Chapter 26

Sections 26.1, 26.2, 26.3, 26.5, 26.6, and 26.8 Gravimetric Analysis, Precipitation Titrations, and Combustion Analysis

In gravimetric analysis, the mass of a product used to calculate the quantity of the original analyte through a process of precipitation of the analyte, isolation of the precipitate, and weighing the isolated product.

Analyte \rightarrow insoluble form \rightarrow dry or ignite ppt. \rightarrow weigh the ppt.

Uses of gravimetric analysis...

- Chemical analysis of ores and industrial materials
- Calibration of instrumentation
- Elemental analysis of inorganic compounds
- 1. A weighed sample is dissolved
- 2. An excess of a precipitating agent is added to this solution
- 3. The resulting precipitate is filtered, dried (or ignited) and weighed
- 4. From the mass and known composition of the precipitate, the amount of the original ion can be determined

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26.1 Examples of Gravimetric Analysis

Example 1) A 10.00-mL solution containing Cl⁻ was treated with excess AgNO₃ to precipitate 0.436 8 g of AgCl (143.321 g/mol). What was the molarity of Cl⁻ in the unknown?

$$Ag^+ + Cl^- \rightarrow AgCl(s)$$
 (26-1)

$$mol \ AgCl = \frac{0.4368 \ g \ AgCl}{143.321 \ g \ AgCl/mol \ AgCl} = 3.048 \ \times 10^{-3} = mol \ Cl^{-3}$$

$$[Cl^{-}] = \frac{3.048 \times 10^{-3} \, mol}{0.01000 \, L} = 0.3048 \, M$$

Q) How many grams of Br^- (FM = 79.904 g/mol) were in a sample that produced 1.000 g of AgBr precipitate (FM = 187.77 g/mol)? (Answer: 0.425 5 g)

Example 2) When 0.091 92 g of pure RaCl₂ was dissolved and treated with excess AgNO₃, 0.088 90 g of AgCl precipitated. How many moles of Cl⁻ were in the RaCl₂? From this measurement, find the atomic mass of Ra.

$$mol \ AgCl = \frac{0.08890 \ g \ AgCl}{143.321 \ g \ AgCl/mol \ AgCl} = 6.202_9 \times 10^{-4} = mol \ Cl^{-1}$$

$$mol\ RaCl_2 = 6.202_9 \times 10^{-4}\ mol\ Cl^- \times \frac{1\ mol\ RaCl_2}{2\ mol\ Cl^-} = 3.101_4 \times 10^{-4}$$

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$$molar\ mass\ of\ RaCl_2 = \frac{0.09192\ g}{3.101_4 \times 10^{-4}\ mol} = 296.3_8\ g/mol$$

Formula mass of
$$RaCl_2 = atomic mass of Ra + 2\left(35.453 \frac{g}{mol}\right) = 296.3_8$$

atomic mass of
$$Ra = 296.3_8 - 70.906 = 225.5 g/mol$$

Q) How many grams of AgBr (FM = 187.77 g/mol) would have been formed from 0.100 g of RaBr₂ (FM = 385.808 g/mol)? (Answer: 0.097 g)

Representative analytical precipitations are listed in **Table 26-1**. A few common organic precipitants (agents that cause precipitation) are listed in **Table 26-2**.

Conditions must be controlled to selectively precipitate one species. Potentially interfering substances may need to be removed prior to analysis.

