### Computer Vision and Machine Learning

(Visual system and Camera)

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Computer Vision -- Intro

### Image formation

- Basic components
  - Light (Wave length, intensity)
  - Camera (intrinsic and extrinsic parameters)
  - Scene (reflectance, orientation, curvature)

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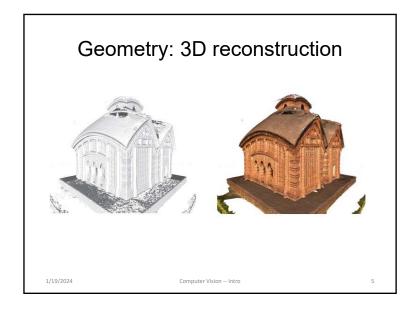
### Shape from X

- Reconstructing 3D object from 2D images
  - Stereo
  - Motion
  - Shading
  - Texture
  - Contour

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## Geometry: 3D reconstruction (cond.) \*\*Translation\*\* | Translation\*\* | Transl



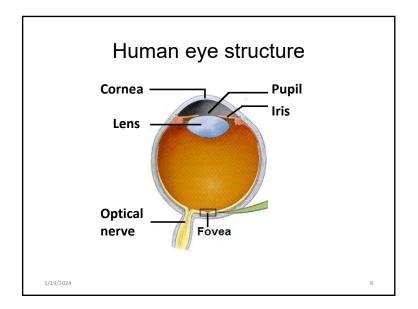
### Human Visual system and Camera

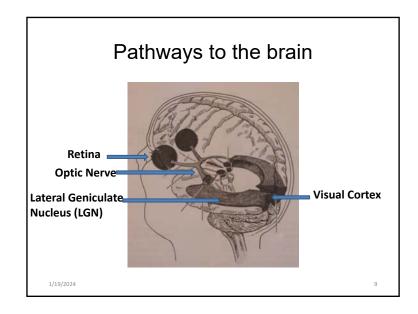
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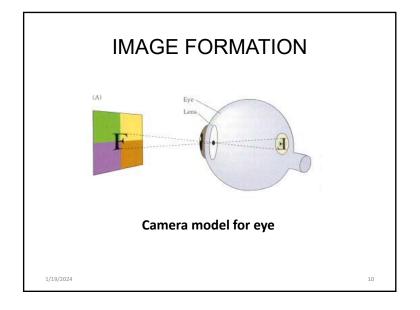
### Human vision

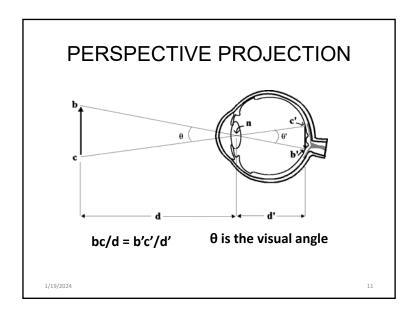
- Most important and powerful sensor in human body.
- The image formation process is well understood.
- The image understanding is the one that remains mysterious.

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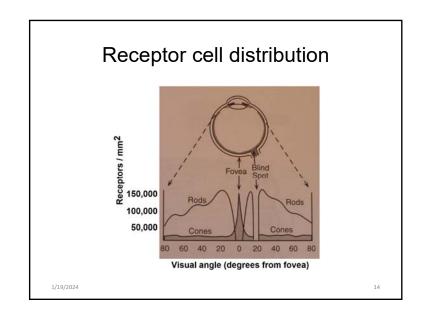
### Light sensors in the eye

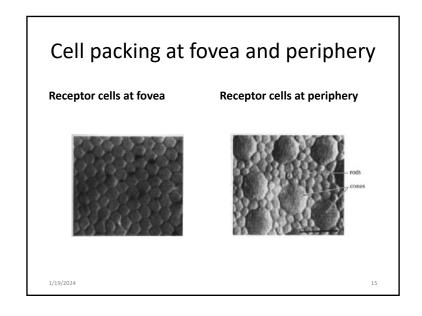
- Image formed on the retina is sensed by special type of cells called *photoreceptors*.
- Photoreceptors convert physical light signal into biological signal that passes through optical nerves.
- There are two types of photoreceptors:
  - Cones
  - Rods

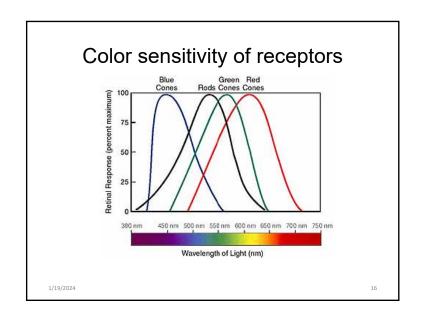
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# Rod and cone cells in eye \* Cones: Color-vision with higher intensity light. \* Rods: Low-intensity light vision, e.g. night vision, e.g. night vision. \* Cones are larger in size and are more densely packed in fovea region. \* Rods are smaller in size, much higher number in periphery.







