

UNIVERSITY *of* WASHINGTON

Data Science UW

Methods for Data

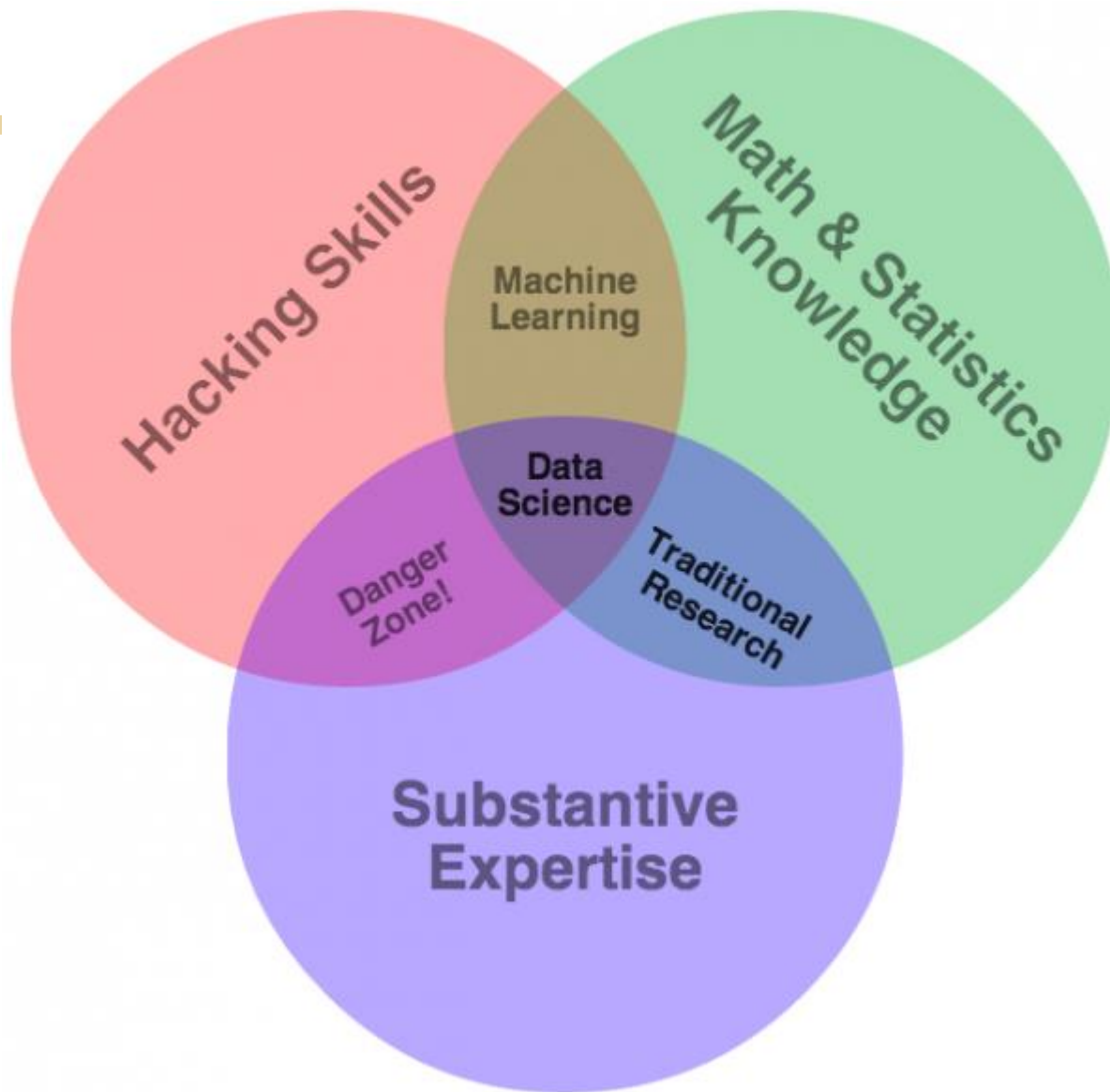
Analysis

Introduction and Data Exploration

Lecture 1

Nick McClure





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Course Purpose

- > This course isn't designed to make you an expert
- > This course is designed to point you in the right direction
- > Course Objectives:
 - Statistical tools for data exploration
 - The use of R to apply these tools to real data
 - Using inferential statistics to interrogate data
 - Testing and experimental design
 - Bayesian and classical statistics
- > See syllabus for more information:
 - On Canvas
 - Or <http://nfmccclure.github.io/DataScience350/>



Course Requirements and Grading

This course will be graded by attendance, homework, and an individual project.

- > Attendance: You MUST attend at least 6 out of 10 classes. This is non-negotiable, a UW requirement.
- > Homework must be completed by the start of the next class. (Assigned weeks 1-8).
 - Returned as a score between 0 and 2.
 - > 2 pts: The homework is well done, submitted on time.
 - > 1.5-1.9 pts: The homework mostly satisfies the criteria. The major concept of the homework was done correctly with minor programming or statistical errors.
 - > 1-1.4pts: The homework misses some key points of the objectives.
 - > 0-1pt: The homework needs much more work in both the statistical and programming structure.
 - > All late homeworks receive a 0.5 point deduction.