TABLE 26-1 Representative gravimetric analyses

Species analyzed	Precipitated form	Form weighed	Interfering species	
K ⁺	KB(C ₆ H ₅) ₄	KB(C ₆ H ₅) ₄	NH ₄ , Ag ⁺ , Hg ²⁺ , Tl ⁺ , Rb ⁺ , Cs ⁺	
Mg ²⁺	Mg(NH ₄)PO ₄ · 6H ₂ O	Mg ₂ P ₂ O ₇	Many metals except Na ⁺ and K ⁺	
Ca ²⁺	CaC ₂ O ₄ · H ₂ O	CaCO ₃ or CaO	Many metals except Mg2+, Na+, K+	
Ba ²⁺	BaSO ₄	BaSO ₄	Na+, K+, Li+, Ca2+, Al3+, Cr3+, Fe3+, Sr2+, Pb2+, NO3	
Ti ⁴⁺	TiO (5,7-dibromo-8- hydroxyquinoline) ₂	Same	Fe ³⁺ , Zr ⁴⁺ , Cu ²⁺ , C ₂ O ₄ ²⁻ , eitrate, HF	
VO ₄	Hg ₃ VO ₄	V2O5	Cl ⁻ , Br ⁻ , l ⁻ , SO ₄ ²⁻ , CrO ₄ ²⁻ , AsO ₄ ³⁻ , PO ₄ ³⁻	
Cr3+	PbCrO ₄	PbCrO ₄	Ag^+ , NH_4^+	
Mn ²⁺	Mn(NH ₄)PO ₄ · H ₂ O	$Mn_2P_2O_7$	Many metals	
Fe ³⁺	Fe(HCO ₂) ₃	Fe ₂ O ₃	Many metals	
Co ²⁺	Co(1-nitroso-2-naphtholate) ₂	CoSO ₄ (by reaction with H ₂ SO ₄)	Fe ³⁺ , Pd ²⁺ , Zr ⁴⁺	
Ni ²⁺	Ni(dimethylglyoximate)2	Same	Pd ²⁺ , Pt ²⁺ , Bi ³⁺ , Au ³⁺	
Cu ²⁺	CuSCN (a ter reduction o Cu ²⁺ to Cu ⁺ with HSO ₁)	CuSCN	NH ₄ ⁺ , Pb ²⁺ , Hg ²⁺ , Ag ⁺	
Zn ²⁺	Zn(NH ₄)PO ₄ · H ₂ O	Zn ₂ P ₂ O ₂	Many metals	
Ce ⁴⁺	Ce(IO ₃) ₄	CeO ₂	Th4+, Ti4+, Zr4+	
Al ³⁺	Al(8-hydroxyquinolate)3	Same	Many metals	
Sn ⁴⁺	Sn(cup erron) ₄	SnO ₂	Cu^{2+} , Pb^{2+} , $As(III)$	
Pb ²⁺	PbSO ₄	PbSO ₄	Ca2+, Sr2+, Ba2+, Hg2+, Ag+, HCl, HNO3	
NH ⁺ ₄	$NH_4B(C_6H_5)_4$	$NH_4B(C_6H_5)_4$	K ⁺ , Rb ⁺ , Cs ⁺	
CI-	AgCI	AgCl	Br-, 1-, SCN-, S2-, S2O3-, CN-	
Br -	AgBr	AgBr	CI ⁻ , I ⁻ , SCN ⁻ , S ²⁻ , S ₂ O ₃ ²⁻ , CN ⁻	
I T	AgI	AgI	Cl ⁻ , Br ⁻ , SCN ⁻ , S ²⁻ , S ₂ O ₃ ²⁻ , CN ⁻	
SCN-	CuSCN	CuSCN	NH ₄ , Pb ²⁺ , Hg ²⁺ , Ag ⁺	
CN ⁻	AgCN	AgCN	Cl ⁻ , Br ⁻ , l ⁻ , SCN ⁻ , S ² ⁻ , S ₂ O ₃ ² ⁻	
F	(C ₆ H ₅) ₃ SnF	(C ₆ H ₅) ₃ SnF	Many metals (except alkali metals), SiO ₄ ⁴⁻ , CO ₃ ²⁻	
CIO	KCIO ₄	KCIO ₄	connection that is a particle of the particl	
SO ₄ ²	BaSO ₄	BaSO ₄	Na+, K+, Li+, Ca2+, Al3+, Cr3+, Fe3+, Sr2+, Pb2+, NO3	
PO4 -	Mg(NH ₄)PO ₄ · 6H ₂ O	Mg ₂ P ₂ O ₇	Many metals except Na+, K+	
NO ₁	Nitron nitrate	Nitron nitrate	ClO ₄ , 1 ⁻ , SCN ⁻ , CrO ₄ ² , ClO ₁ , NO ₇ , Br ⁻ , C ₇ O ₄ ²	
CO2-	CO2 (by acidification)	CO ₂	(The liberated CO2 is trapped with Ascarite and weighed.)	

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TABLE 26-2 Common organic precipitating agents

Name	Structure	Ions precipitated
Dimethylglyoxime	\nearrow_{N-OH}^{N-OH}	Ni^{2+} , Pd^{2+} , Pt^{2+}
Cupferron	$ \bigcirc N = 0 $ $ O^{-}NH_{4}^{+} $	$Fe^{3+}, VO_2^+, Ti^{4+}, Zr^{4+}, Ce^{4+}, Ga^{3+}, Sn^{4+}$
8-Hydroxyquinoline (oxine)	OH OH	$\begin{array}{l} Mg^{2+},Zn^{2+},Cu^{2+},Cd^{2+},Pb^{2+},Al^{3+},Fe^{3+},Bi^{3+},\\ Ga^{3+},Th^{4+},Zr^{4+},UO_2^{2+},TiO^{2+} \end{array}$
Salicylaldoxime	OH OH	Cu^{2+} , Pb^{2+} , Bi^{3+} , Zn^{2+} , Ni^{2+} , Pd^{2+}
1-Nitroso-2-naphthol	ООООН	Co^{2+} , Fe^{3+} , Pd^{2+} , Zr^{4+}
Nitron	C_6H_5 $N_{+}^{-N}C_6H_5$ C_6H_5	NO ₃ ⁻ , ClO ₄ ⁻ , BF ₄ ⁻ , WO ₄ ²⁻
Sodium tetraphenylborate Tetraphenylarsonium chloride	$Na^{+}B(C_6H_5)_4^{-}$ $(C_6H_5)_4As^{+}Cl^{-}$	$K^+, Rb^+, Cs^+, NH_4^+, Ag^+,$ organic ammonium ions $Cr_2O_7^{2-}, MnO_4^-, ReO_4^-, MoO_4^{2-}, WO_4^{2-}, ClO_4^-, I_3^-$

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26.2 Precipitation

The ideal product of a gravimetric analysis should be:

- 1. Insoluble
- 2. Easily filterable
- 3. Very pure
- 4. Possess a known composition.
- → We need to control precipitation conditions:

Solubility:

- * Solubility depends on the temperature and the solvent.
- * The solubility of a precipitate is usually decreased by cooling the solution.

Filterability:

- * Particles of precipitate should not be so small that they clog or pass through the filter.
- * Large crystals are easily filterable and also have less surface area to which foreign species may attach.
- * At the other extreme is a colloidal suspension of particles that have diameter in the range 1-500 nm and pass through most filters.

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Crystal Growth:

* Crystallization occurs in two phases: nucleation and particle growth.

During nucleation: molecules in solution come together randomly and form small aggregates.

Particle growth: involves the addition of more molecules to the nucleus to form a crystal.

In a highly supersaturated solution: nucleation precedes faster than particle growth \rightarrow the results a suspension of tiny particles or, worse, a colloid.

Techniques that promote particle growth include:

- 1. Raising the temperature to increase solubility and thereby decrease supersaturation
- 2. Adding precipitant slowly with vigorous mixing, to prevent a local, highly supersaturated condition where the stream of precipitant first enters the analyte
- 3. Using a large volume of solution so that concentrations of analyte and precipitant are low

Homogenous Precipitation:

Is a technique used for controlling supersaturation. In this technique the precipitant is generated slowly by a chemical reaction (Table 26-3).

