

CMPE 691 – Reconfigurable System Design
PROJECT
ON
MATRIX CONVOLUTION HARDWARE ACCELERATOR

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The computation at first position in the output matrix is shown below. The respective elements will be calculated in the same process.

$$O[0][0] = (0 \cdot 1) + (1 \cdot 0) + (2 \cdot 1) + (5 \cdot 1) + (6 \cdot 0) + (7 \cdot 1) + (10 \cdot 1) + (11 \cdot 0) + (12 \cdot 1)$$

$$O[0][0] = 0 + 0 + 2 + 5 + 0 + 7 + 10 + 0 + 12 = 36$$

2.2 Need for Hardware Acceleration

The main concern unique to matrix convolution is the high computational requirement of the technique. This organization makes efficient use of the processor impossible on general-purpose processors because the sequential nature of the computation means that large datasets cannot be utilized in order to reduce processing time or that applications that require real-time processing are slowed considerably by large matrices. But sometimes, due to a large number of parallel operations required and frequent data reuse optimization, hardware accelerators, especially those on FPGAs, are an efficient solution.

As for matrix convolution, there are more benefits that flow from using hardware accelerators, which include the ability to perform multiple kernel operations at a go; thereby improving of high throughput and scalability [1].

2.3 FSM-Based Hardware Design

Finite State Machines (FSMs) are a reliable basis for supervising sequential processes in hardware. In this project, an FSM based design was used to coordinate the input phase, the computational phase, and the output phase of the moving-average matrix convolution. It evolves through states like IDLE, LOAD, COMPUTE, and DONE, to check for great resource usage.

Due to this approach, the design unknowns are reduced while at the same time addressing the flexibility and scalability issues. The FSM collaboratively operates with the data path to execute the multiply-accumulate (MAC) that convolution entails to deliver reliable computations.

2.4 Relevance of Related Work

The work done by Cao et al. (2019) titled “FPGA-based Accelerator for Convolution Operations” show how FPGA-based design can be used to facilitate convolutional tasks. Their work also concentrates on getting benefits with FPGA resource to increase more throughput while minimizing the latency. But as their design targets systolic arrays [1], this project follows a much simpler FSM design intended for matrix convolution applications.

This distinction makes the hardware accelerator applicable to a wider perspective of other computations other than neural networks. In addition, the design integrates with an Avalon-MM interface to provide clear visibility by displaying it if it needs to communicate with software applications, adding to its flexibility.

3. Design and Implementation

3.1 FSM Design for Matrix Convolution

The flow of the operations at the hardware accelerator was controlled based on the Finite State Machine (FSM) approach. The FSM consists of the following states:

- IDLE: Wait for a write or read signal to start operations.
- LOAD: Reads the input matrix elements from the processor and saves them into internal memory of the system.
- COMPUTE: Computes the output matrix by iteratively passing through the input matrix and the kernel to do the matrix convolution.
- DONE: Indicates the end of convolution process and goes back to the IDLE state.

This FSM based design further ensures that the different blocks of the hardware work in harmony with minimal clock cycles being utilized. Every state changes according to control signals like start and done. Fig 1 depicts the state machine used for matrix convolution with a 3x3 input matrix and a 2x2 kernel matrix. It highlights the four main states IDLE, LOAD, COMPUTE, and DONE that coordinate the operations efficiently. This file is attached as “matrix_convolution3_3.sv”.

```
module matrix_convolution3_3
(
    input logic start,
    input logic done,
    input logic [2:0] input_matrix_0, input_matrix_1, input_matrix_2, // 3x3 input matrix elements
    input logic [1:0] input_matrix_3, input_matrix_4, input_matrix_5, // 2x2 kernel matrix elements
    output logic [2:0] output_matrix_0, output_matrix_1, output_matrix_2, // 3x3 output matrix elements
    output logic [1:0] output_matrix_3, output_matrix_4, output_matrix_5
);

// Local variables
localparam int N = 3; // Input matrix size
localparam int K = 2; // Kernel matrix size
localparam int O = 3; // Output matrix size

// State variables
state_t current_state, next_state; // State register
logic [1:0] mem; // Memory

// State logic
always_comb
begin
    case (current_state)
        IDLE: // Wait for start signal
            if (start)
                next_state = LOAD;
            else
                next_state = IDLE;
        LOAD: // Load input matrix and kernel matrix into memory
            if (mem[0] == 0)
                next_state = COMPUTE;
            else
                next_state = LOAD;
        COMPUTE: // Compute output matrix
            if (mem[0] == 0)
                next_state = DONE;
            else
                next_state = COMPUTE;
        DONE: // Done
            next_state = IDLE;
    endcase
end

// State register
always_ff
begin
    current_state <= next_state;
end

// Memory logic
always_ff
begin
    if (current_state == COMPUTE)
        mem <= mem + 1;
    else
        mem <= 0;
    end
end

// Output logic
always_ff
begin
    if (current_state == COMPUTE)
        output_matrix_0 <= mem[0];
        output_matrix_1 <= mem[1];
        output_matrix_2 <= mem[2];
        output_matrix_3 <= mem[3];
        output_matrix_4 <= mem[4];
        output_matrix_5 <= mem[5];
    else
        output_matrix_0 <= 0;
        output_matrix_1 <= 0;
        output_matrix_2 <= 0;
        output_matrix_3 <= 0;
        output_matrix_4 <= 0;
        output_matrix_5 <= 0;
    end
end

endmodule
```

Fig 1: State Machine for Matrix Convolution for 3*3 Input Matrix and 2*2 Kernel Matrix

