I}^-]^2$$

$$[\text{I}^-]^2 = \frac{K_{\text{sp}}}{[\text{Pb}^{2+}]} = \frac{8.5 \times 10^{-9}}{(2.5 \times 10^{-4})}$$

$$[\text{I}^-] = 5.8 \times 10^{-3} \text{ M}$$

(c) $[I^-] = 2.5 \times 10^{-4} \text{ M}$ $[Pb^{2+}] = ?$



$$K_{sp} = [Pb^{2+}] [I^-]^2$$

$$[Pb^{2+}] = \frac{K_{sp}}{[I^-]^2} = \frac{8.5 \times 10^{-9}}{(2.5 \times 10^{-4})^2}$$

$$[Pb^{2+}] = 0.136 \text{ M}$$

EXAMPLE 4:

The molar solubility of AgBr is 7.1×10^{-7} M at 25°C. Calculate K_{sp} for AgBr at this temperature.

ANSWER

	$\text{AgBr}(s) \rightleftharpoons$	$\text{Ag}^+(aq)$	$+$	$\text{Br}^-(aq)$
$[]_i (M)$	—	0		0
$\Delta (M)$	—	$+ s$		$+ s$
$[]_{eq} (M)$	—	s		s

$$K_{sp} = [\text{Ag}^+] [\text{Br}^-]$$

$$= (s) \times (s)$$

$$= s^2 = (7.1 \times 10^{-7})^2$$

$$= 5.0 \times 10^{-13}$$

EXAMPLE 5:

The solubility of calcium sulphate is found experimentally to be 0.67 g/L.

Calculate the value of K_{sp} for calcium sulphate.

(Molar mass of CaSO_4 = 136.2 g/mol)

ANSWER

Convert solubility (g/L) to molar solubility (mol/L (*M*)):

$$\frac{0.67 \text{ g CaSO}_4}{1 \text{ L solution}} \times \frac{1 \text{ mol CaSO}_4}{136.2 \text{ g CaSO}_4}$$

$$= 4.9 \times 10^{-3} \text{ mol/L}$$

$$= 4.9 \times 10^{-3} \text{ M}$$



$[]_i (M)$

—

0

0

$\Delta(M)$

—

+ s

+ s

$[]_{\text{eq}} (M)$

—

s

s

$$K_{\text{sp}} = [\text{Ca}^{2+}] [\text{SO}_4^{2-}]$$

$$= (s) \times (s)$$

$$= s^2 = (4.9 \times 10^{-3})^2$$

$$= 2.4 \times 10^{-5}$$

EXAMPLE 6:

Calculate the molar solubility of PbCl_2 .

$$K_{\text{sp}} = 1.6 \times 10^{-5}$$

ANSWER

	$\text{PbCl}_2(\text{s})$	\rightleftharpoons	$\text{Pb}^{2+}(\text{aq})$	+	$2\text{Cl}^{-}(\text{aq})$
$[\]_i (M)$	—		0		0
$\Delta(M)$	—		+ s		+ 2s
$[\]_{\text{eq}} (M)$	—		s		2s

$$\begin{aligned}
 K_{\text{sp}} &= [\text{Pb}^{2+}] [\text{Cl}^{-}]^2 \\
 &= (s) \times (2s)^2 \\
 &= 4s^3 = 1.6 \times 10^{-5}
 \end{aligned}$$

$$s = 1.6 \times 10^{-2} M$$

So, the molar solubility of $\text{PbCl}_2 = 1.6 \times 10^{-2} M$

7.3 c) PREDICTING PRECIPITATION OF THE IONIC COMPOUNDS

- ☞ **Precipitate** is an insoluble solid formed in and separates from the solution
- ☞ **K_{sp} values** can be used to make general **prediction concerning precipitation reactions.**
- ☞ To predict whether a precipitate will form, **the ion- product, Q is compared with K_{sp} .**
- ☞ **Q has the same expression as K_{sp}** but the concentrations values are taken at any given time.