Particle size of ferric formate is enhanced by using urea to generate OHions slowly.

For example, urea decomposes slowly in boiling water to produce OH⁻:

$$(H_2N)_2CO + 3H_2O \xrightarrow{Heat} CO_2 + 2NH_4^+ + 2OH^-$$
 (26 – 2)
Urea
 $HCOOH + OH^- \rightarrow HCO_2^- + H_2O$ (26 – 3)
Formic acid Formate
 $3HCO_2^- + Fe^{3+} \rightarrow Fe(HCO_2)_3.nH_2O(s)$ (26 – 4)
Fe(III)formate

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 Table 27-3
 Common reagents used for homogeneous precipitation

Precipitant	Reagent	Reaction	Some elements precipitated
OH-	Urea	$(H_2N)_2CO + 3H_2O \rightarrow CO_2 + 2NH_4^+ + 2OH^-$	Al, Ga, Th, Bi, Fe, Sn
OH-	Potassium cyanate	$HOCN + 2H_2O \rightarrow NH_4^+ + CO_2 + OH^-$ Hydrogen cyanate	Cr, Fe
		S O	
S ²⁻	Thioacetamide ^a	$CH_3CNH_2 + H_2O \rightarrow CH_3CNH_2 + H_2S$	Sb, Mo, Cu, Cd
SO ₄ ²⁻	Sulfamic acid	$^{+}_{3}NSO_{3}- + H_{2}O \rightarrow NH_{4}^{+} + SO_{4}^{2-} + H^{+}$	Ba, Ca, Sr, Pb
		OO 	
C ₂ O ₄ ²⁻	Dimethyl oxalate	$\text{CH}_3\text{OCCOCH}_3 + 2\text{H}_2\text{O} \rightarrow 2\text{CH}_3\text{OH} + \text{C}_2\text{O}_4^{\ 2-} + 2\text{H}^+$	Ca, Mg, Zn
PO ₄ ³⁻	Trimethyl phosphate	$(CH_3O)_3P = O + 3H_2O \rightarrow 3CH_3OH + PO_4^{3-} + 3H^+$	Zr, Hf
CrO ₄ ²⁻	Chromic ion plus bromate	$2Cr^{3+} + BrO_3^{-} + 5H_2O \rightarrow 2CrO_4^{2-} + Br^{-} + 10H^{+}$	Pb
		O	
8-Hydroxyquinoline	8-Acetoxyquinoline	CH_3CO OH OH CH_3CO_2H	Al, U, Mg, Zn

a. Hydrogen sulfide is volatile and toxic; it should be handled only in a well-vented hood. Thioacetamide is a carcinogen that should be handled with gloves. If thioacetamide contacts your skin, wash yourself thoroughly immediately. Leftover reagent is destroyed by heating at 50°C with 5 mol of NaOCl per mole of thioacetamide. [H. Elo, J. Chem. Ed. 1987, 64, A144.]

Precipitation in the Presence of Electrolyte

Ionic compounds are usually precipitated in the presence of an electrolyte. To understand why, we must discuss how tiny colloidal crystallites *coagulate* (come together) into larger crystals. Figure 26-2 shows a colloidal particle of AgCl growing in a solution containing excess Ag^+ , H^+ , and NO_3^- . The surface of the particle has excess positive charge due to the **adsorption** of extra silver ions on exposed chloride ions. (To be adsorbed means to be attached to the surface. In contrast, **absorption** means penetration beyond the surface, to the inside.) The positively charged surface attracts anions and repels cations from the *ionic atmosphere* (Figure 26-2) surrounding the particle. The positively charged particle and the negatively charged ionic atmosphere together are called the **electric double layer.**

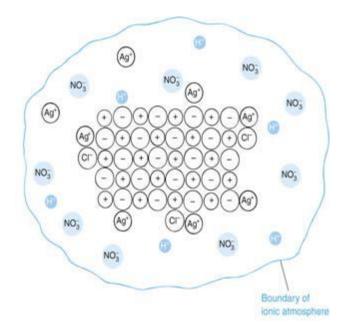


Figure 26-2

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Colloidal particles must collide with one another to coalesce. However, the negatively charged ionic atmospheres of the particles repel one another. Particles must have enough kinetic energy to overcome electrostatic repulsion before they can coalesce.

Heating promotes coalescence by increasing the kinetic energy. Increasing electrolyte concentration (HNO₃ for AgCl) decreases the volume of the ionic atmosphere and allows particles to come closer together before electrostatic repulsion becomes significant. For this reason, most gravimetric precipitations are done in the presence of an electrolyte.

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Digestion:

Liquid from which a substance precipitates or crystallizes is called the mother liquor. After precipitation, most procedures call for a period of standing in the presence of the hot mother liquor. This treatment, called digestion, promotes slow recrystallization of the precipitate. Particle size increases and impurities tend to be expelled from the crystal.

Purity:

Contamination of the precipitate by impurities can be classified as:

- 1) Coprecipitation and 2) Postprecipitation
- 1) **Coprecipitation**: Precipitation of impurities along with the desired product, even though the solubility of the impurity has not been exceeded
- **Coprecipitation** occurs to some degree in every gravimetric analysis and cannot be avoided, but can be minimized by careful precipitation and a thorough washing of the precipitate.
- Coprecipitation can occur by
- A) Adsorption: impurities are bound to the surface of a crystal.
- B) **Absorption**: impurities are held within the crystal.

Absorbed impurities within the crystal are classified as **inclusions** or **occlusions**:

B1) **inclusions**: are impurity ions that randomly occupy sites in the crystal lattice normally occupied by ions that belong in the crystal. The chance of inclusions increases when the impurity ion has a similar size and charge to one of the ions that belong to the product (precipitate). Example: K⁺ in NH₄MgPO₄ (K⁺ is similar to NH₄⁺)

B2) **occlusions**: are impurities trapped (sometimes with solvent) in pockets inside the growing crystal.

