

## JEE Advanced 2022 28th August S2

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Test Date	28/08/2022
Test Time	2:30 PM - 5:30 PM
Subject	JEE Advanced 2022 Paper 2

Section : Math Sec 1

**Q.1**

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

If  $y(x)$  is the solution of the differential equation

$$xdy - (y^2 - 4y)dx = 0 \quad \text{for } x > 0, \quad y(1) = 2,$$

and the slope of the curve  $y = y(x)$  is never zero, then the value of  $10 y(\sqrt{2})$  is \_\_\_\_\_.

Given 8

Answer :

Question Type : SDI

Question ID : 859434326

**Q.2**

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Let  $\beta$  be a real number. Consider the matrix

$$A = \begin{pmatrix} \beta & 0 & 1 \\ 2 & 1 & -2 \\ 3 & 1 & -2 \end{pmatrix}.$$

If  $A^7 - (\beta - 1)A^6 - \beta A^5$  is a singular matrix, then the value of  $9\beta$  is \_\_\_\_\_.

Given 9

Answer :

Question Type : SDI

Question ID : 859434330

**Q.3****SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

If

$$\beta = \lim_{x \rightarrow 0} \frac{e^{x^3} - (1 - x^3)^{\frac{1}{3}} + ((1 - x^2)^{\frac{1}{2}} - 1) \sin x}{x \sin^2 x},$$

then the value of  $6\beta$  is \_\_\_\_\_.**Given 8****Answer :**Question Type : **SDI**Question ID : **859434329****Q.4****SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Consider the hyperbola

$$\frac{x^2}{100} - \frac{y^2}{64} = 1$$

with foci at  $S$  and  $S_1$ , where  $S$  lies on the positive  $x$ -axis. Let  $P$  be a point on the hyperbola, in the first quadrant. Let  $\angle SPS_1 = \alpha$ , with  $\alpha < \frac{\pi}{2}$ . The straight line passing through the point  $S$  and having the same slope as that of the tangent at  $P$  to the hyperbola, intersects the straight line  $S_1P$  at  $P_1$ . Let  $\delta$  be the distance of  $P$  from the straight line  $SP_1$ , and  $\beta = S_1P$ . Then the greatest integer less than or equal to  $\frac{\beta\delta}{9} \sin \frac{\alpha}{2}$  is \_\_\_\_\_.

**Given --****Answer :**Question Type : **SDI**Question ID : **859434331**

Q.5

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Consider the functions  $f, g : \mathbb{R} \rightarrow \mathbb{R}$  defined by

$$f(x) = x^2 + \frac{5}{12} \quad \text{and} \quad g(x) = \begin{cases} 2\left(1 - \frac{4|x|}{3}\right), & |x| \leq \frac{3}{4}, \\ 0, & |x| > \frac{3}{4}. \end{cases}$$

If  $\alpha$  is the area of the region

$$\left\{(x, y) \in \mathbb{R} \times \mathbb{R} : |x| \leq \frac{3}{4}, 0 \leq y \leq \min\{f(x), g(x)\}\right\},$$

then the value of  $9\alpha$  is \_\_\_\_\_.

Given 6

Answer :

Question Type : SDI

Question ID : 859434332

Q.6

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The product of all positive real values of  $x$  satisfying the equation

$$x^{(16(\log_5 x)^3 - 68 \log_5 x)} = 5^{-16}$$

is \_\_\_\_\_.

Given 1

Answer :

Question Type : SDI

Question ID : 859434328

Q.7

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The greatest integer less than or equal to

$$\int_1^2 \log_2(x^3 + 1) dx + \int_1^{\log_2 9} (2^x - 1)^{\frac{1}{3}} dx$$

is \_\_\_\_\_.

Given 5

Answer :

Question Type : **SDI**Question ID : **859434327**

Q.8

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Let  $\alpha$  and  $\beta$  be real numbers such that  $-\frac{\pi}{4} < \beta < 0 < \alpha < \frac{\pi}{4}$ . If  $\sin(\alpha + \beta) = \frac{1}{3}$  and  $\cos(\alpha - \beta) = \frac{2}{3}$ , then the greatest integer less than or equal to

$$\left( \frac{\sin \alpha}{\cos \beta} + \frac{\cos \beta}{\sin \alpha} + \frac{\cos \alpha}{\sin \beta} + \frac{\sin \beta}{\cos \alpha} \right)^2$$

is \_\_\_\_\_.

Given 1

Answer :

Question Type : **SDI**Question ID : **859434325**

Section : Math Sec 2

Q.1

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Let  $G$  be a circle of radius  $R > 0$ . Let  $G_1, G_2, \dots, G_n$  be  $n$  circles of equal radius  $r > 0$ . Suppose each of the  $n$  circles  $G_1, G_2, \dots, G_n$  touches the circle  $G$  externally. Also, for  $i = 1, 2, \dots, n-1$ , the circle  $G_i$  touches  $G_{i+1}$  externally, and  $G_n$  touches  $G_1$  externally. Then, which of the following statements is/are TRUE ?

**Options**

- A. If  $n = 12$ , then  $\sqrt{2}(\sqrt{3} + 1)r > R$
- B. If  $n = 5$ , then  $r < R$
- C. If  $n = 8$ , then  $(\sqrt{2} - 1)r < R$
- D. If  $n = 4$ , then  $(\sqrt{2} - 1)r < R$

Question Type : **MSQ**Question ID : **859434336**

Chosen Option : --

Q.2

## SECTION 2 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
  - Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
  - For each question, choose the option(s) corresponding to (all) the correct answer(s).
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Let

$$\alpha = \sum_{k=1}^{\infty} \sin^{2k} \left(\frac{\pi}{6}\right).$$

Let  $g : [0, 1] \rightarrow \mathbb{R}$  be the function defined by

$$g(x) = 2^{\alpha x} + 2^{\alpha(1-x)}.$$

Then, which of the following statements is/are TRUE ?

## Options A.

The function  $g(x)$  attains its minimum at more than one pointB. The minimum value of  $g(x)$  is  $2^{\frac{7}{6}}$ 

C.

The maximum value of  $g(x)$  is  $1 + 2^{\frac{1}{3}}$ 

D.