Fig 2 shows the state machine for matrix convolution with a 5x5 input matrix and a 3x3 kernel matrix. It illustrates the scalability of the FSM design, showcasing its ability to handle larger matrices by adjusting states and operations to maintain efficiency. This file is attached as “matrix_convolution5_5.sv”.

```

module matrix_convolution5_5 (
    input logic clk,
    input logic reset,
    input logic write,
    input logic read,
    input logic [10:0] data_in,
    output logic [10:0] data_out,
    output logic done
);

// Parameters
parameter INPUT_SIZE = 5;
parameter KERNEL_SIZE = 3;
parameter OUTPUT_SIZE = INPUT_SIZE - KERNEL_SIZE + 1;

// Internal storage for input matrix and kernel
logic [10:0] input_matrix[INPUT_SIZE-1][INPUT_SIZE-1];
logic [10:0] kernel[KERNEL_SIZE-1][KERNEL_SIZE-1];
logic [10:0] output_matrix[OUTPUT_SIZE-1][OUTPUT_SIZE-1];

// Current row and column indices
logic [10:0] row, col, read_row, read_col;
logic [10:0] sum;

// State machine
typedef enum logic [1:0] {IDLE, WRITE_MATRIX, COMPUTE, READ_OUTPUT, DONE} state_t;
state_t state, next_state;

// Initial state
initial begin
    state = IDLE;
    row = 0;
    col = 0;
    read_row = 0;
    read_col = 0;
    sum = 0;
end

// State machine logic
always_ff @(posedge clk or posedge reset) begin
    if (reset) begin
        state = IDLE;
        row = 0;
        col = 0;
        read_row = 0;
        read_col = 0;
        sum = 0;
    end else begin
        state = next_state;
        case (state)
            // WRITE_MATRIX
            WRITE_MATRIX: begin
                if (write) begin
                    input_matrix[row][col] <= data_in;
                    if (col == INPUT_SIZE - 1) begin
                        col = 0;
                        row = row + 1;
                        if (row == INPUT_SIZE - 1) done = 1;
                        else state = COMPUTE;
                    end else
                        col = col + 1;
                end
            end

            // COMPUTE
            COMPUTE: begin
                sum = 0;
                for (int i = 0; i < KERNEL_SIZE; i++) begin
                    for (int j = 0; j < KERNEL_SIZE; j++) begin
                        sum <= sum + input_matrix[row + i][col + j] * kernel[i][j];
                    end
                end
                output_matrix[row][col] <= sum;
                if (col == OUTPUT_SIZE - 1) begin
                    col = 0;
                    row = row + 1;
                    if (row == OUTPUT_SIZE - 1) done = 1;
                    else state = READ_OUTPUT;
                end else
                    col = col + 1;
            end

            // READ_OUTPUT
            READ_OUTPUT: begin
                if (read) begin
                    data_out <= output_matrix[row][col];
                    if (col == OUTPUT_SIZE - 1) begin
                        col = 0;
                        row = row + 1;
                        if (row == OUTPUT_SIZE - 1) done = 1;
                        else state = COMPUTE;
                    end else
                        col = col + 1;
                end
            end

            // DONE
            DONE: begin
                done = 1;
            end
        endcase
    end
end

// Next state logic
always_comb begin
    next_state = state;
    case (state)
        WRITE_MATRIX: next_state = (row == INPUT_SIZE - 1) ? COMPUTE : WRITE_MATRIX;
        COMPUTE: next_state = (row == OUTPUT_SIZE - 1) ? READ_OUTPUT : COMPUTE;
        READ_OUTPUT: next_state = (row == OUTPUT_SIZE - 1) ? DONE : READ_OUTPUT;
        DONE: next_state = DONE;
    endcase
end
endmodule

```

Fig 2: State Machine for Matrix Convolution for 5*5 Input Matrix and 3*3 Kernel Matrix

3.2 Integration with Avalon-MM Interface

Communication between the matrix convolution module and the processor was facilitated by implementing an Avalon-MM interface for the module. This interface contemplates a memory mapping communication that facilitates the data interchange between the FPGA and the CPU. Address decoding was used while integrating, WRITE logic was equally included, and READ-back was part of the integrating procedure.

Key Functionalities of the Integration:

- Write Operation:

In the following, when `avs_s1_write` is 1, the elements in the input matrix and control signals are stored in the internal registers.

By specifying the behavior of internal register `avs_s1_address` it is possible to direct data transfer towards the desired location.

- Read Operation:

In the second stage, when `avs_s1_read` is asserted, a corresponding element in the result matrix, done signal and status register address are read. This makes it easy for the processor to access computed results when the need arise.

- Control and Status Signals:

A control register exists to control the convolution computation while a status register is used to give information concerning the computation.

- A dummy delay pipeline is implemented for some illustrations in order to synchronize control and output signals correctly.

```

// Matrix Convolution Module with Avalon-MM Interface
module matrix_convolution_avalon_interface (
    input logic csi_clockreset_clk, // Clock Input
    input logic csi_clockreset_reset_n, // Active-low reset
    input logic [11:0] avs_s1_address, // Avalon-MM address
    input logic avs_s1_read, // Avalon-MM read signal
    input logic avs_s1_write, // Avalon-MM write signal
    input logic [11:0] avs_s1_writedata, // Avalon-MM write data
    output reg [11:0] avs_s1_readdata // Avalon-MM read data
);

// Internal registers for input/output, control, and status
reg [11:0] a0, a1, a2, a3, a4, a5, a6, a7, a8, control, status, r0, r1, r2,
r3; reg x, y;

// Instance of matrix convolution core
matrix_convolution_dut (
    .csi_clockreset_clk(csi_clockreset_clk),
    .reset(~csi_clockreset_reset_n),
    .start(x),
    .input_matrix_0(a0), .input_matrix_1(a1), .input_matrix_2(a2),
    .input_matrix_3(a3), .input_matrix_4(a4), .input_matrix_5(a5),
    .input_matrix_6(a6), .input_matrix_7(a7), .input_matrix_8(a8),
    .done(r3),
    .output_matrix_0(r0), .output_matrix_1(r1),
    .output_matrix_2(r2), .output_matrix_3(r3)
);

// Write input matrix and control based on address
always @(posedge csi_clockreset_clk) begin
    if (csi_clockreset_reset_n == 0) begin
        a0 <= 0; a1 <= 0; a2 <= 0; a3 <= 0; a4 <= 0;
        a5 <= 0; a6 <= 0; a7 <= 0; a8 <= 0;
    end else if (avs_s1_write) begin
        case (avs_s1_address)
            0: a0 <= avs_s1_writedata;
            1: a1 <= avs_s1_writedata;
            2: a2 <= avs_s1_writedata;
            3: a3 <= avs_s1_writedata;
            4: a4 <= avs_s1_writedata;
            5: a5 <= avs_s1_writedata;
            6: a6 <= avs_s1_writedata;
            7: a7 <= avs_s1_writedata;
            8: a8 <= avs_s1_writedata;
            9: x <= avs_s1_writedata;
            10: control <= avs_s1_writedata;
        endcase
    end
end

// Dummy pipeline for status demonstration
reg [11:0] dummy_delay [10:0];
always @(posedge csi_clockreset_clk) begin
    integer i;
    dummy_delay[0] <= control;
    for (i = 1; i <= 10; i = i + 1)
        dummy_delay[i] <= dummy_delay[i - 1];
    status <= dummy_delay[10];
end

// Read input matrix, done signal, and status based on address
always @(*) begin
    case (avs_s1_address)
        0: avs_s1_readdata = r0;
        1: avs_s1_readdata = r1;
        2: avs_s1_readdata = r2;
        3: avs_s1_readdata = r3;
        4: avs_s1_readdata = x;
        5: avs_s1_readdata = status;
        default: avs_s1_readdata = 0; // NOADDRESS
    endcase
end
endmodule

