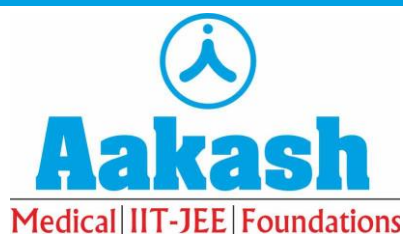


04/04/2024

Morning



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Memory Based Answers & Solutions

Time : 3 hrs.

for

M.M. : 300

JEE (Main)-2024 (Online) Phase-2

(Physics, Chemistry and Mathematics)

IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) This test paper consists of 90 questions. Each subject (PCM) has 30 questions. The maximum marks are 300.
- (3) This question paper contains **Three Parts**. **Part-A** is Physics, **Part-B** is Chemistry and **Part-C** is **Mathematics**. Each part has only two sections: **Section-A** and **Section-B**.
- (4) **Section - A** : Attempt all questions.
- (5) **Section - B** : Attempt any 05 questions out of 10 Questions.
- (6) **Section - A (01 – 20)** contains 20 multiple choice questions which have **only one correct answer**. Each question carries **+4 marks** for correct answer and **-1 mark** for wrong answer.
- (7) **Section - B (21 – 30)** contains 10 **Numerical value** based questions. The answer to each question should be rounded off to the **nearest integer**. Each question carries **+4 marks** for correct answer and **-1 mark** for wrong answer.

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PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

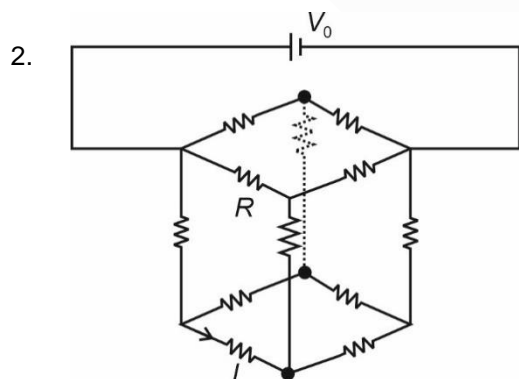
Choose the correct answer:

1. Five identical convex lenses are placed one after the other in close contact. The power of this arrangement is 25 D. Then, power of one such lens is

- (1) 10 D
(2) 5 D
(3) 125 D
(4) 20 D

Answer (2)

Sol. $P = \sum \frac{1}{f_i}$
 $= 5 \times \frac{1}{f}$
 $\Rightarrow \frac{5}{f} = 25$
 $\Rightarrow P = 5 \text{ D}$

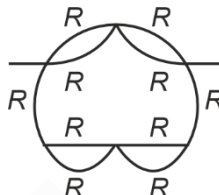


A cubical arrangement of 12 resistors each of R. Each having resistance R is shown. Find I.

- (1) $\frac{V_0}{3R}$
(2) $\frac{V_0}{6R}$
(3) $\frac{V_0}{4R}$
(4) $\frac{V_0}{8R}$

Answer (2)

Sol.



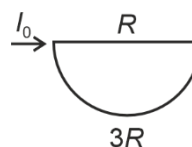
$$R_{eq} = 3R \parallel R$$

$$R_{eq} = \frac{3R}{4}$$

$$i_{3R} = \frac{I_0}{4}$$

$$I = \frac{I_0}{8}$$

$$\Rightarrow i = \frac{1}{8} \left\{ \frac{V_0}{3R/4} \right\} = \frac{V_0}{6R}$$



3. On a given rough inclined plane, a solid sphere and a hollow cylinder are rolled one by one, with same speed. Ratio of heights attained by solid sphere and hollow cylinder is

- (1) $\frac{9}{10}$
(2) $\frac{3}{10}$
(3) $\frac{7}{10}$
(4) $\frac{6}{10}$

Answer (3)

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Sol. Conserving energy :

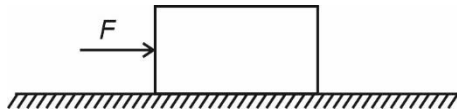
$$\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh$$

$$\Rightarrow \frac{7}{10}mv^2 = mgh_1$$

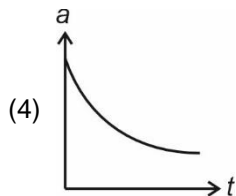
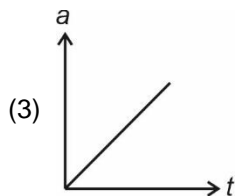
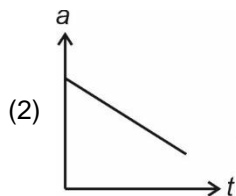
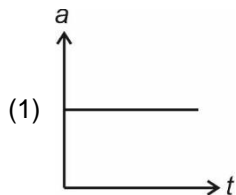
$$\& \quad m'v^2 = m'gh_2$$

$$\Rightarrow \boxed{\frac{7}{10} = \frac{h_1}{h_2}}$$

4. A wooden block is initially at rest. Now a horizontal force is applied on the block which increases linearly with time.



The acceleration - time ($a - t$) graph for the block would be

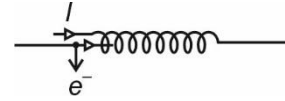


Answer (3)

Sol. $\vec{F} = m\vec{a}$

$\Rightarrow a - t$ graph is also linearly increasing.

5. An electron is projected along the axis of solenoid, the trajectory of electron shall be



- (1) Circular path
- (2) Uniform motion along the axis
- (3) Uniform accelerated motion in straight line
- (4) Parabolic path

Answer (2)

Sol. $\vec{F} = q(\vec{v} \times \vec{B})$

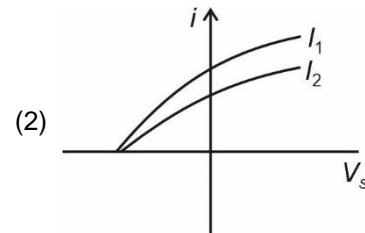
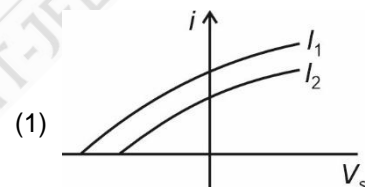
$$\because \vec{v} \parallel \vec{B} \therefore \vec{F} = 0$$

And magnetic force can never do work

\Rightarrow Straight line and uniform motion

6. Which graph correctly represents the photocurrent (i) versus stopping potential (V_s) for same frequency but different intensity?

(Here intensity $I_1 > I_2$)



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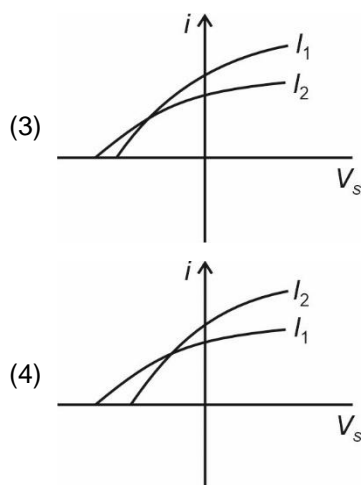
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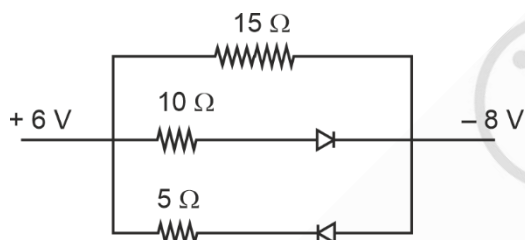


Answer (2)

Sol. f same \Rightarrow same stopping potential

$I_1 > I_2 \Rightarrow$ Saturation current is higher for higher intensity photons.

7. Consider the network shown :



The equivalent resistance of the network is

- (1) 12Ω
- (2) 36Ω
- (3) 20Ω
- (4) 6Ω

Answer (4)

Sol. One diode: short

One diode: open

$$\Rightarrow R_{eq} = \frac{15 \times 10}{15 + 10} \Omega$$

$$= 6 \Omega$$

8. Instantaneous current in a circuit is

$$i(t) = \left[6 + \sqrt{54} \sin \left(2\pi t + \frac{\pi}{3} \right) \right] \text{ A.}$$

RMS value of current is

- (1) $2\sqrt{6} \text{ A}$
- (2) 7 A
- (3) $3\sqrt{7} \text{ A}$
- (4) $6\sqrt{2} \text{ A}$

Answer (3)

Sol. $i(t) = i_1 + i_2 \sin(\omega t + \phi)$

$$\Rightarrow i_{RMS} = \sqrt{\frac{\int [i_1 + i_2 \sin(\omega t + \phi)]^2 dt}{T}}$$

$$= \sqrt{i_1^2 + \frac{i_2^2}{2}}$$

9. The equation of stationary wave is given as

$$y = 2A \sin \left(\frac{2\pi}{\lambda} nt \right) \cos \left(\frac{2\pi}{\lambda} x \right),$$

then which of the

following is not correct.