$$Q = K_{sp}$$

- ☞ Saturated solution formed
- ☞ System is in equilibrium

$$Q > K_{sp}$$

- ☞ Solution is supersaturated
- ☞ Reaction proceeds from right to left
- ☞ Precipitate will formed until the ionic concentration product of the system equals the K_{sp} ($Q = K_{sp}$)

$$Q < K_{sp}$$

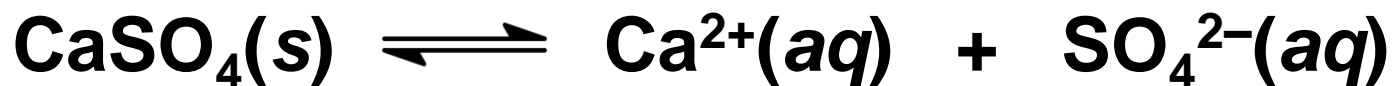
- ☞ Reaction proceeds from left to right
- ☞ Solution is unsaturated and no precipitate formed

EXAMPLE 7:

Will a precipitate of CaSO_4 form in a solution if the Ca^{2+} concentration is 0.0025 M and the SO_4^{2-} concentration is 0.030 M ?

(K_{sp} of $\text{CaSO}_4 = 2.4 \times 10^{-5}$)

ANSWER



$$K_{\text{sp}} = [\text{Ca}^{2+}] [\text{SO}_4^{2-}] = 2.4 \times 10^{-5}$$

$$[\text{Ca}^{2+}] = 0.0025 \text{ M}$$

$$[\text{SO}_4^{2-}] = 0.030 \text{ M}$$

$$\begin{aligned} Q &= [\text{Ca}^{2+}] [\text{SO}_4^{2-}] \\ &= (0.0025) \times (0.030) = 7.5 \times 10^{-5} \end{aligned}$$

$$Q > K_{\text{sp}}$$

So, CaSO_4 will precipitate until $Q = K_{\text{sp}}$

EXAMPLE 8:

Does a precipitate form when 0.100 L of 0.30 M $\text{Ca}(\text{NO}_3)_2$ is mixed with 0.200 L of 0.060 M NaF ?

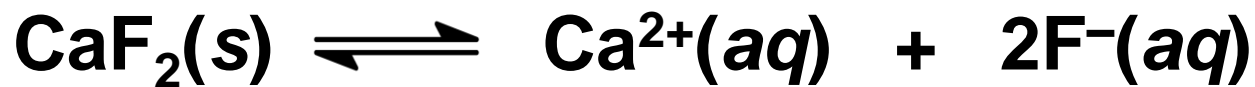
K_{sp} of $\text{CaF}_2 = 3.2 \times 10^{-11}$

ANSWER



Ions present: Ca^{2+} , NO_3^- , Na^+ , F^-

Possible precipitate = CaF_2



$$\begin{aligned} K_{\text{sp}} &= [\text{Ca}^{2+}] [\text{F}^-]^2 \\ &= 3.2 \times 10^{-11} \end{aligned}$$

Mol of $\text{Ca}(\text{NO}_3)_2$

= Molarity x volume of solution

= $0.30 \text{ mol/L} \times 0.100 \text{ L}$

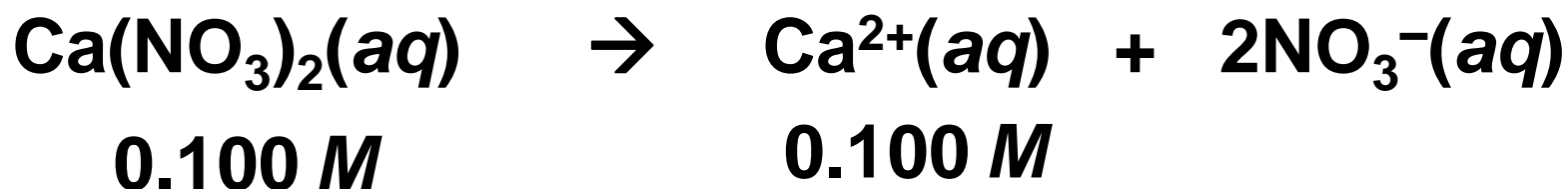
= $0.030 \text{ mol } \text{Ca}(\text{NO}_3)_2$