The function  $g(x)$  attains its maximum at more than one point

Question Type : MSQ

Question ID : 859434334

Chosen Option : -

Q.3

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:
 

<i>Full Marks</i>	: +4 <b>ONLY</b> if (all) the correct option(s) is(are) chosen;
<i>Partial Marks</i>	: +3 If all the four options are correct but <b>ONLY</b> three options are chosen;
<i>Partial Marks</i>	: +2 If three or more options are correct but <b>ONLY</b> two options are chosen, both of which are correct;
<i>Partial Marks</i>	: +1 If two or more options are correct but <b>ONLY</b> one option is chosen and it is a correct option;
<i>Zero Marks</i>	: 0 If none of the options is chosen (i.e. the question is unanswered);
<i>Negative Marks</i>	: -2 In all other cases.

Let  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  be the unit vectors along the three positive coordinate axes. Let

$$\begin{aligned}\vec{a} &= 3\hat{i} + \hat{j} - \hat{k}, \\ \vec{b} &= \hat{i} + b_2\hat{j} + b_3\hat{k}, \quad b_2, b_3 \in \mathbb{R}, \\ \vec{c} &= c_1\hat{i} + c_2\hat{j} + c_3\hat{k}, \quad c_1, c_2, c_3 \in \mathbb{R}\end{aligned}$$

be three vectors such that  $b_2b_3 > 0$ ,  $\vec{a} \cdot \vec{b} = 0$  and

$$\begin{pmatrix} 0 & -c_3 & c_2 \\ c_3 & 0 & -c_1 \\ -c_2 & c_1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} 3 - c_1 \\ 1 - c_2 \\ -1 - c_3 \end{pmatrix}.$$

Then, which of the following is/are TRUE ?

**Options**

A.  $\vec{b} \cdot \vec{c} = 0$

B.  $|\vec{c}| \leq \sqrt{11}$

C.  $\vec{a} \cdot \vec{c} = 0$

D.  $|\vec{b}| > \sqrt{10}$

Question Type : **MSQ**Question ID : **859434337**

Chosen Option : --

Q.4

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Let  $\bar{z}$  denote the complex conjugate of a complex number  $z$ . If  $z$  is a non-zero complex number for which both real and imaginary parts of

$$(\bar{z})^2 + \frac{1}{z^2}$$

are integers, then which of the following is/are possible value(s) of  $|z|$  ?

**Options**

A.  $\left(\frac{9+\sqrt{65}}{4}\right)^{\frac{1}{4}}$

B.  $\left(\frac{43+3\sqrt{205}}{2}\right)^{\frac{1}{4}}$

C.  $\left(\frac{7+\sqrt{33}}{4}\right)^{\frac{1}{4}}$

D.  $\left(\frac{7+\sqrt{13}}{6}\right)^{\frac{1}{4}}$

Question Type : **MSQ**

Question ID : **859434335**

Chosen Option : --

Q.5

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

For  $x \in \mathbb{R}$ , let the function  $y(x)$  be the solution of the differential equation

$$\frac{dy}{dx} + 12y = \cos\left(\frac{\pi}{12}x\right), \quad y(0) = 0.$$

Then, which of the following statements is/are TRUE ?

**Options**

A.  $y(x)$  is a periodic function

B.

There exists a real number  $\beta$  such that the line  $y = \beta$  intersects the curve  $y = y(x)$  at infinitely many points

C.  $y(x)$  is an increasing function

D.  $y(x)$  is a decreasing function

Question Type : **MSQ**

Question ID : **859434338**

Chosen Option : --

Q.6

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Let  $PQRS$  be a quadrilateral in a plane, where  $QR = 1$ ,  $\angle PQR = \angle QRS = 70^\circ$ ,  $\angle PQS = 15^\circ$  and  $\angle PRS = 40^\circ$ . If  $\angle RPS = \theta^\circ$ ,  $PQ = \alpha$  and  $PS = \beta$ , then the interval(s) that contain(s) the value of  $4\alpha\beta \sin \theta^\circ$  is/are

**Options**

- A.  $(\sqrt{2}, 3)$
- B.  $(1, 2)$
- C.  $(2\sqrt{2}, 3\sqrt{2})$
- D.  $(0, \sqrt{2})$

Question Type : **MSQ**Question ID : **859434333**

Chosen Option : --

Section : Math Sec 3

**Q.1****SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

**Full Marks** : +3 If **ONLY** the correct option is chosen;  
**Zero Marks** : 0 If none of the options is chosen (i.e. the question is unanswered);  
**Negative Marks** : -1 In all other cases.

Suppose that

Box-I contains 8 red, 3 blue and 5 green balls,  
 Box-II contains 24 red, 9 blue and 15 green balls,  
 Box-III contains 1 blue, 12 green and 3 yellow balls,  
 Box-IV contains 10 green, 16 orange and 6 white balls.

A ball is chosen randomly from Box-I; call this ball  $b$ . If  $b$  is red then a ball is chosen randomly from Box-II, if  $b$  is blue then a ball is chosen randomly from Box-III, and if  $b$  is green then a ball is chosen randomly from Box-IV. The conditional probability of the event ‘one of the chosen balls is white’ given that the event ‘at least one of the chosen balls is green’ has happened, is equal to

**Options**

- A.  $\frac{5}{52}$
- B.  $\frac{1}{8}$
- C.  $\frac{15}{256}$
- D.  $\frac{3}{16}$

Question Type : MCQ

Question ID : 859434341

Chosen Option : D

Q.2

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
  - Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
  - For each question, choose the option corresponding to the correct answer.
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +3 If ONLY the correct option is chosen;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -1 In all other cases.*

For positive integer  $n$ , define

$$f(n) = n + \frac{16 + 5n - 3n^2}{4n + 3n^2} + \frac{32 + n - 3n^2}{8n + 3n^2} + \frac{48 - 3n - 3n^2}{12n + 3n^2} + \dots + \frac{25n - 7n^2}{7n^2} .$$

Then, the value of  $\lim_{n \rightarrow \infty} f(n)$  is equal to

Options

- A.  $4 - \frac{4}{3} \log_e \left(\frac{7}{3}\right)$
- B.  $3 + \frac{3}{4} \log_e 7$
- C.  $3 + \frac{4}{3} \log_e 7$
- D.  $4 - \frac{3}{4} \log_e \left(\frac{7}{3}\right)$

Question Type : MCQ

Question ID : 859434342

Chosen Option : D

Q.3

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

If  $M = \begin{pmatrix} \frac{5}{2} & \frac{3}{2} \\ \frac{3}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{1}{2} \end{pmatrix}$ , then which of the following matrices is equal to  $M^{2022}$  ?