Individual Project

- > Individual Project: Due at the start of the last class.
 - Counts as 8 points.
- > Must use at least two distinct statistical methods covered in this class.
- > Projects are usually heavily involved either with data gathering xOR with statistical methods.
 - Doing a project that is heavy on both is not recommended.
- > By the beginning of the third class, you will have sent me a project proposal email. It is worth 0.25 points as part of homework #2.
- > Ideal project schedule:
 - By the 5th class, have acquired all necessary data.
 - By the 8th class, have written all code for the project.
 - By the 9th class, have a first draft of the project write up.
 - By the 10th class, submit project.



Course Requirements and Grading

There is a total of 24 possible points. (16 pts for hmk + 8 project)

- > Must get 18 total points to pass.
- > 4 homework assignments must be made in a production level script (every other one = 2,3,5,7).
- > 4 homework assignments are regular script writing (every other one = 1,4,6,8).
- > The individual project must be production level code.



Office Hours and Contact Information

- > List of ways to contact me:
 - nickmc@uw.edu (updated every hour or so)
 - nfmcclure@gmail.com (updated quite continuously)
- > When I'm *usually* available:
 - Off/on for simple things during work. (M-F 8am-5pm PST)
 - Mon-Wed 7pm-10pm.
 - Sunday various afternoon/evening times.

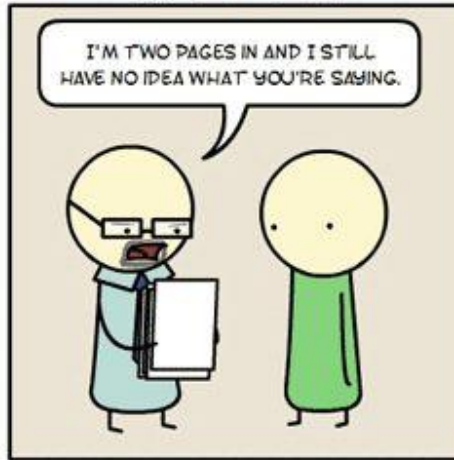


Review

PYTHON



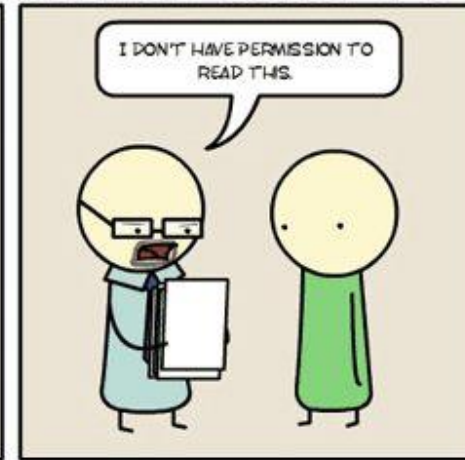
JAVA



C++



UNIX SHELL



ASSEMBLY



C



LATEX



HTML



Topics

- > Probability and Statistics
 - Counting
 - Axioms of Probability
 - Probability Examples
- > R Programming Review
 - R Resources
 - Data Exploration in R



Why Counting?

- > Counting is fundamental to probability theory.
- > Probability is the extent or likelihood of an event or set of events.
 - Depends heavily on the ability to *count* up potential outcomes.



Counting

> This is one of the biggest areas of mathematics, called Combinatorics.

> Example:

- Subway has 4 different breads, 5 different meats, 4 different toppings. How many sandwich combinations?
- How many different 4-beer tasters can I have in a bar with 10 beers on tap?

> Solve these using the ‘Multiplication Principle’.

- Subway Problem:

$$\begin{array}{ccccccc} 4 & * & 5 & * & 4 & & = 80 \\ \hline (\text{\# of breads}) & & (\text{\# of meats}) & & (\text{\# of toppings}) & & \end{array}$$

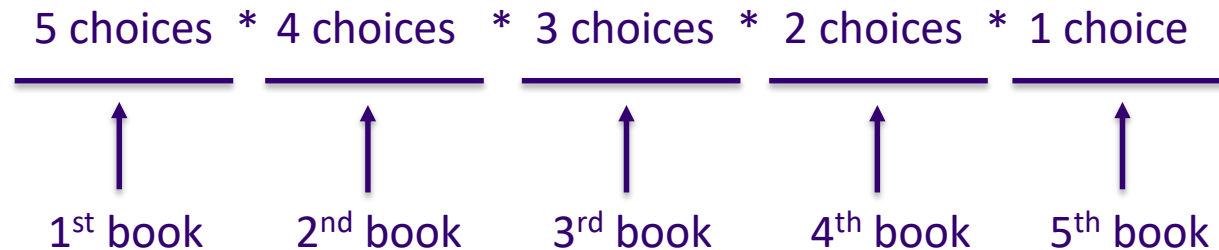
- Beer Problem:

$$\begin{array}{ccccccc} 10 & * & 9 & * & 8 & * & 7 & & = 5,040 \\ \hline (\text{\# for 1st beer}) & & (\text{\# for 2nd beer}) & & (\text{\# for 3rd beer}) & & (\text{\# for 4th beer}) & & \end{array}$$



Multiplication Principle

- > If there are A ways of doing task a, and B ways of doing task b, then there are $A*B$ ways of completing both tasks.
- > Example:
 - If I have 5 books, how many ways can I *order* them on the bookshelf?



$$= 5 \text{ factorial} = 5! = 120$$



Factorials

> Factorials

- Count # ways to order N things = $N!$

> Factorials get VERY large quickly.

- $21!$ Is larger than the biggest long-int in 64 bit.
 - > $21! = 5.1\text{E}19$
 - > Biggest long int (64 bit) = $9.2\text{E}18$
- Fun fact, every 52 card shuffle is highly likely to be the only time that shuffle has ever occurred.