Total volume when $\text{Ca}(\text{NO}_3)_2$ mix with NaF

= $0.100 \text{ L} + 0.200 \text{ L}$

= 0.300 L

$$\begin{aligned}\text{Molarity of Ca(NO}_3)_2 \text{ solution} &= \frac{0.030 \text{ mol Ca(NO}_3)_2}{0.300 \text{ L}} \\ &= 0.100 \text{ M}\end{aligned}$$

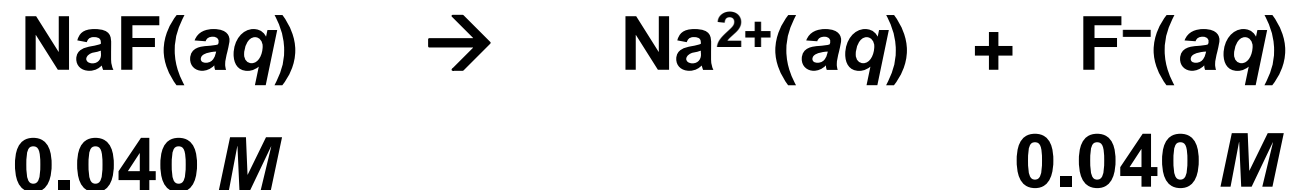


$$[\text{Ca}^{2+}] = 0.100 \text{ M}$$

$$\begin{aligned}\text{Mol of NaF} &= \text{Molarity} \times \text{Volume of solution} \\ &= 0.060 \text{ mol/L} \times 0.200 \text{ L} \\ &= 0.012 \text{ mol NaF}\end{aligned}$$

$$\begin{aligned}\text{Total volume when Ca(NO}_3)_2 \text{ mix with NaF} \\ &= 0.100 \text{ L} + 0.200 \text{ L} \\ &= 0.300 \text{ L}\end{aligned}$$

$$\begin{aligned}\text{Molarity of NaF solution} &= \frac{0.012 \text{ mol NaF}}{0.300 \text{ L}} \\ &= 0.040 \text{ M}\end{aligned}$$



$$[\text{F}^-] = 0.040 \text{ M}$$

$$[\text{Ca}^{2+}] = 0.100 \text{ M}$$

$$[\text{F}^{-}] = 0.040 \text{ M}$$

$$\begin{aligned} Q &= [\text{Ca}^{2+}] [\text{F}^{-}]^2 \\ &= (0.100) \times (0.040)^2 \\ &= 1.6 \times 10^{-4} \end{aligned}$$