- (1) Dimension of x is $[L]$
- (2) Dimension of n is $[LT^{-1}]$
- (3) Dimension of $\frac{n}{\lambda}$ is $[T]$
- (4) Dimension of nt is $[L]$

Answer (3)

Sol. From dimensional analyses

$$\frac{nt}{\lambda} \Rightarrow M^0 L^0 T^0$$

$$\frac{nT}{L} = M^0 L^0 T^0$$

$$n = [LT^{-1}]$$

$$\text{Again } \frac{x}{\lambda} = M^0 L^0 T^0$$

$$x = [L]$$

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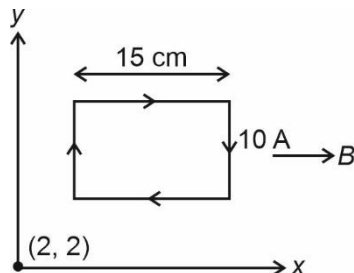
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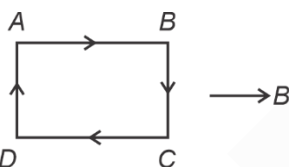
10. In magnetic field varying with x-axis as $B(x) = (1 + 0.2x)\hat{i}$, a square loop of side 15 cm is placed such that its sides are parallel to x & y axes and one corner is at (2, 2) as shown. Net magnetic force on the loop is



(Current in loop is 10 amperes)

- (1) 40 mN
- (2) 10 mN
- (3) Zero
- (4) 45 mN

Answer (4)



Sol.

$$F_{AB} = F_{CD} = 0$$

$$F_{AD} = i\ell B_1 \quad B_1 = (1 + 0.2 \times 2) = 1.4\text{ T}$$

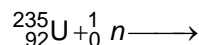
$$F_{BC} = i\ell B_2 \quad B_2 = (1 + 0.2 \times 2.15) = 1.43\text{ T}$$

$$|F_{\text{net}}| = i\ell(B_2 - B_1)$$

$$= 10 \times \frac{15}{100} \times 0.03$$

$$= \frac{4.50}{100} \text{ N} = 45 \text{ mN}$$

11. The correct products of the reaction



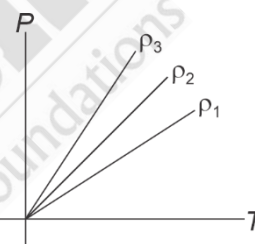
are

- (1) ${}_{56}^{141}\text{Ba} + {}_{36}^{92}\text{Kr} + 3{}_0^1\text{n}$
- (2) ${}_{56}^{141}\text{Ba} + {}_{36}^{92}\text{Kr} + 4{}_0^1\text{n}$
- (3) ${}_{10}^{20}\text{Ne} + {}_{51}^{122}\text{Sb} + 3{}_0^1\text{n}$
- (4) ${}_{10}^{20}\text{Ne} + {}_{51}^{122}\text{Sb} + 4{}_0^1\text{n}$

Answer (1)

Sol. Conserving charge and mass, we get option (1) as correct

12. A given gas is taken through 3 different processes at 3 different densities ρ_1 , ρ_2 and ρ_3 . The corresponding $P-T$ graphs are given. Then :



- (1) $\rho_3 > \rho_2 > \rho_1$
- (2) $\rho_3 < \rho_2 > \rho_1$
- (3) $\rho_3 < \rho_2 < \rho_1$
- (4) $\rho_3 > \rho_2 < \rho_1$

Answer (1)

Sol. $PM = pRT$

$$\Rightarrow \text{Slope} \propto \rho^1$$

$$\Rightarrow \rho_3 > \rho_2 > \rho_1$$

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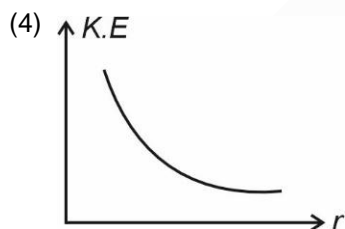
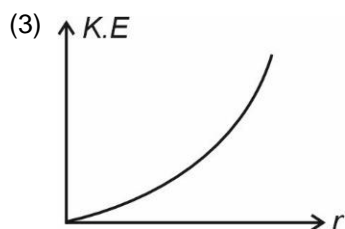
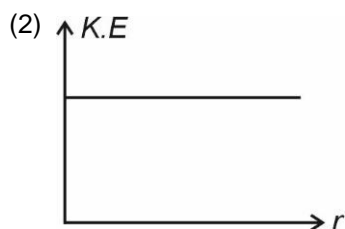
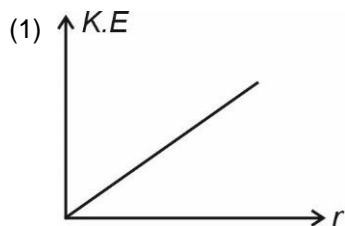
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13. The graphical representation of variation of kinetic energy with radius in case of electron revolving around nucleus of atom is correctly represented by

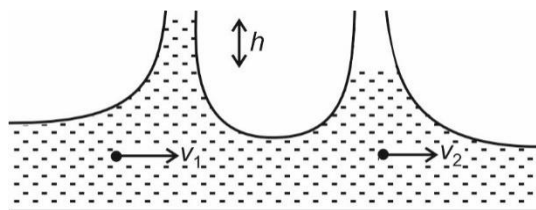


Answer (4)

Sol. $\frac{kze^2}{r^2} = \frac{mv^2}{r}$

$$\frac{1}{2}mv^2 = \frac{1}{2} \frac{kze^2}{r}$$

14. In a pipe, speed of ideal liquid is v_1 at A and v_2 at B. The correct relations between v_1 , v_2 and h is



(g is acceleration due to gravity and ρ is density of liquid)

- (1) $v_2^2 = v_1^2 + 2gh$
- (2) $v_1 v_2 = 2gh$
- (3) $v_1^2 v_2 = \rho gh^2$
- (4) $v_2^2 - v_1^2 + 2gh = 0$

Answer (1)

Sol. $\frac{1}{2}\rho v_1^2 + \rho gh = \frac{1}{2}\rho v_2^2$

$$v_2^2 = v_1^2 + 2gh$$

15. A wire of mass M and length l bent in form of semicircle. A particle of mass m was kept at the centre of the semicircle. Find net gravitational force on particle.

- (1) $\frac{2GMm\pi}{l^2}$
- (2) $\frac{2GMm}{l^2}$
- (3) $\frac{GMm\pi}{l^2}$
- (4) $\frac{3GMm\pi}{l^2}$

Answer (1)

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Sol. $R = \frac{l}{\pi}$

$$E \text{ at centre} = \frac{2GM}{\pi R^2}$$

$$\begin{aligned} \text{Force on particle} &= \frac{2GMm}{\pi R^2} = \frac{2GM}{\pi \cdot l^2} \times \pi^2 \cdot m \\ &= \frac{2GMm\pi}{l^2} \end{aligned}$$

16. The circuit in which phase between maximum current (I_{\max}) and maximum voltage (V_{\max}) is $\frac{\pi}{2}$

- (a) L-circuit
- (b) R-circuit
- (c) C-circuit
- (d) LC-circuit

- (1) a, b, c
- (2) a, c, d
- (3) b, c
- (4) c, d

Answer (2)

Sol. For L-circuit \rightarrow Phase between I_{\max} and V_{\max} is $\frac{\pi}{2}$

For C-circuit \rightarrow Phase between I_{\max} and V_{\max} is $\frac{\pi}{2}$

For LC-circuit \rightarrow Phase between I_{\max} and V_{\max} is $\frac{\pi}{2}$

17. For an electromagnetic wave, electric field is given as $\vec{E} = 40i \cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$ where C is speed of light. (symbols have their usual meanings). The variation of magnetic field is given as

$$(1) \vec{B} = \frac{40}{C} \hat{j} \cos\left(\omega\left(t + \frac{Z}{C}\right)\right)$$

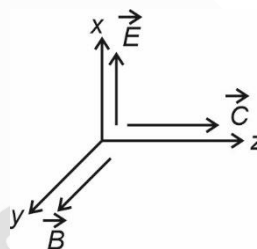
$$(2) \vec{B} = 40C \hat{j} \cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$$

$$(3) \vec{B} = \frac{40}{C} \hat{j} \cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$$

$$(4) \vec{B} = -40C \hat{j} \cos\left(\omega\left(t + \frac{Z}{C}\right)\right)$$

Answer (3)

Sol.



$$\vec{E} \times \vec{B} \uparrow \vec{C}$$

$$\text{Also } E = CB$$

$$\Rightarrow B \text{ is along } +y$$

18. A charged particle is moving in $x - y$ plane where its co-ordinate (x, y) are varying with time t is $x = 2 + 4t$; $y = 3t + 8t^2$. The motion of charged particle is

- (1) Uniform motion
- (2) Uniform accelerated motion along straight line
- (3) Non uniform accelerated motion
- (4) Uniform accelerated motion in a parabolic path

Answer (4)