Counting Subgroups

- > Revisit: 10 beers on tap, need a sample of 4 different beers.
- > Let's assume order matters, i.e., Amber-Stout-Porter-Red is different from Red-Porter-Stout-Amber.
- > Use 'Permutations' (pick):

$$10 * 9 * 8 * 7 = \frac{10!}{6!} = \frac{10!}{(10 - 4)!} = 10P4 = P(10,4)$$



Counting Subgroups

- > Now, Let's assume order doesn't matter.
- > Use 'Combinations' (choose):

$$10 * 9 * 8 * 7 = \frac{10!}{6!} = \frac{10!}{(10 - 4)!} = 10P4 = P(10,4)$$

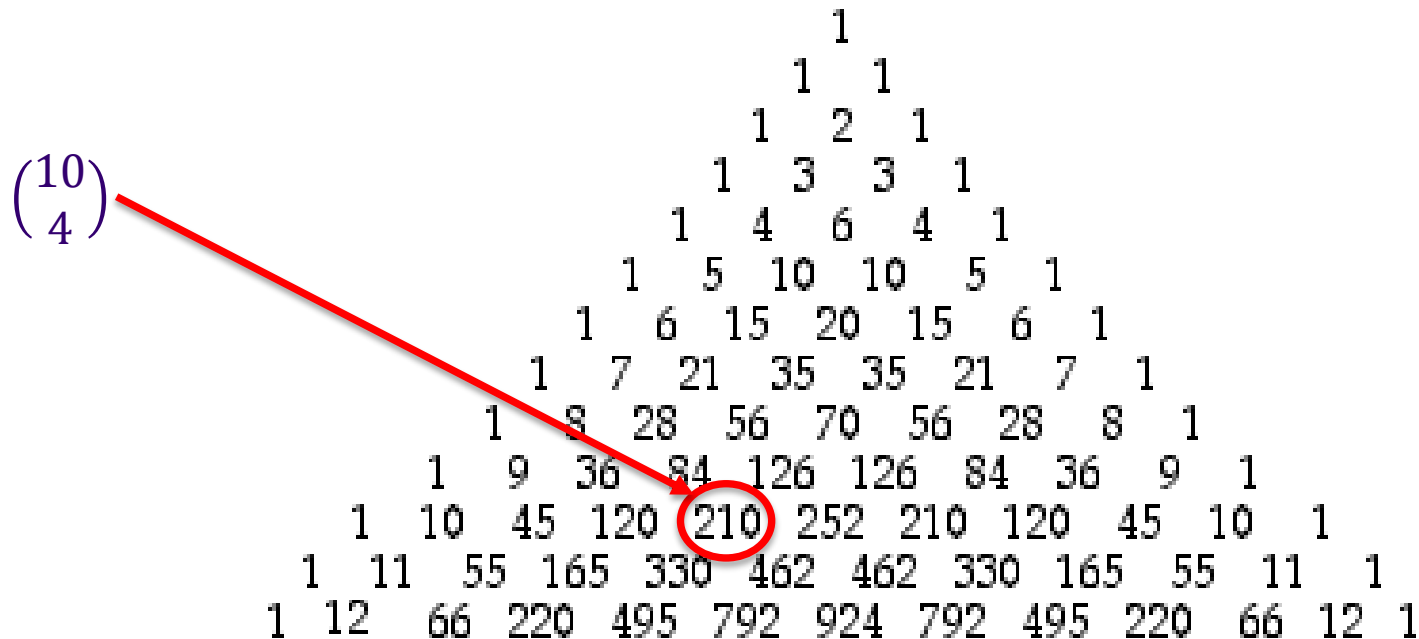
(# of orderings of 4 beers) = 4!

$$= \frac{10!}{4! (10 - 4)!} = 10C4 = C(10,4) = \binom{10}{4}$$



More on Combinations

- > Combinations appear on the Pascal's Triangle!
- > $C(N,x)$ appears on the Nth row, xth number (starting at 0)



Counting Examples

- > There are 10 Light beers on tap, and 10 Dark beers on tap, how many ways can Rick get a 4-beer sampler that contains exactly 1 light beer? (ordering doesn't matter)

$$\frac{(\# \text{ of ways for light beer}) \cdot (\# \text{ of ways for dark beer})}{(\# \text{ of ways to order 1L and 3D})}$$