Coprecipitation tends to be worst in colloidal precipitates such as BaSO₄, Al(OH)₃, and Fe(OH)₃, which all have a large surface area. Many procedures call for washing away the mother liquor, redissolving the precipitate, and *reprecipitating* the product. During the second precipitation, the concentration of impurities in solution is lower than during the first precipitation, and the degree of coprecipitation therefore tends to be lower.

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There is an advantage for coprecipitation to gather the trace components.

- * The precipitate used to collect the trace component is called a **gathering** agent and the process is called **gathering**.
- Toxic metals such as natural arsenic in drinking water in Bangladesh can be removed from wastewater by coprecipitation with Fe(OH)₃. Fe(II) or Fe(s) is added to the water and oxidized in air for several hours to precipitate Fe(OH)₃. After filtration through sand to remove solids, the water is drinkable.

Masking agents

- Some impurities can be treated with a **masking agent** to prevent them from reacting with the precipitant.
- In the gravimetric analysis of Be²⁺, Mg²⁺, Ca²⁺, or Ba²⁺ with the reagent *N-p*-chlorophenylcinnamohydroxamic acid (RH), impurities such as Mn²⁺, Ag²⁺, Zn²⁺, Cd²⁺, Hg²⁺, Fe²⁺, and Ga³⁺ are kept in solution by excess KCN. Pb²⁺, Pd²⁺, Sb³⁺, Sn²⁺, Bi³⁺, Zr⁴⁺, Ti⁴⁺, V⁵⁺, and Mo⁶⁺ are masked with a mixture of citrate and oxalate.

$$Ca^{2+}$$
 + 2RH \rightarrow $CaR_2(s)$ + 2H⁺
Analyte precipitate

 Mn^{2+} + $6CN^ \rightarrow$ $Mn(CN)_6^{4-}$
Impurity (interfering ion) Masking agent Stays in solution

2) Postprecipitation: adsorption (collection) of impurities on the precipitate while it standing in the mother liquor (after the precipitation is over). An example is the crystallization of MgC_2O_4 on CaC_2O_4 .

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Washing of precipitates:

After collection of the precipitate on the filter, it has to be washed to remove any droplets of the mother liquor that contain excess solute.

Some precipitates can be washed with water, but many require electrolyte to maintain coherence. For these precipitates, the ionic atmosphere is required to neutralize the surface charge of the tiny particles. If electrolyte is washed away with water, the charged solid particles repel one another and the product breaks up. This breaking up, called **peptization**, results in loss of product through the filter. AgCl will peptize if washed with water, so it is washed with dilute HNO₃ instead. Electrolyte used for washing must be volatile so that it will be lost during drying. Volatile electrolytes include HNO₃, HCl, NH₄NO₃, NH₄Cl, and (NH₄)₂CO₃.

$$NH_4Cl(s) \xrightarrow{heat} NH_3(g) + HCl(g)$$

Product Composition:

- * The final product must have a stable and known composition
- * A **hygroscopic substance** is one that picks up water from the air and is therefore difficult to weigh accurately.
- * Many precipitates contain a variable quantity of water and must be dried under conditions that give a known (possibly zero) stoichiometry of H₂O.
- * Ignition (strong heating) is often used to change the chemical form of some precipitates.

Examples:

$$Fe(HCO_2)_3.nH_2O \xrightarrow{850^{\circ}C \ for \ 1 \ hour} Fe_2O_3$$

$$Mg(NH_4)PO_4.6H_2O \xrightarrow{1100^{\circ}C} Mg_2 P_2O_7$$

In thermogravimetric analysis, a substance is heated, and its mass is measured as a function of temperature. Figure 26-4 shows how the composition of calcium salicylate changes in four stages: Figure 26-4 shows how the composition of calcium salicylate changes in four stages:

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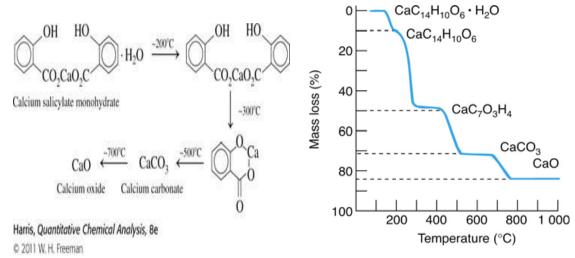


Figure 26-4 Thermogravimetric curve for calcium salicylate

The composition of the product depends on the temperature and duration of heating.

26.3 Examples of Gravimetric Calculations

:NH HN: +
$$2CH_3CO_2H \rightarrow H_2N NH_2(CH_3CO_2)_2$$

Piperazine Acetic acid Piperazine diacetate
FM 86.136 FM 60.052 FM 206.240

Unnumbered figure pg 635a

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Example 1: The piperazine content of an impure commercial material can be determined by precipitating and weighing the diacetate. In one experiment, 0.312 6 g of sample was dissolved in 25 mL of acetone, and 1 mL of acetic acid was added. After 5 min, the precipitate was filtered, washed with acetone, dried at 110°C, and found to weigh 0.712 1 g. Find the wt% of piperazine in the sample.

For each mole of piperazine in the impure material, 1 mol of product is formed.

moles of piperazine diacetate =
$$\frac{0.7121 \text{ g}}{206.240}$$
 = 3.453×10^{-3} mol = moles of piperazine

mass of piperazine =
$$(3.453 \times 10^{-3} \text{ mol}) \left(86.136 \frac{g}{\text{mol}}\right) = 0.2974 \text{ g}$$

Percentage of piperazine =
$$\frac{0.2974 \text{ g}}{0.3126 \text{ g}} \times 100 = 95.14\%$$

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Q) A 0.3854 g sample gave 0.8000 g of product. Find the wt% of piperazine in the sample.