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Sol. $\vec{r} = (2 + 4t)\hat{i} + (3t + 8t^2)\hat{j}$

$$\vec{u} = 4\hat{i} + (3 + 16t)\hat{j}$$

$$\vec{a} = 16\hat{j} \Rightarrow \text{Uniform accelerated}$$

At $t = 0$ $\vec{v} = 4\hat{i} + 3\hat{j}$ is not parallel to \vec{a}

\Rightarrow Parabolic

19. u is object distance and v is image distance formed by convex lens of focal length f . The error in focal length shall be. (Error in measuring u & v are Δu & Δv)

(1) $2f\left(\frac{\Delta v}{v} + \frac{\Delta u}{u}\right)$

(2) $f^2\left(\frac{\Delta v}{v^2} + \frac{\Delta u}{u^2}\right)$

(3) $f\left[\left(\frac{\Delta v}{v}\right)^2 + \left(\frac{\Delta u}{u}\right)^2\right]$

(4) $\frac{\Delta v}{v} + \frac{\Delta u}{u}$

Answer (2)

Sol. $\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$

$$\frac{-1}{f^2} df = \frac{-1}{v^2} dv + \frac{1}{u^2} du$$

$$\Rightarrow (df) = f^2 \left\{ \frac{|dv|}{v^2} + \frac{|du|}{u^2} \right\}$$

20. A rubber ball fall on the floor from height h and bounces back upto height $\frac{h}{2}$. Then percentage loss in energy and velocity of ball just before striking are respectively.

(1) 50%, $\sqrt{2gh}$

(2) 40%, $\sqrt{2gh}$

(3) 50%, \sqrt{gh}

(4) 40%, \sqrt{gh}

Answer (1)

Sol. $\Delta E = \frac{mgh}{2}$

% change in $\Delta E = 50\%$

Velocity just before collision = $\sqrt{2gh}$

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Because of forces (separately) of 3 N and 2 N, elongations in spring are found to be 'a' and 'b' unit respectively then $(2a - 3b)$ is

Answer (0)

Sol. $a = \frac{3}{k}$

$b = \frac{2}{k}$

$\Rightarrow 2a - 3b = 0$

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22. For a temperature change of 40°C , the corresponding temperature change in $^{\circ}\text{F}$ is

Answer (72)

Sol. $F = 32 + \frac{9C}{5}$

$$\Rightarrow \Delta F = \frac{9}{5} \Delta C = 72^{\circ}\text{F}$$

23. A particle covers 102.5 m in n^{th} second and 115 m in $(n + 2)^{\text{th}}$ second. Then the acceleration of the particle is $x \text{ m/s}^2$. Find $4x$.

Answer (25)

Sol. $s_n = u + \frac{a}{2}[2n - 1]$

$$\Rightarrow 102.5 = u + \frac{a}{2}[2n - 1]$$

and $115 = u + \frac{a}{2}[2n + 3]$

$$\Rightarrow 12.5 = \frac{a}{2}(4) \Rightarrow a = \frac{25}{4} \text{ m/s}^2$$

24. The resistance of platinum wire at ice point and steam point are 10Ω and 2Ω respectively. After that wire is dipped in hot bath of temperature 400°C . The resistance of the wire at temperature 400°C is _____ Ω .

Answer (34)

Sol. $\frac{R - R_{M.P}}{R_{B.P} - R_{M.P}} = \frac{T - 0}{100 - 0}$

$$R = 34 \Omega$$

25. A soap bubble has initial radius of 3.5 cm. Work 36960 erg is done on it to blow it. Surface tension = 40 dyne/cm. The new radius is _____ cm.

Answer (7)

Sol. $W = \Delta U = 8\pi [R^2 - r^2] \cdot S$

$$\Rightarrow \frac{36960}{8 \times \frac{22}{7} \times 40} = R^2 - 3.5^2$$

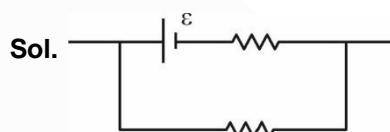
$$\Rightarrow R^2 = 3.5^2 + \frac{147}{4}$$

$$= \frac{49 + 147}{4} = 49$$

$$R = 7 \text{ cm}$$

26. In an experiment to determine internal resistance of battery using potentiometer for external resistance of 10Ω , balancing length is 50 cm and for external resistance of 1Ω , balancing length is 40 cm then internal resistance of battery is x ohms then $7x$ is _____

Answer (2)



$$\varepsilon - \frac{\varepsilon r}{(R+r)} = \frac{\varepsilon R}{R+r} = V = k l$$

$$\frac{\varepsilon R_1}{R_1 + r} = k 50 = \frac{10\varepsilon}{10 + r}$$

$$\left(\frac{\varepsilon R_2}{R_2 + r} \right) = k 40 = \frac{\varepsilon}{1 + r}$$

$$\Rightarrow \frac{5}{4} = \frac{10}{(10 + r)}(1 + r)$$

$$50 + 5r = 40 + 40r$$

$$10 = 35r$$

$$r = \frac{2}{7} \Omega$$

27.

28.

29.

30.

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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. If EMF of Hydrogen electrode at 25°C is zero in pure water then pressure of H₂ in bar

- (1) 10⁻¹⁴ (2) 10⁻⁷
(3) 1 (4) 0.5

Answer (1)

$$\text{Sol. } E_{\text{SHE}} = -\frac{0.0591}{2} \log \frac{P_{\text{H}_2}}{[\text{H}^+]^2} = 0$$

$$\Rightarrow P_{\text{H}_2} = [\text{H}^+]^2$$

$$P_{\text{H}_2} = (10^{-7})^2$$

$$= 10^{-14} \text{ bar}$$

2. For which of the following element only one oxidation state is possible

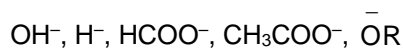
- (1) Sc (2) Co
(3) Ni (4) Fe

Answer (1)

Sol. Only +3 oxidation state is possible for Sc

For other options, more than one oxidation states are possible, correct answer is (1)

3. Among the following, decreasing order of basic strength will be



- (I) (II) (III) (IV) (V)

- (1) II > V > III > I > IV (2) II > V > I > IV > III
(3) III > IV > I > V > II (4) V > I > IV > II > III

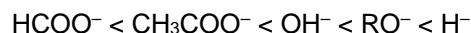
Answer (2)

$$\text{Sol. Basic strength} \propto \frac{1}{\text{Strength of conjugate acid}}$$

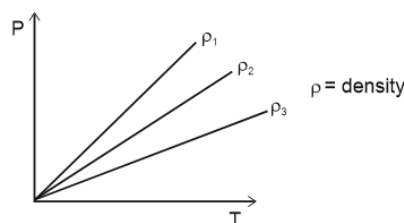
Acidic strength:



Basic strength:



4. We are given with the following graph between P and T



Choose the correct option

- (1) $\rho_1 > \rho_2 > \rho_3$ (2) $\rho_1 < \rho_2 < \rho_3$
(3) $\rho_1 = \rho_2 = \rho_3$ (4) $\rho_2 > \rho_1 > \rho_3$

Answer (1)

$$\text{Sol. } \rho = \frac{P \times \text{MW}}{RT}$$

$$P = \frac{\rho \cdot R \cdot T}{\text{MW}}$$

$$P = \left(\frac{\rho \cdot R}{\text{MW}} \right) \cdot T$$

$$\text{Slope} = \frac{\rho \cdot R}{\text{MW}}$$

Slope $\propto \rho$ (density)

$$\Rightarrow \rho_1 > \rho_2 > \rho_3$$

\Rightarrow Option (1) is correct

5. Which of the following have maximum dipole moment?

- (1) NH₃ (2) PF₅
(3) NF₃ (4) PCl₅

Answer (1)

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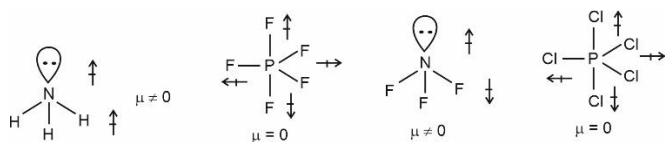
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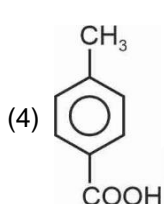
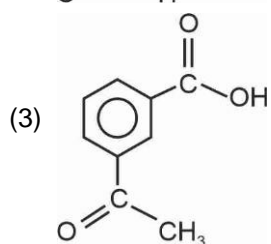
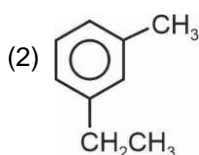
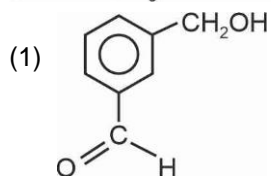
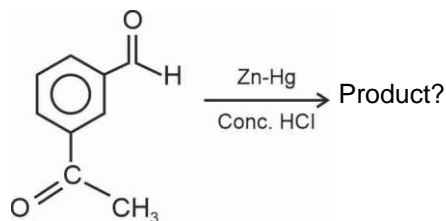
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Sol.