$$\frac{(10) \cdot \binom{10}{3}}{4} = \frac{10 * 120}{4} = 300$$



Counting Examples

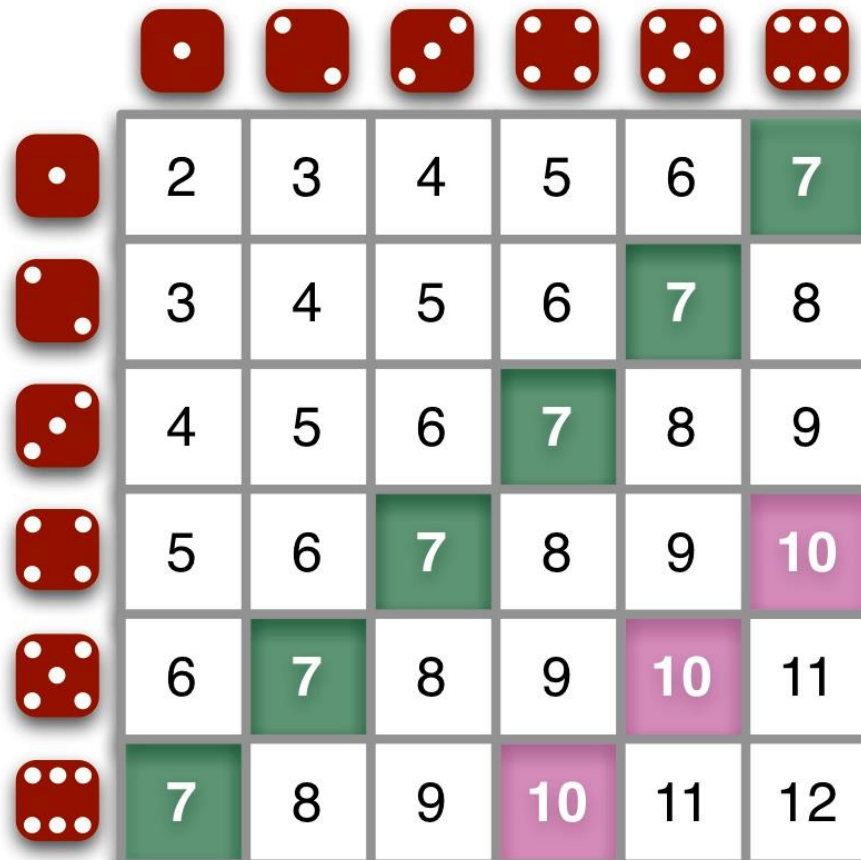
- > 6:5 Blackjack is dealt with a 6 shoe deck ($52 \times 6 = 312$ cards). How many ways can someone get dealt two rank 10 cards?

$$\binom{6\text{decks} * 4\text{ranks} * 4\text{suits}}{2} = \binom{96}{2} = \frac{96!}{2! (94!)} = \frac{96 * 95}{2} = 4560$$



Counting Examples

> How many ways can two dice be rolled to get a sum of 10?



	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

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Counting in R

- > `expand.grid()` – function that creates a data frame from all combinations of vectors supplied.
- > R-demo



Probability

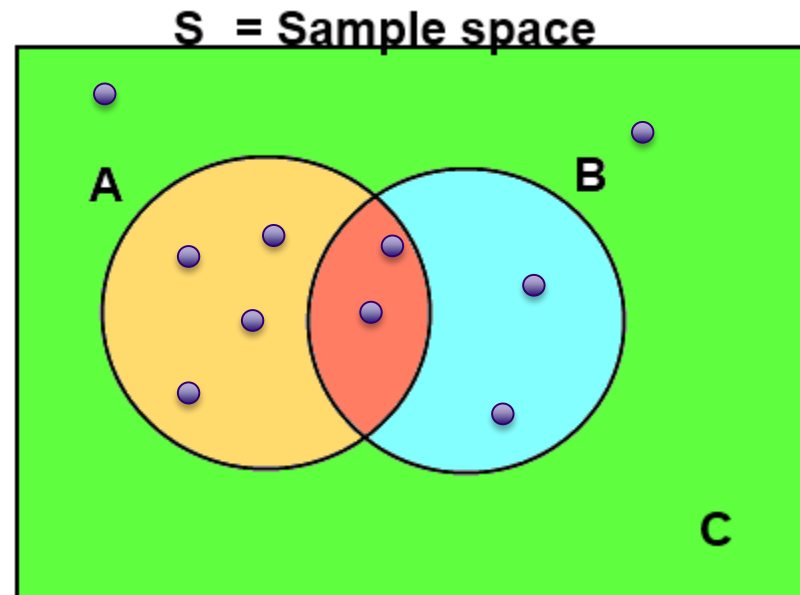
- > The Probability of an event, A, is the number of ways A can occur, divided by the number of total possible outcomes in our Sample Space, S.

$$P(A) = \frac{N(A)}{N(S)}$$

- > If \bullet is an event, then

$$P(A) = \frac{6}{10} = \frac{3}{5}$$

$$P(B) = \frac{4}{10} = \frac{2}{5}$$



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Probability

> If \bullet is an event, then

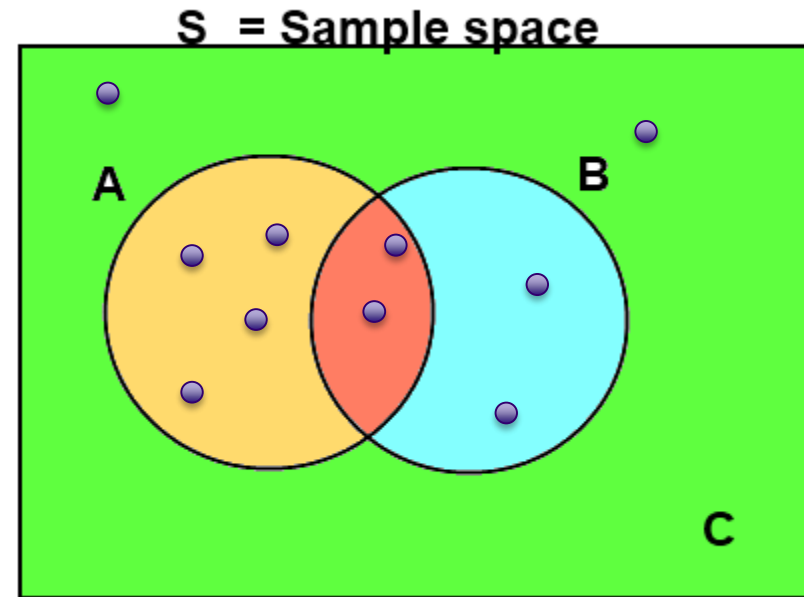
– Intersection: $P(A \cap B) = \frac{2}{10} = \frac{1}{5}$