**Options**

- A.  $\begin{pmatrix} 3034 & -3033 \\ 3033 & -3032 \end{pmatrix}$
- B.  $\begin{pmatrix} 3034 & 3033 \\ -3033 & -3032 \end{pmatrix}$
- C.  $\begin{pmatrix} 3032 & 3031 \\ -3031 & -3030 \end{pmatrix}$
- D.  $\begin{pmatrix} 3033 & 3032 \\ -3032 & -3031 \end{pmatrix}$

Question Type : MCQ

Question ID : 859434340

Chosen Option : --

Q.4

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

Consider 4 boxes, where each box contains 3 red balls and 2 blue balls. Assume that all 20 balls are distinct. In how many different ways can 10 balls be chosen from these 4 boxes so that from each box at least one red ball and one blue ball are chosen ?

**Options**

- A. 156816
- B. 21816
- C. 85536
- D. 12096

Question Type : MCQ

Question ID : 859434339

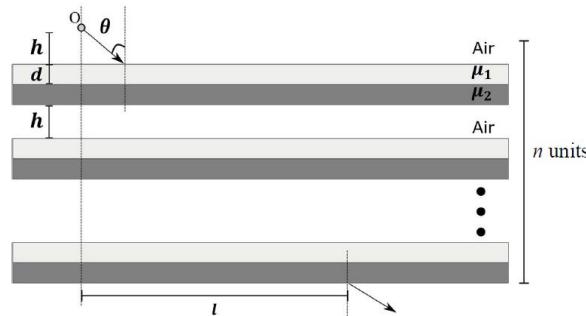
Chosen Option : B

Q.1

## SECTION 1 (Maximum marks: 24)

- This section contains **EIGHT (08)** questions.
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- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Consider a configuration of  $n$  identical units, each consisting of three layers. The first layer is a column of air of height  $h = \frac{1}{3} \text{ cm}$ , and the second and third layers are of equal thickness  $d = \frac{\sqrt{3}-1}{2} \text{ cm}$ , and refractive indices  $\mu_1 = \sqrt{\frac{3}{2}}$  and  $\mu_2 = \sqrt{3}$ , respectively. A light source O is placed on the top of the first unit, as shown in the figure. A ray of light from O is incident on the second layer of the first unit at an angle of  $\theta = 60^\circ$  to the normal. For a specific value of  $n$ , the ray of light emerges from the bottom of the configuration at a distance  $l = \frac{8}{\sqrt{3}} \text{ cm}$ , as shown in the figure. The value of  $n$  is \_\_\_\_.



Given --

Answer :

Question Type : SDI

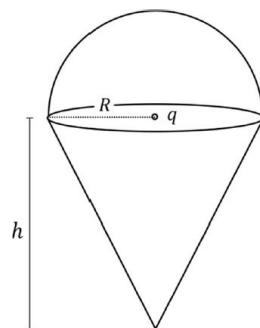
Question ID : 859434347

Q.2

## SECTION 1 (Maximum marks: 24)

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

A charge  $q$  is surrounded by a closed surface consisting of an inverted cone of height  $h$  and base radius  $R$ , and a hemisphere of radius  $R$  as shown in the figure. The electric flux through the conical surface is  $\frac{nq}{6\epsilon_0}$  (in SI units). The value of  $n$  is \_\_\_\_.



Given 3

Answer :

Question Type : SDI

Question ID : 859434348

Q.3

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

In a particular system of units, a physical quantity can be expressed in terms of the electric charge  $e$ , electron mass  $m_e$ , Planck's constant  $h$ , and Coulomb's constant  $k = \frac{1}{4\pi\epsilon_0}$ , where  $\epsilon_0$  is the permittivity of vacuum. In terms of these physical constants, the dimension of the magnetic field is  $[B] = [e]^{\alpha}[m_e]^{\beta}[h]^{\gamma}[k]^{\delta}$ . The value of  $\alpha + \beta + \gamma + \delta$  is \_\_\_\_.

Given --

Answer :

Question Type : SDI

Question ID : 859434346

Q.4

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

A particle of mass  $1 \text{ kg}$  is subjected to a force which depends on the position as  $\vec{F} = -k(x\hat{i} + y\hat{j}) \text{ kg m s}^{-2}$  with  $k = 1 \text{ kg s}^{-2}$ . At time  $t = 0$ , the particle's position  $\vec{r} = \left(\frac{1}{\sqrt{2}}\hat{i} + \sqrt{2}\hat{j}\right) \text{ m}$  and its velocity  $\vec{v} = \left(-\sqrt{2}\hat{i} + \sqrt{2}\hat{j} + \frac{2}{\pi}\hat{k}\right) \text{ m s}^{-1}$ . Let  $v_x$  and  $v_y$  denote the  $x$  and the  $y$  components of the particle's velocity, respectively. **Ignore gravity**. When  $z = 0.5 \text{ m}$ , the value of  $(x v_y - y v_x)$  is \_\_\_\_  $\text{m}^2 \text{s}^{-1}$ .

Given 1

Answer :

Question Type : SDI

Question ID : 859434343

Q.5

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If ONLY the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

In a radioactive decay chain reaction,  $^{230}_{90}\text{Th}$  nucleus decays into  $^{214}_{84}\text{Po}$  nucleus. The ratio of the number of  $\alpha$  to number of  $\beta^-$  particles emitted in this process is \_\_\_\_.

Given 2

Answer :

Question Type : SDI

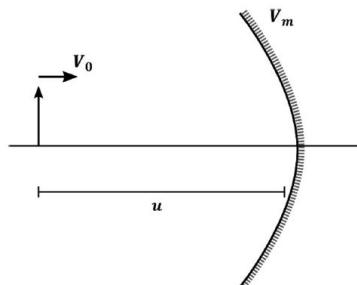
Question ID : 859434344

Q.6

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

An object and a concave mirror of focal length  $f = 10 \text{ cm}$  both move along the principal axis of the mirror with constant speeds. The object moves with speed  $V_0 = 15 \text{ cm s}^{-1}$  towards the mirror with respect to a laboratory frame. The distance between the object and the mirror at a given moment is denoted by  $u$ . When  $u = 30 \text{ cm}$ , the speed of the mirror  $V_m$  is such that the image is instantaneously at rest with respect to the laboratory frame, and the object forms a real image. The magnitude of  $V_m$  is \_\_\_\_\_  $\text{cm s}^{-1}$ .