```

Fig 3: Avalon-MM interface for the module Matrix Convolution for 3*3 Input Matrix and 2*2 Output Matrix

Fig 3 illustrates the Avalon-MM interface implemented for the matrix convolution module. It shows the memory-mapped communication protocol, detailing the flow of read and write operations between the processor and FPGA. Control signals and address decoding are used to ensure proper data transfer. This file is attached as “matrix_convolution_avalon_interface.sv”. In this project, we used 3*3 input matrix module for Hardware software codesign.

Signal	Direction	Description
avs_sl_write	Input	Write enable for input data
avs_sl_read	Input	Read enable for output data
avs_sl_address	Input	Specifies the target register
avs_sl_writedata	Input	Input data for the convolution
avs_sl_readdata	Output	Output data (convolution result)

3.3 Custom Component Creation

The netlist description of the matrix convolution accelerator was implemented with the help of Intel Quartus Prime to obtain the custom component. The design included the following steps:

- **FSM Implementation:** The FSM and associated data path were described in system verilog to implement the functionality of convolution.
- **Avalon-MM Interface Integration:** It became necessary to map signals to the Avalon-MM protocol.
- **System Integration:** This was implemented in the Platform Designer (Qsys) and memory mapped was initialized with a base address.
- **Header File Generation:** The .socinfo file was further used to create another header point for the software application to use, the macros included concerned memory-mapping.

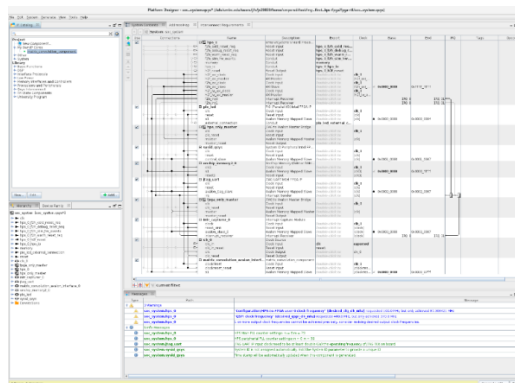


Fig 4: Custom Component Creation for Matrix Convolution

Fig 4 shows the process of custom component creation for the matrix convolution module. It highlights the steps taken in Intel Quartus Prime, including FSM implementation, Avalon-MM integration, and system-level configuration, to create a functional hardware component.

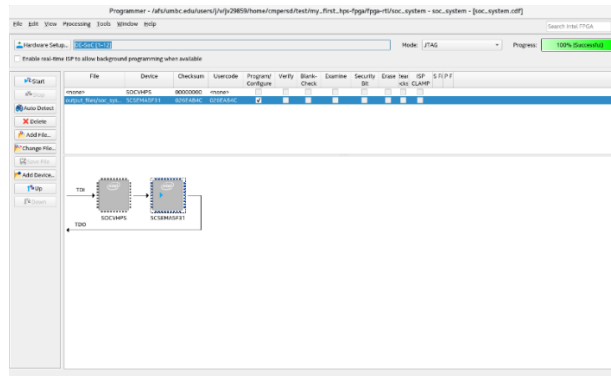


Fig 5: FPGA is programmed successfully

Fig 5 confirms the successful programming of the FPGA for executing matrix convolution operations. It demonstrates the completion of hardware configuration, readying the system for validation and testing.

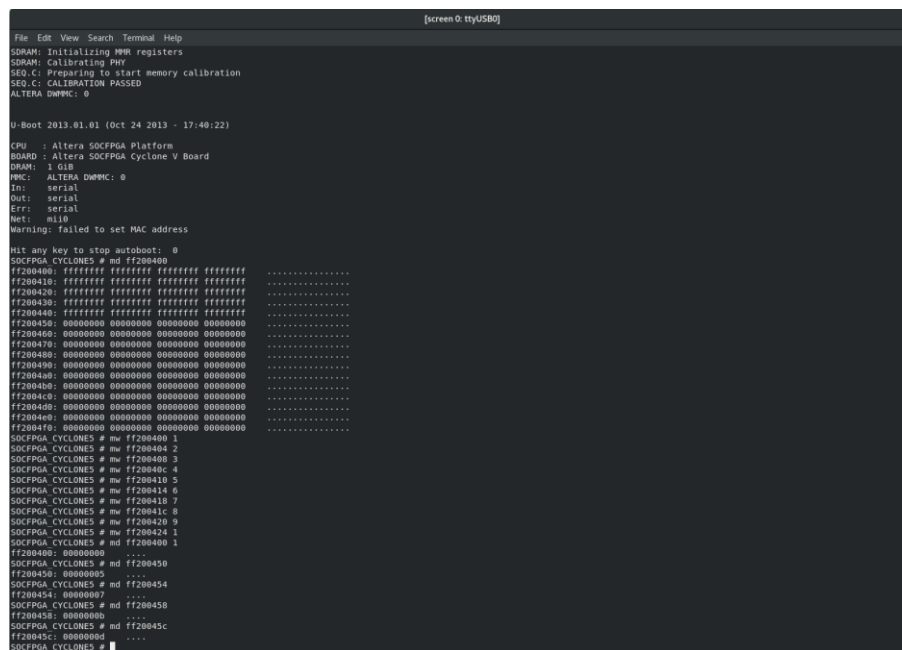


Fig 6: Writing and Reading into registers using U-Boot terminal

Fig 6 shows the writing and reading of data into registers using the U-Boot terminal. It provides an example of how input data is stored and output data is retrieved, illustrating the interaction between hardware and software components.

3.4 Software Hardware Codesign

The specific software application also known as main.c was completed and designed to directly operate with the hardware accelerators. It performed the following operations:

- Writing Input Matrix: The processor stored this input matrix with 3 rows and 3 columns to the hardware through the memory-map I/O.
- Triggering Computation: After accepting the input, the hardware went to the COMPUTE state on its own accord.
- Reading Output Matrix: The processor also got the computed 2*2 output matrix from the hardware.