– Union: $P(A \cup B) = \frac{8}{10} = \frac{4}{5}$

– Negation: $P(A') = \frac{4}{10} = \frac{2}{5}$

$$P((A \cup B)') = P(C) = \frac{2}{10} = \frac{1}{5}$$

$$P(A' \cap B') = P(C) = \frac{2}{10} = \frac{1}{5}$$



Axioms of Probability

- > Probability is bounded between 0 and 1.

$$0 \leq P(A) \leq 1$$

Note: “Percent” literally means per one hundred

- > Probability of the Sample Space = 1.

$$P(S) = 1$$

- > The probability of finite *mutually exclusive* unions is the sum of their probabilities.

$$P(A \cup B) = P(A) + P(B) \quad \text{If A and B are M.E.}$$



Data Exploration (Descriptive Statistics)

- > Purpose: To gain a clear understanding of your data.
 - How large is it?
 - What columns are of interest?
 - Missing data?
 - Outliers?



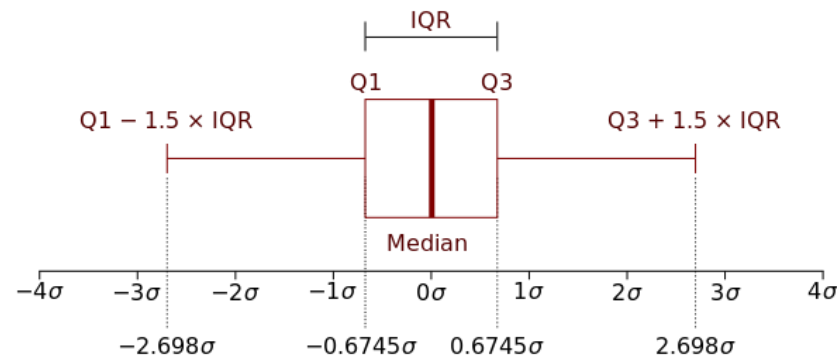
Numerical Exploration

- > `str()`: structure of the data frame
- > `summary()`: summary of each of the columns
- > `head()` / `tail()`: top / bottom of data frame
- > `table()`: frequency table



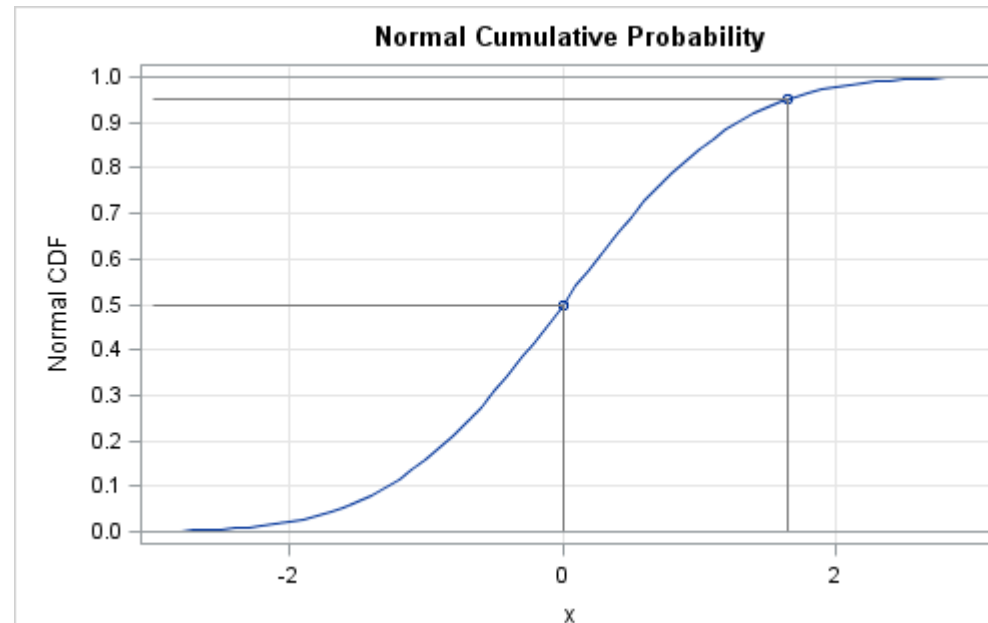
Numerical Exploration

> IQR(): inner quartile range ($Q3 - Q1$)



Numerical Exploration

- > `quantile()`: quantiles of numerical vectors
 - Quantiles are inverse values of the CDF (cumulative distribution function).
 - Standard Normal: (shown in figure)
 - > $\text{Quantile}(0.5) = 0$, means at $x=0$, 50% of the distribution lies to the left. (This is also the median)
 - > $\text{Quantile}(0.95) = 1.65$