NH_3 has greater dipole moment than NF_3

6.



Answer (2)

Sol. This is an example of Clemmensen reduction reaction. In this reaction carbonyl group is reduced to methylene group.

7. Which of the following is the correct order of first ionization enthalpy?

- (1) $\text{Be} < \text{B} < \text{O} < \text{F} < \text{N}$
- (2) $\text{B} < \text{Be} < \text{O} < \text{N} < \text{F}$
- (3) $\text{B} < \text{Be} < \text{N} < \text{F} < \text{O}$
- (4) $\text{Be} < \text{B} < \text{N} < \text{O} < \text{F}$

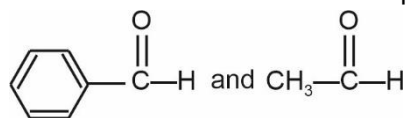
Answer (2)

Sol. Be has more value of first ionization enthalpy than B due to fully filled configuration and N has more value of first ionization enthalpy than O due to half filled configuration

The correct order is $\text{B} < \text{Be} < \text{O} < \text{N} < \text{F}$

8. Statement-1 : Aldol condensation is caused by acidity of α hydrogen

Statement-2 : Cross aldol is not possible between

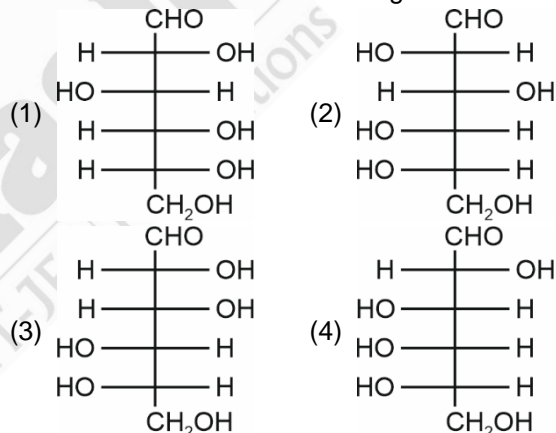


- (1) Both statement-1 and statement-2 are correct
- (2) Both statement-1 and statement-2 are incorrect
- (3) Statement-1 is correct but statement-2 is incorrect
- (4) Statement-1 is incorrect but statement-2 is correct

Answer (3)

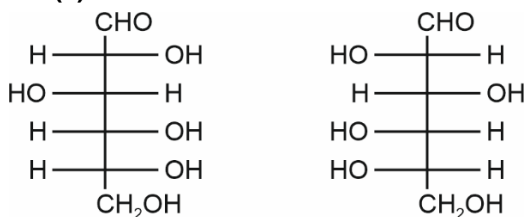
Sol. Aldol reaction is given by those carbonyl compounds which have at least one α hydrogen atom because α -hydrogen of carbonyl compounds is acidic. Benzaldehyde and acetaldehyde will form cross aldol because acetaldehyde has α -hydrogen atom.

9. Select the correct structure of L-glucose.



Answer (2)

Sol.



D-Glucose

L-Glucose

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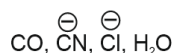


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10. Decreasing order of the field strength of the following ligands will be:



- (1) $\text{CO} > \text{CN}^{\ominus} > \text{H}_2\text{O} > \text{Cl}^{\ominus}$ (2) $\text{CO} > \text{CN}^{\ominus} > \text{Cl}^{\ominus} > \text{H}_2\text{O}$
(3) $\text{CN}^{\ominus} > \text{CO} > \text{H}_2\text{O} > \text{Cl}^{\ominus}$ (4) $\text{CN}^{\ominus} > \text{CO} > \text{Cl}^{\ominus} > \text{H}_2\text{O}$

Answer (1)

Sol. $\text{CO} > \text{CN}^{\ominus} > \text{H}_2\text{O} > \text{Cl}^{\ominus}$

11. Calculate the molarity of NaCl solution, if 5.85 gm of NaCl is dissolved in 500 ml of solution.

- (1) 0.1 M (2) 0.2 M
(3) 0.32 M (4) 0.4 M

Answer (2)

Sol. $\text{Molarity} = \frac{\text{Number of moles of solute}}{\text{Volume of solution (in L)}}$
$$= \frac{5.85 \times 1000}{58.5 \times 500} = 0.1 \times 2 = 0.2 \text{ M}$$

12. Which of the following does not give Lassaigne's test?

- (1) Urea (2) Azobenzene
(3) Hydrazine (4) Phenylhydrazine

Answer (3)

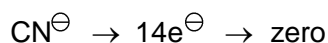
Sol. Hydrazine ($\text{NH}_2 - \text{NH}_2$) does not contain carbon. On fusion with sodium metal, it cannot form NaCN. So hydrazine does not show Lassaigne's test.

13. Among the following, species that have one unpaired e^- ?

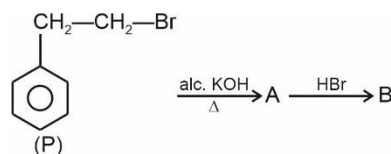
- (1) CN^{\ominus} (2) O_2^{2-}
(3) O_2^+ (4) NO^{\ominus}

Answer (3)

Sol. Unpaired e^-



14. For a given reaction

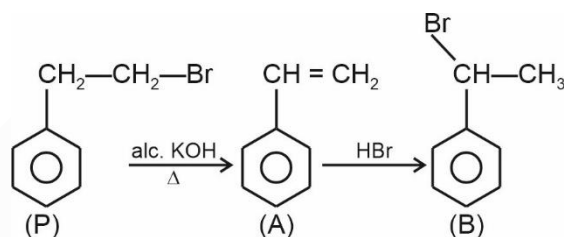


Relation between the molecules P and B are:

- (1) Enantiomer (2) Diastereomers
(3) Positional isomers (4) Functional isomers

Answer (3)

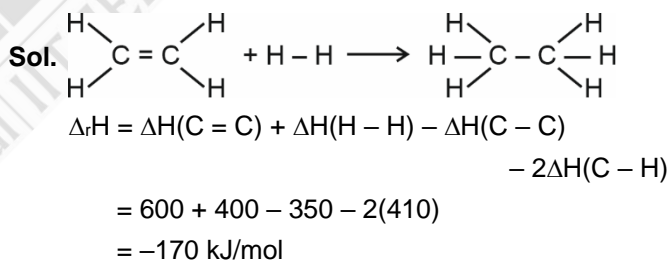
Sol. Positional isomers.



15. From the given data, find enthalpy of hydrogenation of ethene in kJ/mol

- (a) B.E. of $\text{C} - \text{C} = 350 \text{ kJ/mol}$
(b) B.E. of $\text{C} = \text{C} = 600 \text{ kJ/mol}$
(c) B.E. of $\text{H} - \text{H} = 400 \text{ kJ/mol}$
(d) B.E. of $\text{C} - \text{H} = 410 \text{ kJ/mol}$
(1) -170 (2) -580
(3) $+170$ (4) $+580$

Answer (1)



16. Find out wavelength of a photon having frequency equal to 900 sec^{-1} .

- (1) $3.33 \times 10^5 \text{ m}$ (2) $3.33 \times 10^5 \text{ cm}$
(3) $3.33 \times 10^7 \text{ m}$ (4) $3.33 \times 10^4 \text{ m}$

Answer (1)

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Sol. $v = \frac{c}{\lambda}$

$$\lambda = \frac{c}{v}$$

$$\lambda = \frac{3 \times 10^8 \text{ m sec}^{-1}}{900 \text{ sec}^{-1}}$$

$$= \frac{3 \times 10^8}{900}$$

$$= \frac{3 \times 10^6}{9}$$

$$= \frac{1}{3} \times 10^6$$

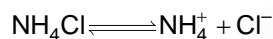
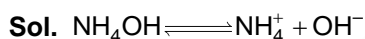
$$= 0.333 \times 10^6$$

$$= 3.33 \times 10^5 \text{ m}$$

17. Why NH_4Cl is added before NH_4OH for the ppt. of Fe^{3+} ions?

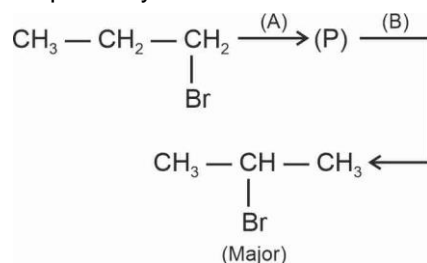
- (1) To decrease OH^- ion concentration
- (2) To increase Cl^- ion concentration
- (3) To increase NH_4^+ ion concentration
- (4) To decrease H^+ ion concentration

Answer (1)



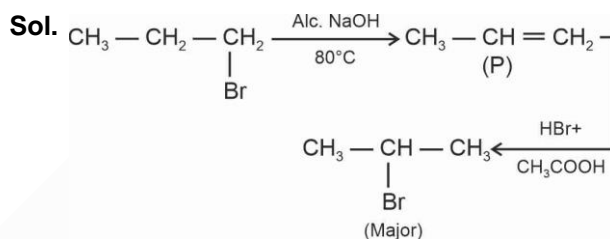
Solid NH_4Cl is added to NH_4OH solution to decrease the OH^- ion concentration due to common ion effect.