Fig 7 depicts the software and hardware integration code (main.c). It demonstrates the functions for writing input matrices, triggering computation, and reading output matrices via the Avalon-MM interface, ensuring smooth operation of the hardware accelerator. The file is attached as “main.c”.

```

// File name: main.c
// Program to interface with FPGA Matrix Convolution Module via Avalon-MM over IPS to FPGAs bridge.

#include <stdio.h>
#include <unistd.h>
#include <fcntl.h>
#include <sys/mman.h>
#include <time.h> // for benchmarking
#include <math.h>
#include <fcntl.h>
#include <sys/mman.h>
#include <fcntl.h>
#include <sys/mman.h>
#include <fcntl.h>
#include <sys/mman.h>

// Map to FPGAs bridge memory map constants
#define HW_REGS_BASE (ALT_STM_OFFSET)
#define HW_REGS_SPAN (8444800)
#define HW_REGS_MASK (HW_REGS_SPAN - 1)

// Base address for the device configuration module
#define MATRIX_CONVOLUTION_BASE 0x0200400

// Macros to calculate register addresses
#define IO_PTR(BASE, OFFSET) ((volatile uint32_t *) (virtual_base + ((BASE + OFFSET) & HW_REGS_MASK)))

// Function prototypes
void write_input_matrix(void *virtual_base);
void start_computation(void *virtual_base);
void add_basic_delay();
void read_output_matrix(void *virtual_base);
void print_current_time();
double get_time_diff(struct timespec start, struct timespec end);

int main() {
    void *virtual_base; // Virtual memory pointer
    int fd; // File descriptor for /dev/mem
    struct timespec total_start, total_end, start_time, end_time;
    double elapsed_time, total_time;

    // Open /dev/mem to access FPGA registers
    if ((fd = open("/dev/mem", O_RDWR | O_SYNC)) == -1) {
        printf("ERROR: Could not open /dev/mem...\n");
        return 1;
    }

    // Map FPGA registers into user space
    virtual_base = mmap(0, HW_REGS_SPAN, (PROT_READ | PROT_WRITE), MAP_SHARED, fd, HW_REGS_BASE);
    if (virtual_base == MAP_FAILED) {
        printf("ERROR: mmap() failed...\n");
        close(fd);
        return 1;
    }
    printf("INFO: FPGA memory mapped successfully.\n");

    // Measure total execution time
    clock_gettime(CLOCK_MONOTONIC, &total_start);
    print_current_time();

    // Write input matrix and measure time
    clock_gettime(CLOCK_MONOTONIC, &start_time);
    printf("DEBUG: Writing input matrix to FPGA...\n");
    write_input_matrix(virtual_base);
    clock_gettime(CLOCK_MONOTONIC, &end_time);
    printf("BENCHMARK: Writing inputs took %.6f seconds.\n", get_time_diff(start_time, end_time));

    // Start computation and measure time
    clock_gettime(CLOCK_MONOTONIC, &start_time);
    printf("DEBUG: Starting computation...\n");
    start_computation(virtual_base);
    add_basic_delay();
    clock_gettime(CLOCK_MONOTONIC, &end_time);
    printf("BENCHMARK: Computation took %.6f seconds.\n", get_time_diff(start_time, end_time));

    // Read output matrix and measure time
    clock_gettime(CLOCK_MONOTONIC, &start_time);
    printf("DEBUG: Reading output matrix from FPGA...\n");
    read_output_matrix(virtual_base);
    clock_gettime(CLOCK_MONOTONIC, &end_time);
    printf("BENCHMARK: Reading outputs took %.6f seconds.\n", get_time_diff(start_time, end_time));

    // Measure total execution time
    clock_gettime(CLOCK_MONOTONIC, &total_end);
    printf("TOTAL EXECUTION TIME: %.6f seconds.\n", get_time_diff(total_start, total_end));

    // Clean up
    if (munmap(virtual_base, HW_REGS_SPAN) != 0) {
        printf("Error: munmap() failed...\n");
        close(fd);
        return 1;
    }
    close(fd);
    printf("INFO: /dev/mem closed successfully.\n");
    return 0;
}

// Write input matrix values to FPGA registers
void write_input_matrix(void *virtual_base) {
    for (int i = 0; i < 8; i++) {
        *IO_PTR(MATRIX_CONVOLUTION_BASE, i * 4) = i + 1; // Write input values
        uint32_t value = *IO_PTR(MATRIX_CONVOLUTION_BASE, i * 4); // Read back to confirm
        printf("DEBUG: Write and = %d, Read back: %d\n", i + 1, value);
    }
    printf("INFO: Input matrix written successfully.\n");
}

// Start the FPGA computation
void start_computation(void *virtual_base) {
    *IO_PTR(MATRIX_CONVOLUTION_BASE, 0 * 4) = 1; // Write '1' to start register
    uint32_t start_value = *IO_PTR(MATRIX_CONVOLUTION_BASE, 0 * 4);
    printf("DEBUG: Computation started, Read back: %d\n", start_value);
}

// Add a basic software delay for FPGA computation time
void add_basic_delay() {
    volatile int delay_count = 1000000;
    while (delay_count > 0) {
        printf("DEBUG: Basic delay completed.\n");
    }
}

// Read output matrix values from FPGA registers
void read_output_matrix(void *virtual_base) {
    uint32_t expected_values[] = {5, 0, 1, 1}; // Expected results
    for (int i = 0; i < 4; i++) {
        uint32_t value = *IO_PTR(MATRIX_CONVOLUTION_BASE, i * 4);
        printf("DEBUG: Read %d = %d (Expected: %d)\n", i, value, expected_values[i]);
    }
    printf("INFO: Output matrix read successfully.\n");
}

// Calculate time difference in seconds
double get_time_diff(struct timespec start, struct timespec end) {
    return (end.tv_sec - start.tv_sec) + (end.tv_nsec - start.tv_nsec) / 1e9;
}

// Print current system time
void print_current_time() {
    time_t now = time(NULL);
    struct tm *local_time = localtime(&now);
    printf("CURRENT TIME: %02d:%02d:%02d\n",
        local_time->tm_hour,
        local_time->tm_min,
        local_time->tm_sec);
}

```

Fig 7: Software and Hardware Integration Code (main.c)

3.5 Testbench and Validation

To demonstrate the implementation of the FSM and the data path, a system verilog testbench has been created and implemented. The testbench simulated across a input scenario and captured waveform to verify:

- Proper state transition in the FSM has been verified.
- Proper calculation of the given convolution operation is done.
- Avalon-MM interface to FSM and vice versa must exchange the correct data.
- Waveform analysis shows that the design meets functional and timing specifications.
- Here, two testbenches are written, one for 3*3 input matrix and 2*2 output matrix. On the other hand, another testbench is for 5*5 input matrix and 3*3 output matrix. Those results are shown below respectively.

```
// Testbench for module of 3x3 Matrix convolution
module tb_matrix_convolution;
    // Define testbenches
    logic clk;
    logic reset;
    logic start;
    logic [11:0] input_matrix_0, input_matrix_1, input_matrix_2;
    logic [11:0] input_matrix_3, input_matrix_4, input_matrix_5;
    logic [11:0] input_matrix_6, input_matrix_7, input_matrix_8;

    logic done;
    logic [11:0] output_matrix_0, output_matrix_1;
    logic [11:0] output_matrix_2, output_matrix_3;

    // Instantiate the matrix convolution module
    matrix_convolution uut (
        .clk(clk),
        .reset(reset),
        .start(start),
        .input_matrix_0(input_matrix_0), .input_matrix_1(input_matrix_1),
        .input_matrix_2(input_matrix_2), .input_matrix_3(input_matrix_3),
        .input_matrix_4(input_matrix_4), .input_matrix_5(input_matrix_5),
        .input_matrix_6(input_matrix_6), .input_matrix_7(input_matrix_7),
        .input_matrix_8(input_matrix_8),
        .done(done),
        .output_matrix_0(output_matrix_0), .output_matrix_1(output_matrix_1),
        .output_matrix_2(output_matrix_2), .output_matrix_3(output_matrix_3)
    );

    // Clock generation
    initial begin
        clk = 0;
        forever #5 clk = ~clk; // 10 ns clock period
    end

    // Stimulus block
    initial begin
        $dumpfile("waveform.vcd"); // Create a waveform file
        $dumpvars(0, tb_matrix_convolution); // Dump all variables in the testbench

        reset = 1; // Apply reset
        start = 0; // Start signal function
        #10 reset = 0; // Deassert reset after 10 ns

        // Initialize input matrix
        input_matrix_0 = 1; input_matrix_1 = 2; input_matrix_2 = 3;
        input_matrix_3 = 4; input_matrix_4 = 5; input_matrix_5 = 6;
        input_matrix_6 = 7; input_matrix_7 = 8; input_matrix_8 = 9;

        // Start the convolution
        start = 1;
        #10 start = 0;

        // Wait for the done signal
        wait(done);

        // Display the output matrix
        $display("Output Matrix-1");
        $display("%d %d", output_matrix_0, output_matrix_1);
        $display("%d %d", output_matrix_2, output_matrix_3);
        #10

        // Finish simulation
        $stop;
    end
endmodule
```

Fig 8: Testbench for Matrix Convolution module for 3*3 Input Matrix and 2*2 output Matrix

Fig 8 presents the SystemVerilog testbench for the matrix convolution module with a 3x3 input matrix and a 2x2 output matrix. It validates the FSM and datapath, checking for proper state transitions and correct data exchange through the Avalon-MM interface. This file is attached as “matrix_convolution3_3tb.sv”.

Fig 9 shows the simulation results for the 3x3 input matrix and 2x2 output matrix. It verifies the

correctness of the matrix convolution module by comparing the expected output with the computed results.

```
xcelium> run
Output Matrix:
      5      7
     11     13
Simulation stopped via $stop(1) at time 75 NS + 0
./testbench.sv:61      $stop;
xcelium> TOOL: xrun      23.09-s001: Exiting on Dec 15, 2024 at 23:37:27 EST (total: 00:00:02)
Finding VCD file...
./waveform.vcd
[2024-12-16 04:37:27 UTC] opening EPWave...
Done
```

Fig 9: Simulation Results for Matrix Convolution module for 3*3 Input Matrix and 2*2 output Matrix



Fig 10: Waveform for Matrix Convolution module for 3*3 Input Matrix and 2*2 output Matrix

Fig 10 displays the waveform for the matrix convolution module with a 3x3 input matrix and a 2x2 output matrix. It confirms the proper timing and functional behavior of the FSM and data path during the computation process.

3.6 Clock Cycle Analysis

The clock cycle waveform demonstrates the behavior of the FSM-based matrix convolution hardware. The analysis is as follows:

1. Input Matrix Loading (WRITE_MATRIX):

- All input matrix elements (input_matrix_0 to input_matrix_8) are loaded simultaneously within a single clock cycle.
- **Total Clock Cycles for Input Load: 1 clock cycle.**

2. Convolution Computation (COMPUTE):

- The computation phase processes all output elements together and completes in just 2 clock cycles.

- **Total Clock Cycles for Computation: 2 clock cycles.**

3. **Output Matrix Generation (READ_OUTPUT):**

- The output matrix elements (output_matrix_0 to output_matrix_3) are produced sequentially, one per clock cycle.
- For **4 output elements**, the total time for the readout phase is:
 $4\text{elements} \times 1\text{clock cycle/element} = 4\text{clock cycles}.$

4. **Total Execution Time:**

Summing up all phases, the total clock cycles required are:

- **Input Write:** 1 clock cycle
- **Computation:** 2 clock cycles
- **Output Read:** 4 clock cycles