Numerical Exploration

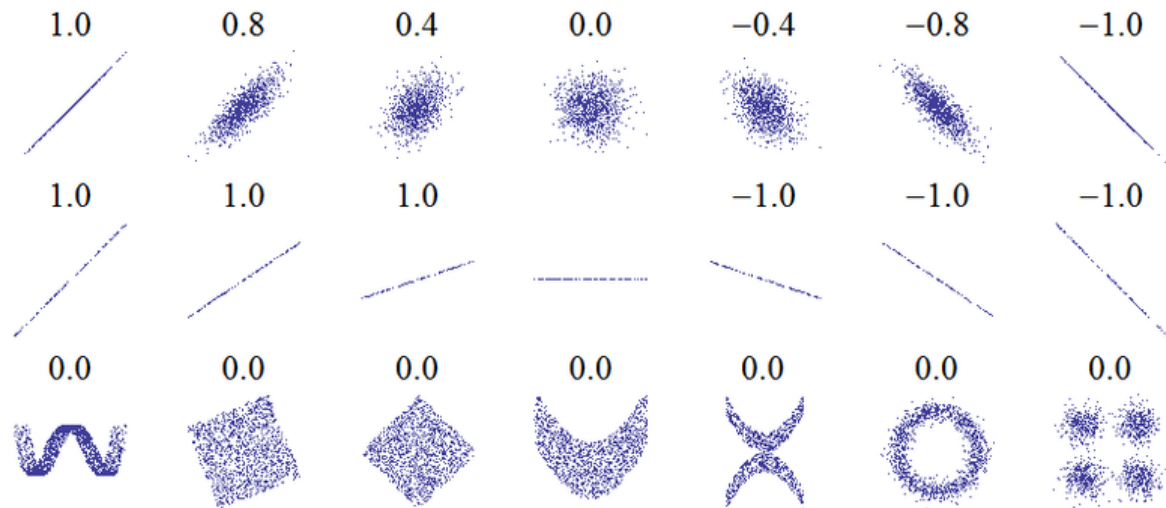
> Relationships:

- `cov()`: covariances

$$\text{cov}(x, y) = E((x - \mu_x)(y - \mu_y))$$

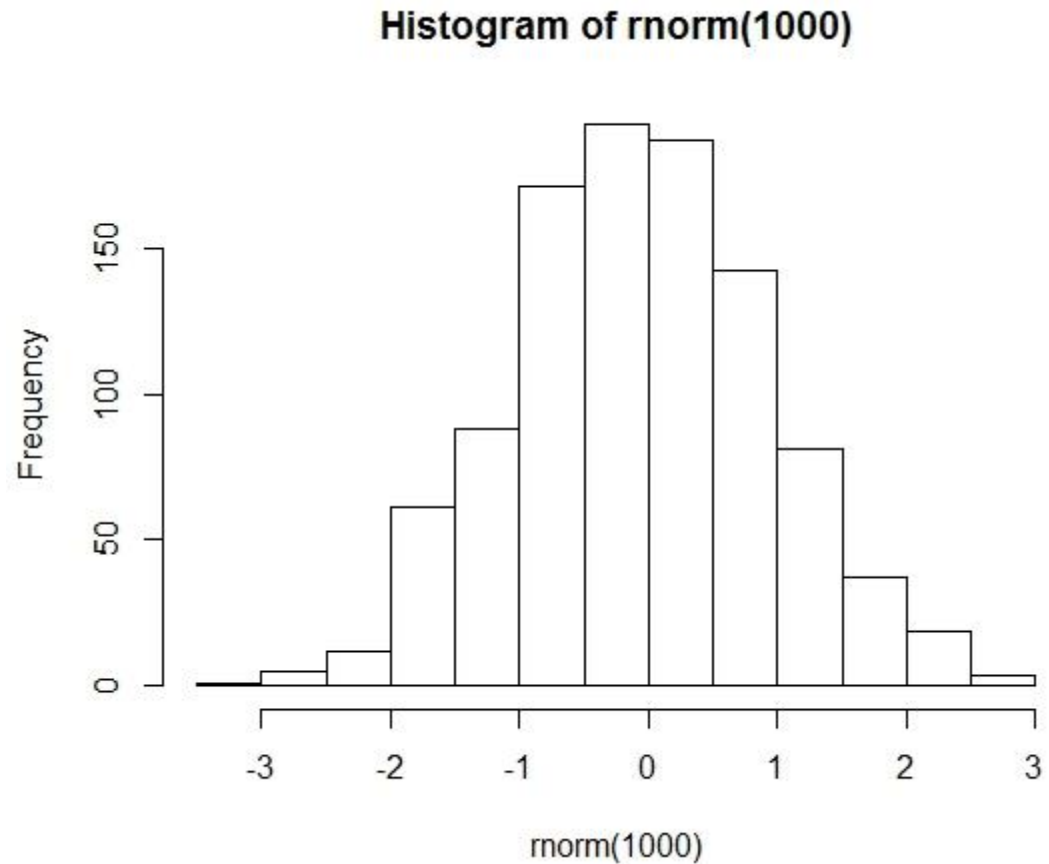
- Interpretation: Expected value of the differences between x and y and their corresponding mean.
- E.g. if x is above its mean when y is also above its mean, then they will have a high covariance.
- Highly interpretable, but not bounded.





Visual Exploration

> Histograms:



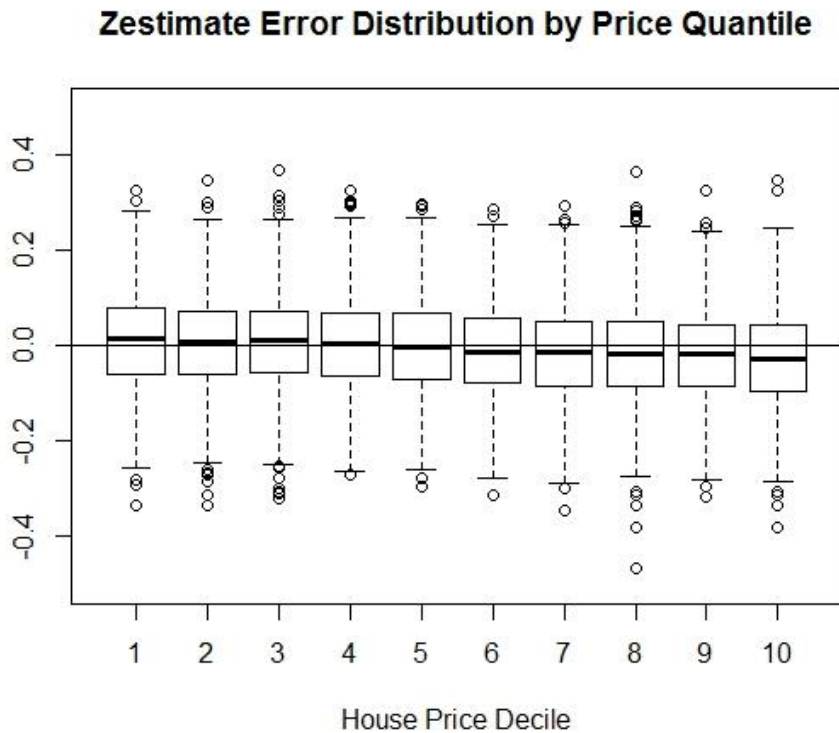
Base:
hist()

ggplot2:
+ geom_histogram()

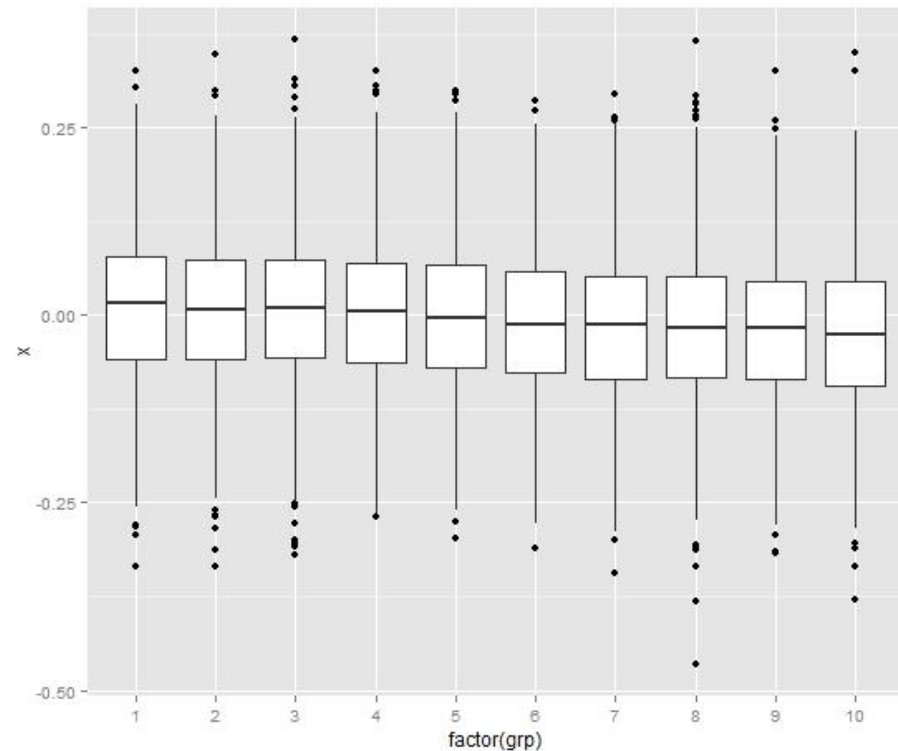


Visual Exploration

> Boxplots:



Base:
`boxplot()`



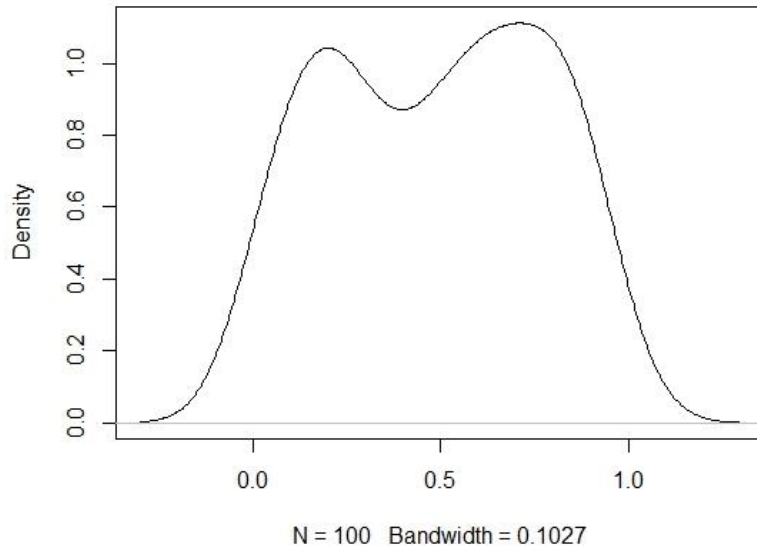
ggplot2:
`+ geom_boxplot()`



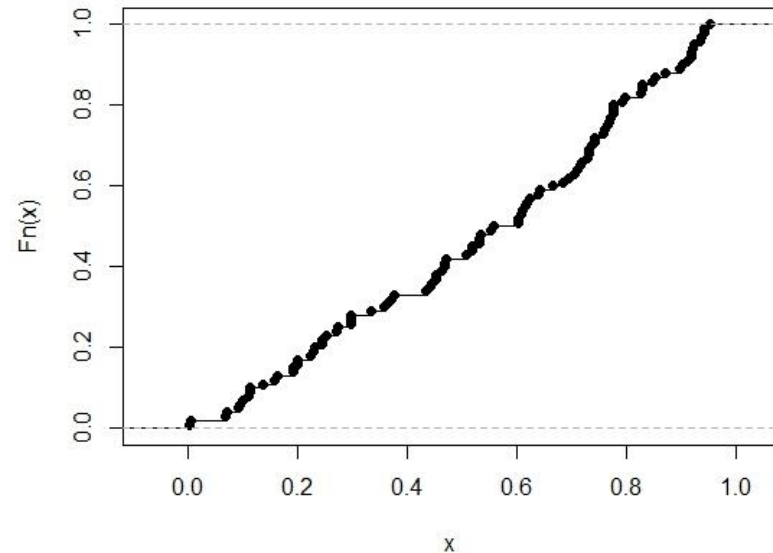
Visual Exploration

> Densities/CDFs:

`density.default(x = runif(100))`



`ecdf(runif(100))`



Base:

`plot(density())`

`plot(ecdf())`

ggplot2:

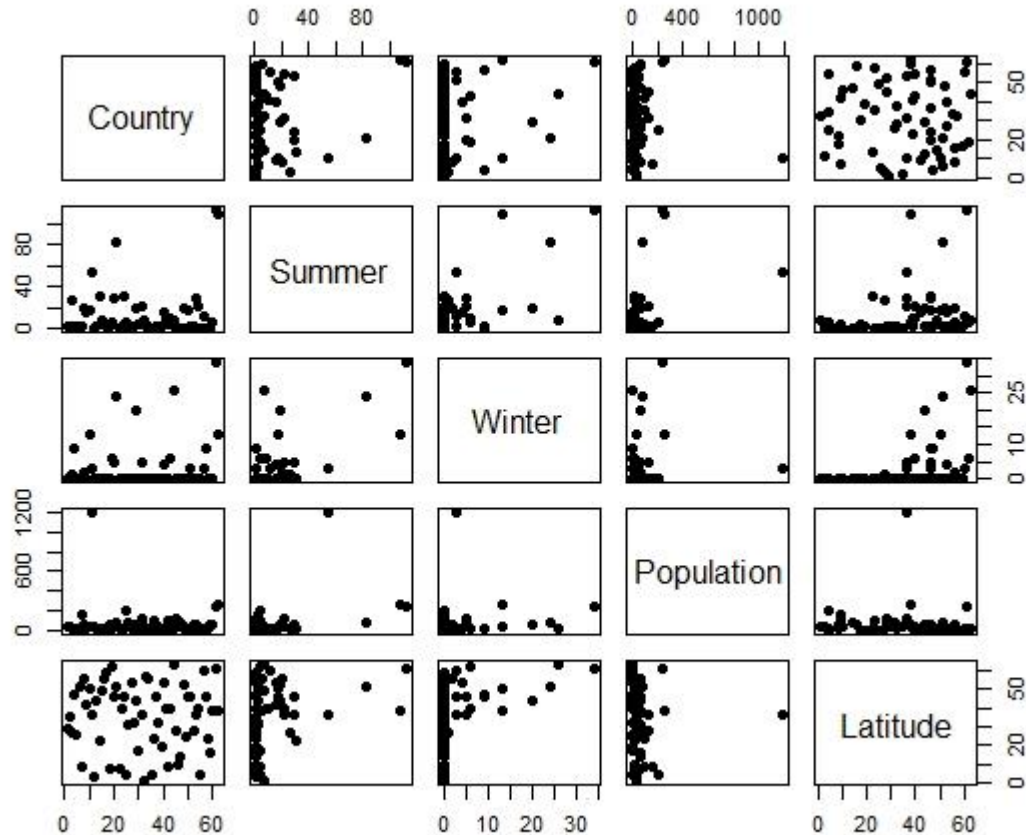
`+ geom_density()`

`+ stat_ecdf()`

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Visual Exploration

> Scatterplots



Base:
pairs()

ggplot2:
ggpairs()

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R Resources

- R page:
 - > <http://www.r-project.org/other-docs.html>
- Stackoverflow:
 - > <http://www.stackoverflow.com>
- ‘Little’ R intro:
 - > <http://cran.r-project.org/doc/contrib/Rossiter-RIntro-ITC.pdf>
- Quick R:
 - > <http://statmethods.net/>
- There are many tutorials available online, e.g.,
 - > <http://cyclismo.org/tutorial/R/>
- Notes from a two day course at UW:
 - > <http://faculty.washington.edu/tlumley/Rcourse/>
- Hadley Wickham’s Style Guide:
 - > <http://adv-r.had.co.nz/Style.html>
- DataCamp R Exercises:
 - > Link in Canvas announcements.



Assignment

> Go to:

- Vote for extra topics (time permitting)
- <https://www.surveymonkey.com/r/SK6VX5T>

> Complete Homework 1:

- Explore 'JitteredHeadCount.csv', a data set from Caesar's Entertainment that has falsified/jittered table headcounts.
- Write **script level** R program that shows/illustrates 3 key takeaways of your choosing from exploring the data.
- You should submit:
 - > **ONE R-script.**
 - > **One word document with 3 key points.** (example next page).

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Example Takeaway

- > The aggregate table headcounts on the weekends are X% higher than non-weekends (figure 1). In fact, the game that has the highest difference between average highs and average low days is Gamecode AA with a difference of x.xx heads/table.
- > R script Example Demo