18. Consider the following sequence of reactions and identify the unknown reagents (A) and (B) respectively.

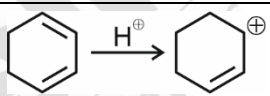


- (1) (A) : Dil. aq NaOH at 20°C
(B) : HBr, CH_3COOH
- (2) (A) : Dil. aq NaOH at 20°C
(B) : Br_2 , CHCl_3
- (3) (A) : Alc. NaOH at 80°C
(B) : HBr, CH_3COOH
- (4) (A) : Alc. NaOH at 80°C
(B) : Br_2 , CHCl_3

Answer (3)

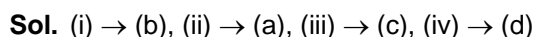


19. Match the following

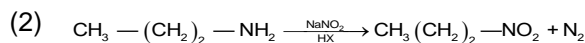
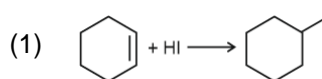
(i)	Nitrobenzene	(a)	+R
(ii)	Aniline	(b)	-R
(iii)		(c)	+E
(iv)	$\text{CH}_3 - \overset{\text{O}}{\parallel}{\text{C}} - \text{H} \xrightarrow{\text{CN}^-} \text{CH}_3 - \overset{\text{O}^-}{\parallel}{\text{C}} - \text{H} \xrightarrow{\text{CN}^-} \text{CH}_3 - \overset{\text{O}^-}{\parallel}{\text{C}}(\text{CN}) - \text{H}$	(d)	-E

- (1) (i) \rightarrow (b), (ii) \rightarrow (a), (iii) \rightarrow (c), (iv) \rightarrow (d)
- (2) (i) \rightarrow (a), (ii) \rightarrow (b), (iii) \rightarrow (c), (iv) \rightarrow (d)
- (3) (i) \rightarrow (c), (ii) \rightarrow (b), (iii) \rightarrow (a), (iv) \rightarrow (d)
- (4) (i) \rightarrow (d), (ii) \rightarrow (c), (iii) \rightarrow (a), (iv) \rightarrow (b)

Answer (1)



20. Which of the following is not possible major product?



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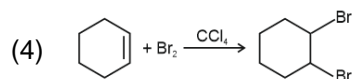
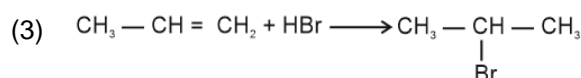
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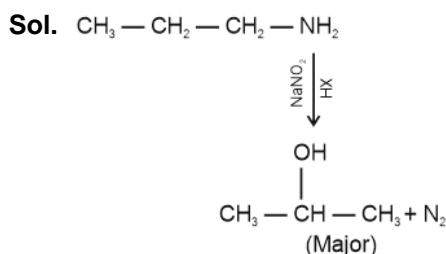
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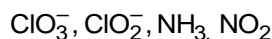
Answer (2)



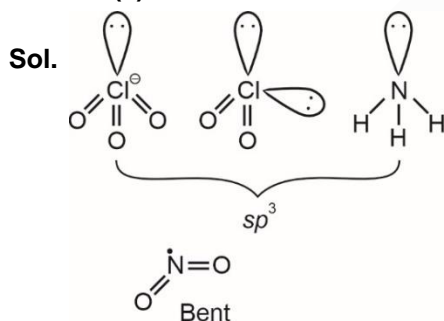
SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. How many of the following compounds are sp^3 hybridised?



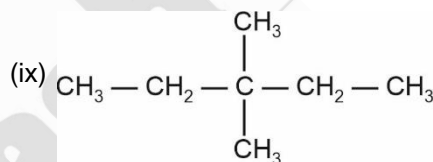
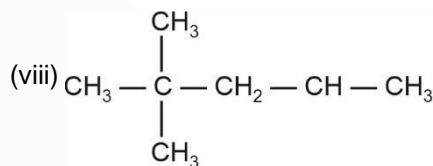
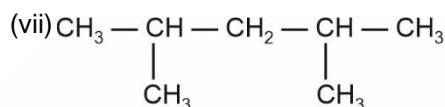
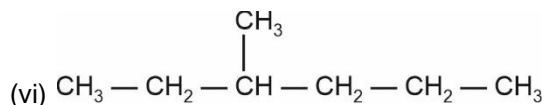
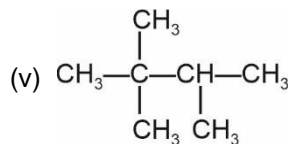
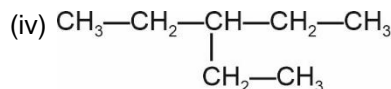
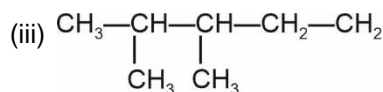
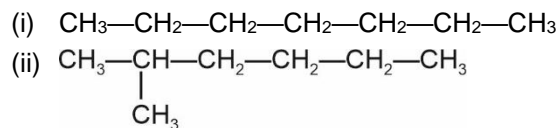
Answer (3)



22. Total number of structural isomers possible for a compound with molecular formula C_7H_{16} are:

Answer (5)

Sol. C_7H_{16} has DoU = 0



23. The de-Broglie wavelength of an electron in 4th orbit of hydrogen atom is _____ πa_0 (a_0 = Bohr radius).

Answer (8)

Sol. $\therefore \lambda_{\text{de-Broglie}} = \frac{2\pi r}{n} = \frac{2\pi}{n} \times 0.529 \frac{n^2}{z} \text{ \AA}$

or, $\lambda_{\text{de-Broglie}} = 2\pi \times n \times a_0 \text{ \AA}$

$= 2\pi \times 4 \times a_0 \text{ \AA}$

$= 8\pi a_0 \text{ \AA}$

24. 50 mL of KMnO_4 solution is used for titration with 20 mL of 2M oxalic acid solution in Acidic medium. The molarity of KMnO_4 solution is $x \times 10^{-2}$ M. The value of x is

Answer (32)

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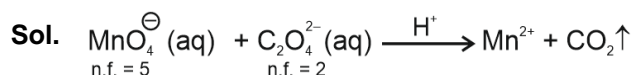
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$$5 \times M_{\text{KMnO}_4} \times 50 = 2 \times 20 \times 2$$

$$M_{\text{KMnO}_4} = \frac{8}{25} = 32 \times 10^{-2} \text{M}$$

$$x = 32$$

25. A solution having non-volatile solute in water shows elevation in boiling point of 2°C . Find out vapour pressure of solution (in mm Hg) (Nearest integer)

Vapour pressure of pure water = 760 mm Hg

K_b of water = $0.52 \text{ K.kg mole}^{-1}$

Answer (711)

Sol. $\Delta T_b = (K_b) (m)$

$$2 = (0.52) (m)$$

$$m = 3.846$$

$$X_{\text{Solute}} = \frac{m}{m + 55.5} = 0.0648$$

$$\frac{760 - X}{760} = 0.0648$$

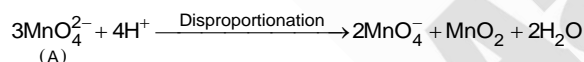
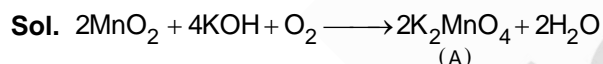
$$\Rightarrow P_{\text{solution}} = 710.74 \text{ mm Hg}$$

$$\approx 711 \text{ mm Hg}$$



'A' disproportionate into 'B' and 'C'. Find the sum of magnetic moment (spin only) (in B.M.) of B and C (Nearest integer)

Answer (4)



B and C are MnO_4^- and MnO_2

Mn in MnO_2 has +4 oxidation state hence it has $(n-1)d^3 ns^0$ electronic configuration
 unpaired e = 3

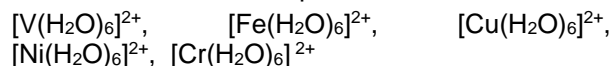
Mag. moment : 3.87 B.M. by $\sqrt{n(n+2)}$

$\text{KMnO}_4/\text{MnO}_4^-$ is diamagnetic hence magnetic moment = 0 because it has no unpaired electron.

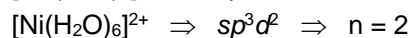
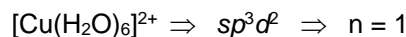
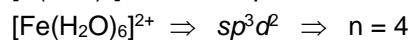
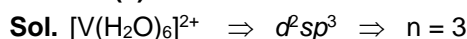
Hence, sum of mag. moment = 3.87 B.M.

Nearest integer = 4

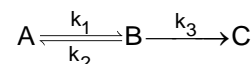
27. How many of the following coordination compounds have even number of unpaired electrons?