Total Execution Time: 7 clock cycles

The total execution time for the matrix convolution operation is **7 clock cycles**, demonstrating an optimized and efficient hardware implementation.

```

module tb_sliding_window_convolution;

logic clk, reset, write, read;
logic [15:0] data_in;
logic [15:0] data_out;
logic done;

// Instantiate the component under test (CUT)
sliding_window_convolution dut (
    .clk(clk),
    .reset(reset),
    .write(write),
    .read(read),
    .data_in(data_in),
    .data_out(data_out),
    .done(done)
);

// Clock generation
initial begin
    clk = 0;
    forever #10 clk = ~clk; // 10 ns clock period
end

// Load the matrix
initial begin
    // Load the matrix values on initial reset
    matrix_values[0] = 4;
    matrix_values[1] = 4;
    matrix_values[2] = 4;
    matrix_values[3] = 4;
    matrix_values[4] = 4;
    matrix_values[5] = 4;
    matrix_values[6] = 4;
    matrix_values[7] = 4;
    matrix_values[8] = 4;
    matrix_values[9] = 4;
end

// Testbench logic
initial begin
    // Write the input matrix
    write = 0;
    read = 0;
    data_in = 0;
    data_out = 0;
    done = 0;

    // Apply reset
    #10 reset = 1;

    // Wait for reset
    #100 reset = 0;

    // Specify the data file name
    $write($testdir + "sliding_window_convolution.txt"); // Specify the data file name
    $read($testdir + "sliding_window_convolution.txt"); // Read the data from the file

    // Write the input matrix
    for (int i = 0; i < 5; i++) begin
        for (int j = 0; j < 5; j++) begin
            matrix_values[i*5+j] = 4;
        end
    end

    // Write the input matrix
    $write($testdir + "sliding_window_convolution.txt");
    for (int i = 0; i < 5; i++) begin
        for (int j = 0; j < 5; j++) begin
            data_in = matrix_values[i*5+j]; // Assign values from the input matrix
            $write($testdir + "sliding_window_convolution.txt");
        end
    end

    // Read the output matrix
    $read($testdir + "sliding_window_convolution.txt");
    for (int i = 0; i < 5; i++) begin
        for (int j = 0; j < 5; j++) begin
            data_out = matrix_values[i*5+j];
        end
    end

    // Read the output matrix
    $read($testdir + "sliding_window_convolution.txt");
    for (int i = 0; i < 5; i++) begin
        for (int j = 0; j < 5; j++) begin
            data_out = matrix_values[i*5+j];
        end
    end

    // Wait for computation to complete
    $wait(100);
    $display("Computation completed.");

    // Read the output matrix values in the format
    $read($testdir + "sliding_window_convolution.txt");
    for (int row = 0; row < 5; row++) begin
        for (int col = 0; col < 5; col++) begin
            data_out = matrix_values[row*5+col];
        end
    end

    // Read the output matrix values in the format
    $read($testdir + "sliding_window_convolution.txt");
    for (int row = 0; row < 5; row++) begin
        for (int col = 0; col < 5; col++) begin
            data_out = matrix_values[row*5+col];
        end
    end

    // Wait for computation to complete
    $wait(100);
    $display("Testbench completed.");
end
endmodule

```

Fig 11: Testbench for Matrix Convolution module for 5*5 Input Matrix and 3*3 output Matrix

Fig 11 depicts the testbench for the matrix convolution module with a 5x5 input matrix and a 3x3 output matrix. It expands on the design's scalability and demonstrates accurate computation for larger data sizes. This file is attached as “matrix_convolution5_5tb.sv”.


```

kernel Matrix:
1 0 1
1 0 1
1 0 1
Starting to write input matrix...
Input Matrix:
0 1 2 3 4
5 6 7 8 9
10 11 12 13 14
15 16 17 18 19
20 21 22 23 24
waiting for computation...
Computation completed.
Output Matrix:
36 42 48
66 72 78
96 102 108
Testbench completed.
simulation complete via $finish(1) at time 455 NS + 0
./testbench.sv:103      $finish;

```

Fig 12: Simulation Results for Matrix Convolution module for 5*5 Input Matrix and 3*3 output Matrix

Fig 12 presents the simulation results for the 5x5 input matrix and 3x3 output matrix. It validates the hardware's functionality and ability to compute matrix convolutions for larger input data efficiently.

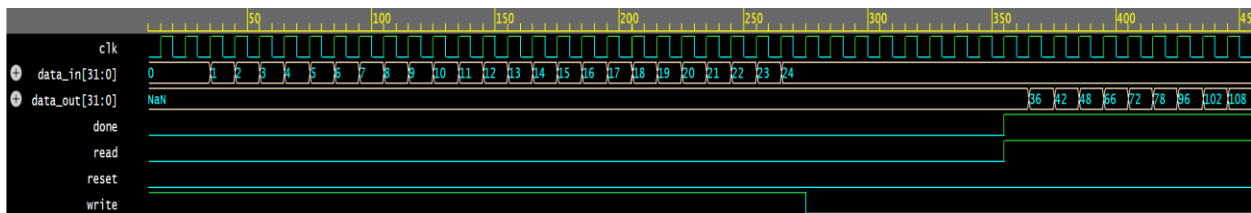


Fig 13: Waveform for Matrix Convolution module for 5*5 Input Matrix and 3*3 output Matrix

Fig 13 shows the waveform for the matrix convolution module with a 5x5 input matrix and a 3x3 output matrix. It illustrates the FSM's timing behavior and verifies the correctness of state transitions and output generation.

3.7 Implementation with only software

To set up a performance baseline, a C program for software only implementation for matrix convolution operation was designed. This implementation performed the following steps:

- Input Matrix: The 3*3 input matrix and 2*2 kernel were described in the program.

- Convolution Operation: Kernel sliding over the input matrix and performing the dot product computation was implemented using nested loop architecture.
- Output Matrix: To validate the outputs, they were saved in a 2*2 matrix output section.
- Here, two software implementations are written, one for 3*3 input matrix and 2*2 output matrix. On the other hand, another is for 5*5 input matrix and 3*3 output matrix. Those results are shown below respectively.

```

#include <stdio.h>
#include <time.h>

// Matrix dimensions
#define INPUT_ROWS 3
#define INPUT_COLS 3
#define KERNEL_ROWS 2
#define KERNEL_COLS 2
#define OUTPUT_ROWS (INPUT_ROWS - KERNEL_ROWS + 1)
#define OUTPUT_COLS (INPUT_COLS - KERNEL_COLS + 1)

// Function to perform matrix convolution
void matrix_convolution(int input[INPUT_ROWS][INPUT_COLS], int kernel[KERNEL_ROWS][KERNEL_COLS], int output[OUTPUT_ROWS][OUTPUT_COLS]);

int main() {
    // Input matrix (3x3)
    int input[INPUT_ROWS][INPUT_COLS] = {
        {1, 2, 3},
        {4, 5, 6},
        {7, 8, 9}
    };

    // Kernel matrix (2x2)
    int kernel[KERNEL_ROWS][KERNEL_COLS] = {
        {1, 0},
        {1, 0}
    };

    // Output matrix (2x2)
    int output[OUTPUT_ROWS][OUTPUT_COLS] = {0};

    // Start benchmarking
    clock_t start_time = clock();

    // Perform matrix convolution
    matrix_convolution(input, kernel, output);

    // End benchmarking
    clock_t end_time = clock();

    // Calculate total execution time in seconds
    double total_time = (double)(end_time - start_time) / CLOCKS_PER_SEC;

    // Print the input matrix
    printf("Input Matrix:\n");
    for (int i = 0; i < INPUT_ROWS; i++) {
        for (int j = 0; j < INPUT_COLS; j++) {
            printf("%d ", input[i][j]);
        }
        printf("\n");
    }

    // Print the kernel matrix
    printf("Kernel Matrix:\n");
    for (int i = 0; i < KERNEL_ROWS; i++) {
        for (int j = 0; j < KERNEL_COLS; j++) {
            printf("%d ", kernel[i][j]);
        }
        printf("\n");
    }

    // Print the output matrix
    printf("Output Matrix:\n");
    for (int i = 0; i < OUTPUT_ROWS; i++) {
        for (int j = 0; j < OUTPUT_COLS; j++) {
            printf("%d ", output[i][j]);
        }
        printf("\n");
    }

    // Print the total execution time
    printf("Execution Time: %.2f seconds\n", total_time);
    return 0;
}

// Function to perform matrix convolution
void matrix_convolution(int input[INPUT_ROWS][INPUT_COLS], int kernel[KERNEL_ROWS][KERNEL_COLS], int output[OUTPUT_ROWS][OUTPUT_COLS]) {
    for (int i = 0; i < OUTPUT_ROWS; i++) {
        for (int j = 0; j < OUTPUT_COLS; j++) {
            int sum = 0;
            for (int k1 = 0; k1 < KERNEL_ROWS; k1++) {
                for (int k2 = 0; k2 < KERNEL_COLS; k2++) {
                    sum += input[i + k1][j + k2] * kernel[k1][k2];
                }
            }
            output[i][j] = sum;
        }
    }
}