Given 3

Answer :

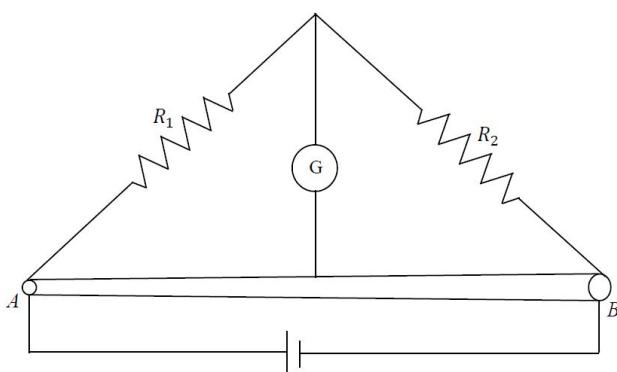
Question Type : **SDI**Question ID : **859434350**

Q.7

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Two resistances  $R_1 = X \Omega$  and  $R_2 = 1 \Omega$  are connected to a wire  $AB$  of uniform resistivity, as shown in the figure. The radius of the wire varies linearly along its axis from  $0.2 \text{ mm}$  at  $A$  to  $1 \text{ mm}$  at  $B$ . A galvanometer ( $G$ ) connected to the center of the wire,  $50 \text{ cm}$  from each end along its axis, shows zero deflection when  $A$  and  $B$  are connected to a battery. The value of  $X$  is \_\_\_\_\_.



Given 5

Answer :

Question Type : **SDI**Question ID : **859434345**

Q.8

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

On a frictionless horizontal plane, a bob of mass  $m = 0.1 \text{ kg}$  is attached to a spring with natural length  $l_0 = 0.1 \text{ m}$ . The spring constant is  $k_1 = 0.009 \text{ Nm}^{-1}$  when the length of the spring  $l > l_0$  and is  $k_2 = 0.016 \text{ Nm}^{-1}$  when  $l < l_0$ . Initially the bob is released from  $l = 0.15 \text{ m}$ . Assume that Hooke's law remains valid throughout the motion. If the time period of the full oscillation is  $T = (n \pi) \text{ s}$ , then the integer closest to  $n$  is \_\_\_\_.

Given 6  
Answer :

Question Type : SDI

Question ID : 859434349

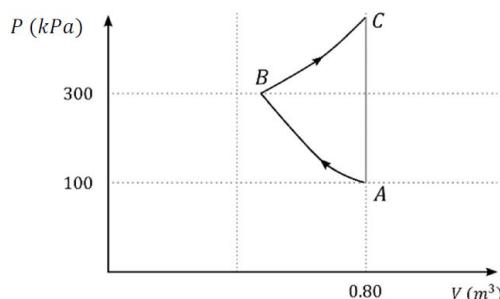
Section : Phy Sec 2

Q.1

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen;  
 Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;  
 Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;  
 Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -2 In all other cases.

In the given  $P$ - $V$  diagram, a monoatomic gas ( $\gamma = \frac{5}{3}$ ) is first compressed adiabatically from state  $A$  to state  $B$ . Then it expands isothermally from state  $B$  to state  $C$ . [Given:  $(\frac{1}{3})^{0.6} \approx 0.5$ ,  $\ln 2 \approx 0.7$  ].



Which of the following statement(s) is(are) correct?

Options A.

- A. The magnitude of the work done in the process  $A \rightarrow B$  is  $60 \text{ kJ}$ .
- B. The magnitude of the work done in the process  $C \rightarrow A$  is zero.
- C. The magnitude of the work done in the process  $B \rightarrow C$  is  $84 \text{ kJ}$ .
- D. The magnitude of the total work done in the process  $A \rightarrow B \rightarrow C$  is  $144 \text{ kJ}$ .

Question Type : MSQ

Question ID : 859434356

Chosen Option : A,B,C

Q.2

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 **ONLY** if (all) the correct option(s) is(are) chosen;  
*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;  
*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;  
*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;  
*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);  
*Negative Marks* : -2 In all other cases.

A disk of radius  $R$  with uniform positive charge density  $\sigma$  is placed on the  $xy$  plane with its center at the origin. The Coulomb potential along the  $z$ -axis is

$$V(z) = \frac{\sigma}{2\epsilon_0} (\sqrt{R^2 + z^2} - z).$$

A particle of positive charge  $q$  is placed initially at rest at a point on the  $z$  axis with  $z = z_0$  and  $z_0 > 0$ . In addition to the Coulomb force, the particle experiences a vertical force  $\vec{F} = -c \hat{k}$  with  $c > 0$ . Let  $\beta = \frac{2c\epsilon_0}{q\sigma}$ . Which of the following statement(s) is(are) correct?

**Options A.**

For  $\beta = \frac{1}{4}$  and  $z_0 = \frac{3}{7}R$ , the particle reaches the origin.

B.

For  $\beta > 1$  and  $z_0 > 0$ , the particle always reaches the origin.

C.

For  $\beta = \frac{1}{4}$  and  $z_0 = \frac{25}{7}R$ , the particle reaches the origin.

D.

For  $\beta = \frac{1}{4}$  and  $z_0 = \frac{R}{\sqrt{3}}$ , the particle returns back to  $z = z_0$ .

+2

Question Type : **MSQ**Question ID : **859434354**Chosen Option : **B,D**

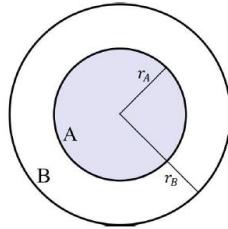
Q.3

## SECTION 2 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

In the figure, the inner (shaded) region  $A$  represents a sphere of radius  $r_A = 1$ , within which the electrostatic charge density varies with the radial distance  $r$  from the center as  $\rho_A = kr$ , where  $k$  is positive. In the spherical shell  $B$  of outer radius  $r_B$ , the electrostatic charge density varies as  $\rho_B = \frac{2k}{r}$ . Assume that dimensions are taken care of. All physical quantities are in their SI units.



