

Unit 7 Pre-Class Warm-up

w203 Instructional Team

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Maximum Likelihood Overview

Each time Paul Laskowski attempts a joke in class, he secretly records the number of students that laugh (Sometimes, the Human Subjects Board is just in a great mood). Paul gives you a dataset of 500 jokes and insists that you model each observation as an independent random variable that's distributed according to the HyperGaussian distribution, which has a single parameter, $h \in \mathbb{R}$. The probability density function of this distribution can be written $f_H(x; h)$.

In your own words, list the four or five key steps you would take to perform a maximum likelihood estimate of h . (Just a sentence per step)

1. Write a likelihood function as $l(h) = f(x_1, x_2, \dots, x_{500}; h) = f(x_1, h) * f(x_2, h) * \dots * f(x_{500}, h)$ based on observations x_i , where $i = 1, 2, \dots, 500$
2. Take a derivative of the likelihood function $f(x_1, x_2, \dots, x_{500}; h)$
3. Set f' to be 0 to get the h value that has the maximum likelihood
4. Compute the h that makes f' zero, which gives $l(h)$ the maximum likelihood