Answer (3)



28. Consider the following reaction sequence :



$$\text{Overall } k = \frac{k_1 k_2}{k_3}$$

$$\text{if } E_{a_1} = 300 \text{ kJ/mole}$$

$$E_{a_2} = 200 \text{ kJ/mole}$$

$$\text{Overall, } (E_a)_{\text{eff}} = 400 \text{ kJ/mole}$$

$$\text{Find out } E_{a_3} \text{ (in kJ/mole)}$$

Answer (100)

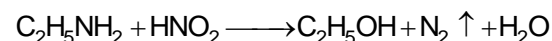
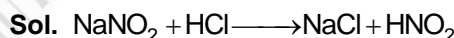
Sol. $(E_a)_{\text{eff}} = E_{a_1} + E_{a_2} - E_{a_3}$

$$400 = 300 + 200 - E_{a_3}$$

$$E_{a_3} = 100 \text{ kJ/mole}$$

29. x g of ethylamine on reaction with NaNO_2 and HCl , produces 2.24 L of $\text{N}_2(\text{g})$ at NTP. The value of 2x will be

Answer (9)



$$\text{Mole of } \text{N}_2(\text{g}) \text{ produced} = \frac{2.24}{22.4} = 0.1 \text{ mol}$$

$$\text{So, mole of } \text{C}_2\text{H}_5\text{NH}_2 \text{ used} = 0.1 \text{ mol}$$

$$\text{Mass of } \text{C}_2\text{H}_5\text{NH}_2 = 45 \times 0.1 = 4.5 \text{ g}$$

$$\text{So, } 2x = 2 \times 4.5$$

$$= 9$$

30.

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MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. If $f(x) = \begin{cases} x-2, & 0 < x \leq 2 \\ -2, & -2 \leq x \leq 0 \end{cases}$ and

$h(x) = f(|x|) + |f(x)|$ then

find $\int_0^k h(x) dx$ is equal to ($k > 0$)

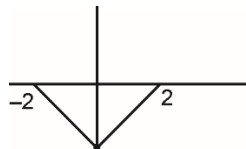
- (1) 0 (2) $\frac{k}{2}$
(3) $2k$ (4) k

Answer (1)

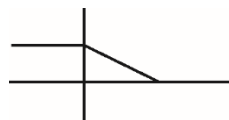
Sol. Graph of $f(x)$



$f(|x|)$



$$\Rightarrow f(|x|) = \begin{cases} -2-x, & x < 0 \\ x-2, & x > 0 \end{cases}$$



$$|f(x)| = \begin{cases} 2, & x < 0 \\ 2-x, & x > 0 \end{cases}$$

$$\Rightarrow h(x) = f(|x|) + |f(x)| = \begin{cases} -x, & x < 0 \\ 0, & x > 0 \end{cases}$$

$$\Rightarrow \int_0^k h(x) dx = \int_0^k 0 dx = 0$$

2. Let three urn A, B, C : A = 7 red, 5 black

B = 5 red, 7 black

C = 6 red, 6 black

Urn is selected and black ball is taken. Then the probability that the selected urn is A is equal to

- (1) $\frac{7}{18}$ (2) $\frac{5}{17}$
(3) $\frac{7}{19}$ (4) $\frac{5}{18}$

Answer (4)

Sol. Urn A has 7 red, 5 black balls

Urn B has 5 red, 7 black balls.

Urn C has 6 red, 6 black balls

If ball drawn is black then probability that it is chosen from urn A.

$$\begin{aligned} &= \frac{\frac{1}{3} \times \frac{5}{12}}{\frac{1}{3} \times \frac{5}{12} + \frac{1}{3} \times \frac{7}{12} + \frac{1}{3} \times \frac{6}{12}} \\ &= \frac{\frac{5}{36}}{\frac{5}{36} + \frac{7}{36} + \frac{6}{36}} \\ &= \frac{5}{18} = \frac{5}{18} \end{aligned}$$

3. $\int_{-\pi/2}^{\pi/2} \frac{\sin^2 x}{1+2^x} dx =$

- (1) $\left(\frac{\pi}{4}\right)$ (2) $\frac{\pi}{8}$
(3) 4π (4) $\frac{\pi}{2}$

Answer (1)

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Sol. $I = \int_0^{\pi/2} \left(\frac{\sin^2 x}{1+2^x} + \frac{\sin^2(x)}{1+2^{-x}} \right) dx$

$$I = \int_0^{\pi/2} \sin^2 x \, dx$$

$$I = \int_0^{\pi/2} \cos^2 x \, dx$$

$$2I = \int_0^{\pi/2} 1 \, dx$$

$$I = \frac{\pi}{4}$$

4. If $f(x) = \frac{2x^2 - 3x + 8}{2x^2 + 3x + 8}$ then sum of maximum and minimum values of $f(x)$ is

- (1) $\frac{136}{55}$ (2) $\frac{146}{55}$
 (3) $\frac{146}{11}$ (4) $\frac{136}{11}$

Answer (2)

Sol. $y = \frac{2x^2 - 3x + 8}{2x^2 + 3x + 8}, \quad 2x^2 + 3x + 8 > 0 \quad \forall x \in \mathbb{R}$

$$\Rightarrow x^2(2y - 2) + x(3y + 3) + 8y - 8 = 0$$

Since $x \in \mathbb{R}$, the equation has real roots

\Rightarrow Discriminant is greater than or equal to 0

$$\Rightarrow (3y + 3)^2 - 4(2y - 2)(8y - 8) \geq 0$$

$$\Rightarrow 9(y + 1)^2 - 64y(y - 1)^2 \geq 0$$

$$\Rightarrow (3y + 3)^2 - (8y - 8)^2 \geq 0$$

$$\Rightarrow (11y - 5)(-5y + 11) \geq 0$$

$$\Rightarrow \left(y - \frac{5}{11}\right) \left(y - \frac{11}{5}\right) \leq 0$$

$$\Rightarrow y \in \left[\frac{5}{11}, \frac{11}{5}\right]$$

$$\begin{aligned} \Rightarrow \text{Sum of } y_{\max} \text{ and } y_{\min} &= \frac{5}{11} + \frac{11}{5} \\ &= \frac{121 + 25}{55} \\ &= \left(\frac{146}{55}\right) \end{aligned}$$

5. The coefficient of x^7 in

$(1 - x - x^2 + x^3)^6$ equals to

- (1) 132 (2) 144
 (3) -132 (4) -144

Answer (4)

Sol. Coefficient of x^7 in $(1 - x)^6 (1 - x^2)^6$

$${}^6C_1 {}^6C_3 - {}^6C_3 {}^6C_2 + {}^6C_5 {}^6C_1$$

$$120 - 15 \times 20 + 6 \times 6$$

$$120 - 300 + 36$$

$$= -144$$

6. If $(\bar{z})^2 + |z| = 0$ and if α is sum of roots and β is product of non-zero roots, then $4(\alpha^2 + \beta^2)$ is

- (1) $\frac{1}{4}$ (2) 1
 (3) 4 (4) 2

Answer (3)

Sol. $(\bar{z})^2 + |z| = 0$

Let $z = x + iy$

$$\Rightarrow (x - iy)^2 + \sqrt{x^2 + y^2} = 0$$

$$\Rightarrow (x^2 - y^2) + \sqrt{x^2 + y^2} - 2xyi = 0$$

$$\Rightarrow x^2 - y^2 + \sqrt{x^2 + y^2} = 0 \text{ and } 2xy = 0$$

$$\Rightarrow x = 0 \text{ and } y \neq 0$$

Case I

$$\Rightarrow -y^2 + |y| = 0 \Rightarrow |y| = y^2 \Rightarrow y = \pm 1$$

Case II

$$x \neq 0 \text{ and } y = 0$$

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$$\Rightarrow x^2 + |x| = 0 \Rightarrow x = 0 \text{ only not possible}$$

$$\Rightarrow x = 0, y = 0 \text{ satisfies}$$

$$\Rightarrow z = i, -i, 0 \text{ are solution}$$

$$\alpha = i - i = 0$$

$$\beta = (i)(-i) = -1 \Rightarrow 4(\alpha^2 + \beta^2) = 4$$

7. If α & β are roots of $ax^2 + bx + c = 0$ then equation whose roots are $\frac{1}{\alpha}, \frac{1}{\beta}$ is

$$(1) cx^2 + bx + a = 0$$

$$(2) bx^2 + ax + c = 0$$

$$(3) ax^2 + bx + c = 0$$

$$(4) cx^2 + ax + b = 0$$

Answer (1)

