

# Week 9 Live Session

*w203 Instructional Team*

## Announcements

Feedback about Quiz 1.

Remember that Lab 3 is being released this week.

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## Common hypothesis testing errors

For each of the following scenarios, explain the key error in the statistical procedure.

- Bill hypothesizes that the average student drinks between 100 and 200 grams of caffeine during a take-home lab. He measures mean caffeine intake for a random sample of 50 lab-takers, then computes the p-value associated with his hypothesis.
- Mike likes peanuts. Mike likes peanuts so much that he conducts a study to show how peanut allergies are an NIH sponsored hoax. He recruits 20 toddlers and randomly assigns each into two groups: peanut butter and brown sugar paste. To Mike's delight, he fails to find evidence for a difference between the groups ( $p = .34$ ). Mike concludes by accepting the null hypothesis (that peanut allergies do not exist).
- Anne replicates Mike's study and estimates a p-value of .03, she concludes that the alternative hypothesis has a 97% chance of being true.
- Tim asks 50 passengers on the 8am Staten Island Ferry to complete his survey about attitudes toward atheists. He finds a statistically significant difference between attitudes toward atheists and attitudes toward scientologists ( $p = .04$ ). Huzzah! Tim concludes that the US public is more fearful of atheists than scientologists.

## Comparing Means

The file `united_states_senate_2014.csv` contains data on the 100 members of the US senate that served in 2014. We will consider this group to be a sample (for example, from some generative process that creates senators).

```
S = read.csv("united_states_senate_2014.csv")
summary(S)
```

```
##           Senator.Names      Gender      State      Party
## Alan "Al" Franken: 1      Female:20      Alabama   : 2      Democrat   :53
## Amy Klobuchar       : 1      Male   :80      Alaska     : 2      Independent: 2
## Angus King          : 1                               Arizona    : 2      Republican :45
## Barbara Boxer        : 1                               Arkansas   : 2
## Barbara Mikulski     : 1                               California: 2
## Benjamin Cardin      : 1                               Colorado   : 2
## (Other)              :94                               (Other)    :88
##           Religion  Campaign.Money.Raised..millions.of...
## Protestant      :49      Min.       : 0.100
## Catholic         :27      1st Qu.: 4.575
## Jewish           :10      Median   : 7.550
```

```
## Other Christian: 7   Mean   : 9.645
## Mormon          : 2   3rd Qu.:13.800
## Unaffiliated    : 2   Max.    :44.200
## (Other)         : 3
## Campaign.Money.Spent..millions.of...
## Min.           : 0.200
## 1st Qu.        : 2.975
## Median         : 6.000
## Mean           : 8.227
## 3rd Qu.        :12.225
## Max.           :43.400
##
```

You will be placed in a breakout room and assigned a single question to investigate using this dataset. Each question involves a comparison of means.

In your breakout rooms, examine the data and decide what type of test is most appropriate. You may select a paired or an unpaired test. You may also select a parametric or a nonparametric test. Conduct your test and interpret your results.

Room 1: Is there a difference between the amount of money a senator raises and the amount spent?

Room 2: Do female Democratic senators raise more or less money than female Republican senators?

Room 3: Do protestant Senators spend more or less money than non-protestant senators?

Room 4: Choose your own question to investigate.

## Demonstration of Confidence Intervals

The following exercise is meant to demonstrate what the confidence level in a confidence interval represents. For this exercise, we will assume a standard normal population distribution and simulate what happens when we draw a sample and compute a confidence interval.

Your task is to complete the following function so that it,

- 1) simulates and stores  $n$  draws from a standard normal distribution
- 2) based on those draws, computes a valid confidence interval with confidence level  $\alpha$ .

Your function should return a vector of length 2, containing the lower bound and upper bound of the confidence interval.

```
sim_conf_int = function(n, alpha) {
  # Your code to
  # 1. simulate n draws from a standard normal dist.
  # 2. compute a confidence interval with confidence level alpha
  return(c(-1,1)) # replace with the interval you compute.
}
```

When your function is complete, you can use the following code to run your function 100 times and plot the results.

```
many_conf_int = function(m, n, alpha) {
  results = NULL
  for(i in 1:m) {
    interval = sim_conf_int(n, alpha)
    results = rbind(results, c(interval[1], interval[2], interval[1]<0 & interval[2]>0))
  }
  resultsdf = data.frame(results)
}
```

```

names(resultsdf) = c("low", "high", "captured")
return(resultsdf)
}

n = 20
cints = many_conf_int(100, n, .05)

plot(NULL, type="n", xlim=c(1,100), ylim=c(min(cints$low), max(cints$high)), xlab="Trial", ylab=expression(
abline(h = c(0, qt(0.975, n-1)/sqrt(n), qt(0.025, n-1)/sqrt(n)), lty = c(1,2,2), col = "gray")
points(cints$high, col = 2+cints$captured, pch = 20)
points(cints$low, col = 2+cints$captured, pch = 20)
for(i in 1:100)
{
  lines(c(i,i), c(cints$low[i],cints$high[i]), col = 2+cints$captured[i], pch = 19)
}
title(expression(paste("Simulation of t-Confidence Intervals for ", mu,
" with Sample Size 20")))
legend(0,-.65, legend = c(expression(paste(mu," Captured")),
expression(paste(mu," Not Captured"))), fill = c(3,2))

```

Simulation of t-Confidence Intervals for  $\mu$  with Sample Size 20