Which of the following statement(s) is(are) correct?

**Options A.**

If  $r_B = \frac{5}{2}$ , then the magnitude of the electric field just outside  $B$  is  $\frac{13\pi k}{\epsilon_0}$ .

B.

If  $r_B = \sqrt{\frac{3}{2}}$ , then the electric field is zero everywhere outside  $B$ .

C.

If  $r_B = 2$ , then the total charge of the configuration is  $15\pi k$ .

D.

If  $r_B = \frac{3}{2}$ , then the electric potential just outside  $B$  is  $\frac{k}{\epsilon_0}$ .

Question Type : **MSQ**

Question ID : **859434351**

Chosen Option : **D**

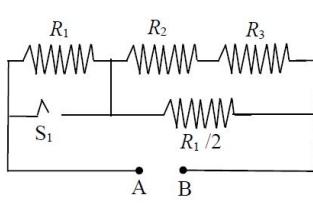
Q.4

## SECTION 2 (Maximum Marks: 24)

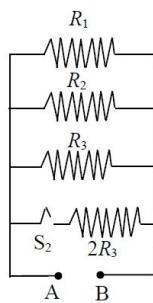
- This section contains **SIX (06)** questions.
  - Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
  - For each question, choose the option(s) corresponding to (all) the correct answer(s).
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

In Circuit-1 and Circuit-2 shown in the figures,  $R_1 = 1 \Omega$ ,  $R_2 = 2 \Omega$  and  $R_3 = 3 \Omega$ .  
 $P_1$  and  $P_2$  are the power dissipations in Circuit-1 and Circuit-2 when the switches  $S_1$  and  $S_2$  are in open conditions, respectively.

$Q_1$  and  $Q_2$  are the power dissipations in Circuit-1 and Circuit-2 when the switches  $S_1$  and  $S_2$  are in closed conditions, respectively.



Circuit-1



Circuit-2

Which of the following statement(s) is(are) correct?

## Options A.

When a constant current source of 2 Amp is connected across A and B in both circuits,  $P_1 > P_2$ .

## B.

When a voltage source of 6 V is connected across A and B in both circuits,  $P_1 < P_2$ .

## C.

When a voltage source of 6 V is connected across A and B in Circuit-1,  $Q_1 > P_1$ .

## D.

When a constant current source of 2 Amp is connected across A and B in both circuits,  $Q_2 < Q_1$ .

Question Type : MSQ

Question ID : 859434352

Chosen Option : C,D

Q.5

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

A bubble has surface tension  $S$ . The ideal gas inside the bubble has ratio of specific heats  $\gamma = \frac{5}{3}$ . The bubble is exposed to the atmosphere and it always retains its spherical shape. When the atmospheric pressure is  $P_{a1}$ , the radius of the bubble is found to be  $r_1$  and the temperature of the enclosed gas is  $T_1$ . When the atmospheric pressure is  $P_{a2}$ , the radius of the bubble and the temperature of the enclosed gas are  $r_2$  and  $T_2$ , respectively.

Which of the following statement(s) is(are) correct?

**Options A.**

If the surface of the bubble is a perfect heat insulator, then the total internal energy of the bubble including its surface energy does not change with the external atmospheric pressure.

**B.**

$$\text{If the surface of the bubble is a perfect heat insulator, then } \left(\frac{T_2}{T_1}\right)^{\frac{5}{2}} = \frac{P_{a2} + \frac{4S}{r_2}}{P_{a1} + \frac{4S}{r_1}}.$$

**C.**

$$\text{If the surface of the bubble is a perfect heat insulator, then } \left(\frac{r_1}{r_2}\right)^5 = \frac{P_{a2} + \frac{2S}{r_2}}{P_{a1} + \frac{2S}{r_1}}.$$

**D.**

$$\text{If the surface of the bubble is a perfect heat conductor and the change in atmospheric temperature is negligible, then } \left(\frac{r_1}{r_2}\right)^3 = \frac{P_{a2} + \frac{4S}{r_2}}{P_{a1} + \frac{4S}{r_1}}.$$

Question Type : **MSQ**Question ID : **859434353**Chosen Option : **C**

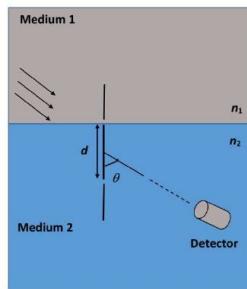
Q.6

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

**Full Marks** : +4 **ONLY** if (all) the correct option(s) is(are) chosen;  
**Partial Marks** : +3 If all the four options are correct but **ONLY** three options are chosen;  
**Partial Marks** : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;  
**Partial Marks** : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;  
**Zero Marks** : 0 If none of the options is chosen (i.e. the question is unanswered);  
**Negative Marks** : -2 In all other cases.

A double slit setup is shown in the figure. One of the slits is in medium 2 of refractive index  $n_2$ . The other slit is at the interface of this medium with another medium 1 of refractive index  $n_1$  ( $\neq n_2$ ). The line joining the slits is perpendicular to the interface and the distance between the slits is  $d$ . A monochromatic parallel beam of light is incident on the slits from medium 1. A detector is placed in medium 2 at a large distance from the slits, and at an angle  $\theta$  from the line joining them, so that  $\theta$  equals the angle of refraction of the beam. Consider two approximately parallel rays from the slits received by the detector.



Which of the following statement(s) is(are) correct?

**Options A.**

The phase difference between the two rays is independent of  $d$ .

**B.**

The phase difference between the two rays vanishes only for certain values of  $d$  and the angle of incidence of the beam, with  $\theta$  being the corresponding angle of refraction.

**C.**

The two rays interfere constructively at the detector.

**D.**

The phase difference between the two rays depends on  $n_1$  but is independent of  $n_2$ .

Question Type : **MSQ**

Question ID : **859434355**

Chosen Option : --

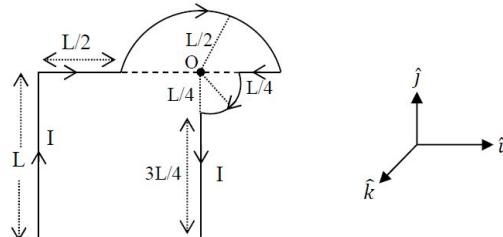
Section : Phy Sec 3

Q.1

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
  - Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
  - For each question, choose the option corresponding to the correct answer.
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +3 If ONLY the correct option is chosen;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -1 In all other cases.*

Which one of the following options represents the magnetic field  $\vec{B}$  at O due to the current flowing in the given wire segments lying on the  $xy$  plane?