### Colour sensitivity

- Wavelength of visible spectrum ranges from 0.38 μm to 0.76 μm (approx.)
- Response characteristics  $h_B(v)$  for blue attains maximum at about  $6.8 \times 10^4$  Hz or  $0.44 \mu m$
- Response characteristics  $h_G(v)$  for green attains maximum at about 5.8 x 10<sup>4</sup> Hz or 0.52  $\mu$ m
- Response characteristics  $h_R(v)$  for red attains maximum at about 4.3 x 10<sup>4</sup> Hz or 0.70  $\mu$ m

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## Retina and camera sensor Light Perion Cones are widely spaced in the periphery 1/19/2024 1/19/2024

### Bayer filter is a color filter array used with sensor of digital camera. Arranged in square grid with 50% G, 25% R and 25% B. Each pixel gets one particular color that the filter allows to reach the sensor. Other color components are interpolated (averaged) from the neighborhood. Apper filter Resulting patter Resulting patter Reput filter Support filter Apper filter

### Human eye: Summary

### Frontal part

- Cornea
- · Pupil and Iris
- Lens

### Retina:

- Rods (low-intensity light, night vision)
- Cones (color-vision)
- Synapses and ganglions
- Optic nerve fibers

Does sensing and low-level processing.

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### Human vision vs. Computer Vision

The camera replaces the eye:

- Eye lens → Camera Optics
- Cones and Rods → CCD array
- Ganglion cells → Filter banks

The computer replaces the brain:

• But how?

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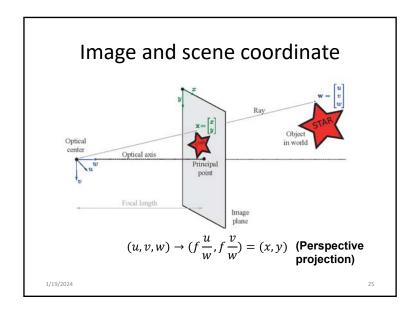
### The Objective • Want to make a computer understand images • We know it is possible – we do it effortlessly! Real world scene Sensing device Interpreting device Interpretation A person / A person with turban / Manmohan Singh

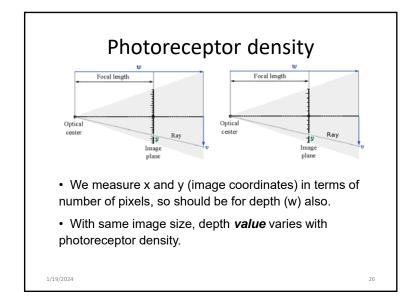
# Camera model Vivi/2024 23

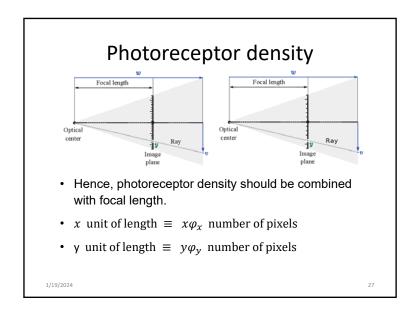
### Projection properties

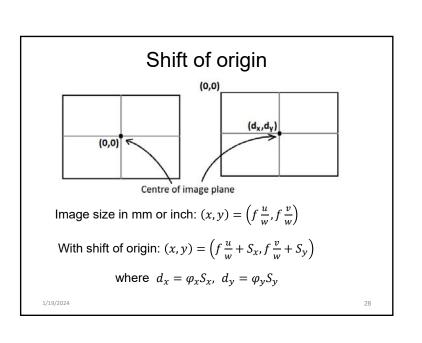
- Many-to-one: any point along same *visual* ray map to same point in image
- Point → point
- Line → line (collinearity is preserved)
  - But line through focal point (visual ray) projects to a point
- Plane → plane (or half-planes)
  - But plane through focal point projects to line

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### Photoreceptor density and shift

$$(u, v, w) \rightarrow (f\frac{u}{w}, f\frac{v}{w}) = (x, y)$$

turns to 
$$(u, v, w) \rightarrow (f \frac{\varphi_x u}{w}, f \frac{\varphi_y v}{w}) = (x, y)$$

Instead of origin (0,0) at the centre of image it usually at top-left corner, i.e., principal point is at  $(d_x, d_y)$ . Thus

$$x = f \frac{\varphi_x u}{w} + d_x$$
$$y = f \frac{\varphi_y v}{w} + d_y$$

 $(f, \varphi_x, \varphi_y, d_x, d_y)$  are *intrinsic parameters* of the camera.