Answer: 86.69%

Example 2: (a) To measure the nickel content in steel, the alloy is dissolved in 12 M HCl and neutralized in the presence of citrate ion, which maintains iron in solution. The slightly basic solution is warmed, and dimethylglyoxime (DMG) is added to precipitate the red DMG-nickel complex quantitatively. The product is filtered, washed with cold water, and dried at 110°C.

If the nickel content is known to be near 3 wt% and you wish to analyze 1.0 g of steel, what volume of 1.0 wt% alcoholic DMG solution should be used to give a 50% excess of DMG for the analysis? Assume that the density of the alcohol solution is 0.79 g/mL.

Because the Ni content is about 3%, 1.0 g of steel will contain about 0.03 g of Ni

moles of
$$Ni = \frac{0.03 \ g}{58.69 \ g/mol} = 5.11 \times 10^{-4} \ mol$$

moles of DMG =
$$2 \times 5.11 \times 10^{-4}$$
 mol = 1.02×10^{-3}

mass of DMG =
$$1.02 \times 10^{-3} \times 116.12 \frac{g}{mol} = 0.118 g$$

100 g solution
$$\rightarrow$$
 1 g DMG
? \rightarrow 0.118 g

mass of solution needed =
$$\frac{100 \times 0.118 g}{1 g}$$
 = 11.8 g

volume of solution needed =
$$\frac{11.8 \text{ g}}{0.79 \text{ g/mL}} = 15 \text{ mL}$$

volume of solution neede to give 50% excess = 1.5×15 mL = 23 mL

(b) If 1.163 4 g of steel gives 0.179 5 g of precipitate, what is the percentage of Ni in the steel?

moles of
$$Ni(DMG)_2 = \frac{0.1795 g}{288.91 g/mol} = 6.213 \times 10^{-4}$$

= moles of Ni
mass of $Ni = 6.213 \times 10^{-4} mol \times 58.69 \frac{g}{mol} = 0.03646 g$

Percentage of Ni in steel =
$$\frac{0.03646 \text{ g}}{1.1634 \text{ g g}} \times 100 = 3.134\%$$

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Example 3: A problem with two components

A mixture of the 8-hydroxyquinoline complexes of Al and Mg weighed 1.084 3 g. When ignited in a furnace open to the air, the mixture decomposed, leaving a residue of Al₂O₃ and MgO weighing 0.134 4 g. Find the weight percent of Al(C₉H₆NO)₃ in the original mixture.

Unnumbered figure pg 636

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We will abbreviate the 8-hydroxyquinoline anion as Q. Letting the mass of AlQ₃ be x and the mass of MgQ₂ be y, we can write

26.5 Precipitation Titration Curves

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- Precipitation titrations are used in very limited instances, but are widely used to explain titration theory.
- Usually in a precipitation titration, we are determining some analyte that the titrant forms a precipitate with.
- For example, one can determine the concentration of many anions (especially halides) using silver as a titrant.

$$Ag^{+}(aq) + Cl^{-}(aq) \leftrightarrows AgCl(s)$$
Analyte Titrant

- ➤ The **titration curve** is a plot of how the concentration of a reactant varies with titrant
- ➤ Concentration varies over orders of magnitude, so it is useful to plot the p function

P Function:
$$pX = -log_{10}[X]$$

where [X] is the concentration of X.

➤ A titration curve has three distinct regions: before, at, and after the equivalence point

Steps....

- ➤ Write a balanced equation
- \triangleright Write the K_{sp} equilibrium expression
- \triangleright Calculate V_{eq} (volume of equivalence point)
- ➤ Determine where in the titration curve you are (Before, At, After Veq)
- > Solve
- ➤ Plot Titration Curve if necessary
- > Let's sketch the titration curve

Consider the titration of 25.00 mL of 0.1000 M I⁻ with 0.05000 M Ag⁺,

Titration reaction:
$$I^- + Ag^+ \rightarrow AgI(s)$$
 (26-9)

and suppose that we are monitoring $[Ag^+]$ with an electrode. Reaction 26-9 is the reverse of the dissolution of AgI(s), whose solubility product is rather small:

$$AgI(s) \leftrightarrows Ag^+ + I^- \quad K_{sp} = [Ag^+][I^-] = 8.3 \times 10^{-17} \quad (26 - 10)$$

The equilibrium constant for the titration reaction 26-9 is large ($K = \frac{1}{K_{sp}} = 1.2 \times 10^{16}$), so the equilibrium lies far to the right. Each aliquot of Ag^+ reacts nearly completely with I^- , leaving only a tiny amount of Ag^+ in solution. At the equivalence point, there will be a sudden increase in $[Ag^+]$ because there is no I^- left to consume the added Ag^+ .