**Options**

- A  $\vec{B} = -\frac{\mu_0 I}{L} \left( 1 + \frac{1}{4\sqrt{2}\pi} \right) \hat{k}$
- B  $\vec{B} = -\frac{\mu_0 I}{L} \left( \frac{3}{2} + \frac{1}{2\sqrt{2}\pi} \right) \hat{k}$
- C  $\vec{B} = \frac{-\mu_0 I}{L} \left( 1 + \frac{1}{4\pi} \right) \hat{k}$
- D  $\vec{B} = \frac{-\mu_0 I}{L} \left( \frac{3}{2} + \frac{1}{4\sqrt{2}\pi} \right) \hat{k}$

Question Type : MCQ

Question ID : 859434360

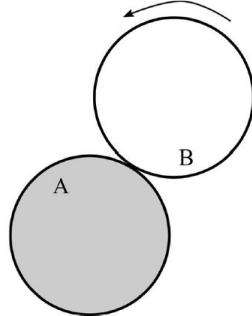
Chosen Option : C

Q.2

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

A flat surface of a thin uniform disk *A* of radius *R* is glued to a horizontal table. Another thin uniform disk *B* of mass *M* and with the same radius *R* rolls without slipping on the circumference of *A*, as shown in the figure. A flat surface of *B* also lies on the plane of the table. The center of mass of *B* has fixed angular speed  $\omega$  about the vertical axis passing through the center of *A*. The angular momentum of *B* is  $nM\omega R^2$  with respect to the center of *A*. Which of the following is the value of *n*?



- Options**
- A. 5
  - B.  $\frac{9}{2}$
  - C.  $\frac{7}{2}$
  - D. 2

Question Type : MCQ

Question ID : 859434357

Chosen Option : A

Q.3

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

When light of a given wavelength is incident on a metallic surface, the minimum potential needed to stop the emitted photoelectrons is 6.0 V. This potential drops to 0.6 V if another source with wavelength four times that of the first one and intensity half of the first one is used. What are the wavelength of the first source and the work function of the metal, respectively? [Take  $\frac{hc}{e} = 1.24 \times 10^{-6} \text{ J m C}^{-1}$ .]

- Options**
- A.  $3.78 \times 10^{-7} \text{ m}$ , 1.20 eV
  - B.  $1.72 \times 10^{-7} \text{ m}$ , 1.20 eV
  - C.  $1.72 \times 10^{-7} \text{ m}$ , 5.60 eV
  - D.  $3.78 \times 10^{-7} \text{ m}$ , 5.60 eV

Question Type : MCQ

Question ID : 859434358

Chosen Option : B

Q.4

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

Area of the cross-section of a wire is measured using a screw gauge. The pitch of the main scale is 0.5 mm. The circular scale has 100 divisions and for one full rotation of the circular scale, the main scale shifts by two divisions. The measured readings are listed below.

<b>Measurement condition</b>	<b>Main scale reading</b>	<b>Circular scale reading</b>
Two arms of gauge touching each other without wire	0 division	4 divisions
Attempt-1: With wire	4 divisions	20 divisions
Attempt-2: With wire	4 divisions	16 divisions

What are the diameter and cross-sectional area of the wire measured using the screw gauge?

**Options**

- $2.22 \pm 0.02 \text{ mm}$ ,  $\pi(1.23 \pm 0.02)\text{mm}^2$
- $2.22 \pm 0.01 \text{ mm}$ ,  $\pi(1.23 \pm 0.01)\text{mm}^2$
- $2.14 \pm 0.01 \text{ mm}$ ,  $\pi(1.14 \pm 0.01)\text{mm}^2$
- $2.14 \pm 0.02 \text{ mm}$ ,  $\pi(1.14 \pm 0.02)\text{mm}^2$

Question Type : **MCQ**Question ID : **859434359**Chosen Option : **C**

Section : Chem Sec 1

Q.1

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Thermal decomposition of  $\text{AgNO}_3$  produces two paramagnetic gases. The total number of electrons present in the antibonding molecular orbitals of the gas that has the higher number of unpaired electrons is \_\_\_\_\_.

Given **6**

Answer :

Question Type : **SDI**Question ID : **859434365**

Q.2

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

An aqueous solution is prepared by dissolving 0.1 mol of an ionic salt in 1.8 kg of water at 35 °C. The salt remains 90% dissociated in the solution. The vapour pressure of the solution is 59.724 mm of Hg. Vapor pressure of water at 35 °C is 60.000 mm of Hg. The number of ions present per formula unit of the ionic salt is \_\_\_\_\_.

Given 5

Answer :

Question Type : SDI

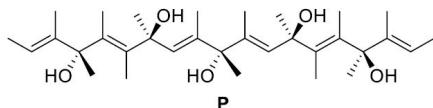
Question ID : 859434362

Q.3

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The total number of chiral molecules formed from one molecule of P on complete ozonolysis ( $O_3$ ,  $Zn/H_2O$ ) is \_\_\_\_\_.



Given 2

Answer :

Question Type : SDI

Question ID : 859434368

Q.4

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

Concentration of  $H_2SO_4$  and  $Na_2SO_4$  in a solution is 1 M and  $1.8 \times 10^{-2}$  M, respectively. Molar solubility of  $PbSO_4$  in the same solution is  $X \times 10^{-Y}$  M (expressed in scientific notation). The value of Y is \_\_\_\_\_.

[Given: Solubility product of  $PbSO_4$  ( $K_{sp}$ ) =  $1.6 \times 10^{-8}$ . For  $H_2SO_4$ ,  $K_{a1}$  is very large and  $K_{a2} = 1.2 \times 10^{-2}$ ]

Given 7

Answer :

Question Type : SDI

Question ID : 859434361

**Q.5****SECTION 1 (Maximum marks: 24)**

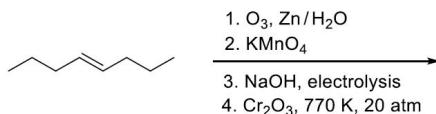
- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The reaction of Xe and O<sub>2</sub>F<sub>2</sub> gives a Xe compound P. The number of moles of HF produced by the complete hydrolysis of 1 mol of P is \_\_\_\_\_.