```

Fig 14: Software only Implementation of Matrix Convolution for 3*3 Input Matrix and 2*2 output Matrix

Fig 14 depicts the software-only implementation for matrix convolution using a 3x3 input matrix and a 2x2 kernel matrix. It highlights the C code structure used to perform the operation and sets the baseline for hardware comparison. This file is attached as “software3_3.c”.

```

Input Matrix:
1 2 3
4 5 6
7 8 9

Kernel Matrix:
1 0
1 0

Output Matrix:
5 7
11 13

Execution Time: 0.000002 seconds

...Program finished with exit code 0
Press ENTER to exit console.

```

Fig 15: Results for Software only Implementation of Matrix Convolution for 3*3 Input Matrix and 2*2 output Matrix

Fig 15 shows the results of the software-only implementation for the 3x3 input matrix and 2x2 kernel matrix. It validates the correctness of the output generated by the software approach.

```

#include <stdio.h>
#include <time.h>

// Define dimensions
#define INPUT_ROWS 5
#define INPUT_COLS 5
#define KERNEL_ROWS 3
#define KERNEL_COLS 3
#define OUTPUT_ROWS (INPUT_ROWS - KERNEL_ROWS + 1)
#define OUTPUT_COLS (INPUT_COLS - KERNEL_COLS + 1)

// Function prototypes
void matrix_convolution(int input[INPUT_ROWS][INPUT_COLS], int kernel[KERNEL_ROWS][KERNEL_COLS], int output[OUTPUT_ROWS][OUTPUT_COLS]);

int main() {
    // Create input matrix
    int input[INPUT_ROWS][INPUT_COLS] = {
        {1, 2, 3, 4, 5},
        {6, 7, 8, 9, 10},
        {11, 12, 13, 14, 15},
        {16, 17, 18, 19, 20},
        {21, 22, 23, 24, 25}
    };

    // Create kernel matrix
    int kernel[KERNEL_ROWS][KERNEL_COLS] = {
        {1, 0, 1},
        {0, 1, 0},
        {1, 0, 1}
    };

    // Output matrix
    int output[OUTPUT_ROWS][OUTPUT_COLS] = {0};

    // Perform matrix convolution
    matrix_convolution(input, kernel, output);

    // Print the input matrix
    printf("Input Matrix:\n");
    for (int i = 0; i < INPUT_ROWS; i++) {
        for (int j = 0; j < INPUT_COLS; j++) {
            printf("%d ", input[i][j]);
        }
        printf("\n");
    }

    // Print the kernel matrix
    printf("Kernel Matrix:\n");
    for (int i = 0; i < KERNEL_ROWS; i++) {
        for (int j = 0; j < KERNEL_COLS; j++) {
            printf("%d ", kernel[i][j]);
        }
        printf("\n");
    }

    // Print the output matrix
    printf("Output Matrix:\n");
    for (int i = 0; i < OUTPUT_ROWS; i++) {
        for (int j = 0; j < OUTPUT_COLS; j++) {
            printf("%d ", output[i][j]);
        }
        printf("\n");
    }

    return 0;
}

// Function to perform matrix convolution
void matrix_convolution(int input[INPUT_ROWS][INPUT_COLS], int kernel[KERNEL_ROWS][KERNEL_COLS], int output[OUTPUT_ROWS][OUTPUT_COLS]) {
    for (int i = 0; i < OUTPUT_ROWS; i++) {
        for (int j = 0; j < OUTPUT_COLS; j++) {
            int sum = 0;
            for (int k1 = 0; k1 < KERNEL_ROWS; k1++) {
                for (int k2 = 0; k2 < KERNEL_COLS; k2++) {
                    sum += input[i + k1][j + k2] * kernel[k1][k2];
                }
            }
            output[i][j] = sum;
        }
    }
}

```

Fig 16: Software only Implementation of Matrix Convolution module for 5*5 Input Matrix and 3*3 output Matrix

Fig 16 depicts the software-only implementation for a 5x5 input matrix and a 3x3 kernel matrix. It demonstrates the nested loop structure used to perform convolutions on larger matrices. This file is attached as “software5_5.c”.

```
Input Matrix:
0 1 2 3 4
5 6 7 8 9
10 11 12 13 14
15 16 17 18 19
20 21 22 23 24

Kernel Matrix:
1 0 1
1 0 1
1 0 1

Output Matrix:
36 42 48
66 72 78
96 102 108

...Program finished with exit code 0
Press ENTER to exit console.
```

Fig 17: Results for Software only Implementation of Matrix Convolution for 5*5 Input Matrix and 3*3 output Matrix

Fig 17 shows the results of the software-only implementation for the 5x5 input matrix and 3x3 kernel matrix. It verifies the accuracy of the output and establishes a baseline for larger matrix convolutions.