Sol. $ax^2 + bx + c = 0$ $\begin{matrix} \alpha \\ \beta \end{matrix}$

$$\alpha + \beta = \frac{-b}{a}$$

$$\alpha\beta = \frac{c}{a}$$

$$\text{Now } \frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta} = -\frac{b}{c}$$

$$\frac{1}{\alpha\beta} = \frac{a}{c}$$

$$x^2 - \left(\frac{1}{\alpha} + \frac{1}{\beta}\right)x + \frac{1}{\alpha\beta} = 0$$

$$x^2 + \frac{b}{c}x + \frac{a}{c} = 0$$

$$cx^2 + bx + a = 0$$

8. Let $f(x) = \begin{cases} \frac{1 - \cos \alpha x}{x^2}; & x < 0 \\ 2; & x = 0 \\ \frac{\beta \sqrt{1 - \cos x}}{x}; & x > 0 \end{cases}$

is continuous at $x = 0$. Then $\alpha^2 + \beta^2$ equals to

$$(1) 10$$

$$(2) 12$$

$$(3) 13$$

$$(4) 9$$

Answer (2)

Sol. Given $f(x)$ is continuous at $x = 0$

$$\therefore \lim_{x \rightarrow 0^-} f(x) = f(0) = \lim_{x \rightarrow 0^+} f(x)$$

When $x < 0, x = 0 - h$

$$\therefore \lim_{h \rightarrow 0} \frac{1 - \cos(\alpha(0 - h))}{(0 - h)^2}$$

$$= \lim_{h \rightarrow 0} \frac{1 - \cos(h\alpha)}{h^2}$$

$$= \lim_{h \rightarrow 0} \left(\frac{1 - \cos(\alpha h)}{\alpha^2 h^2} \right) \alpha^2$$

$$= \alpha^2 \lim_{h \rightarrow 0} \frac{1 - \cos(\alpha h)}{(\alpha h)^2}$$

$$= \frac{\alpha^2}{2} \quad \dots(1)$$

When $x > 0$

$$x = 0 + h$$

$$\lim_{h \rightarrow 0} \frac{\beta \sqrt{1 - \cos h}}{h} = \lim_{h \rightarrow 0} \frac{\beta \sqrt{\frac{1 - \cosh}{h^2}} \cdot h^2}{h}$$

$$= \frac{\beta}{\sqrt{2}} \quad \dots(2)$$

$$\text{as } f(0) = 2 \quad \dots(3)$$

\therefore From (1), (2) and (3)

$$\frac{\alpha^2}{2} = 2, \quad \frac{\beta}{\sqrt{2}} = 2$$

$$\alpha = 2, \quad \beta = 2\sqrt{2}$$

$$\alpha^2 + \beta^2 = 4 + 8 = 12$$

9. If the length of focal chord of $y^2 = 12x$ is 15 and if the distance of the focal chord from origin is P then $10P^2$ is equal to

$$(1) 36$$

$$(2) 25$$

$$(3) 72$$

$$(4) 144$$

Answer (3)

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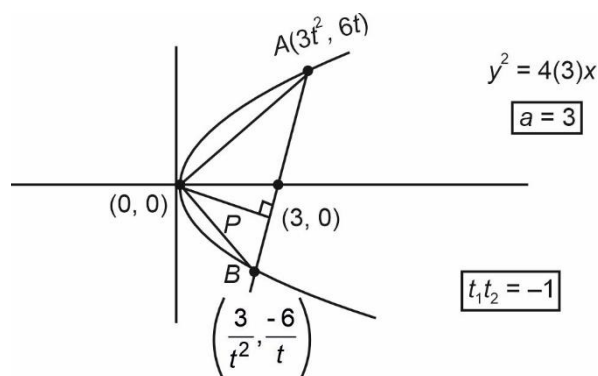
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**Sol.**

$$\Rightarrow AB = 15$$

$$\left(3t^2 - \frac{3}{t^2}\right)^2 + \left(6t + \frac{6}{t}\right)^2 = 225$$

$$\Rightarrow 9\left(t^2 - \frac{1}{t^2}\right)^2 + 36\left(t + \frac{1}{t}\right)^2 = 225$$

$$\Rightarrow 9\left(t + \frac{1}{t}\right)^2 \left[\left(t - \frac{1}{t}\right)^2 + 4\right] = 225$$

$$\Rightarrow 9\left(t + \frac{1}{t}\right)^2 \left(t + \frac{1}{t}\right)^2 = 225$$

$$\Rightarrow t + \frac{1}{t} = \left(\frac{225}{9}\right)^{1/4} = (25)^{1/4} = \sqrt{5}$$

$$\text{Equation of } AB \equiv (y-0) = \frac{2}{\left(t - \frac{1}{t}\right)}(x-3) \Rightarrow \left|t - \frac{1}{t}\right| = 1$$

$$\Rightarrow y = 2x - 6 \Rightarrow y - 2x + 6 = 0$$

$$\text{Distance from origin} \Rightarrow P = \frac{6}{\sqrt{5}} \Rightarrow 10P^2 = \frac{10 \times 36}{5}$$

$$= 72$$

10. Numbers $-3, 4, 7, -6, \alpha, \beta$

Mean = 2, Variance = 23, then

Mean deviation about mean equals to

(1) $\frac{13}{8}$

(2) $\frac{13}{3}$

(3) $\frac{13}{7}$

(4) $\frac{13}{9}$

Answer (2)

$$\text{Sol. Mean} = \frac{-3 + 4 + 7 + (-6) + \alpha + \beta}{6} = 2$$

$$= 2 + \alpha + \beta = 2 \times 6$$

$$\Rightarrow \alpha + \beta = 10$$

$$\text{Variance} = \frac{\sum xi^2}{n} - \left(\frac{\sum x}{n}\right)^2 = 23$$

$$= \frac{\sum xi^2}{n} = 23 + 4$$

$$= \sum xi^2 = 27 \times 6$$

$$= 9 + 16 + 49 + 36 + \alpha^2 + \beta^2 = 162$$

$$\Rightarrow \alpha^2 + \beta^2 = 52$$

\Rightarrow We get α and β as 4 and 6

So, mean deviation about mean

$$= \frac{|-3-2| + |4-2| + |7-2| + |-6-2| + |4-2| + |6-2|}{6}$$

$$= \frac{5+2+5+8+2+4}{6}$$

$$= \frac{26}{6} = \frac{13}{3}$$

11. If $\frac{dy}{dx} = \frac{2x^2 + 2x + 3}{x^4 + 2x^3 + 3x^2 + 2x + 2}$

and $y(-1) = -\frac{\pi}{4}$

then $y(0)$ is

(1) $\frac{\pi}{3}$

(2) $\frac{\pi}{4}$

(3) $\frac{\pi}{2}$

(4) $\frac{\pi}{6}$

Answer (2)

$$\text{Sol. } \int dy = \int \frac{2x^2 + 2x + 3}{x^4 + 2x^3 + 3x^2 + 2x + 2} dx$$

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$$= \int \frac{2x^2 + 2x + 3}{(x^2 + 1)(x^2 + 2x + 2)} dx$$

$$= \int \frac{1}{x^2 + 2x + 2} dx + \int \frac{1}{x^2 + 1} dx$$

$$= \int \frac{1}{1 + (x+1)^2} dx + \tan^{-1} x + C$$

$$y = \tan^{-1}(x+1) + \tan^{-1} x + C$$

$$y(-1) = -\frac{\pi}{4}$$

$$-\frac{\pi}{4} = 0 - \frac{\pi}{4} + C$$

$$\Rightarrow C = 0$$

$$\therefore y = \tan^{-1}(x+1) + \tan^{-1}(x)$$

$$\text{Now } y(0) = \tan^{-1}(1) + \tan^{-1}(0) = \frac{\pi}{4}$$

12. If \vec{c} is a variable unit vector and \vec{c} makes angle of 45° with \vec{b} and 60° with \vec{a} with $\vec{b} = \hat{i} - \hat{k}$ and $\vec{a} = 2\hat{i} + 2\hat{j} - \hat{k}$ then $|\vec{c} + 2\vec{a} - 3\vec{b}|$ is

- (1) 19 (2) 20
(3) $\sqrt{19}$ (4) $\sqrt{20}$

Answer (3)

Sol. \vec{c} is unit vector

$$\vec{b} = \hat{i} - \hat{k}$$

$$\vec{a} = 2\hat{i} + 2\hat{j} - \hat{k}$$

$$|\vec{a}| = 3, |\vec{b}| = \sqrt{2}, |\vec{c}| = 1$$

$$|\vec{c} + 2\vec{a} - 3\vec{b}|^2 = |\vec{c}|^2 + 4|\vec{a}|^2 + 9|\vec{b}|^2 + 4\vec{a} \cdot \vec{c}$$

$$-12\vec{a} \cdot \vec{b} - 6\vec{b} \cdot \vec{c}$$

$$= 1 + 36 + 18 + 4|\vec{a}||\vec{c}|\cos 60^\circ - 12[3]$$

$$-6|\vec{b}||\vec{c}|\cos 45^\circ$$

$$= 55 + 12 \times \frac{1}{2} - 36 - 6\sqrt{2} \times \frac{1}{\sqrt{2}}$$

$$= 55 + 6 - 36 - 6$$

$$= 19$$

$$|\vec{c} + 2\vec{a} - 3\vec{b}| = \sqrt{19}$$

13. If the system of equations

$$A + \sqrt{2} \sin x B + \sqrt{2} \cos x C = 0$$

$$A + \sin x B - \cos x C = 0$$

$A + \cos x B + \sin x C = 0$ has non-trivial solution then

the value of $x, x \in \left(0, \frac{\pi}{2}\right)$ is

- (1) $\frac{5\pi}{12}$ (2) $\frac{\pi}{12}$
(3) $\frac{5\pi}{24}$ (4) $\frac{\pi}{8}$