**Given 6****Answer :****Question Type : SDI****Question ID : 859434364****Q.6****SECTION 1 (Maximum marks: 24)**

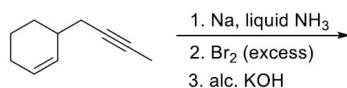
- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The number of -CH<sub>2</sub>- (methylene) groups in the product formed from the following reaction sequence is \_\_\_\_\_.

**Given --****Answer :****Question Type : SDI****Question ID : 859434367****Q.7****SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
- The answer to each question is a **SINGLE DIGIT INTEGER** ranging from **0 TO 9, BOTH INCLUSIVE**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct integer is entered;  
 Zero Marks : 0 If the question is unanswered;  
 Negative Marks : -1 In all other cases.

The number of isomeric tetraenes (NOT containing sp-hybridized carbon atoms) that can be formed from the following reaction sequence is \_\_\_\_\_.

**Given 2****Answer :****Question Type : SDI****Question ID : 859434366**

Q.8

**SECTION 1 (Maximum marks: 24)**

- This section contains **EIGHT (08)** questions.
  - The answer to each question is a **SINGLE DIGIT INTEGER ranging from 0 TO 9, BOTH INCLUSIVE**.
  - For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +3 If ONLY the correct integer is entered;*  
*Zero Marks : 0 If the question is unanswered;*  
*Negative Marks : -1 In all other cases.*

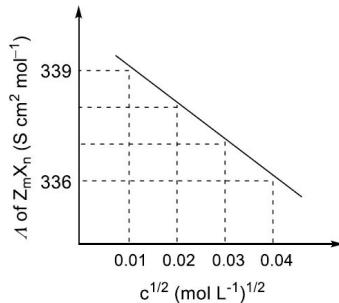
Consider the strong electrolytes  $Z_mX_n$ ,  $U_mY_p$  and  $V_mX_n$ . Limiting molar conductivity ( $\Lambda^0$ ) of  $U_mY_p$  and  $V_mX_n$  are 250 and 440  $S\ cm^2\ mol^{-1}$ , respectively. The value of  $(m + n + p)$  is \_\_\_\_\_.

Given:

Ion	$Z^{n+}$	$U^{p+}$	$V^{n+}$	$X^{m-}$	$Y^{m-}$
$\lambda^0\ (S\ cm^2\ mol^{-1})$	50.0	25.0	100.0	80.0	100.0

$\lambda^0$  is the limiting molar conductivity of ions

The plot of molar conductivity ( $\Lambda$ ) of  $Z_mX_n$  vs  $c^{1/2}$  is given below.



Given 7

Answer :

Question Type : **SDI**

Question ID : **859434363**

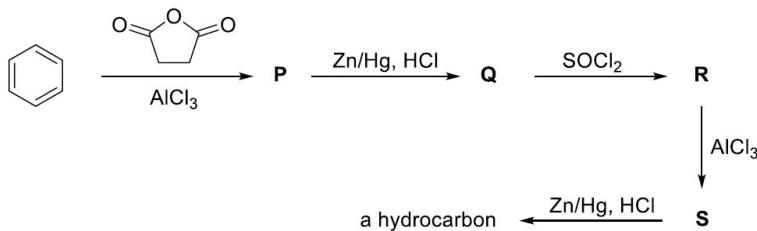
Section : Chem Sec 2

Q.1

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
  - Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
  - For each question, choose the option(s) corresponding to (all) the correct answer(s).
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Considering the following reaction sequence, the correct statement(s) is(are)



**Options A.**

Compounds **P** and **S** react with hydroxylamine to give the corresponding oximes.

**B.**

**Compound S decolorizes bromine water.**

**C.**

Compound **R** reacts with dialkylcadmium to give the corresponding tertiary alcohol.

**D.**

**Compounds P and Q are carboxylic acids.**

Question Type : **MSQ**

Question ID : **859434373**

Chosen Option : **A,D**

Q.2

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

The correct option(s) related to the extraction of iron from its ore in the blast furnace operating in the temperature range 900 – 1500 K is(are)

**Options A.**

**A.** Limestone is used to remove silicate impurity.

**B.** Pig iron obtained from blast furnace contains about 4% carbon.

**C.** Coke (C) converts  $\text{CO}_2$  to CO.

**D.**

Exhaust gases consist of  $\text{NO}_2$  and CO.

Question Type : MSQ

Question ID : 859434372

Chosen Option : --

Q.3

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

Among the following, the correct statement(s) about polymers is(are)

**Options A.**

**A.** The polymerization of chloroprene gives natural rubber.

**B.** Teflon is prepared from tetrafluoroethene by heating it with persulphate catalyst at high pressures.

**C.** PVC are thermoplastic polymers.

**D.**

Ethene at 350-570 K temperature and 1000-2000 atm pressure in the presence of a peroxide initiator yields high density polythene.

Question Type : MSQ

Question ID : 859434374

Chosen Option : --

Q.4

**SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

To check the principle of multiple proportions, a series of pure binary compounds ( $P_m Q_n$ ) were analyzed and their composition is tabulated below. The correct option(s) is(are)

Compound	Weight % of P	Weight % of Q
<b>1</b>	50	50
<b>2</b>	44.4	55.6
<b>3</b>	40	60

**Options A.**

If atomic weight of P and Q are 70 and 35, respectively, then the empirical formula of compound **1** is  $P_2Q$ .

B.

If empirical formula of compound **2** is  $PQ$ , then the empirical formula of the compound **1** is  $P_5Q_4$ .

C.

If empirical formula of compound **3** is  $P_3Q_4$ , then the empirical formula of compound **2** is  $P_3Q_5$ .

D.

If empirical formula of compound **3** is  $P_3Q_2$  and atomic weight of element P is 20, then the atomic weight of Q is 45.