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### Projection matrix for camera

Projection is a matrix multiplication using homogeneous coordinates:

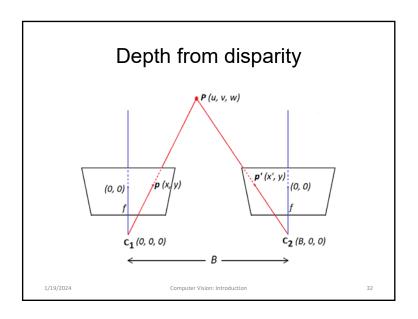
$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1/f & 0 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix} = \begin{bmatrix} u \\ v \\ w/f \end{bmatrix} \implies (f \frac{u}{w}, f \frac{v}{w})$$

Considering photoreceptor density and shift:

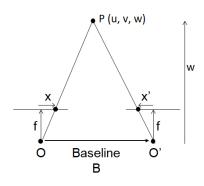
$$\begin{bmatrix} \varphi_{x} & 0 & d_{x} \\ 0 & \varphi_{y} & d_{y} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1/f & 0 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix} = \begin{bmatrix} u\varphi_{x} + wd_{x}/f \\ v\varphi_{y} + wd_{y}/f \\ w/f \end{bmatrix}$$
$$\Rightarrow \left( f \frac{\varphi_{x}u}{w} + d_{x}, f \frac{\varphi_{y}v}{w} + d_{y} \right)$$

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Depth from disparity P(u, v, w)  $c_1(0, 0, 0)$ Computer Vision: Introduction 31



### Depth from disparity



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### Depth from disparity

- Camera-2 is shifted from camera-1 only along horizontal direction and no rotation.
- Camera-1:
  - Optical centre  $O_1$ : (0,0,0)
  - World point P: (u, v, w)
  - Image coordinate:  $x = f \frac{u}{w} \implies \frac{x}{f} = \frac{u}{w}$  (1
- Camera-2:
  - Optical centre  $O_1$ : (B, 0, 0)
  - World point P: (u B, v, w)
  - Image coordinate:  $x' = f \frac{u-B}{w} \implies \frac{x'}{f} = \frac{u-B}{w}$  (2)

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### Depth from disparity (contd.)

• Subtracting equation (2) from equation (1):

$$\frac{x - x'}{f} = \frac{B}{w}$$

• This implies

$$w = \frac{B \cdot f}{x - x'}$$

• Once we know *w*, *u* can be easily determined as

$$u = w \frac{x}{f}$$

Similarly *y*.

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### Position and orientation of camera

- Camera may be placed anywhere in a scene.
- Same object may appear differently while captured by same camera at different position and orientation.
- It would be easier to handle if the relation between their geometry is known.

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### Coordinate transformation

- World coordinate system
  - World (object) centric scene coordinates
- Camera coordinate system
  - Camera centric scene coordinates
- Transforming world (scene) coordinate to camera coordinate
  - Rotation, translation and (optional) scaling
  - Linear transformation is advantageous.

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### 2D transforms

Rotation:  $\begin{bmatrix} u' \\ v' \end{bmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} \equiv p' = Rp$ 

(Coordinate axis is rotated anti-clockwise by an angle  $\theta$ .)

Scaling:  $\begin{bmatrix} u' \\ v' \end{bmatrix} = \begin{bmatrix} S_u & 0 \\ 0 & S_v \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} \equiv p' = Sp$ 

(Coordinate axis is squeezed / expanded  $1/S_u$  and  $1/S_v$ .)

Translation:  $\begin{bmatrix} u' \\ v' \end{bmatrix} = \begin{bmatrix} u \\ v \end{bmatrix} + \begin{bmatrix} t_u \\ t_v \end{bmatrix}$  p' = p + t

(Coordinate axis is translated by  $-t_u$  and  $-t_v$ .)