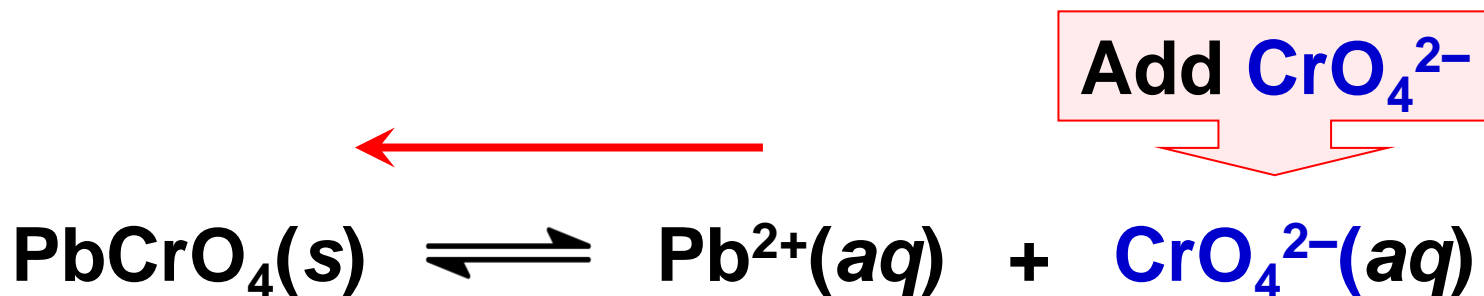
$$Q > K_{\text{sp}}$$

So, CaF_2 will precipitate until $Q = K_{\text{sp}}$

7.3 d) COMMON ION EFFECT

Shift of equilibrium caused by addition or the presence of a compound having an ion in common with the dissolved substance

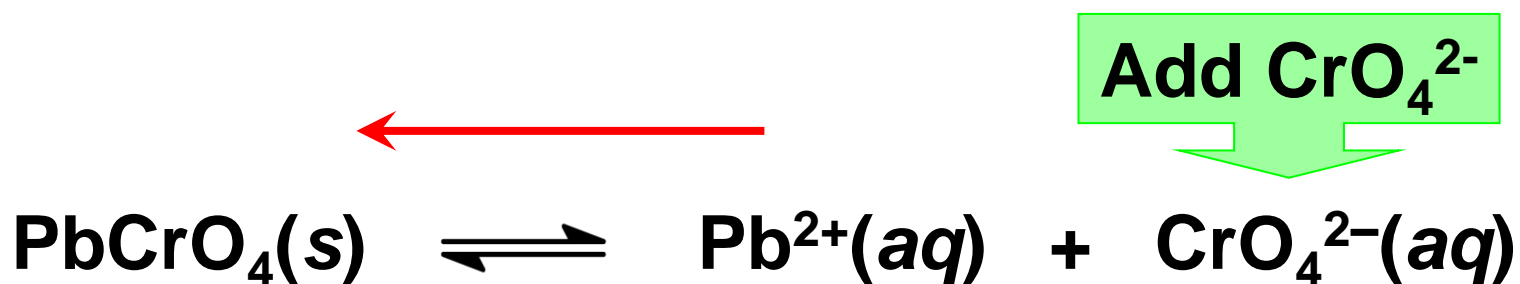
EXAMPLE:



Common ion: CrO_4^{2-}

➡ Presence of a common ion **decreases solubility** of slightly soluble ionic compound

EXAMPLE: Addition of Na_2CrO_4 (soluble salt) to saturated solution of PbCrO_4



$$\begin{aligned} K_{\text{sp}} &= [\text{Pb}^{2+}] [\text{CrO}_4^{2-}] \\ &= 2.3 \times 10^{-13} \end{aligned}$$

EXAMPLE:

Add CrO_4^{2-}



➤ Effect of the addition of common ion CrO_4^{2-} :

➤ $[\text{CrO}_4^{2-}]$ increase

➤ Position of equilibrium will shift to the left.
Some CrO_4^{2-} combine with Pb^{2+} to form
solid PbCrO_4

➤ Solubility of PbCrO_4 decrease

EXAMPLE 9:

What is the solubility (in M) of Ca(OH)_2 in $0.10\ M\ \text{Ca(NO}_3)_2$?

$$K_{\text{sp}} \text{ of } \text{Ca(OH)}_2 = 6.5 \times 10^{-6}$$

ANSWER



$[]_i (M)$	–	0.10	0
$\Delta(M)$	–	+ s	+ 2s
$[]_{\text{eq}} (M)$	–	0.1 + s	2s

Assume s is very small ~~is~~ $0.1 + s \approx 0.1$

$$\begin{aligned} K_{\text{sp}} &= [\text{Ca}^{2+}] [\text{OH}^{-}]^2 \\ &= (0.1) \times (2s)^2 \\ &= 0.4s^2 = 6.5 \times 10^{-6} \end{aligned}$$

$$s = 4.0 \times 10^{-3} M$$

So, the molar solubility of $\text{Ca(OH)}_2 = 4.0 \times 10^{-3} M$

EXAMPLE 10:

What is the molar solubility of AgBr in

(a) pure water

(b) 0.0010 M NaBr

(c) compare the solubility of AgBr in water and NaBr

$$K_{\text{sp}} \text{ of AgBr} = 7.7 \times 10^{-13}$$

ANSWER

(a)	$\text{AgBr}(s) \rightleftharpoons \text{Ag}^+(aq) + \text{Br}^-(aq)$	
$[]_i (M)$	–	0
$\Delta (M)$	–	+ s
$[]_{eq} (M)$	–	s

$$\begin{aligned}K_{sp} &= [\text{Ag}^+] [\text{Br}^-] \\&= (s) \times (s) \\&= s^2 = 7.7 \times 10^{-13}\end{aligned}$$

$$s = 8.8 \times 10^{-7} M$$

So, the molar solubility of AgBr in pure water = **$8.8 \times 10^{-7} M$**

(b)	$\text{AgBr(s)} \rightleftharpoons \text{Ag}^+(\text{aq}) + \text{Br}^-(\text{aq})$	
$[\text{ }]_i (\text{M})$	—	0
$\Delta (\text{M})$	—	+ s
$[\text{ }]_{\text{eq}} (\text{M})$	—	s
		0.0010 + s

s is very small $\Rightarrow 0.0010 + s \approx 0.0010$

$$K_{\text{sp}} = [\text{Ag}^+][\text{Br}^-]$$

$$= (s) \times (0.0010)$$

$$= 0.0010s = 7.7 \times 10^{-13}$$

$$s = 7.7 \times 10^{-10} \text{ M}$$

So, the molar solubility of AgBr in NaBr = $7.7 \times 10^{-10} \text{ M}$

molar solubility of AgBr in NaBr = $7.7 \times 10^{-10} \text{ M}$

molar solubility of AgBr in water = $8.8 \times 10^{-7} \text{ M}$

- ☞ The solubility of AgBr in NaBr is **lower** than in water.
- ☞ The presence of the **common ion Br⁻** increases the concentration of Br⁻ ion and thus shifts the equilibrium position to the left. Hence increase the formation of AgBr and decrease/reduce the solubility

EXERCISE 1:

K_{sp} for AgCl is 1.7×10^{-10} . Calculate the molar solubility of AgCl in:

i. Water

$[1.30 \times 10^{-5} \text{ M}]$

ii. In a solution of 0.1 mol dm^{-3} KCl.

$[1.70 \times 10^{-9} \text{ M}]$

EXERCISE 2

1. It was found experimentally that the solubility of calcium sulphate is 0.67 g L^{-1} . Calculate the K_{sp} for calcium sulphate. (2.4×10^{-5})
2. The solubility of silver sulphate is $1.5 \times 10^{-2} \text{ mol L}^{-1}$. Calculate the solubility product of the salt. (1.35×10^{-5})
3. Will precipitate form if 200 mL of 0.0040 M BaCl_2 are added to 600 mL of 0.0080 M K_2SO_4 ?
 $K_{\text{sp}} \text{ BaSO}_4 = 1.1 \times 10^{-10}$
($Q > K_{\text{sp}}$ therefore BaSO_4 will precipitate)

GLOSSARY

NO	TERM	SYMBOL/ FORMULA	DEFINE
1.	Arrhenius acid	-	Substance that dissociate in water to produce H_3O^+ ion.
2.	Arrhenius base	-	Substance that dissociate in water to produce OH^- ion.
3.	Bronsted-Lowry acid	-	Any substance that can donate a proton, (H^+) to other substance.
4.	Bronsted-Lowry base	-	Any substance that can accept a proton, (H^+) from other substance.
5.	Conjugate Acid	-	A species that remains when one proton, (H^+) has been added to the base.
6.	Conjugate Base	-	A species that remains when one proton, (H^+) has been removed from the acid.
7.	Strong acids	-	completely dissociated in aqueous solution