Question Type : **MSQ**Question ID : **859434369**Chosen Option : **B,D**

**Q.5****SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

The correct option(s) about entropy (S) is(are)

[R = gas constant, F = Faraday constant, T = Temperature]

**Options A.**

A.  $\Delta S > 0$ , for  $[\text{Ni}(\text{H}_2\text{O})_6]^{2+} + 3 \text{ en} \rightarrow [\text{Ni}(\text{en})_3]^{2+} + 6\text{H}_2\text{O}$  (where en = ethylenediamine).

B.

The cell reaction, Pt(s) | H<sub>2</sub>(g, 1bar) | H<sup>+</sup>(aq, 0.01M) || H<sup>+</sup>(aq, 0.1M) | H<sub>2</sub>(g, 1bar) | Pt(s), is an entropy driven process.

C.

For the reaction, M(s) + 2H<sup>+</sup>(aq) → H<sub>2</sub>(g) + M<sup>2+</sup>(aq), if  $\frac{dE}{dt} = -\frac{R}{F}$ , then the entropy change of the reaction is R (assume that entropy and internal energy changes are temperature independent).

D.

For racemization of an optically active compound,  $\Delta S > 0$ .

+2

Question Type : **MSQ**

Question ID : **859434370**

Chosen Option : **A,B**

**Q.6****SECTION 2 (Maximum Marks: 24)**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options. **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks : +4 ONLY if (all) the correct option(s) is(are) chosen;*  
*Partial Marks : +3 If all the four options are correct but ONLY three options are chosen;*  
*Partial Marks : +2 If three or more options are correct but ONLY two options are chosen, both of which are correct;*  
*Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -2 In all other cases.*

The compound(s) which react(s) with NH<sub>3</sub> to give boron nitride (BN) is(are)

**Options**

A. B

+2

B. B<sub>2</sub>H<sub>6</sub>

C. B<sub>2</sub>O<sub>3</sub>

D. HBF<sub>4</sub>

Question Type : **MSQ**

Question ID : **859434371**

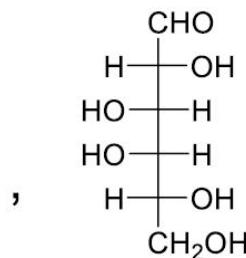
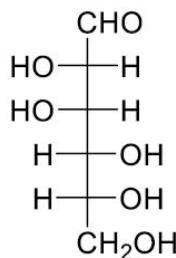
Chosen Option : **A,B**

Q.1

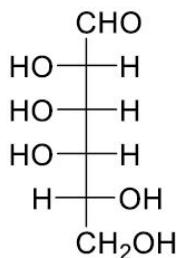
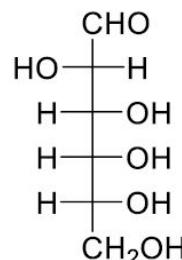
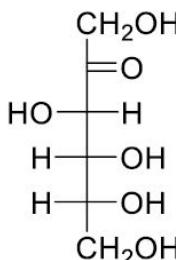
**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
  - Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
  - For each question, choose the option corresponding to the correct answer.
  - Answer to each question will be evaluated according to the following marking scheme:
- Full Marks** : +3 If **ONLY** the correct option is chosen;  
**Zero Marks** : 0 If none of the options is chosen (i.e. the question is unanswered);  
**Negative Marks** : -1 In all other cases.

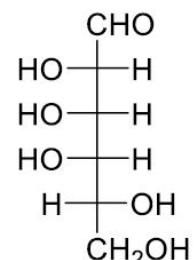
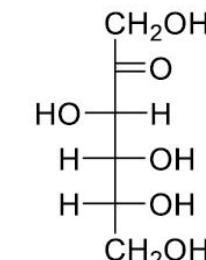
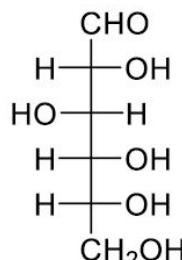
Treatment of D-glucose with aqueous NaOH results in a mixture of monosaccharides, which are

**Options A.**

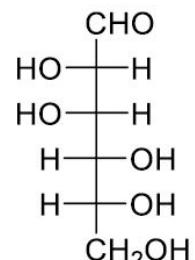
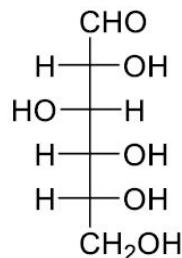
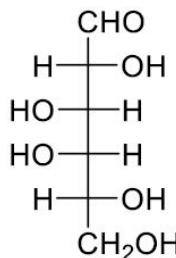
and

**B.**

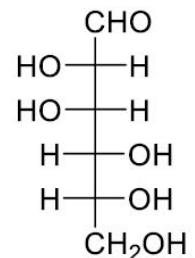
and

**C.**

and

**D.**

and

Question Type : **MCQ**Question ID : **859434378**Chosen Option : **C**

Q.2

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

The reaction of  $\text{Pb}(\text{NO}_3)_2$  and  $\text{NaCl}$  in water produces a precipitate that dissolves upon the addition of  $\text{HCl}$  of appropriate concentration. The dissolution of the precipitate is due to the formation of

**Options**

- A.  $[\text{PbCl}_4]^{2-}$
- B.  $[\text{PbCl}_6]^{2-}$
- C.  $\text{PbCl}_2$
- D.  $\text{PbCl}_4$

Question Type : MCQ

Question ID : 859434377

Chosen Option : A

Q.3

**SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
 Full Marks : +3 If **ONLY** the correct option is chosen;  
 Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);  
 Negative Marks : -1 In all other cases.

The reaction of  $\text{HClO}_3$  with  $\text{HCl}$  gives a paramagnetic gas, which upon reaction with  $\text{O}_3$  produces

**Options**

- A.  $\text{Cl}_2\text{O}_6$
- B.  $\text{ClO}_2$
- C.  $\text{Cl}_2\text{O}$
- D.  $\text{Cl}_2\text{O}_7$

Question Type : MCQ

Question ID : 859434376

Chosen Option : D

**Q.4****SECTION 3 (Maximum marks: 12)**

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options. **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  
*Full Marks : +3 If ONLY the correct option is chosen;*  
*Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);*  
*Negative Marks : -1 In all other cases.*

Atom X occupies the fcc lattice sites as well as alternate tetrahedral voids of the same lattice. The packing efficiency (in %) of the resultant solid is closest to

**Options**

- A. 25
- B. 75
- C. 35
- D. 55

**Question Type : MCQ****Question ID : 859434375****Chosen Option : B**