What volume of Ag^+ titrant is needed to reach the equivalence point? We calculate this volume, designated V_e , with the fact that 1 mol of Ag^+ reacts with 1 mol of I^-

At the equivalence point (V_e) :

moles of
$$Ag^+ = moles \ of \ I^-$$

$$0.05000 \times V_e = 0.1000 \times 25.00$$

$$V_e = \frac{0.1000 \times 25.00}{0.05000} = 80.00 \ mL$$

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Before the Equivalence Point

Suppose that 10.00 mL of Ag^+ have been added. There are more moles of I^- than Ag^+ at this point, so virtually all Ag^+ is "used up" to make AgI(s). We want to find the small concentration of Ag^+ remaining in solution after reaction with I^- . Imagine that Reaction 26-9 has gone to

completion and that some AgI redissolves (Reaction 26-10). The solubility of Ag^+ is determined by the concentration of free I^- remaining in the solution:

$$[Ag^+] = \frac{K_{sp}}{[I^-]} \tag{26-11}$$

Free I^- is overwhelmingly from the I^- that has not been precipitated by 10.00 mL of Ag^+ . By comparison, I^- from dissolution of AgI(s) is negligible. So let's find the concentration of unprecipitated I^- :

Moles of
$$I^-$$
 = original mols of I^- — moles of Ag^+ added
= $(0.025\ 00\ L)(0.100\ mol/L)$ — $(0.010\ 00\ L)(0.050\ 00\ mol/L)$ = $0.002\ 000\ mol\ I^-$

The volume is 0.035~00~L~(25.00~mL + 10.00~mL), so the concentration is

$$[I^{-}] = \frac{0.002000 \ mol \ I^{-}}{0.03500 \ L} = 0.05714 \ M \qquad (26 - 12)$$

The concentration of Ag^+ in equilibrium with this much I^- is

$$[Ag^{+}] = \frac{K_{sp}}{[I^{-}]} = \frac{8.3 \times 10^{-17}}{0.05714} = 1.4_{5} \times 10^{-15} M \qquad (26 - 13)$$
$$p^{Ag^{+}} = -log[Ag^{+}] = -log1.4_{5} \times 10^{-15} = 14.84 \qquad (26 - 14)$$

Shortcut Calculations

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The preceding step-by-step calculation is a tedious way to find the concentration of I^- . Here is a streamlined procedure that is well worth learning. Bear in mind that Ve = 50.00 mL. When 10.00 mL of Ag^+ have been added, the reaction is **one-fifth** complete because 10.00 mL out of the 50.00 mL of Ag^+ needed for complete reaction have been added. Therefore, **fourfifths** of the I^- is unreacted. If there were no dilution, $[I^-]$ would be four-fifths of its original value. However, the original volume of 25.00 mL has been increased to 35.00 mL. If no I^-

had been consumed, the concentration would be the original value of $[I^-]$ times (25.00/35.00). Accounting for both the reaction and the dilution, we can write

$$[I^{-}] = \begin{pmatrix} \frac{40}{50} \end{pmatrix} \quad (0.1000 \, M) \quad \begin{pmatrix} \frac{25.00}{35.00} \end{pmatrix} = 0.05714 \, M$$
Fraction Original Dilution remaining concentration factor

This is the same result found in Equation 26-12.

25.00 mL is the original volume of I^- 35.00 mL is the total volume of solution

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EXAMPLE Using the Streamlined Calculation

Let's calculate pAg^+ when (the volume added from the buret) is 49.00 mL.

$$\begin{bmatrix} I^{-} \end{bmatrix} = \left(\frac{1}{50}\right) (0.1000 \text{ M}) \left(\frac{25.00}{74.00}\right) = 6.76 \times 10^{-4} \text{M}$$

$$\begin{bmatrix} Ag^{+} \end{bmatrix} = \frac{K_{sp}}{\boxed{I^{-}}} = \frac{8.3 \times 10^{-17}}{6.76 \times 10^{-4} \text{M}} = 1.2 \times 10^{-13} \text{ M}$$

$$pAg^{+} = -\log \left[Ag^{+}\right] = -\log \left[1.2 \times 10^{-13}\right] = 12.91$$

The concentration of Ag^+ is negligible compared with the concentration of unreacted I^- , even though the titration is 98% complete.

Question: Find p Ag^+ at 49.1 mL. (Answer: 12.86)

At the Equivalence Point

- At the equivalence point, we have added the exact amount of Ag⁺ needed to react with I⁻
 - \triangleright pAg⁺ is found by solving for *x* from K_{sp}

$$[Ag^+][I^-] = K_{sp}$$

$$(x)(x) = 8.3 \times 10^{-17} \rightarrow x = 9.1 \times 10^{-9} \rightarrow pAg^{+} = -log 9.1 \times 10^{-9} = 8.04$$

This value of pAg^+ is independent of the original concentrations or volumes.

After the Equivalence Point

- ➤ After the equivalence point, pAg⁺ is simply determined by calculating the excess Ag⁺
- ➤ Suppose we have added 52.00 mL of Ag⁺ solution. The volume past the equivalence point is 2.00 mL. The calculation proceeds as follows

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$$mol Ag_{excess}^{+} = (0.00200 L)(0.050 M) = 0.000100 mol$$
$$[Ag^{+}] = 0.000100 mol/0.07700 L = 1.30 \times 10^{-3} M$$
$$pAg^{+} = -log[Ag^{+}] = -log[1.30 \times 10^{-3}] = 2.89$$

For a streamlined calculation, the concentration of Ag^+ in the burette is 0.050 00 M, and 2.00 mL of titrant are being diluted to (25.00 + 52.00) = 77.00 mL. Hence, $[Ag^+]$ is

$$[Ag^{+}] = (0.05000 \, M) \left(\frac{2.00}{77.00}\right) = 1.3 \times 10^{-3} \, M$$

$$\begin{array}{cc} Original & Dilution \\ concentration & factor \\ of Ag^{+} \end{array}$$

2.00 mL is the volume of excess Ag^+ 77.00 mL is the total volume of solution

The Shape of the Titration Curve

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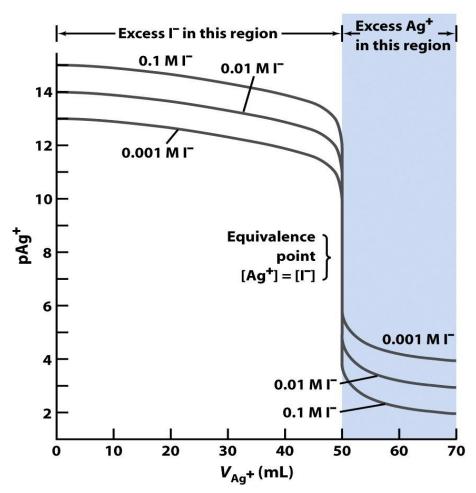


Figure 7-6

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Figure 26-8

Titration curves in Figure 26-8 illustrate the effect of **reactant concentration**. The equivalence point is the steepest point of the curve. In titrations involving 1:1 stoichiometry of reactants, the equivalence point is the steepest point of the titration curve. For stoichiometries other than 1:1, such as $2Ag^+ + CrO_4^{2-} \rightarrow Ag_2CrO_4(s)$, the curve is not symmetric. The equivalence point is not at the center of the steepest section of the curve, and it is not an inflection point.