4. Benchmarking and Validation

4.1 Software-Only Implementation Results

The software-only implementation was executed on a general-purpose processor to calculate the matrix convolution. The execution time is 0.000002 seconds.

```
Input Matrix:
1 2 3
4 5 6
7 8 9

Kernel Matrix:
1 0
1 0

Output Matrix:
5 7
11 13

Execution Time: 0.000002 seconds

...Program finished with exit code 0
Press ENTER to exit console.
```

Fig 18: Results for Software only Implementation of Matrix Convolution for 3*3 Input Matrix and 2*2 output Matrix

Fig 18 presents the results of the software-only implementation for the 3x3 input matrix and 2x2 output matrix, highlighting the minimal execution time and correctness of the operation.

4.2 Hardware-Accelerated Implementation Results

The hardware accelerator was implemented on FPGA and validated using hardware-software co-design. The software interacted with the hardware via the Avalon-MM interface, using memory-mapped I/O to transfer input and output data.

Performance Metrics:

- **Input Write Time:** 0.000138 seconds
- **Computation Time:** 0.010058 seconds
- **Output Read Time:** 0.000053 seconds
- **Total Execution Time:** 0.010249 seconds

```

[screen 0: ttyUSB0]
File Edit View Search Terminal Help
Stopping Bootlog daemon: bootlogd.

Poky 8.0 (Yocto Project 1.3 Reference Distro) 1.3
ttyS0

socfpga login: root
root@socfpga:~# ls
custom component test  gmon.out
custom component_test1 helloworld
root@socfpga:~# ./custom_component_test
INFO: FPGA memory mapped successfully.
CURRENT TIME: 05:20:08
DEBUG: Writing input matrix to FPGA...
DEBUG: Wrote a0 = 1 at address 0xFF200400, Read back: -1
DEBUG: Wrote a1 = 2 at address 0xFF200404, Read back: -1
DEBUG: Wrote a2 = 3 at address 0xFF200408, Read back: -1
DEBUG: Wrote a3 = 4 at address 0xFF20040C, Read back: -1
DEBUG: Wrote a4 = 5 at address 0xFF200410, Read back: -1
DEBUG: Wrote a5 = 6 at address 0xFF200414, Read back: -1
DEBUG: Wrote a6 = 7 at address 0xFF200418, Read back: -1
DEBUG: Wrote a7 = 8 at address 0xFF20041C, Read back: -1
DEBUG: Wrote a8 = 9 at address 0xFF200420, Read back: -1
INFO: Input matrix written successfully.
BENCHMARK: Writing inputs took 0.000138 seconds.
DEBUG: Starting computation...
DEBUG: Wrote start = 1 at address 0xFF200424, Read back: -1
INFO: Computation started.
DEBUG: Basic delay completed.
BENCHMARK: computation took 0.010058 seconds.
DEBUG: Reading output matrix from FPGA...
DEBUG: Read r0 = 5 at address 0xFF200450 (Expected: 5)
DEBUG: Read r1 = 7 at address 0xFF200454 (Expected: 7)
DEBUG: Read r2 = 11 at address 0xFF200458 (Expected: 11)
DEBUG: Read r3 = 13 at address 0xFF20045C (Expected: 13)
INFO: Output matrix read successfully.
BENCHMARK: Reading outputs took 0.000053 seconds.
TOTAL EXECUTION TIME: 0.010249 seconds.
INFO: /dev/mem closed successfully.
root@socfpga:~#

```

Fig 19: Results for Software Hardware Codesign Implementation of Matrix Convolution for 3*3 Input Matrix and 2*2 output Matrix using Uboot Terminal

Fig 19 shows the results of the software-hardware co-design implementation using the U-Boot terminal. It demonstrates the hardware-accelerated matrix convolution results, comparing execution times with the software-only implementation and showcasing the benefits of offloading computation to hardware.

The benchmarking process evaluated the correctness and performance of both software-only and hardware-accelerated implementations. The software implementation produced the correct output with minimal execution time due to the small matrix size, completing the convolution

operation in 0.000002 seconds. However, the hardware accelerator, while introducing overhead due to data transfer, demonstrated the capability to offload computation effectively. Future benchmarks with larger input sizes are expected to highlight the FPGA's parallel processing advantage.

4.3 Performance Comparison

Metric	Software Only	Hardware Accelerated
Execution time (seconds)	0.000002	0.010249
Correctness	Matched	Matched
Communication overhead	N/A	Present
Scalability	Limited	High for larger matrices

4.4 Analysis and Discussion

The results indicate that software only approach is slightly faster for this specific small matrix size (3x3 output). This is due to the following factors:

- **Communication Overhead:** Sending data between the CPU and FPGA adds delay and destroys performance for finer tasks creating hardware fewer than elaborate projects.
- **Problem Size:** Program in the hardware accelerator does not show its advantages with small matrices, as with them, the modern processor calculates the lightening fast.
- **Setup Overhead:** Synchronization at the first use of additional hardware and access via a memory-mapped range have an unavoidable cost.

However, hardware acceleration offers significant advantages for:

- **Larger Matrices:** It should also be noted that the present work has demonstrated that as matrix size increases (e.g., 100 x 100 or 1000 x 1000), the parallel FPGA architecture will offer better performance than a CPU.
- **Repeated Computations:** For real time or repeated processing, the hardware accelerator cuts CPU load and improves operating efficiency.

5. Conclusion

This project successfully demonstrated designing and implementing a hardware accelerator for matrix convolution operations. The FSM based design is integrated with Avalon-MM interface provided effective interconnection between the processor and FPGA. However, because of low computational complexity, the software-only implementation proved faster than the hardware design for small matrix sizes except for the spatial design where the proposed hardware accelerator achieved functional correctness and is capable of offloading computation.

The results suggest FPGA-based hardware acceleration is very efficient for computational-only tasks particularly at large problem sizes. In more detail, the approach of the hardware accelerator is to rely on the possibility of parallel processing for larger matrices and repetitive calculations.

6. Future Work

Future improvements to this project could focus on:

- **Scalability for Larger Matrices:** Benchmarking the hardware accelerator with larger input sizes (e.g., 100x100 or 1000x1000) to demonstrate its parallel processing advantage.
- **Pipelined Design:** Introducing pipelining in the FSM to reduce latency and improve throughput.

References:

- [1] Cao, Y., Wei, X., Qiao, T., & Chen, H. (2019, December). FPGA-based accelerator for convolution operations. In *2019 IEEE International Conference on Signal, Information and Data Processing (ICSIDP)* (pp. 1-5). IEEE.
- [2] Snytsar, R. (2023). Sliding window sum algorithms for deep neural networks. *arXiv preprint arXiv:2305.16513*.