Answer (3)

Sol. For non-trivial solution

$$\begin{vmatrix} 1 & \sqrt{2} \sin x & \sqrt{2} \cos x \\ 1 & \sin x & -\cos x \\ 1 & \cos x & \sin x \end{vmatrix} \text{ is zero}$$

$$\Rightarrow 1 - 1(\sqrt{2} \sin^2 x - \sqrt{2} \cos^2 x) + 1(-2\sqrt{2} \sin x \cos x) = 0$$

$$\Rightarrow 1 + \sqrt{2}(\cos 2x) - \sqrt{2} \sin 2x = 0$$

$$\Rightarrow \sqrt{2}(\cos 2x - \sin 2x) = -1$$

$$\Rightarrow \cos\left(2x + \frac{\pi}{4}\right) = \frac{-1}{2}$$

$$x \in \left(0, \frac{\pi}{2}\right)$$

$$2x \in (0, \pi)$$

$$2x + \frac{\pi}{4} \in \left(\frac{\pi}{4}, \frac{5\pi}{4}\right)$$

$$\Rightarrow \cos\left(2x + \frac{\pi}{4}\right) = \frac{-1}{2} \Rightarrow 2x + \frac{\pi}{4} = \frac{2\pi}{3}$$

$$2x = \frac{2\pi}{3} - \frac{\pi}{4} = \frac{5\pi}{12}$$

$$\Rightarrow x = \frac{5\pi}{24}$$

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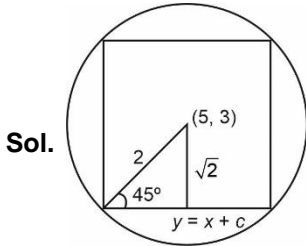
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14. A line L_1 having equation $y = x + 3$. A square is inscribed in a circle $x^2 + y^2 - 10x - 6y + 30 = 0$ such that one side of square is parallel to L_1 . Find $\sum_{i=1}^4 (x_i^2 + y_i^2)$ where $(x_i, y_i) \ i \in \{1, 2, 3, 4\}$ are the vertices of square.

- (1) 152 (2) 162
(3) 172 (4) 182

Answer (1)



Distance of $(5, 3)$ to the line $y = x + c$ is $\sqrt{2}$

$$\Rightarrow \frac{|3 - 5 - c|}{\sqrt{2}} = \sqrt{2}$$

$$|c + 2| = 2$$

$$\Rightarrow c = 0$$

$$c = -4$$

So, the lines are $y = x$ and $y = x - 4$

Now, solving these lines with the circle

$$y = x \text{ and } x^2 + y^2 - 10x - 6y + 30 = 0$$

$$2x^2 - 16x + 30 = 0$$

$$x^2 - 8x + 15 = 0$$

$$x = 3, y = 3$$

$$x = 5, y = 5$$

$$y = x - 4 \text{ and } x^2 + y^2 - 10x - 6y + 30 = 0$$

$$2x^2 - 24x + 70 = 0$$

$$x^2 - 12x + 35 = 0$$

$$x = 5, y = 1$$

$$x = 7, y = 3$$

$$\sum_{i=1}^4 x_i^2 + y_i^2 = 9 + 9 + 25 + 25 + 25 + 1 + 49 + 9 = 152$$

15.
16.
17.
18.
19.
20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The number of rational numbers in the expansion of $(2^{1/5} + 5^{1/3})^{15}$ is

Answer (02)

Sol. $T_{r+1} = {}^{15}C_r (5^{1/3})^r (2^{1/5})^{15-r}, r \in \{0, 1, \dots, 15\}$

$$= {}^{15}C_r 5^{\left(\frac{r}{3}\right)} \cdot 2^{\left(3 - \frac{r}{5}\right)}, \quad r \in \{0, 1, \dots, 15\}$$

For rational terms,

$$\frac{r}{3} \in \text{integer and } \frac{r}{5} \in \text{integer}$$

$$\Rightarrow 3 \text{ and } 5 \text{ divides } r \Rightarrow 15 \text{ divides } r$$

$$\Rightarrow r = 0 \text{ and } 15$$

$$\Rightarrow \text{only 2 rational terms.}$$

22. In $\triangle ABC$ there are 18 points, on side AB there are P_1, P_2, P_3, P_4, P_5 points, on BC there are P_6, P_7, \dots, P_{11} points and on CA P_{12}, \dots, P_{18} points. By joining any three points from P_1, P_2, \dots, P_{18} form a triangle. Then number of triangles possible are

Answer (751)

Sol. Total ways to select three points out of 18 points = ${}^{18}C_3$

$$\text{Total ways to select 3 points from } P_1 \dots P_5 = {}^5C_3$$

$$\text{Total ways to select 3 points from } P_6 \dots P_{11} = {}^6C_3$$

$$\text{Total ways to select 3 points from } P_{12} \dots P_{18} = {}^7C_3$$

Total number of triangles possible

$$= {}^{18}C_3 - {}^5C_3 - {}^6C_3 - {}^7C_3$$

$$= 751$$

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23. If $\lim_{x \rightarrow 1} \frac{(5x+1)^{1/3} - (x+5)^{1/3}}{(2x+3)^{1/2} - (x+4)^{1/2}} = \frac{m(5)^{1/2}}{n(2n)^{2/3}}$

Then $8m + 12n$ is

Answer (100)

Sol. $\lim_{x \rightarrow 1} \frac{(5x+1)^{1/3} - (x+5)^{1/3}}{(2x+3)^{1/2} - (x+4)^{1/2}}$

$$\lim_{x \rightarrow 1} \frac{\frac{1}{3}(5x+1)^{-2/3} \cdot 5 - \frac{1}{3}(x+5)^{-2/3}}{2 \times \frac{1}{2}(2x+3)^{-1/2} - \frac{1}{2}(x+4)^{-1/2}}$$

$$= \frac{\frac{1}{3} \times \frac{5}{(6)^{2/3}} - \frac{1}{3} \times \frac{1}{(6)^{2/3}}}{\frac{1}{2} \times \frac{2}{(5)^{1/2}} - \frac{1}{2} \times \frac{1}{(5)^{1/2}}}$$

$$= \frac{\frac{4}{3 \times (6)^{2/3}}}{\frac{1}{2 \cdot (5)^{1/2}}} = \frac{8(5)^{1/2}}{3(6)^{2/3}} = \frac{m(5)^{1/2}}{n(2n)^{2/3}}$$

$$\Rightarrow m = 8, n = 3$$

$$8m + 12n = 64 + 36 = 100$$

24. In a G.P. $T_1 = 2$, $T_2 = P$, $T_3 = Q$, these are also terms of A.P. (7^{th} , 8^{th} and 13^{th} term).

If 5^{th} term of G.P = n^{th} term of A.P. Then n is

Answer (27)

Sol. $T_1 = 2$

$a = 2$

$T_2 = P$

$2r = P \Rightarrow r = \frac{P}{2}$

$T_3 = Q$

$2r^2 = Q \Rightarrow r^2 = \frac{Q}{2}$

$a' + 6d = 2 \quad \dots(1)$

$a' + 7d = P \quad \dots(2)$

$a' + 12d = Q \quad \dots(3)$

$d = 2(r - 1)$

$2r(r - 1) = 5d$

$\frac{5d}{d} = \frac{-2r(r-1)}{2(r-1)}$

$r = 5 \Rightarrow d = 8$

$a + 48 = 2$

$a = -46$

$2.3^4 = -46 + (n - 1) \times 8$

$\Rightarrow n = 27$

25. Domain of $\sin^{-1}\left(\frac{3x-22}{2x-19}\right) + \log_e\left(\frac{3x^2-8x+5}{x^2-3x-10}\right)$

is $(\alpha, \beta]$. Then $3\alpha + 10\beta$ equals to

Answer (97)

Sol. $-1 \leq \frac{3x-22}{2x-19} \leq 1$

$\frac{3x-22-2x+19}{2x-19} \leq 0$

$\frac{x-3}{2x-19} \leq 0$

$\begin{array}{c} + \quad - \quad + \\ \hline 3 \quad \quad 19 \\ \quad \quad 2 \end{array}$

$\left[3, \frac{19}{2}\right)$

$\frac{3x-22+2x-19}{2x-19} \geq 0$

$\frac{5x-41}{2x-19} \geq 0$

$\begin{array}{c} + \quad - \quad + \\ \hline 41 \quad \quad 19 \\ \quad \quad 5 \quad \quad 2 \end{array}$

$\left(-\infty, \frac{41}{5}\right] \cup \left(\frac{19}{2}, \infty\right)$

Taking intersection

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