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Effect of K_{sp} on the Curve

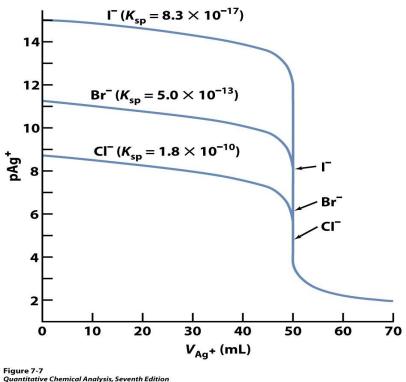


Figure 26-9: Titration curves showing the effect of K_{sp} . Each curve is calculated for 25.00 mL of 0.100 0 M halide titrated with 0.050 00 M Ag^+ . Equivalence points are marked by arrows.

Figure 26-9 illustrates how K_{sp} affects the titration of halide ions. The least soluble product, AgI, gives the sharpest change at the equivalence point. However, even for AgCl, the curve is steep enough to locate the equivalence point accurately. The larger the equilibrium constant for a titration reaction, the more pronounced will be the change in concentration near the equivalence point.

Example

 25.00 mL of 0.04132 M Hg₂(NO₃)₂ was titrated with 0.05789 M KIO₃:

$$Hg_2^{2+}(aq) + 2IO_3^{-}(aq) \rightarrow Hg_2(IO_3)_2(s)$$

Ksp for $Hg_2(NO_3)_2$ is $1.3x10^{-18}$ Calculate the concentration of Hg_2^{2+} in solution

- after addition of 34.00 mL KIO₃,
- after addition of 36.00 mL KIO₃, and
- at the equivalence point

The volume of iodate needed to reach the equivalence point is found as follows:

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moles of
$$IO_3^- = 2moles$$
 of Hg_2^+
 $(0.05789 M) \times (V_e) = 2(0.04132 M)(25.00 mL)$
 $V_e = 35.69 mL$

(A) After addition of 34.00 mL KIO₃

Example A

 □If V=34.00 mL, Hg₂⁺² precipitation is not complete

$$[Hg_2^{2+}] = \left(\frac{35.69 - 34.00}{35.69}\right)(0.04132 \text{ M})\left(\frac{25.00}{25.00 + 34.00}\right) = 8.29 \times 10^{-4} \text{ M}$$
From Remaining Dilution Factor

(B) After addition of 36.00 mL KIO₃

Example B

 If V=36.00 mL, the precipitation is complete and we have gone past the equivalence point

$$[IO_{3}^{*}] = \left(\frac{36.00 - 35.69}{25.00 + 36.00}\right)(0.05789 \text{ M}) = 2.9 \times 10^{-4} \text{ M}$$

$$[Hg_{2}^{2+}] = \frac{K_{ap}}{[IO_{3}^{*}]^{2}} = \frac{1.3 \times 10^{-18}}{(2.9 \times 10^{-4})^{2}} = 1.5 \times 10^{-11} \text{ M}$$

(C) At the equivalence point, there is exactly enough IO_3^- to react with all Hg_2^+ . We can imagine that all of the ions precipitate and then some $Hg_2(IO_3)_2(s)$ redissolves, giving two moles of iodate for each mole of mercurous ion:

$$Hg_2(IO_3)_2 \leftrightarrows Hg_2^{2+} + 2IO_3^-$$

 $(x)(2x)^2 = K_{sp} \to x = [Hg_2^{2+}] = 6.9 \times 10^{-7} M$

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Q) Find $[Hg_2^{2+}]$ at 34.50 and 36.50 mL. (Answer: $5.79 \times 10^{-4} M$, $2.2 \times 10^{-12} M$

26.6 Titration of a Mixture

If a mixture of two ions is titrated, the less soluble precipitate forms first. If the solubilities are sufficiently different, the first precipitation is nearly complete before the second commences.

Consider the addition of AgNO₃ to a solution containing KI and KCl. Because K_{sp} (AgI) $<< K_{sp}$ (AgCl), AgI precipitates first. When precipitation of I^- is almost complete, the concentration of Ag^+ abruptly increases and AgCl begins to precipitate. When Cl^- is consumed,

another abrupt increase in $[Ag^+]$ occurs. We expect two breaks in the titration curve, first at V_e for AgI and then at V_e for AgCl.

Figure 26-10 shows an experimental curve for this titration. The apparatus used to measure the curve is shown in Figure 26-11.

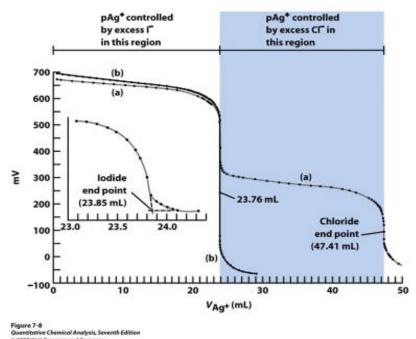
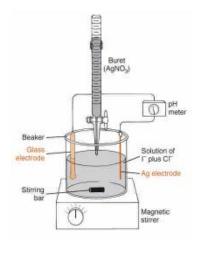


Figure 26-10

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Technique to Monitor Titration



The technique used to monitor the mixture titration of Ag* with I and Cl was electrochemistry. An electrode specific to Ag* was used to monitor [Ag*]

The principles of electrochemistry and electrode operation will be discussed in Chs. 14-15. As discussed, this is just one method of monitoring a titration. Spectroscopy is another.