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### 3D transforms

Rotation: 
$$R_u = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & \sin \alpha \\ 0 & -\sin \alpha & \cos \alpha \end{bmatrix}$$

$$R_v = \begin{bmatrix} \cos \beta & 0 & -\sin \beta \\ 0 & 1 & 0 \\ \sin \beta & 0 & \cos \beta \end{bmatrix} \qquad R_w = \begin{bmatrix} \cos \gamma & \sin \gamma & 0 \\ -\sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R = R_u R_v R_w \equiv \mathbf{p}' = R \mathbf{p}$$
, where  $R = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix}$ 

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### 3D transforms

Scaling: 
$$\begin{bmatrix} u' \\ v' \\ w' \end{bmatrix} = \begin{bmatrix} s_u & 0 & 0 \\ 0 & s_v & 0 \\ 0 & 0 & s_w \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} \equiv \mathbf{p}' = S\mathbf{p}$$

Translation: 
$$\begin{bmatrix} u' \\ v' \end{bmatrix} = \begin{bmatrix} u \\ v \\ w \end{bmatrix} + \begin{bmatrix} t_u \\ t_v \\ t_w \end{bmatrix} \equiv p' = p + t$$

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### Projection matrix for camera

 World to camera co-ordinate system using homogeneous coordinates:

$$\begin{bmatrix} u^{c} \\ v^{c} \\ w^{c} \\ 1 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_{u} \\ r_{32} & r_{22} & r_{23} & t_{v} \\ r_{31} & r_{32} & r_{33} & t_{w} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix}$$
$$\boldsymbol{p}^{c} = T\boldsymbol{p} = \begin{bmatrix} \boldsymbol{R} & \boldsymbol{t} \\ \boldsymbol{0}^{T} & 1 \end{bmatrix} \boldsymbol{p}$$

• The elements of the matrix R, i.e.,  $r_{i,j}$  and  $t_k$  are **extrinsic parameters**.

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3D translation

Translation:

$$\begin{bmatrix} u' \\ v' \\ w' \end{bmatrix} = \begin{bmatrix} u + t_u \\ v + t_v \\ w + t_w \end{bmatrix} = \begin{bmatrix} u \\ v \\ w \end{bmatrix} + \begin{bmatrix} t_u \\ t_v \\ t_w \end{bmatrix} \quad \equiv \quad p' = p + t$$

In homogeneous coordinate system

$$\begin{bmatrix} u' \\ v' \\ w' \\ 1 \end{bmatrix} = \begin{bmatrix} u + t_u \\ v + t_v \\ w + t_w \\ 1 + 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & t_u \\ 0 & 1 & 0 & t_v \\ 0 & 0 & 1 & t_w \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix} \equiv p'_h = T \mathbf{p}_h$$

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### Projection matrix for image formation

In practice: lots of coordinate transformations...

$$\begin{bmatrix} 2D \\ \text{point} \\ (3x1) \end{bmatrix} = \begin{bmatrix} \text{Camera to} \\ \text{pixel coord.} \\ \text{trans. matrix} \\ (3x3) \end{bmatrix} \begin{bmatrix} \text{Perspective} \\ \text{projection matrix} \\ (3x4) \end{bmatrix} \begin{bmatrix} \text{World to} \\ \text{camera coord.} \\ \text{trans. matrix} \\ (4x1) \end{bmatrix} \begin{bmatrix} 3D \\ \text{point} \\ \text{trans. matrix} \\ (4x1) \end{bmatrix}$$

$$\begin{bmatrix} u^c \varphi_x + w^c d_x / f \\ v^c \varphi_y + w^c d_y / f \end{bmatrix} = \begin{bmatrix} \varphi_x & 0 & d_x \\ 0 & \varphi_y & d_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 / f & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_u \\ r_{32} & r_{22} & r_{23} & t_v \\ r_{31} & r_{32} & r_{33} & t_w \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} u^c \varphi_x + w^c d_x / f \\ v^c \varphi_y + w^c d_y / f \\ w^c / f \end{bmatrix} = \begin{bmatrix} \varphi_x & 0 & d_x / f & 0 \\ 0 & \varphi_y & d_y / f & 0 \\ 0 & 0 & 1 / f & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_u \\ r_{32} & r_{22} & r_{23} & t_v \\ r_{31} & r_{32} & r_{33} & t_w \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \\ 1 \end{bmatrix}$$

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### Thank you! Any question?

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