NO	TERM	SYMBOL/ FORMULA	DEFINE
8.	Weak acids	-	partially dissociate in aqueous solution.
9.	Strong base	-	completely dissociated in aqueous solution
10.	Weak base	-	partially dissociate in aqueous solution
11.	<u>pH</u>	$\text{pH} = -\log [\text{H}^+]$	pH is a measure of the concentration of $\text{H}^+/\text{H}_3\text{O}^+$ ions in a solution
12.	<u>pOH</u>	$\text{pOH} = -\log [\text{OH}^-]$	pOH is a measure of the concentration of OH^- ions a solution
13.	<u>pKw</u>	$\text{pKw} = -\log (K_w)$	pKw is a measure of negative logarithm (- log) of the dissociation or ionisation constant of water.
14.	Degree of dissociation (α)	$\alpha = \frac{\text{Concentration of acid or base dissociation}}{\text{Initial concentration}}$	Ability of acids or bases to ionize or dissociate in aqueous solution

NO	TERM	SYMBOL/ FORMULA	DEFINE
15.	Salt	-	an ionic compound that is formed by the reaction of an acid with a base.
16.	Hydrolysis	-	The reaction of cations/anions (or both) from salts with water molecules to produce H ⁺ or OH ⁻
17.	buffer	-	A solution which has the ability to maintain its pH when a small amount of strong acid or strong base is added to the solution.
18.	Acidic buffer	$pH = pK_a + \log \frac{[conjugate\ base]}{[weak\ acid]}$	a solution that contains a weak acid and its salt (or its conjugate base)
19.	Basic buffer	$pOH = pK_b + \log \frac{[conjugate\ acid]}{[weak\ base]}$	a solution that contains a weak base and its salt (or its conjugate acid)

NO	TERM	SYMBOL/ FORMULA	DEFINE
20.	Titration	-	Method for determining the concentration of an unknown solution by using another solution of known concentration
21.	Standard Solution	-	Solution of known concentration
22.	Titrant	-	<p>The solution in a titration that is added from a burette to a measured quantity of another solution</p> <p>@</p> <p>A solution of known concentration that is added (titrated) to another solution</p>
23.	Analyte	-	<p>A substance or sample being analyzed</p> <p>@</p> <p>The solution with unknown concentration</p>
24.	Acid-Base Titrations	-	A method of quantitative analysis for determining the concentration of an acid or base by exactly neutralizing it with a standard solution of base or acid having known concentration.

NO	TERM	SYMBOL/ FORMULA	DEFINE
25.	End Point	-	The point where an indicator changes color
26.	Equivalence Point	-	<p>The point where the mole of acid and base is stoichiometrically equivalent</p> <p>@</p> <p>mole of H^+ equals to mole of OH^- (no more acid or base left in the solution)</p>
27.	Titration Curves	-	A plot of the pH of a solution of acid (or base) versus the volume of base (or acid) added to the solution
28.	pH Jump	-	Steep portion or sharp portion in titration curves.
29.	Indicators	-	<p>A weak organic acid that has different color than it conjugate base and color changes occurring over a specific and relatively narrow pH range.</p> <p>@</p> <p>A weak organic acid that changes colour according to the concentration of hydrogen ions in the solution to which the indicator is added</p>

NO	TERM	SYMBOL/ FORMULA	DEFINE
30.	Solubility	s	Mass of solute (g) dissolved in 1 L of a saturated solution. Unit: g/L
31.	Molar Solubility	s	Moles of solute dissolved in L of a saturated solution. Unit: mol/L
32.	Solubility Product	K _{sp}	The product of the molar concentrations of the constituent ions, each raised to the power of its stoichiometric coefficient in the equilibrium equation.
33.	Common Ion Effect	-	Shift of equilibrium caused by addition or the presence of a compound having an ion in common with the dissolved substance
34.	Common Ion	-	An ion that is already contained in the solution
35.	Precipitation	-	The action or process of precipitating a substance from a solution.
36.	Precipitate	-	An insoluble solid formed in and separates from the solution