Figure 26-11

The I^- end point is taken as the intersection of the steep and nearly horizontal curves shown in the inset of Figure 26-10. Precipitation of I^- is not quite complete when Cl^- begins to precipitate. (The way we know that I^- precipitation is not complete is by a calculation. That's what these obnoxious calculations are for!) Therefore, the end of the steep portion (the intersection) is a better approximation of the equivalence point than is the middle of the steep section. The Cl^- end point is taken as the midpoint of the second steep section, at 47.41 mL. The moles of Cl^- in the sample equal the moles of Ag^+ delivered between the first and second end points. That is, it requires 23.85 mL of Ag^+ to precipitate I^- , and (47.41 - 23.85) = 23.56 mL of Ag^+ to precipitate Cl^- .

26.8 End-Point Detection

Precipitation titration end points are commonly found with electrodes (Figure 26-11) or indicators. We now describe two indicator methods for the titration of Cl^- with Ag^+ :

Volhard titration: formation of a soluble, colored complex at the end point

Fajans titration: adsorption of a colored indicator on the precipitate at the end point

Volhard Titration

The Volhard titration is a titration of Ag^+ in HNO₃ solution. For Cl^- , a back titration is necessary. First, Cl^- is precipitated by a known, excess quantity of standard AgNO₃.

$$Ag^+ + Cl^- \rightarrow AgCl(s)$$

The AgCl is filtered and washed, and excess Ag^+ in the combined filtrate is titrated with standard KSCN (potassium thiocyanate) in the presence of Fe^{3+} .

$$Ag^+ + SCN^- \rightarrow AgSCN(s)$$

When all Ag^+ has been consumed, SCN^- reacts with Fe^{3+} to form a red complex.

$$Fe^{3+} + SCN^{-} \rightarrow FeSCN^{2+}$$
Red

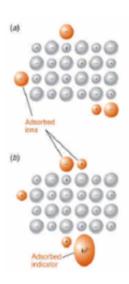
The appearance of red color is the end point. Knowing how much SCN^- was required for the back titration tells us how much Ag^+ was left over from the reaction with Cl^- . The total amount of Ag^+ is known, so the amount consumed by Cl^- can be calculated.

In the analysis of Cl^- by the Volhard method, the end point would slowly fade if the AgCl were not filtered off, because AgCl is more soluble than AgSCN. The AgCl slowly dissolves and is replaced by AgSCN. To eliminate this secondary reaction, we filter the AgCl and titrate only the Ag^+ in the filtrate. Br^- and I^- , whose silver salts are less soluble than AgSCN, can be titrated by the Volhard method without isolating the silver halide precipitate.

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Fajans Titration

Fajans Titration



The technique uses an adsorption indicator. Prior to the equivalence point, there is excess CI- in solution. Some is adsorbed on the surface of the crystal, giving a partial negative charge. After the equivalence point, there is excess Ag+ in solution. Some adsorbs to the surface imparting a partial positive charge to the precipitate. Choosing an indicator with a partial negative charge will cause it to adsorb to the surface

Common Precipitation Titrations				
Table 7-1 Applications of precipitation titrations Species analyzed Notes				
	Volumen Mitteon			
Br , 1 , SCN , CNO , AsO [Precipitate removal is unnecessary.			
CI , PO , CN , C O , CO , CO , CO , S ² , CIO .	Precipitate removal required.			
BH ₄	Back titration of Ag^+ left after reaction with BH_4^+ : $BH_4^- + 8Ag^+ + 8OH^- \rightarrow 8Ag(x) + H_2BO_3^- + 5H_3O$			
K*	K ⁺ is first precipitated with a known excess of (C ₀ H ₃) ₄ B ⁻ . Remaining (C ₀ H ₂) ₂ B ⁻ is precipitated with a known excess of Ag ⁺ . Unreacted Ag ⁺ is then sitrated with SCN ⁺ Parces METHOD.			
Cl", Br", I", SCN", Fe(CN)	Titration with Ag ⁺ . Detection with dyes such as fluorescein, dichlorofluorescein, eosin, bromophenol blue.			
F-	Titration with Th(NO ₃) ₂ to produce ThF ₄ . End point detected with alizarin red S.			
Zn²†	Titration with K ₃ Fe(CN) _k to produce K ₂ Zn ₃ [Fe(CN) _k I ₂ . End-point detection with diphenylamine.			
SO2	Titration with Ba(OH), in 50 vol % aqueous methanol using alizarin red S as indicator.			
Hgl*	Titration with NaCl to produce Hg ₂ Cl ₂ . End point detected with bromophenol blue.			
PO]-, C ₂ O]-	Titration with Ph(CH ₃ CO ₂) ₂ to give Pb ₃ (PO ₄) ₂ or PbC ₂ O ₄ . End point detected with dibromofluorescein (PO ₂ ⁽¹⁾) or fluorescein (C ₃ O ₂ ⁽¹⁾).			

Table 26-5

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Applications of precipitation titrations are listed in Table 26-5. Whereas the Volhard method is an argentometric titration, the Fajans method has wider applications. Because the Volhard titration is carried out in acidic solution (typically 0.2 M HNO₃), it avoids certain interferences that affect other titrations. Silver salts of CO_3^{2-} , $C_2O_4^{2-}$, and AsO_4^{3-} are soluble in acidic solution, so these anions do not interfere.